

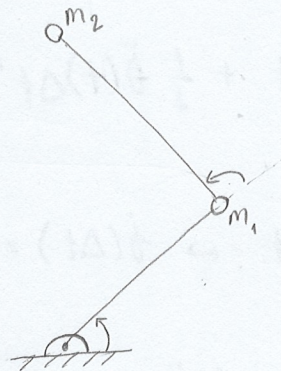
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Mass parameters:

$$m_1 = 10 \text{ kg}$$

$$m_2 = 5 \text{ kg}$$

$$l_1 = l_2 = 0,5 \text{ m}$$



$$\theta_1(0) = 30^\circ ; \dot{\theta}_1(0) = 0 ; \theta_2(0) = 150^\circ ; \dot{\theta}_2(0) = 0 ; t_f = 1 \text{ sec}$$

When $\tau_1 = 10 \sin(0,5\pi t)$
 $\tau_2 = 10 \sin(0,5\pi t)$ is applied

Find the trajectories of each point $\theta_1(t), \theta_2(t)$ $0 \leq t \leq 1$.

Solve:

We have: $\theta(0) = \begin{bmatrix} \theta_1(0) \\ \theta_2(0) \end{bmatrix} = \begin{bmatrix} 30^\circ \\ 150^\circ \end{bmatrix} ; \dot{\theta}(0) = \begin{bmatrix} \dot{\theta}_1(0) \\ \dot{\theta}_2(0) \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$

Acceleration at $t=0$ can be calculated by:

$$\ddot{\theta}(0) = M^{-1} [\tau - V - G]$$

$$M = \begin{bmatrix} l_1^2 m_2 + 2l_1 l_2 m_2 c_2 + l_1^2 (m_1 + m_2) & l_1^2 m_2 + l_1 l_2 m_2 c_2 \\ l_1^2 m_2 + l_1 l_2 m_2 c_2 & l_2^2 m_2 \end{bmatrix} = \begin{bmatrix} 2,8340 & 0,1675 \\ 0,1675 & 1,25 \end{bmatrix}$$

$$\rightarrow M^{-1} = \begin{bmatrix} 0,3556 & -0,0476 \\ -0,0476 & 0,8064 \end{bmatrix}$$

$$\tau(0) = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

$$V = \begin{bmatrix} -m_2 l_1 l_2 s_2 \dot{\theta}_1^2 - 2m_2 l_1 l_2 s_2 \dot{\theta}_1 \dot{\theta}_2 \\ m_2 l_1 l_2 s_2 \dot{\theta}_1^2 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

$$G = \begin{bmatrix} m_2 l_2 g c_{12} + (m_1 + m_2) l_1 g c_1 \\ m_2 l_1 g c_{12} \end{bmatrix} = \begin{bmatrix} 39,1928 \\ -24,525 \end{bmatrix}$$

$$\Rightarrow \ddot{\theta}(0) = \begin{bmatrix} -15,1035 \\ 21,6435 \end{bmatrix}$$