

* Graph exercise:

Given $\zeta = 0.5$, $\omega_n = 1$, compute t_s , t_p , M_p ?

- $\sigma = \zeta \cdot \omega_n = 0.5 \times 1 = 0.5$

- $t_s = \frac{4}{\sigma} = \frac{4}{0.5} = 8 \text{ (s)}$

- $\omega_d = \omega_n \sqrt{1 - \zeta^2} = 1 \cdot \sqrt{1 - 0.5^2} \approx 0.866$

- $t_p = \frac{\pi}{\omega_d} = \frac{\pi}{0.866} \approx \text{~~3.627~~ 3.627}$

- $M_p = \exp(-\zeta\pi / \sqrt{1 - \zeta^2}) = \exp(-0.5\pi / \sqrt{1 - 0.5^2})$
 ≈ 0.163

Step Response of Second-Order System with $\omega_n = 1$, $\zeta = 0.5$

