

bitmask DP

```
for (int mask = 0; mask < (1 << n); mask++) {
    for (int submask = mask; submask != 0; submask = (submask - 1) & mask) {
        int subset = mask ^ submask;
        // do whatever you need to do here
    }
}
```

The goal of this problem is to partition the elements into sets such that (any condition we will dp on it).

```
#define ON(n, k)      ((n) | (1 << (k)))      // Set k-th bit ON
#define OFF(n, k)     ((n) & ~(1 << (k)))     // Set k-th bit OFF
#define isON(n, k)    (((n) >> (k)) & 1)      // Check if k-th bit is ON
#define isPow2(n)     (!(n & (n - 1)))        // Check if number is power of two

int addJthBit(int x, int bit) {
    return x | (1 << bit);                    // Turn bit ON
}

int removeJthBit(int x, int bit) {
    return x & ~(1 << bit);                   // Turn bit OFF
}

bool checkBit(int x, int bit) {
    return (x >> bit) & 1;                    // Return true if bit is set
}

int toggleBit(int x, int bit) {
    return x ^ (1 << bit);                    // Toggle bit
}

int allBitsOne(int numberOfBits) {
    return (1 << numberOfBits) - 1;           // Return mask of all 1s
}

bool checkPowerOfTwo(int x) {
    return !(x & (x - 1));                    // Another way to check power of 2
}

bool isDivisibleByPowerOf2(int n, int k) {
    int powerOf2 = 1 << k;
    return (n & (powerOf2 - 1)) == 0;
}

string toBinary(int x) {
    string res;
    while (x) {
        res += char((x % 2) + '0');
        x >>= 1;
    }
    while (res.size() < 4) res += '0';         // Pad to 4 bits if needed
    reverse(res.begin(), res.end());
    return res;
}

void go() {
    int n, x;
    cin >> n >> x;
    int a[n + 2];
    for (int i = 0; i < n; i++) cin >> a[i];

    int lim = (1 << n);
    for (int msk = 0; msk < lim; msk++) {
        int sum = 0;
        cout << "Current Mask = " << msk << '\n';
        cout << toBinary(msk) << '\n';
    }
}
```

```
for (int elm = 0; elm < n; elm++) {
    cout << "Current element index = " << elm
        << " status = " << checkBit(msk, elm) << '\n';
    if (checkBit(msk, elm))
        sum += a[elm];
}
cout << "Sum of the current Mask = " << sum << '\n';
if (sum == x) {
    cout << "Found\nMask = " << msk << '\n';
    return;
}
}
cout << "Not Found\n";
}
```

bitset [Cheat Sheet in C++](#)

```
#include <bitset>

// Initialization Examples
bitset<8> b;           // 8 bits, all initialized to 0
bitset<8> b("10101010"); // from binary string (rightmost is LSB)
bitset<8> b(42);       // from integer value
```

Basic Operations

| Operation | Description | Example |
|-------------|-------------------------------|--------------|
| b.set() | Set all bits to 1 | b.set(); |
| b.set(i) | Set bit at position i to 1 | b.set(2); |
| b.set(i, v) | Set bit i to value v (0 or 1) | b.set(2, 0); |
| b.reset() | Set all bits to 0 | b.reset(); |
| b.reset(i) | Set bit at position i to 0 | b.reset(2); |
| b.flip() | Flip all bits | b.flip(); |
| b.flip(i) | Flip bit at position i | b.flip(2); |

Query & Utility Operations

| Operation | Description | Example |
|---------------|---------------------------------------|----------------|
| b.test(i) | Check if bit i is set (bool) | b.test(3) |
| b[i] | Access bit at position i (read/write) | b[2] = 1; |
| b.count() | Count of bits set to 1 | b.count(); |
| b.size() | Total number of bits | b.size(); |
| b.any() | True if any bit is 1 | b.any(); |
| b.none() | True if all bits are 0 | b.none(); |
| b.all() | True if all bits are 1 | b.all(); |
| b.to_ulong() | Convert to unsigned long | b.to_ulong(); |
| b.to_ullong() | Convert to unsigned long long | b.to_ullong(); |
| b.to_string() | Convert to string of 0s and 1s | b.to_string(); |