# Homework 3

Due: Monday, April 19, at 11:00 PM Seattle time on Gradescope

## 1 Complex Diagonalization

Diagonalize each of the following matrices

A. 
$$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$$

B. 
$$\begin{pmatrix} 3 & -2 \\ 2 & 3 \end{pmatrix}$$

C. 
$$\begin{pmatrix} 7 & -5 \\ 13 & -9 \end{pmatrix}$$

## 2 Complex General Solutions

For each of the following ODEs, find the (complex) general solution.

A. 
$$x' = \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} x$$

B. 
$$x' = \begin{pmatrix} 3 & -2 \\ 2 & 3 \end{pmatrix} x$$

$$C. \ x' = \begin{pmatrix} 7 & -5 \\ 13 & -9 \end{pmatrix} x$$

### 3 Real General Solutions

For each of the following ODEs, find the real general solution.

A. 
$$x' = \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} x$$

B. 
$$x' = \begin{pmatrix} 3 & -2 \\ 2 & 3 \end{pmatrix} x$$

$$C. \ x' = \begin{pmatrix} 7 & -5 \\ 13 & -9 \end{pmatrix} x$$

### 4 Initial Value Problems

Find the solution to each of the following IVPs

A. 
$$x' = \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} x$$
,  $x(0) = (1, 2)$ 

B. 
$$x' = \begin{pmatrix} 3 & -2 \\ 2 & 3 \end{pmatrix} x$$
,  $x(0) = (1, -1)$ 

C. 
$$x' = \begin{pmatrix} 7 & -5 \\ 13 & -9 \end{pmatrix} x$$
,  $x(0) = (3,4)$ 

#### 5 Limiting Behavior

For each of the following IVPs, compute the limit  $\lim_{t\to\infty} |x(t)|$ , for the solution x.

A. 
$$x' = \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} x$$
,  $x(0) = (1, 2)$ 

B. 
$$x' = \begin{pmatrix} 3 & -2 \\ 2 & 3 \end{pmatrix} x$$
,  $x(0) = (1, -1)$ 

C. 
$$x' = \begin{pmatrix} 7 & -5 \\ 13 & -9 \end{pmatrix} x$$
,  $x(0) = (3,4)$ 

#### 6 Direction Fields

Draw the direction field (approximately) for each of the following ODEs

A. 
$$x' = \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} x$$

B. 
$$x' = \begin{pmatrix} 3 & -2 \\ 2 & 3 \end{pmatrix} x$$

$$C. \ x' = \begin{pmatrix} 7 & -5 \\ 13 & -9 \end{pmatrix} x$$