# Fluid Simulation

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### **Navier-Stokes equations for incompressible flow**

$$\frac{\partial \vec{u}}{\partial t} + \vec{u} \cdot \nabla \vec{u} + \frac{1}{\rho} \nabla p = \vec{g} + \nu \nabla \cdot \nabla \vec{u}, \qquad (1.1)$$

$$\nabla \cdot \vec{u} = 0. \qquad (1.2)$$



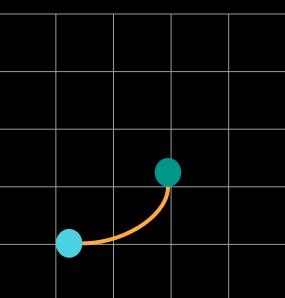
### **Algorithm**

- Advection of Fluid
- Diffusion
- Pressure Solve
- Advection of Diffusion of others
- Boundary set



#### Advection

- Describes how the fluid move things (itself included)
- Given some quantity Q on our simulation grid, how will Q change  $\Delta t$  later?
- $q(x, t+\Delta t) = q(integrate(x, velocity(x, t), \Delta t), t)$
- integrate(x, velocity(x, t), dt):
  - Euler
  - o RK2
  - o RK4



#### **Pressure solve**

- Poisson Equation
- Solve analytically
  - Jacobi
  - Gauss-Seidel

$$w = u + \nabla p$$

$$\nabla .w = \nabla .(u + \nabla p)$$

$$\nabla .w = \nabla .u + \nabla^2 p; \ \nabla .u = 0 (2)$$

$$\nabla^2 p = \nabla .w$$



#### **Diffusion**

- Viscosity: how resistance is the fluid to change
- Viscosity solve using poisson equation as well
- Can be discarded reduced to Euler Equation

#### **Boundary**

- No-slip (zero) velocity boundary condition
- Pure Neumann pressure boundary condition
- To satisfy the conditions, the boundary values should be:
  - o Pressure: same value as the neighboring cell
  - Velocity: the negative of the neighboring cell value

#### **Technical details**

- Made using
  - OpenGL for display
  - imgui for UI
  - o Fluid solve available in CUDA and CPU
- Performance difference is too great



## Results



#### References



- Braley, Colin and Adrian Sandu. Fluid Simulation For Computer Graphics: A Tutorial in Grid Based and Particle Based Methods, 2009.
- Bridson, Robert. Fluid Simulation for Computer Graphics. CRC Press, 2016.
- Harris, Mark. "Chapter 38. Fast Fluid Dynamics Simulation on the GPU." GPU Gems.
   Nvidia,
  - https://developer.nvidia.com/gpugems/gpugems/part-vi-beyond-triangles/chapter-38-fast-fluid-dynamics-simulation-gpu
- KAUST's GPU and Scientific Visualization slides :D



# Thank you!