

CSCI 232:

Data Structures and Algorithms

Binary Search Trees (BST) Part 2

Reese Pearsall
Spring 2024

Announcements

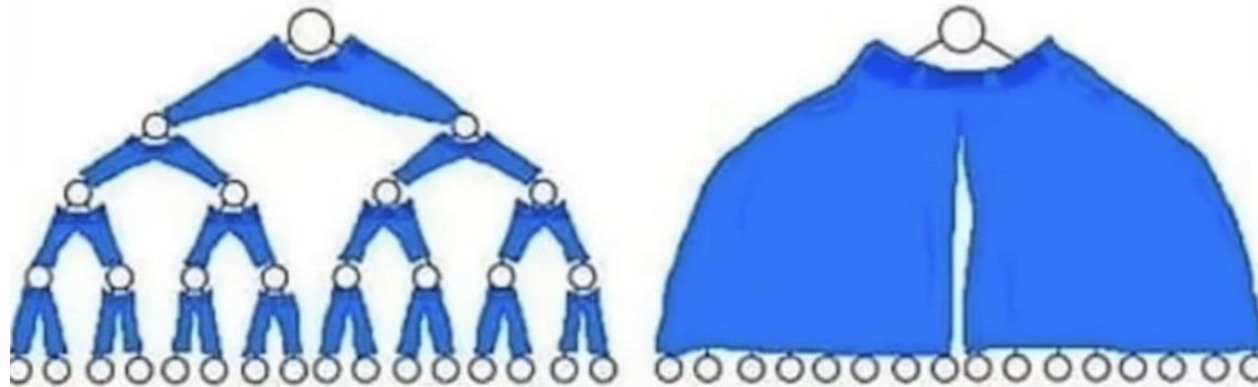
Program 1 posted, due Feb 27

**If a binary tree wore pants
would he wear them...**

like this

or

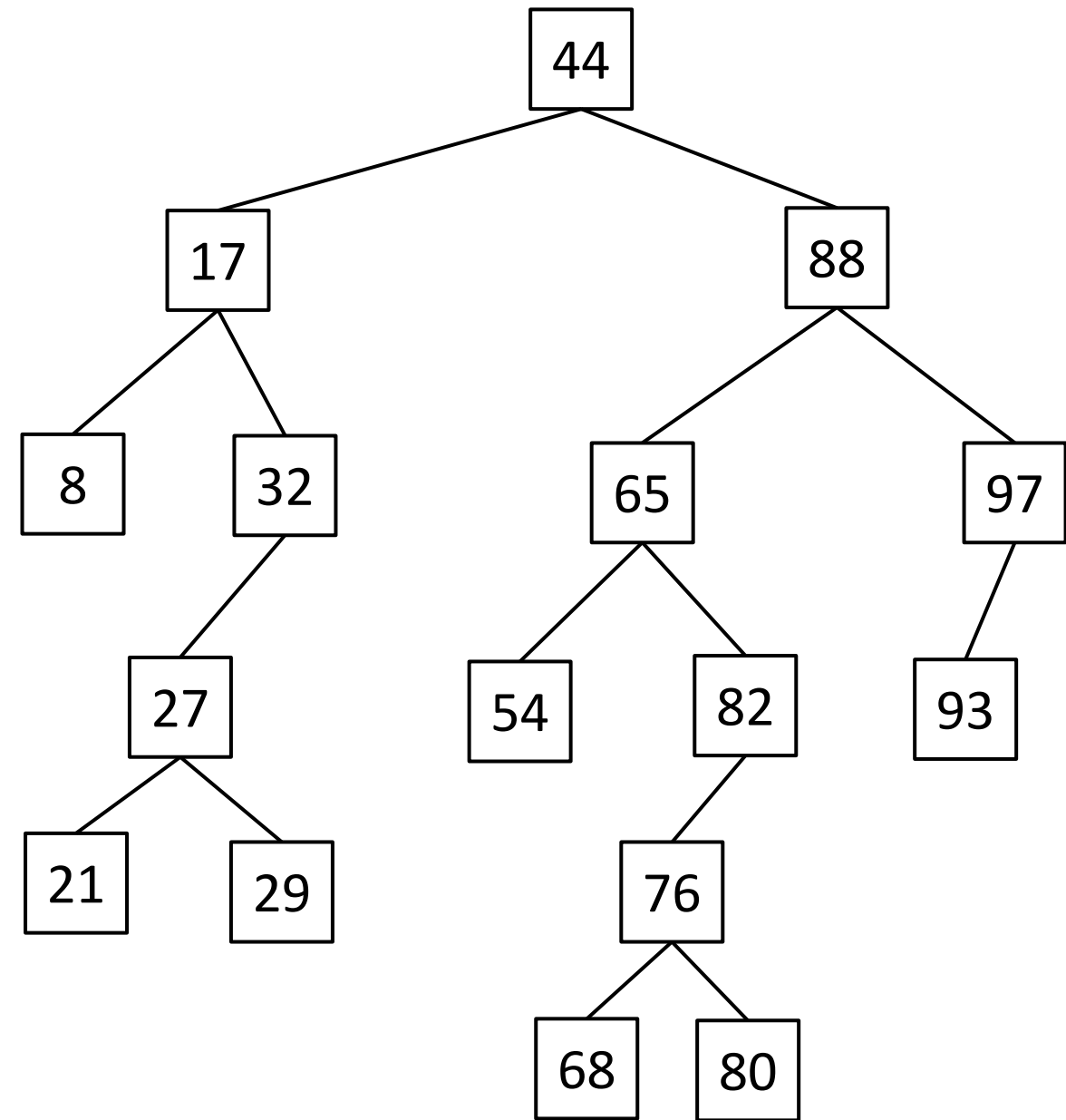
like this?



Binary Search Tree

Properties of a BST:

- Composed of **Comparable** data elements
- Each node as at most two children
- For a given node, all left-hand descendants have values that are less than the node
- For a given node, all right-hand descendants have values that are greater than the node
- No duplicate values



Binary Search Tree - Insertion

```
public void insert(int newValue) {
    if(root == null) {
        root = new Node(newValue);
    }
    else {
        Node currentNode = root;
        boolean placed = false;
        while(!placed) {
            if(currentNode.getValue() == newValue) {
                placed = true;
                System.out.println("No duplicate values allowed");
            }
            else if(newValue < currentNode.getValue()) {
                if(currentNode.getLeft() == null) {
                    currentNode.setLeft(new Node(newValue));
                    currentNode.getLeft().setParent(currentNode);
                    placed = true;
                }
                else {
                    currentNode = currentNode.getLeft();
                }
            }
            else {
                if(currentNode.getRight() == null) {
                    currentNode.setRight(new Node(newValue));
                    currentNode.getRight().setParent(currentNode);
                    placed = true;
                }
                else {
                    currentNode = currentNode.getRight();
                }
            }
        }
    }
}
```

Binary Search Tree - Insertion

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                    placed = true;
                }
                else {
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                }
            }
            else {
                if(currentNode.getRight() == null) {
                    currentNode.setRight(new Node(newValue));
                    currentNode.getRight().setParent(currentNode);
                    placed = true;
                }
                else {
                    currentNode = currentNode.getRight();
                }
            }
        }
    }
}
```

We repeatedly move left or right until we find the correct spot for our new node

Binary Search Tree - Insertion

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public void insert(int newValue) {  
    if(root == null) {  
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                    placed = true;  
                }  
                else {  
                    currentNode = currentNode.getLeft();  
                }  
            }  
            else {  
                if(currentNode.getRight() == null) {  
                    currentNode.setRight(new Node(newValue));  
                    currentNode.getRight().setParent(currentNode);  
                    placed = true;  
                }  
                else {  
                    currentNode = currentNode.getRight();  
                }  
            }  
        }  
    }  
}
```

We repeatedly move left or right until we find the correct spot for our new node

Once we find the correct spot, we update some pointers

Binary Search Tree - Insertion

Running time?

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public void insert(int newValue) {
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        }
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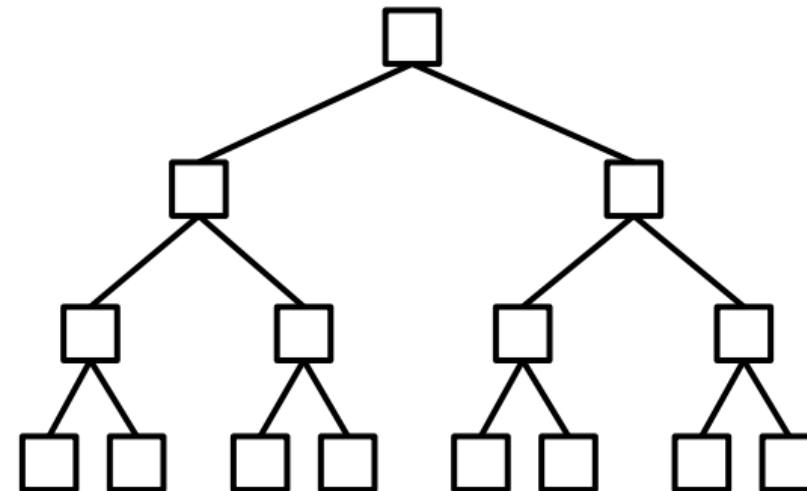
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                    currentNode = currentNode.getRight();
                }
            }
        }
    }
}
```

Running time?

We will always be inserting a leaf node, so worst cast scenario we will need to travel the **height** of the tree

If we have a “balanced tree” the height of the tree, is $\log(n)$ $n = \#$ of nodes



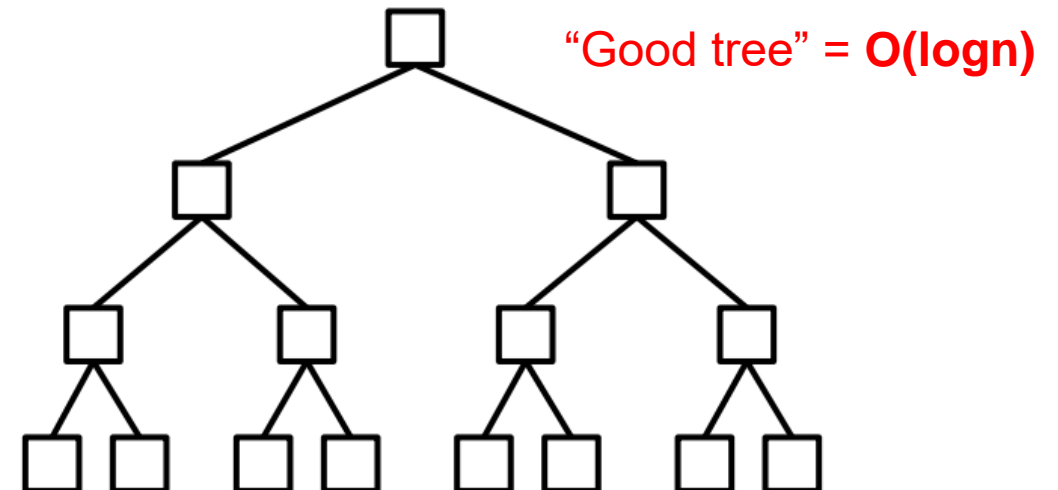
Binary Search Tree - Insertion

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                else {
                    currentNode = currentNode.getRight();
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            }
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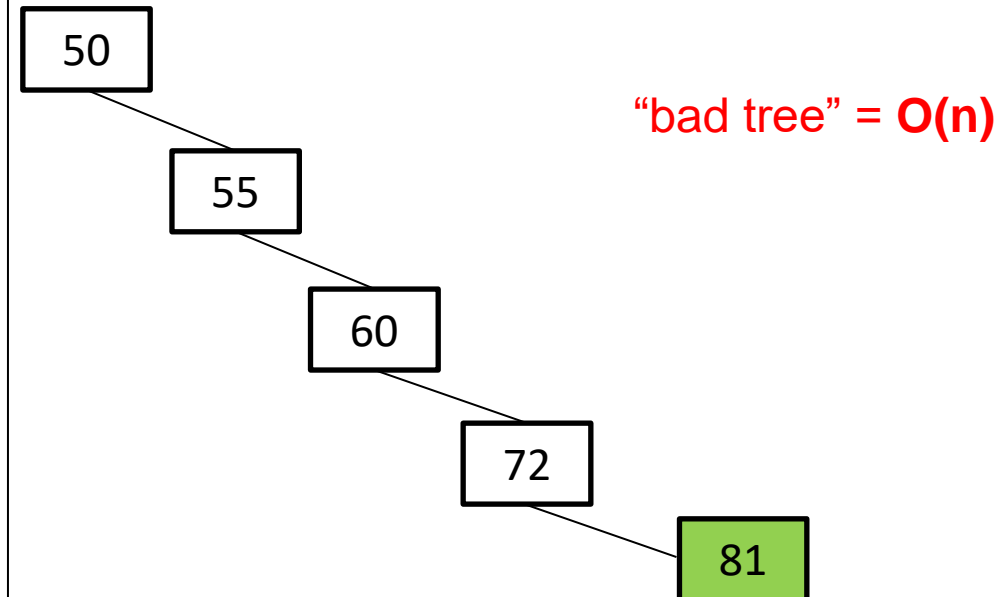
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                }
                else {
                    currentNode = currentNode.getLeft();
                }
            }
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                    currentNode.getRight().setParent(currentNode);
                    placed = true;
                }
                else {
                    currentNode = currentNode.getRight();
                }
            }
        }
    }
}
```

Running time?

We will always be inserting a leaf node, so worst cast scenario we will need to travel the **height** of the tree

If we have a “bad tree” the height of the tree, is $O(n-1)$ n = # of nodes



Binary Search Tree - Insertion

```
public void insert(int newValue) {
    if(root == null) {
        root = new Node(newValue);
    }
    else {
        Node currentNode = root;
        boolean placed = false;
        while(!placed) {
            if(currentNode.getValue() == newValue) {
                placed = true;
                System.out.println("No duplicate values allowed");
            }
            else if(newValue < currentNode.getValue()) {
                if(currentNode.getLeft() == null) {
                    currentNode.setLeft(new Node(newValue));
                    currentNode.getLeft().setParent(currentNode);
                    placed = true;
                }
                else {
                    currentNode = currentNode.getLeft();
                }
            }
            else {
                if(currentNode.getRight() == null) {
                    currentNode.setRight(new Node(newValue));
                    currentNode.getRight().setParent(currentNode);
                    placed = true;
                }
                else {
                    currentNode = currentNode.getRight();
                }
            }
        }
    }
}
```

Running time?

We will always be inserting a leaf node, so worst cast scenario we will need to travel the **height** of the tree

“Bad” tree $\rightarrow O(n)$
“Good” tree $\rightarrow O(\log n)$

$O(h) \rightarrow h = \text{height of tree}$

Running time for adding to an array?

$O(n)$



Binary Search Tree - Insertion

```
public void insert(int newValue) {
```

```
    if (root == null) {
```

```
        root = new Node(newValue);
```

```
    } else {
```

```
        boolean found = false;
```

```
        while (true) {
```

```
            if (newValue < root.val) {
```

```
                root = root.left;
```

```
            } else if (newValue > root.val) {
```

```
                root = root.right;
```

```
            } else {
```

```
                found = true;
```

```
            } if (found) break;
```

```
            root = new Node(newValue);
```

```
        }
```

```
    }
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}
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}
```

If we can find a way to keep a tree “balanced”, we can achieve **$O(\log n)$** insertion time, and **$O(\log n)$** searching time

Running time?

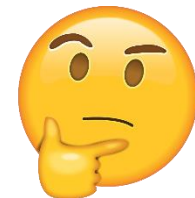
We will always be inserting a leaf node, so worst cast scenario we will need to travel the **height** of the tree

“Bad” tree $\rightarrow O(n)$
“Good” tree $\rightarrow O(\log n)$

$O(h) \rightarrow h = \text{height of tree}$

Running time for adding to an array?

$O(n)$



Binary Search Tree - Insertion

Running time?

We will always be inserting a leaf node, so worst cast scenario we will need to travel the **height** of the tree

“Bad” tree $\rightarrow O(n)$
“Good” tree $\rightarrow O(\log n)$

$O(h) \rightarrow h = \text{height of tree}$

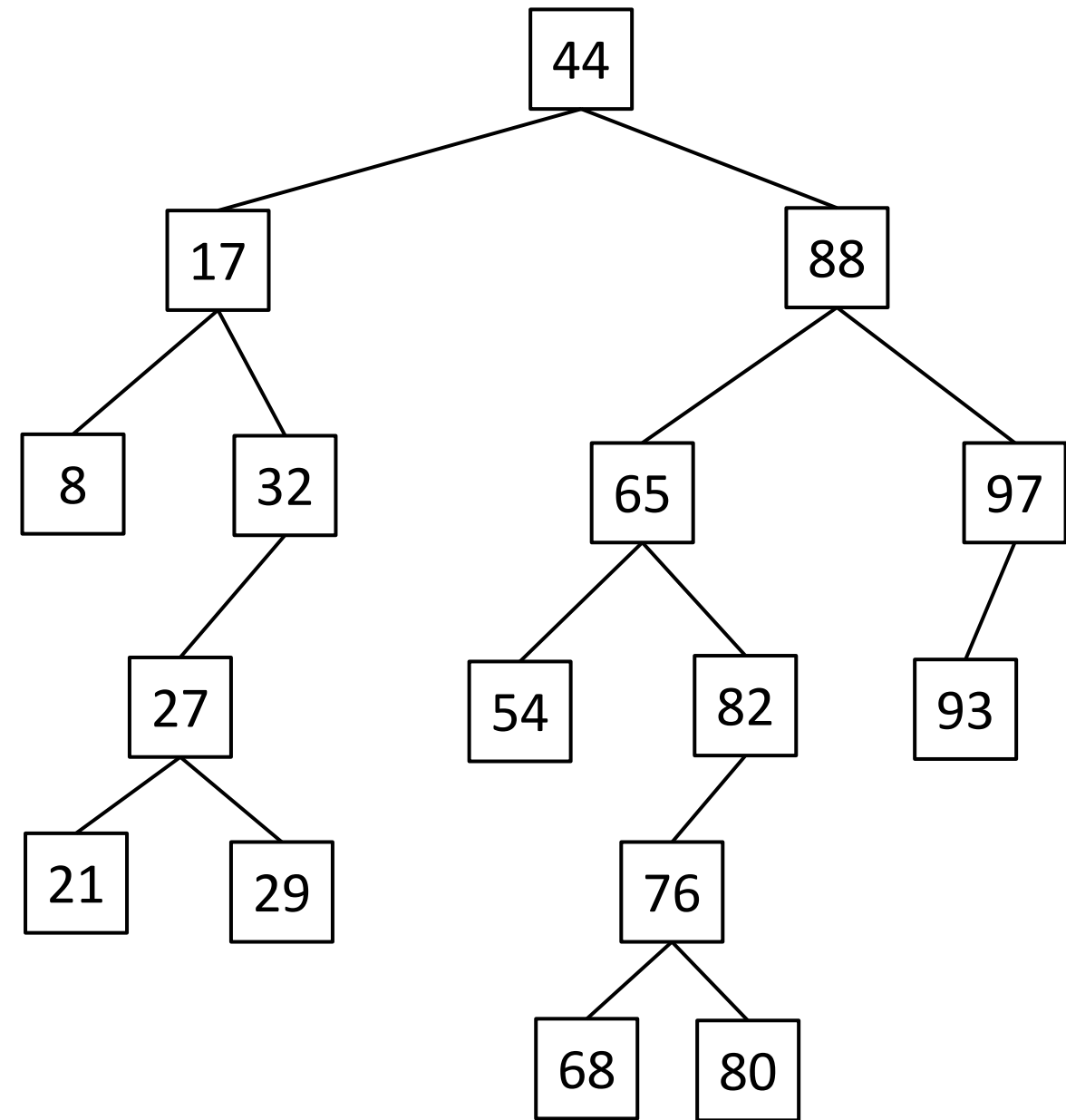
Running time for adding to an array?

$O(n)$



Binary Search Tree- Removal

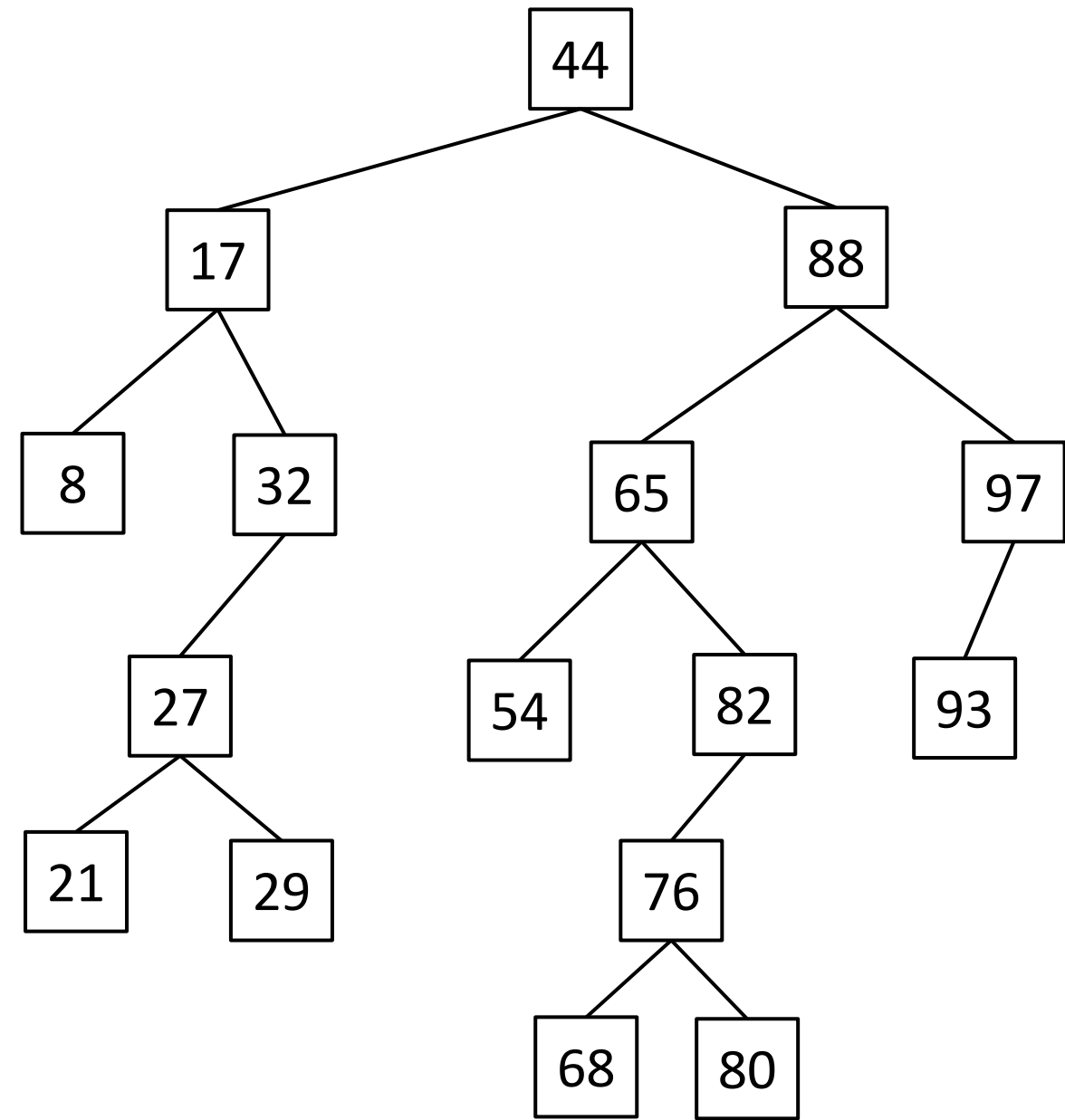
`remove(68);`



Binary Search Tree- Removal

`remove(68);`

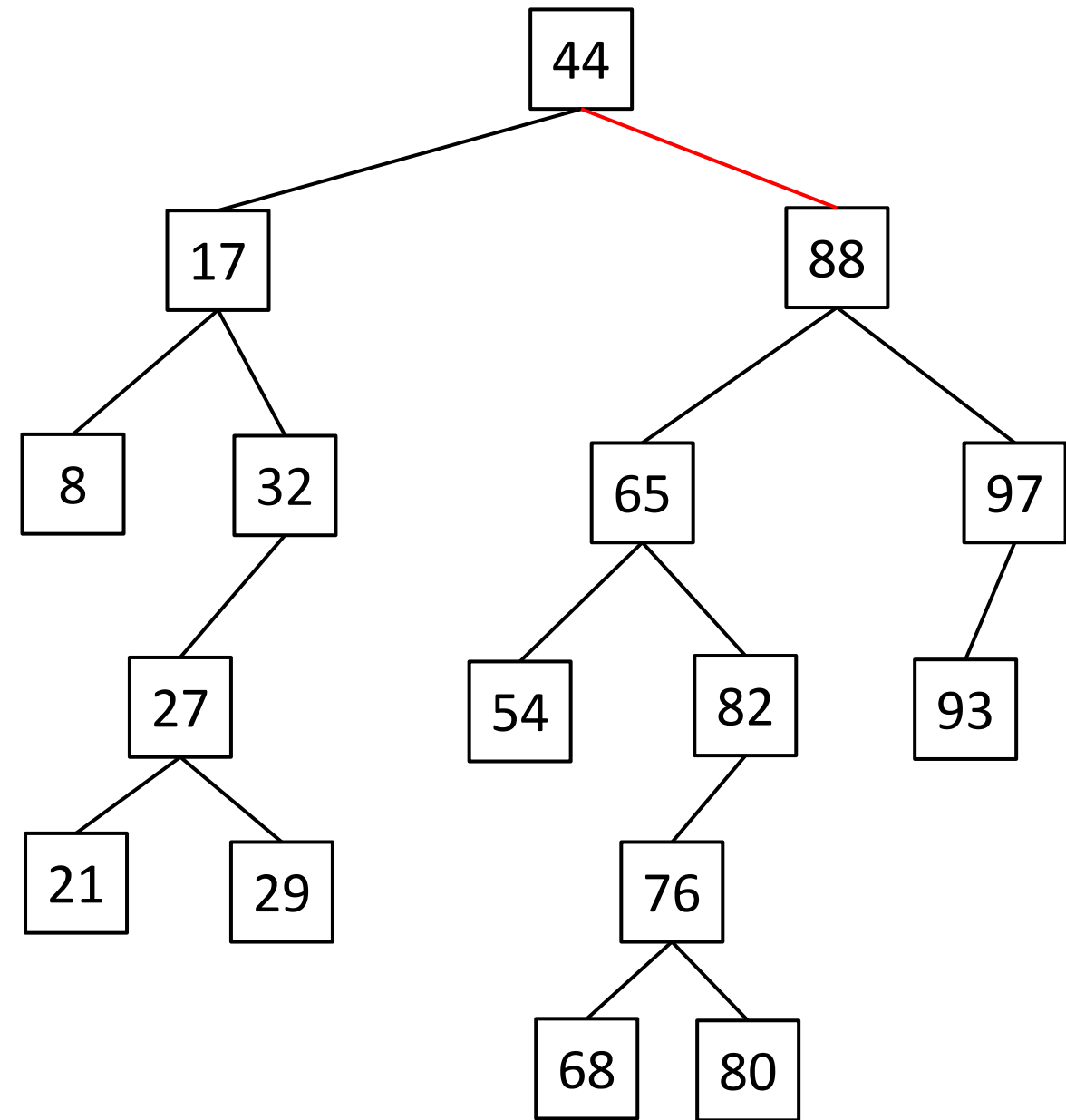
Step 1: Find the node in the tree



Binary Search Tree- Removal

`remove(68);`

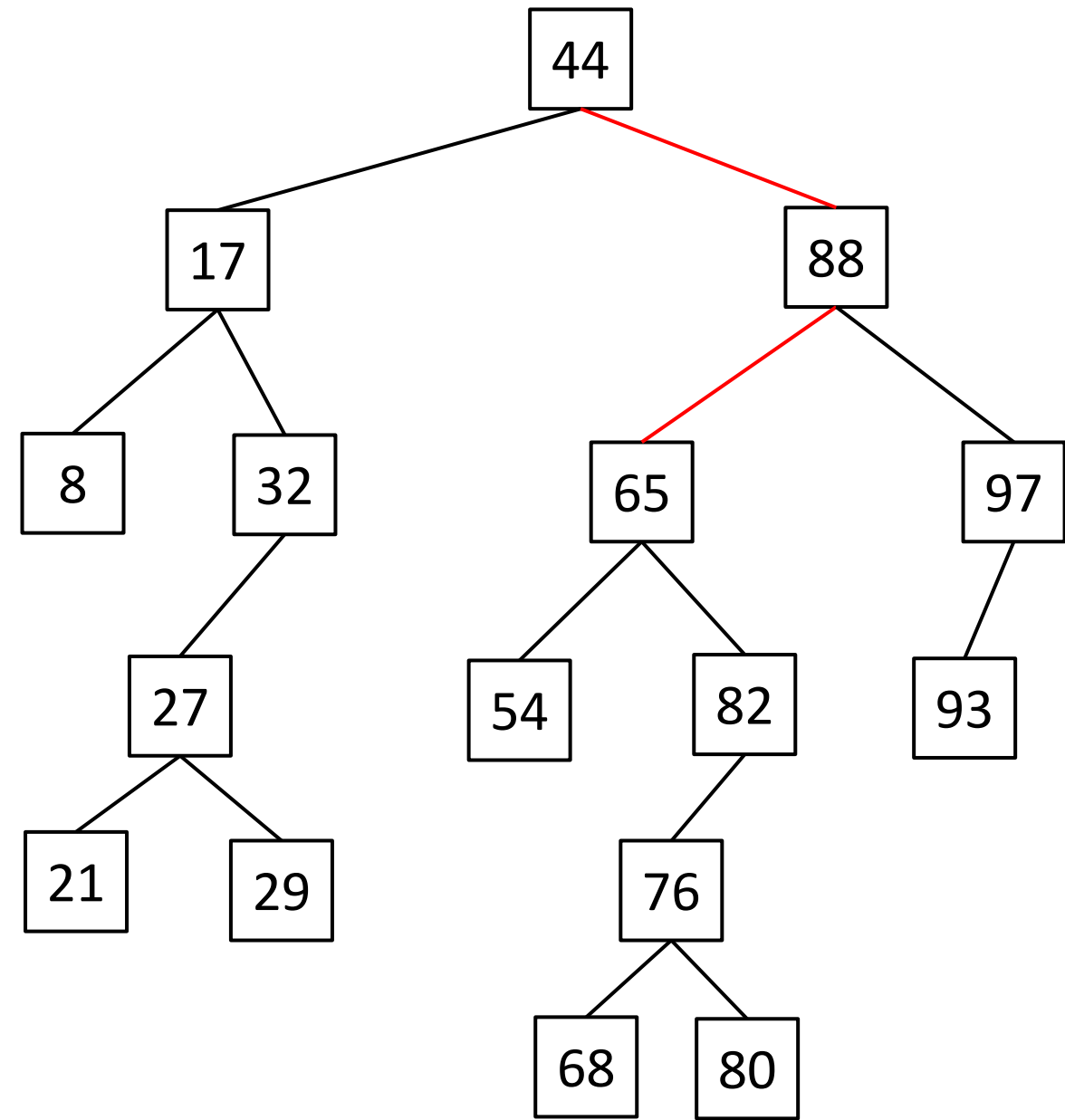
Step 1: Find the node in the tree



Binary Search Tree- Removal

`remove(68);`

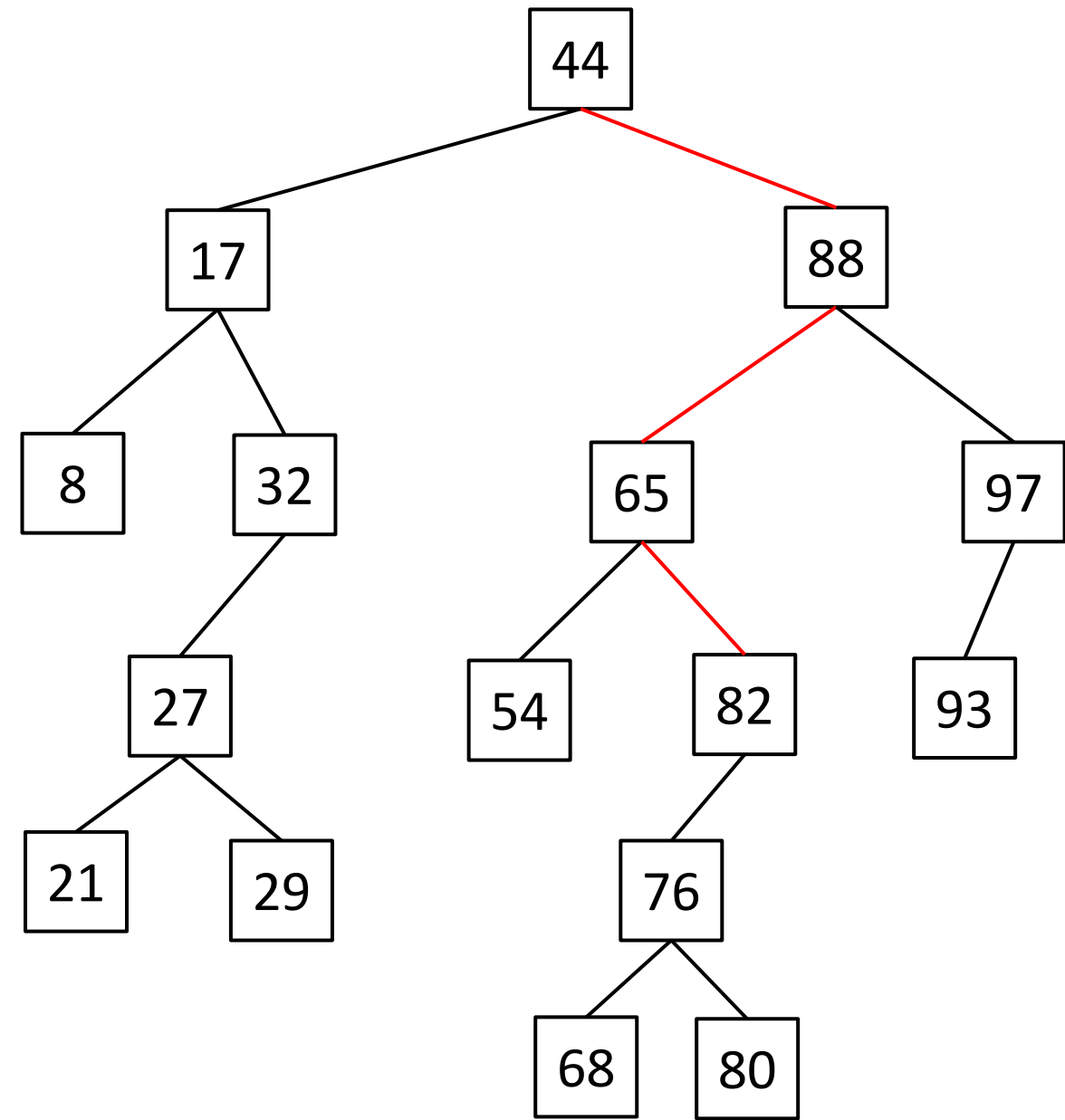
Step 1: Find the node in the tree



Binary Search Tree- Removal

`remove(68);`

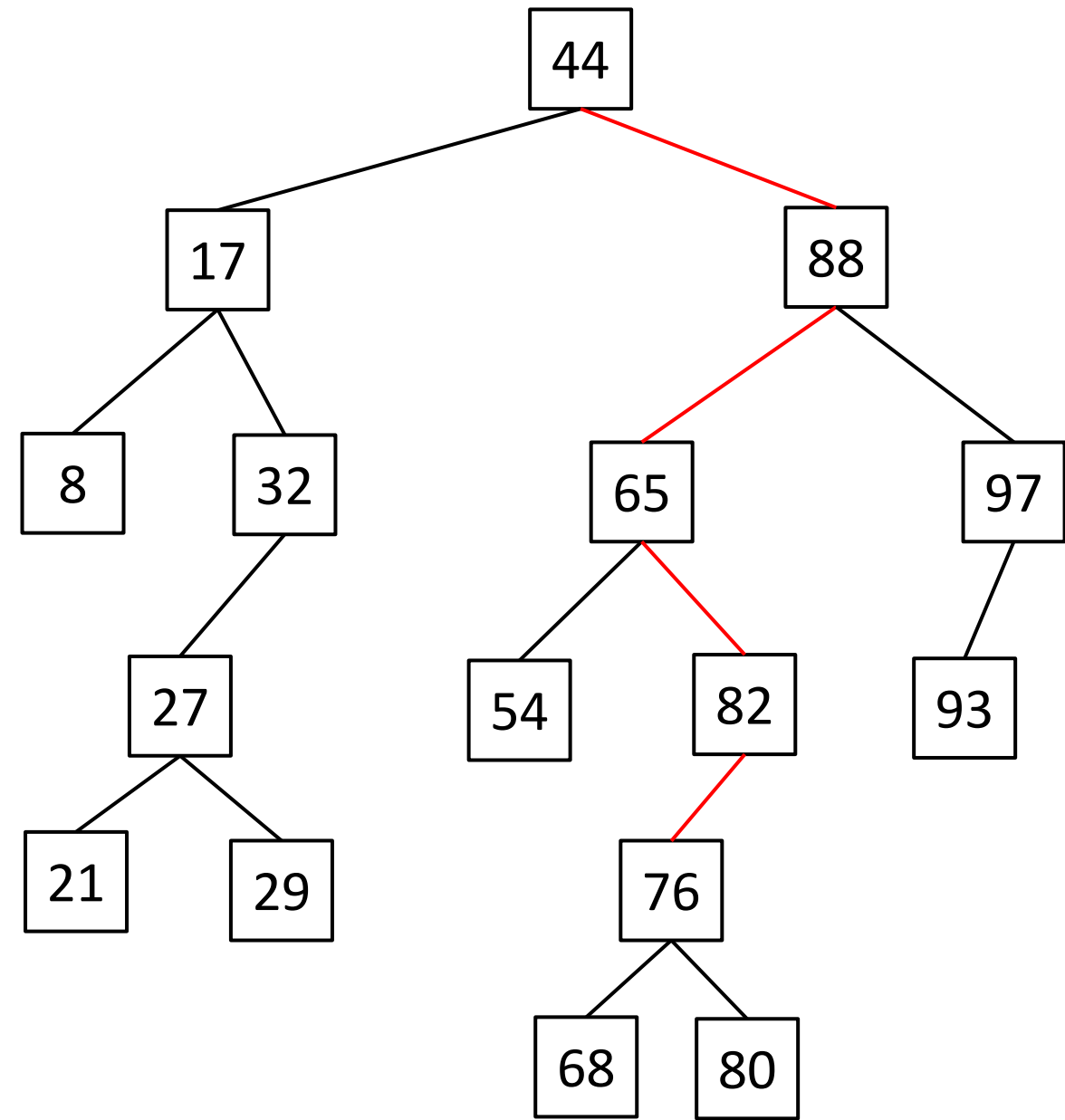
Step 1: Find the node in the tree



Binary Search Tree- Removal

`remove(68);`

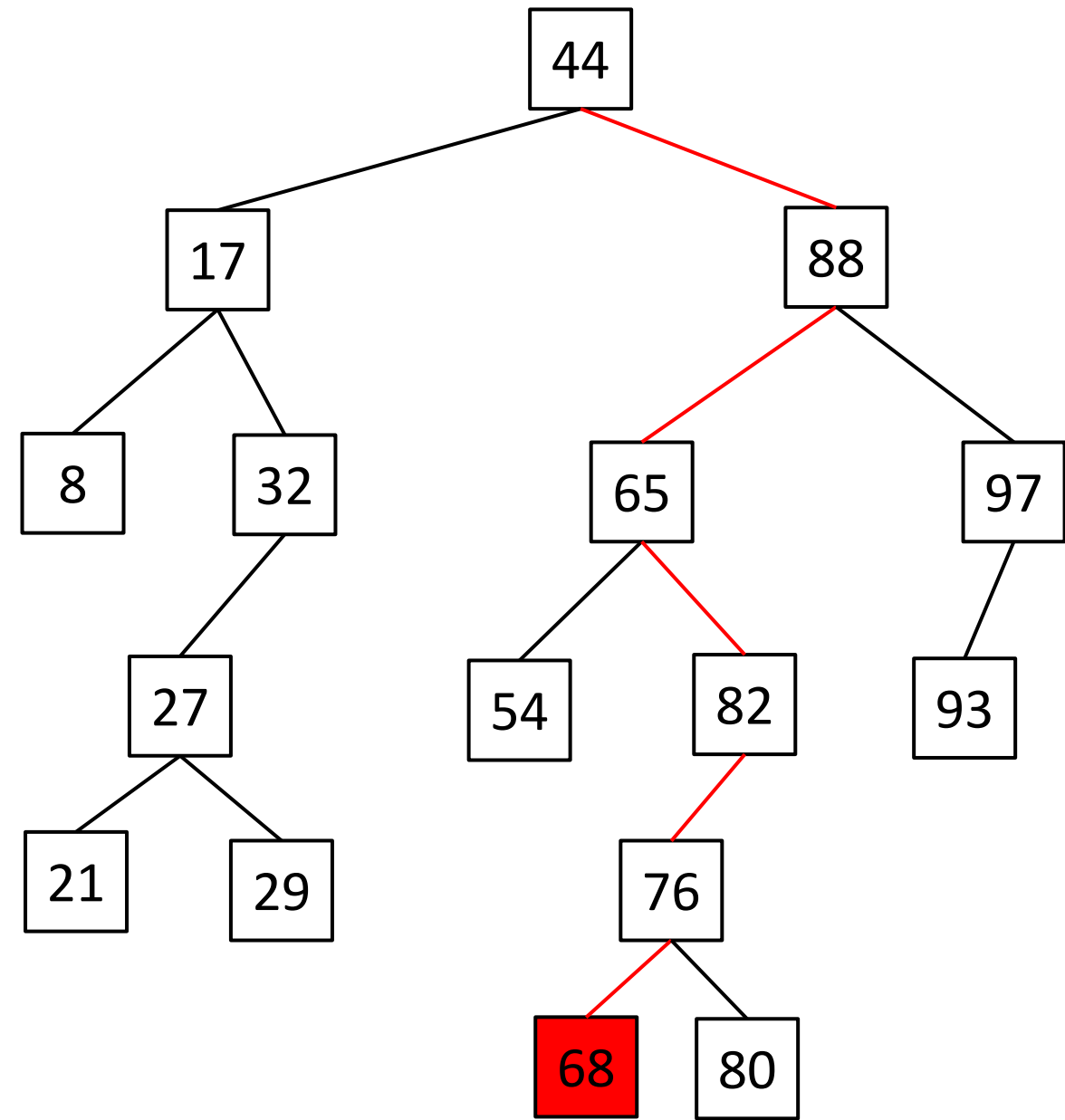
Step 1: Find the node in the tree



Binary Search Tree- Removal

`remove(68);`

Step 1: Find the node in the tree

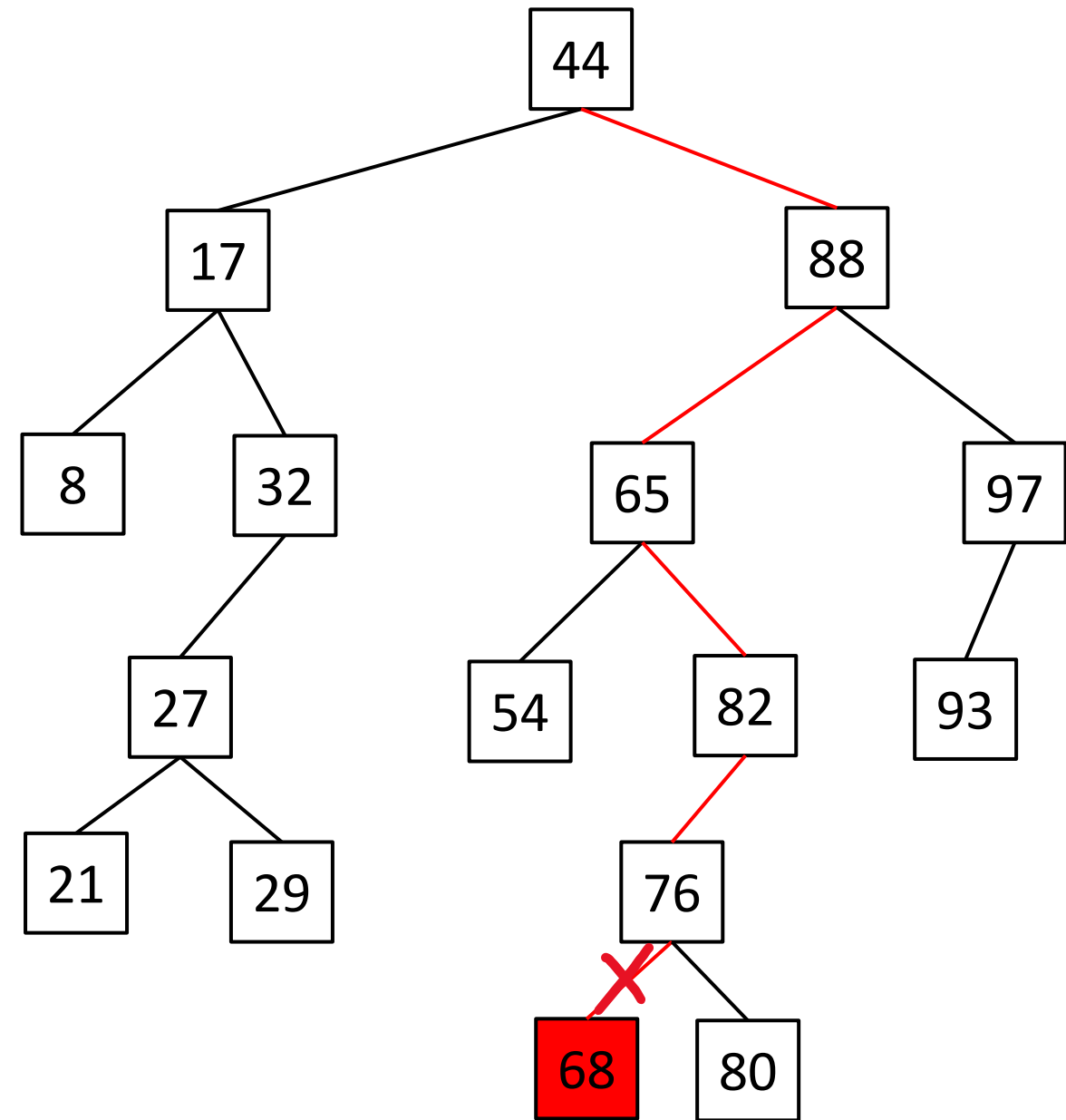


Binary Search Tree- Removal

`remove(68);`

Step 1: Find the node in the tree

Step 2: Change parent to point to null



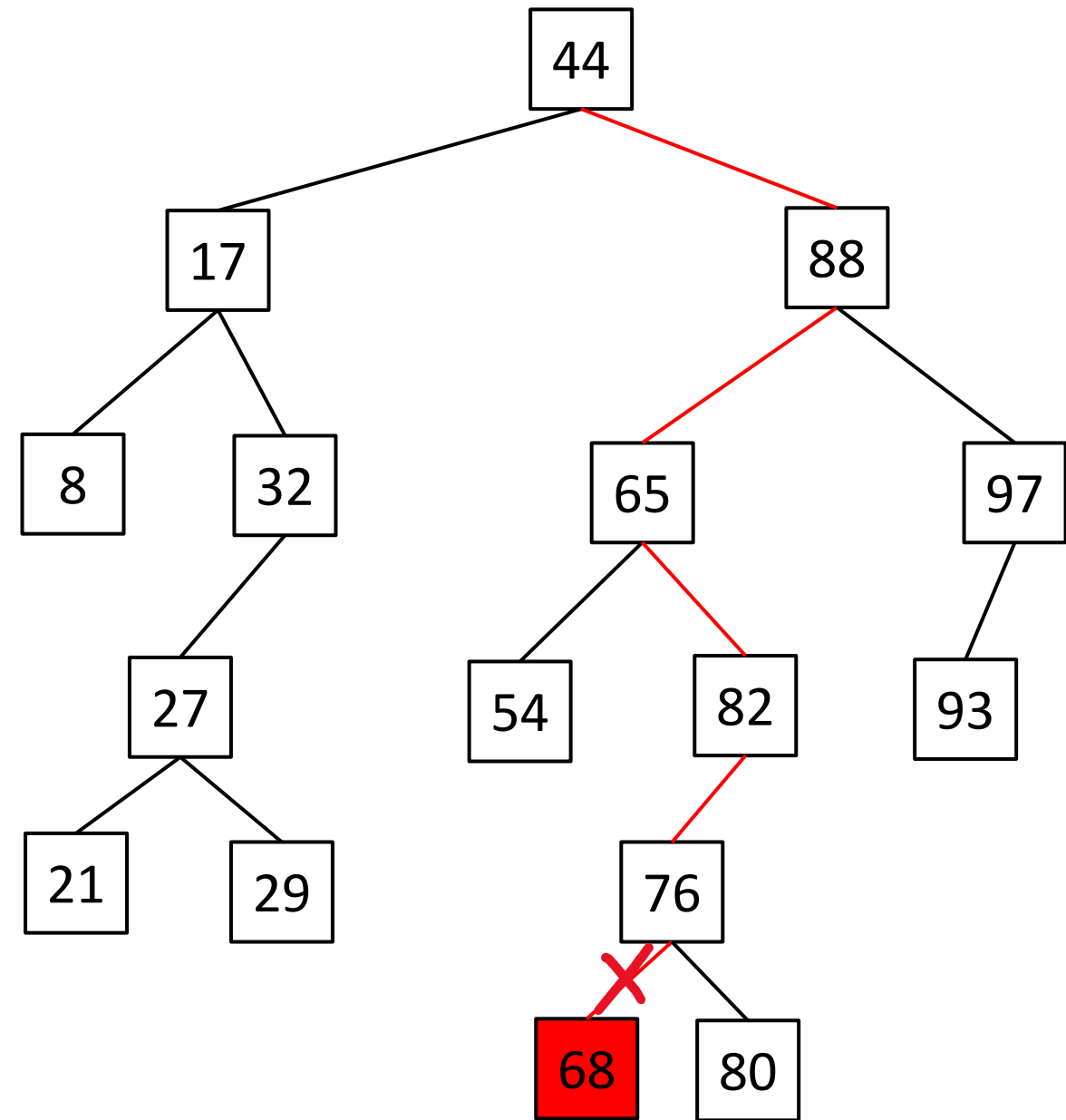
Binary Search Tree- Removal

`remove(68);`

Step 1: Find the node in the tree

Step 2: Change parent to point to null

Does this always work?



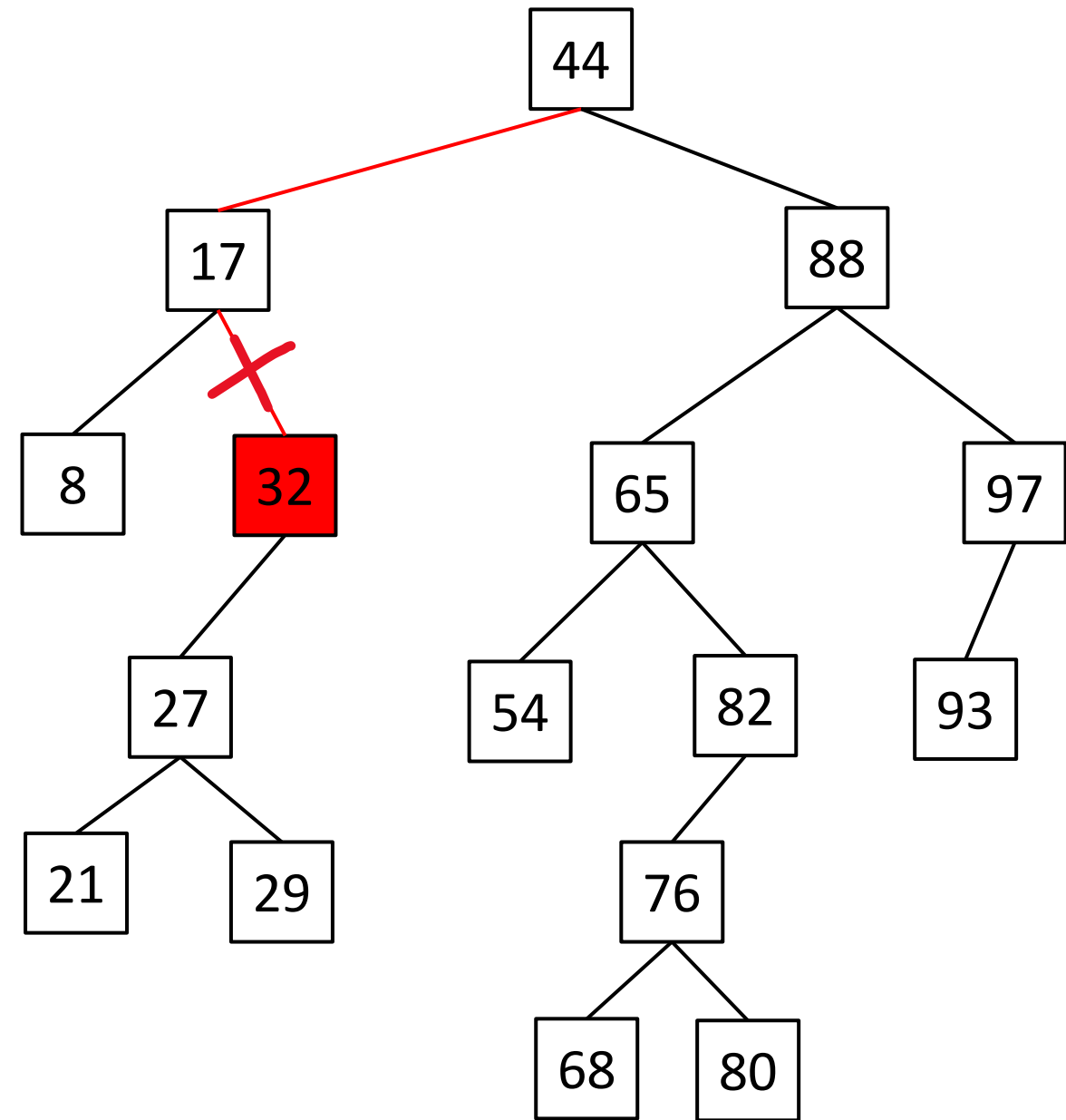
Binary Search Tree- Removal

`remove(32);`

Step 1: Find the node in the tree

Step 2: Change parent to point to null

This does not always work

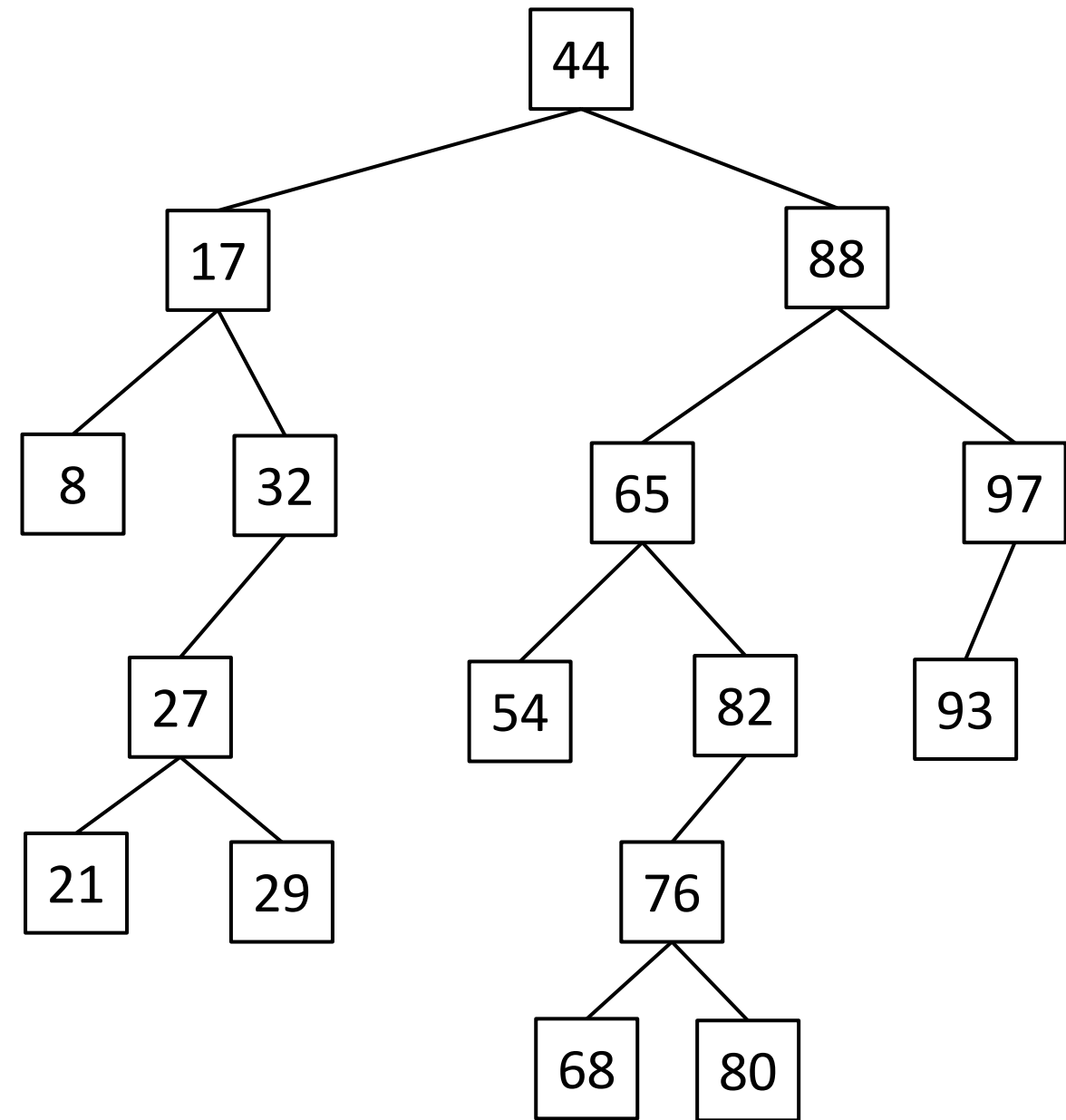


Binary Search Tree- Removal

Case 1: Node has no children

Case 2: Node has one child

Case 3: Node has two children



Binary Search Tree- Removal

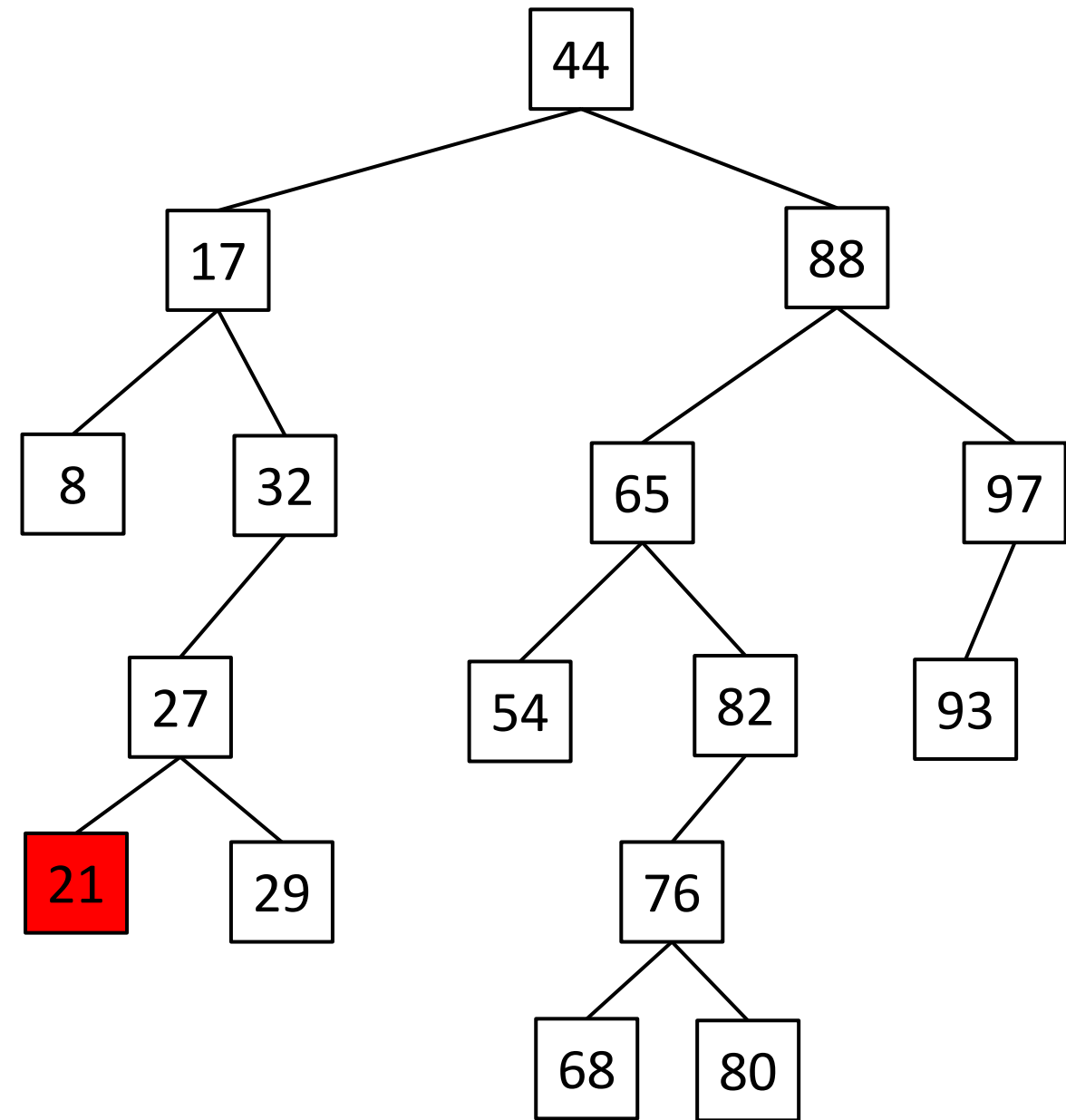
Case 1: Node has no children

Case 2: Node has one child

Case 3: Node has two children

`remove(21);`

How do we know it has no children?



Binary Search Tree- Removal

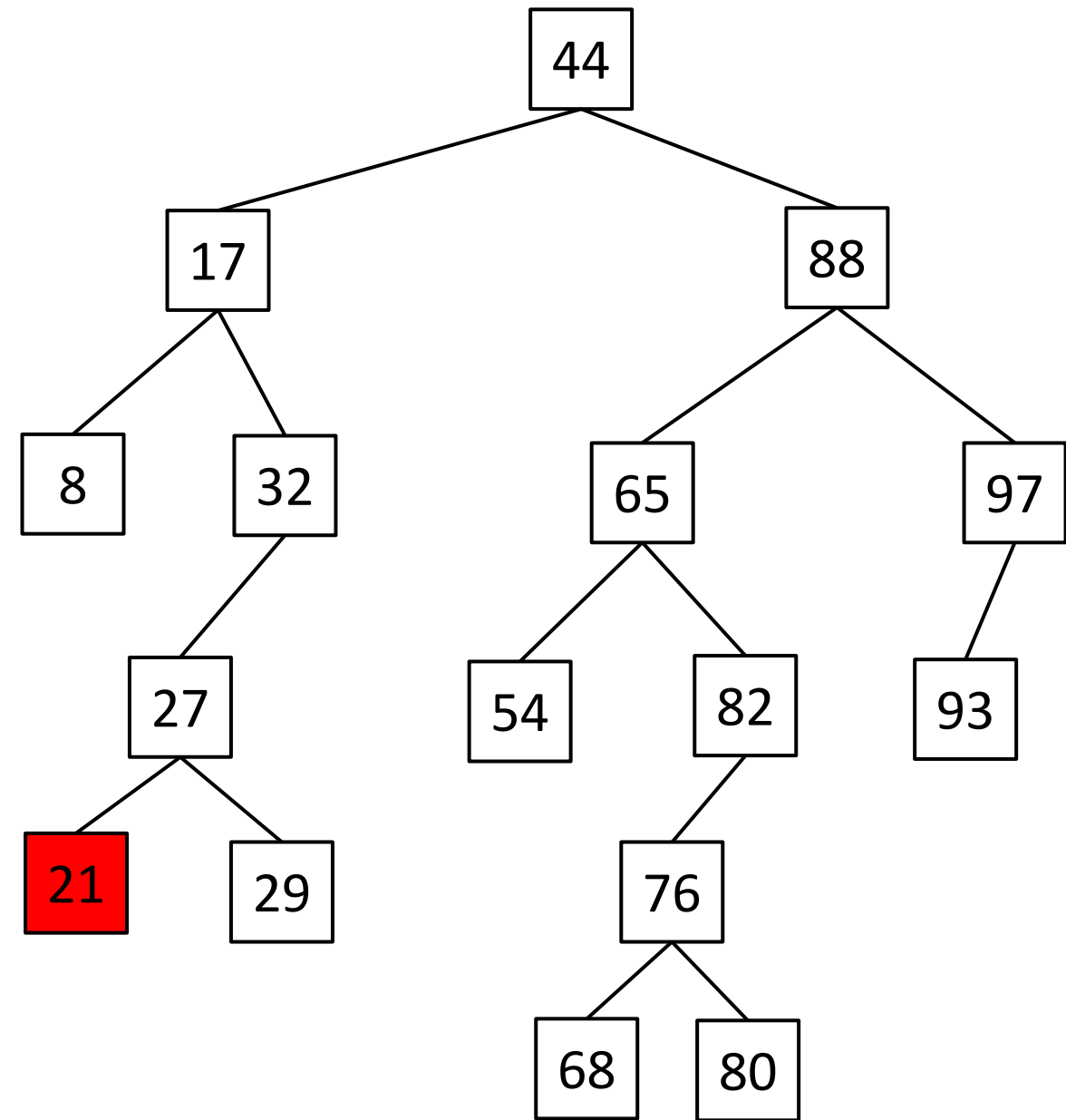
Case 1: Node has no children

Case 2: Node has one child

Case 3: Node has two children

`remove(21);`

How do we know it has no children?
If its left and right child are both null



Binary Search Tree- Removal

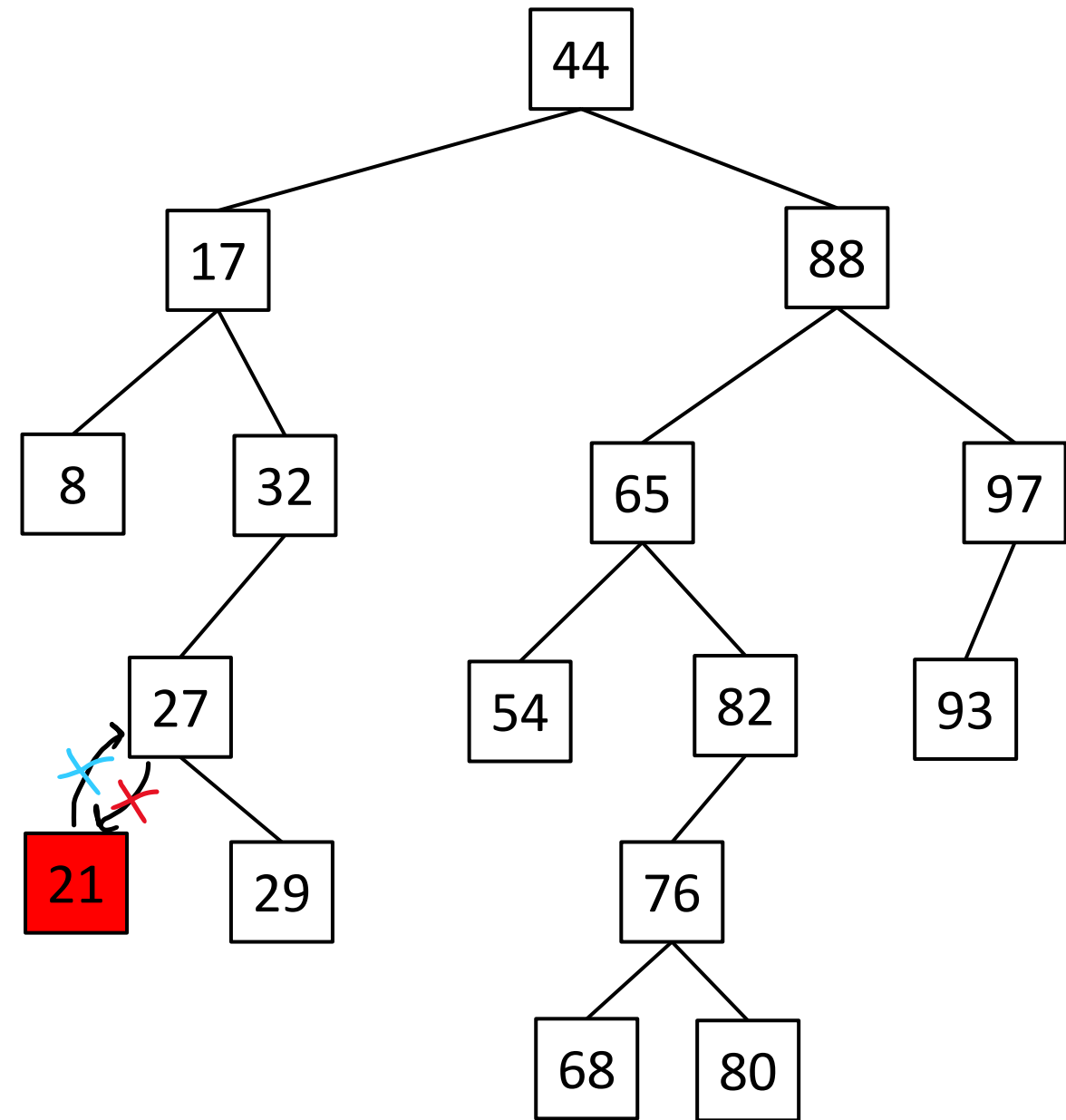
Case 1: Node has no children

Case 2: Node has one child

Case 3: Node has two children

`remove(21);`

1. Update parent's **child** to point to **null**
2. Update Node's **parent** to point to **null**



Binary Search Tree- Removal

Case 1: Node has no children

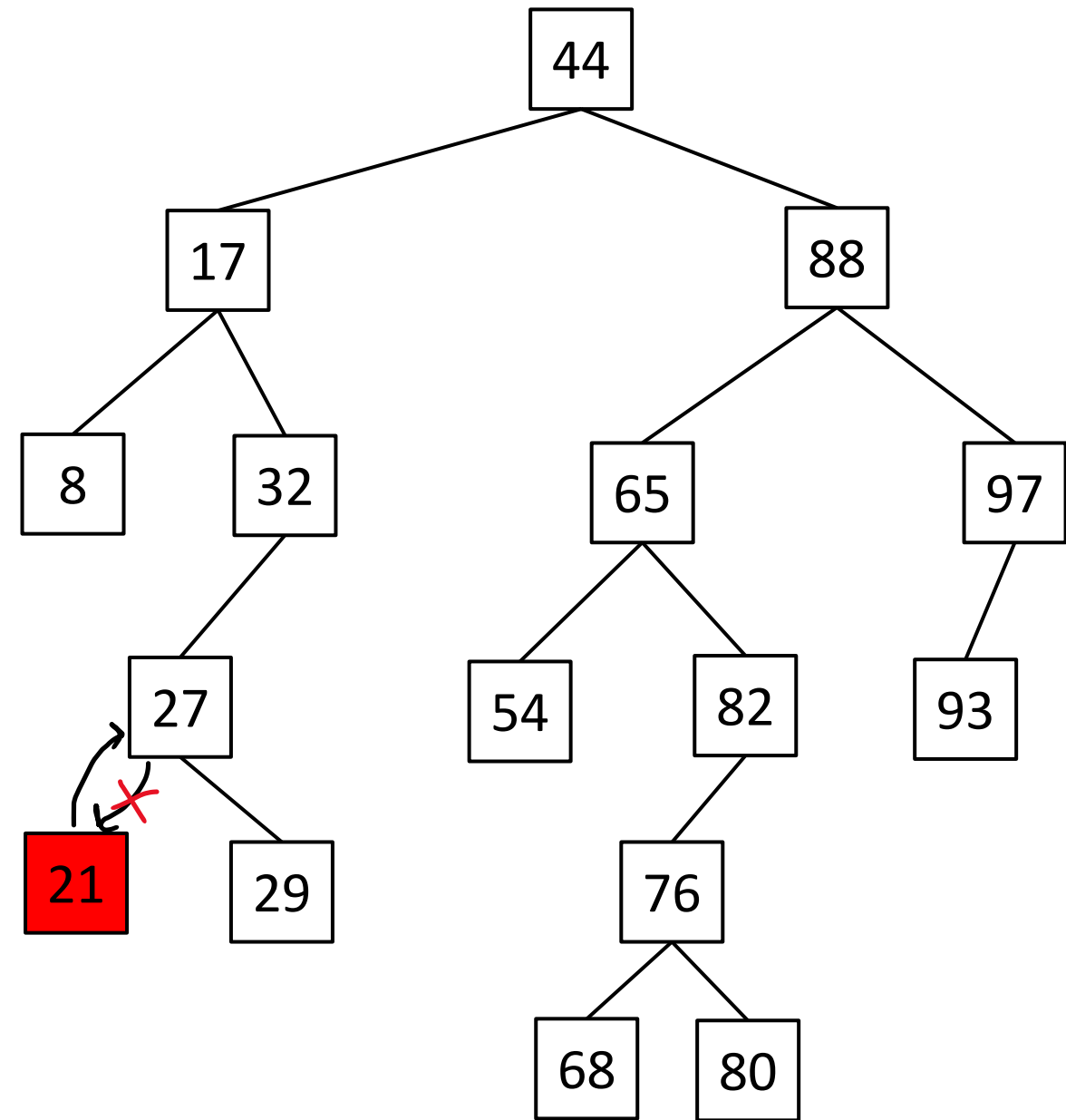
Case 2: Node has one child

Case 3: Node has two children

`remove(21);`

1. Update parent's **child** to point to **null**

2. ~~Update Node's **parent** to point to **null**~~



Binary Search Tree- Removal

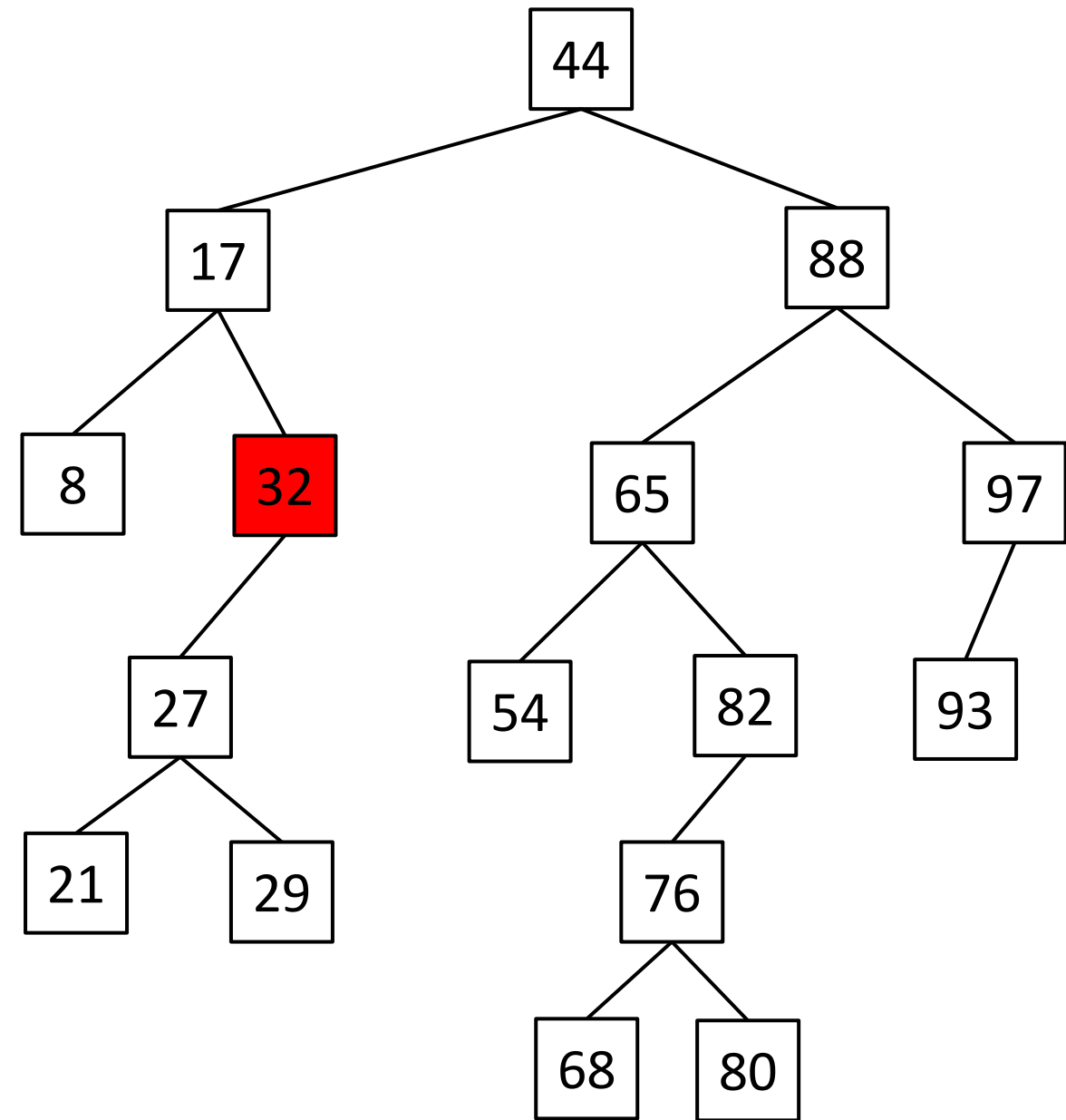
Case 1: Node has no children

Case 2: Node has one child

Case 3: Node has two children

`remove(32);`

???



Binary Search Tree- Removal

Case 1: Node has no children

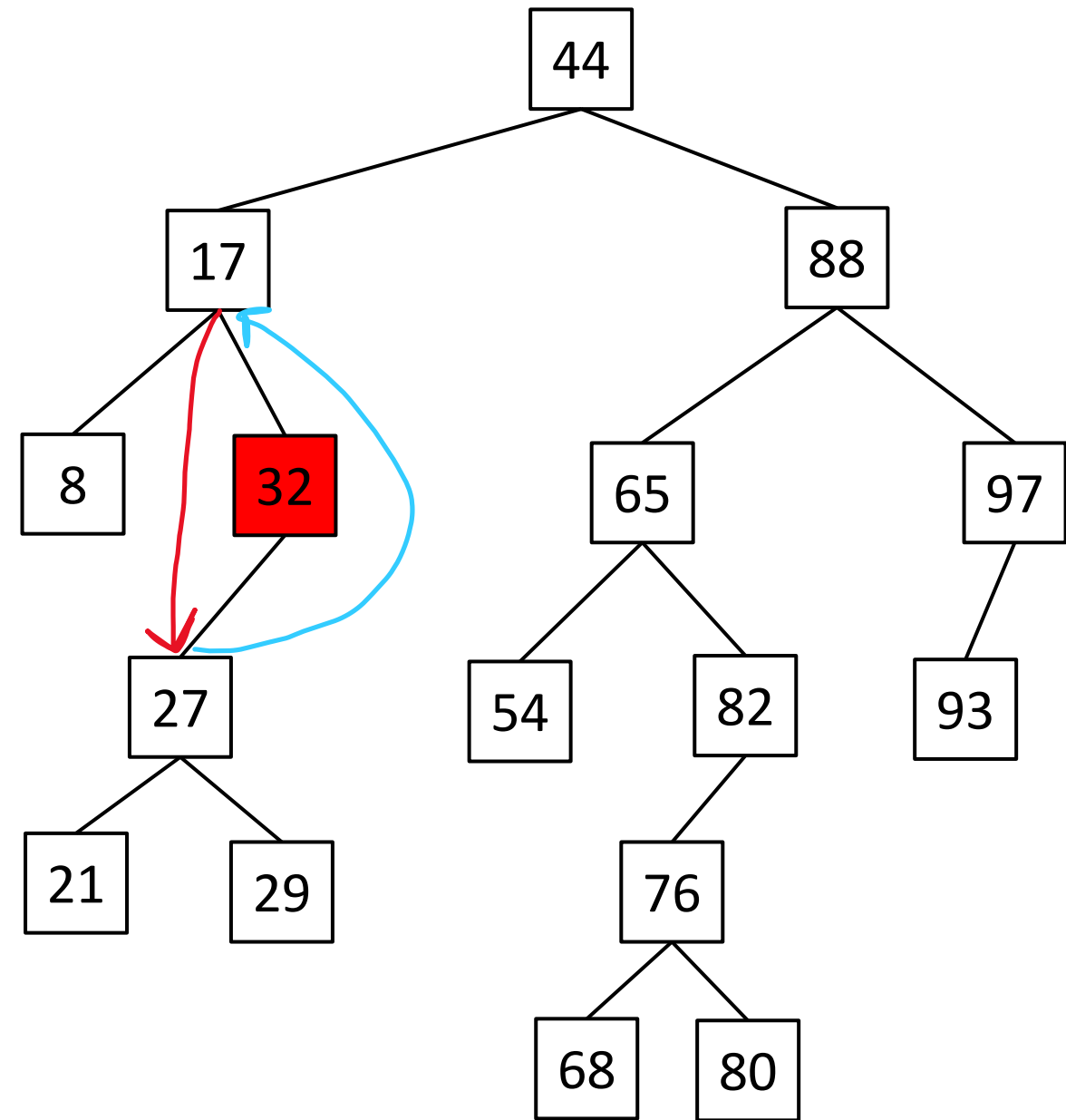
Case 2: Node has one child

Case 3: Node has two children

`remove(32);`

Change the Node's parent to point to the only child

Update the Node's only child parent to point to the Node's Parent



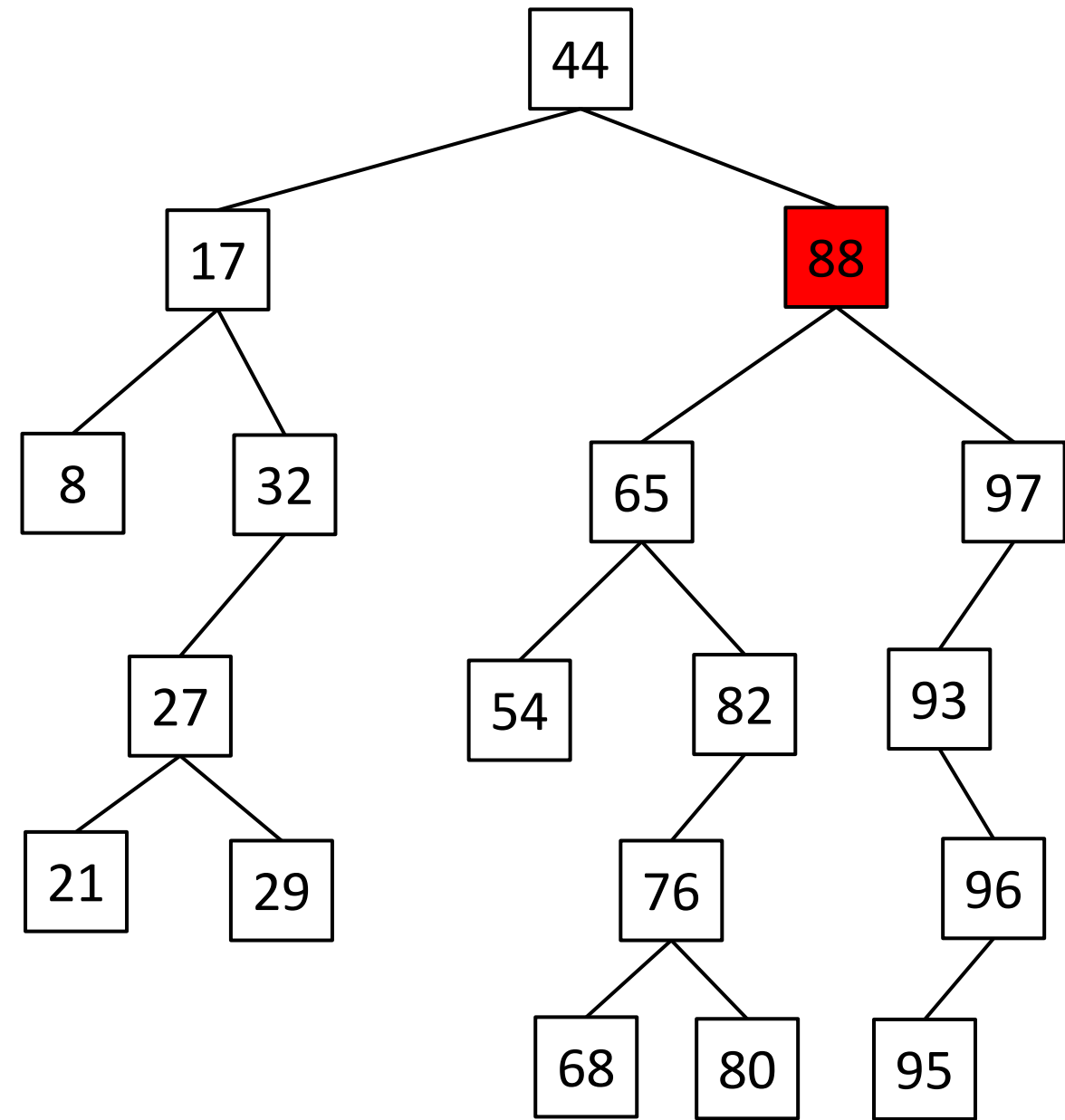
Binary Search Tree- Removal

Case 1: Node has no children

Case 2: Node has one child

Case 3: Node has two children

`remove(88);`



Binary Search Tree- Removal

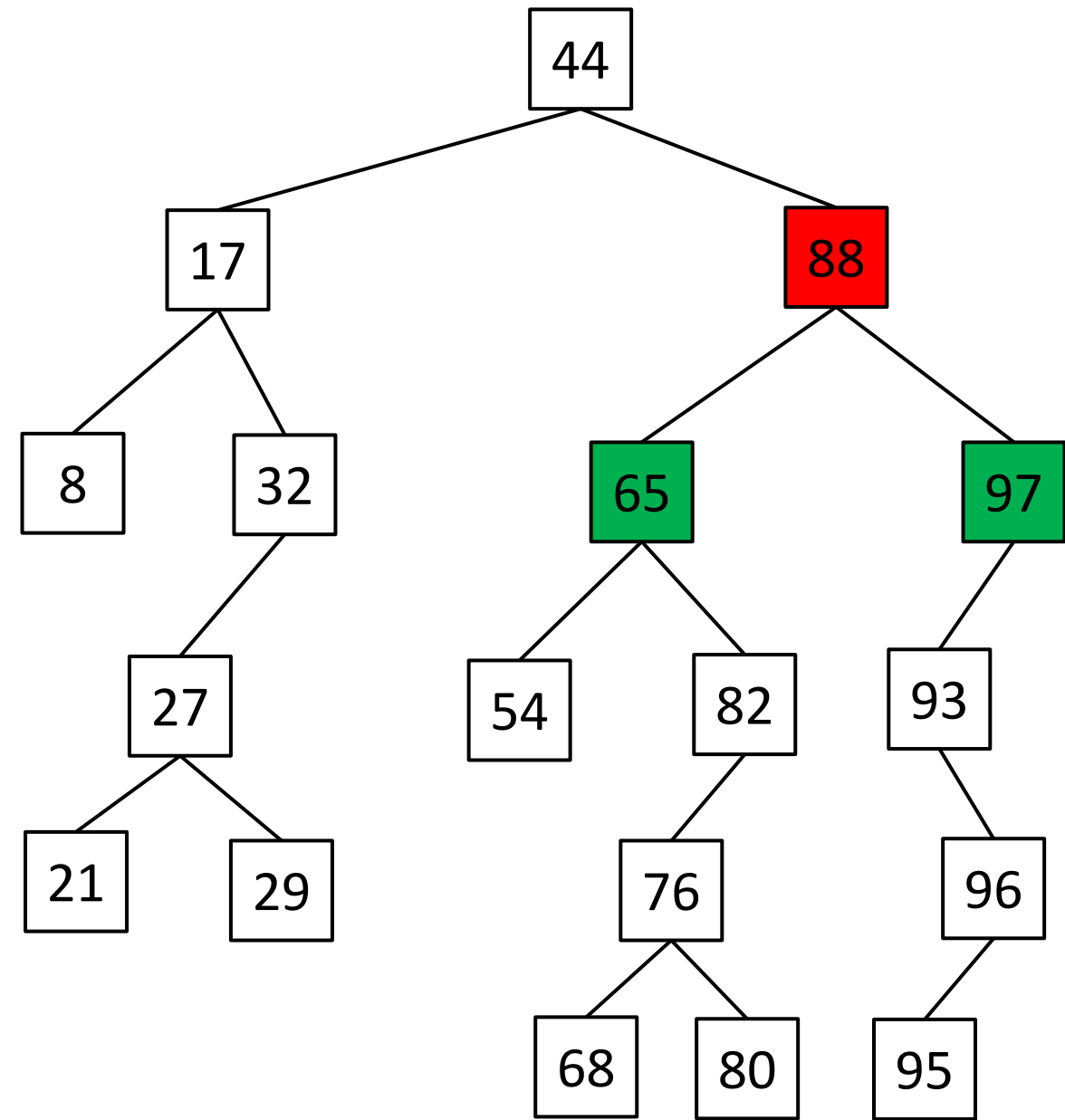
Case 1: Node has no children

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Case 3: Node has two children

`remove(88);`

Which child to use?



Binary Search Tree- Removal

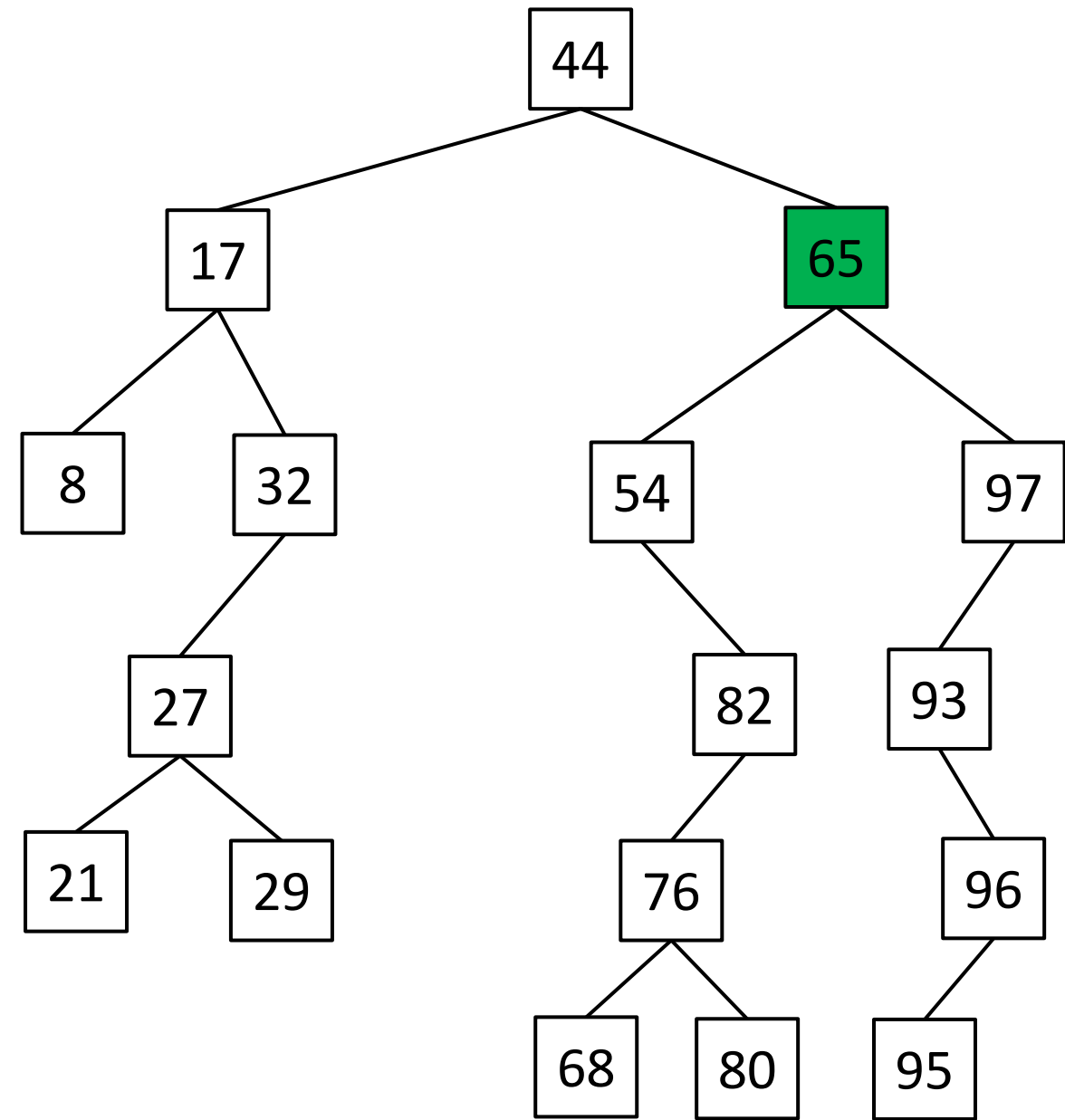
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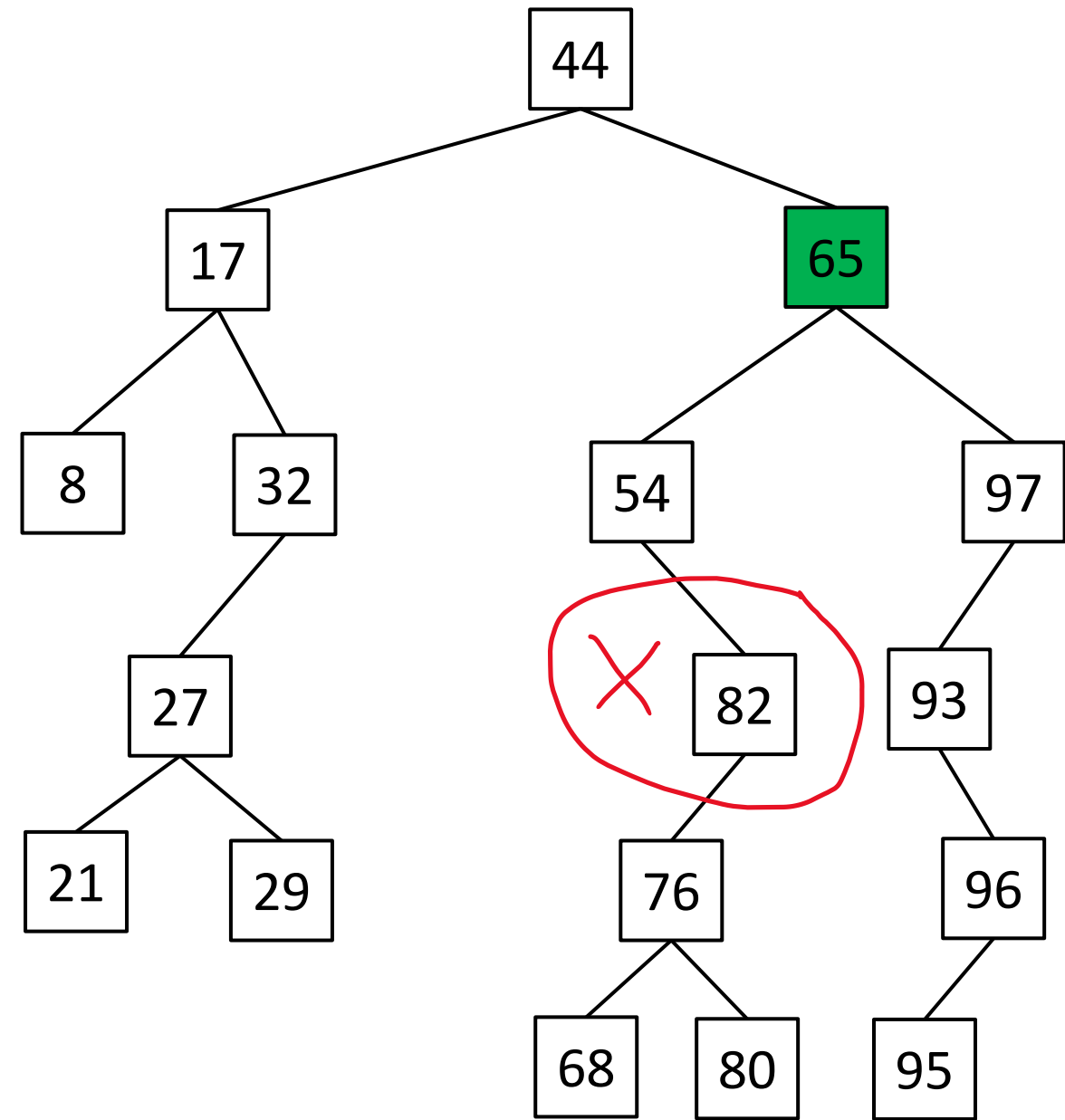
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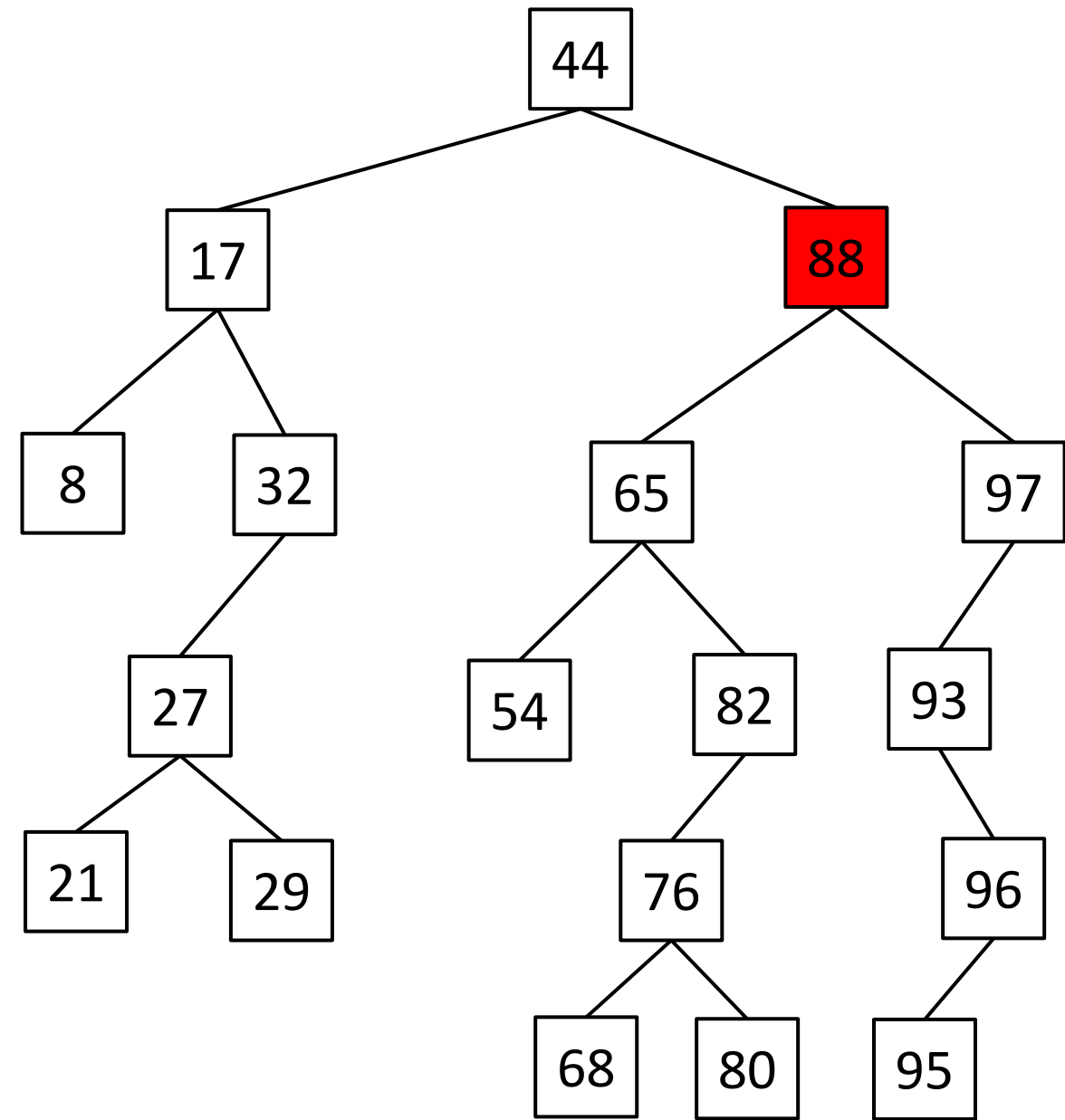
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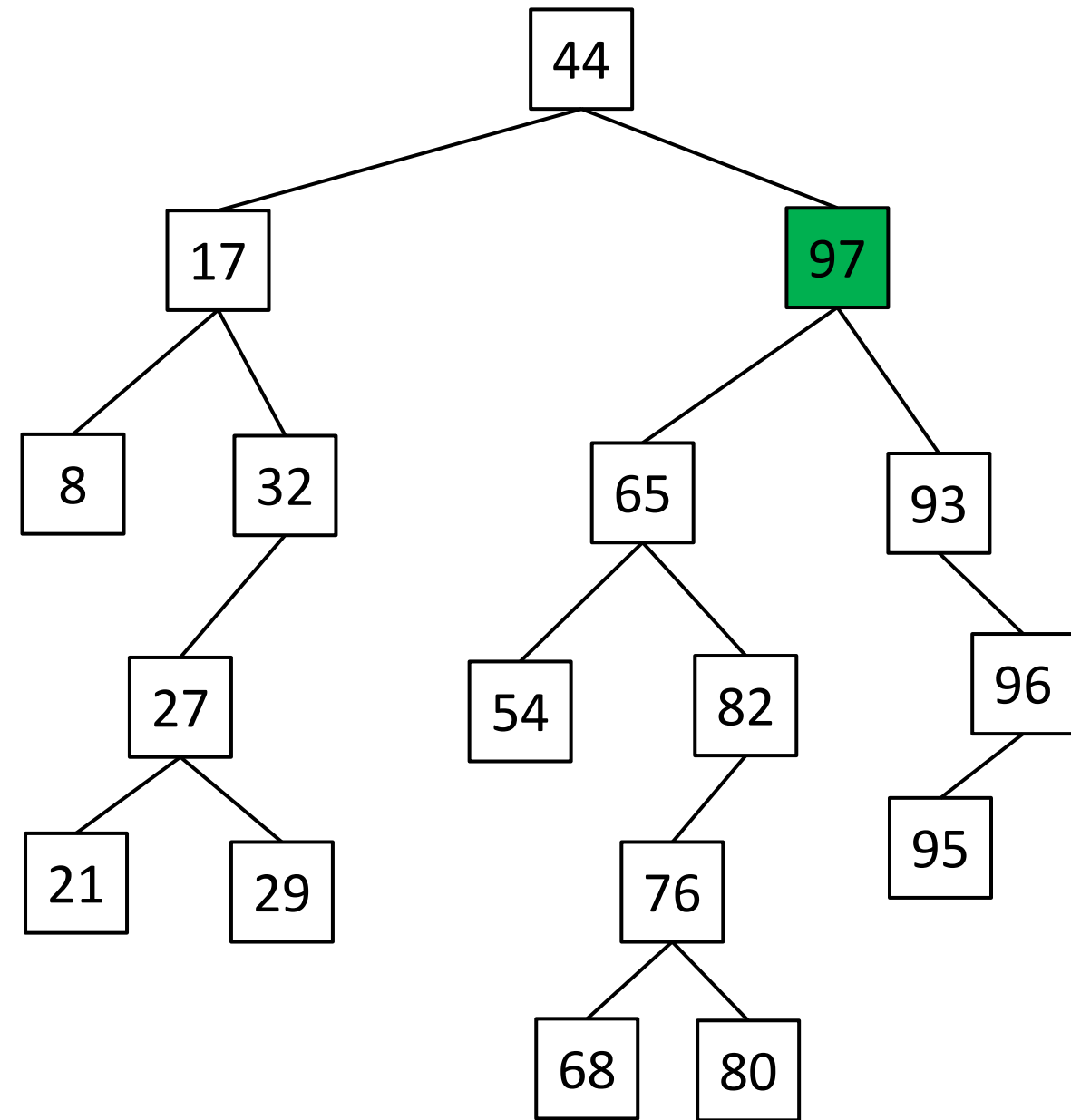
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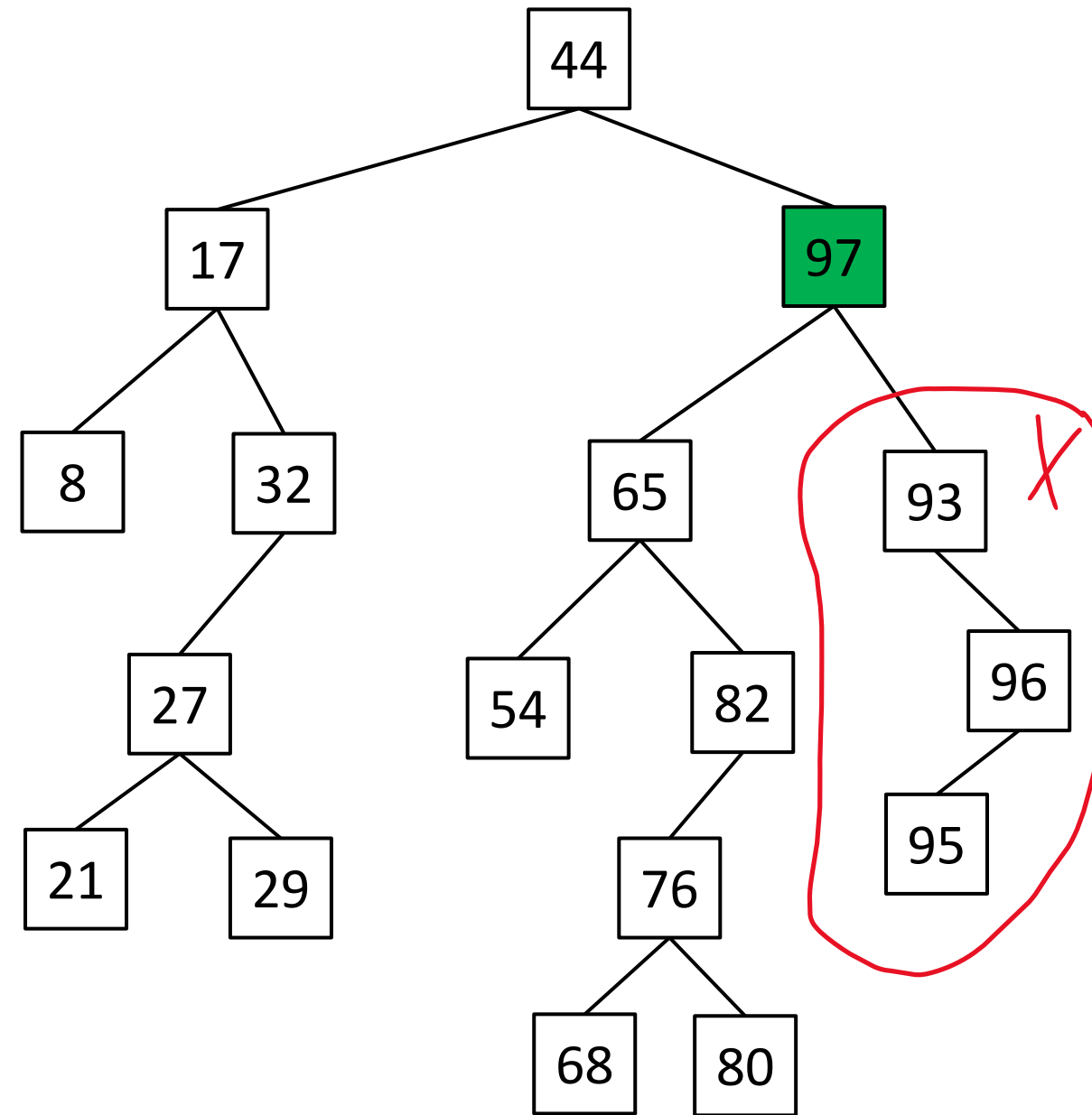
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Binary Search Tree- Removal

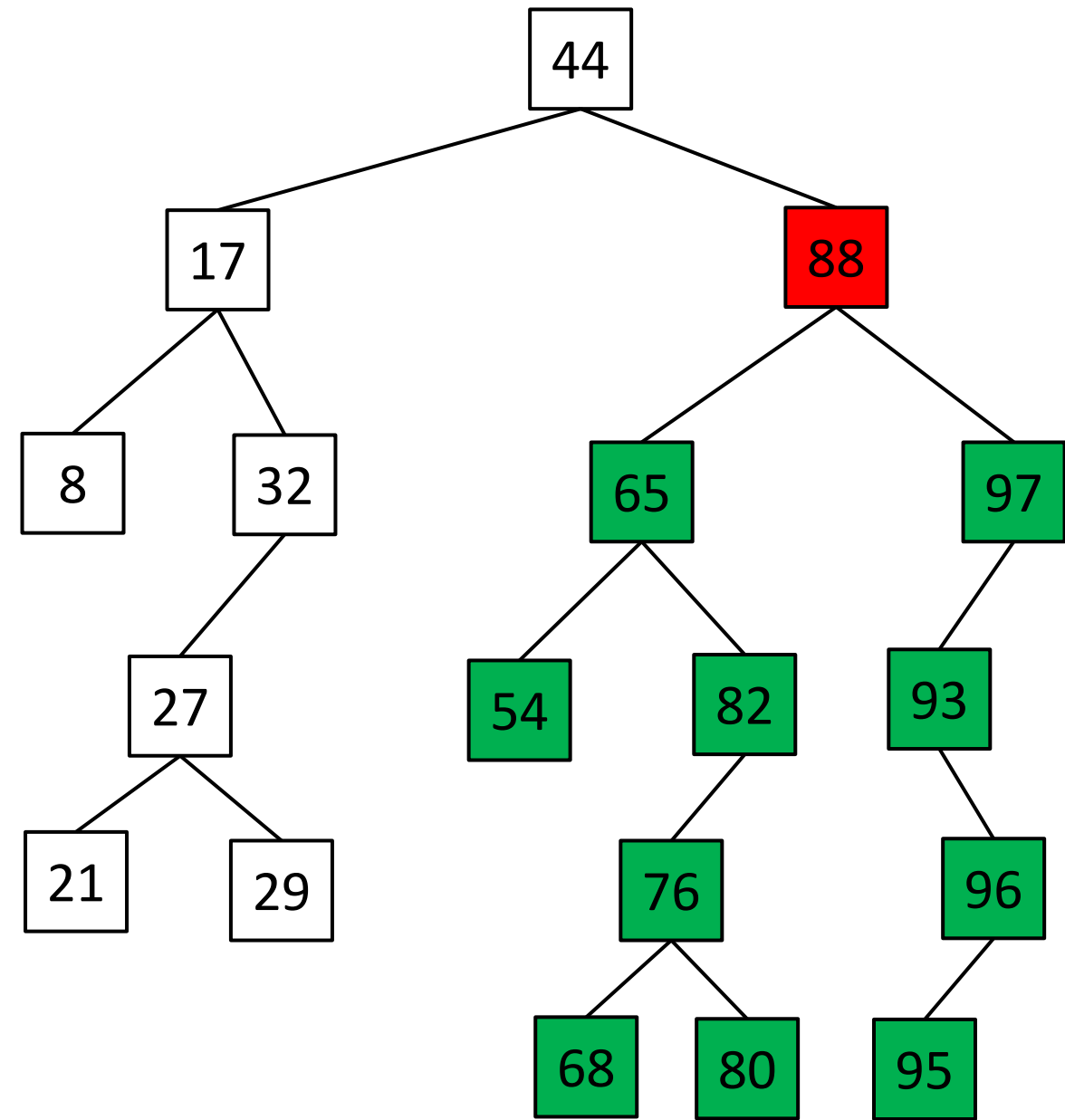
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`remove(88);`

Which ~~child~~ **descendant** to use?



Binary Search Tree- Removal

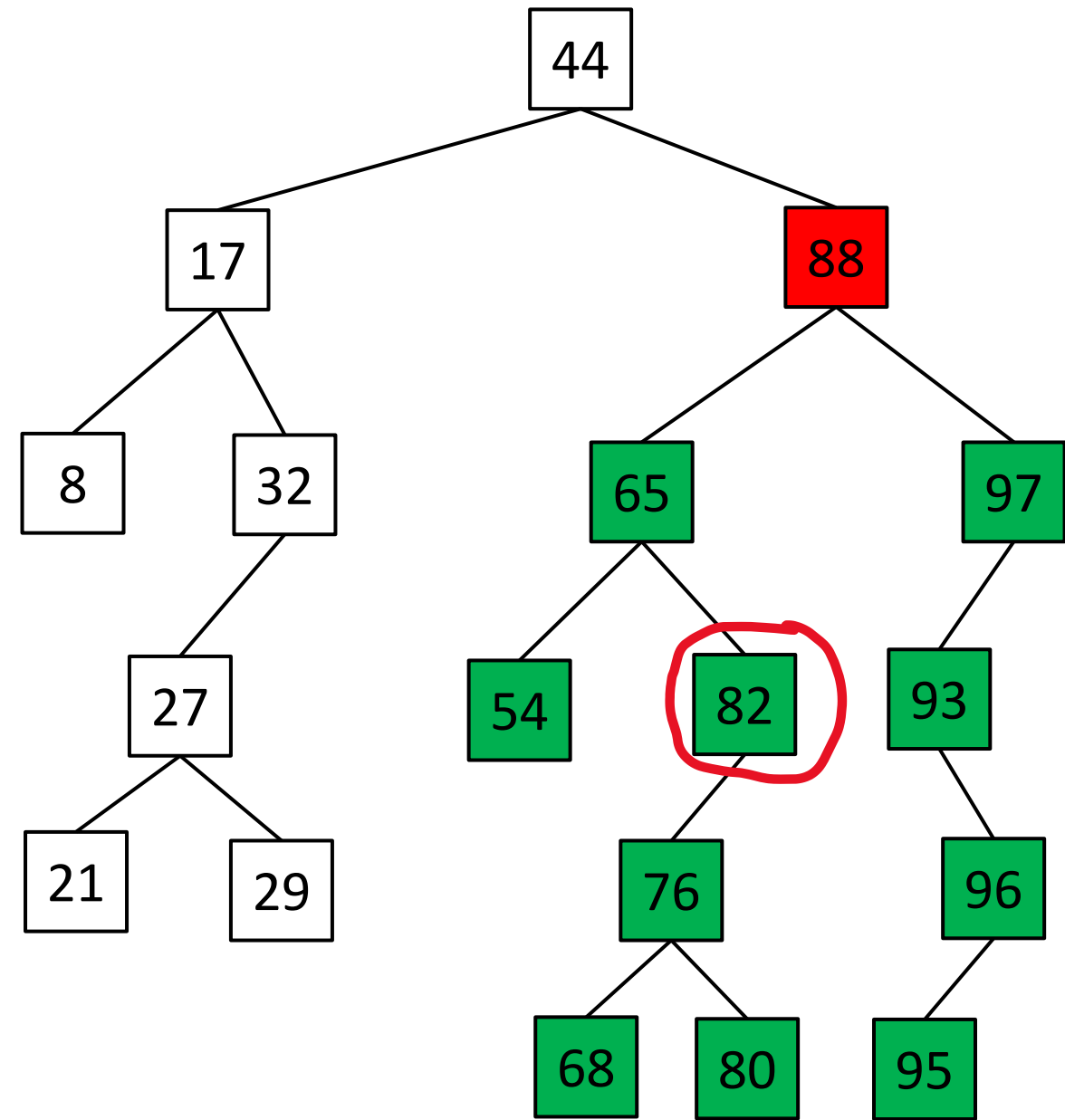
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Binary Search Tree- Removal

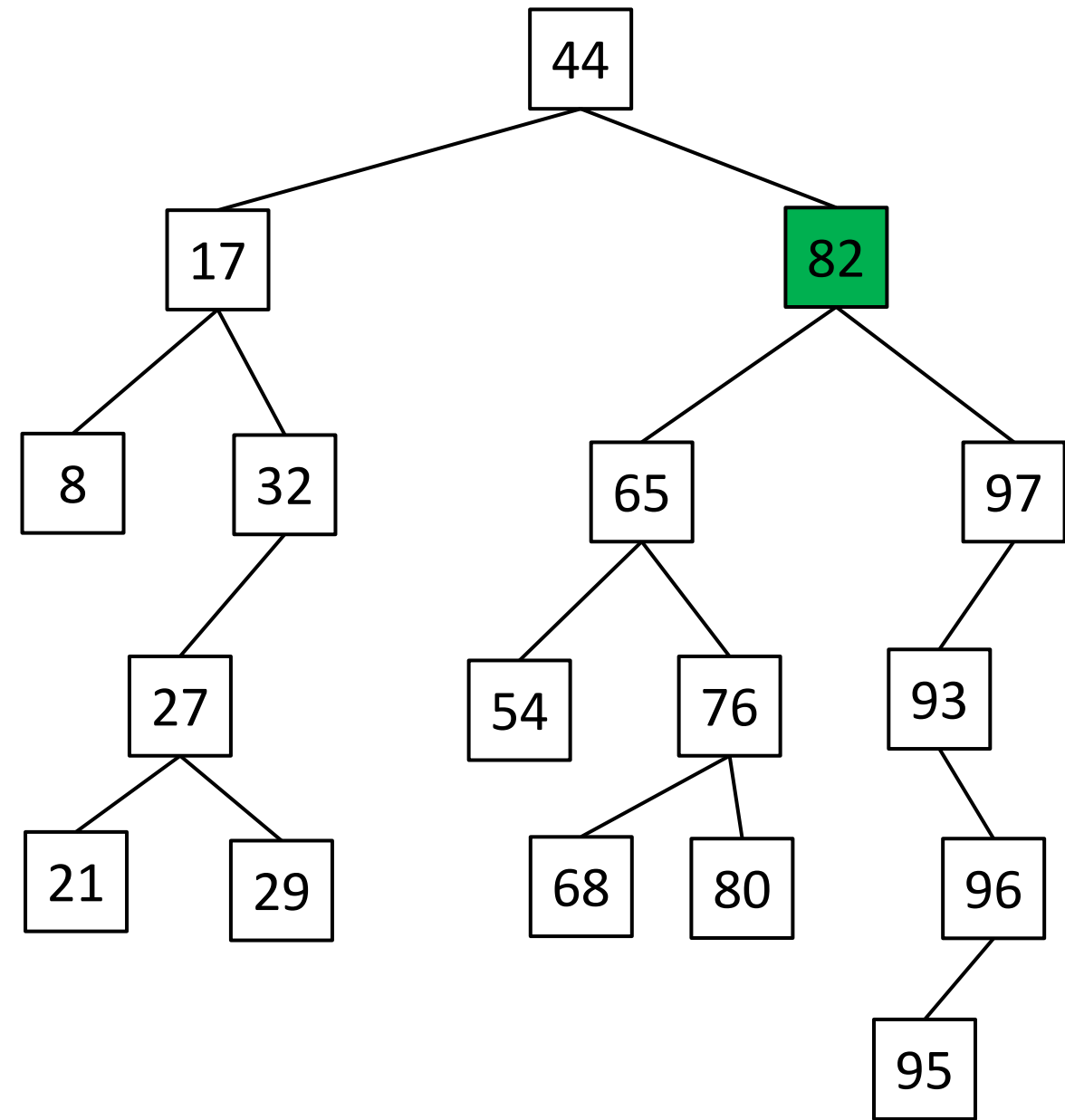
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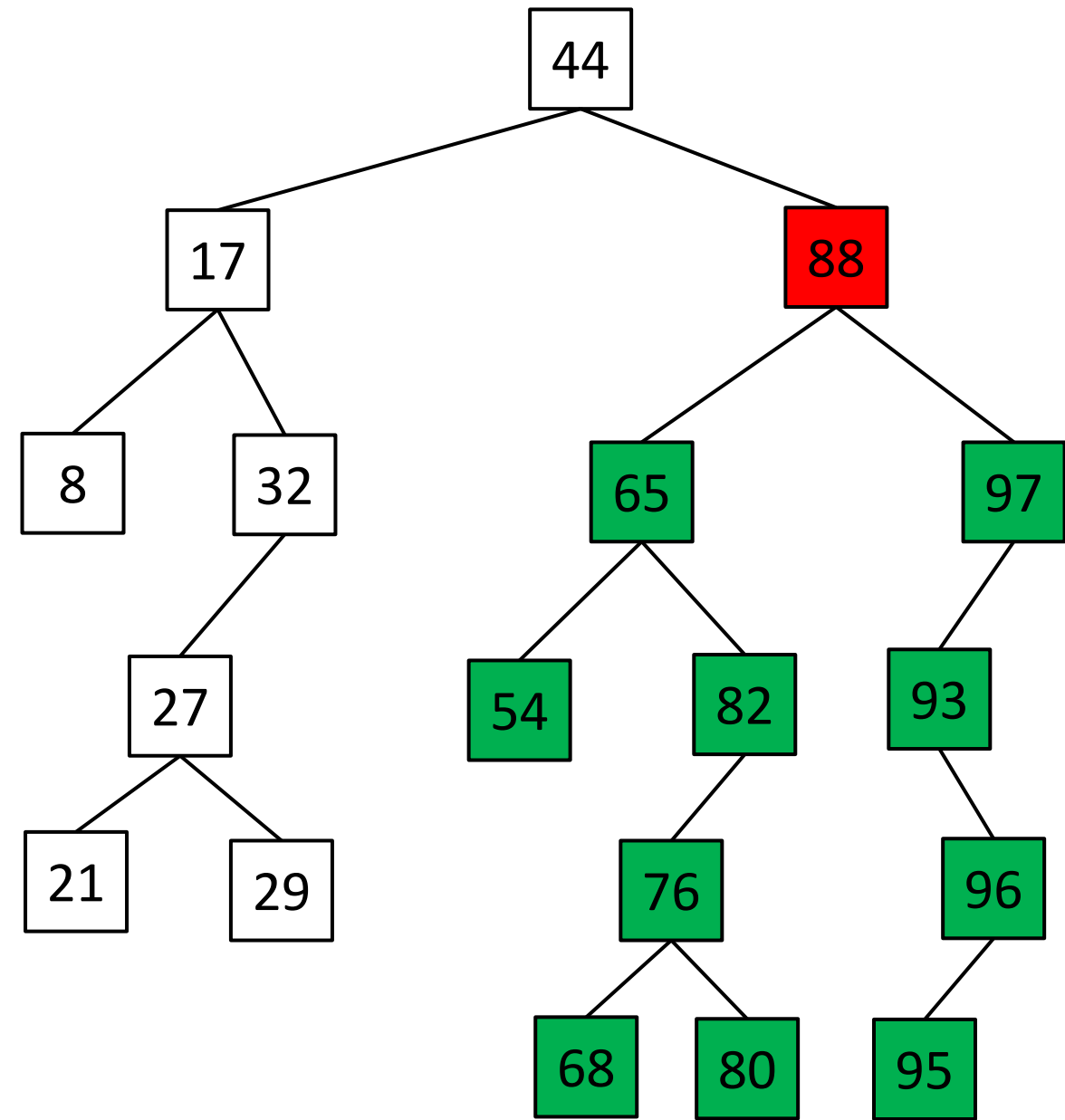
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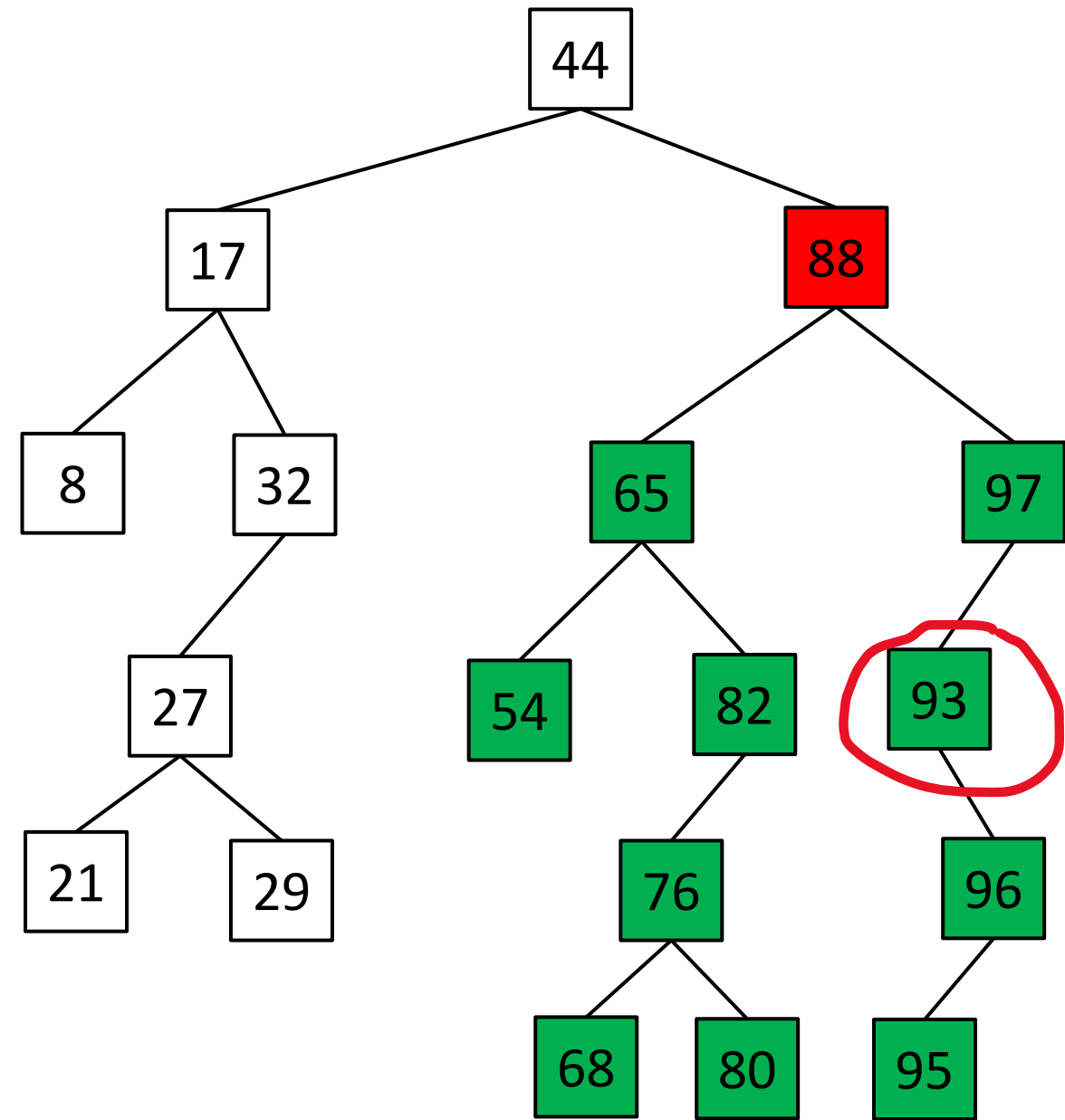
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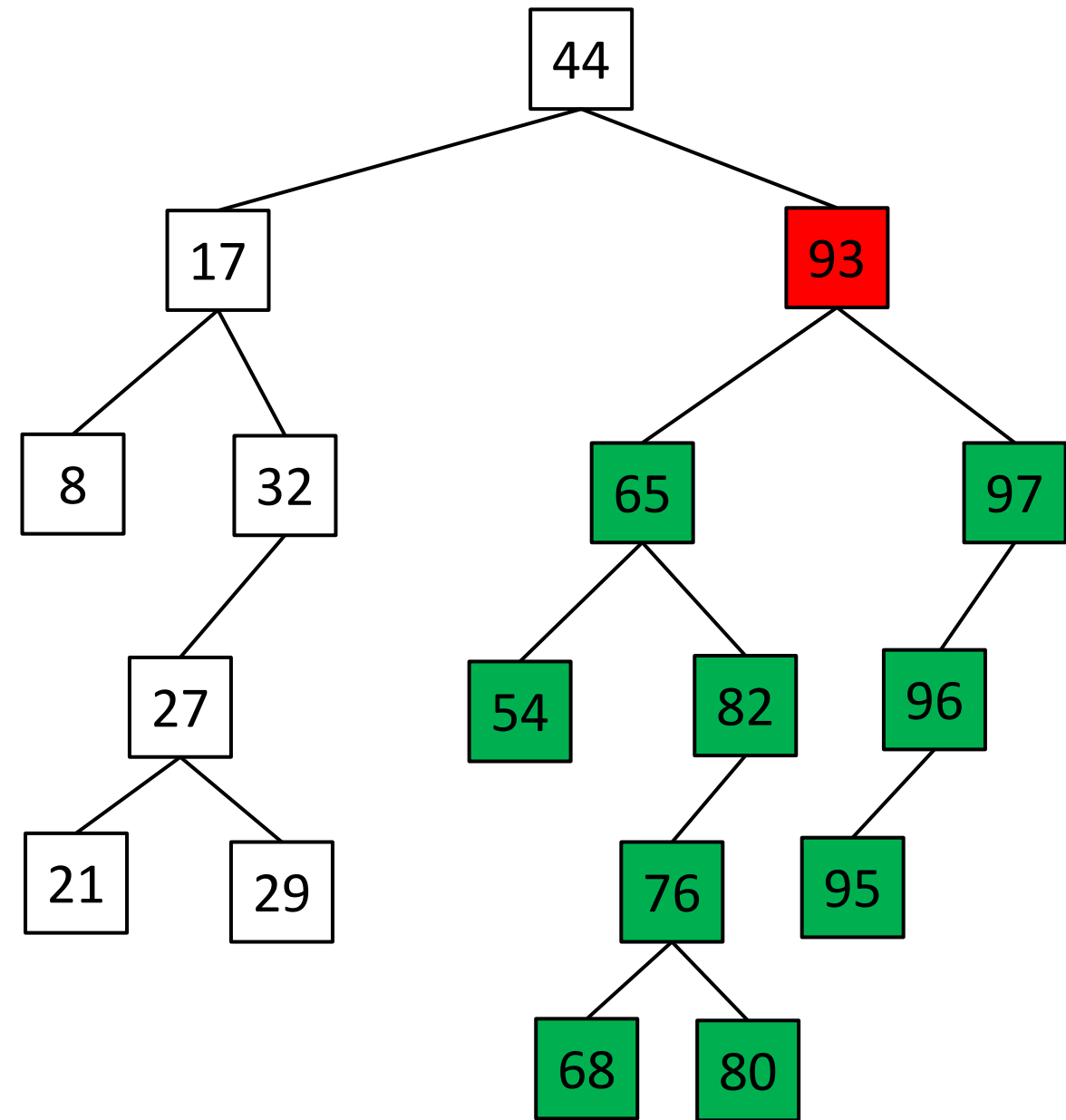
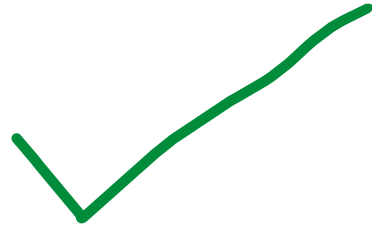
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Which ~~child~~ **descendant** to use?



Binary Search Tree- Removal

Case 1: Node has no children

Case 2: Node has one child

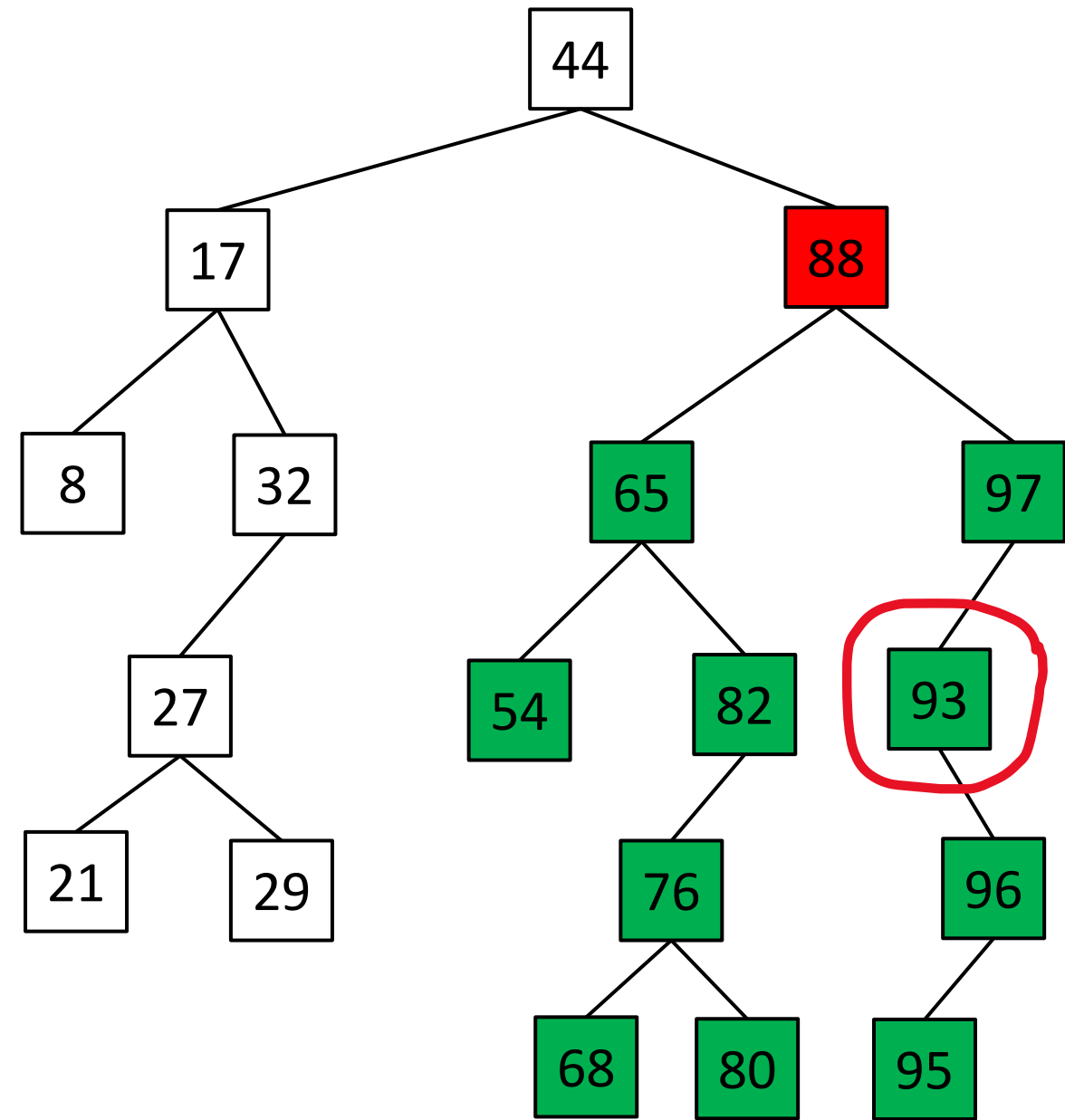
Case 3: Node has two children

`remove(88);`

Which ~~child~~ **descendant** to use?

The lowest value in the right subtree

or the highest value in the left subtree



Binary Search Tree- Removal

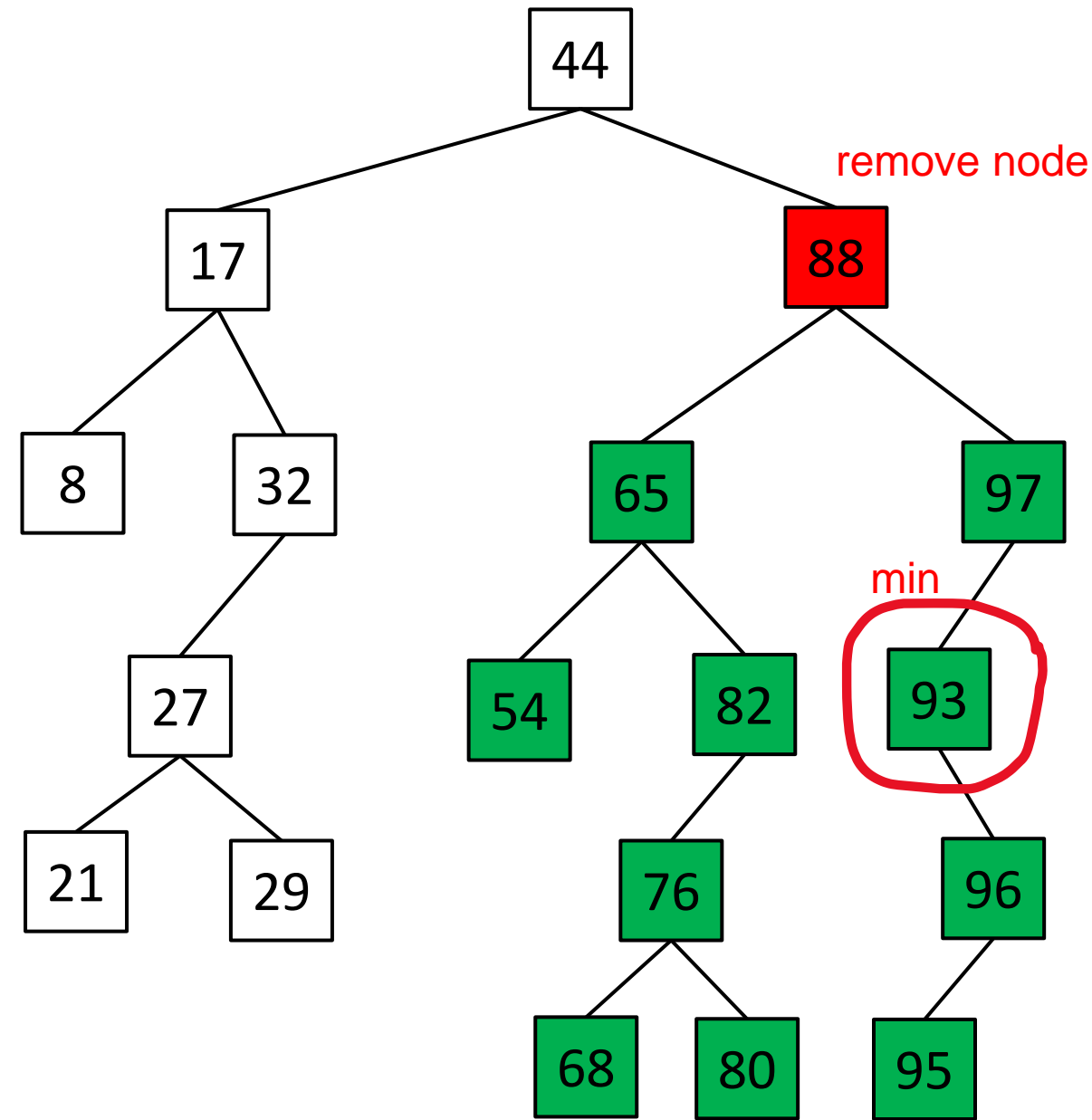
Case 1: Node has no children

Case 2: Node has one child

Case 3: Node has two children

`remove(88);`

1. Find smallest node in right sub tree (min)
2. Update the of remove node to be the value of min
3. Update the parents of min
4. Update children on remove node



Binary Search Tree- Removal

Case 1: Node has no children

Case 2: Node has one child

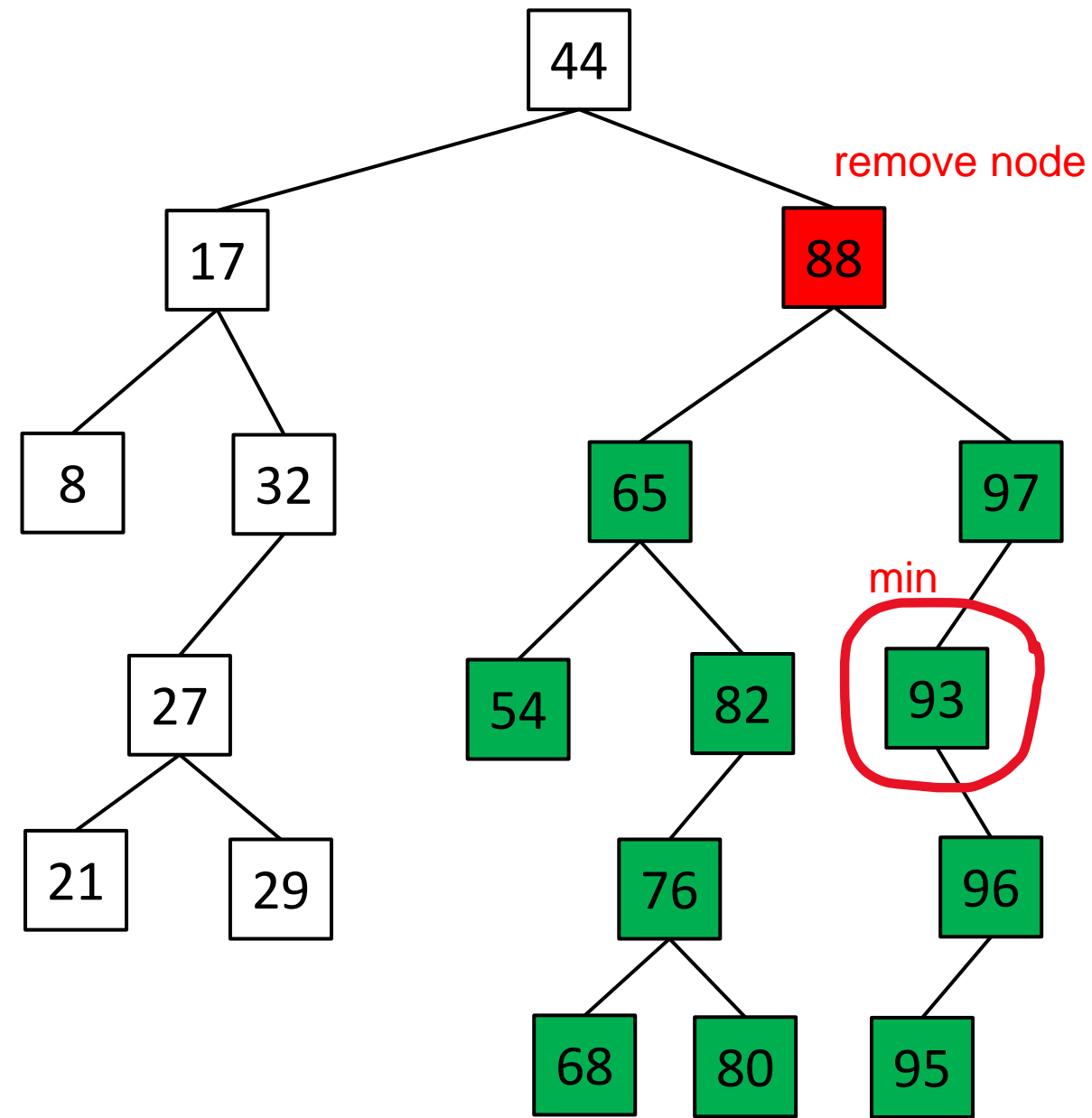
Case 3: Node has two children

`remove(88);`

Running time?

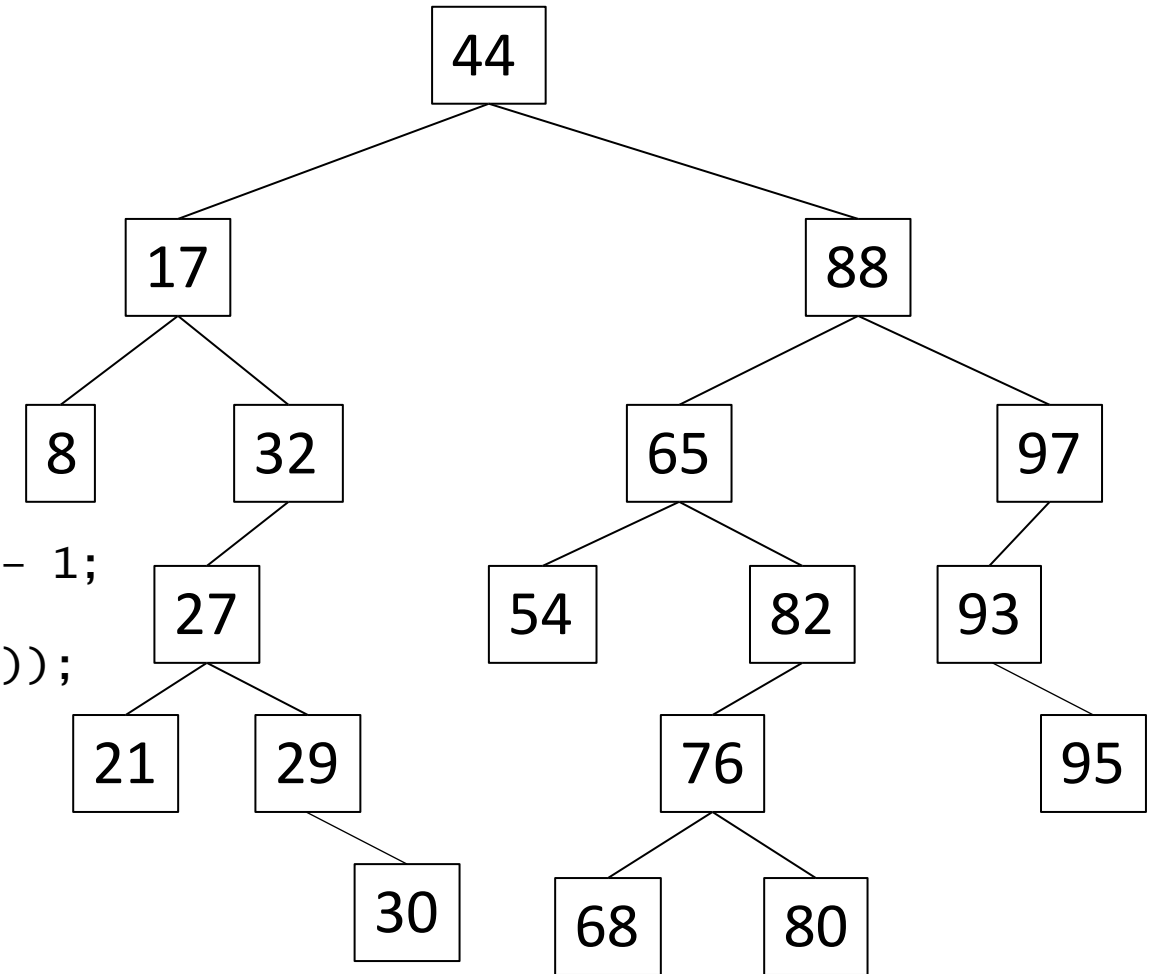
“Bad” tree $\rightarrow O(n)$
“Good” tree $\rightarrow O(\log n)$

$O(h) \rightarrow h = \text{height of tree}$



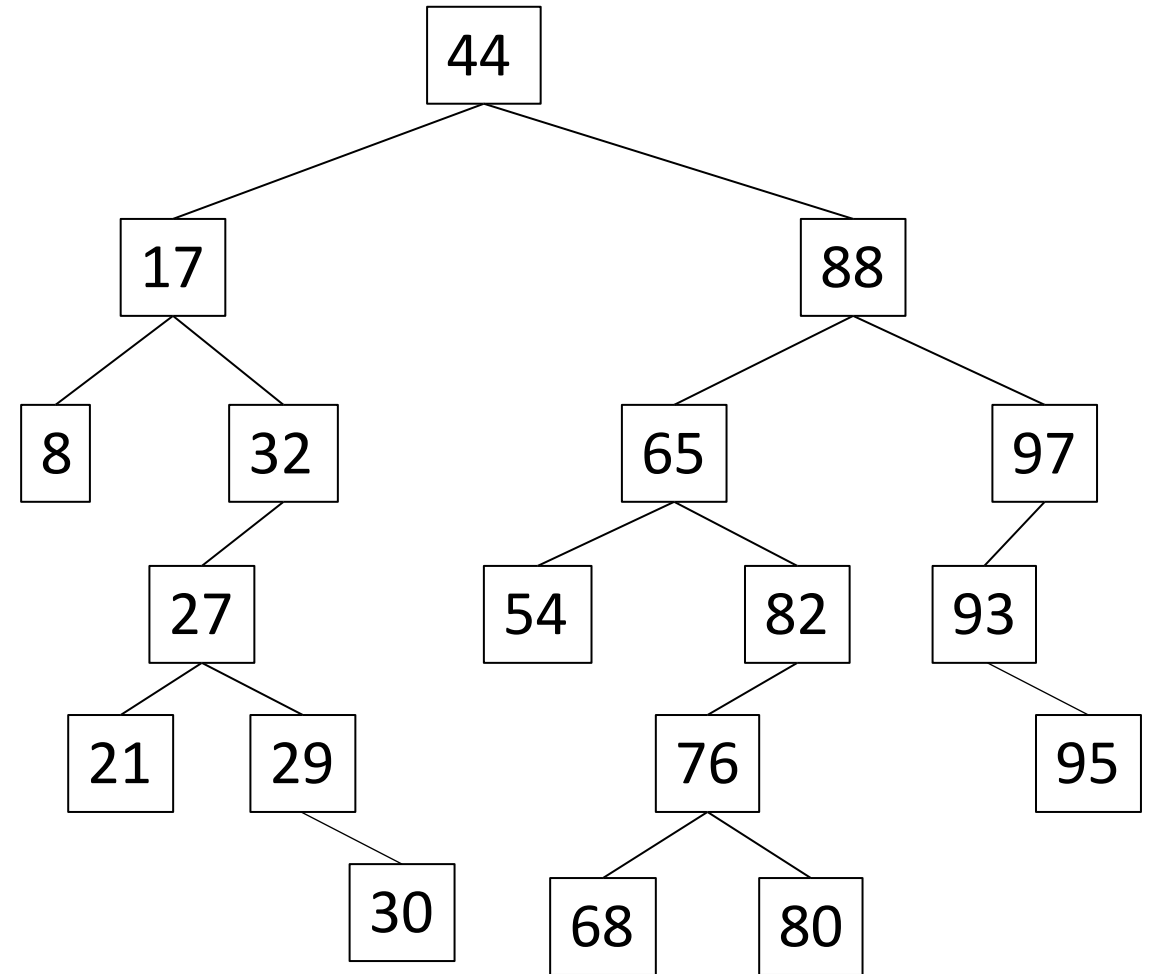
Binary Search Tree - Traversal

```
public void depthFirst() {  
    Stack<Node> stack = new Stack<>();  
    if (root != null) {  
        stack.add(root);  
        while(!stack.isEmpty()) {  
            Node node = stack.pop();  
            System.out.println(node.getName());  
            for (int i = node.getChildren().size() - 1;  
                i >= 0; i--) {  
                stack.push(node.getChildren().get(i));  
            }  
        }  
    }  
}
```



Binary Search Tree - Traversal

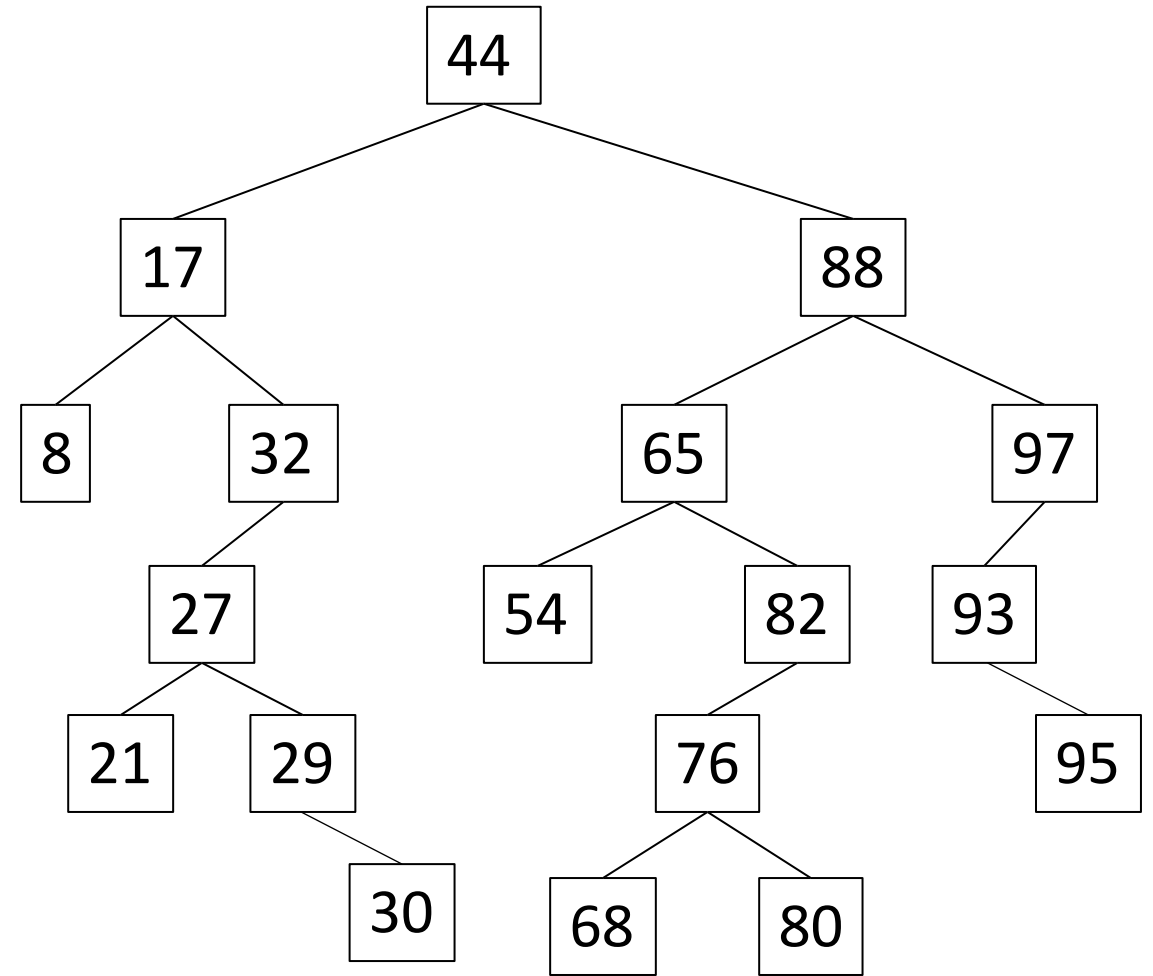
Recursion:



Binary Search Tree - Traversal

Recursion:

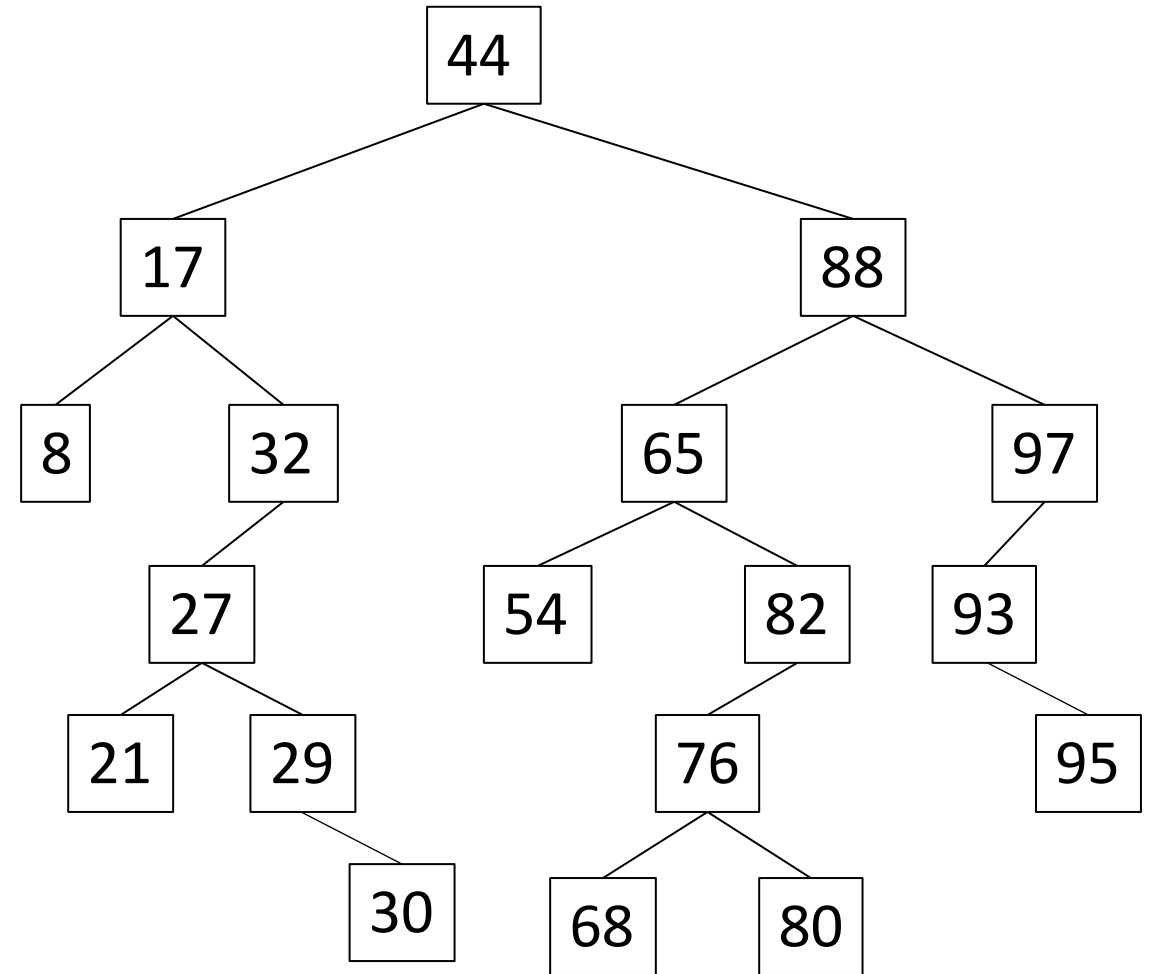
- Calling a method from inside itself.



Binary Search Tree - Traversal

Recursion:

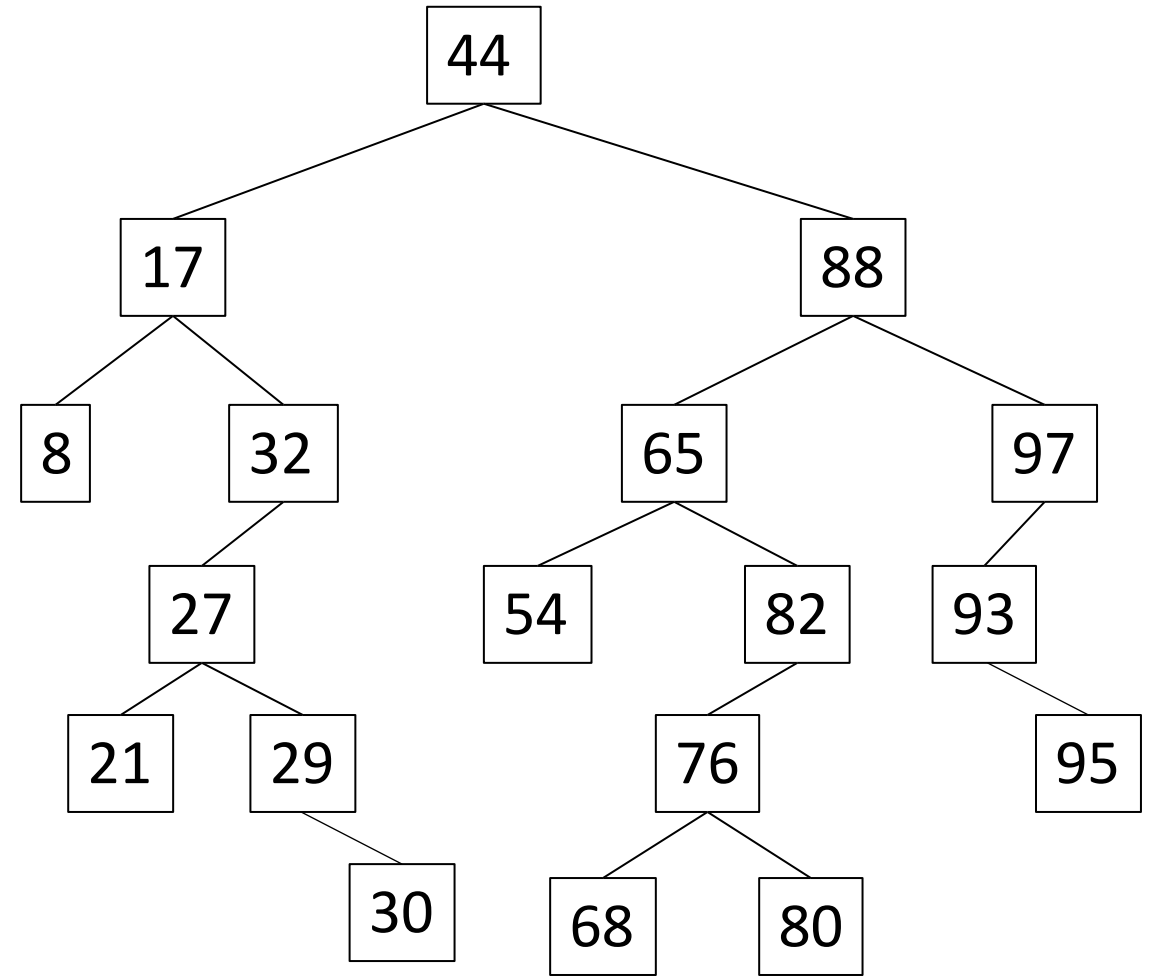
- Calling a method from inside itself.
- Solve the problem by solving identical smaller problems.



Binary Search Tree - Traversal

Recursion:

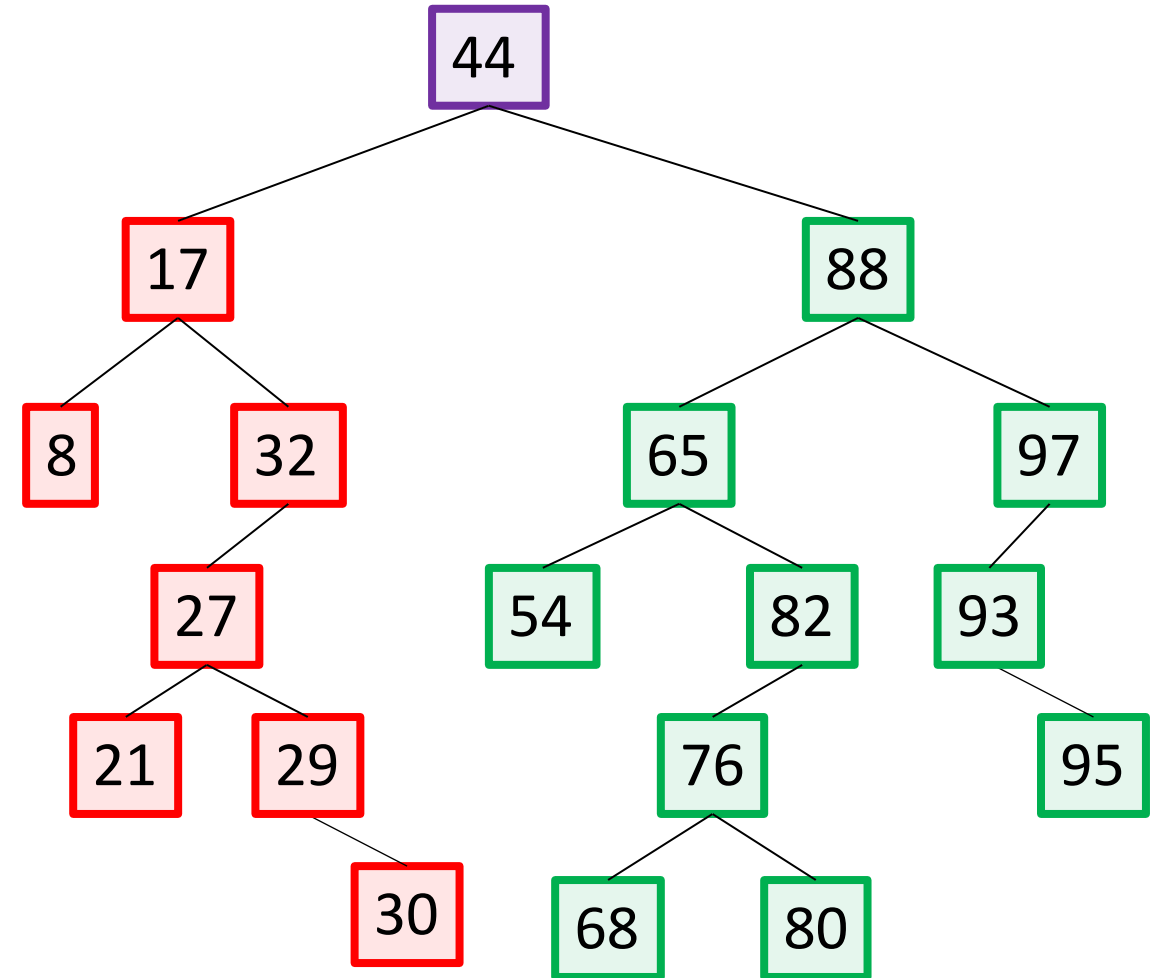
- Calling a method from inside itself.
- Solve the problem by solving identical smaller problems.
- What is the “smaller problem”?



Binary Search Tree - Traversal

Recursion:

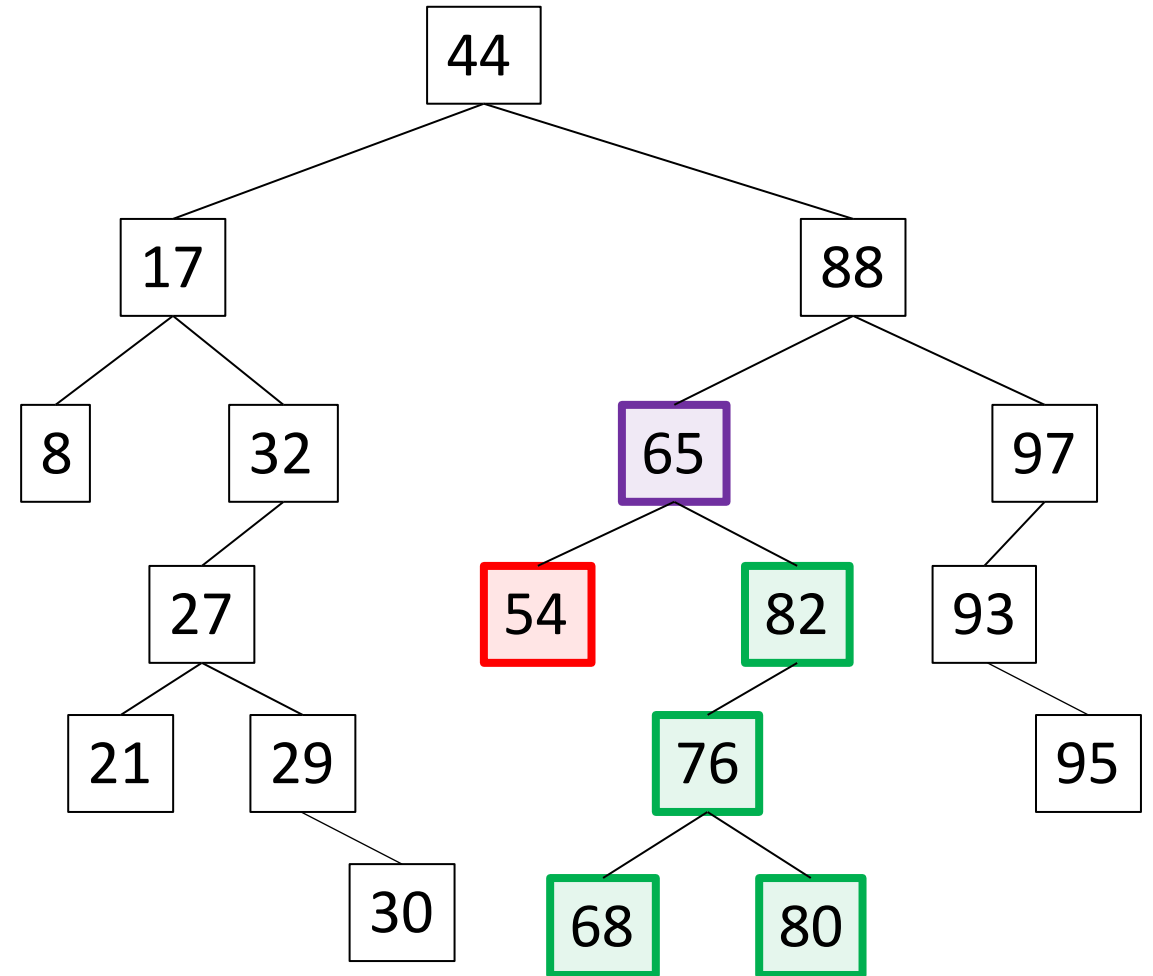
- Calling a method from inside itself.
- Solve the problem by solving identical smaller problems.
- What is the “smaller problem”?
 - Process the **left side**, then process the **right side**.



Binary Search Tree - Traversal

Recursion:

- Calling a method from inside itself.
- Solve the problem by solving identical smaller problems.
- What is the “smaller problem”?
 - Process the **left side**, then process the **right side**.

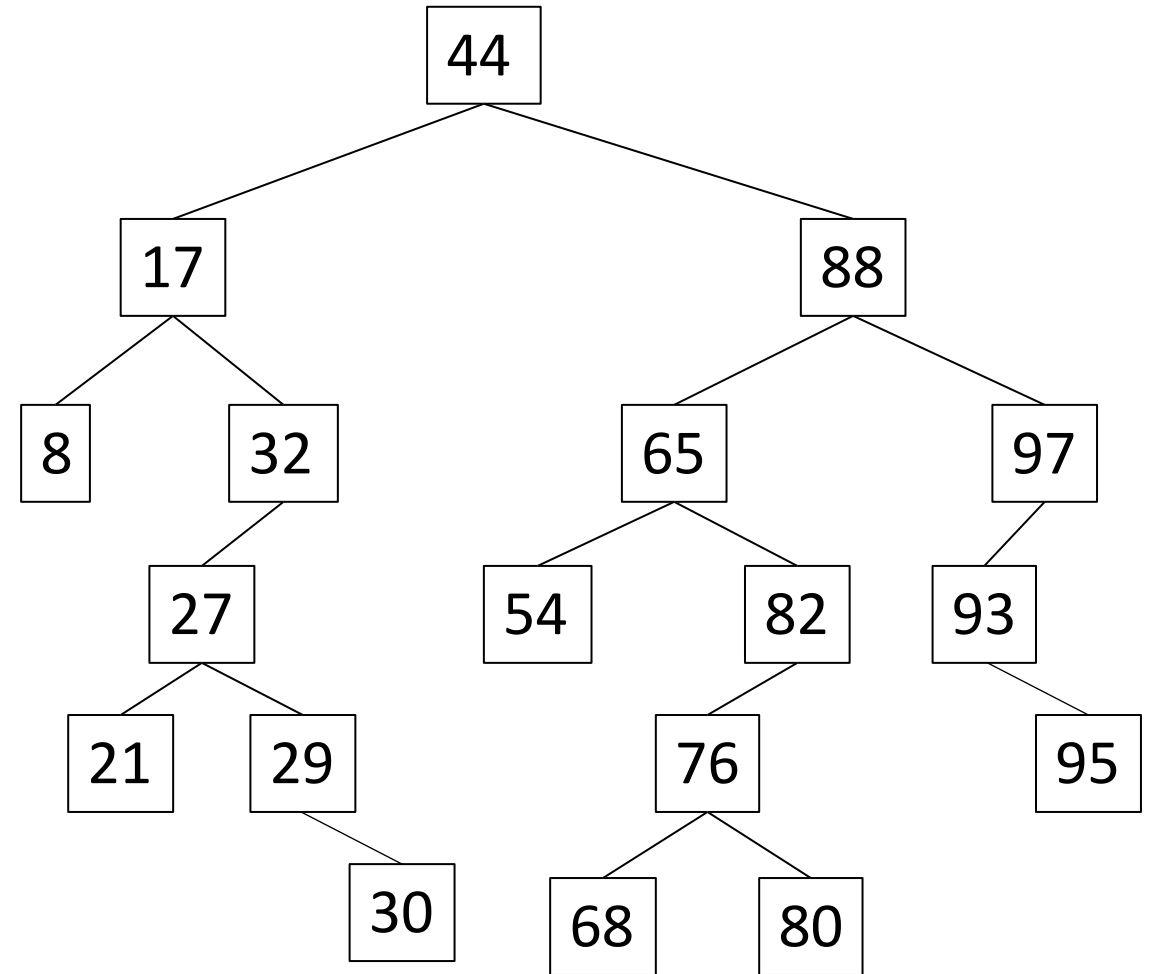


Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

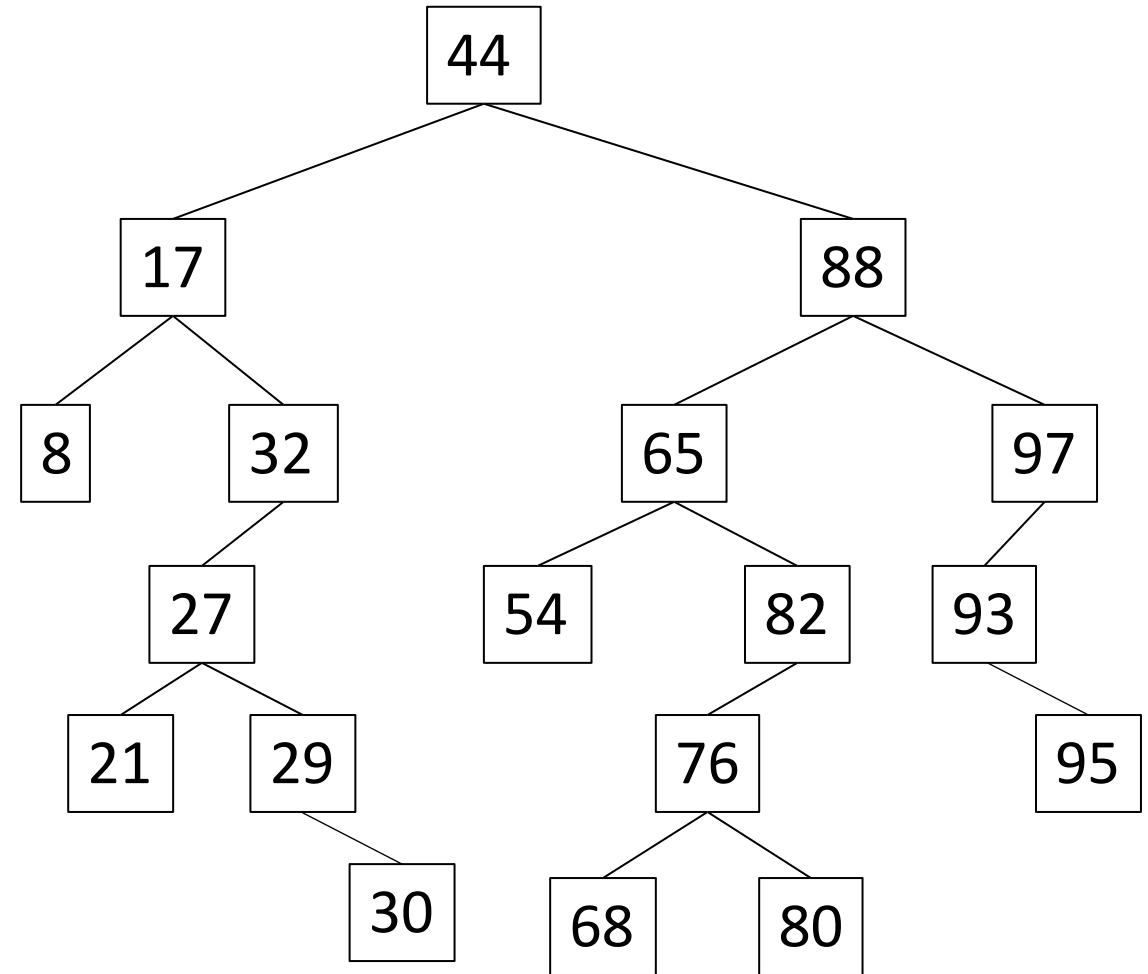
Recursion:

- Calling a method from inside itself.
- Solve the problem by solving identical smaller problems.
- What is the “smaller problem”?
 - Process the left side, then process the right side.



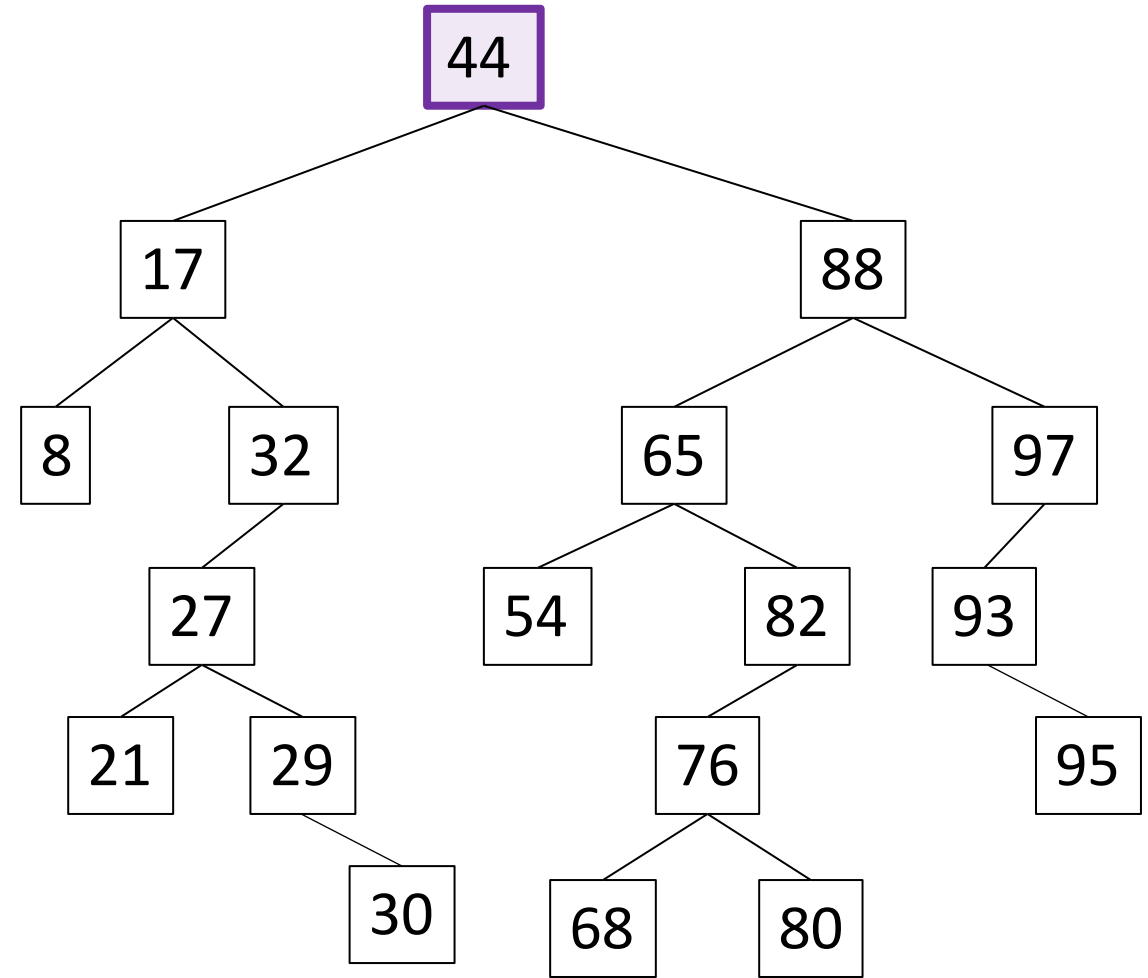
Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```



Binary Search Tree - Traversal

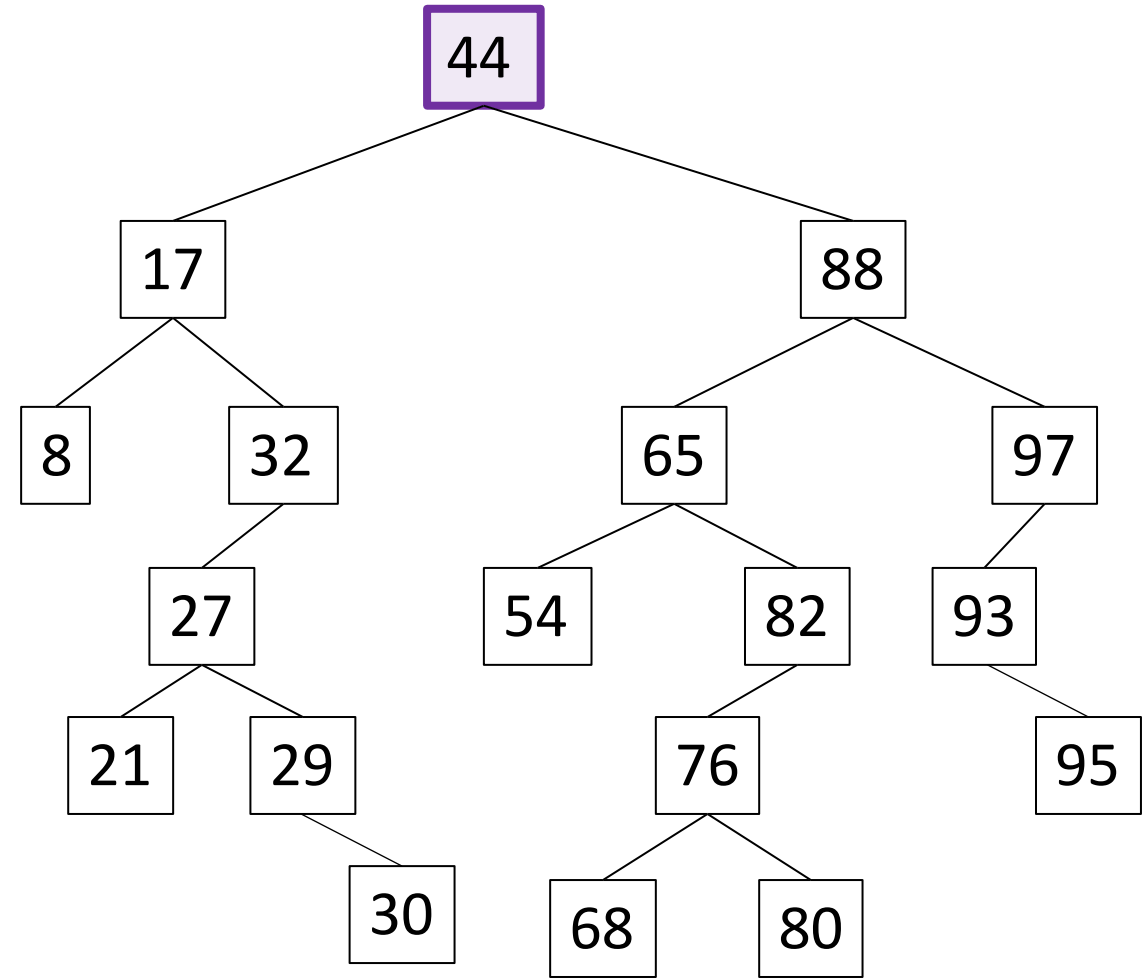
```
public void depthFirst(44) {  
    if (n != null) {  
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        depthFirst(n.getRight());  
    }  
}
```



Output:
44

Binary Search Tree - Traversal

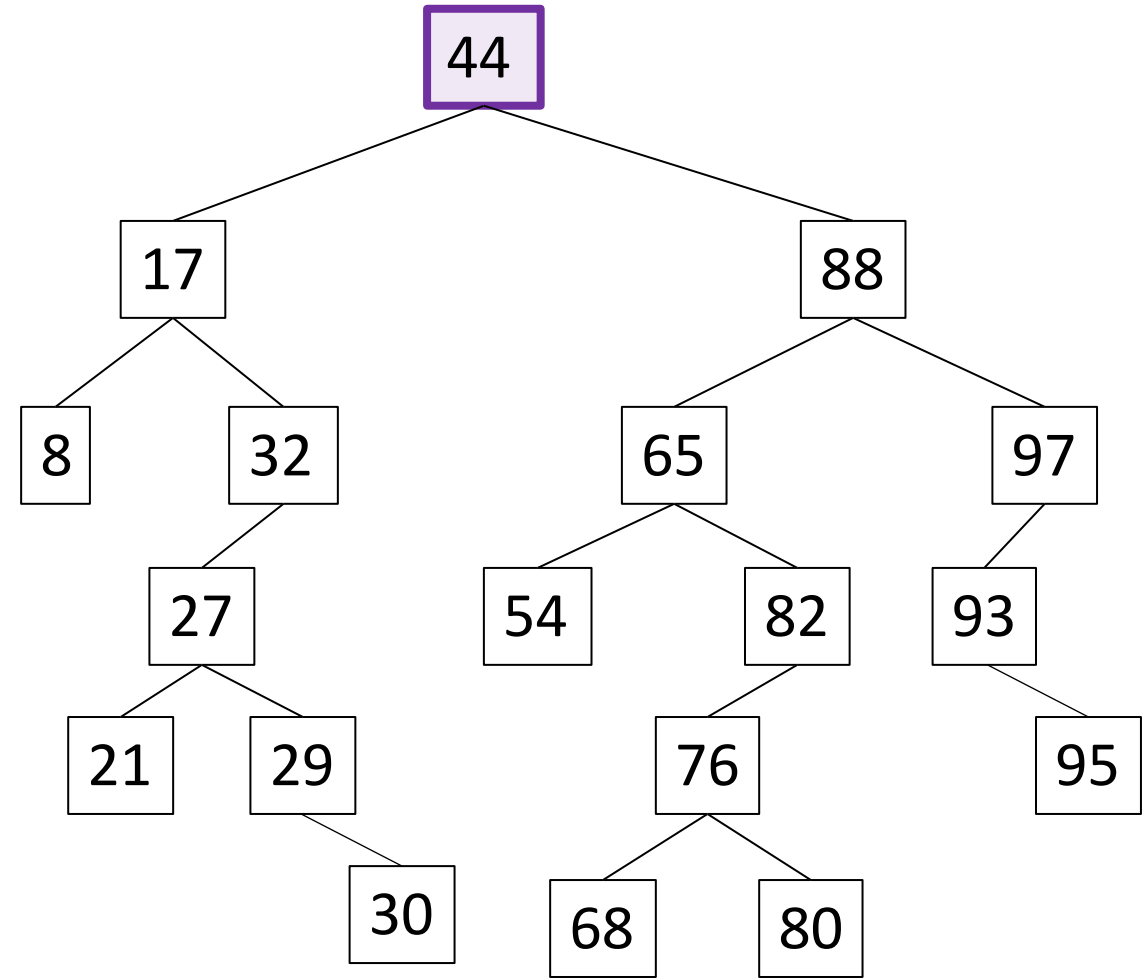
```
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        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```



Output:
44

Binary Search Tree - Traversal

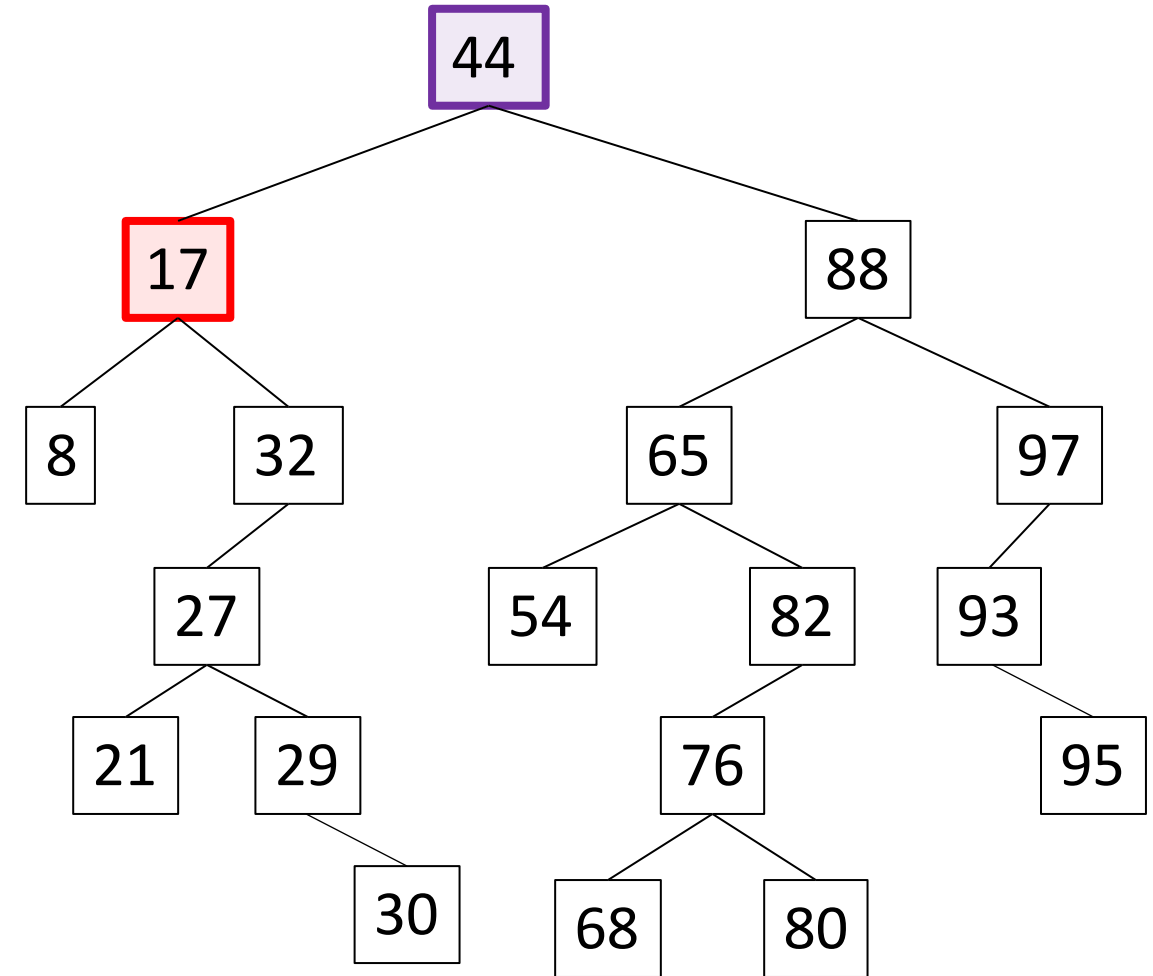
```
public void depthFirst(44) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```



Binary Search Tree - Traversal

```
public void depthFirst(44) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

```
public void depthFirst(17) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
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    }  
}
```

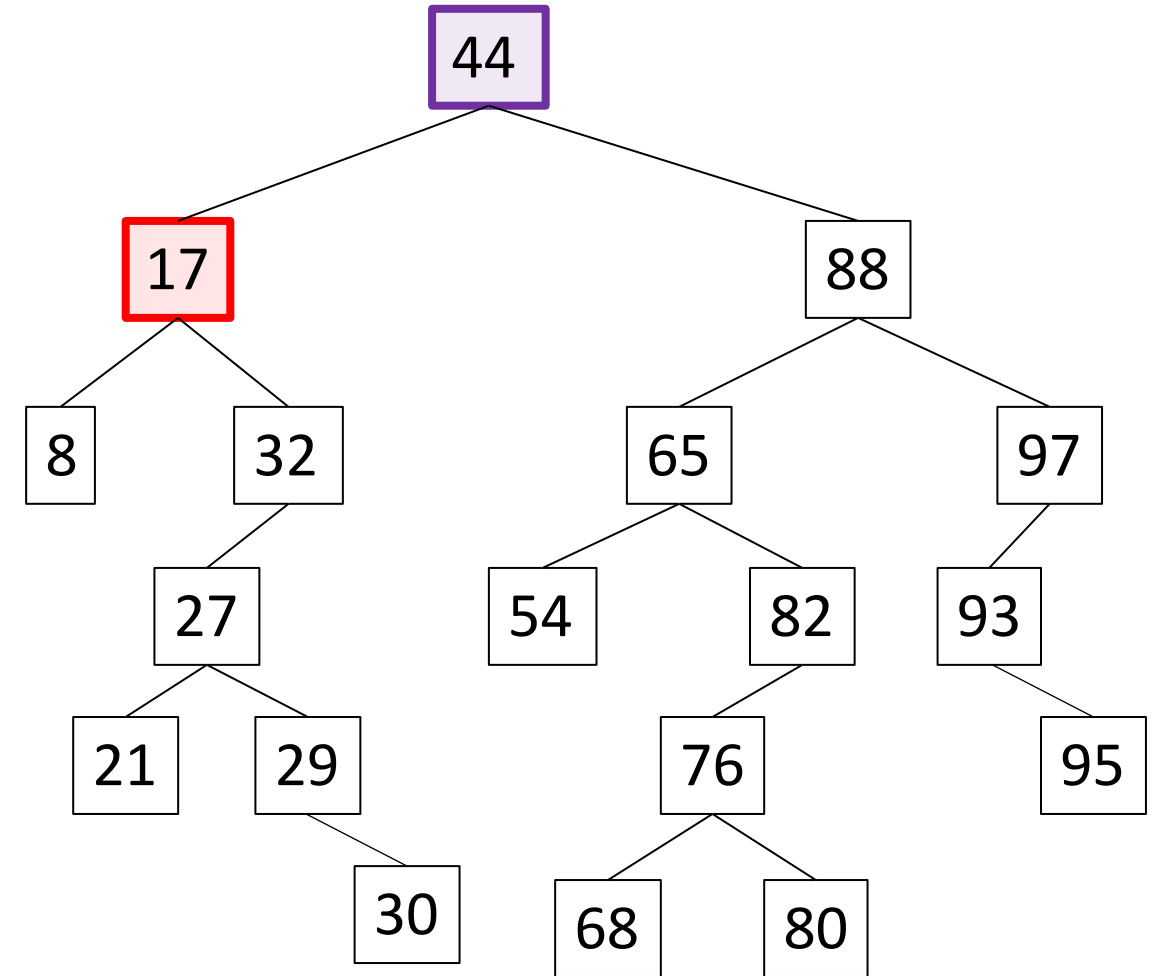


Output:
44
17

Binary Search Tree - Traversal

```
public void depthFirst(44) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

```
public void depthFirst(17) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

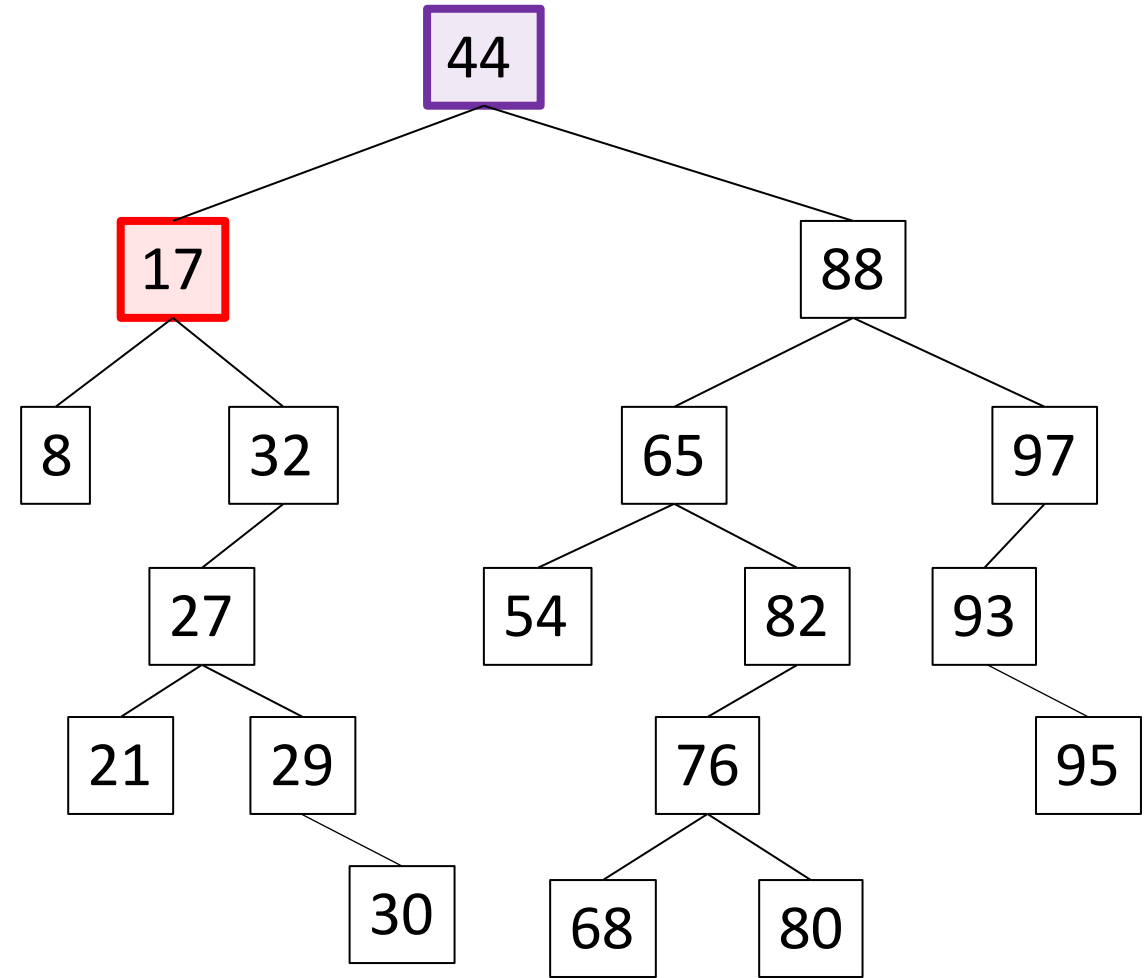


Output:
44
17

Binary Search Tree - Traversal

```
public void depthFirst(44) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
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    }  
}
```

```
public void depthFirst(17) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```



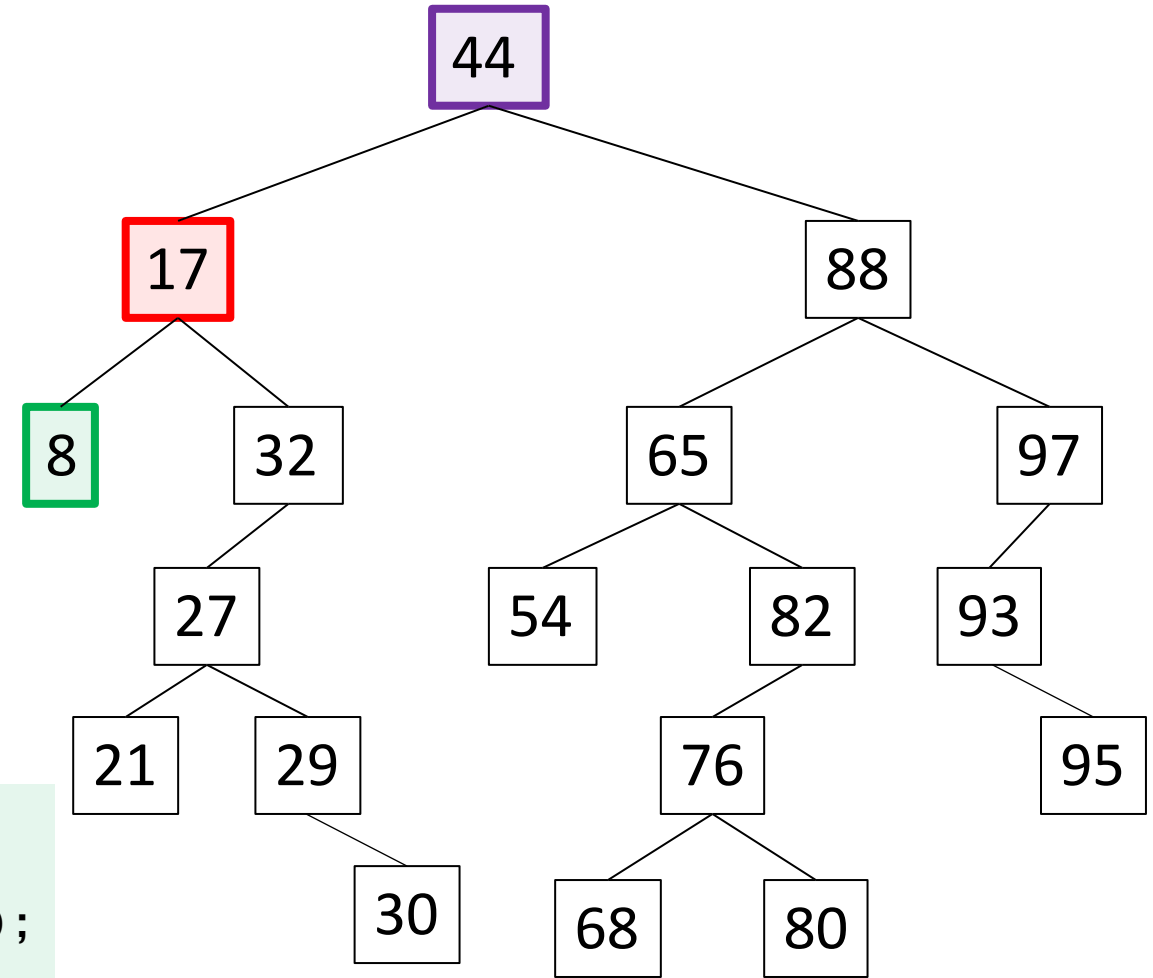
Output:
44
17

Binary Search Tree - Traversal

```
public void depthFirst(44) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

```
public void depthFirst(17) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

```
public void depthFirst(8) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```



Binary Search Tree - Traversal

Output:

44

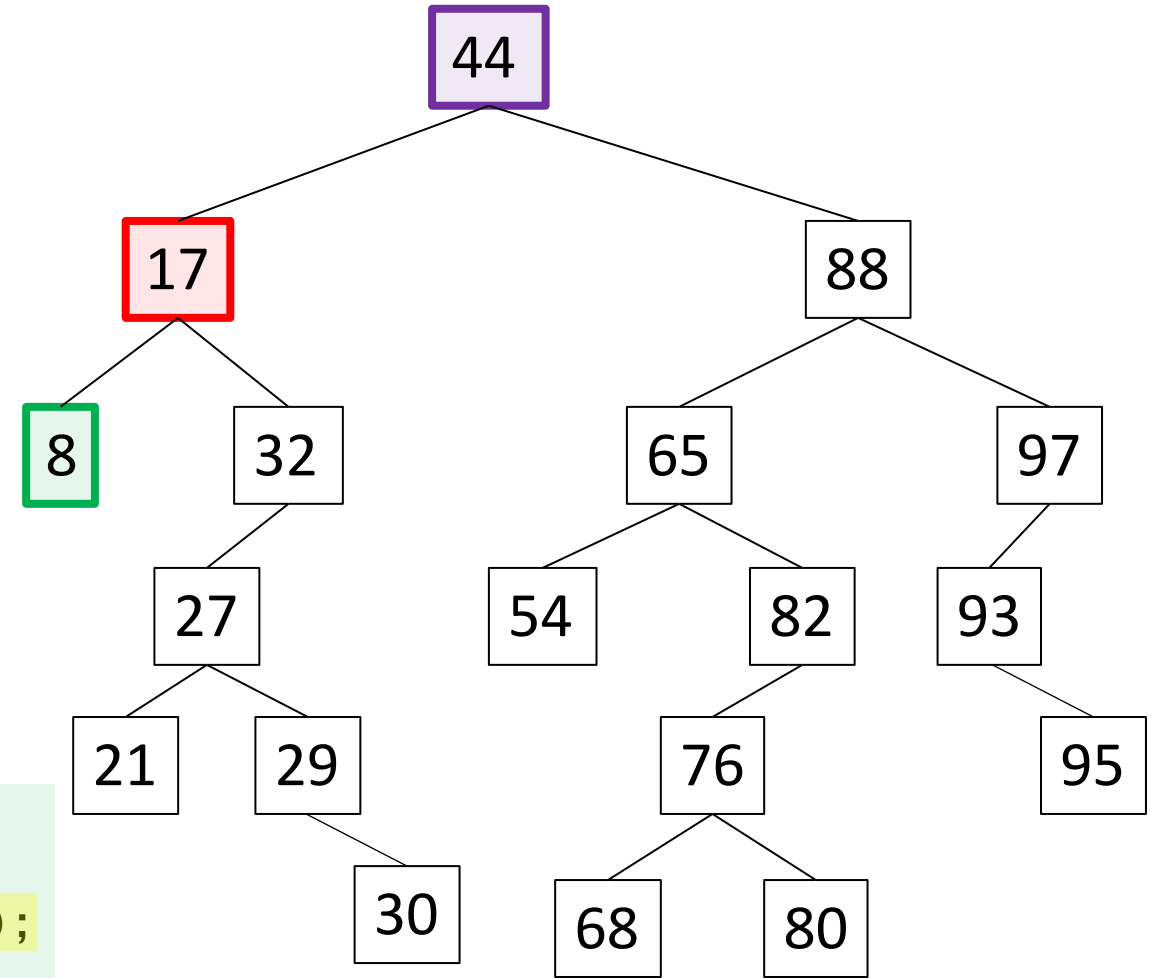
17

8

```
public void depthFirst(44) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
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    }  
}
```

```
public void depthFirst(17) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

```
public void depthFirst(8) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```



Output:

44

17

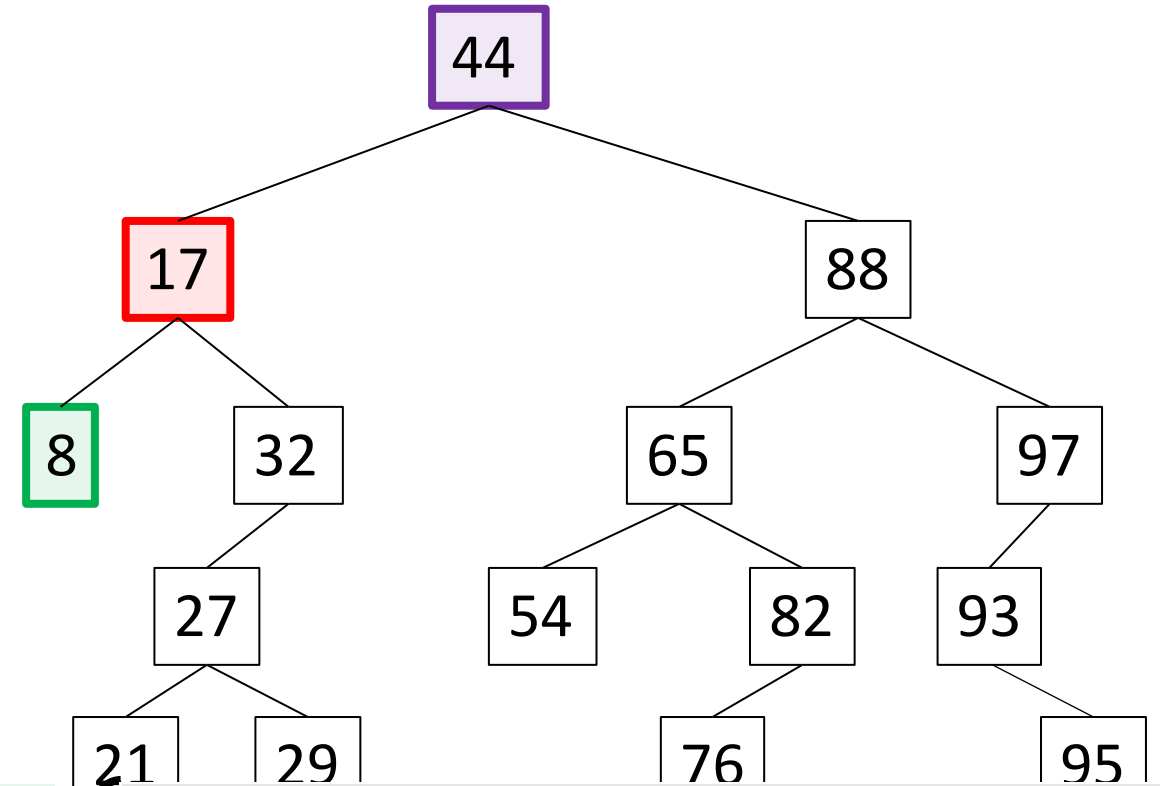
8

Binary Search Tree - Traversal

```
public void depthFirst(44) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

```
public void depthFirst(17) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
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    }  
}
```

```
public void depthFirst(8) {  
    if (n != null) {  
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        depthFirst(n.getRight());  
    }  
}
```



```
public void depthFirst(null) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```


Output:

44

17

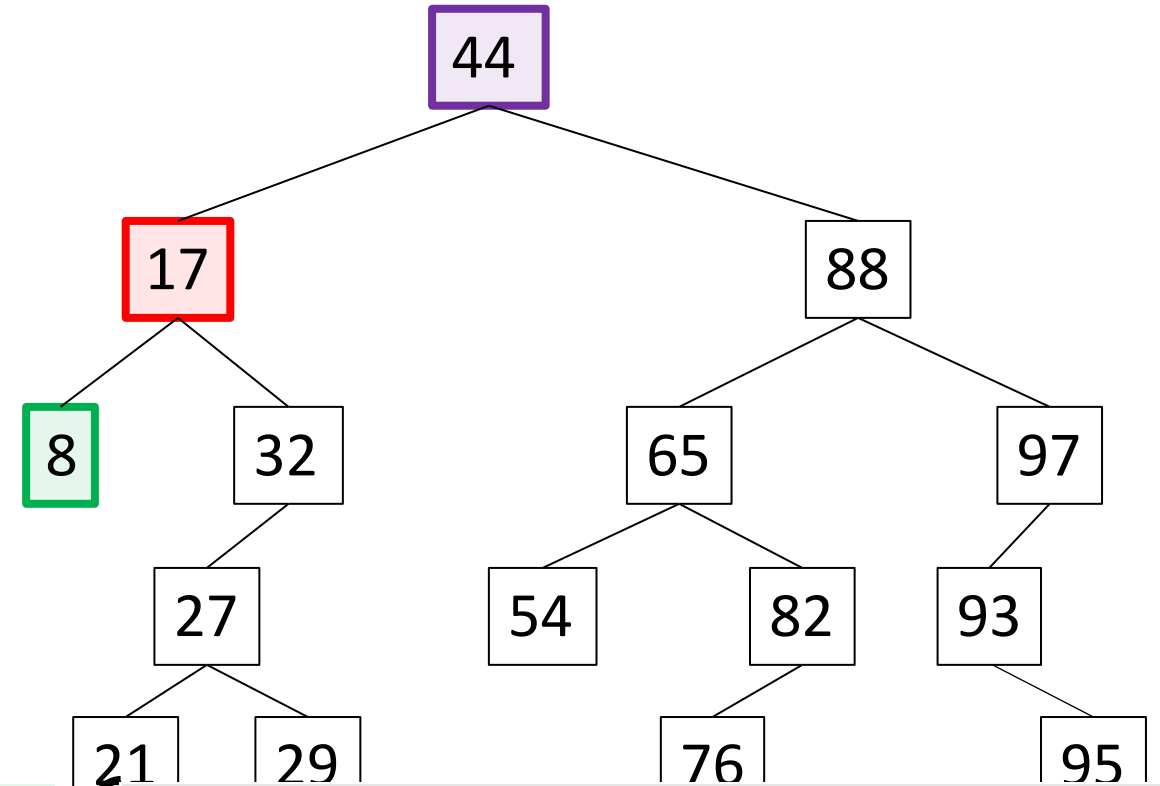
8

Binary Search Tree - Traversal

```
public void depthFirst(44) {  
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    if (n != null) {  
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```
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    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

Output:

44

17

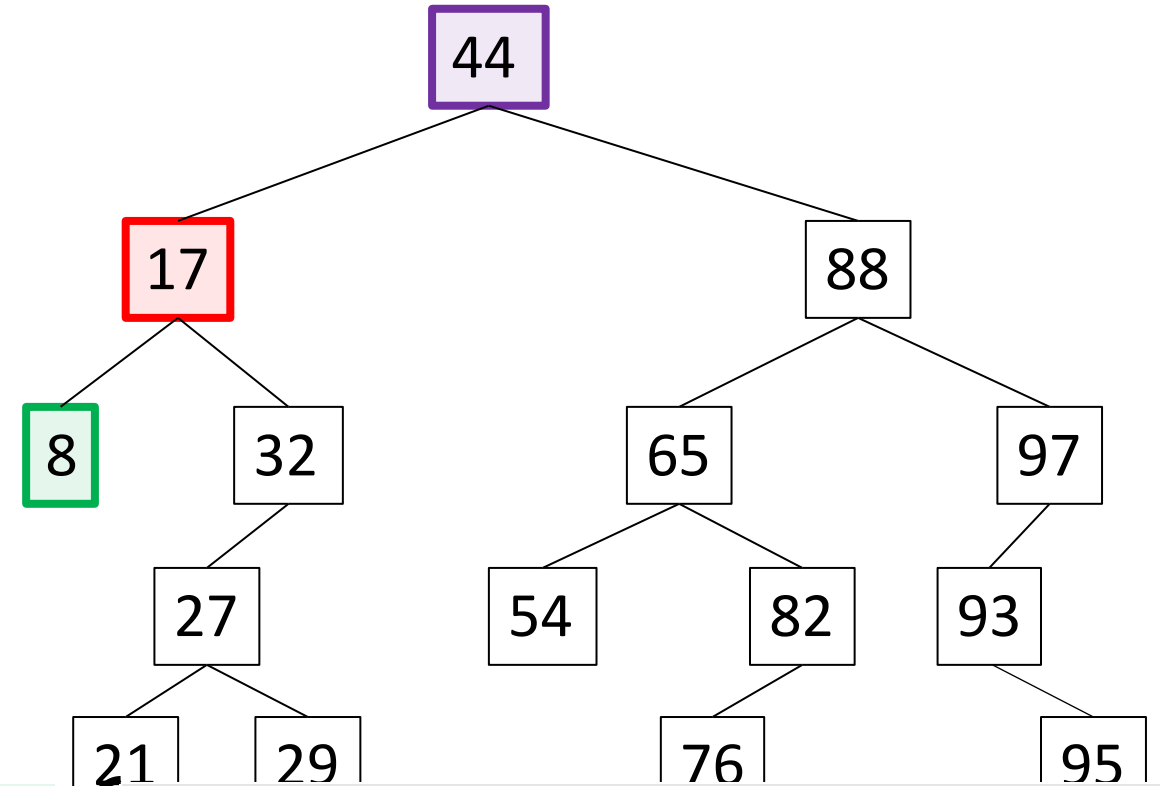
8

Binary Search Tree - Traversal

```
public void depthFirst(44) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

```
public void depthFirst(17) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

```
public void depthFirst(8) {  
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    }  
}
```

Binary Search Tree - Traversal

Output:

44

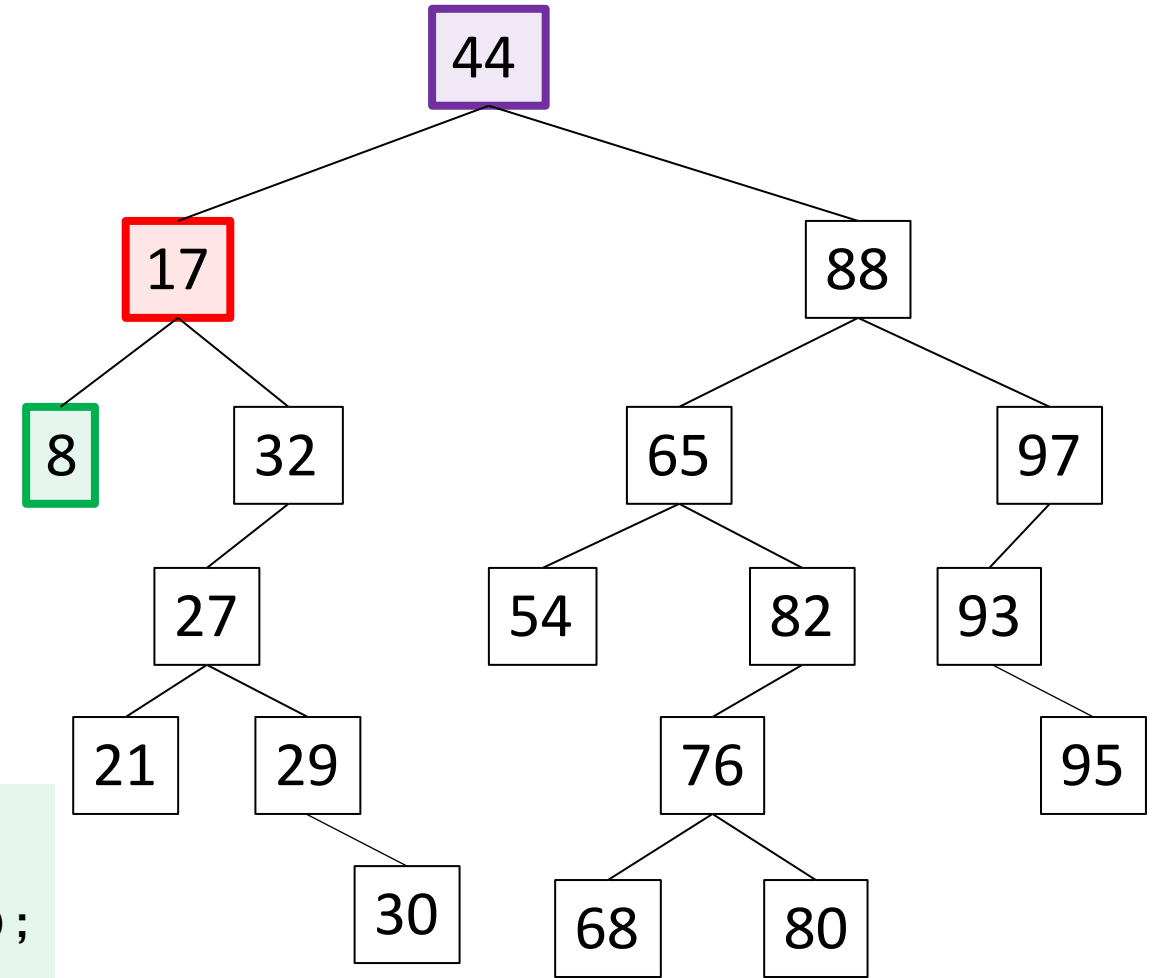
17

8

```
public void depthFirst(44) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
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```
public void depthFirst(8) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```



Output:

44

17

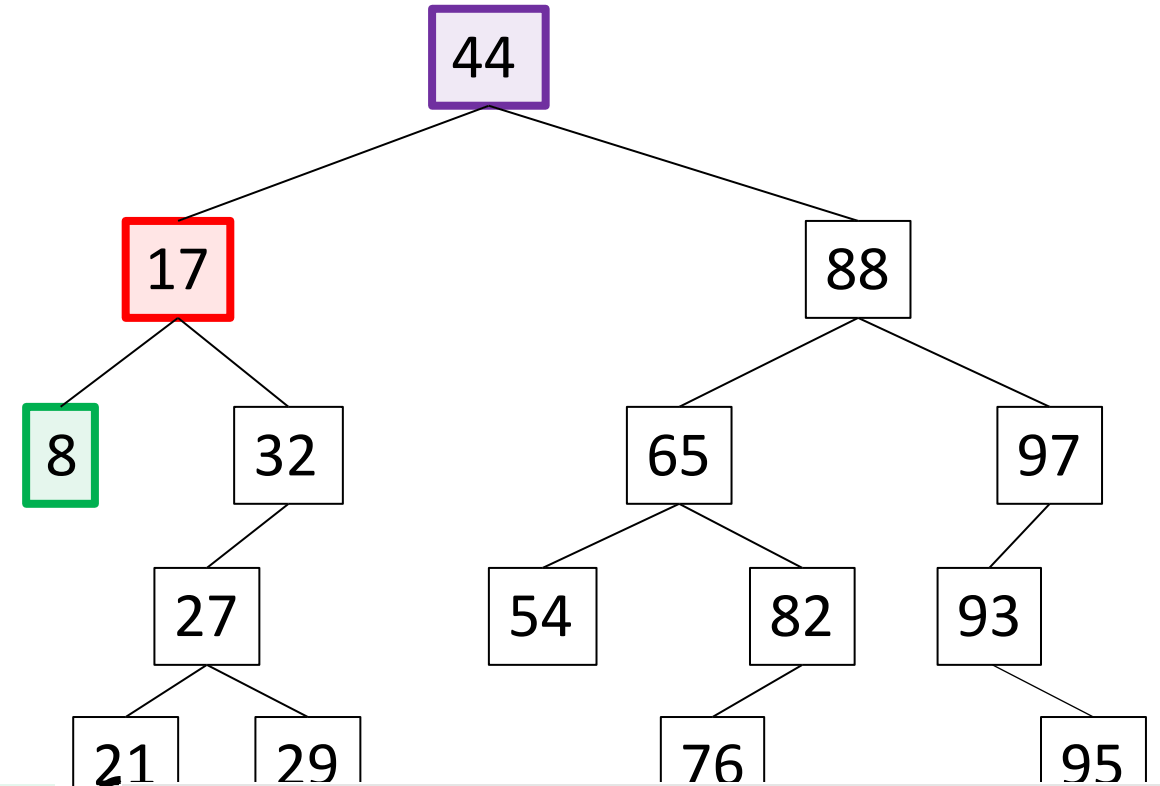
8

Binary Search Tree - Traversal

```
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        depthFirst(n.getRight());  
    }  
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```

```
public void depthFirst(17) {  
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        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

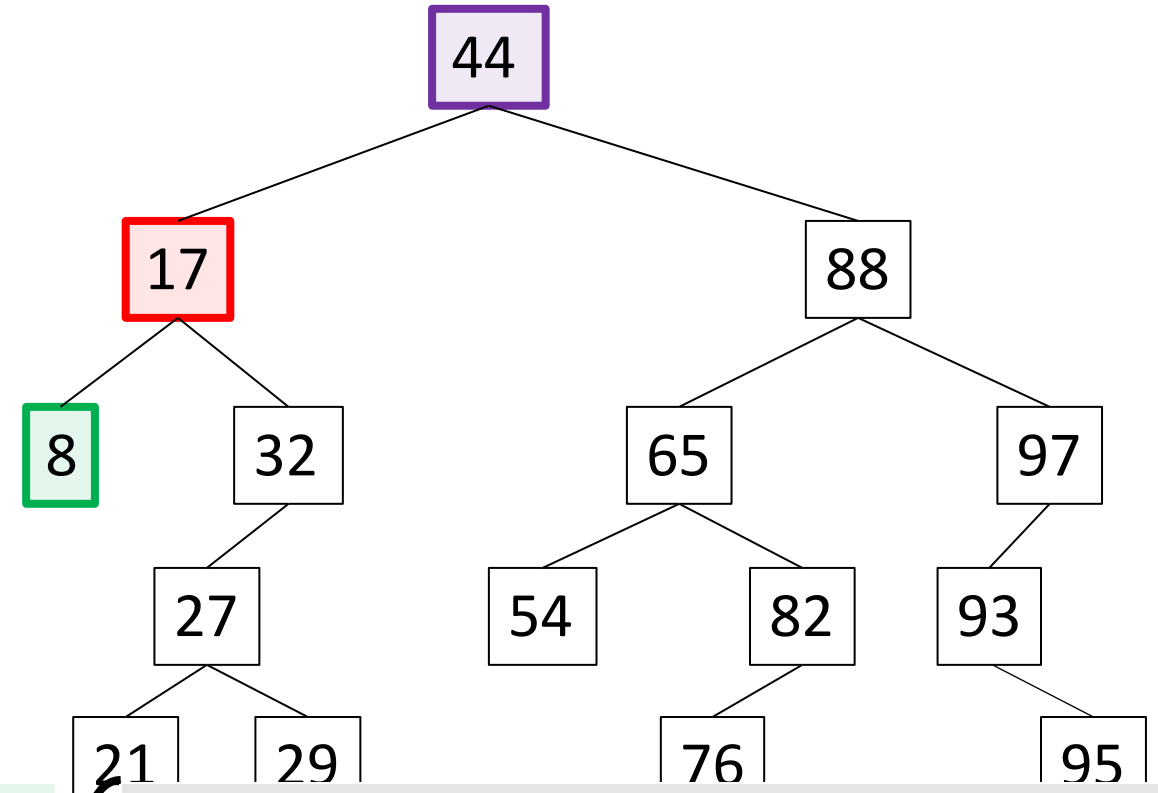
```
public void depthFirst(8) {  
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```
public void depthFirst(null) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
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    }  
}
```

44
17
8

```
public void depthFirst(null) {
    if (n != null) {
        System.out.println(n.getValue());
        depthFirst(n.getLeft());
        depthFirst(n.getRight());
    }
}
```



Output:

44

17

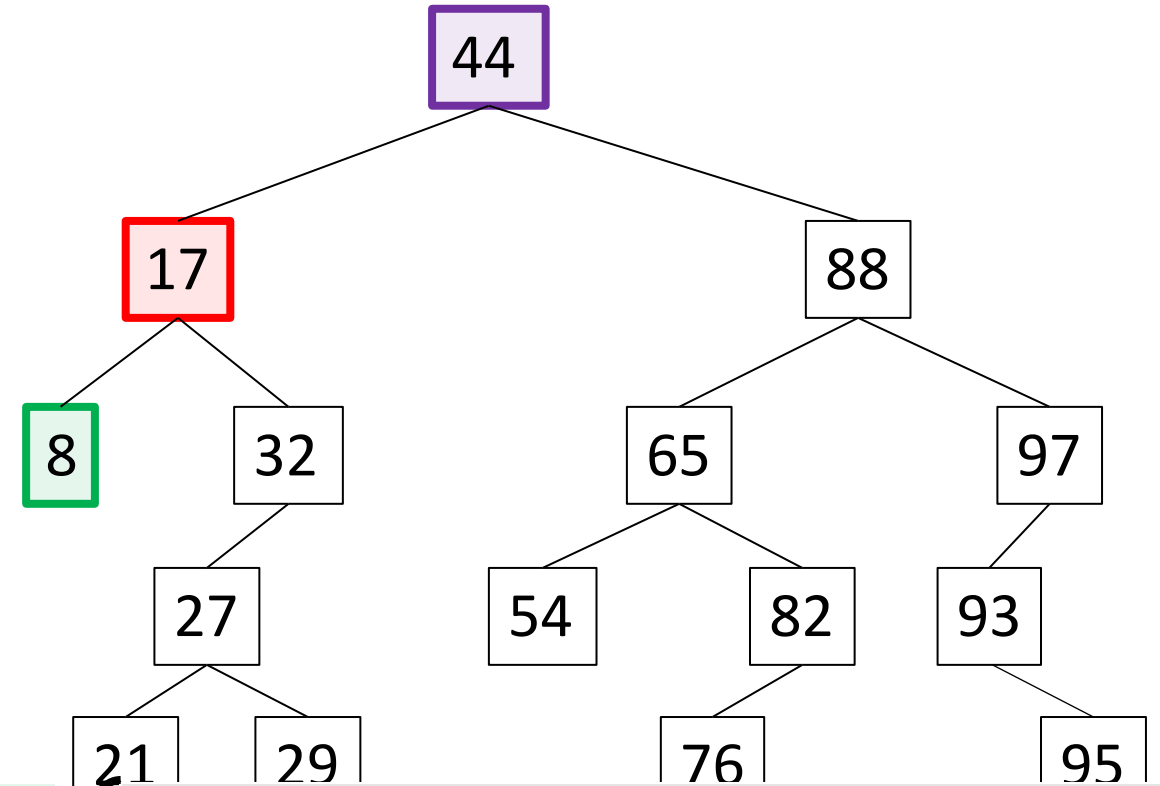
8

Binary Search Tree - Traversal

```
public void depthFirst(44) {  
    if (n != null) {  
        System.out.println(n.getValue());  
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```



```
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    if (n != null) {  
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        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

Binary Search Tree - Traversal

Output:

44

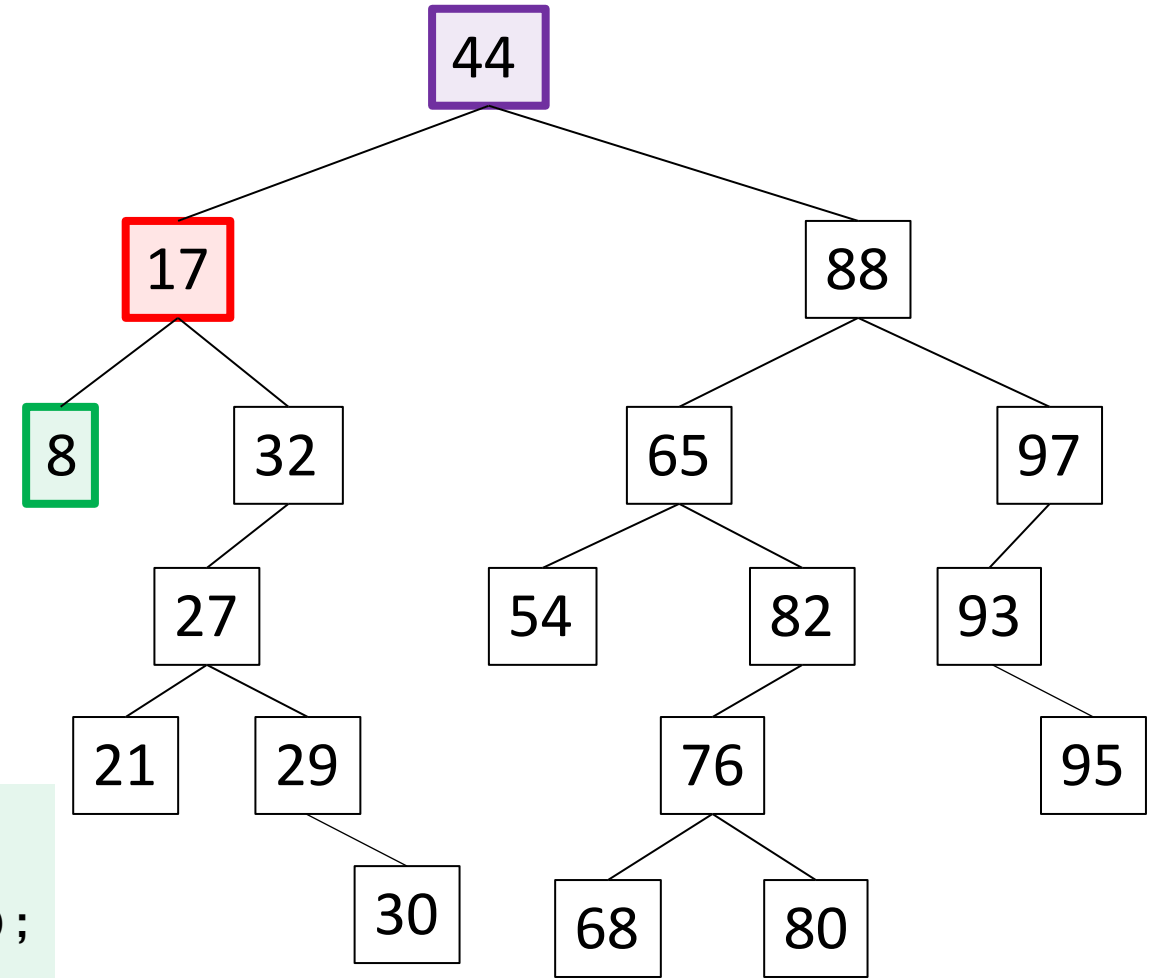
17

8

```
public void depthFirst(44) {  
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}
```

```
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    if (n != null) {  
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    }  
}
```

```
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    if (n != null) {  
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    }  
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```



Binary Search Tree - Traversal

Output:

44

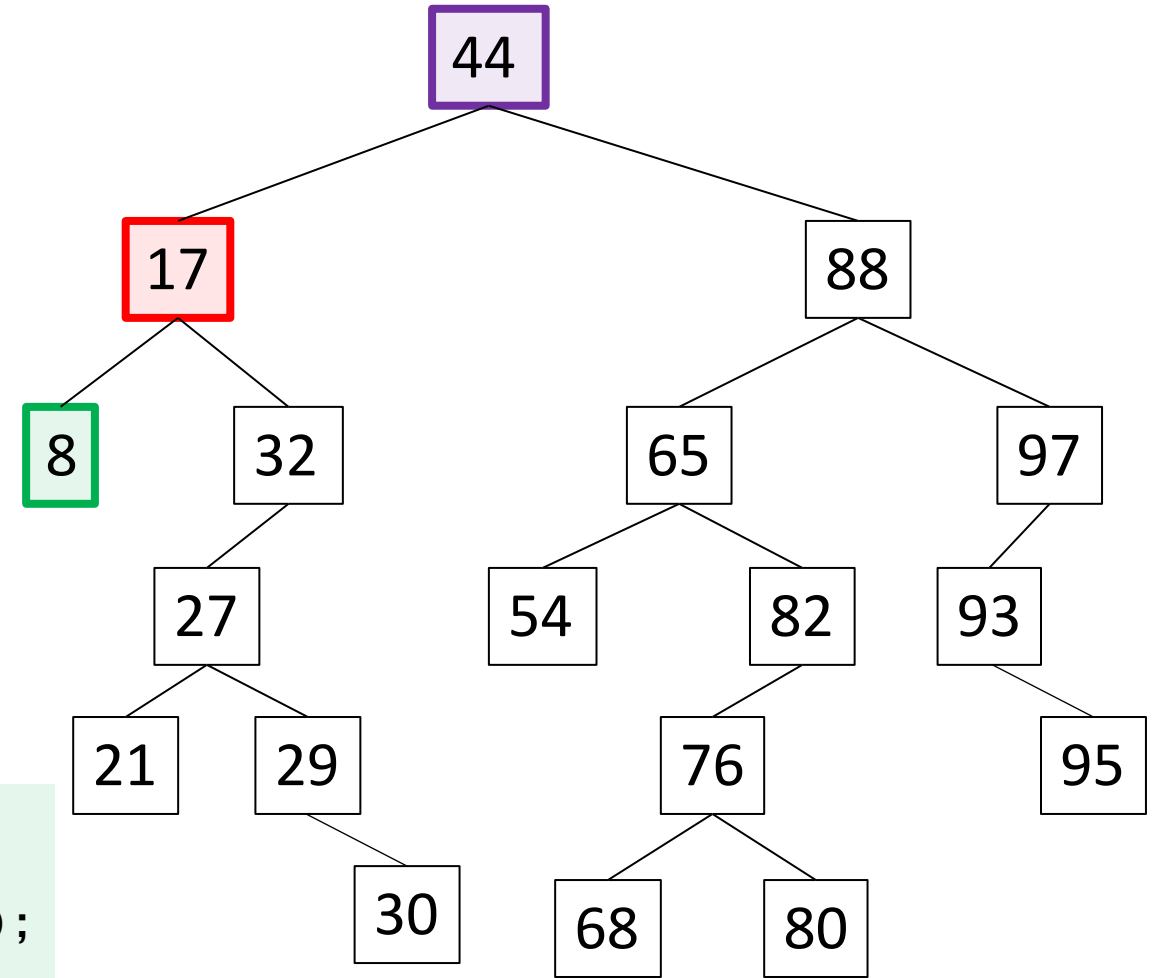
17

8

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```



Binary Search Tree - Traversal

Output:

44

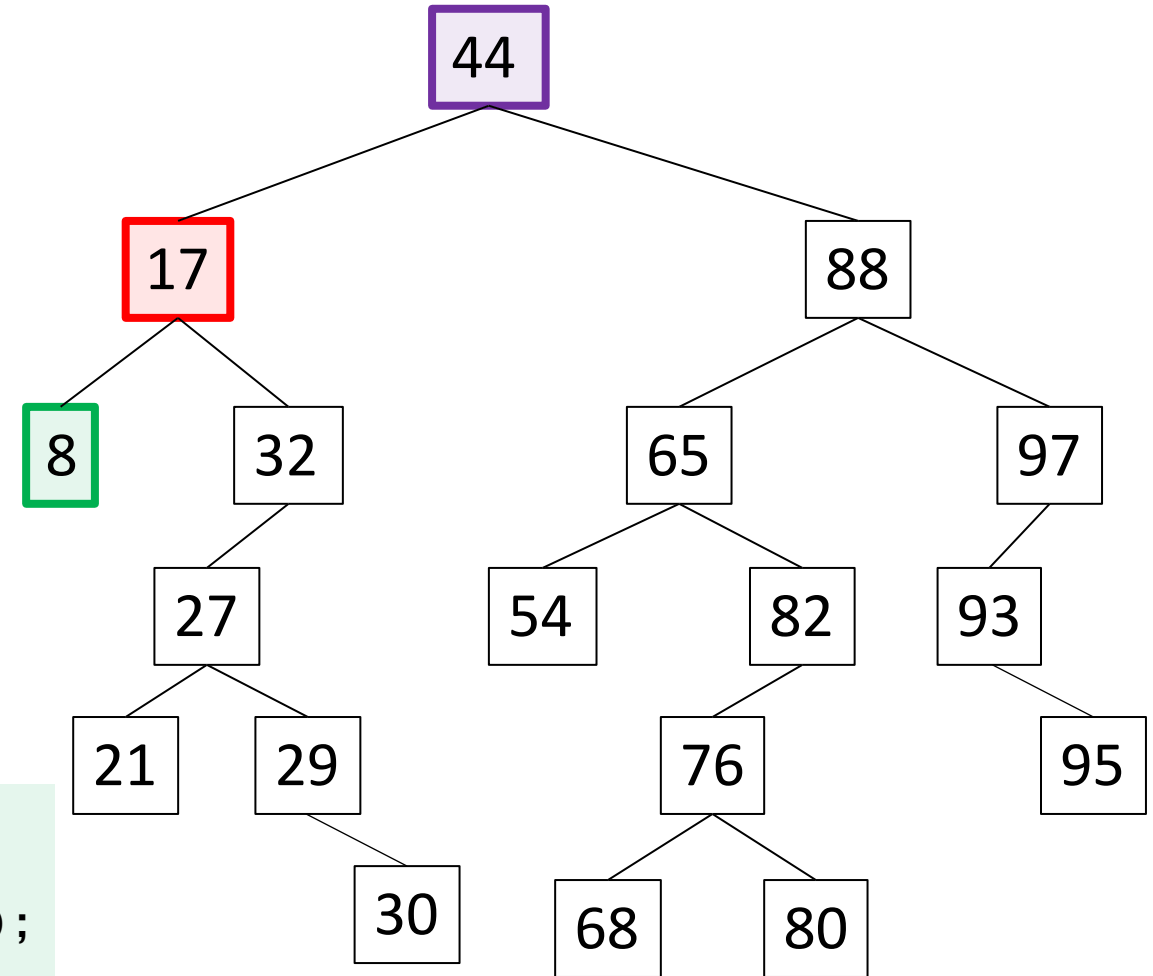
17

8

```
public void depthFirst(44) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
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    if (n != null) {  
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    }  
}
```

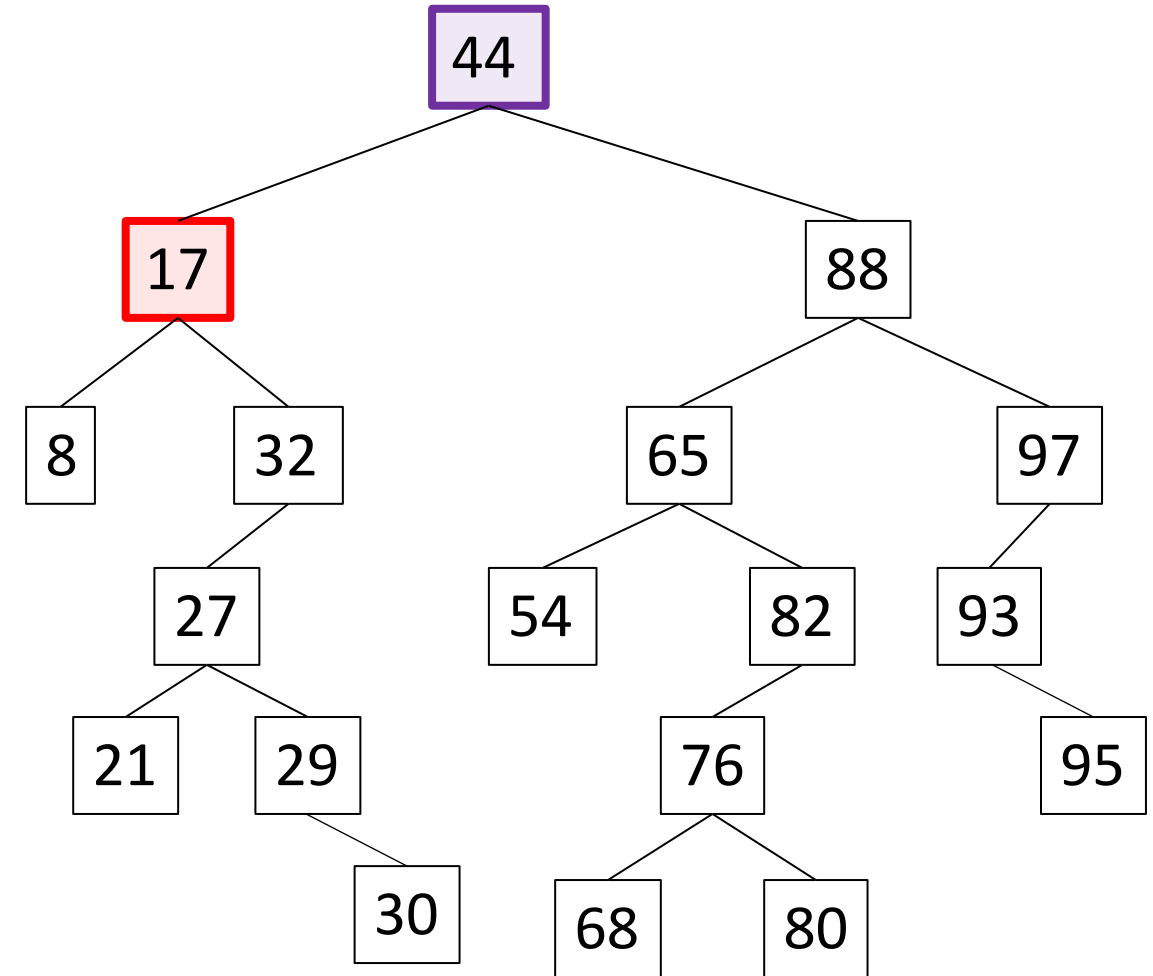
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public void depthFirst(8) {  
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        System.out.println(n.getValue());  
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```



Binary Search Tree - Traversal

```
public void depthFirst(44) {  
    if (n != null) {  
        System.out.println(n.getValue());  
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    if (n != null) {  
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        depthFirst(n.getLeft());  
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    }  
}
```



Output:

44

17

8

Binary Search Tree - Traversal

Output:

44

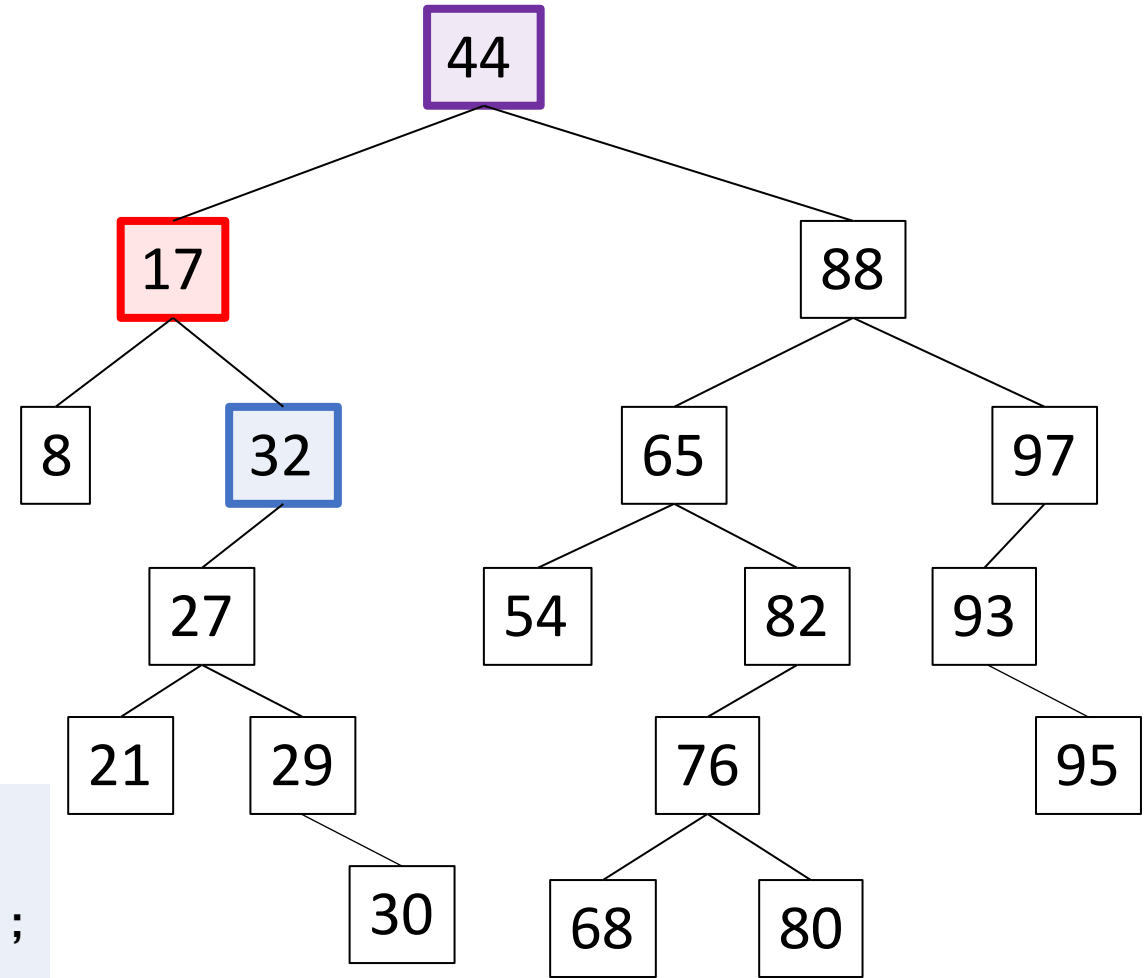
17

8

```
public void depthFirst(44) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

```
public void depthFirst(17) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

```
public void depthFirst(32) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

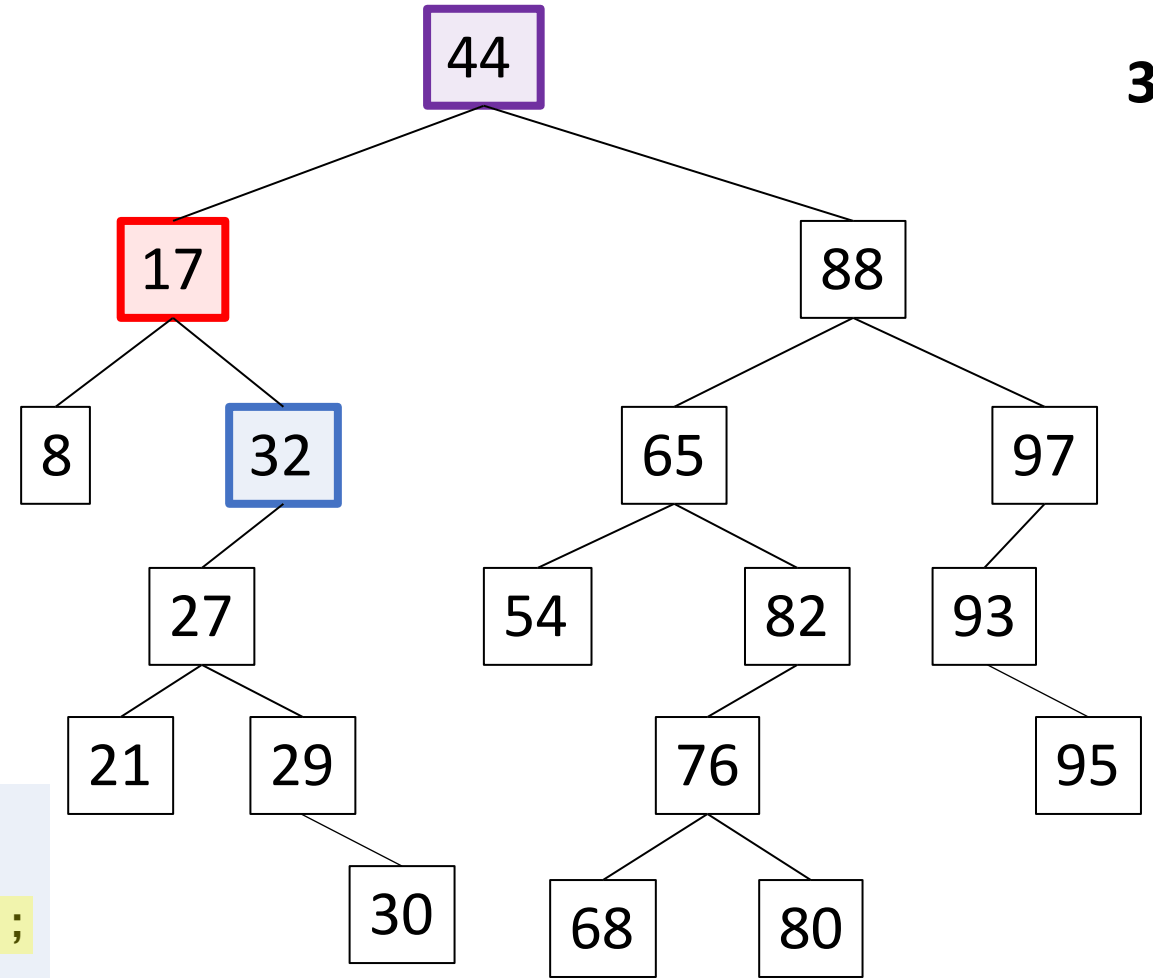


Binary Search Tree - Traversal

```
public void depthFirst(44) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

```
public void depthFirst(17) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

```
public void depthFirst(32) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```



Output:

44

17

8

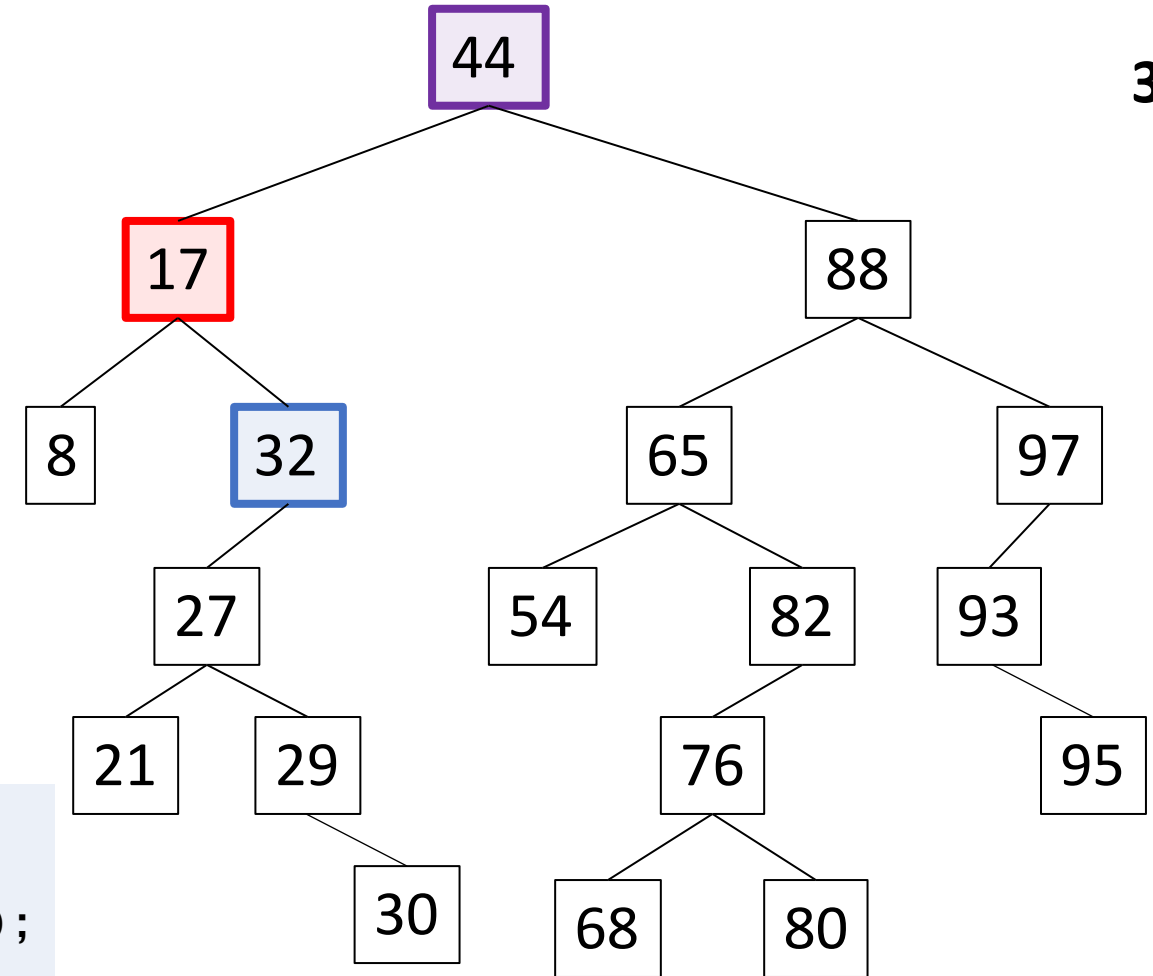
32

Binary Search Tree - Traversal

```
public void depthFirst(44) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

```
public void depthFirst(17) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

```
public void depthFirst(32) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```



Output:

44

17

8

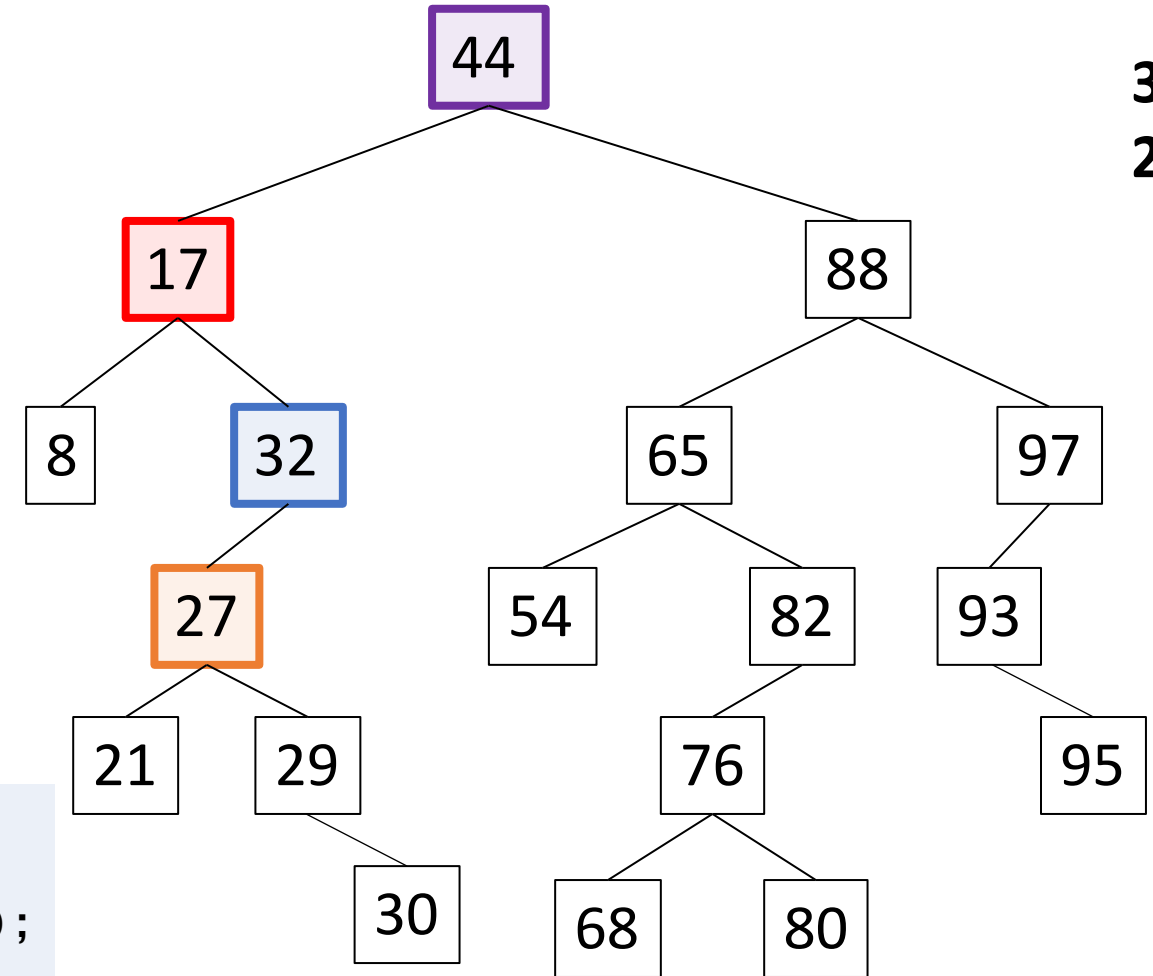
32

Binary Search Tree - Traversal

```
public void depthFirst(44) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

```
public void depthFirst(17) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

```
public void depthFirst(32) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```



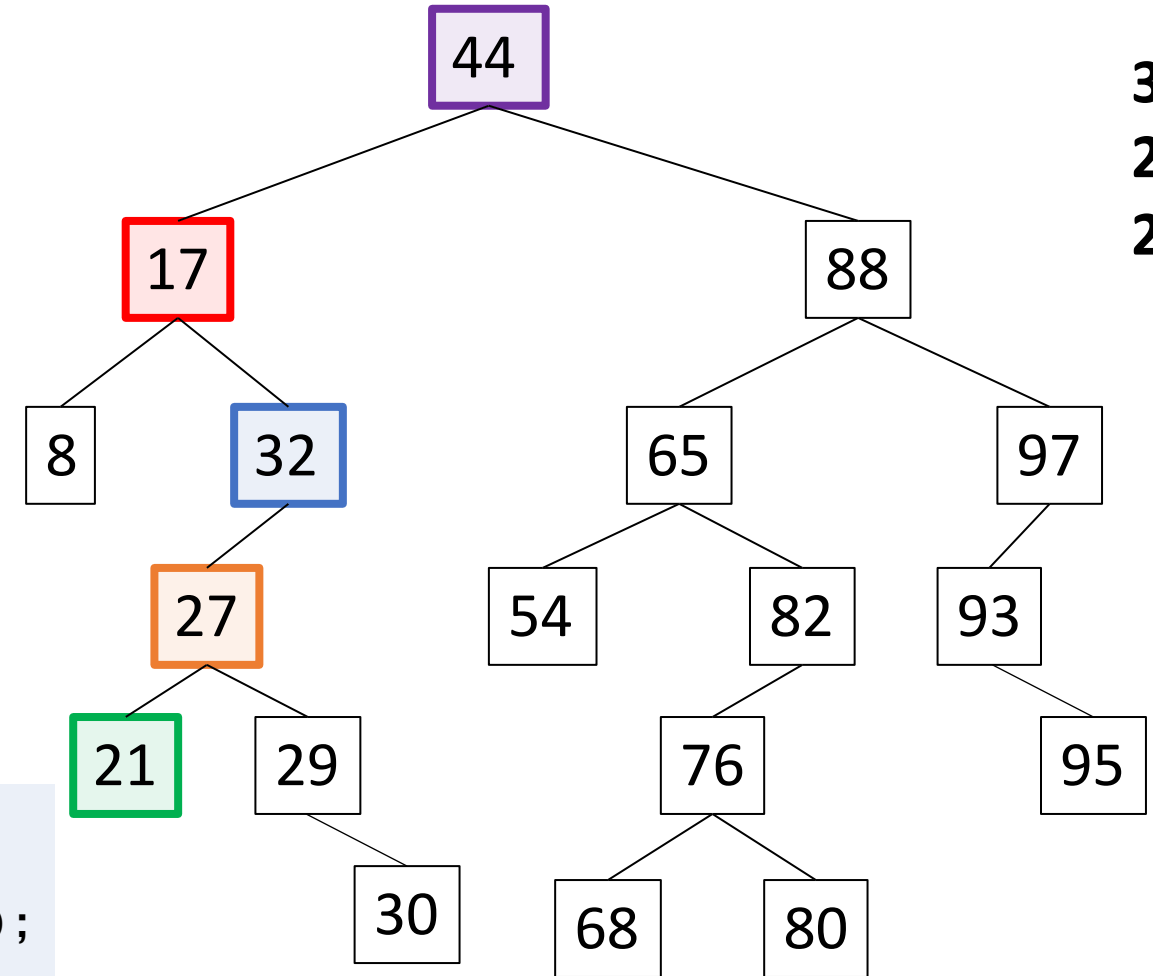
Output:
44
17
8
32
27

Binary Search Tree - Traversal

```
public void depthFirst(44) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

```
public void depthFirst(17) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

```
public void depthFirst(32) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```



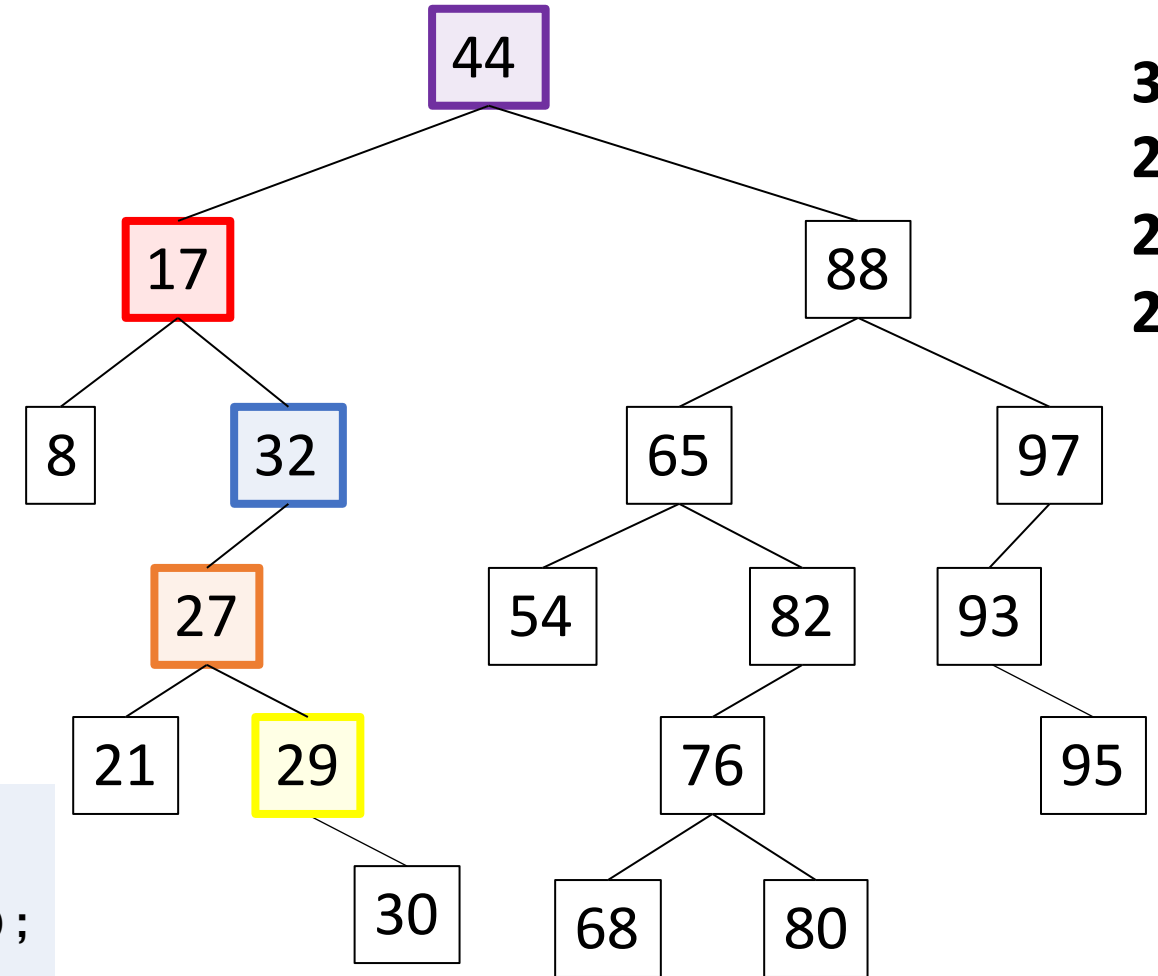
Output:
44
17
8
32
27
21

Binary Search Tree - Traversal

```
public void depthFirst(44) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

```
public void depthFirst(17) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

```
public void depthFirst(32) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```



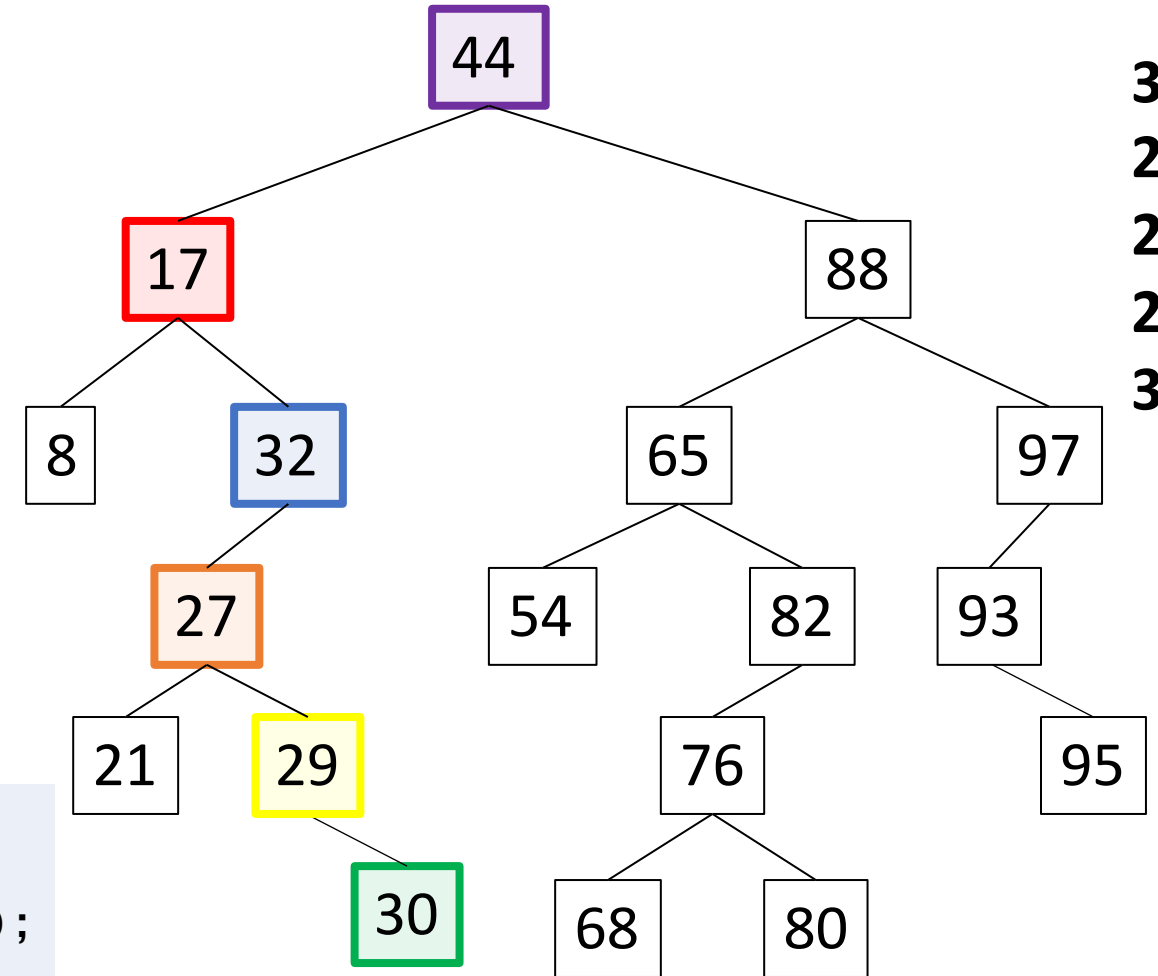
Output:
44
17
8
32
27
21
29

Binary Search Tree - Traversal

```
public void depthFirst(44) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

```
public void depthFirst(17) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

```
public void depthFirst(32) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```



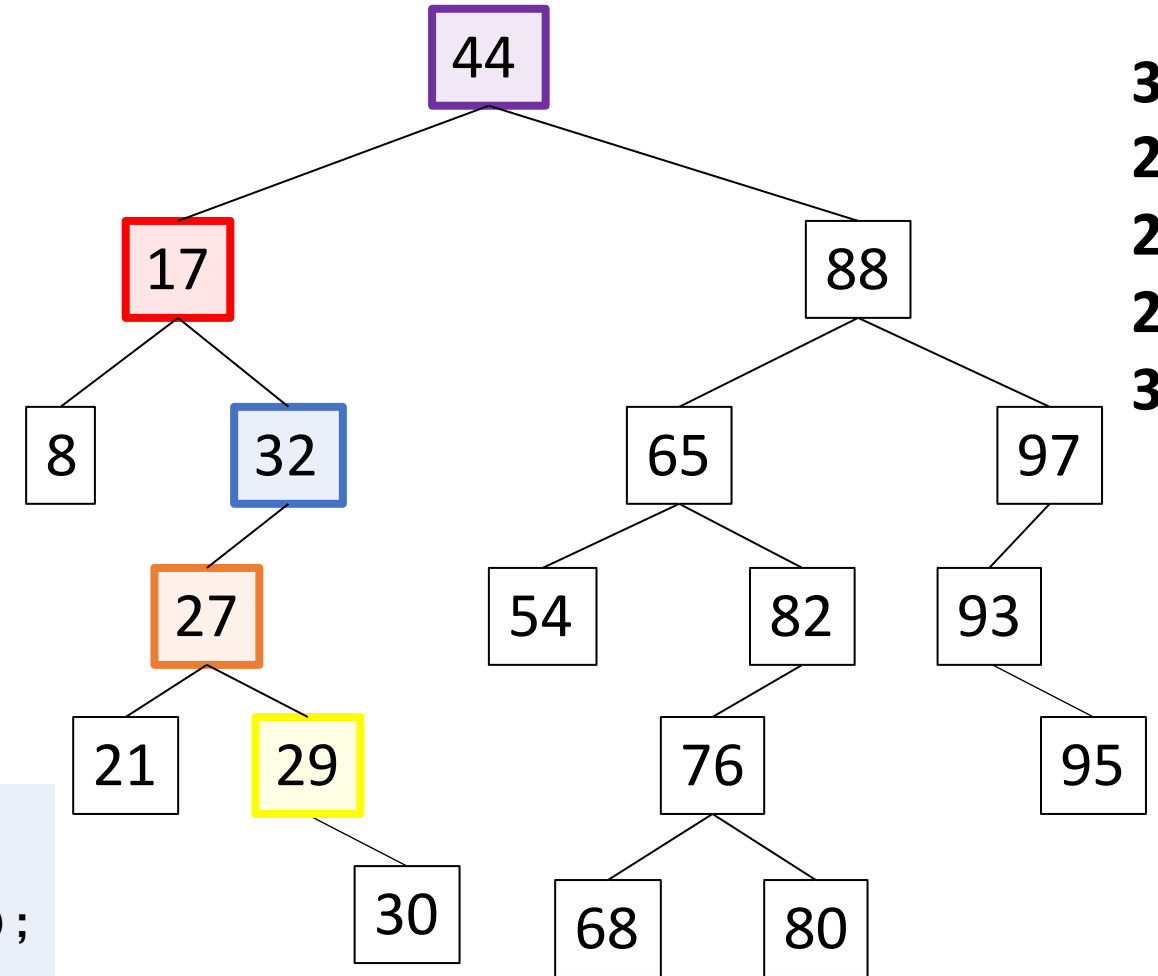
Output:
44
17
8
32
27
21
29
30

Binary Search Tree - Traversal

```
public void depthFirst(44) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

```
public void depthFirst(17) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

```
public void depthFirst(32) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```



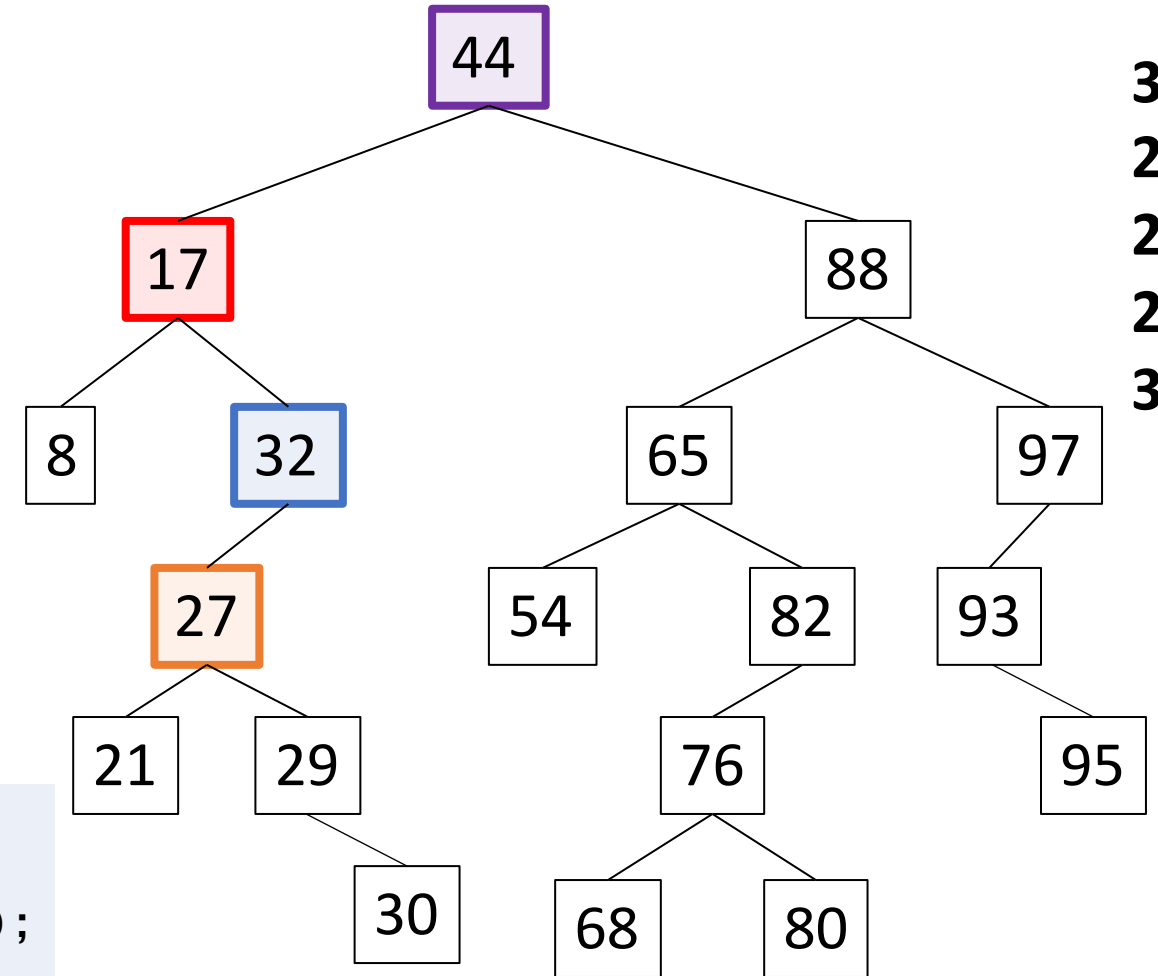
Output:
44
17
8
32
27
21
29
30

Binary Search Tree - Traversal

```
public void depthFirst(44) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

```
public void depthFirst(17) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

```
public void depthFirst(32) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```



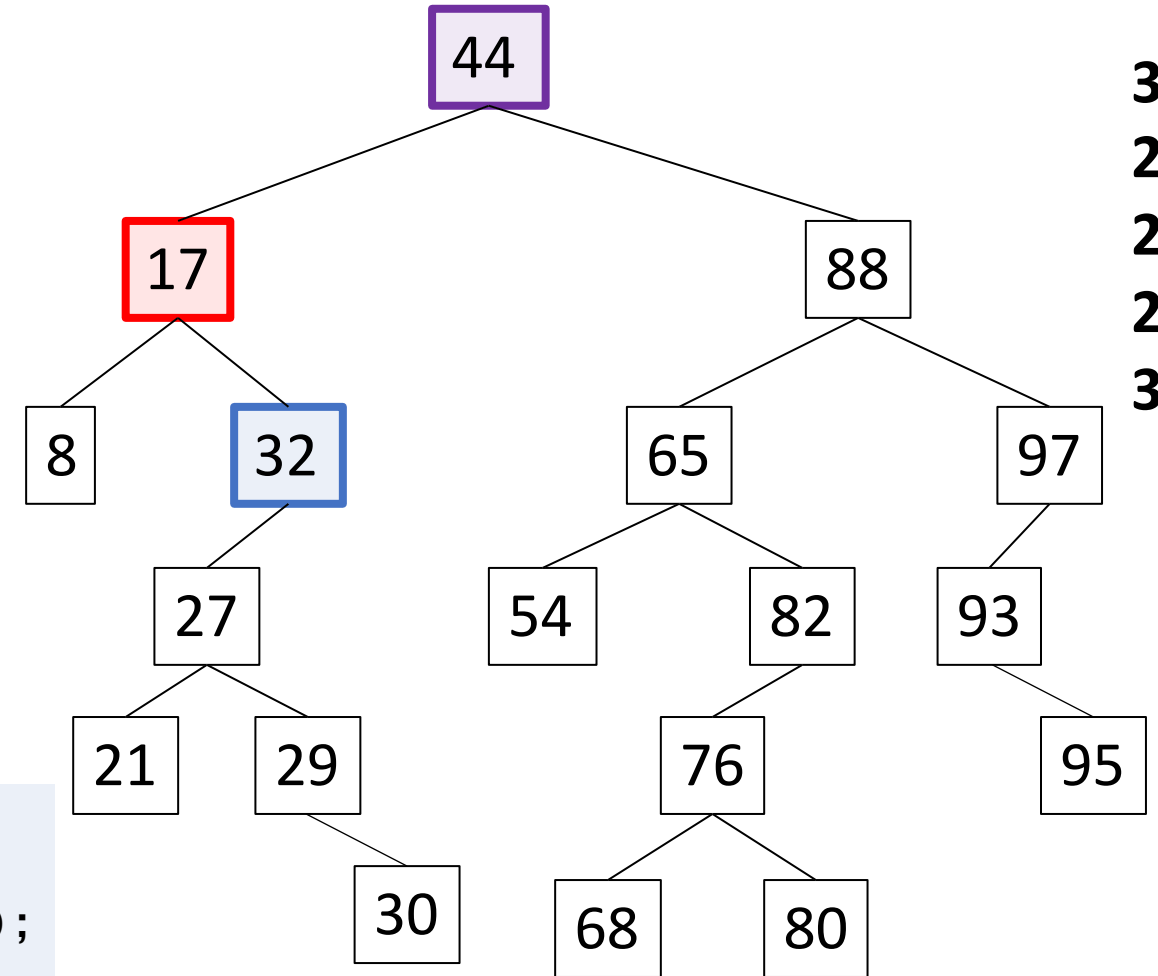
Output:
44
17
8
32
27
21
29
30

Binary Search Tree - Traversal

```
public void depthFirst(44) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

```
public void depthFirst(17) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

```
public void depthFirst(32) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

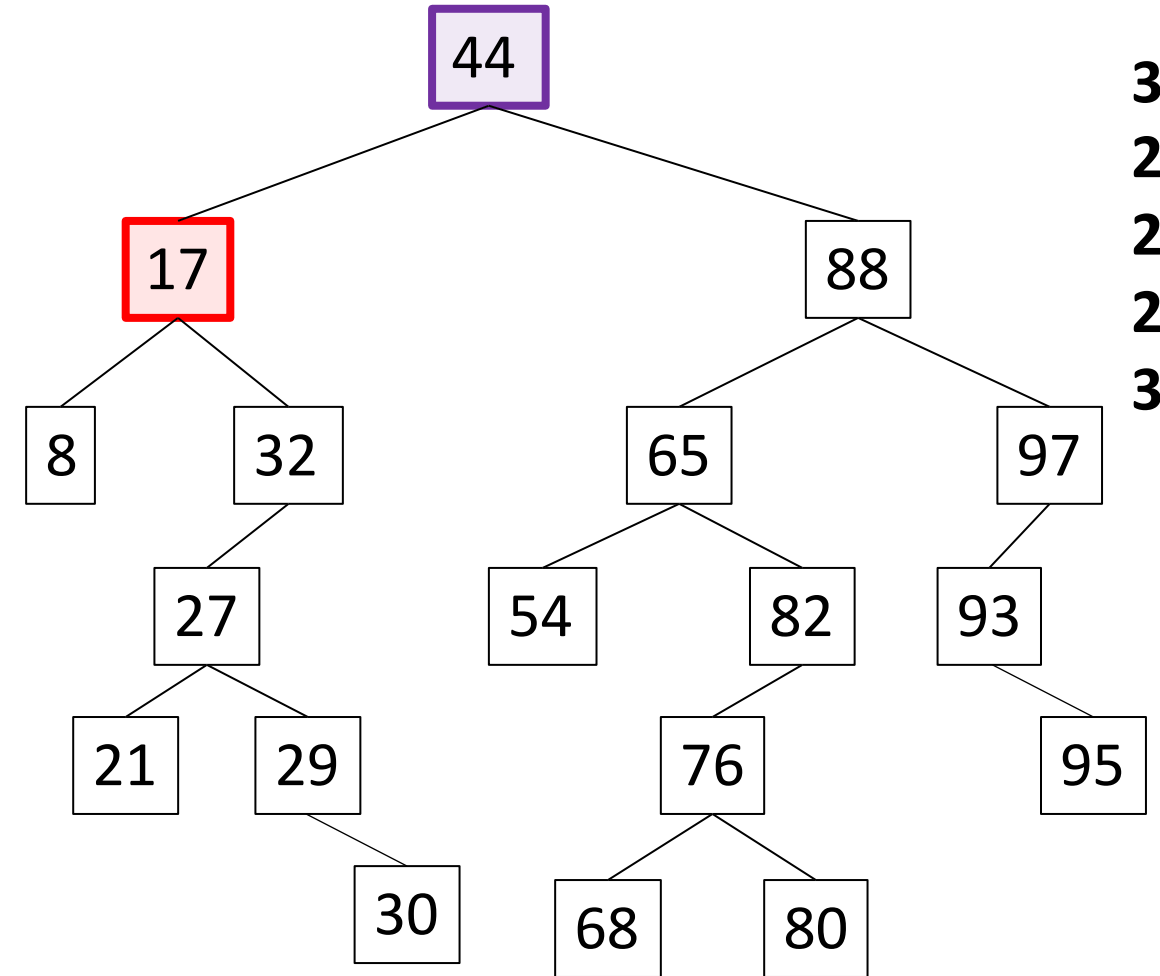


Output:
44
17
8
32
27
21
29
30

Binary Search Tree - Traversal

```
public void depthFirst(44) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

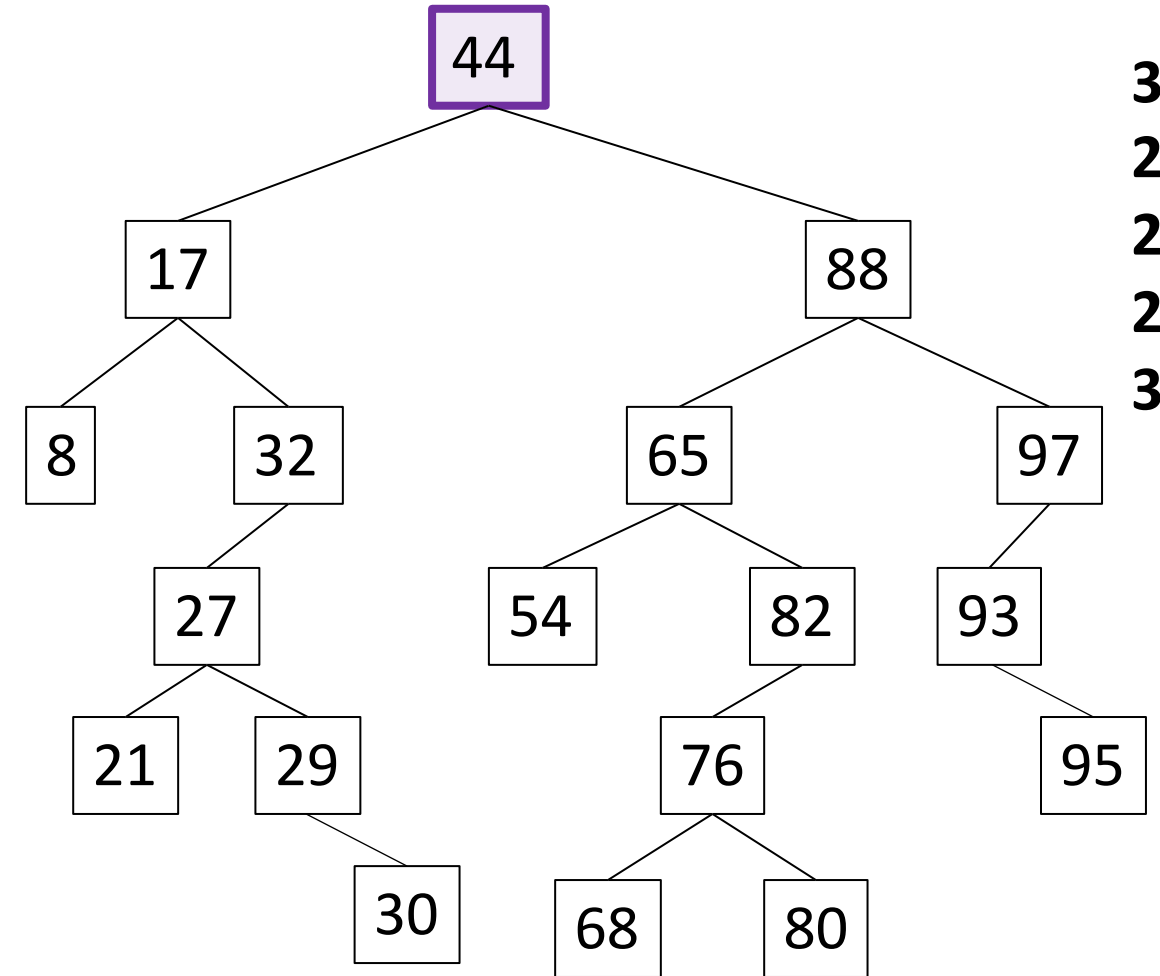
```
public void depthFirst(17) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```



Output:
44
17
8
32
27
21
29
30

Binary Search Tree - Traversal

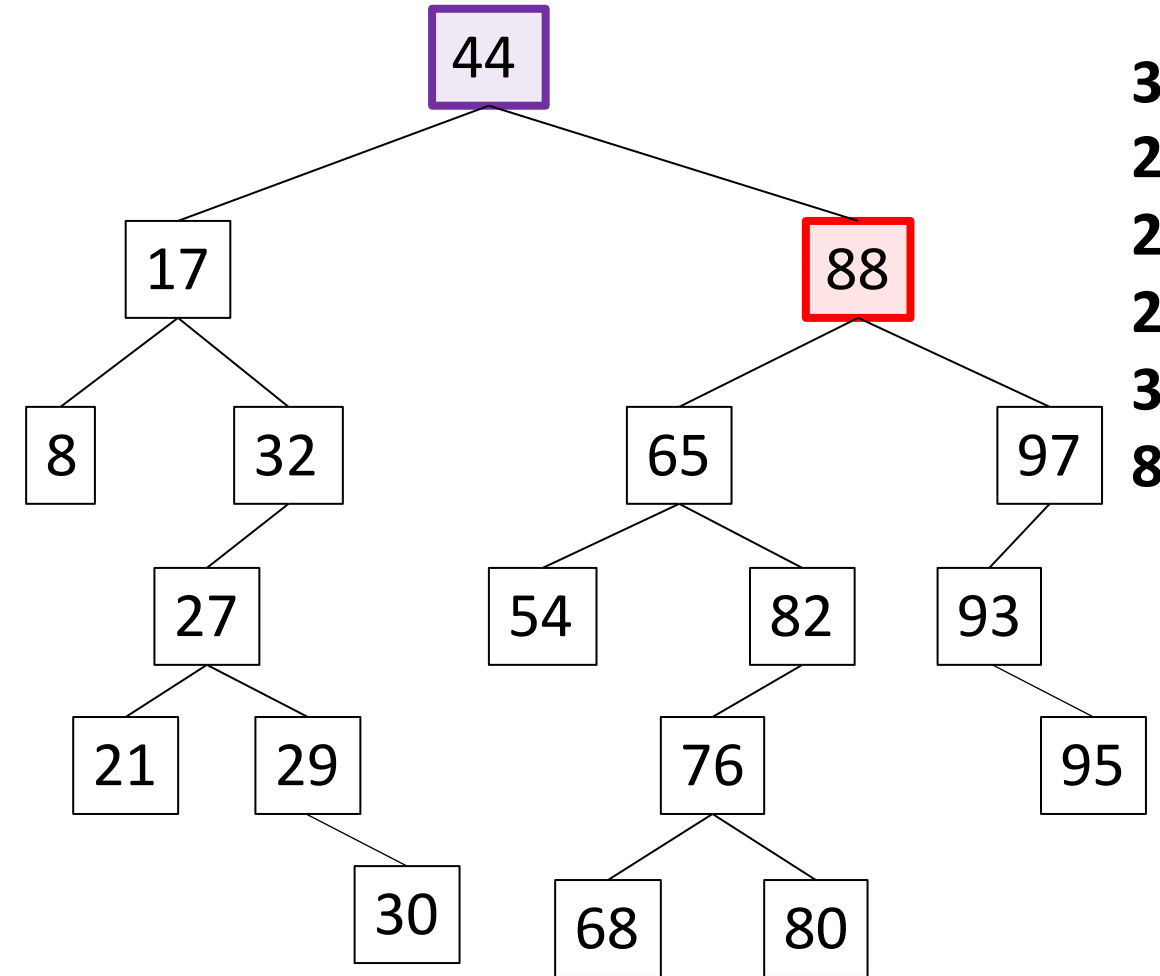
```
public void depthFirst(44) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```



Output:
44
17
8
32
27
21
29
30

Binary Search Tree - Traversal

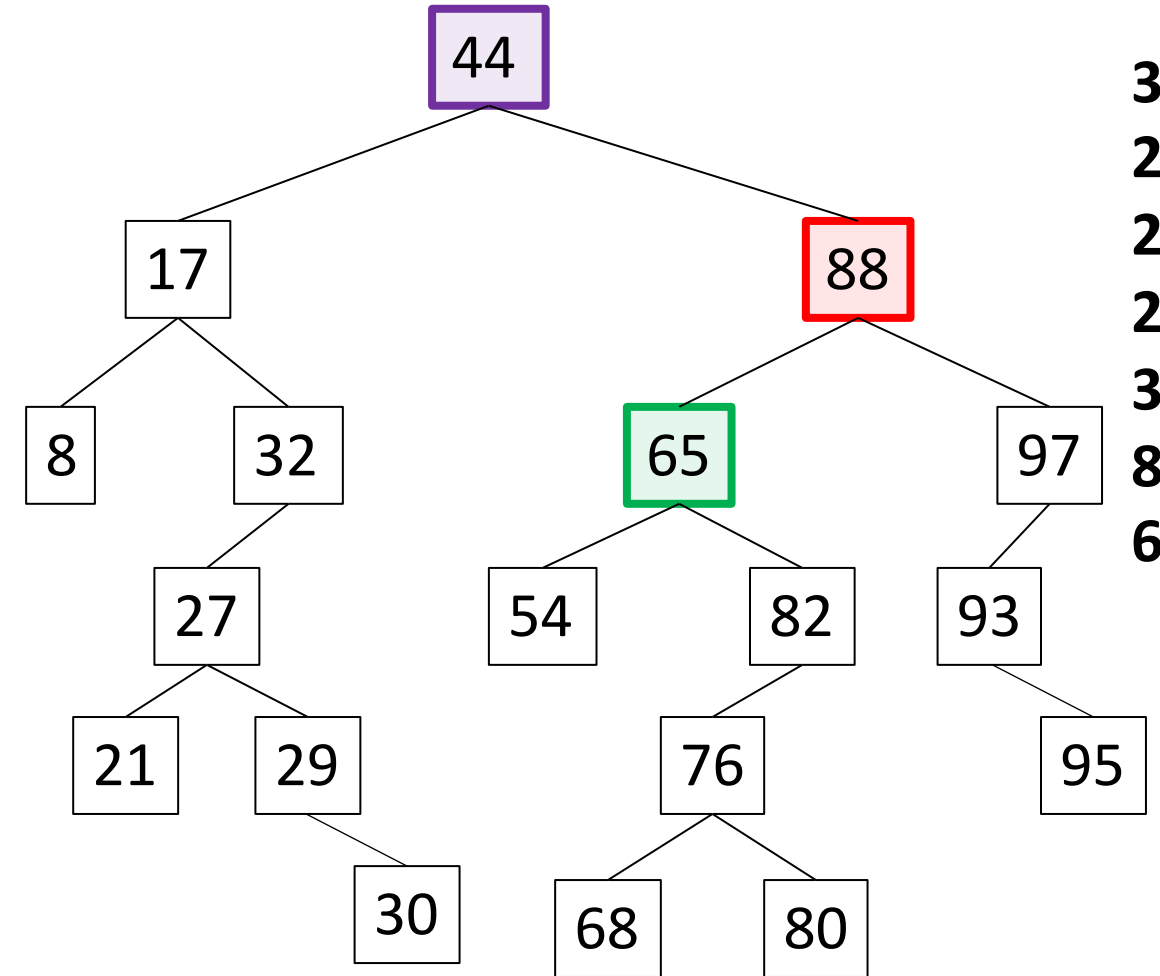
```
public void depthFirst(44) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```



Output:
44
17
8
32
27
21
29
30
88

Binary Search Tree - Traversal

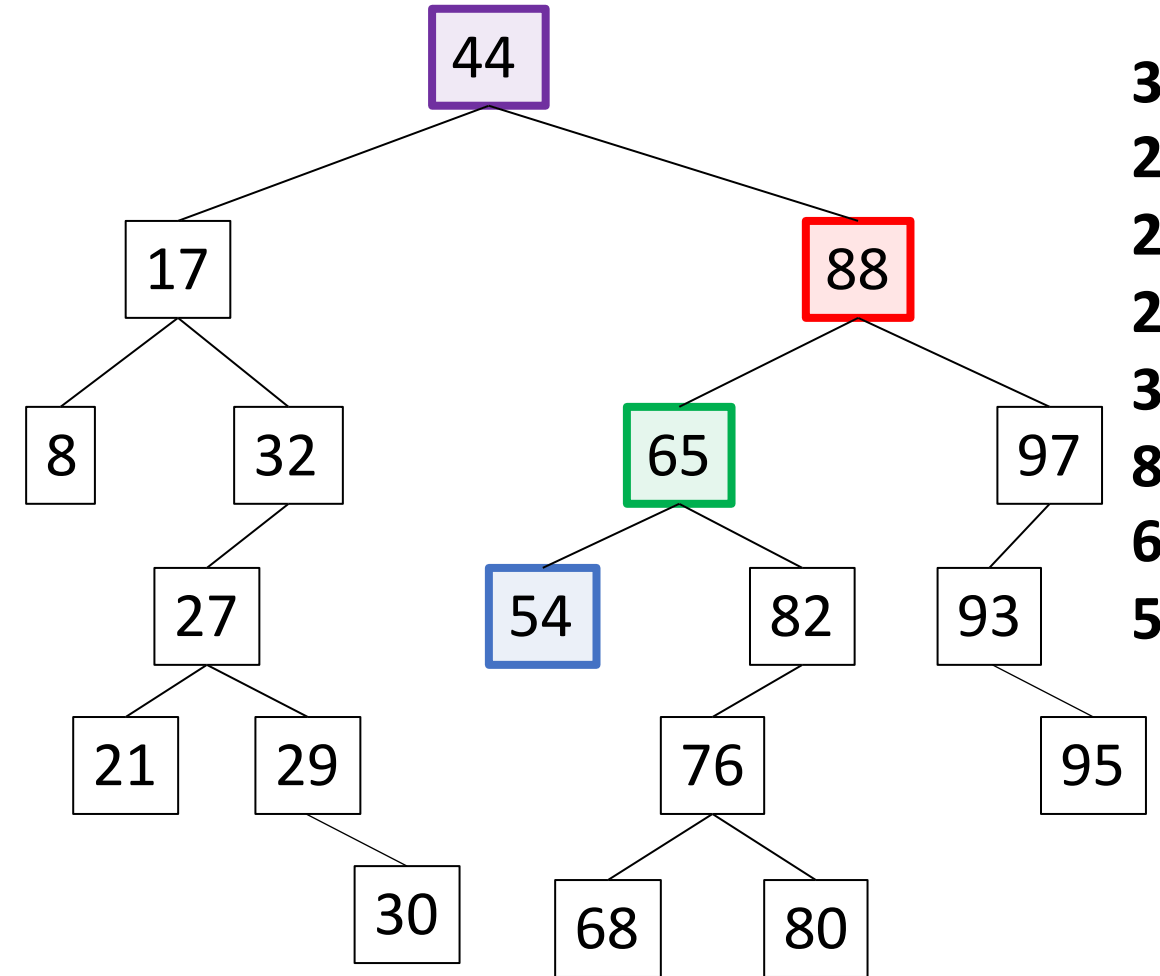
```
public void depthFirst(44) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```



Output:
44
17
8
32
27
21
29
30
88
65

Binary Search Tree - Traversal

```
public void depthFirst(44) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```



Output:

44
17
8
32
27
21
29
30
88
65
54

Output:

44

17

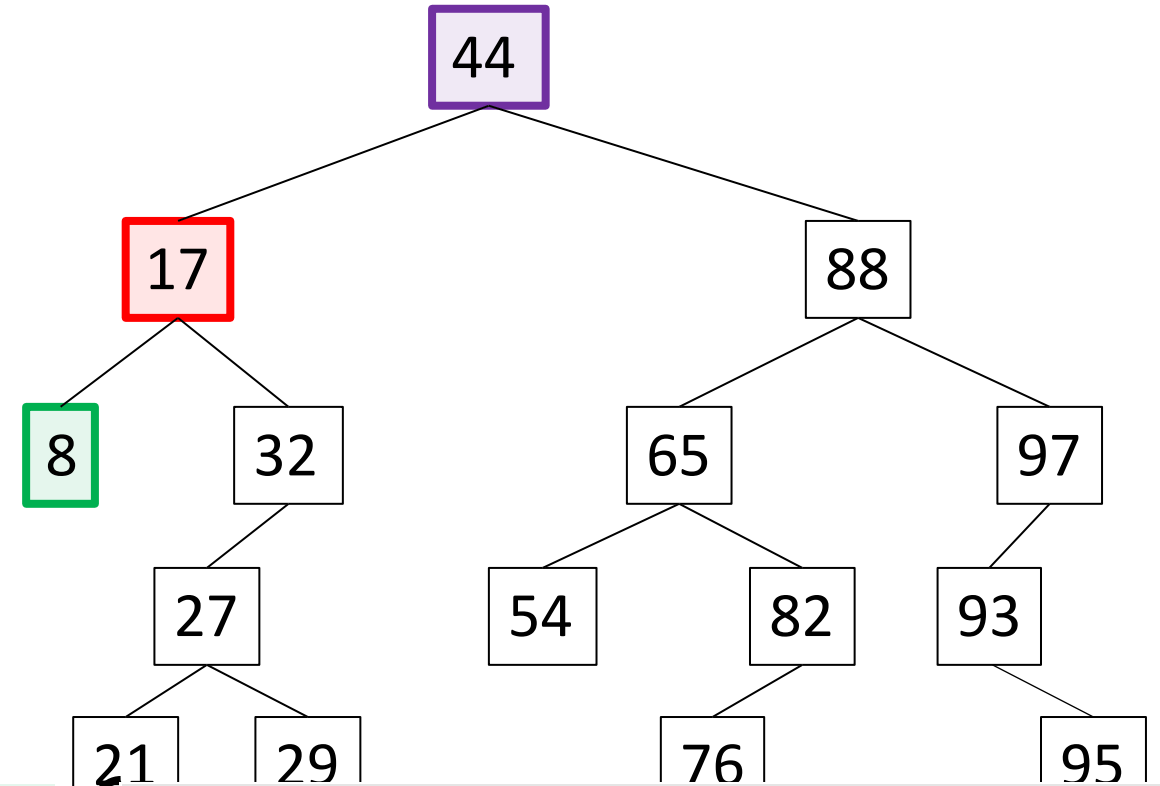
8

Binary Search Tree - Traversal

```
public void depthFirst(44) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

```
public void depthFirst(17) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

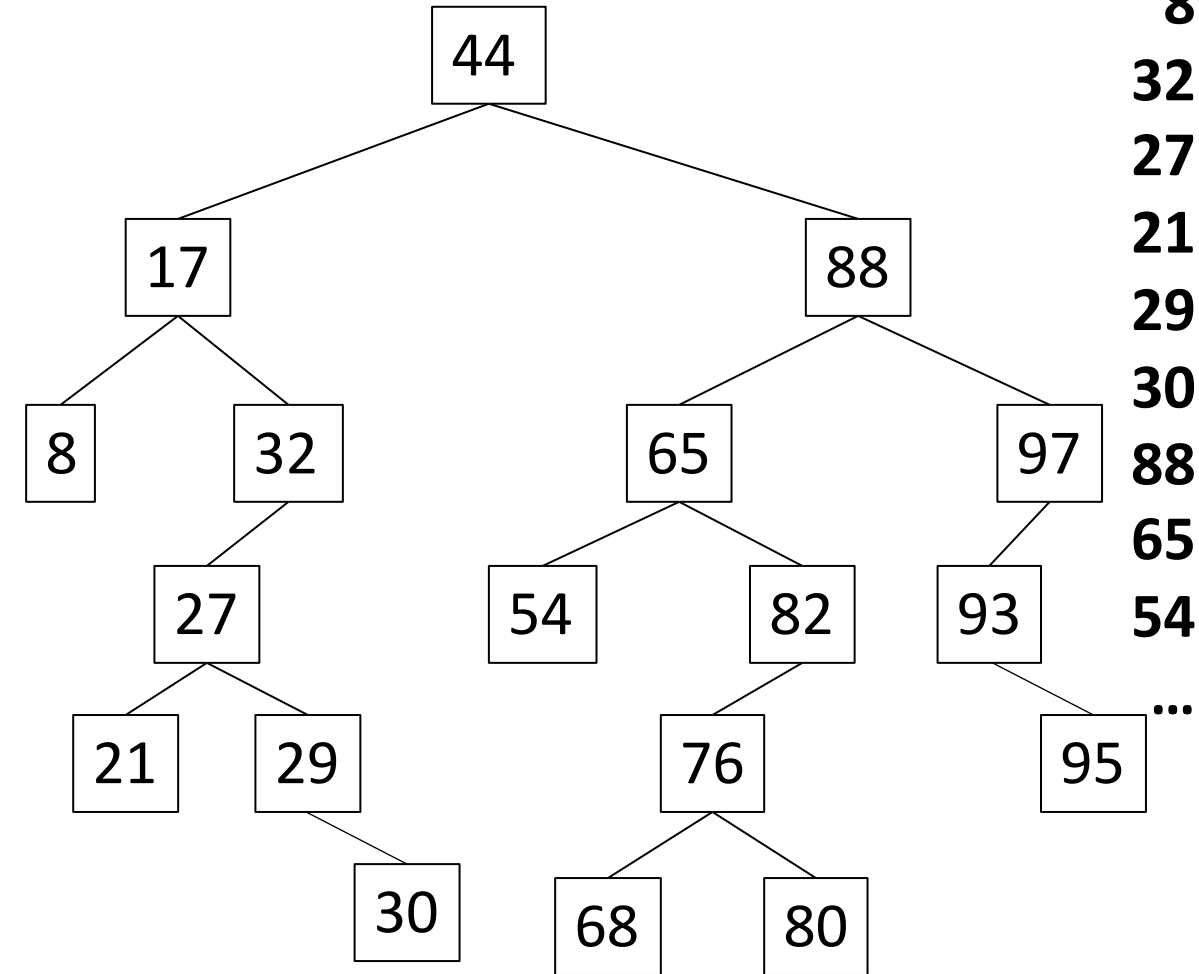
```
public void depthFirst(8) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```



```
public void depthFirst(null) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```

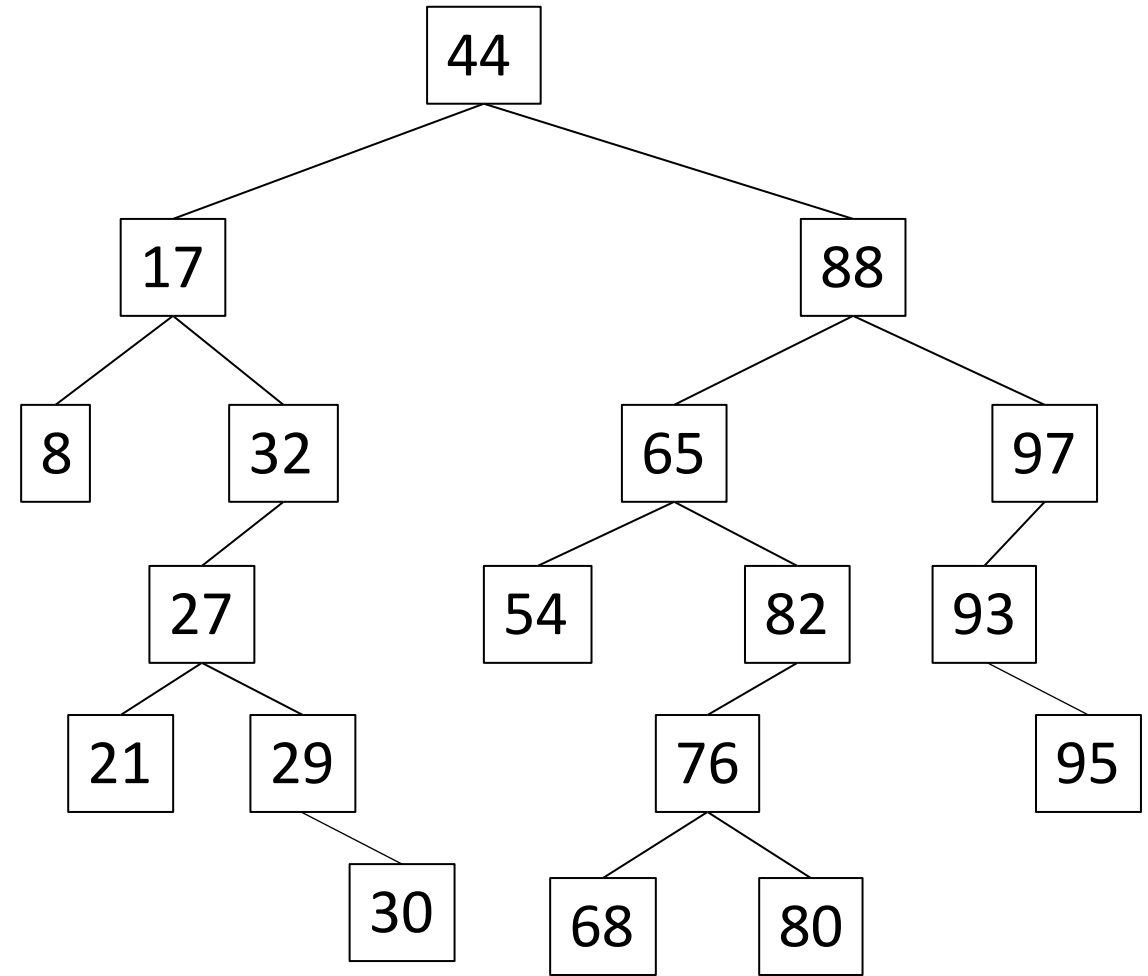
Binary Search Tree - Traversal

```
public void depthFirst(44) {  
    if (n != null) {  
        System.out.println(n.getValue());  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
    }  
}
```



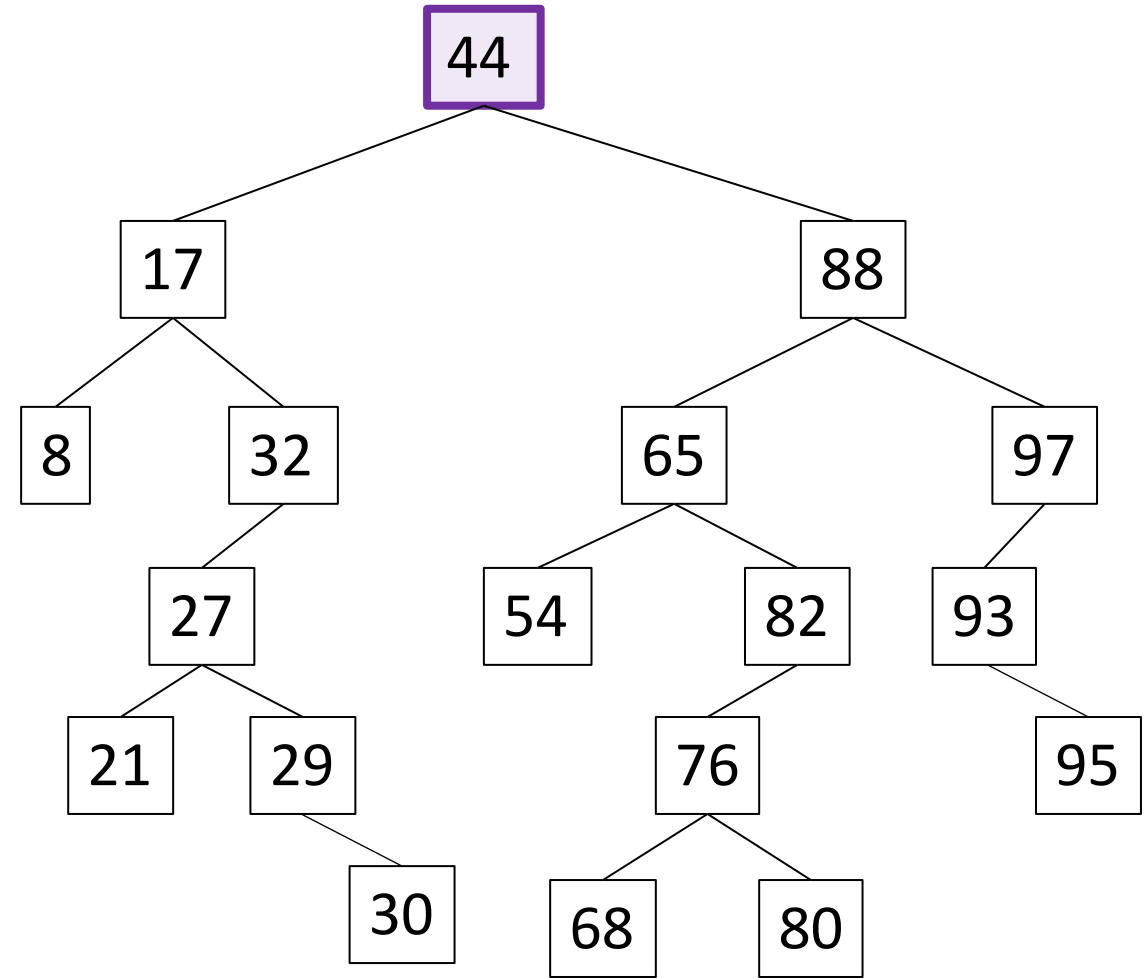
Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
        System.out.println(n.getValue());  
    }  
}
```



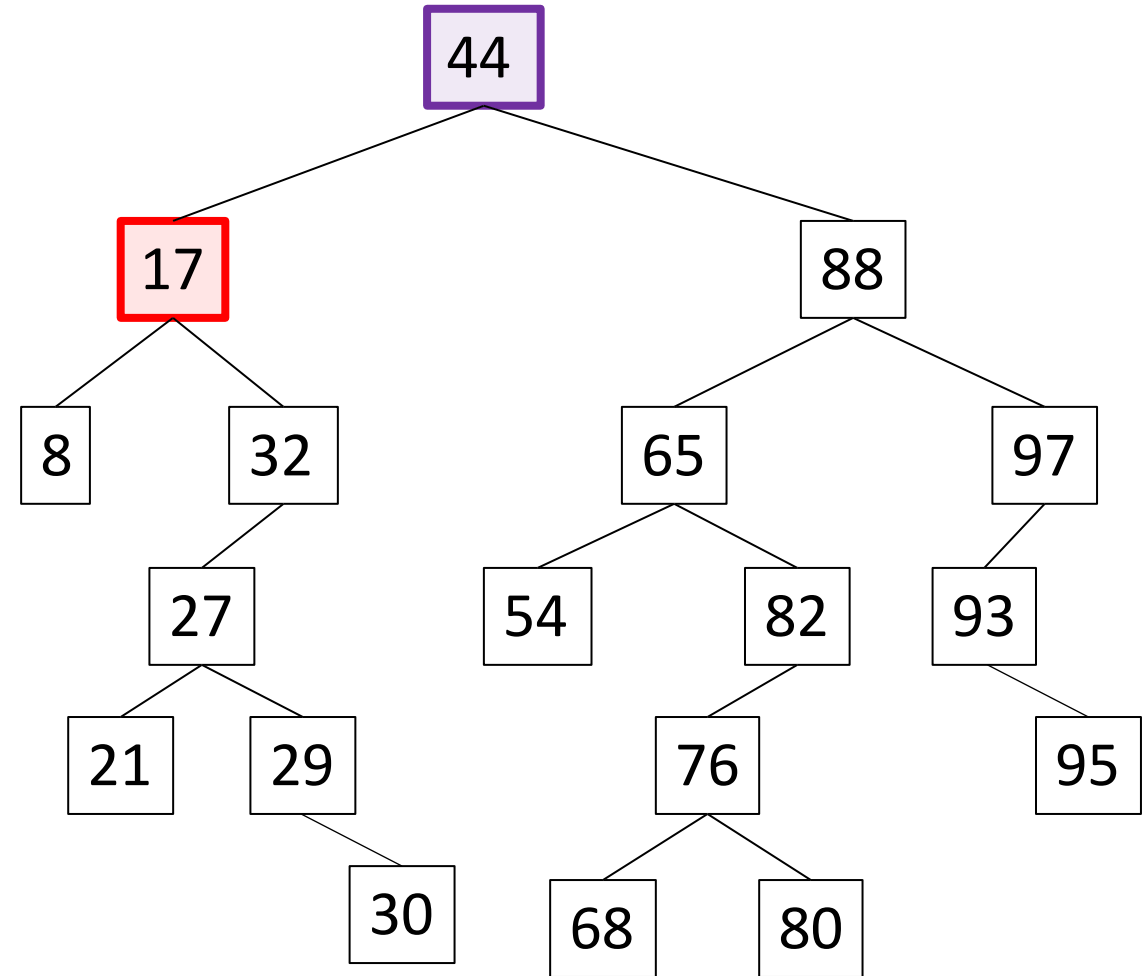
Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
        System.out.println(n.getValue());  
    }  
}
```



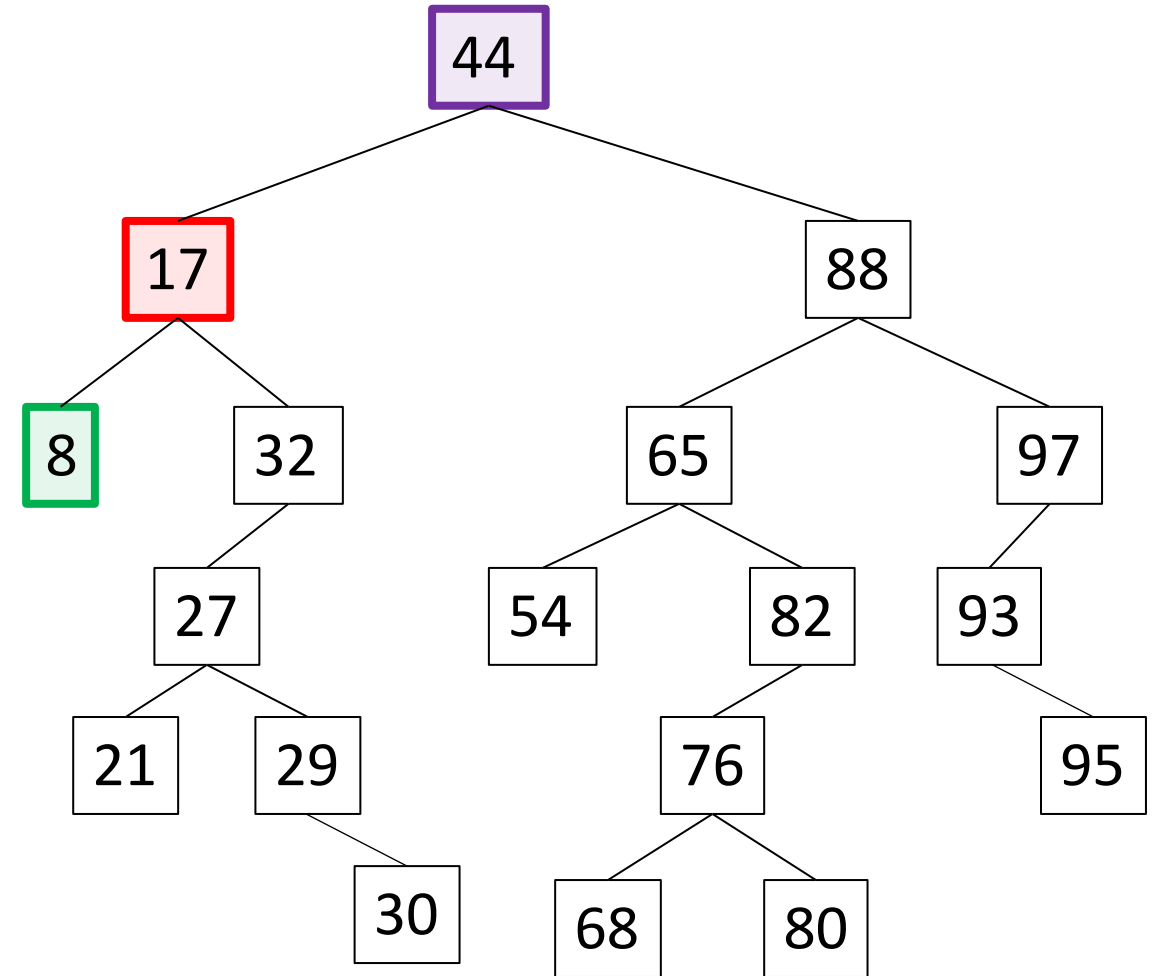
Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
        System.out.println(n.getValue());  
    }  
}
```



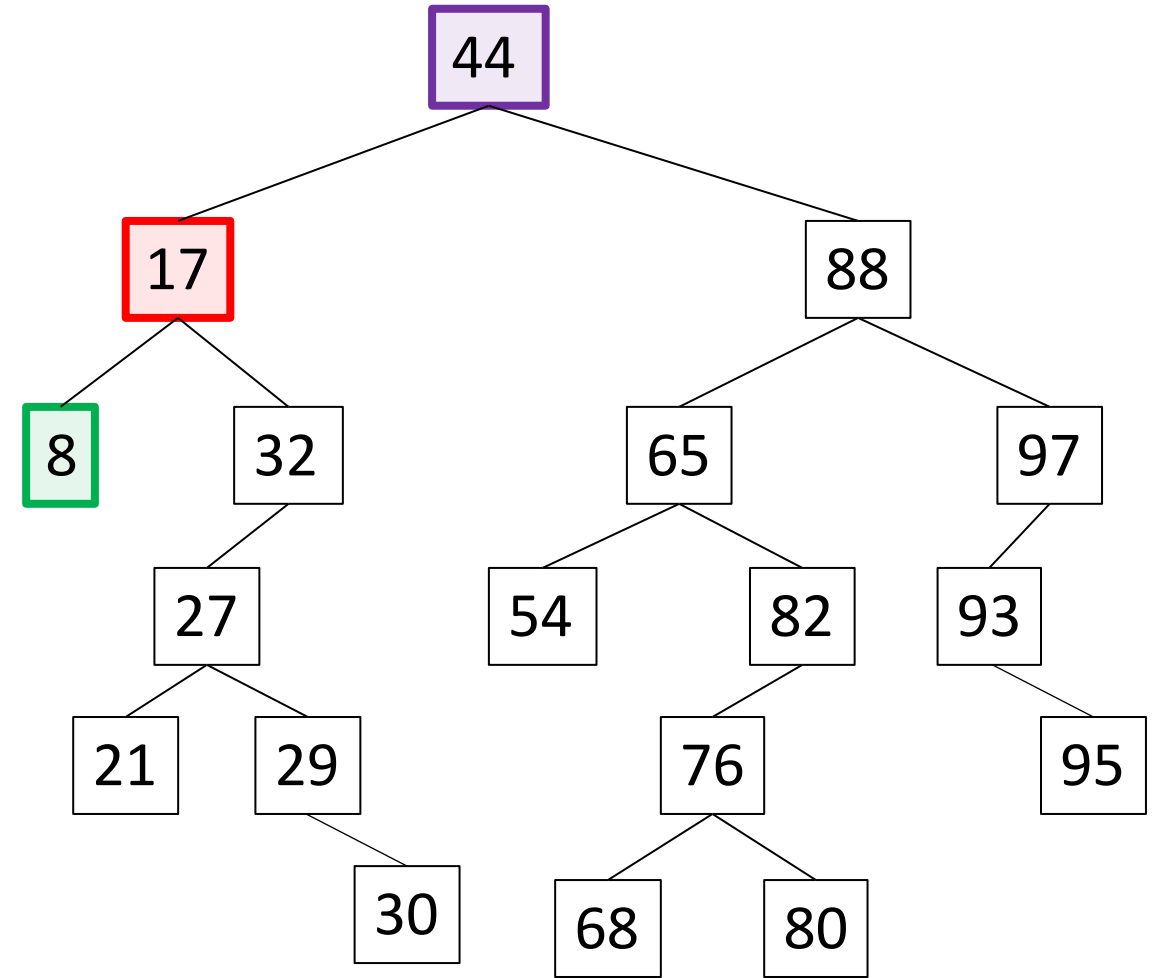
Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
        System.out.println(n.getValue());  
    }  
}
```



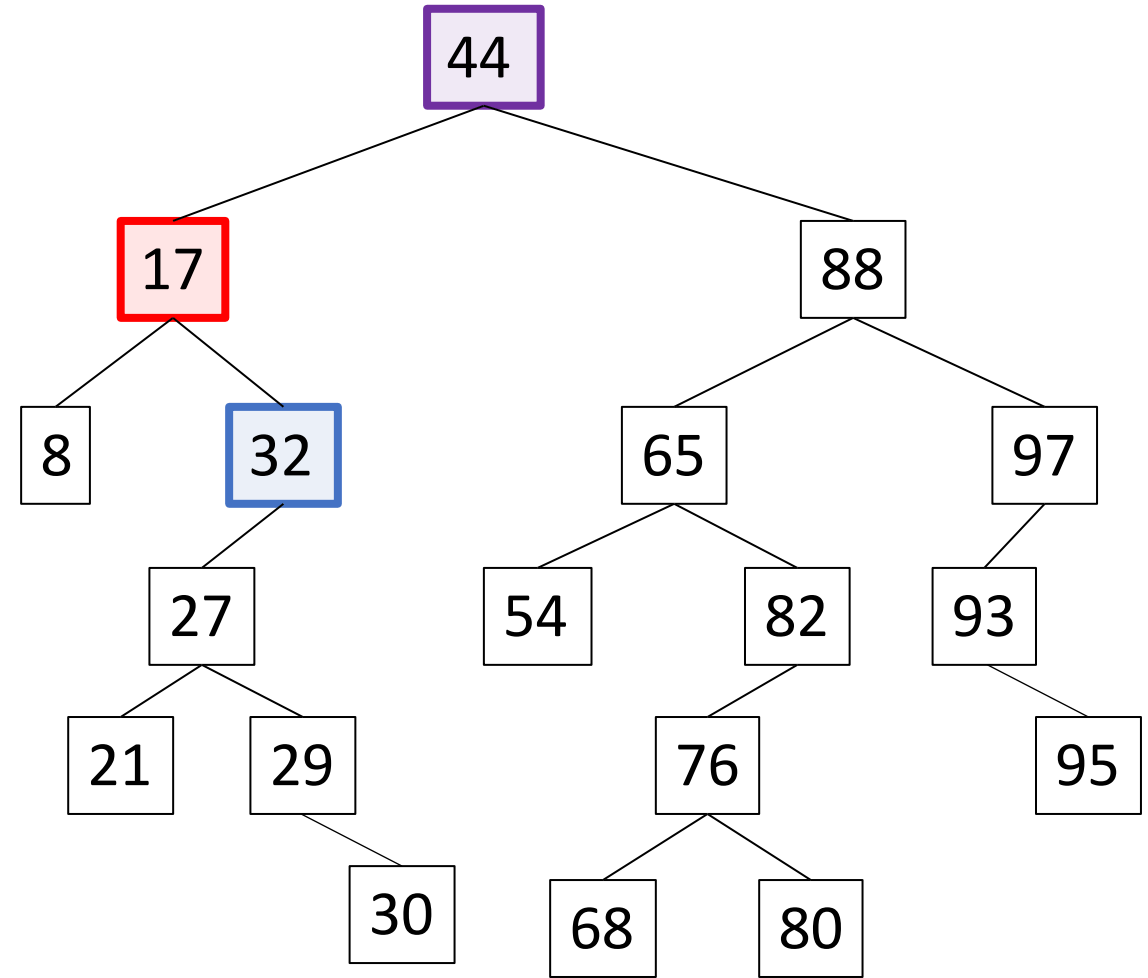
Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
        System.out.println(n.getValue());  
    }  
}
```



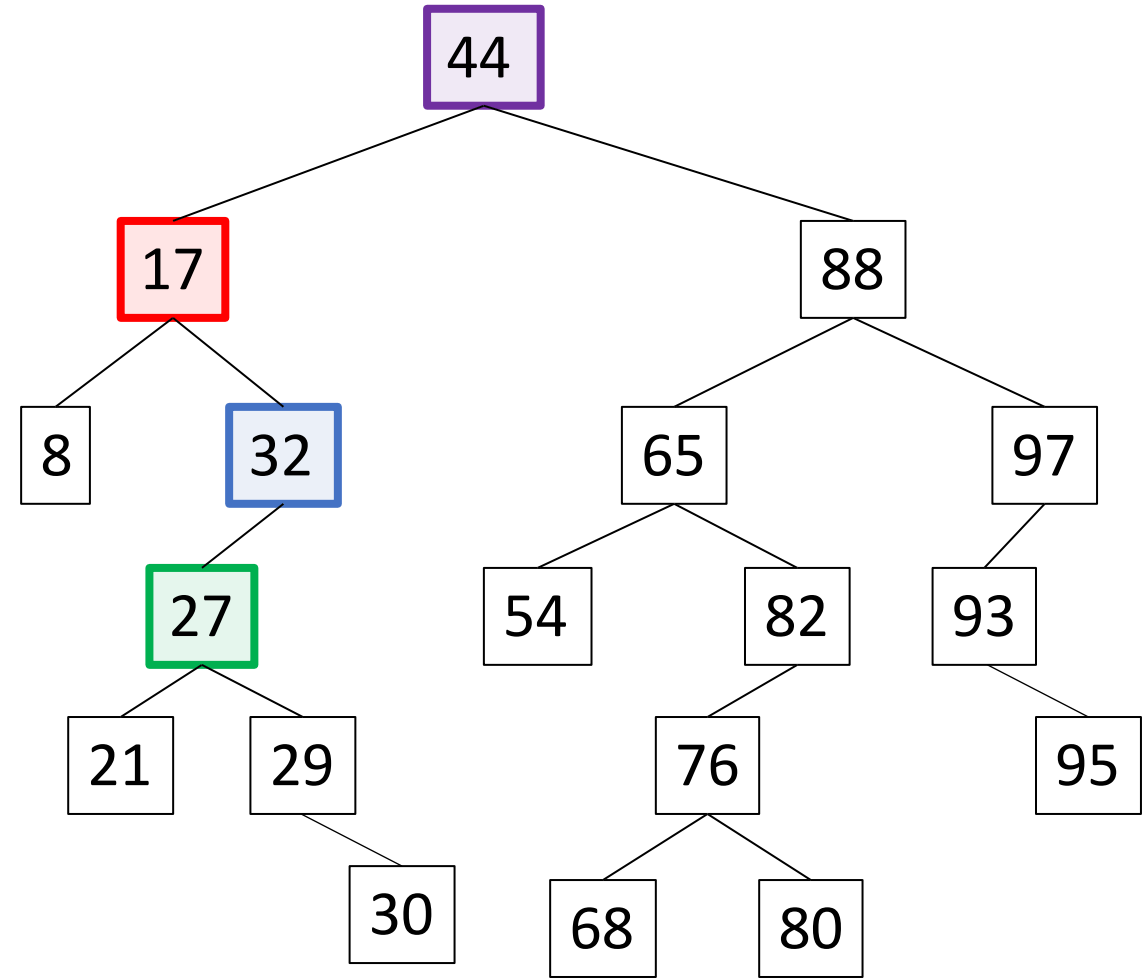
Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
        System.out.println(n.getValue());  
    }  
}
```



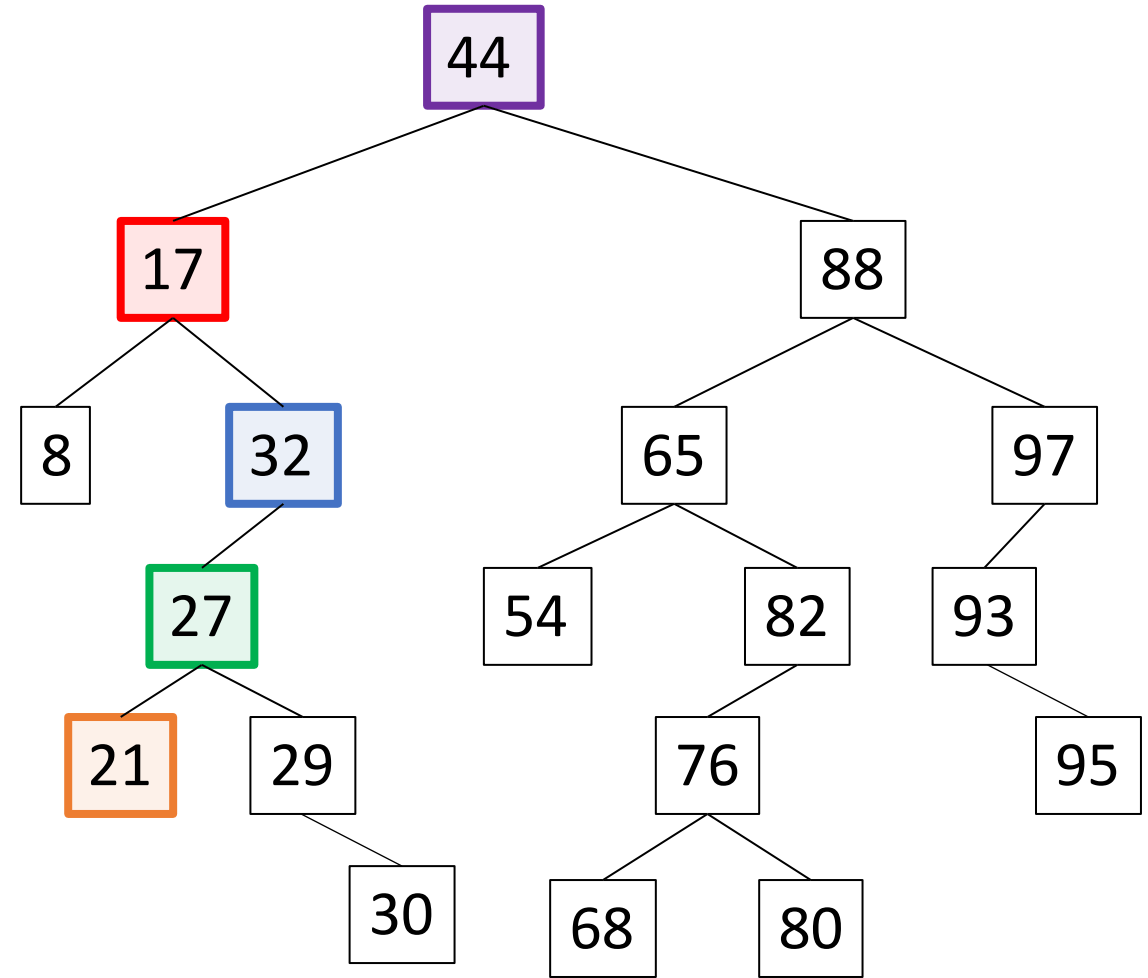
Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
        System.out.println(n.getValue());  
    }  
}
```



Binary Search Tree - Traversal

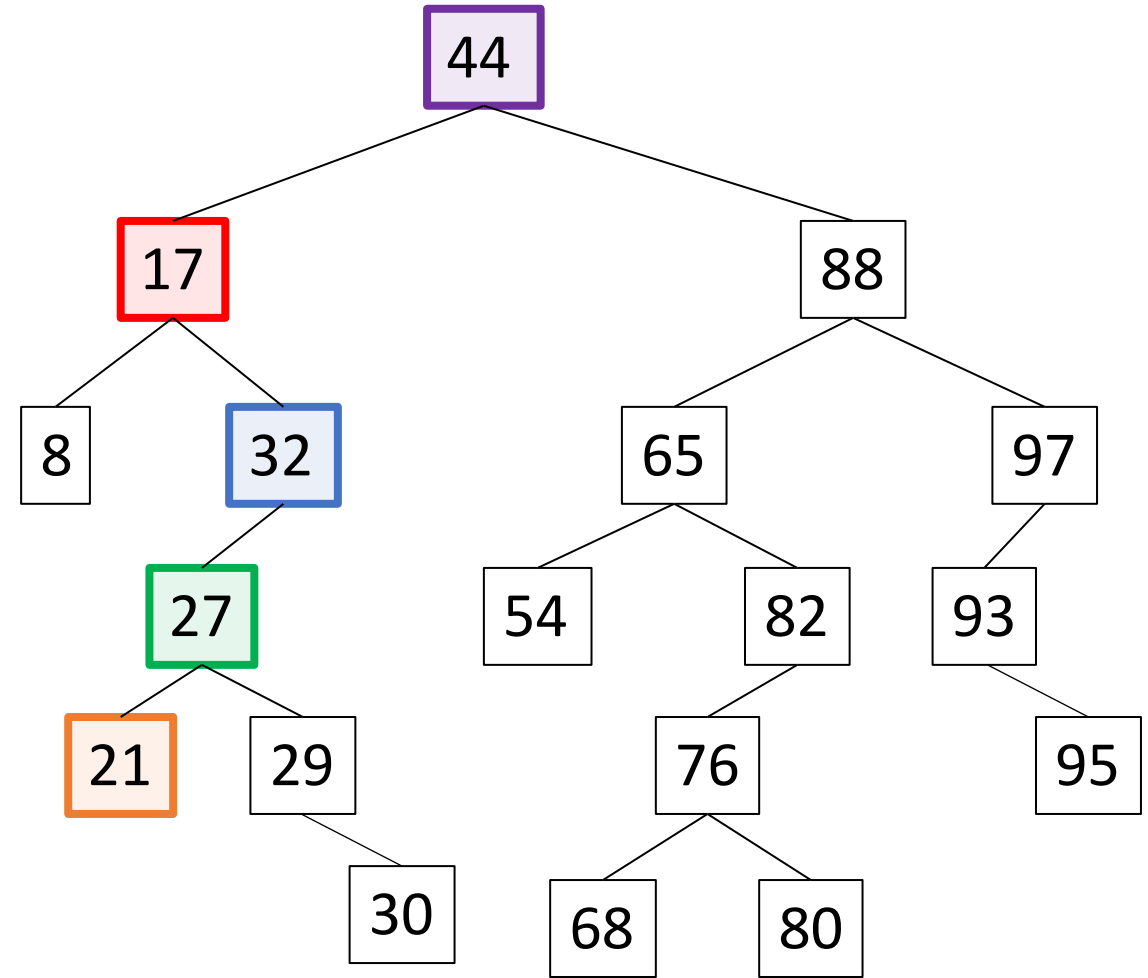
```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
        System.out.println(n.getValue());  
    }  
}
```



Output:
8
21

Binary Search Tree - Traversal

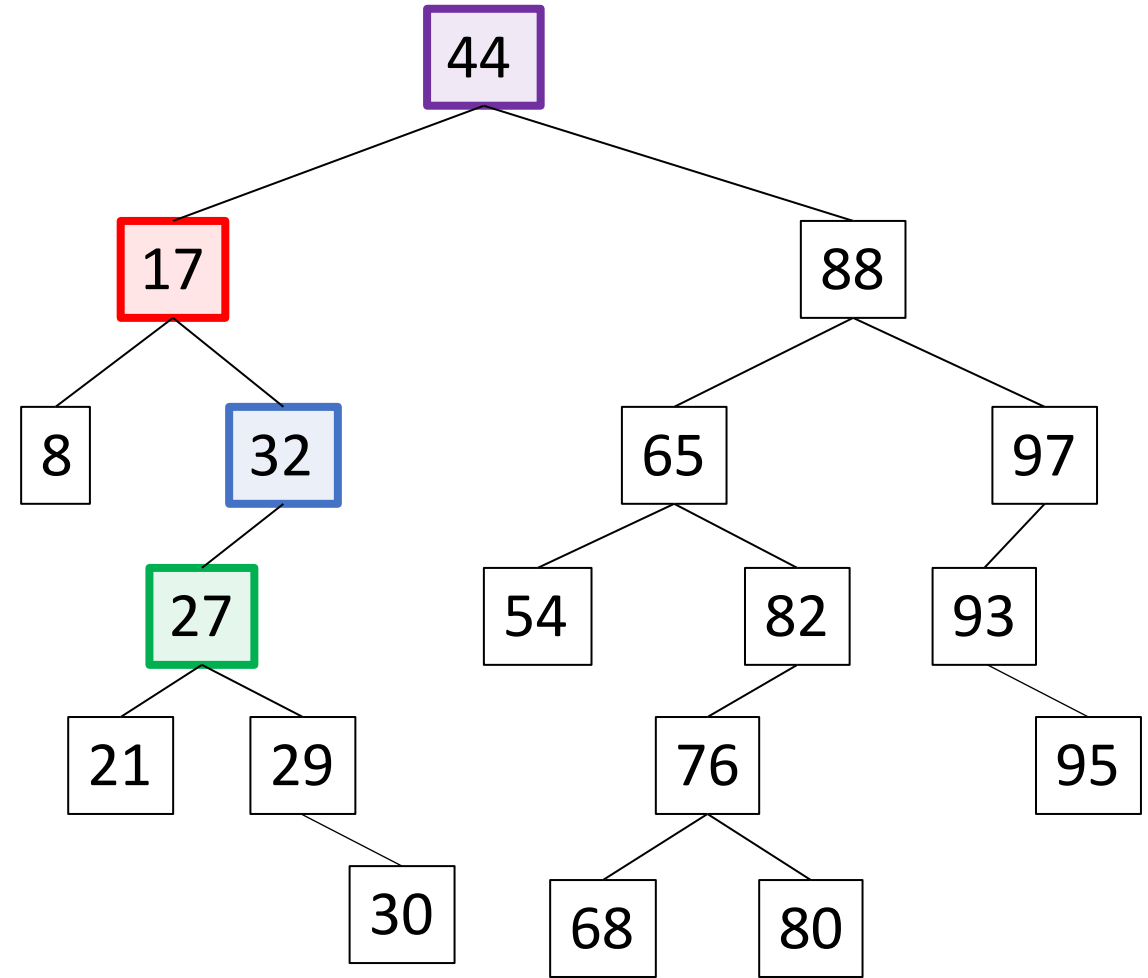
```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
        System.out.println(n.getValue());  
    }  
}
```



Output:
8
21

Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
        System.out.println(n.getValue());  
    }  
}
```



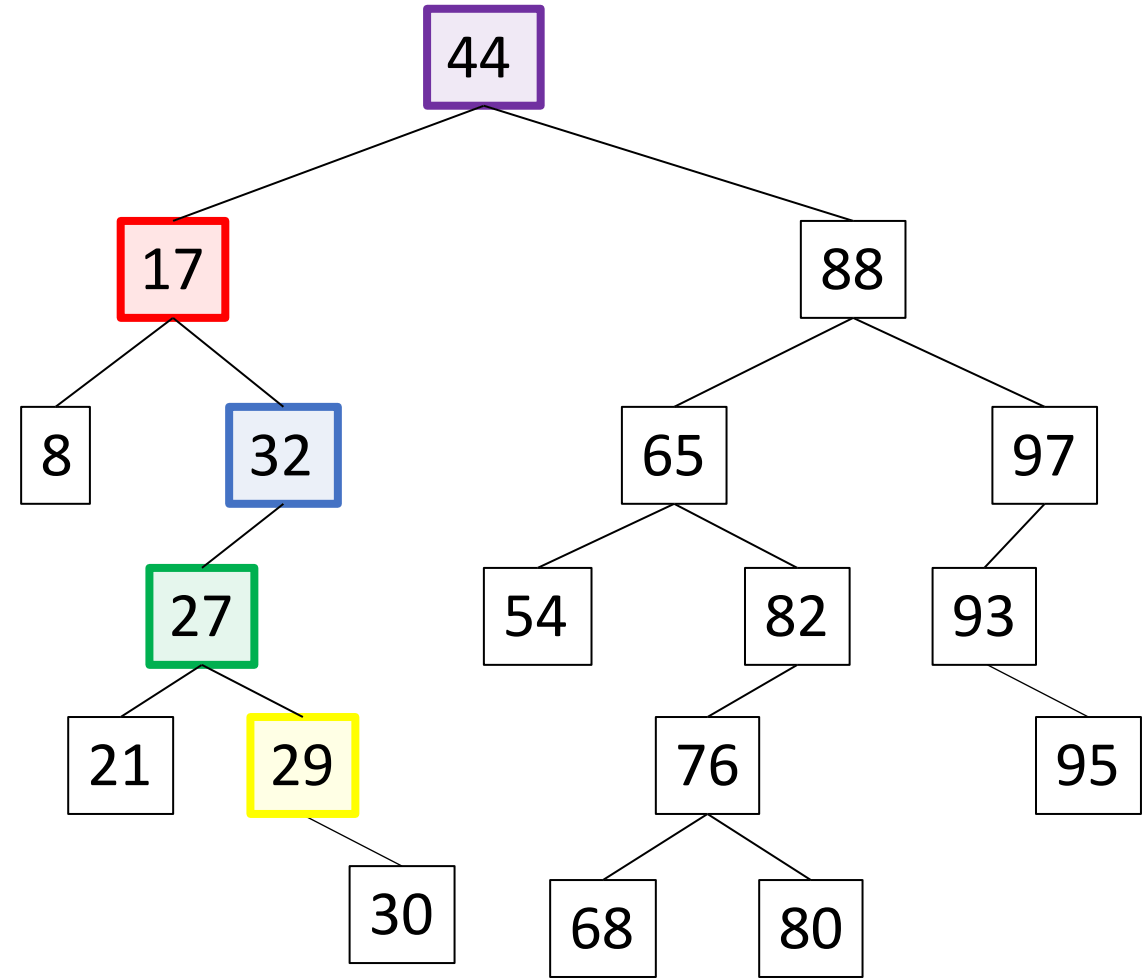
Output:

8

21

Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
        System.out.println(n.getValue());  
    }  
}
```



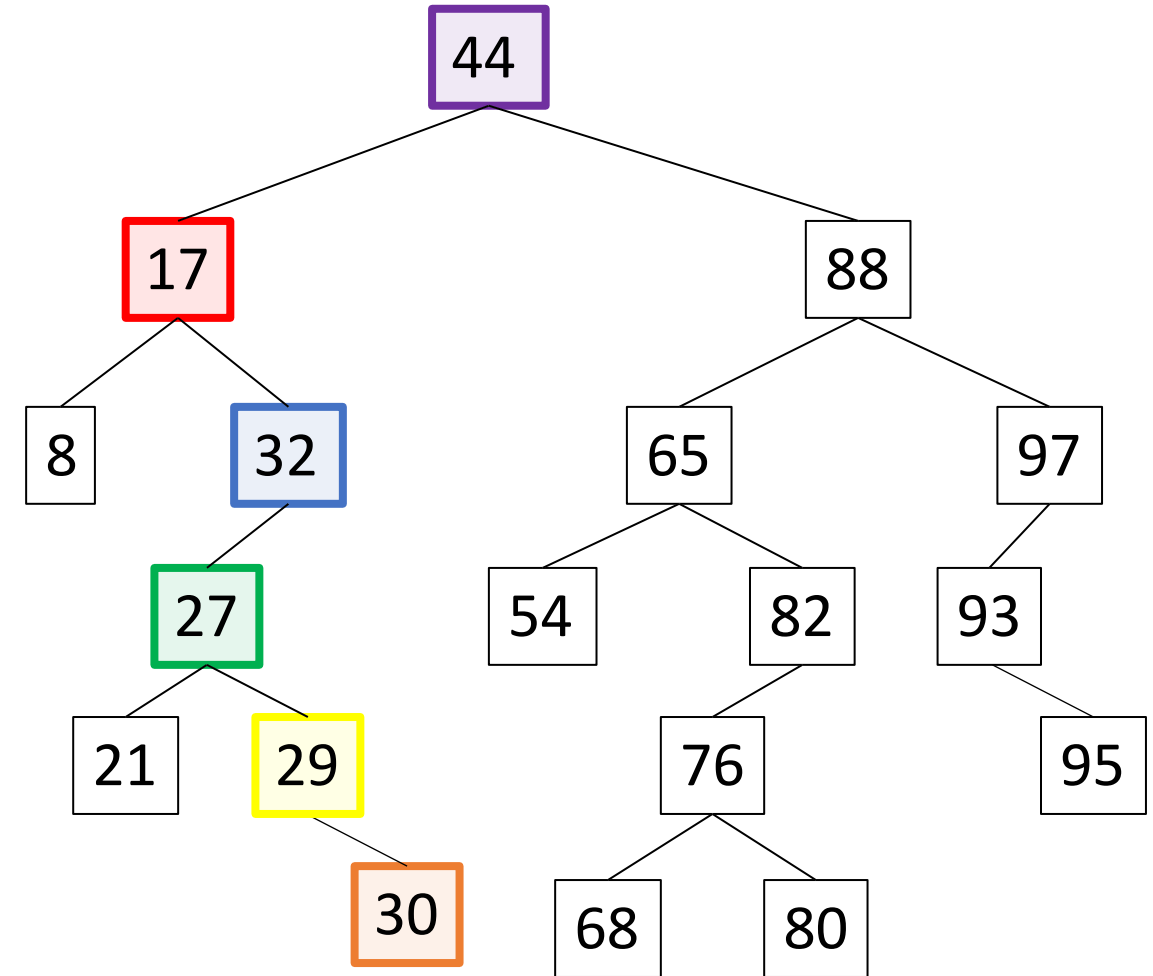
Output:

8

21

Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
        System.out.println(n.getValue());  
    }  
}
```



Binary Search Tree - Traversal

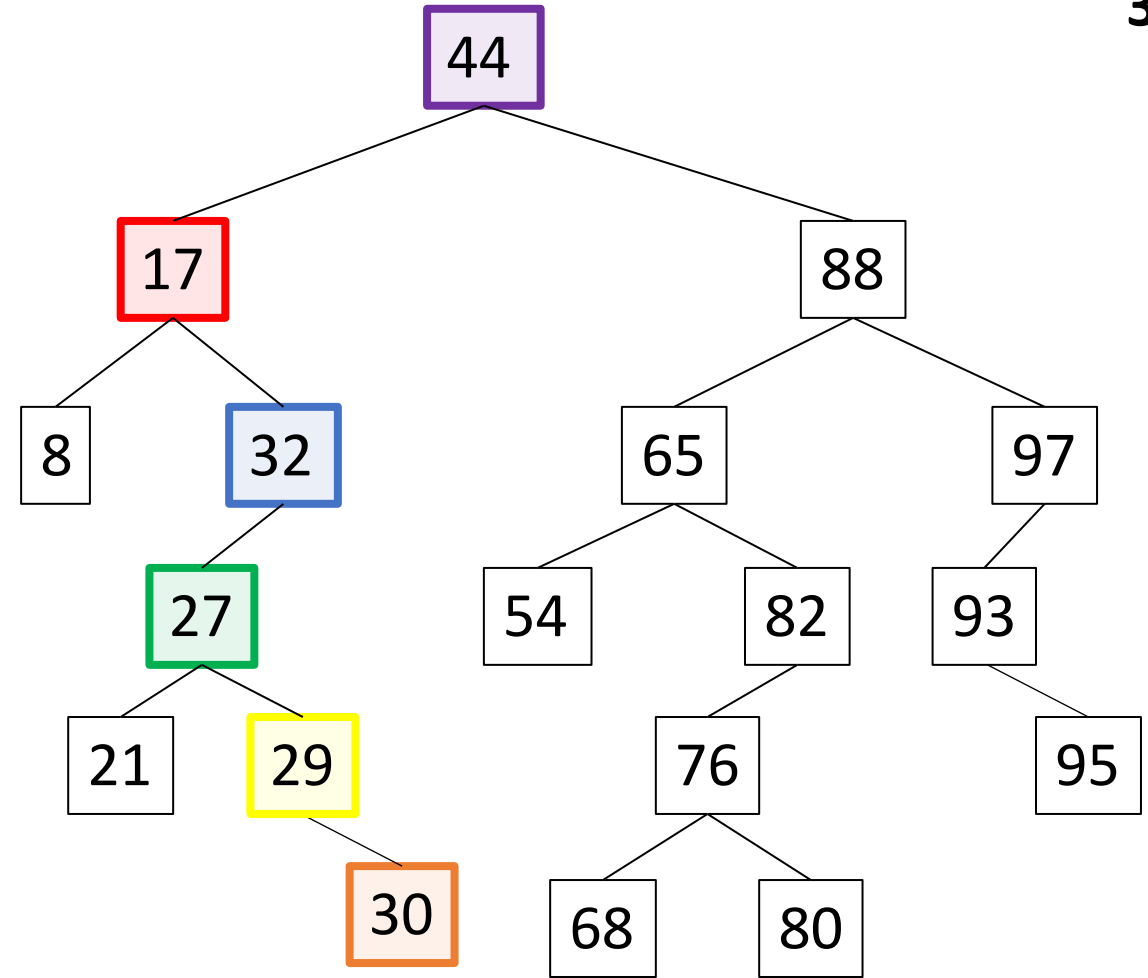
```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
        System.out.println(n.getValue());  
    }  
}
```

Output:

8

21

30



Binary Search Tree - Traversal

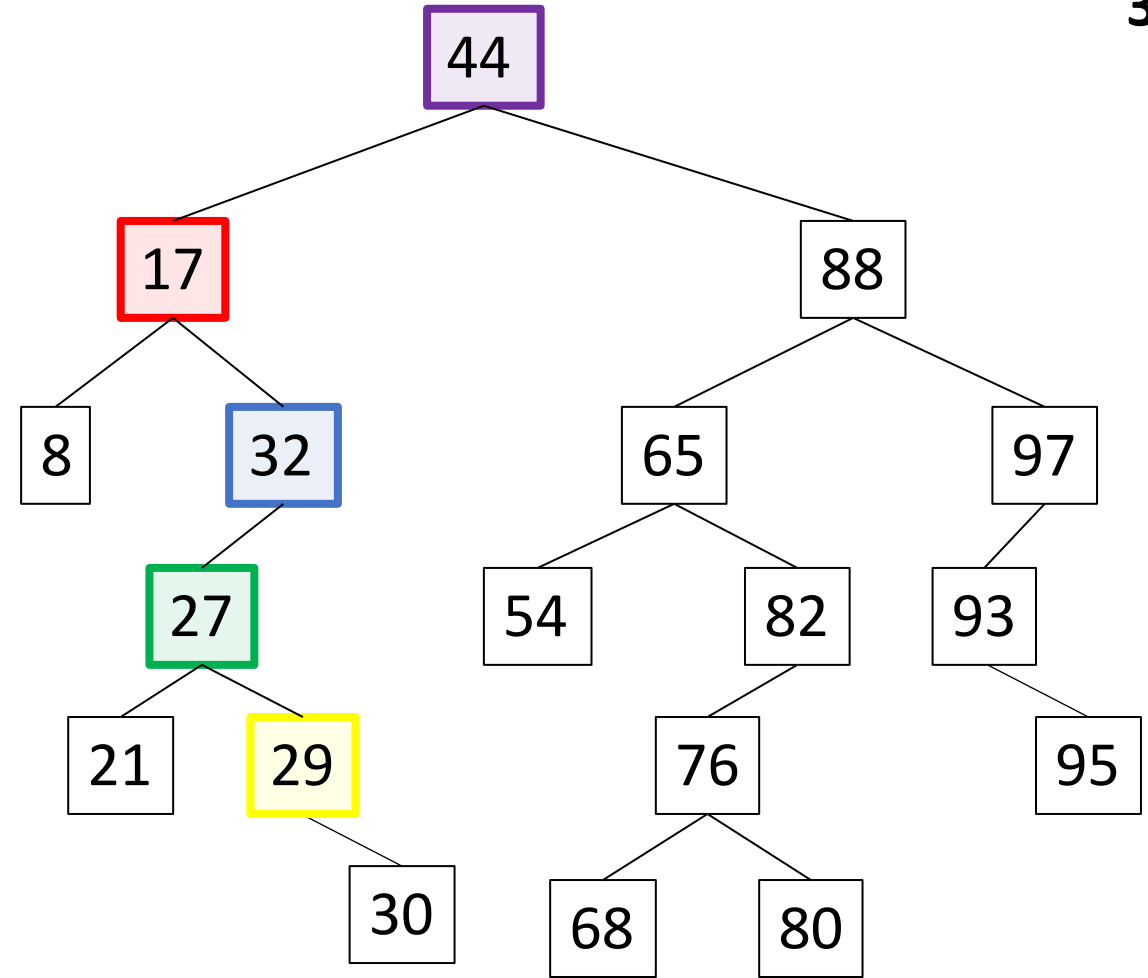
```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
        System.out.println(n.getValue());  
    }  
}
```

Output:

8

21

30



Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
        System.out.println(n.getValue());  
    }  
}
```

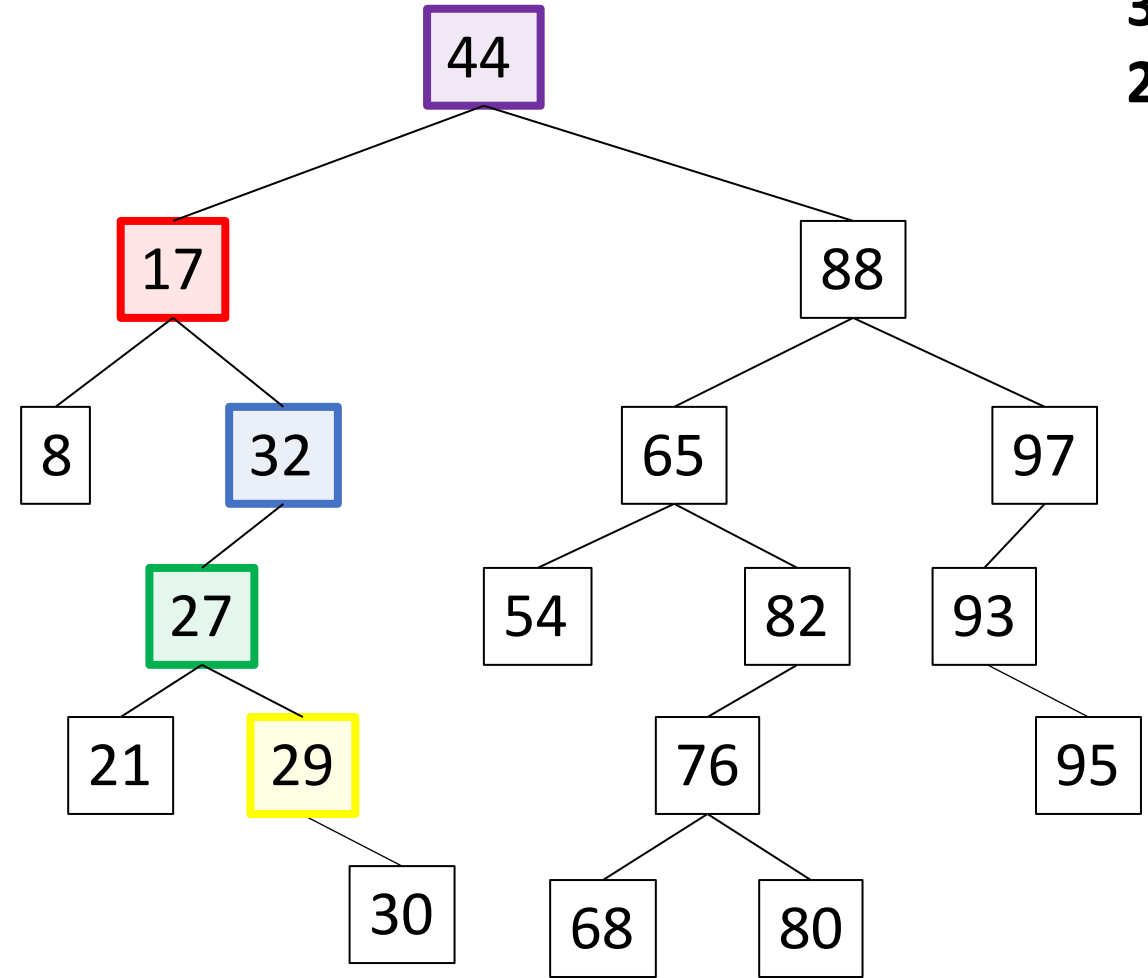
Output:

8

21

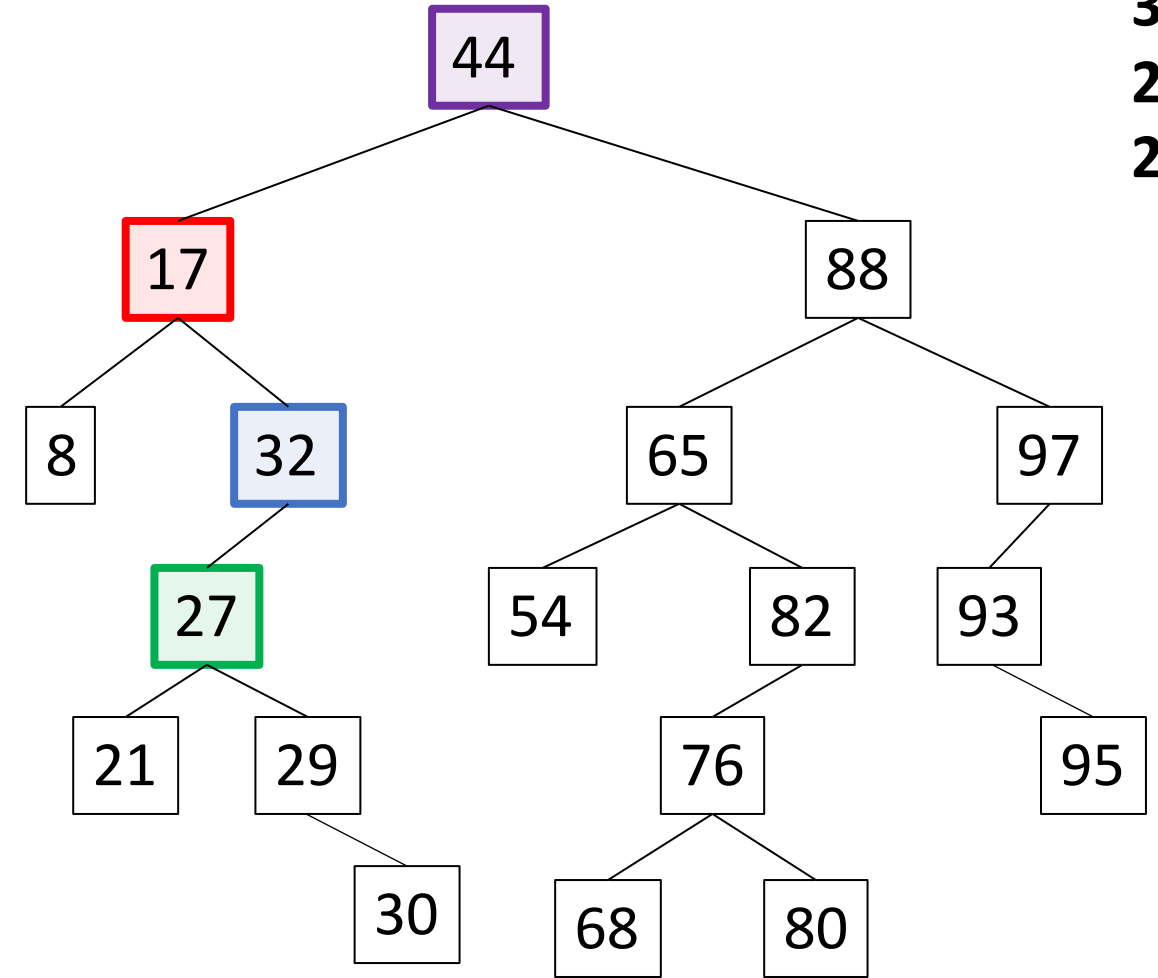
30

29



Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
        System.out.println(n.getValue());  
    }  
}
```



Output:

8

21

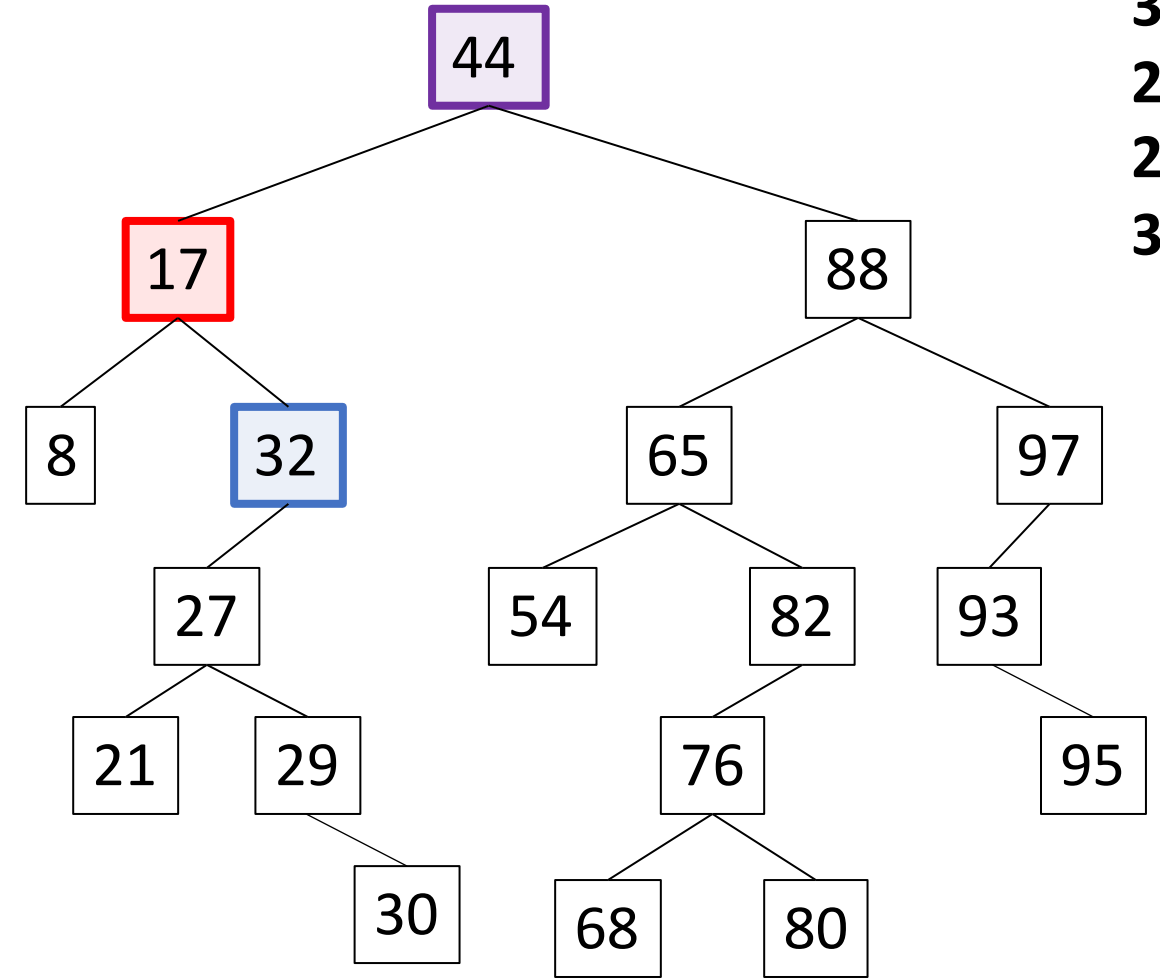
30

29

27

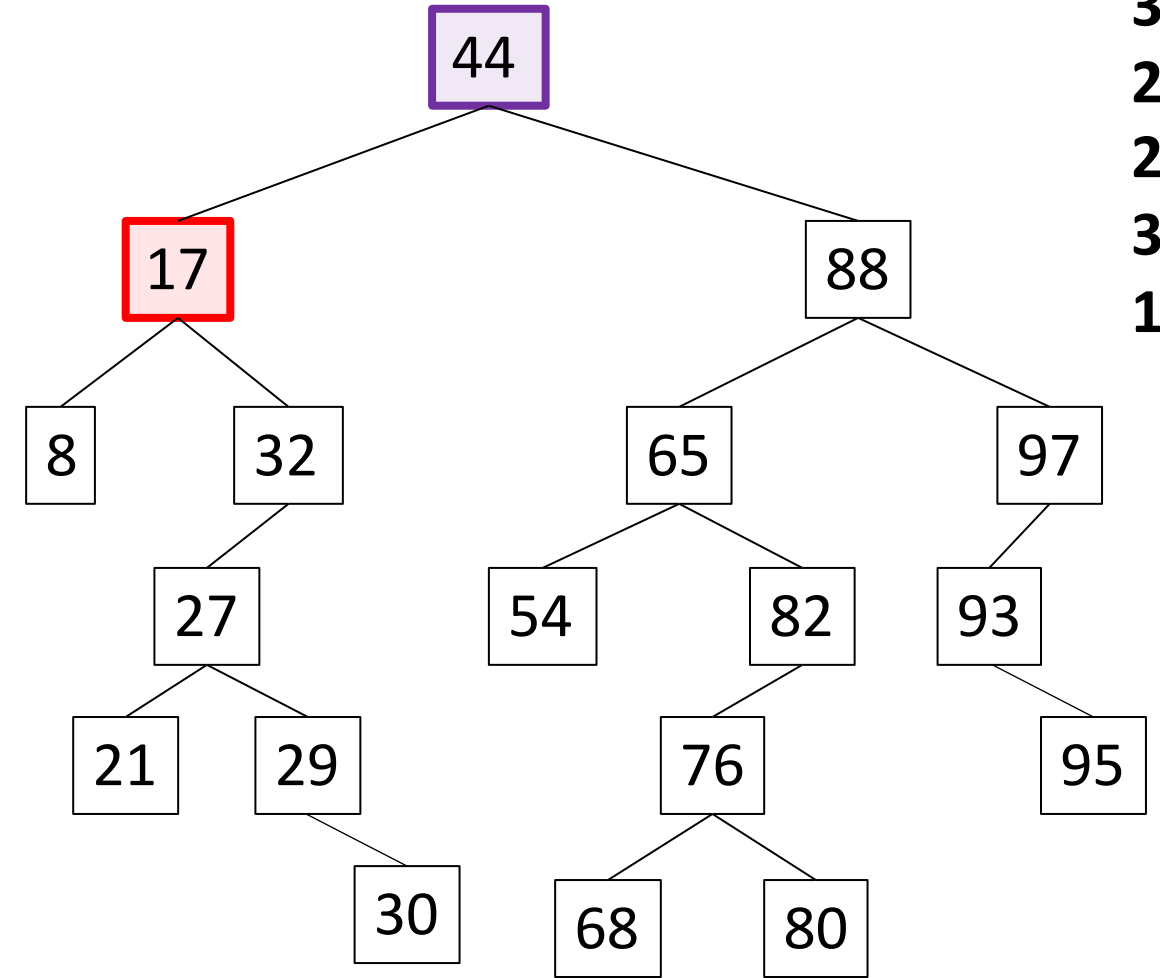
Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
        System.out.println(n.getValue());  
    }  
}
```



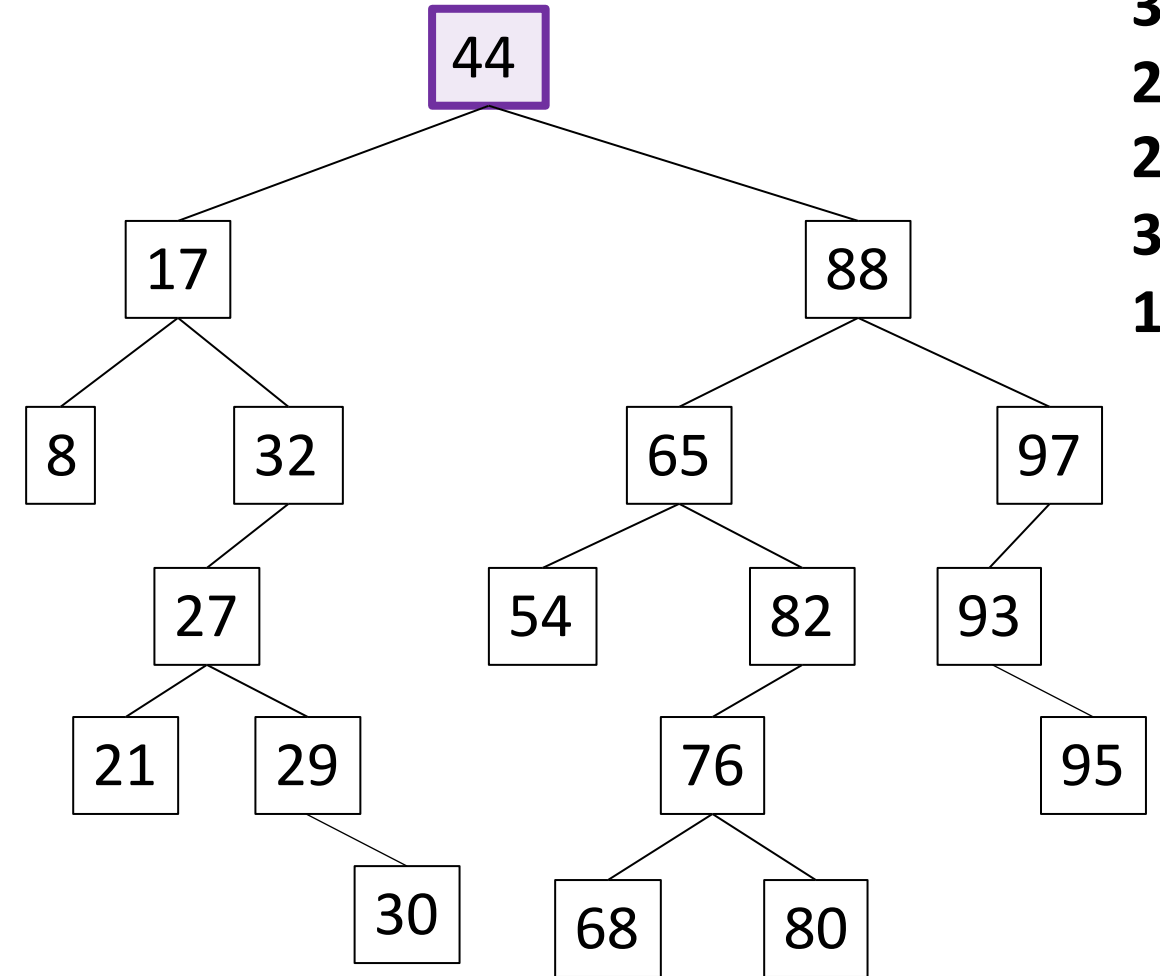
Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
        System.out.println(n.getValue());  
    }  
}
```



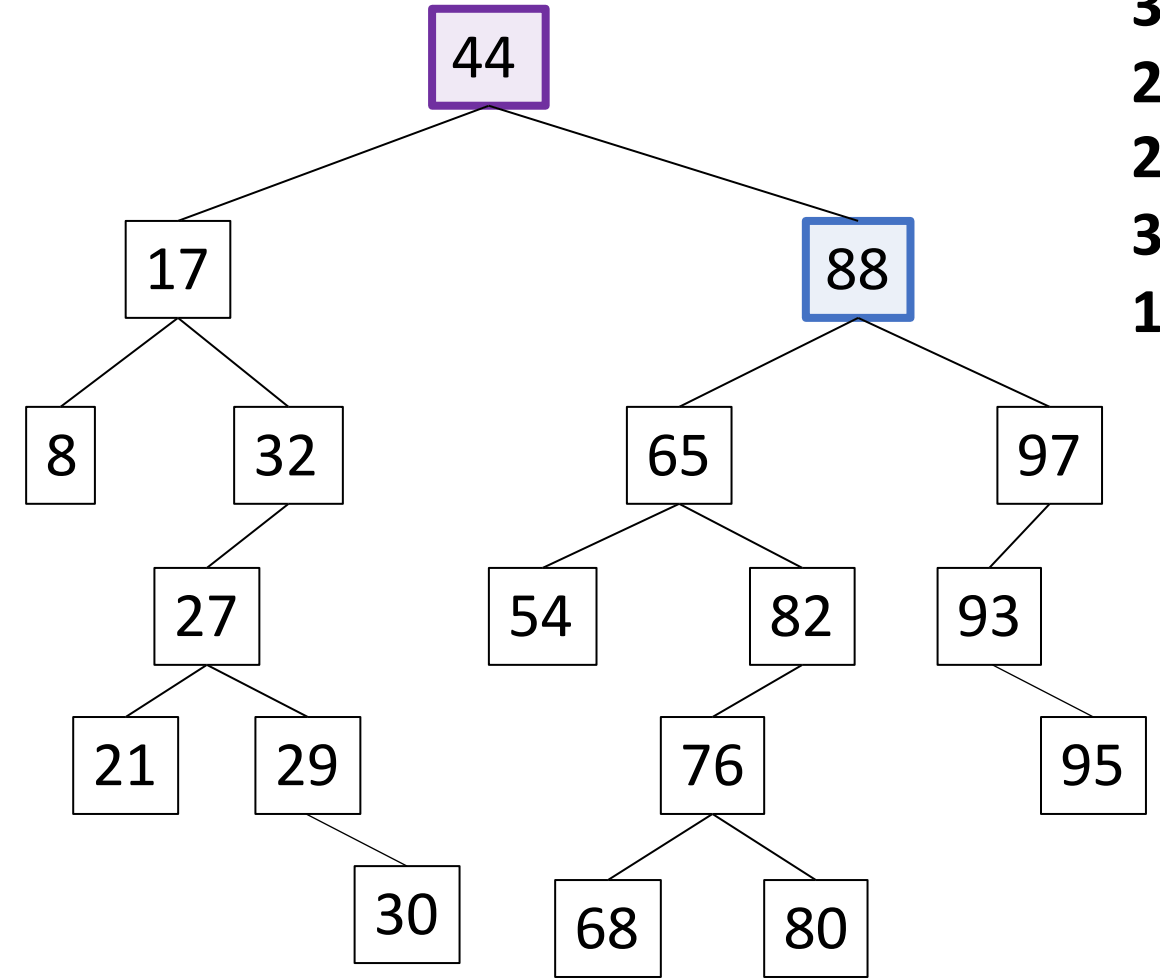
Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
        System.out.println(n.getValue());  
    }  
}
```



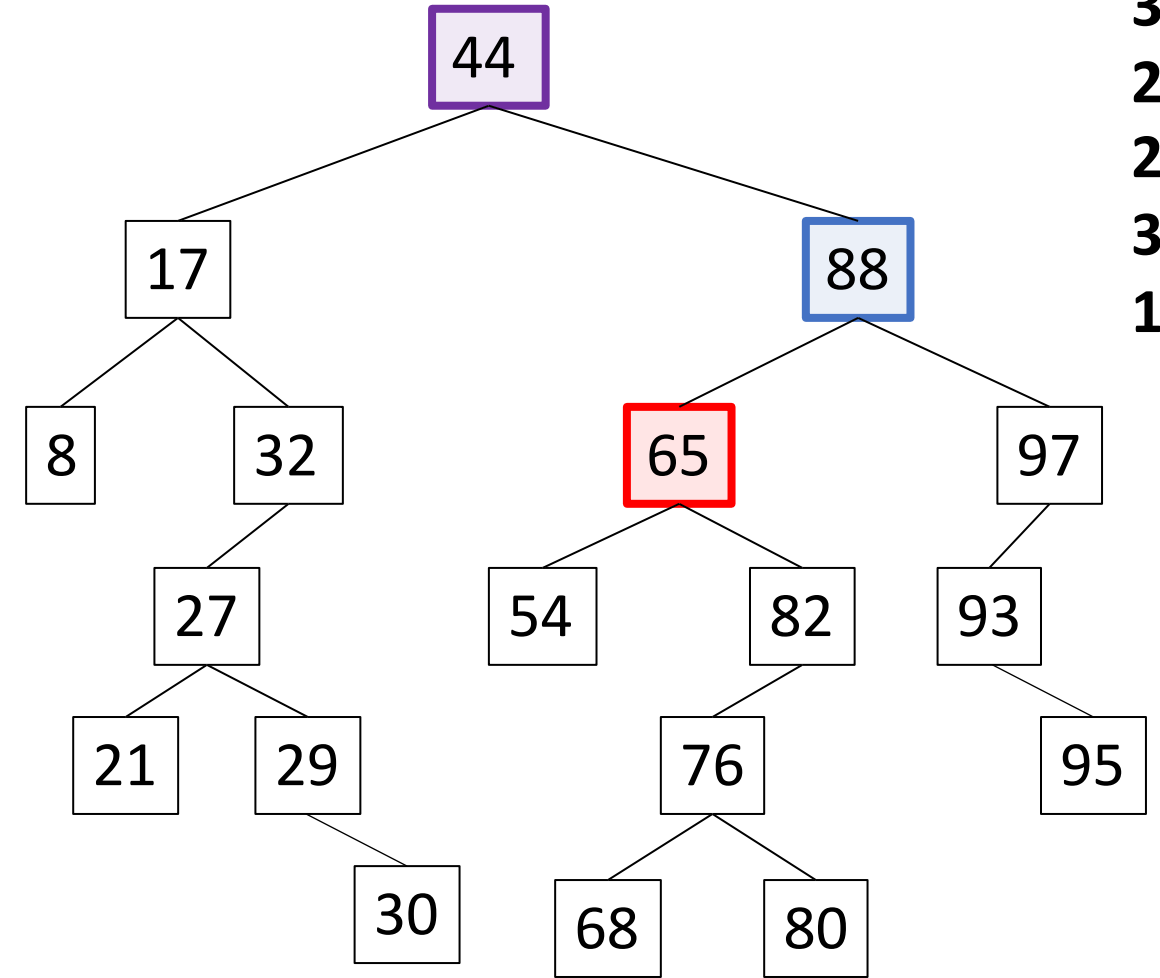
Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
        System.out.println(n.getValue());  
    }  
}
```



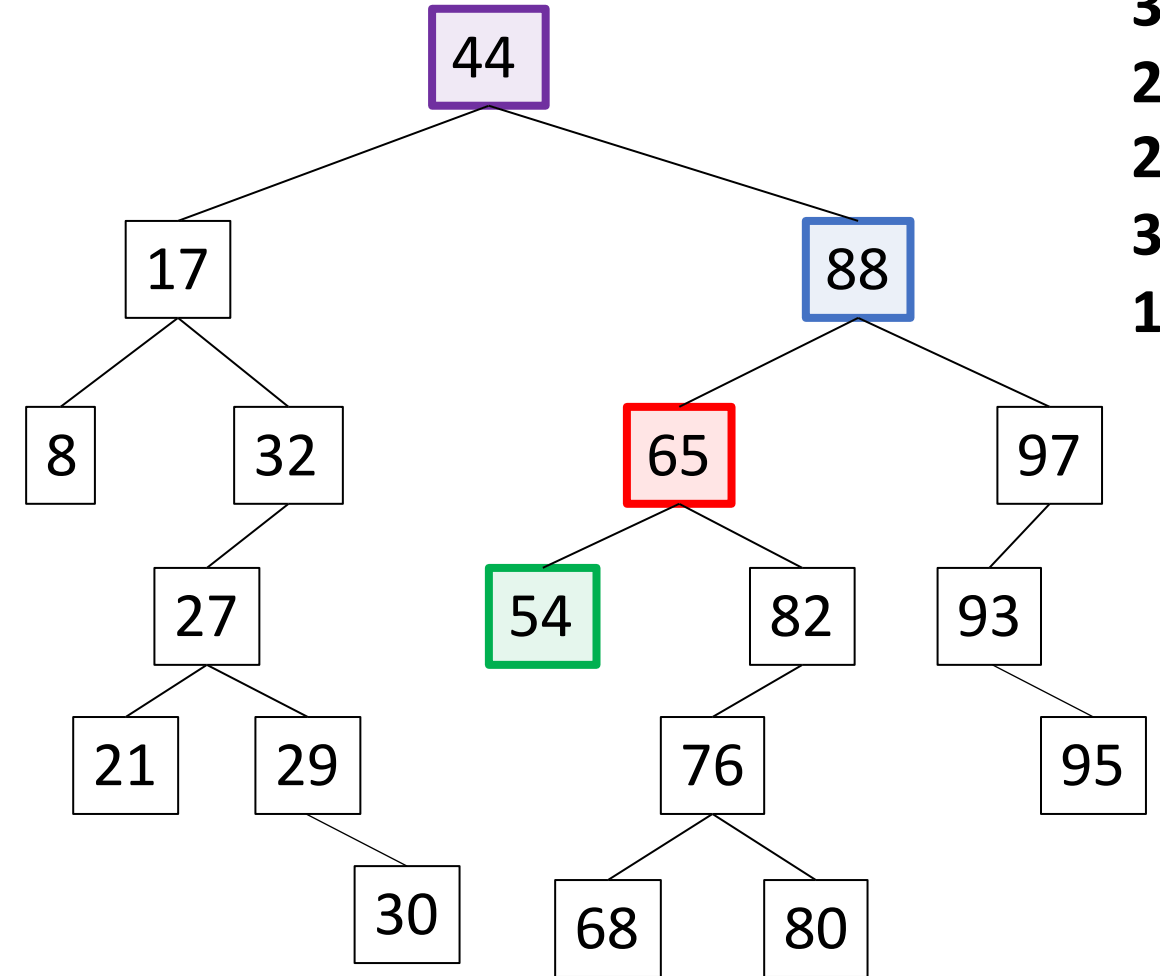
Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
        System.out.println(n.getValue());  
    }  
}
```



Binary Search Tree - Traversal

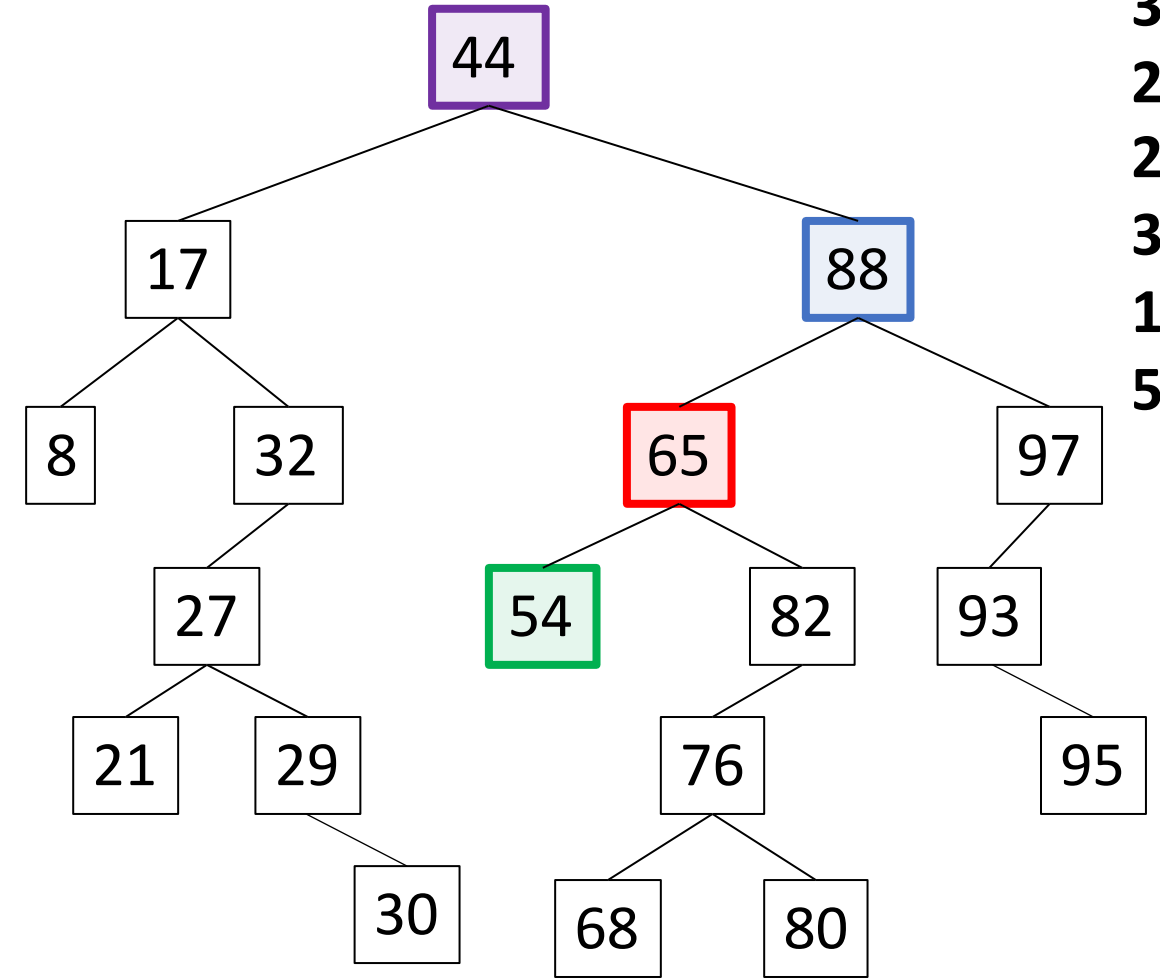
```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
        System.out.println(n.getValue());  
    }  
}
```



Output:
8
21
30
29
27
32
17

Binary Search Tree - Traversal

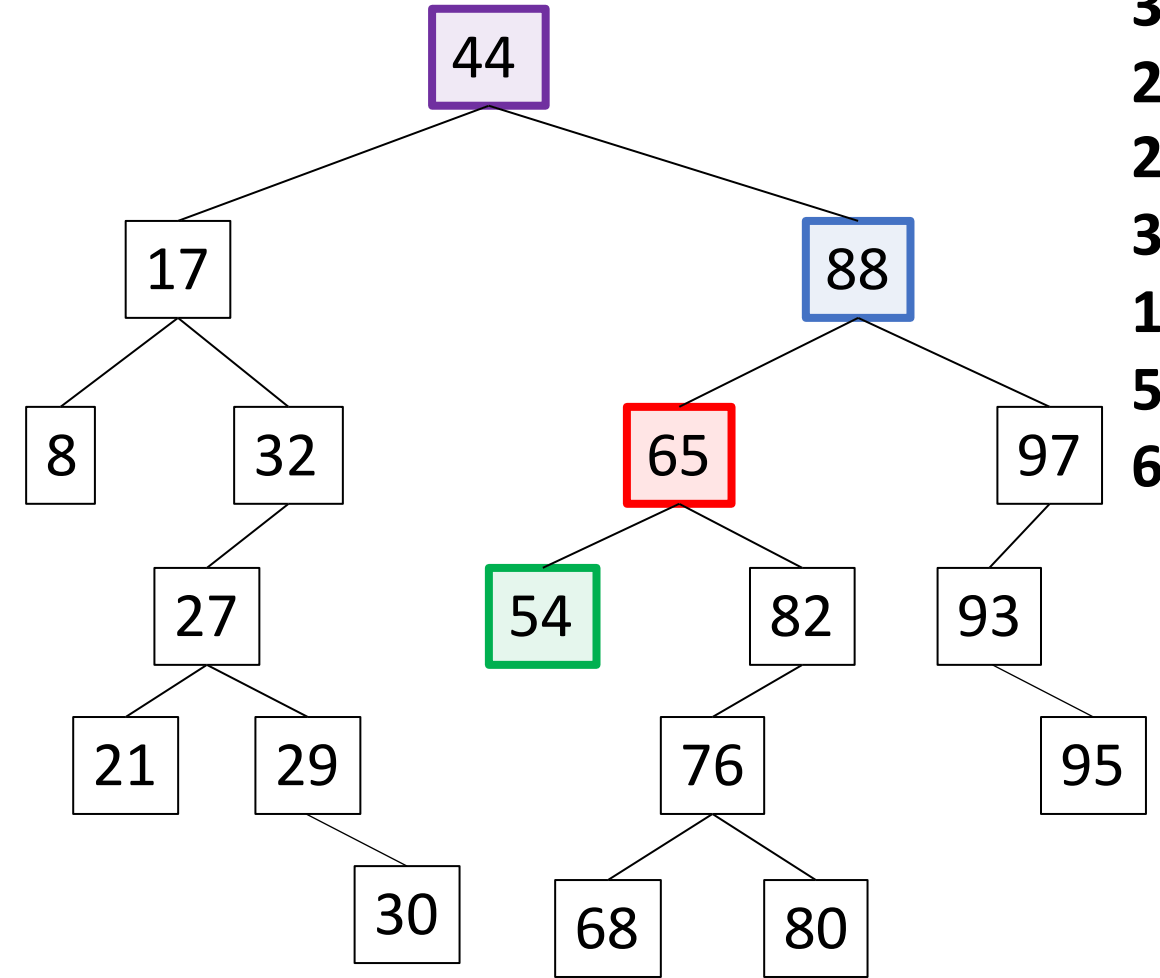
```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
        System.out.println(n.getValue());  
    }  
}
```



Output:
8
21
30
29
27
32
17
54

Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
        System.out.println(n.getValue());  
    }  
}
```

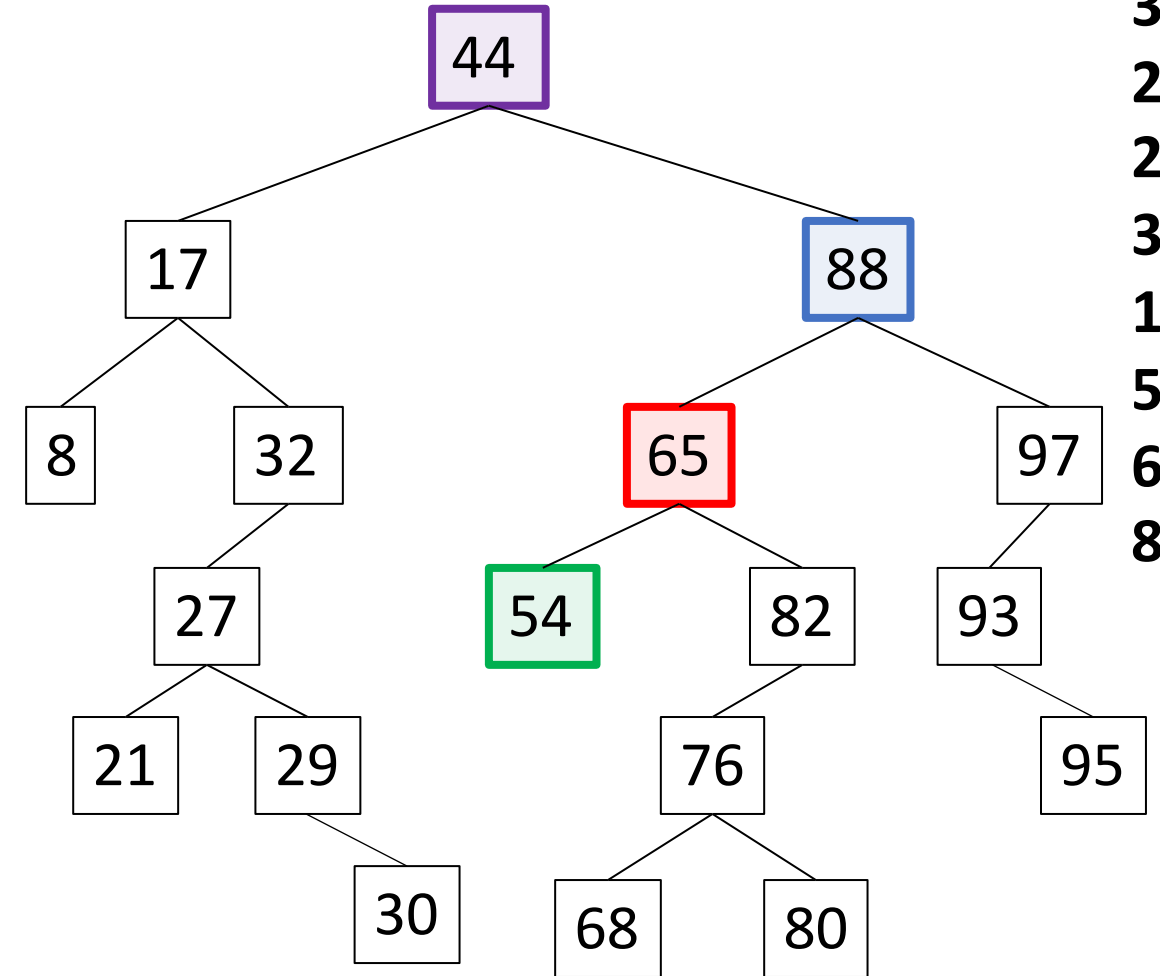


Output:

8
21
30
29
27
32
17
54
68

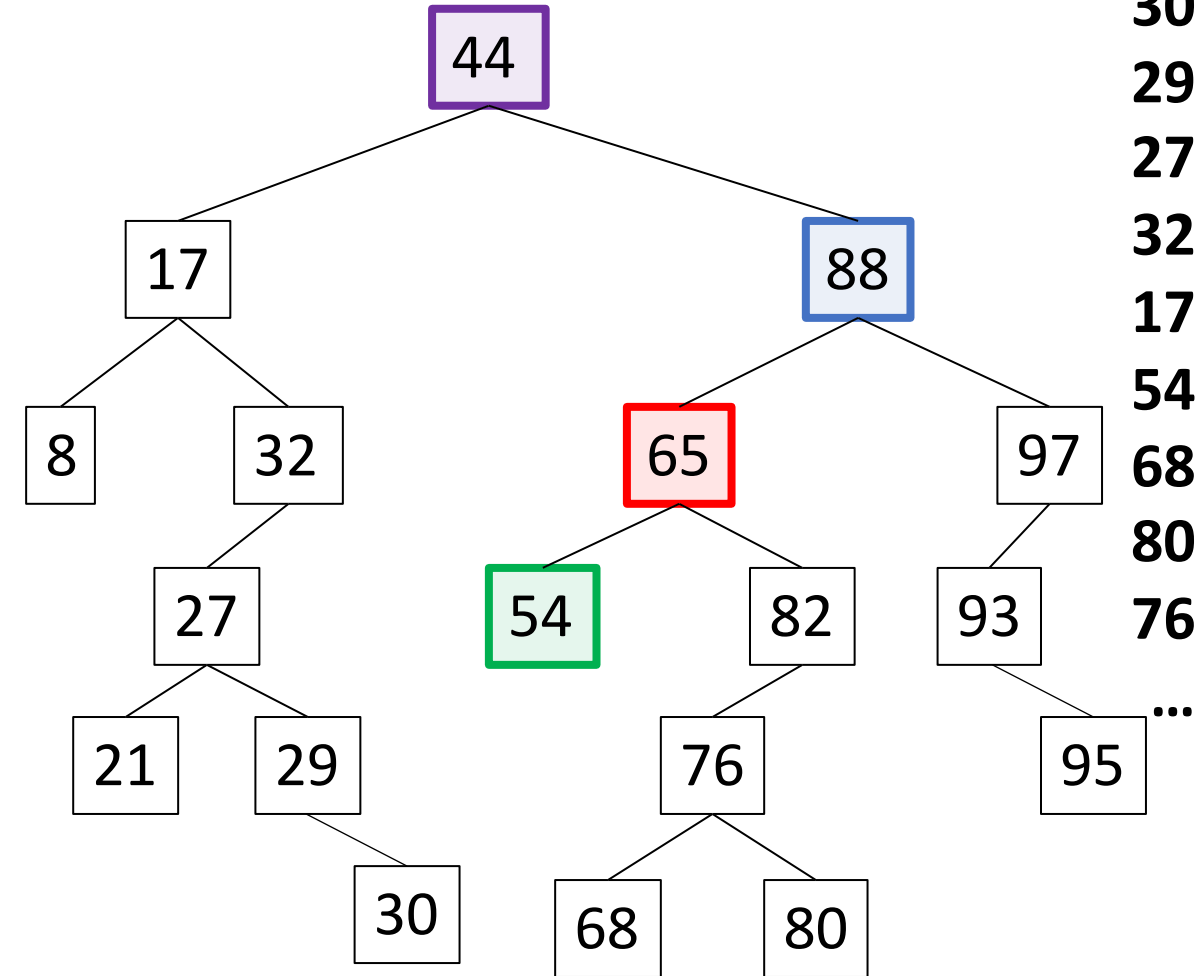
Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
        System.out.println(n.getValue());  
    }  
}
```



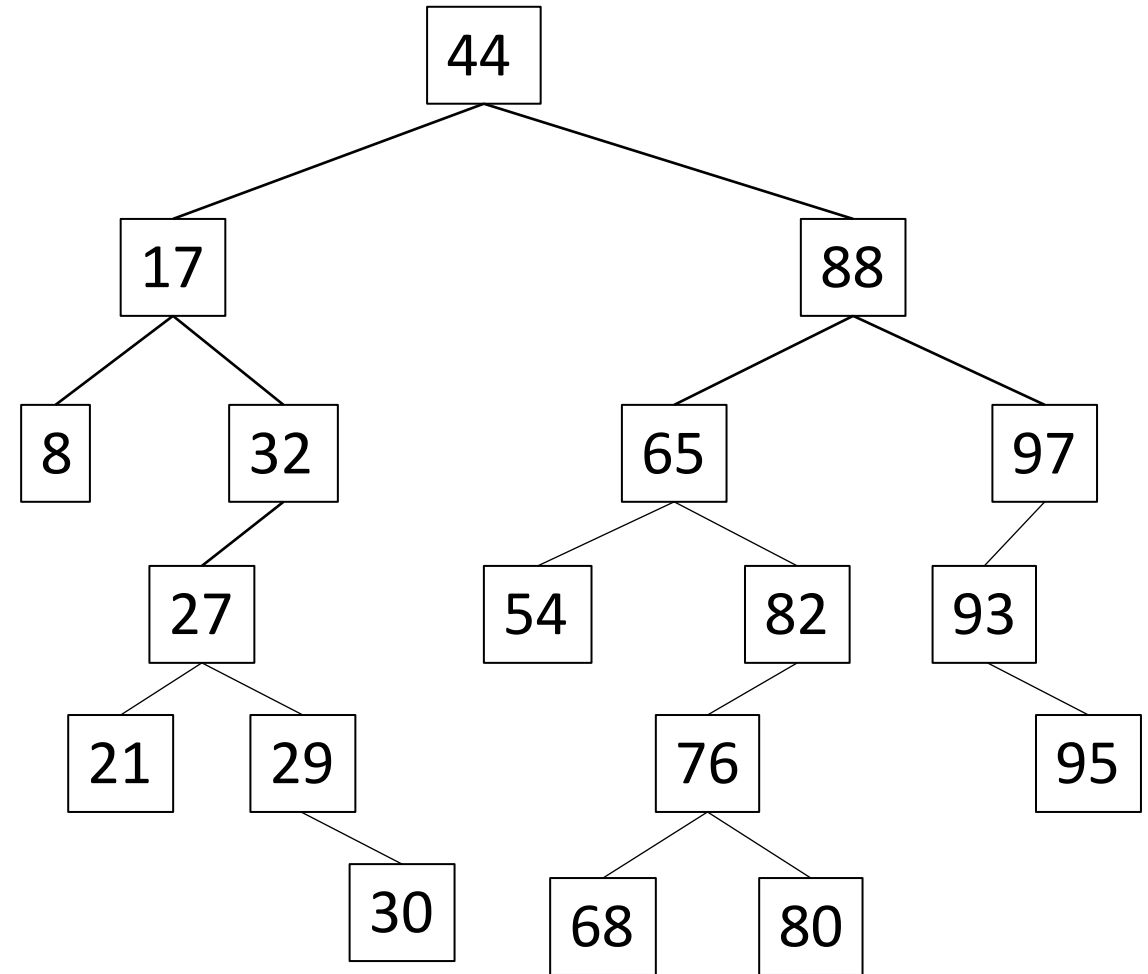
Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        depthFirst(n.getRight());  
        System.out.println(n.getValue());  
    }  
}
```



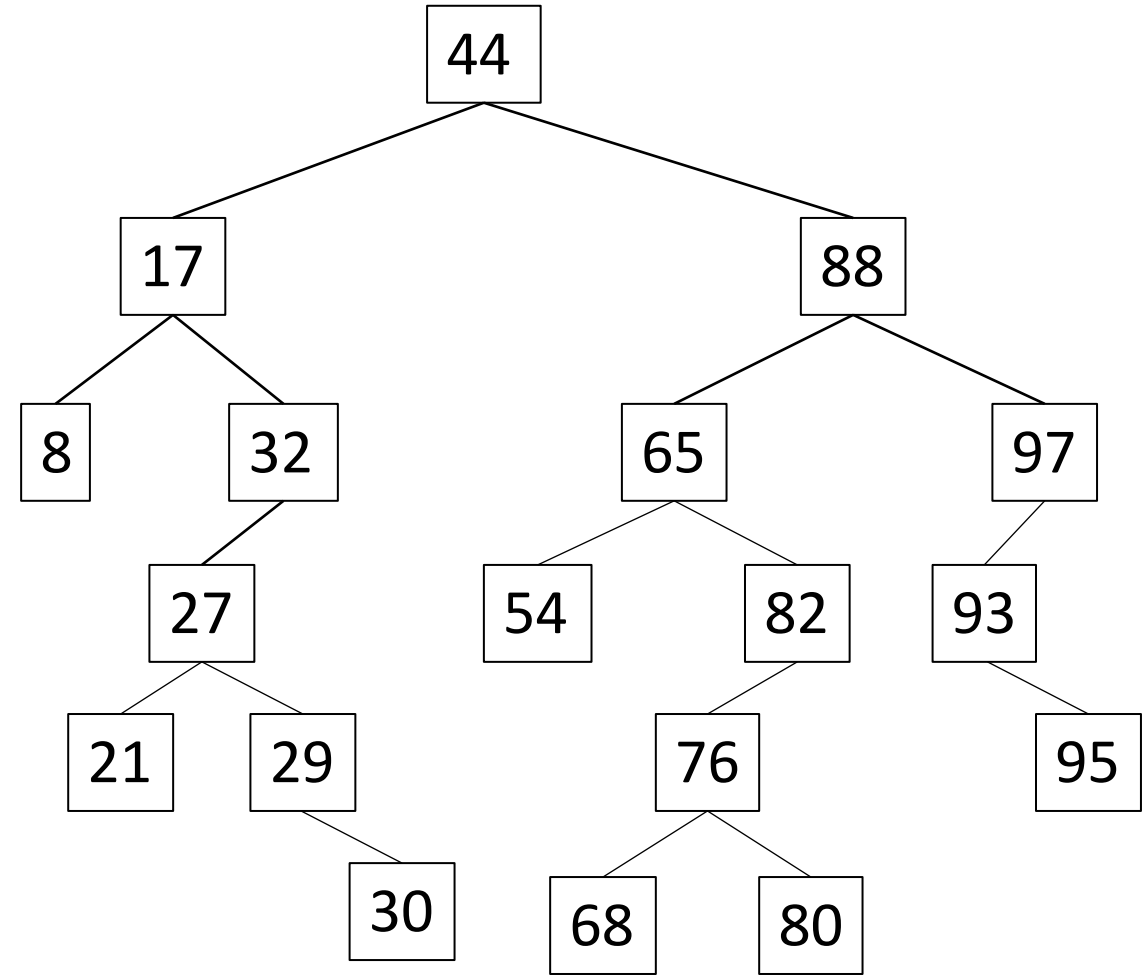
Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        System.out.println(n.getValue());  
        depthFirst(n.getRight());  
    }  
}
```



Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        System.out.println(n.getValue());  
        depthFirst(n.getRight());  
    }  
}
```



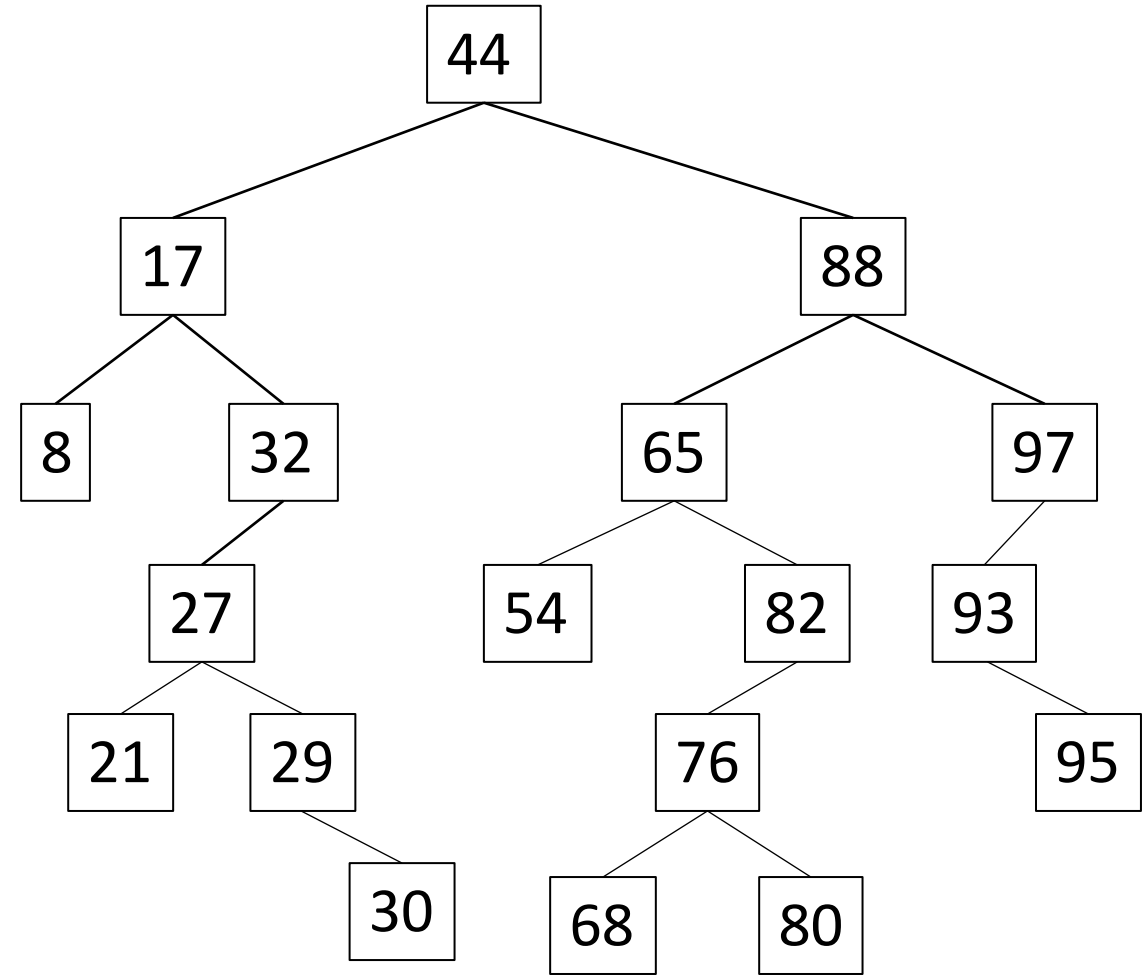
Output:

8

17

Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        System.out.println(n.getValue());  
        depthFirst(n.getRight());  
    }  
}
```

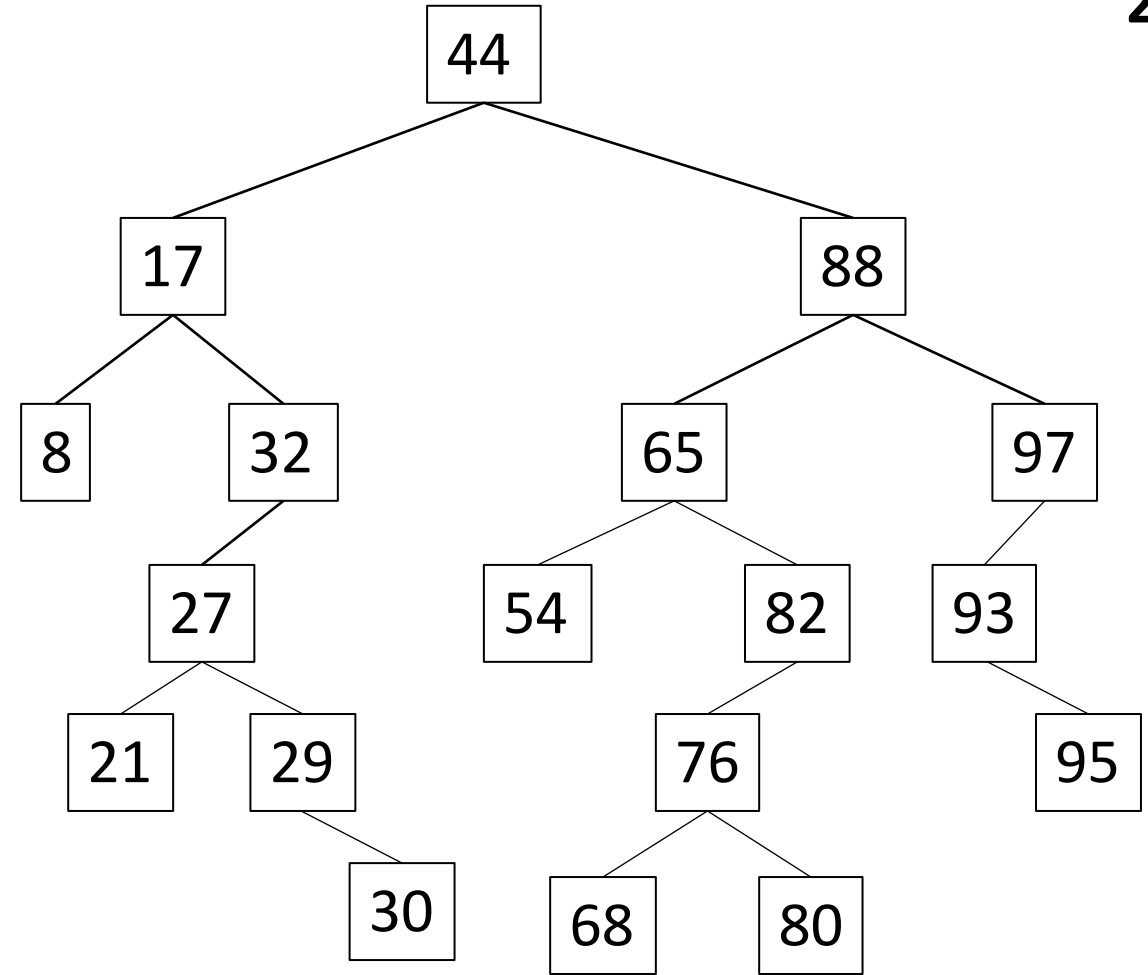


Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        System.out.println(n.getValue());  
        depthFirst(n.getRight());  
    }  
}
```

Output:

**8
17
21**

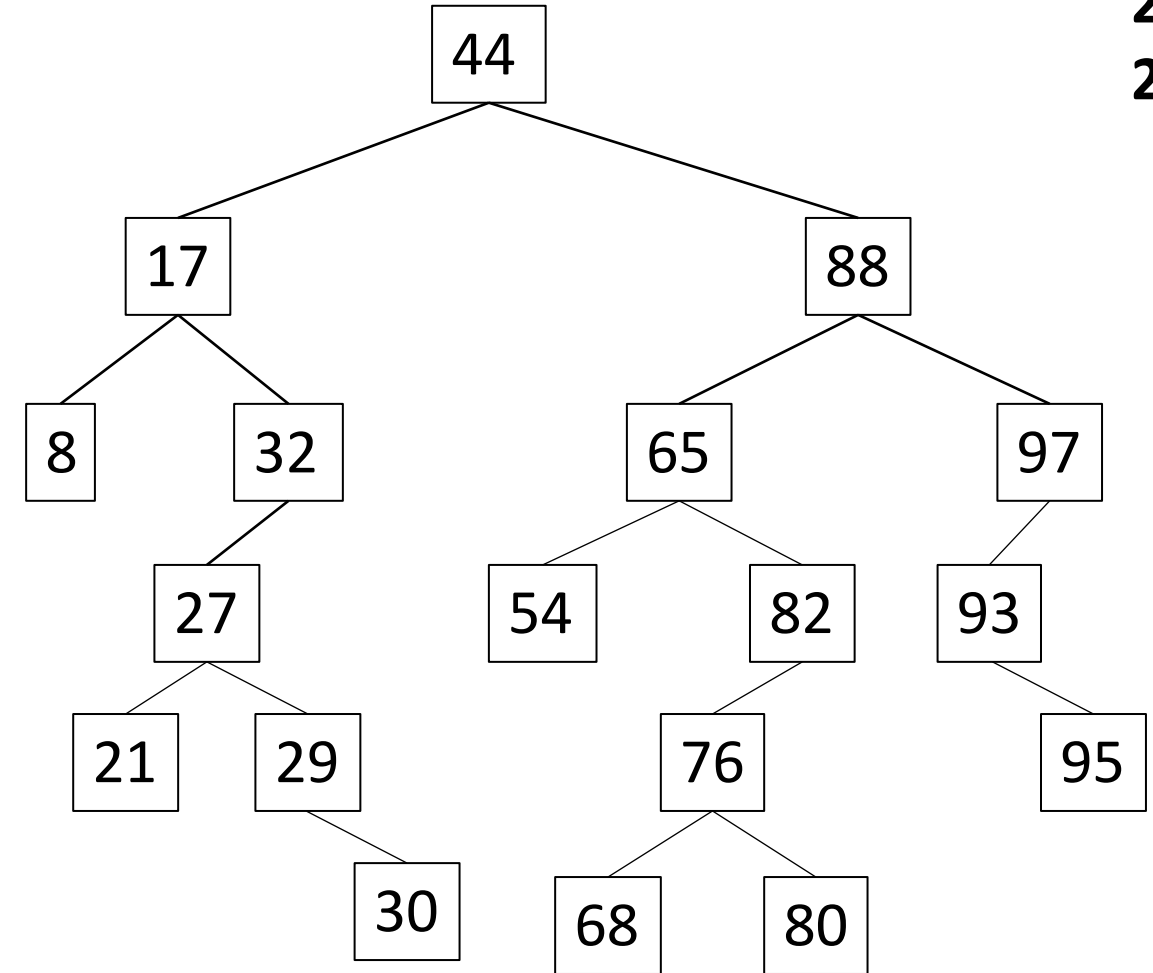


Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        System.out.println(n.getValue());  
        depthFirst(n.getRight());  
    }  
}
```

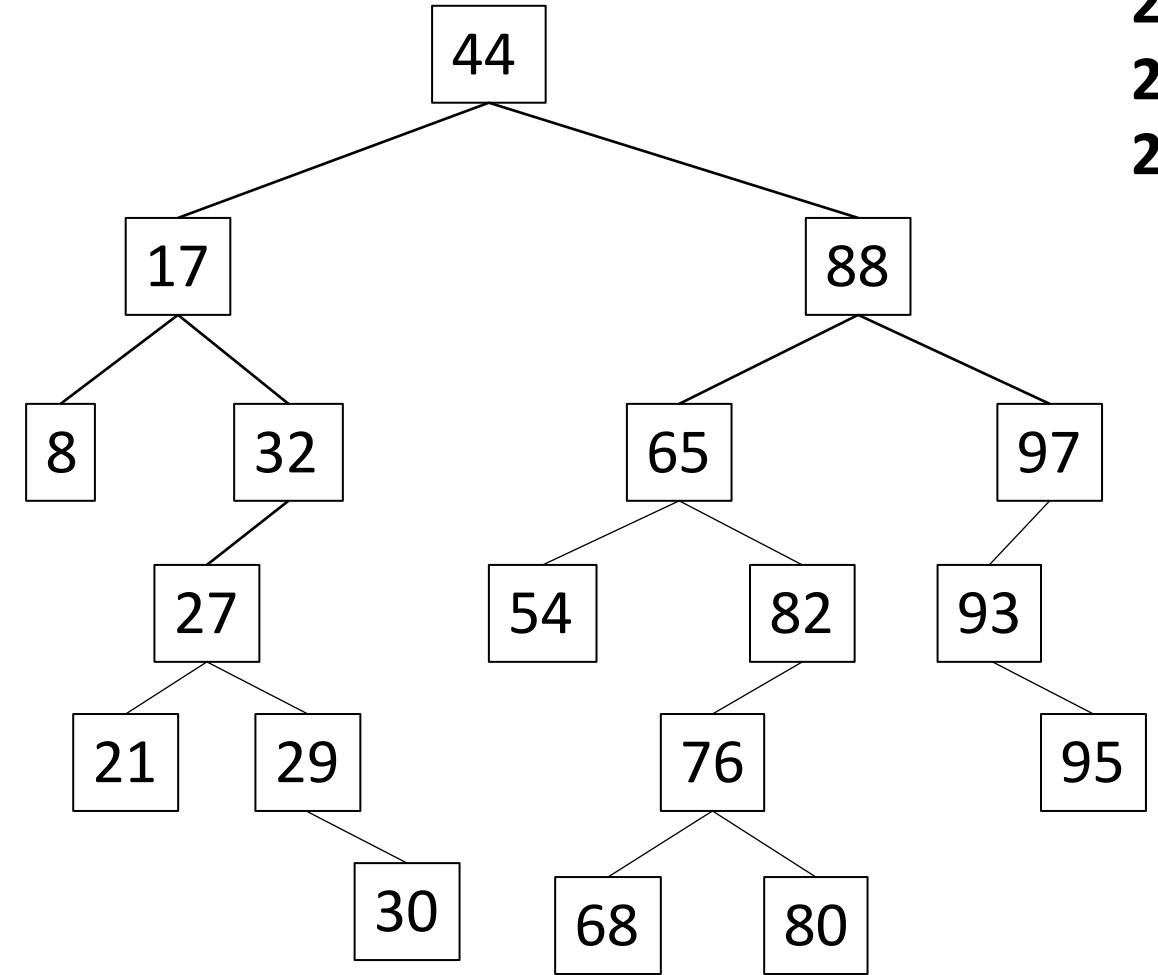
Output:

8
17
21
27



Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        System.out.println(n.getValue());  
        depthFirst(n.getRight());  
    }  
}
```



Output:

8

17

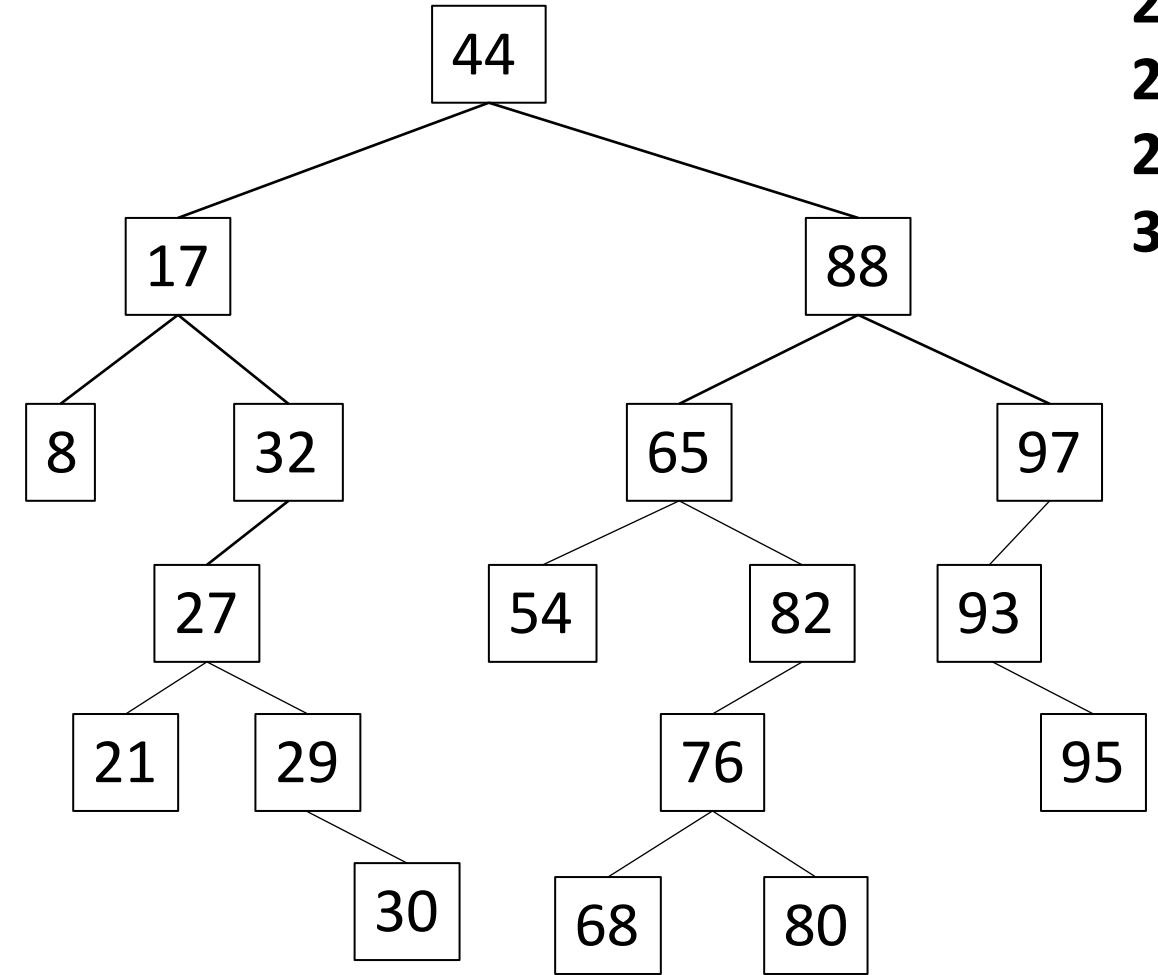
21

27

29

Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        System.out.println(n.getValue());  
        depthFirst(n.getRight());  
    }  
}
```



Output:

8

17

21

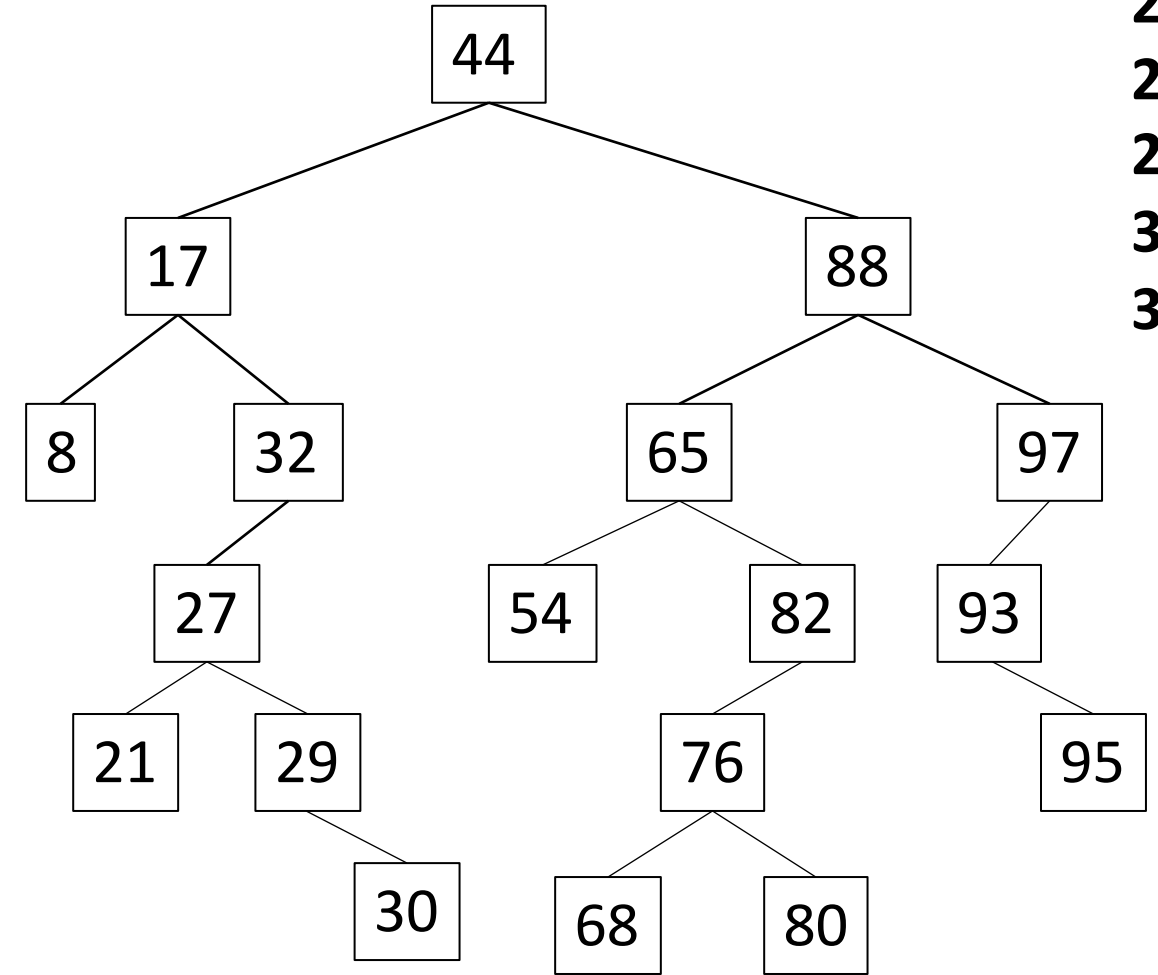
27

29

30

Binary Search Tree - Traversal

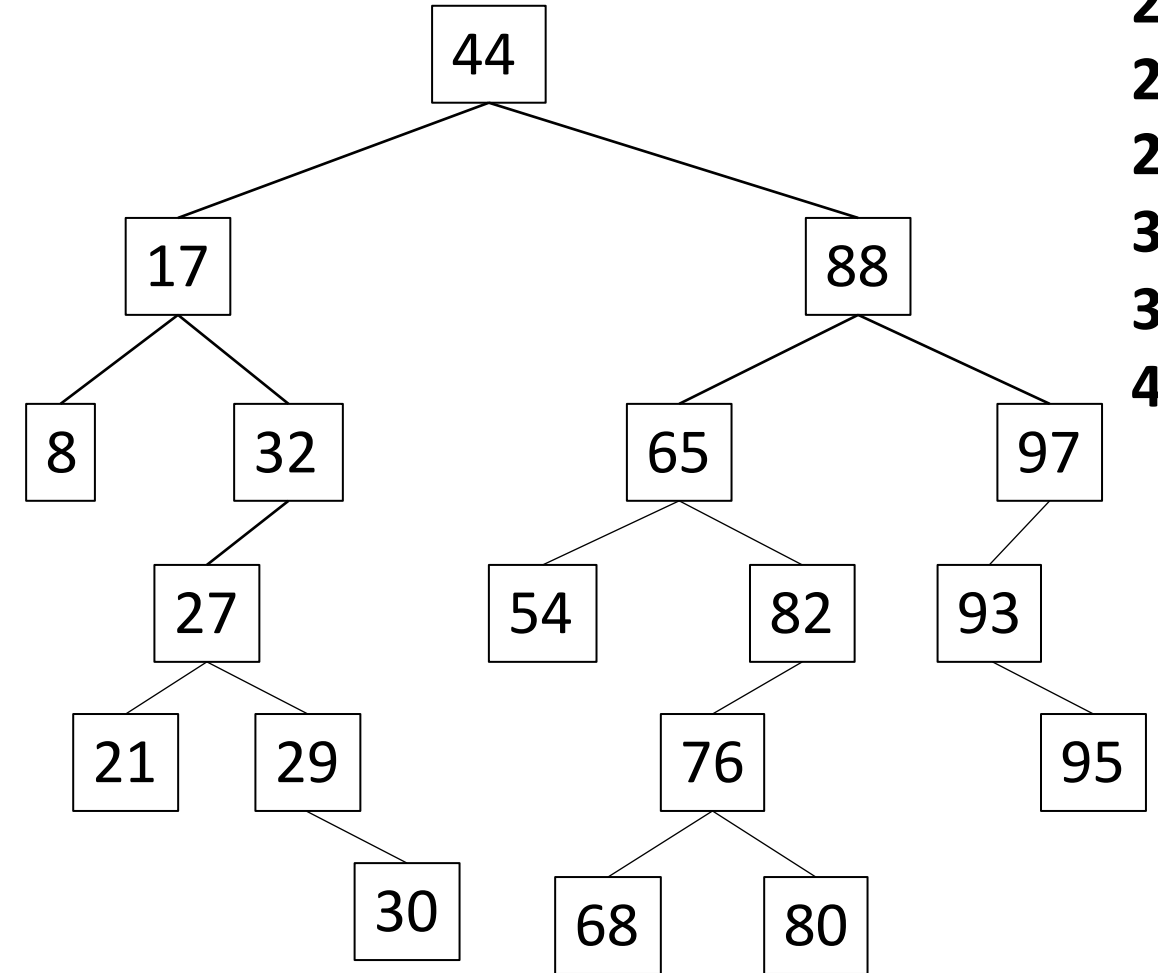
```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        System.out.println(n.getValue());  
        depthFirst(n.getRight());  
    }  
}
```



Output:
8
17
21
27
29
30
32

Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        System.out.println(n.getValue());  
        depthFirst(n.getRight());  
    }  
}
```

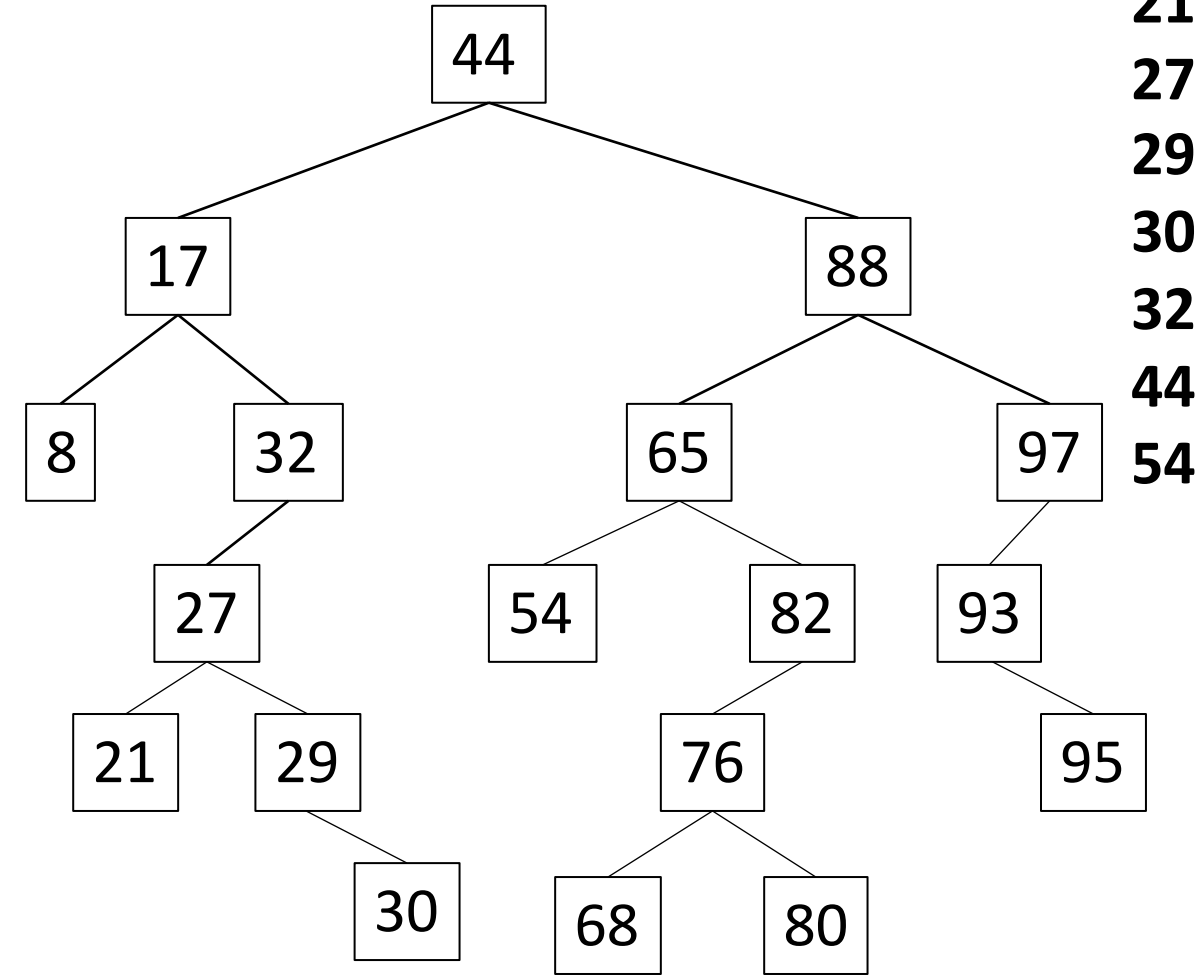


Output:

8
17
21
27
29
30
32
44

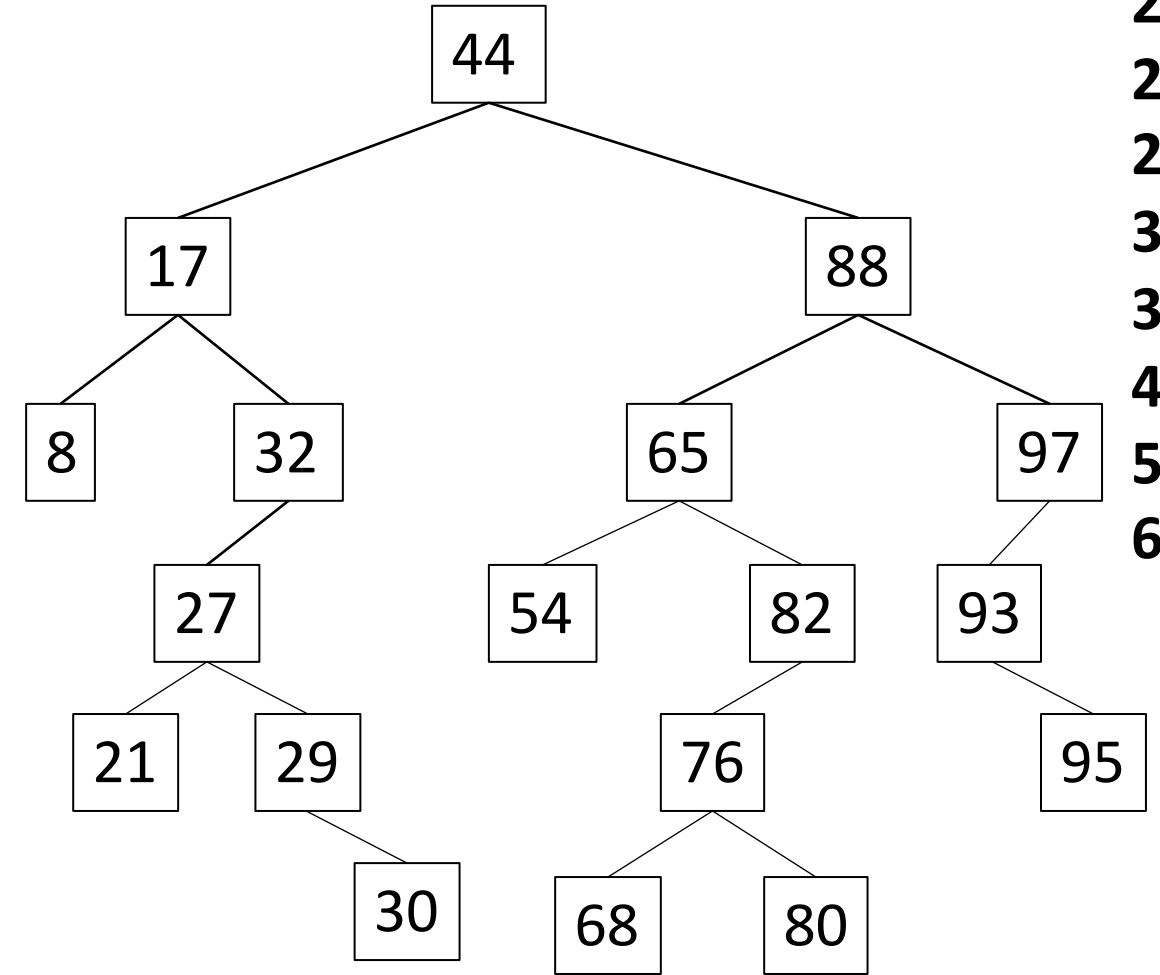
Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        System.out.println(n.getValue());  
        depthFirst(n.getRight());  
    }  
}
```



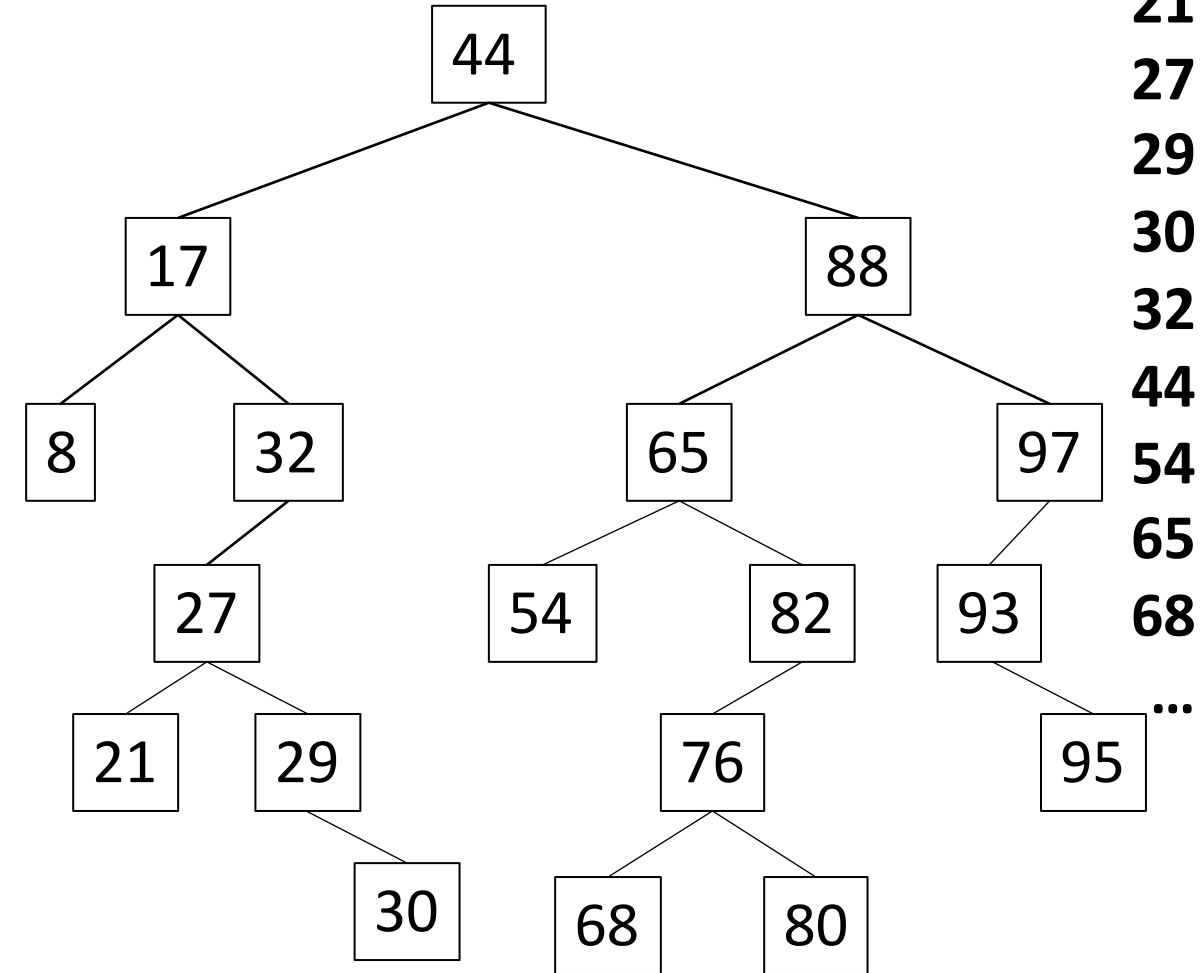
Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        System.out.println(n.getValue());  
        depthFirst(n.getRight());  
    }  
}
```



Binary Search Tree - Traversal

```
public void depthFirst(Node n) {  
    if (n != null) {  
        depthFirst(n.getLeft());  
        System.out.println(n.getValue());  
        depthFirst(n.getRight());  
    }  
}
```

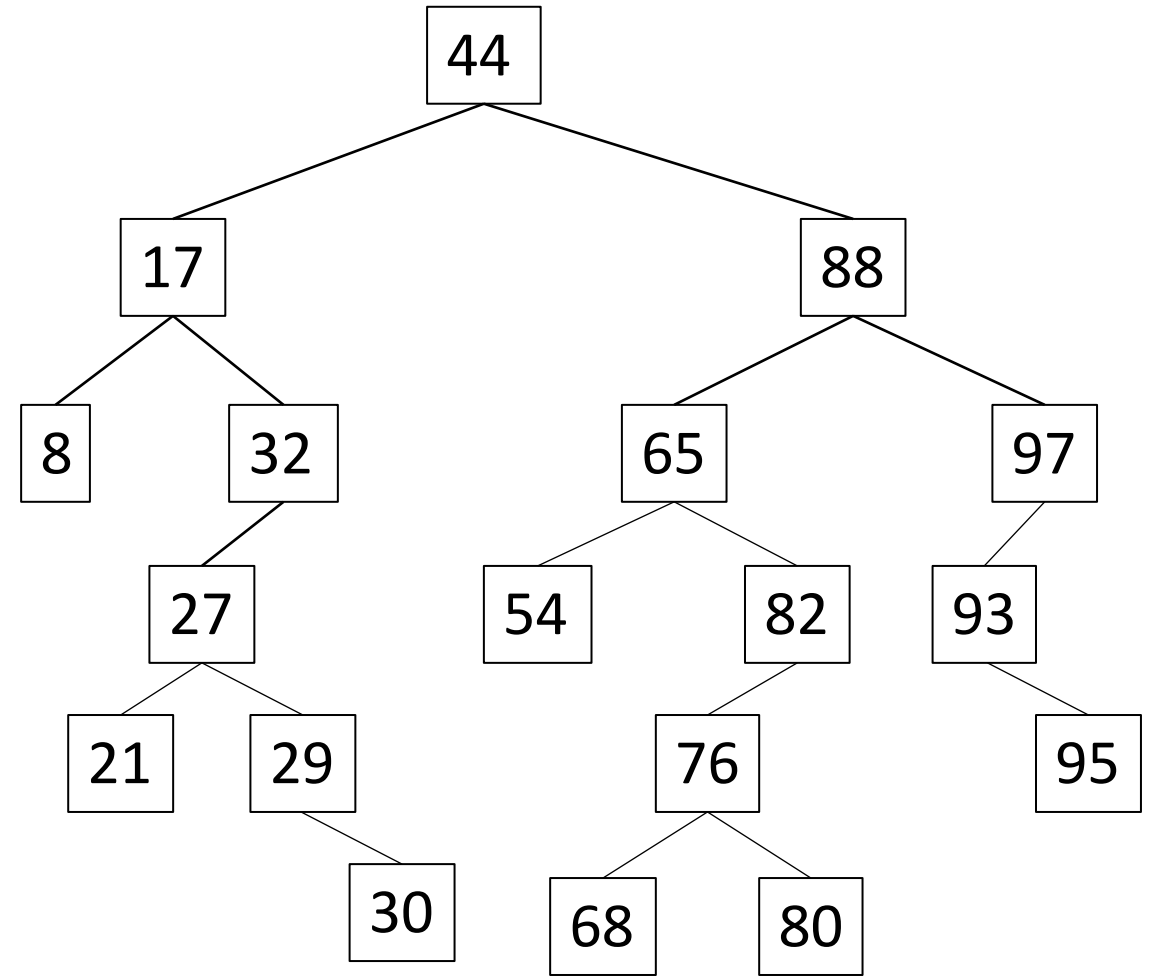


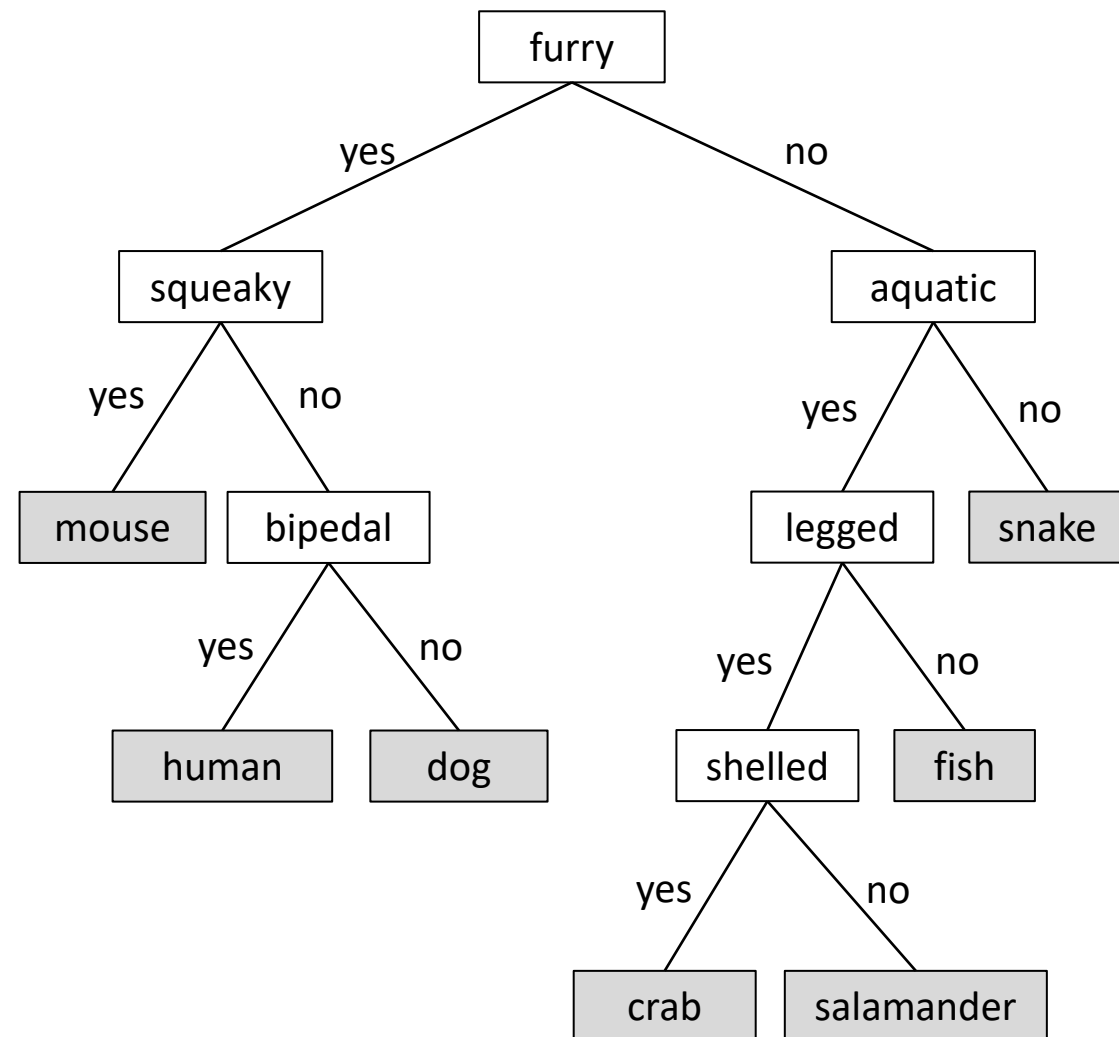
Binary Search Tree - Traversal

```
public void depthFirst(Node n) { Preorder
    if (n != null) {
        System.out.println(n.getValue());
        depthFirst(n.getLeft());
        depthFirst(n.getRight());
    }
}
```

```
public void depthFirst(Node n) { Postorder
    if (n != null) {
        depthFirst(n.getLeft());
        depthFirst(n.getRight());
        System.out.println(n.getValue());
    }
}
```

```
public void depthFirst(Node n) { Inorder
    if (n != null) {
        depthFirst(n.getLeft());
        System.out.println(n.getValue());
        depthFirst(n.getRight());
    }
}
```





Do you have another animal to identify? (Y/N) > Y

Is this animal furry? (Y/N) > Y

Is this animal squeaky? (Y/N) > N

Is this animal bipedal? (Y/N) > Y

Is this animal a human? (Y/N) > N

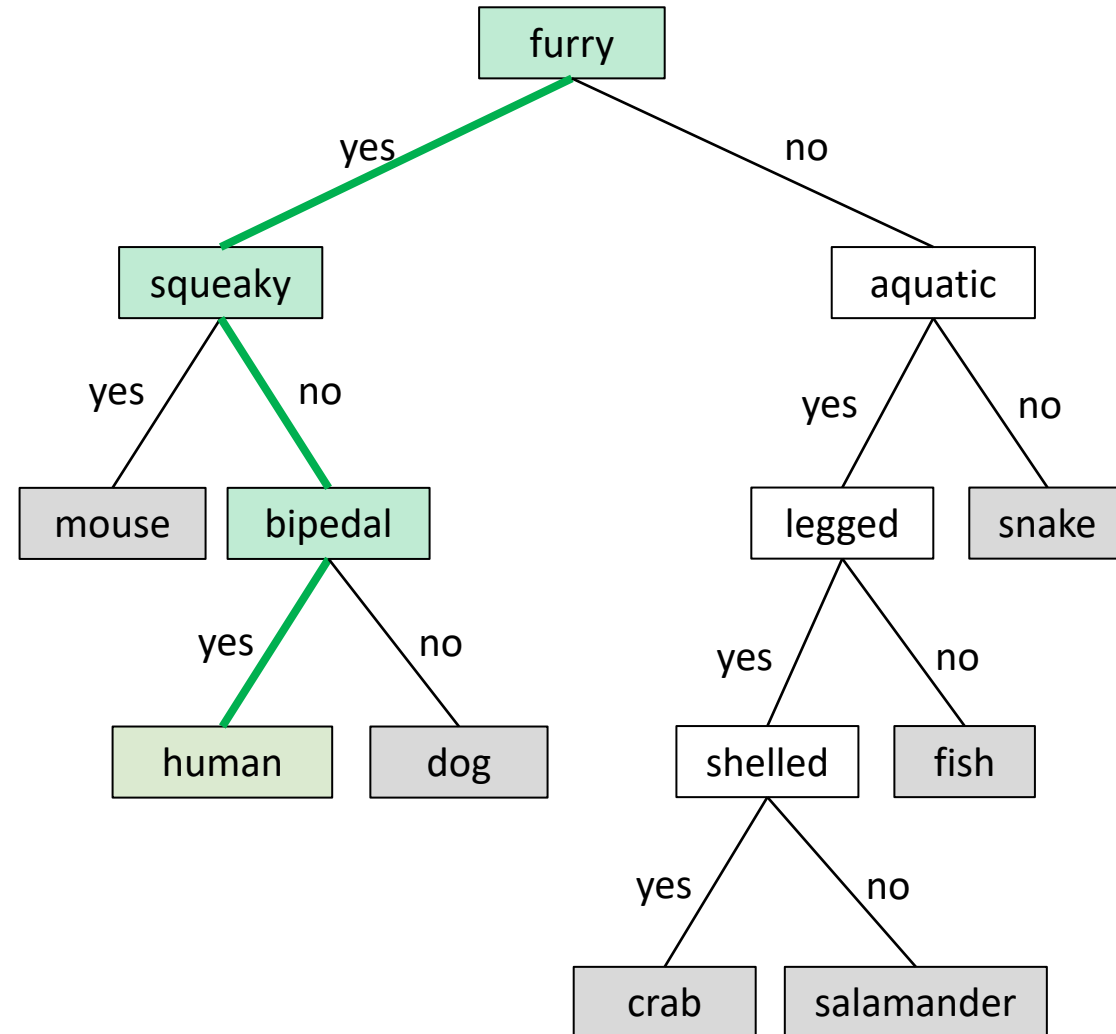
I don't know any furry, not squeaky, bipedal animals that aren't a human.

What is the new animal? > bigfoot

What characteristic does a bigfoot have that a human does not? > reclusive

Program Execution:

1.



Do you have another animal to identify? (Y/N) > Y

Is this animal furry? (Y/N) > Y

Is this animal squeaky? (Y/N) > N

Is this animal bipedal? (Y/N) > Y

Is this animal a human? (Y/N) > N

I don't know any furry, not squeaky, bipedal animals that aren't a human.

What is the new animal? > bigfoot

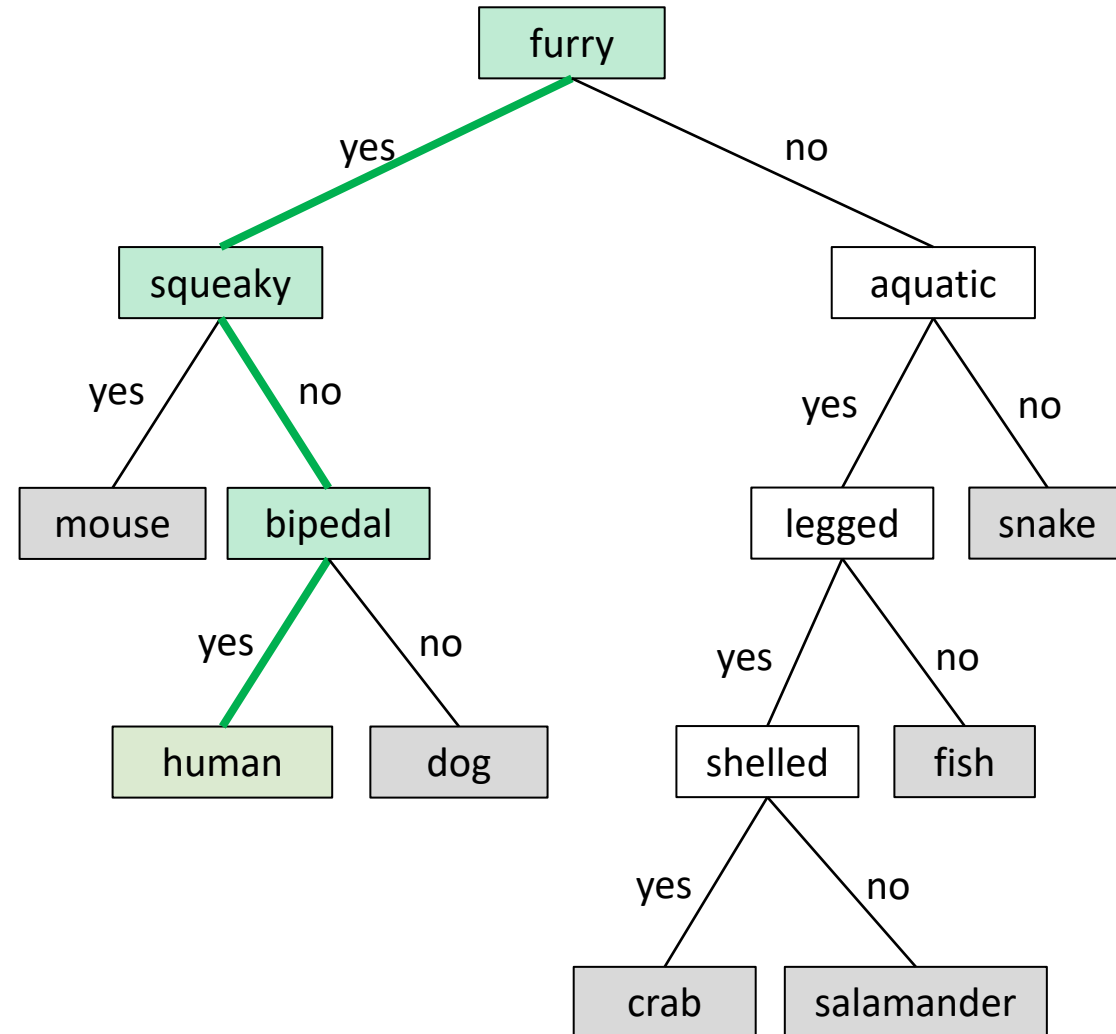
What characteristic does a bigfoot have that a human does not? > reclusive

Program Execution:

1. Yes/No questions to navigate to a leaf (animal).

2. Is animal correct?

3.



Do you have another animal to identify? (Y/N) > Y

Is this animal furry? (Y/N) > Y

Is this animal squeaky? (Y/N) > N

Is this animal bipedal? (Y/N) > Y

Is this animal a human? (Y/N) > N

I don't know any furry, not squeaky, bipedal animals that aren't a human.

What is the new animal? > bigfoot

What characteristic does a bigfoot have that a human does not? > reclusive

Program Execution:

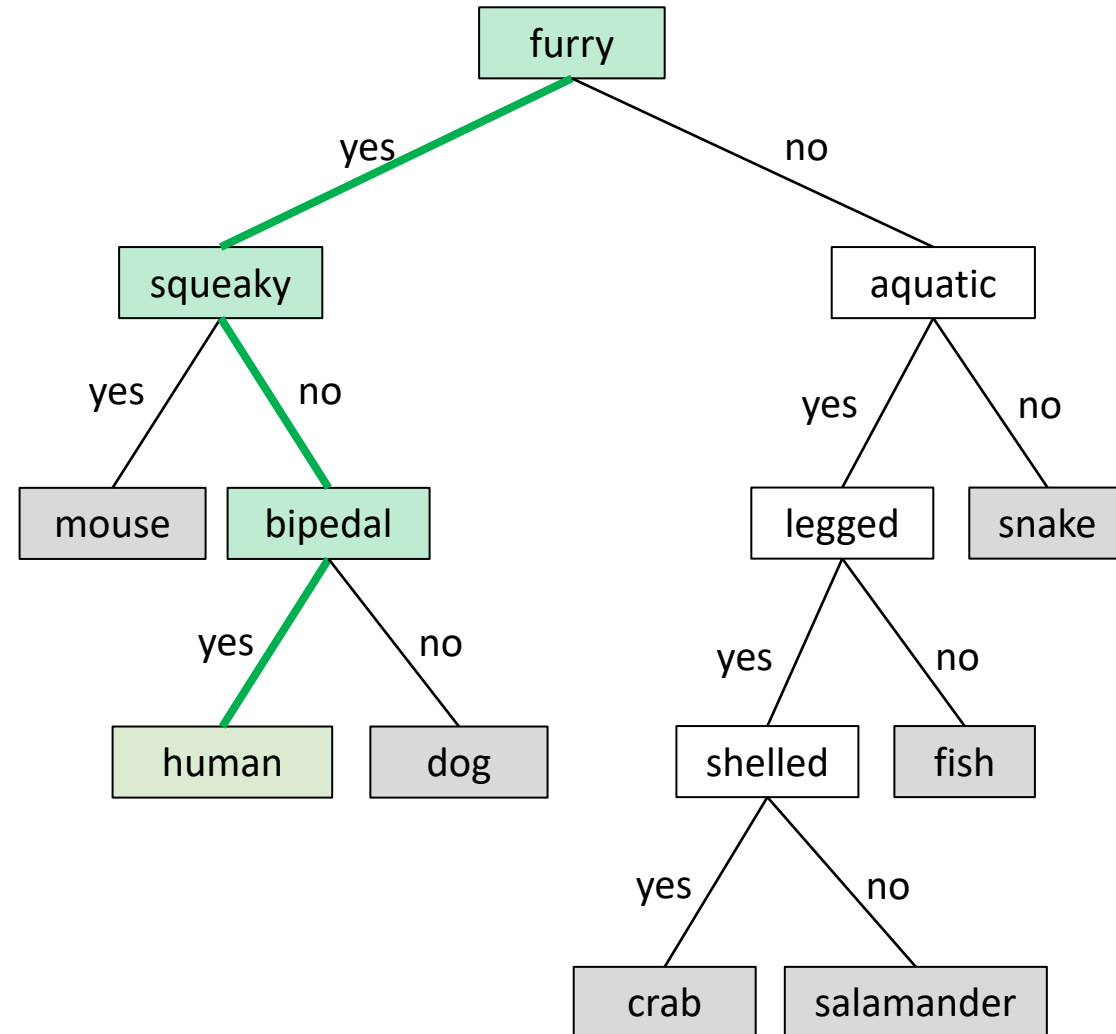
1. Yes/No questions to navigate to a leaf (animal).

2. Is animal correct?

3. If not:

3.1. Print location in tree.

3.2.



Do you have another animal to identify? (Y/N) > Y

Is this animal furry? (Y/N) > Y

Is this animal squeaky? (Y/N) > N

Is this animal bipedal? (Y/N) > Y

Is this animal a human? (Y/N) > N

I don't know any furry, not squeaky, bipedal animals that aren't a human.

What is the new animal? > bigfoot

What characteristic does a bigfoot have that a human does not? > reclusive

Program Execution:

1. Yes/No questions to navigate to a leaf (animal).

2. Is animal correct?

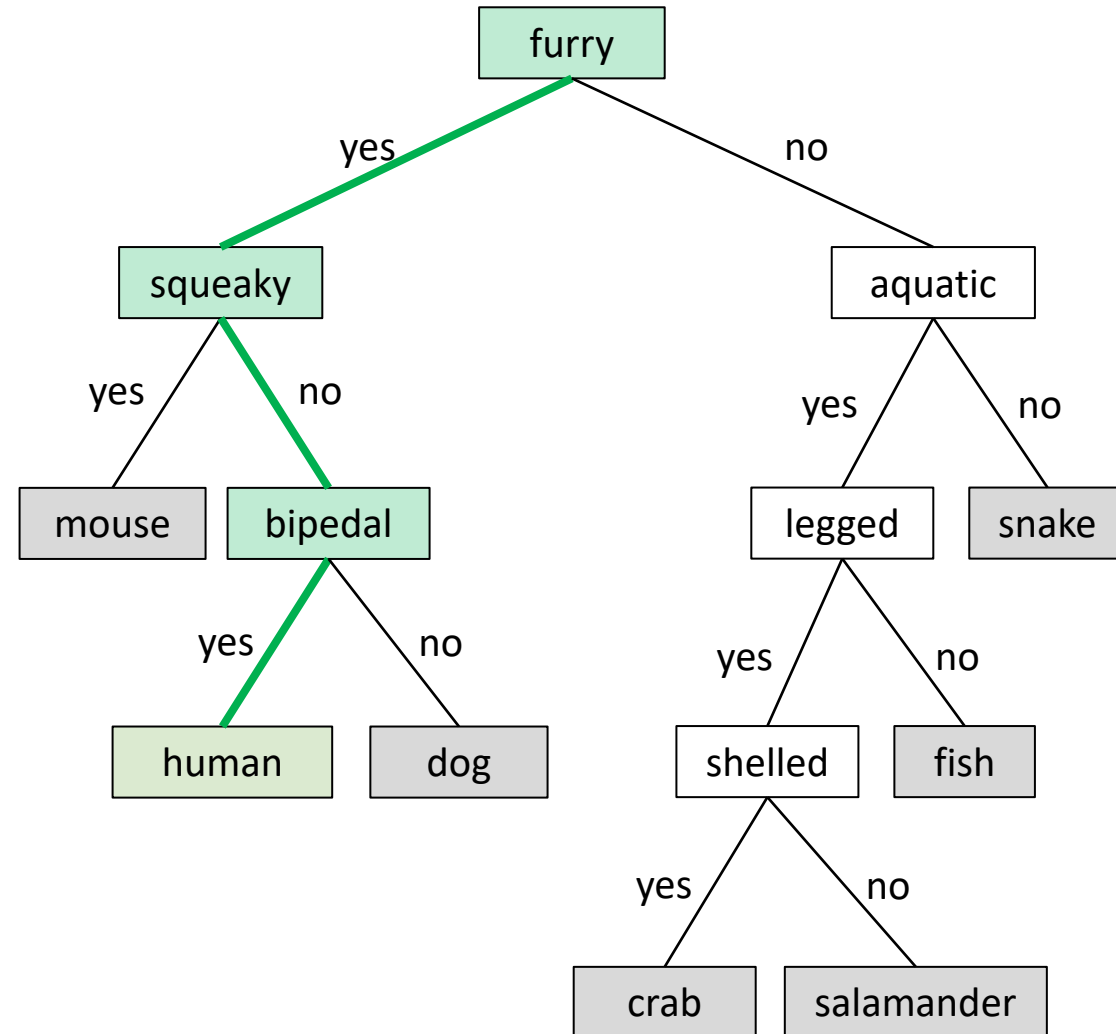
3. If not:

3.1. Print location in tree.

3.2. Get name of new animal.

3.3. Get distinguishing characteristic.

3.4.



Do you have another animal to identify? (Y/N) > Y

Is this animal furry? (Y/N) > Y

Is this animal squeaky? (Y/N) > N

Is this animal bipedal? (Y/N) > Y

Is this animal a human? (Y/N) > N

I don't know any furry, not squeaky, bipedal animals that aren't a human.

What is the new animal? > bigfoot

What characteristic does a bigfoot have that a human does not? > reclusive

Program Execution:

1. Yes/No questions to navigate to a leaf (animal).

2. Is animal correct?

3. If not:

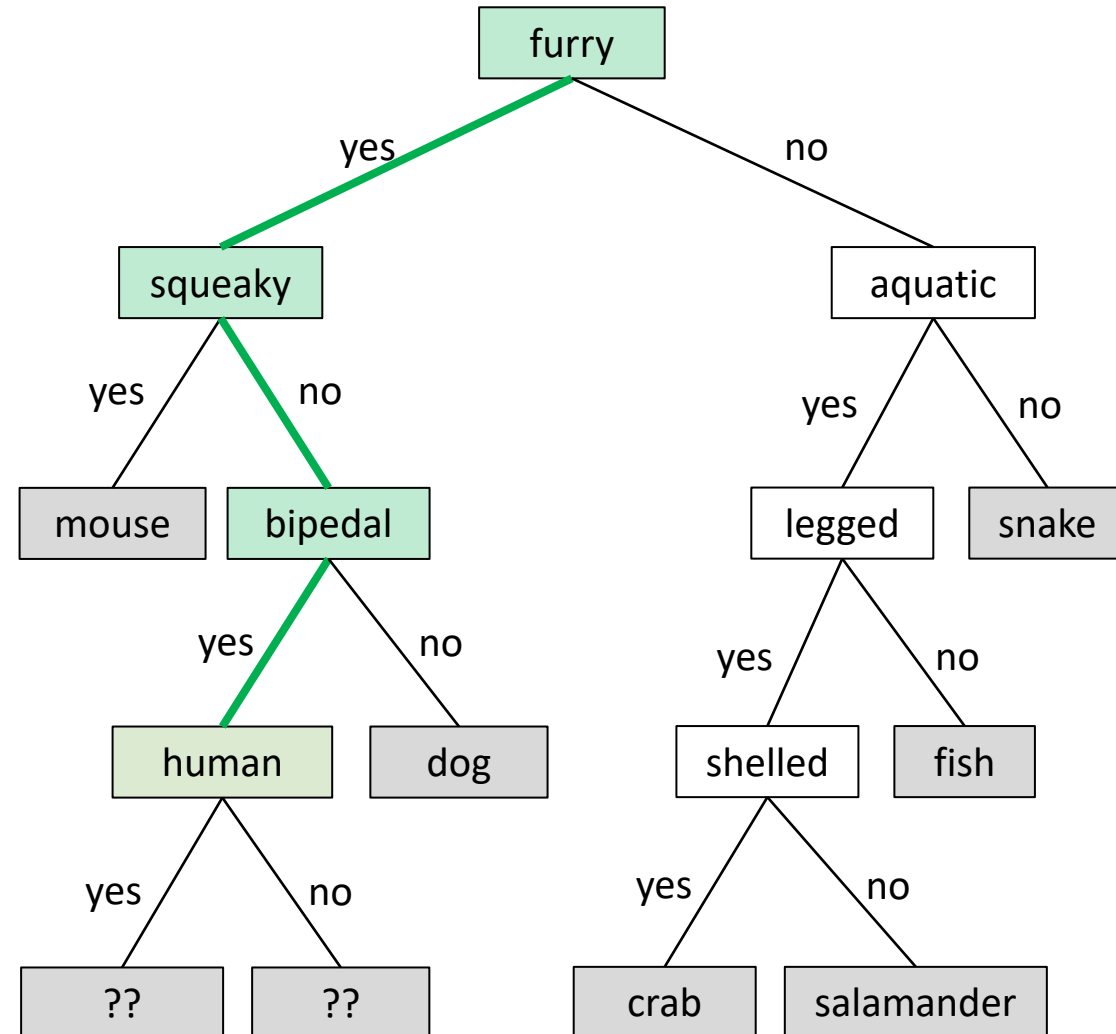
3.1. Print location in tree.

3.2. Get name of new animal.

3.3. Get distinguishing characteristic.

3.4. Modify tree:

3.4.1.



Do you have another animal to identify? (Y/N) > Y

Is this animal furry? (Y/N) > Y

Is this animal squeaky? (Y/N) > N

Is this animal bipedal? (Y/N) > Y

Is this animal a human? (Y/N) > N

I don't know any furry, not squeaky, bipedal animals that aren't a human.

What is the new animal? > bigfoot

What characteristic does a bigfoot have that a human does not? > reclusive

Program Execution:

1. Yes/No questions to navigate to a leaf (animal).

2. Is animal correct?

3. If not:

3.1. Print location in tree.

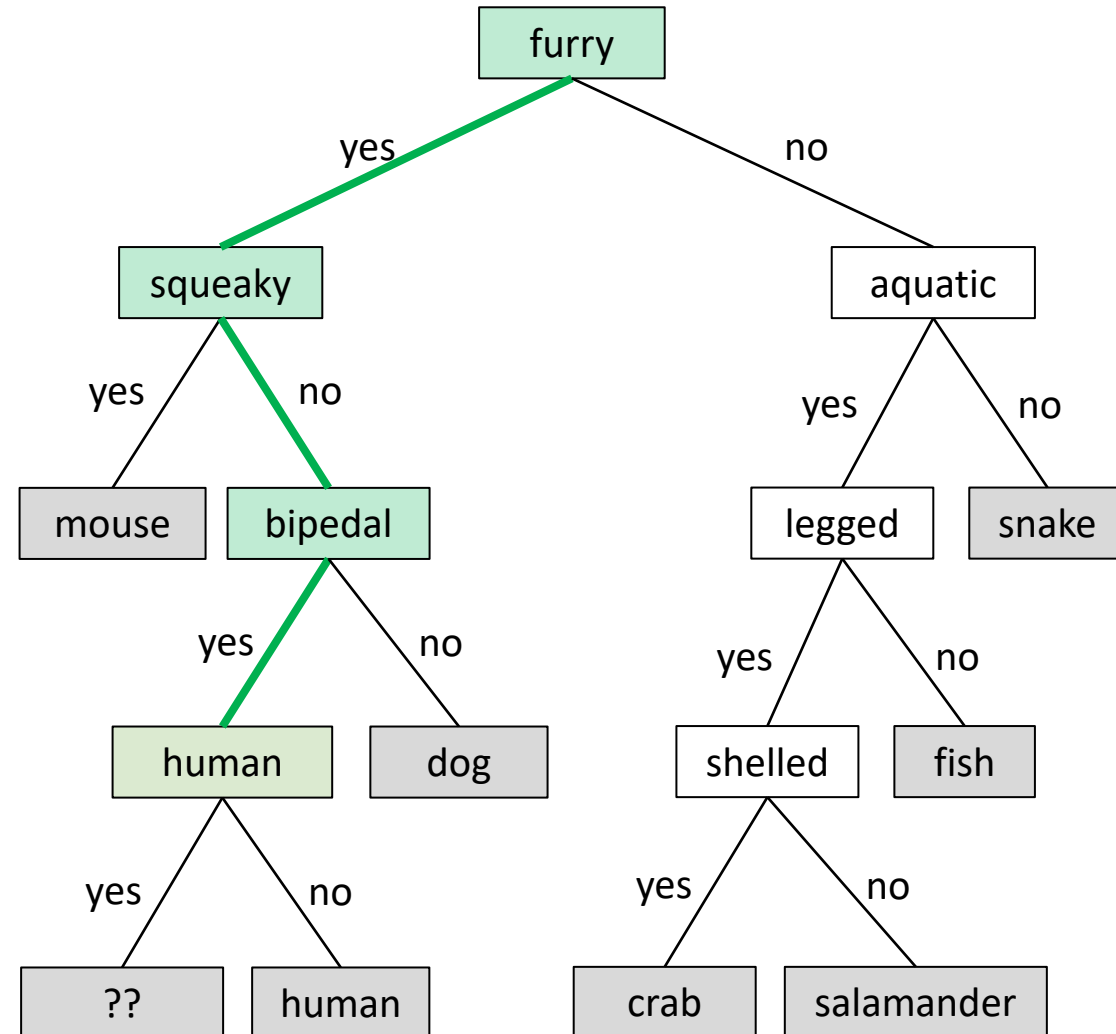
3.2. Get name of new animal.

3.3. Get distinguishing characteristic.

3.4. Modify tree:

3.4.1. Create two new child nodes at current leaf.

3.4.2.



Do you have another animal to identify? (Y/N) > Y

Is this animal furry? (Y/N) > Y

Is this animal squeaky? (Y/N) > N

Is this animal bipedal? (Y/N) > Y

Is this animal a human? (Y/N) > N

I don't know any furry, not squeaky, bipedal animals that aren't a human.

What is the new animal? > bigfoot

What characteristic does a bigfoot have that a human does not? > reclusive

Program Execution:

1. Yes/No questions to navigate to a leaf (animal).

2. Is animal correct?

3. If not:

3.1. Print location in tree.

3.2. Get name of new animal.

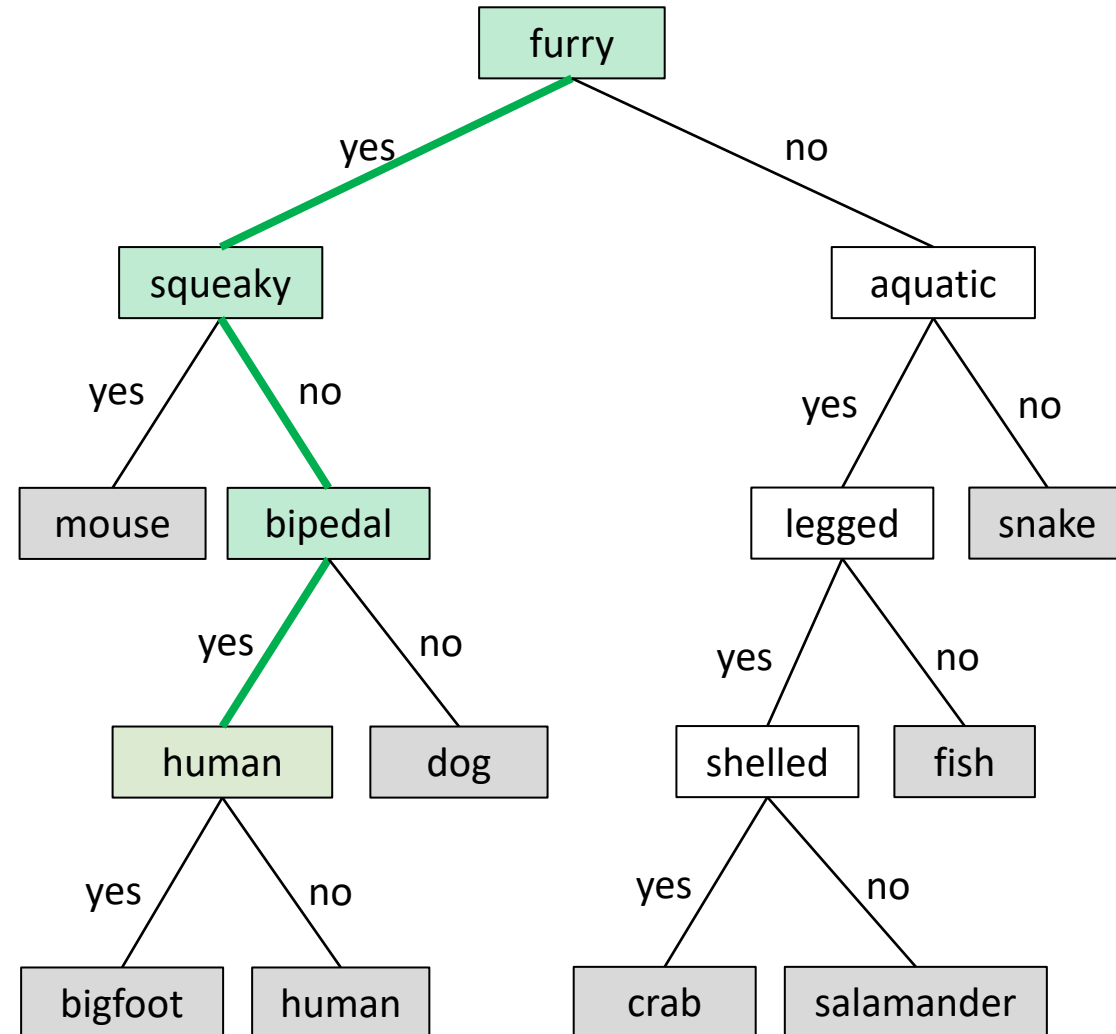
3.3. Get distinguishing characteristic.

3.4. Modify tree:

3.4.1. Create two new child nodes at current leaf.

3.4.2. Make "no" child node animal be old leaf.

3.4.3.



Do you have another animal to identify? (Y/N) > Y

Is this animal furry? (Y/N) > Y

Is this animal squeaky? (Y/N) > N

Is this animal bipedal? (Y/N) > Y

Is this animal a human? (Y/N) > N

I don't know any furry, not squeaky, bipedal animals that aren't a human.

What is the new animal? > bigfoot

What characteristic does a bigfoot have that a human does not? > reclusive

Program Execution:

1. Yes/No questions to navigate to a leaf (animal).

2. Is animal correct?

3. If not:

3.1. Print location in tree.

3.2. Get name of new animal.

3.3. Get distinguishing characteristic.

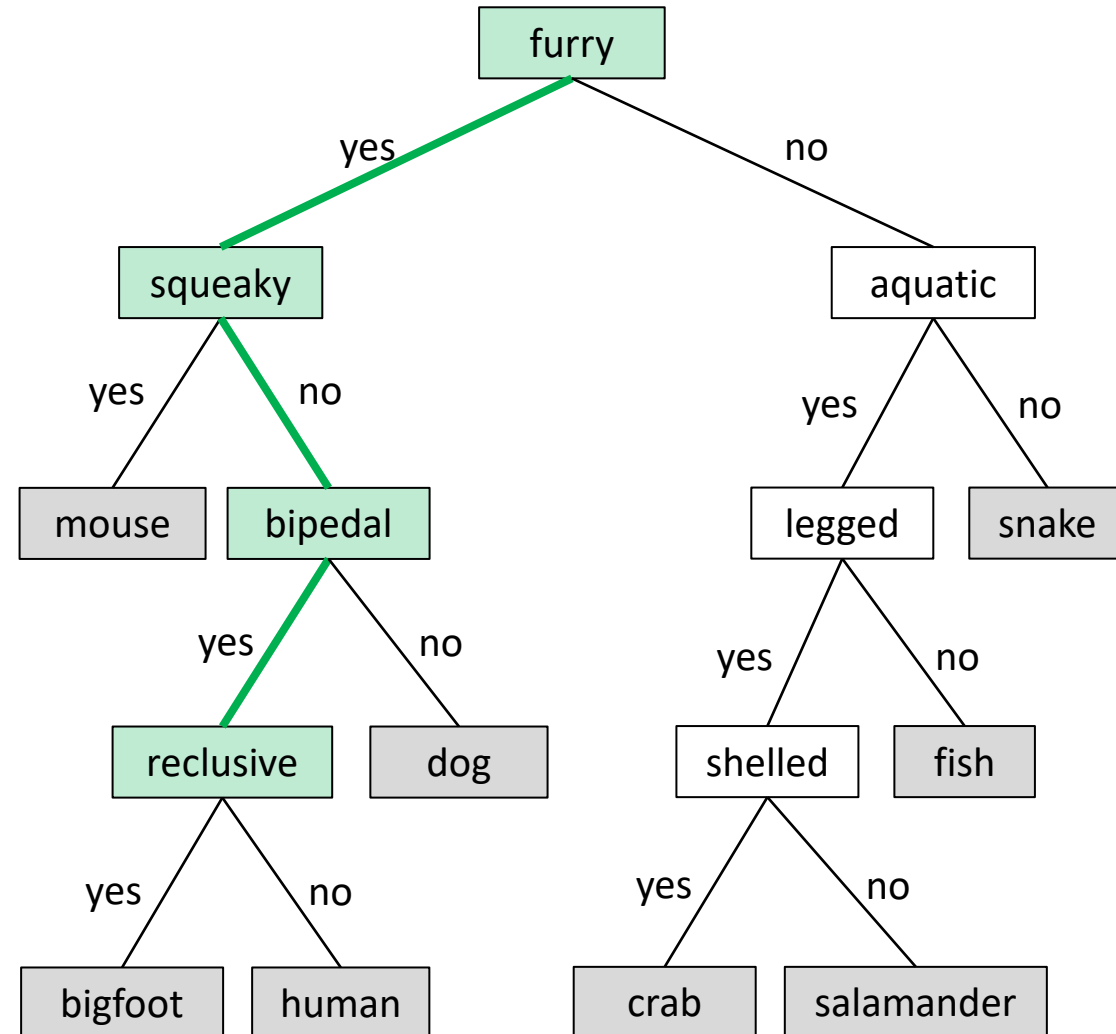
3.4. Modify tree:

3.4.1. Create two new child nodes at current leaf.

3.4.2. Make "no" child node animal be old leaf.

3.4.3. Make "yes" child node animal be new animal.

3.4.4.



Do you have another animal to identify? (Y/N) > Y

Is this animal furry? (Y/N) > Y

Is this animal squeaky? (Y/N) > N

Is this animal bipedal? (Y/N) > Y

Is this animal a human? (Y/N) > N

I don't know any furry, not squeaky, bipedal animals that aren't a human.

What is the new animal? > bigfoot

What characteristic does a bigfoot have that a human does not? > reclusive

Program Execution:

1. Yes/No questions to navigate to a leaf (animal).

2. Is animal correct?

3. If not:

3.1. Print location in tree.

3.2. Get name of new animal.

3.3. Get distinguishing characteristic.

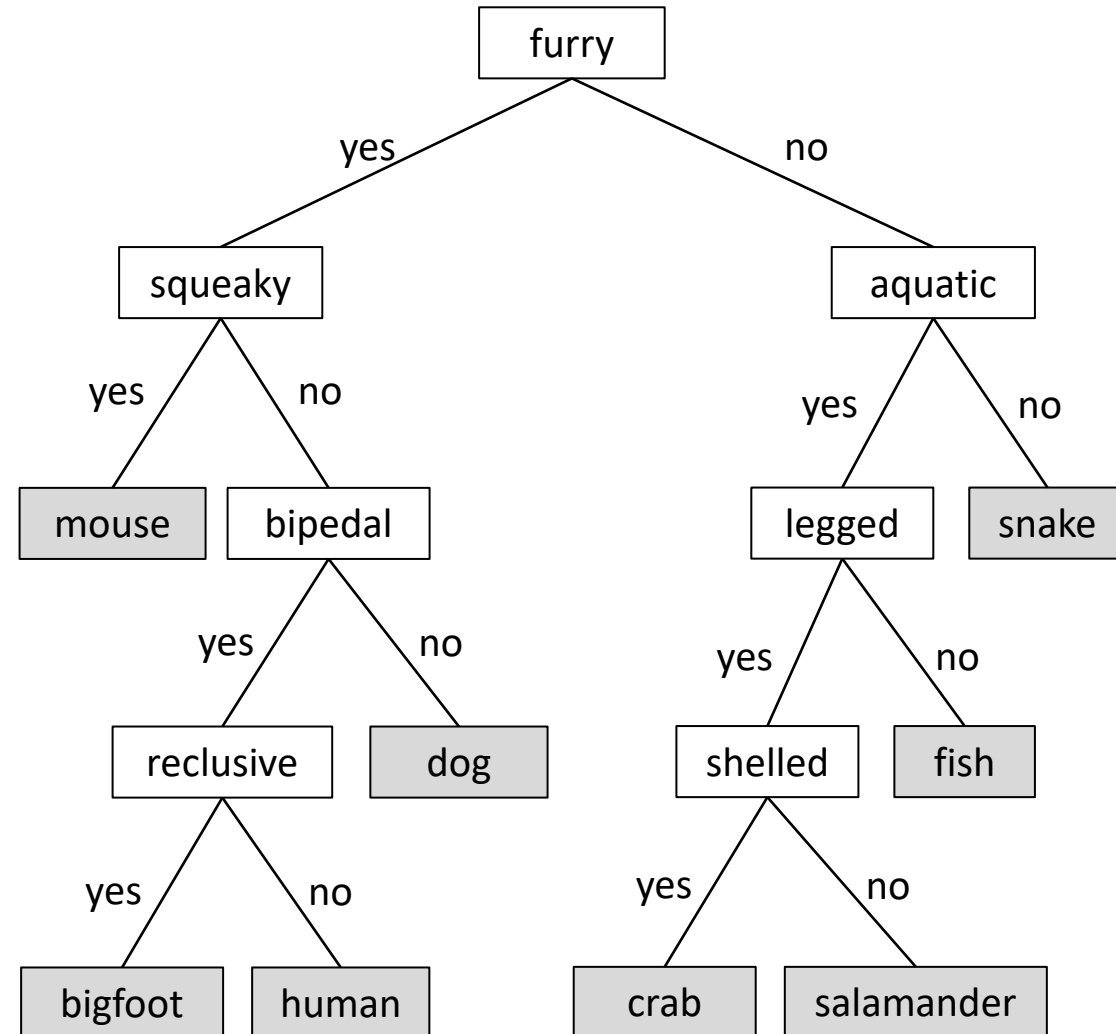
3.4. Modify tree:

3.4.1. Create two new child nodes at current leaf.

3.4.2. Make "no" child node animal be old leaf.

3.4.3. Make "yes" child node animal be new animal.

3.4.4. Make old leaf be distinguishing characteristic.



Do you have another animal to identify? (Y/N) > Y

Is this animal furry? (Y/N) > Y

Is this animal squeaky? (Y/N) > N

Is this animal bipedal? (Y/N) > Y

Is this animal a human? (Y/N) > N

I don't know any furry, not squeaky, bipedal animals that aren't a human.

What is the new animal? > bigfoot

What characteristic does a bigfoot have that a human does not? > reclusive

Program Execution:

1. Yes/No questions to navigate to a leaf (animal).

2. Is animal correct?

3. If not:

3.1. Print location in tree.

3.2. Get name of new animal.

3.3. Get distinguishing characteristic.

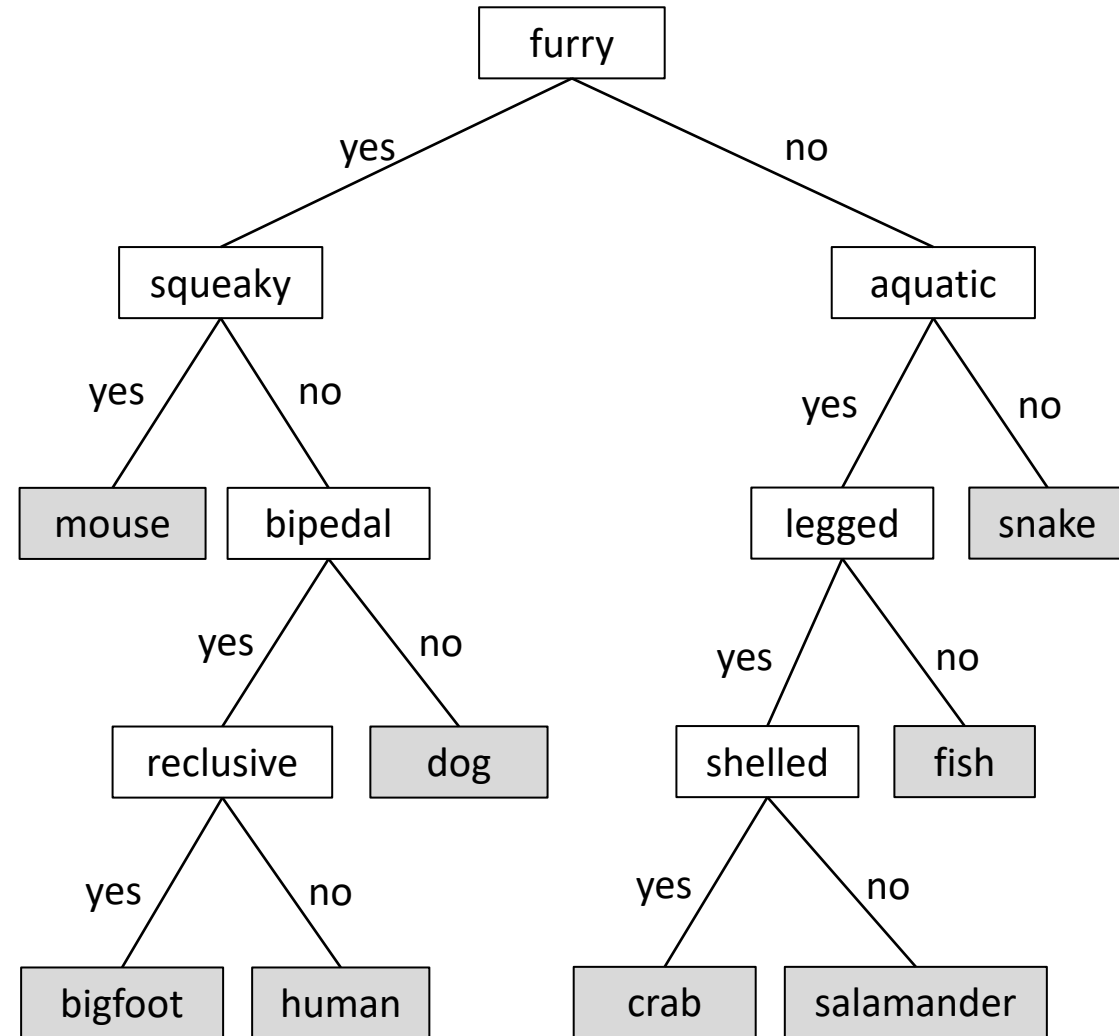
3.4. Modify tree:

3.4.1. Create two new child nodes at current leaf.

3.4.2. Make "no" child node animal be old leaf.

3.4.3. Make "yes" child node animal be new animal.

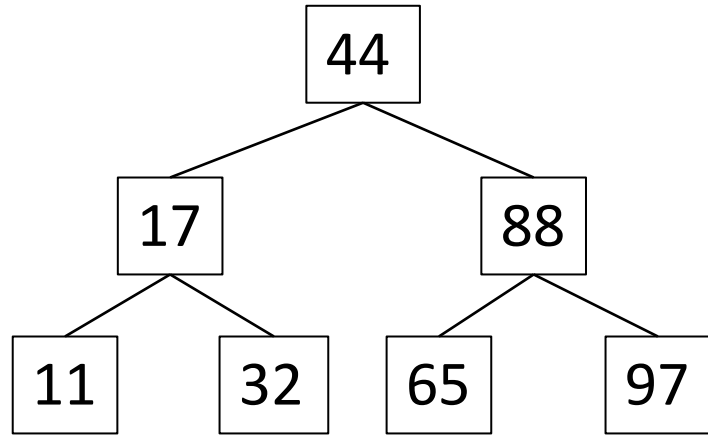
3.4.4. Make old leaf be distinguishing characteristic.



```
public class Node {  
    private String text;  
    private Node yesChild;  
    private Node noChild;  
    private Node parent;  
  
    ...  
}
```

File read/writing

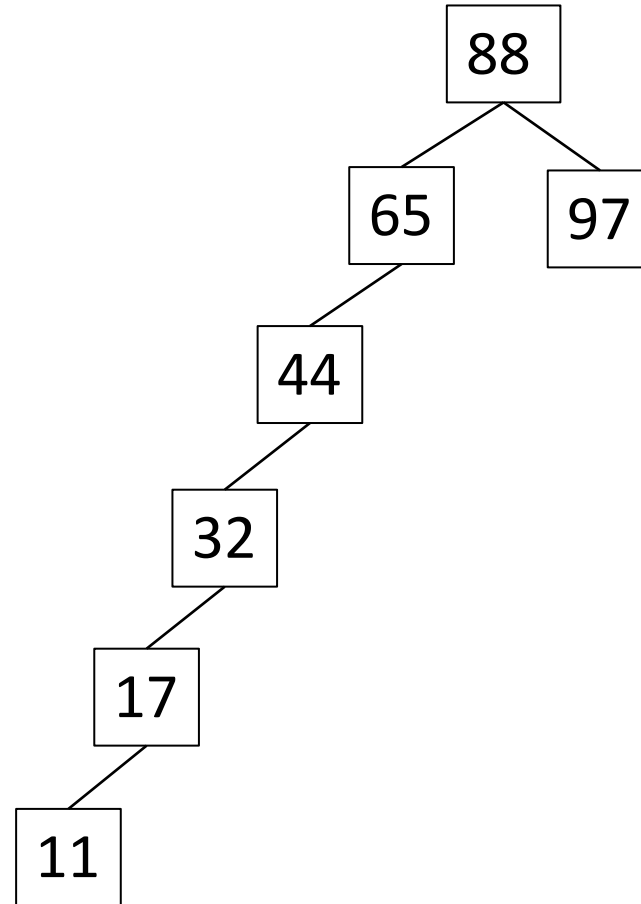
Order Matters



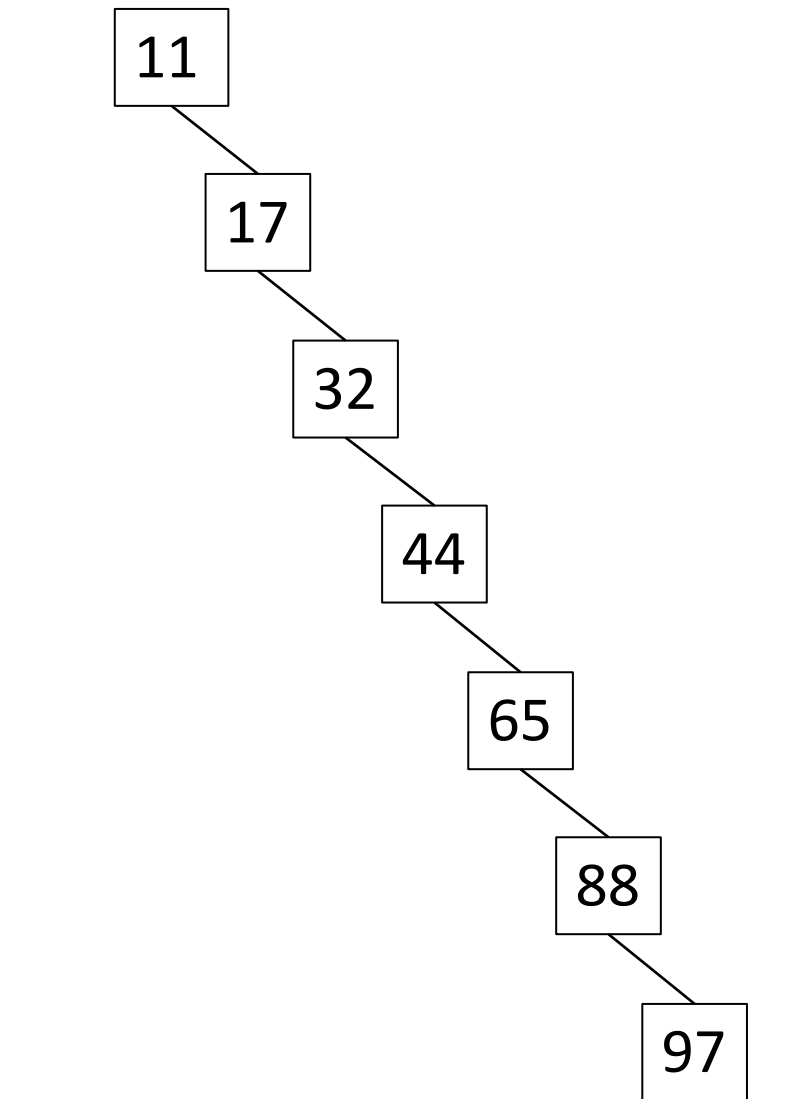
44, 17, 88, 11, 32, 65, 97

44, 17, 32, 88, 11, 97, 65

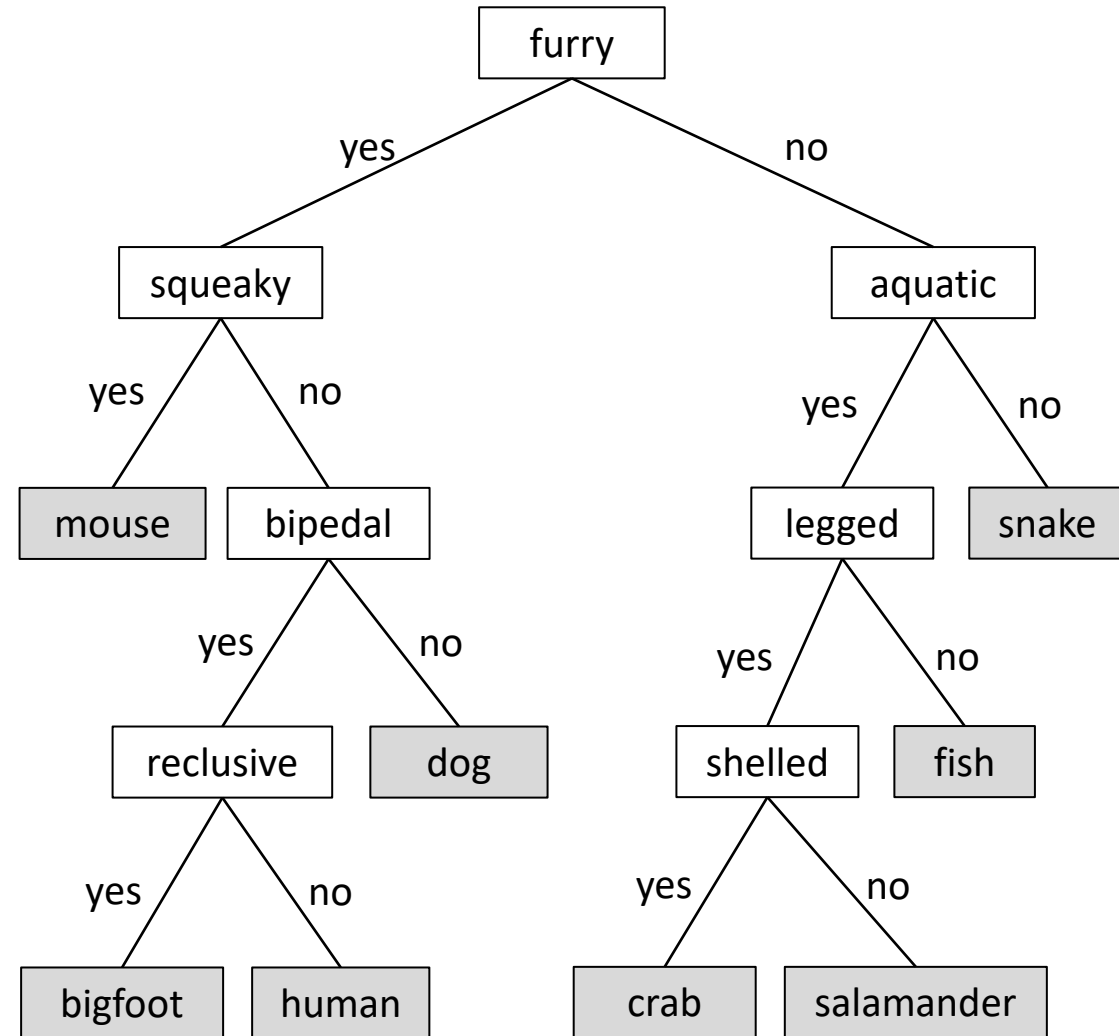
44, 88, 65, 97, 17, 32, 11



88, 65, 44, 32, 97, 17, 11

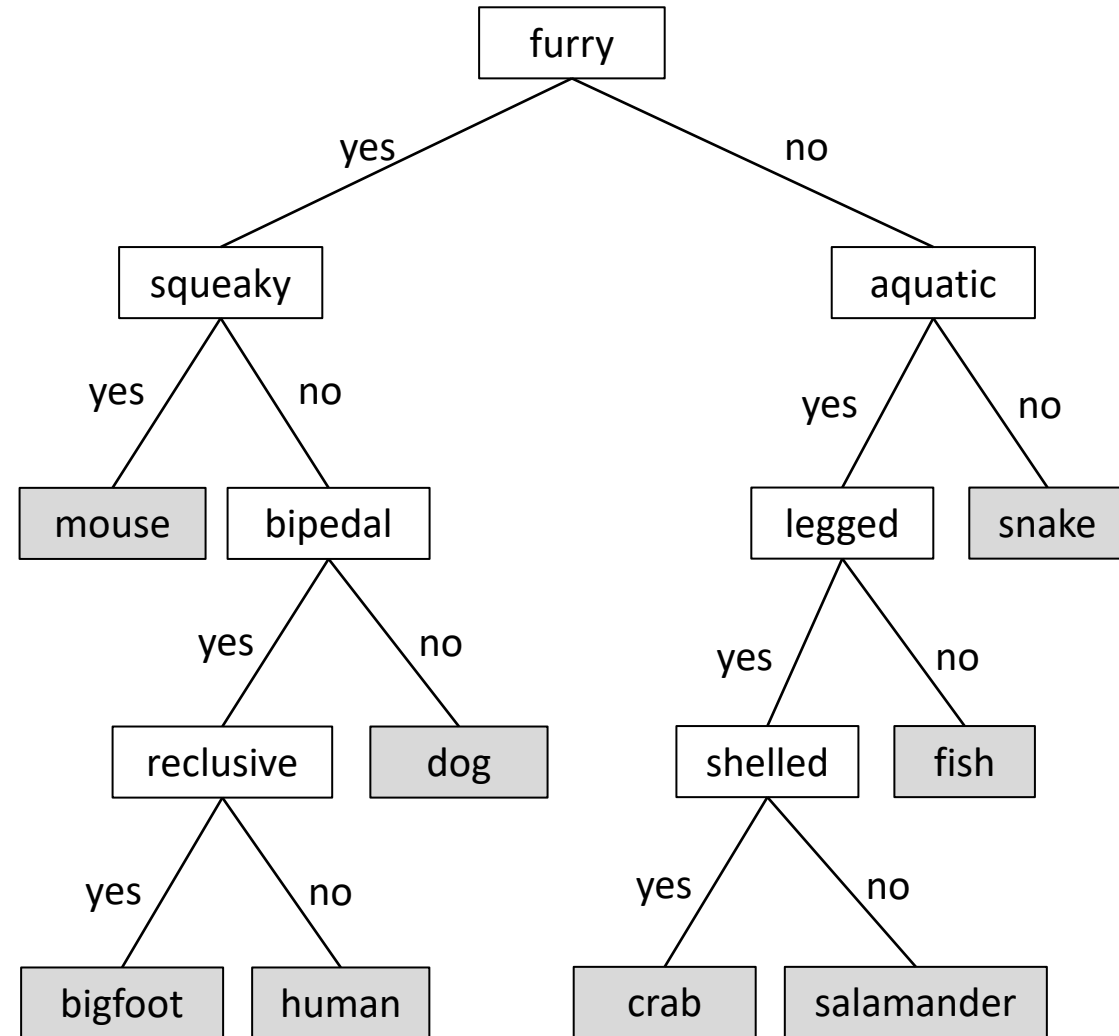


11, 17, 32, 44, 65, 88, 97



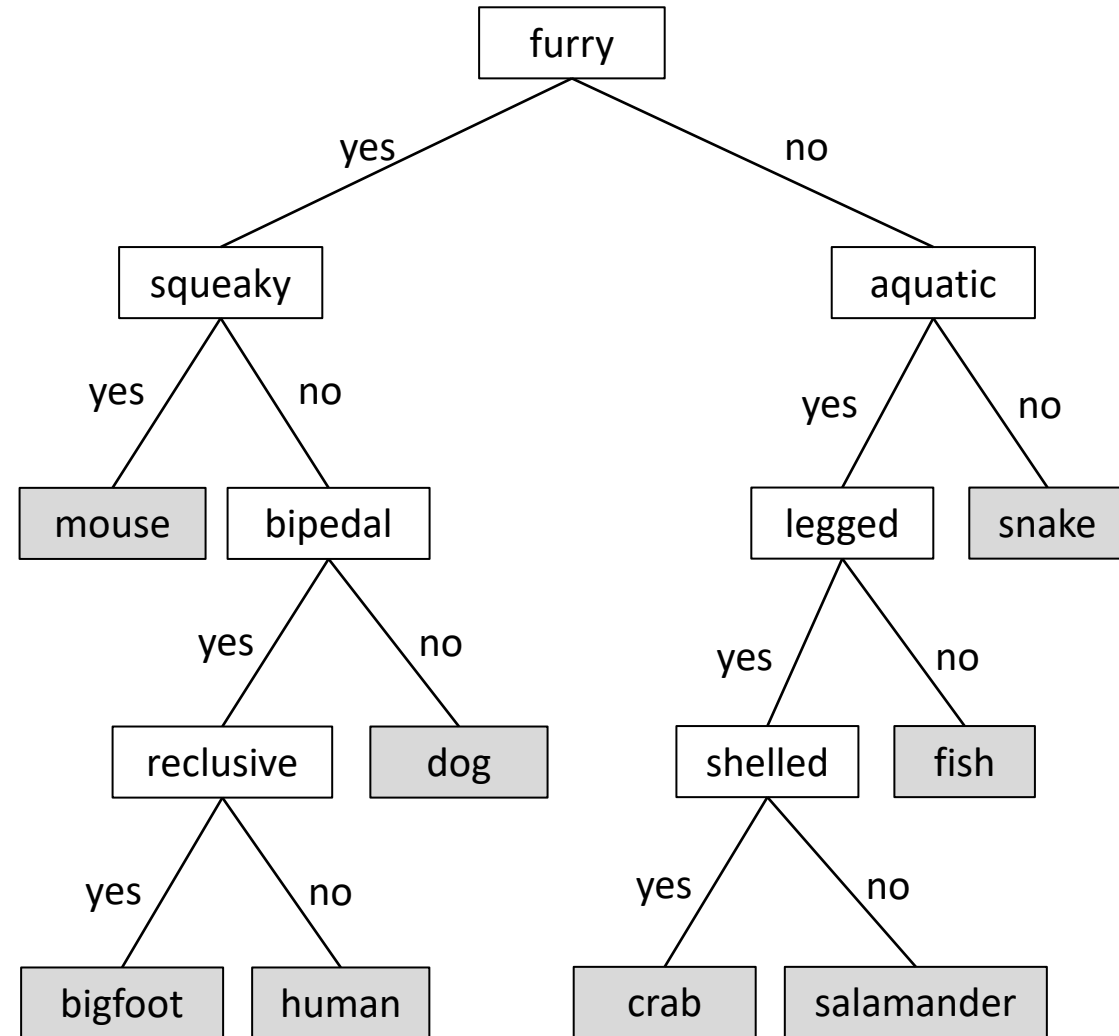
```
public class Node {  
    private String text;  
    private Node yesChild;  
    private Node noChild;  
    private Node parent;  
  
    ...  
}
```

File read/writing



```
public class Node {  
    private String text;  
    private Node yesChild;  
    private Node noChild;  
    private Node parent;  
    private int tag;  
    ...  
}
```

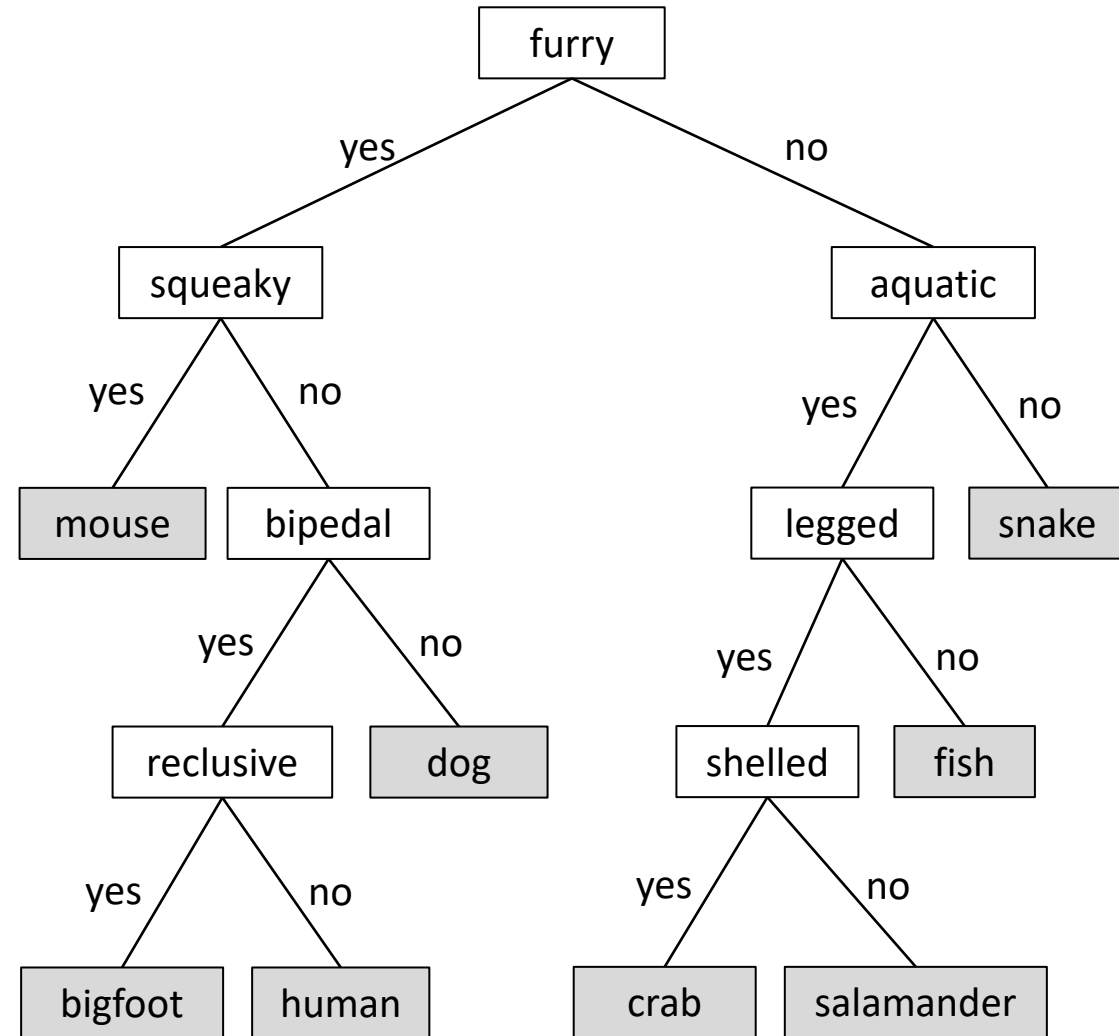
File read/writing



```
public class Node {  
    private String text;  
    private Node yesChild;  
    private Node noChild;  
    private Node parent;  
    private int tag;  
    ...  
}
```

Save to file:

File read/writing

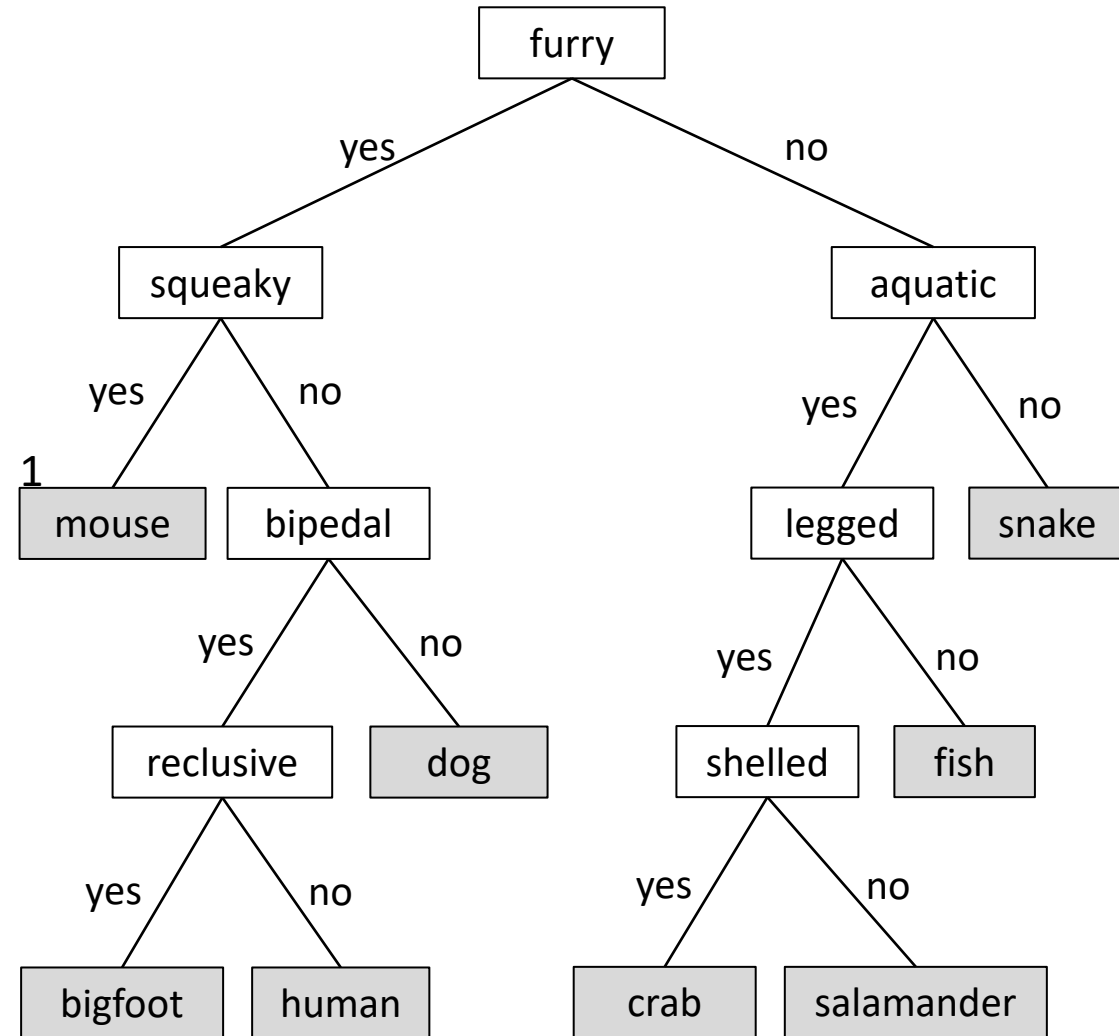


```
public class Node {  
    private String text;  
    private Node yesChild;  
    private Node noChild;  
    private Node parent;  
    private int tag;  
    ...  
}
```

Save to file:

1. Do inorder traversal of tree and assign sequential integer tag values.

File read/writing

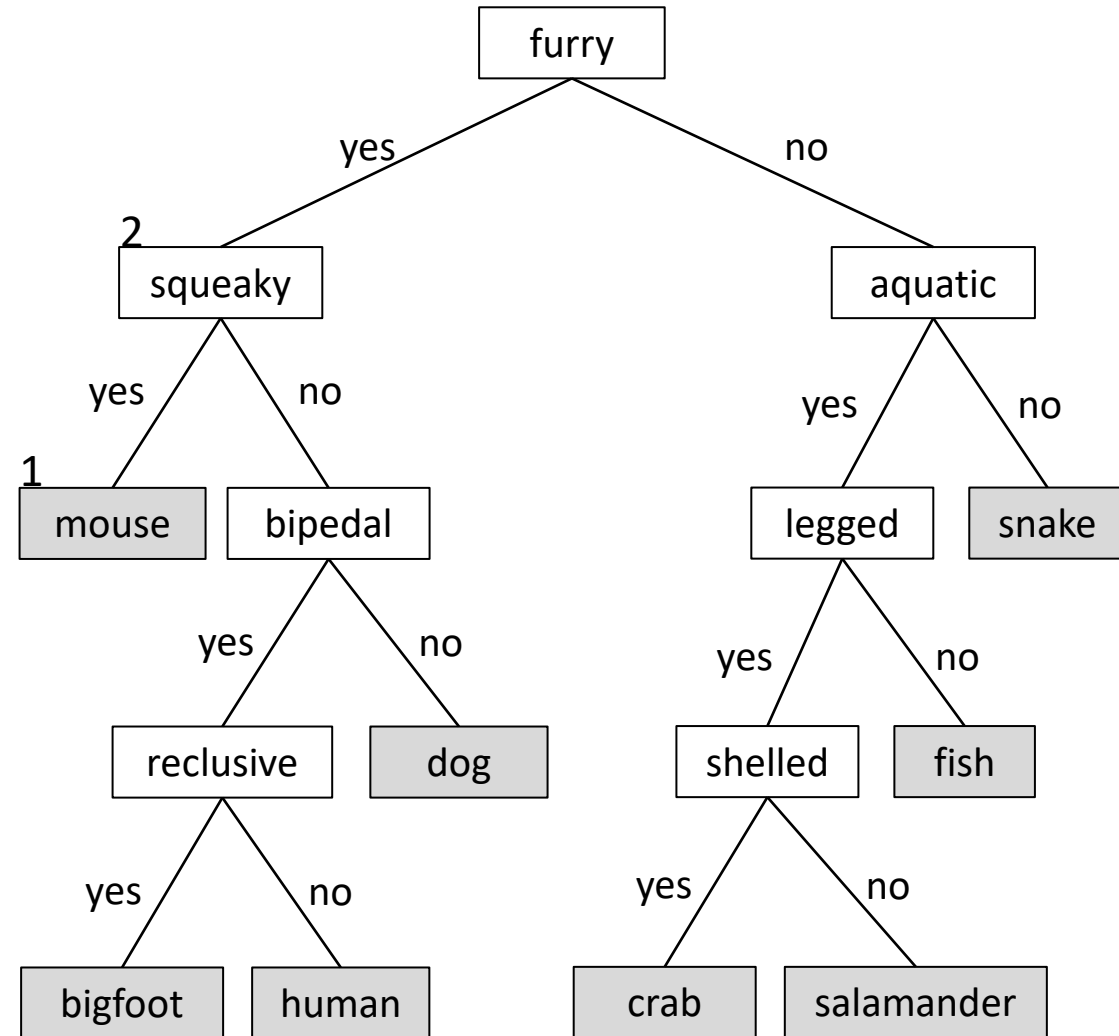


```
public class Node {  
    private String text;  
    private Node yesChild;  
    private Node noChild;  
    private Node parent;  
    private int tag;  
    ...  
}
```

Save to file:

1. Do inorder traversal of tree and assign sequential integer tag values.

File read/writing

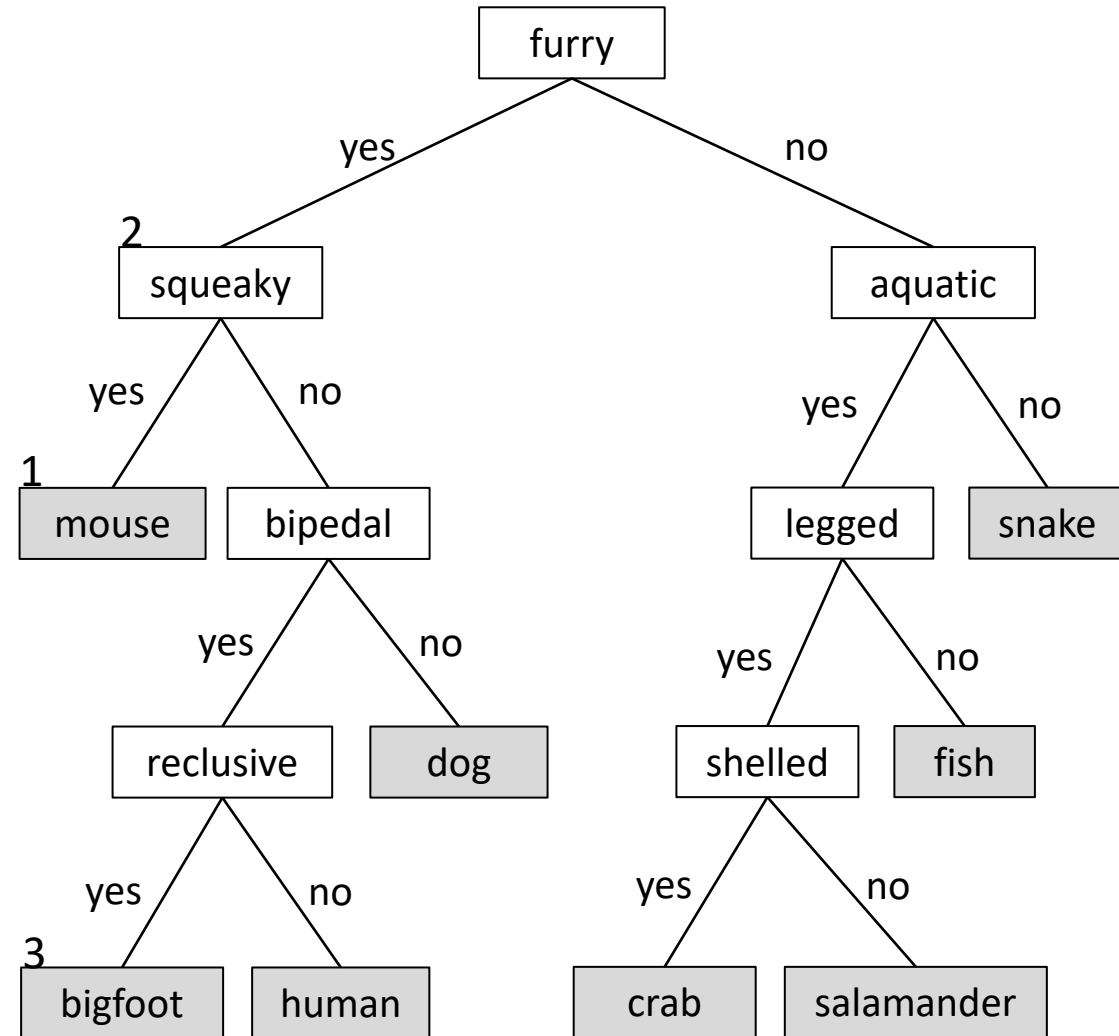


```
public class Node {  
    private String text;  
    private Node yesChild;  
    private Node noChild;  
    private Node parent;  
    private int tag;  
    ...  
}
```

Save to file:

1. Do inorder traversal of tree and assign sequential integer tag values.

File read/writing

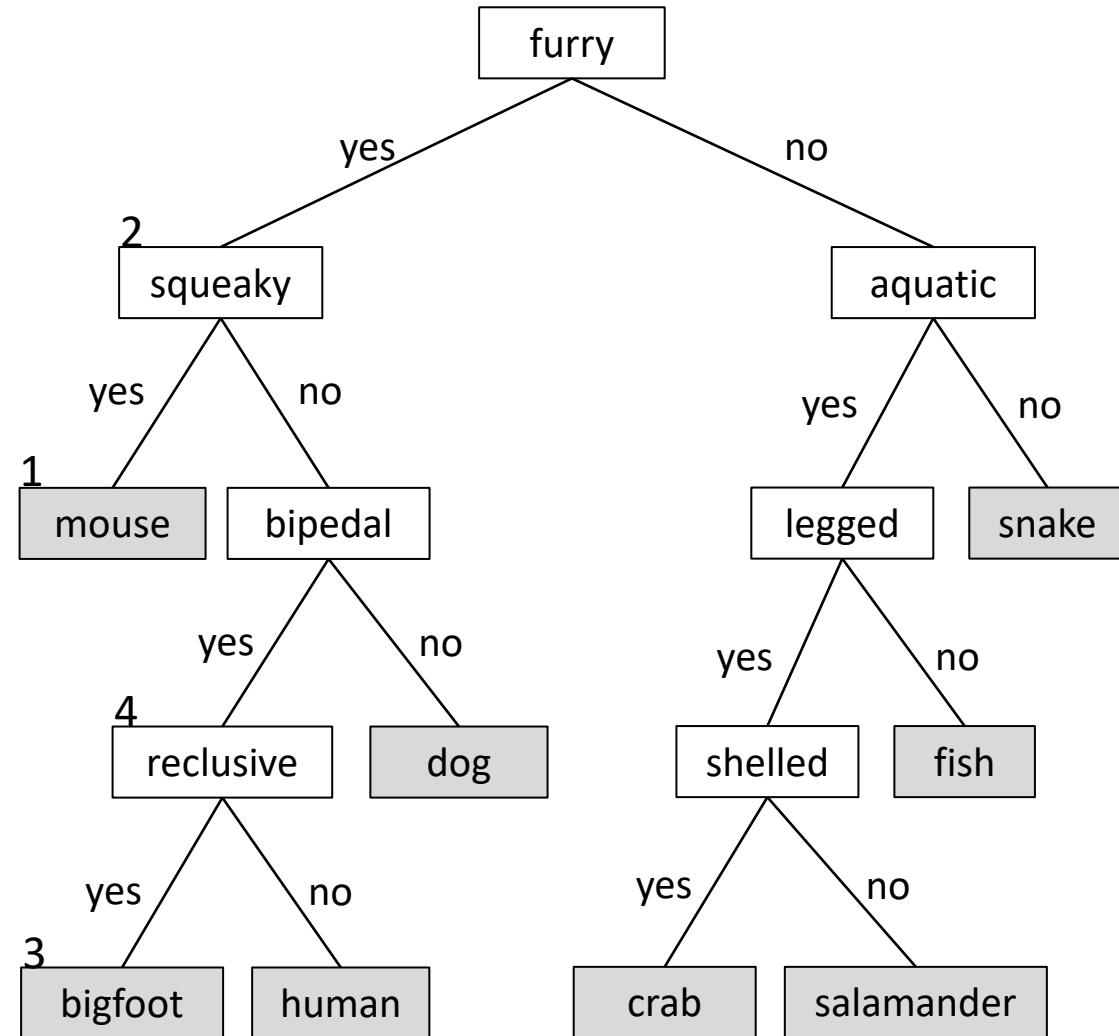


```
public class Node {  
    private String text;  
    private Node yesChild;  
    private Node noChild;  
    private Node parent;  
    private int tag;  
    ...  
}
```

Save to file:

1. Do inorder traversal of tree and assign sequential integer tag values.

File read/writing

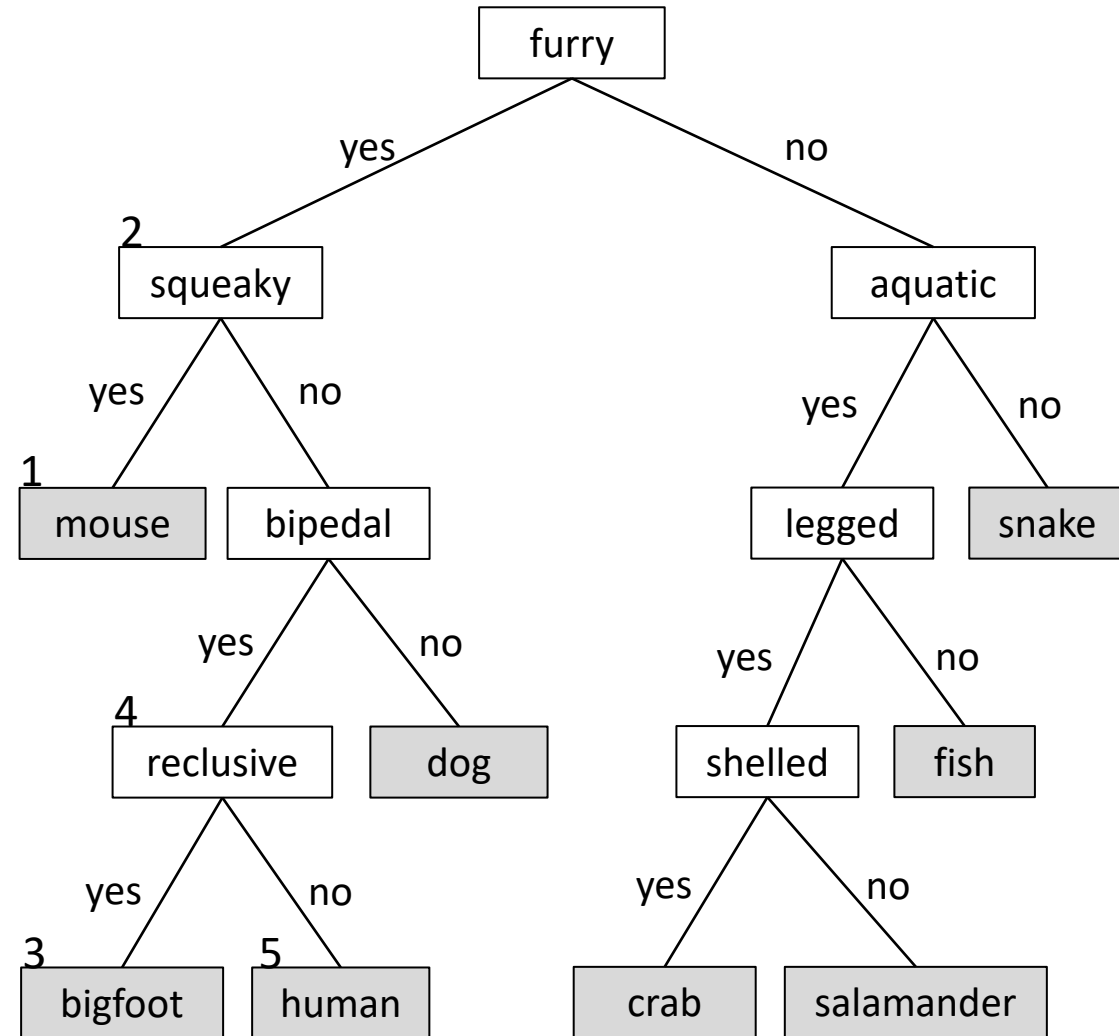


```
public class Node {  
    private String text;  
    private Node yesChild;  
    private Node noChild;  
    private Node parent;  
    private int tag;  
    ...  
}
```

Save to file:

1. Do inorder traversal of tree and assign sequential integer tag values.

File read/writing

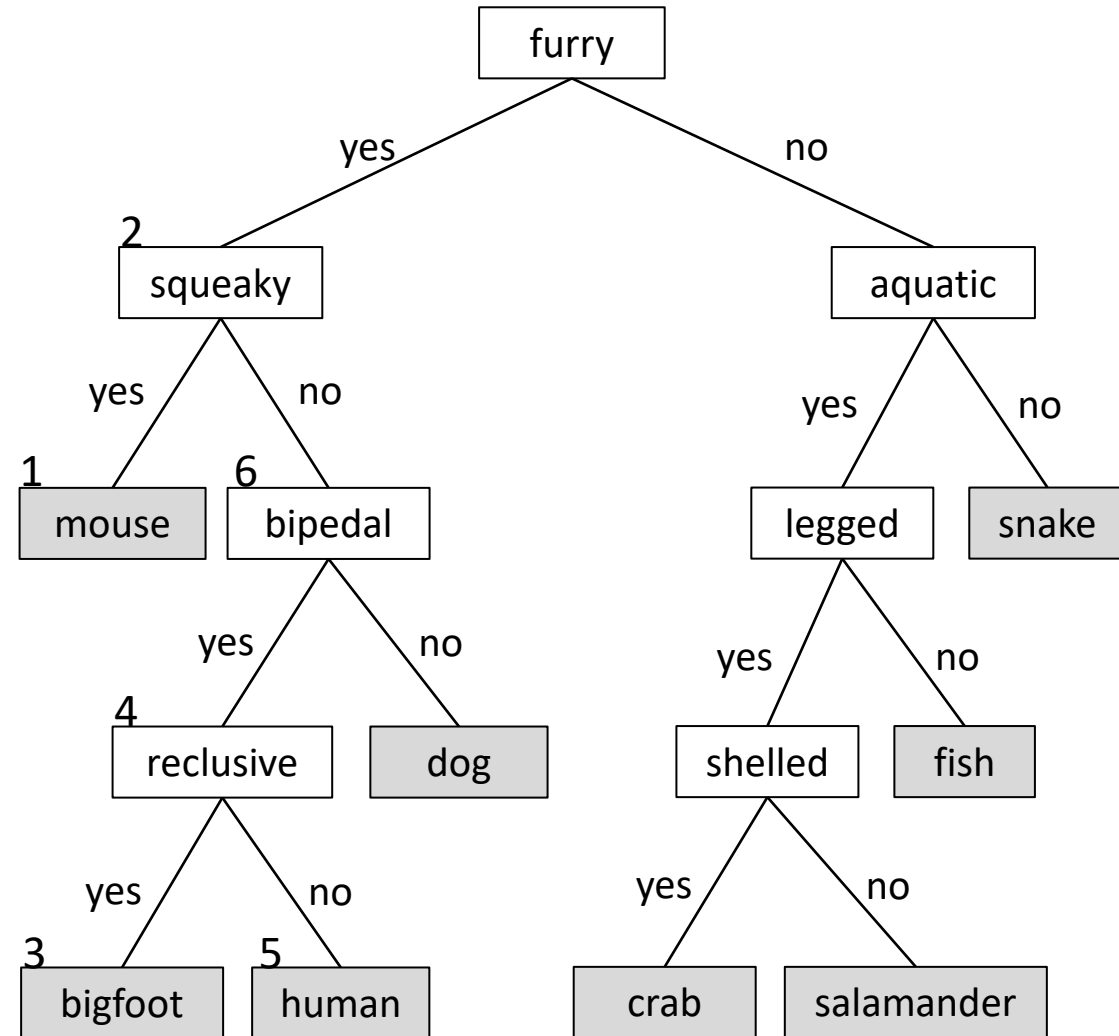


```
public class Node {  
    private String text;  
    private Node yesChild;  
    private Node noChild;  
    private Node parent;  
    private int tag;  
    ...  
}
```

Save to file:

1. Do inorder traversal of tree and assign sequential integer tag values.

File read/writing

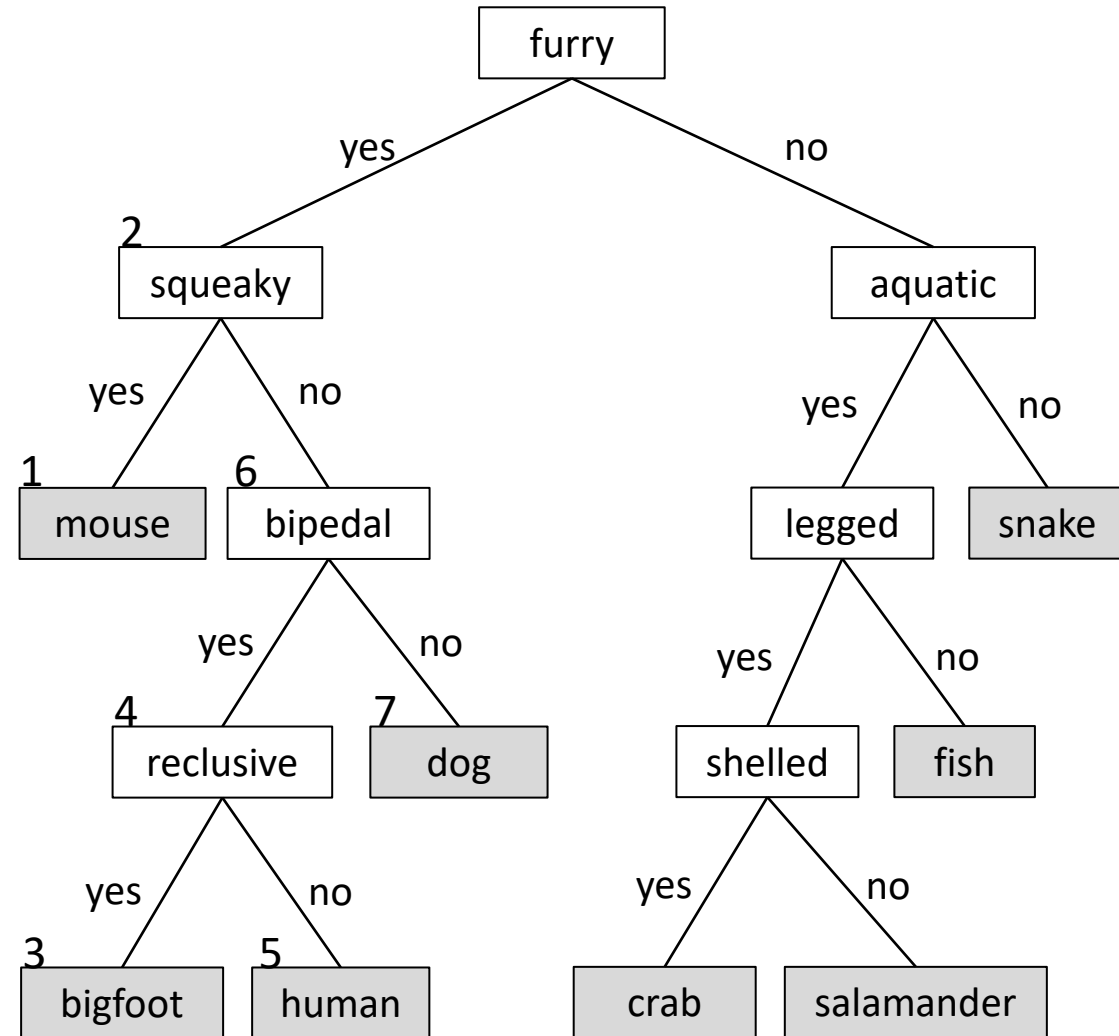


```
public class Node {  
    private String text;  
    private Node yesChild;  
    private Node noChild;  
    private Node parent;  
    private int tag;  
    ...  
}
```

Save to file:

1. Do inorder traversal of tree and assign sequential integer tag values.

File read/writing

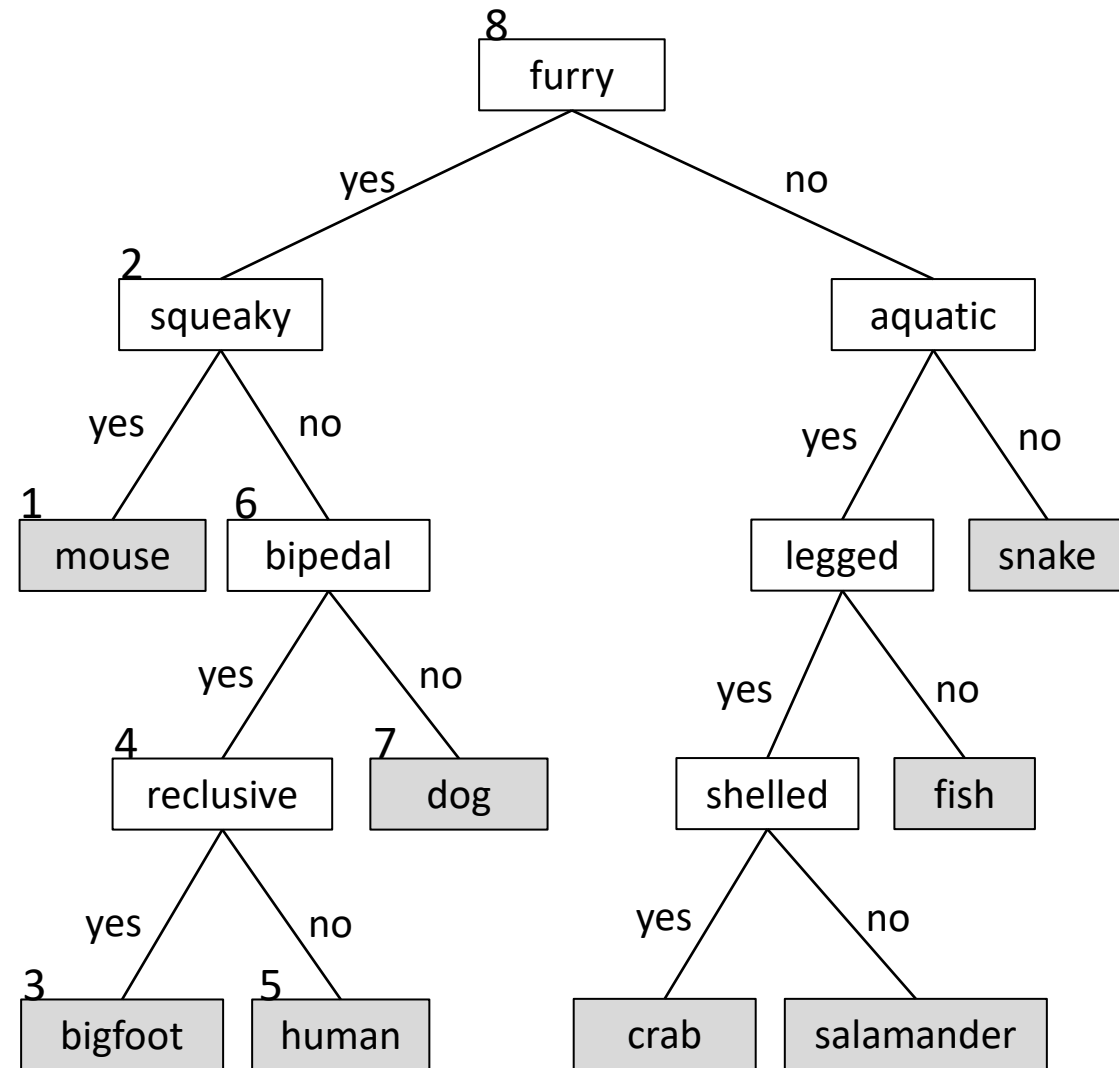


```
public class Node {  
    private String text;  
    private Node yesChild;  
    private Node noChild;  
    private Node parent;  
    private int tag;  
    ...  
}
```

Save to file:

1. Do inorder traversal of tree and assign sequential integer tag values.

File read/writing

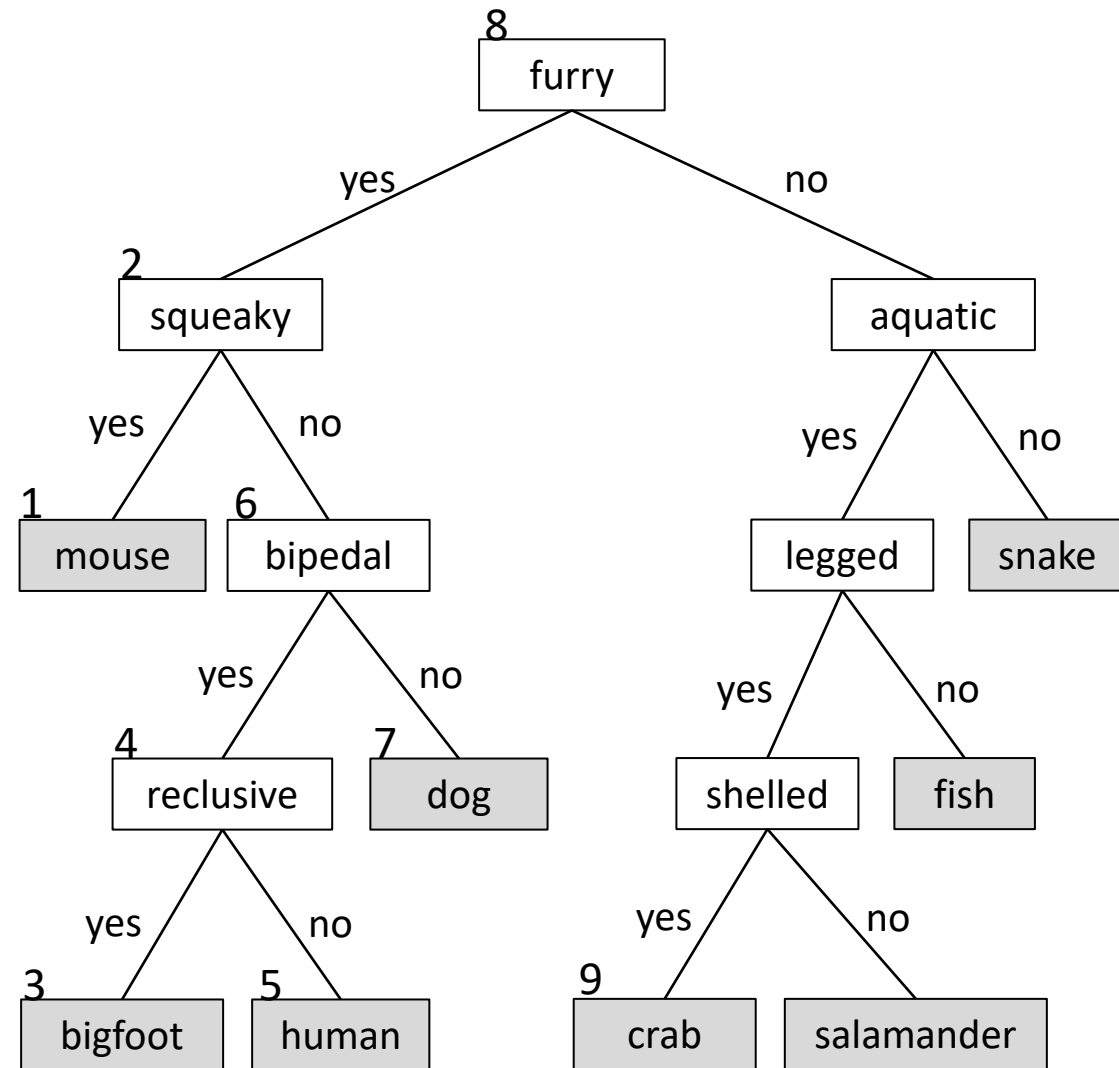


```
public class Node {  
    private String text;  
    private Node yesChild;  
    private Node noChild;  
    private Node parent;  
    private int tag;  
    ...  
}
```

Save to file:

1. Do inorder traversal of tree and assign sequential integer tag values.

File read/writing

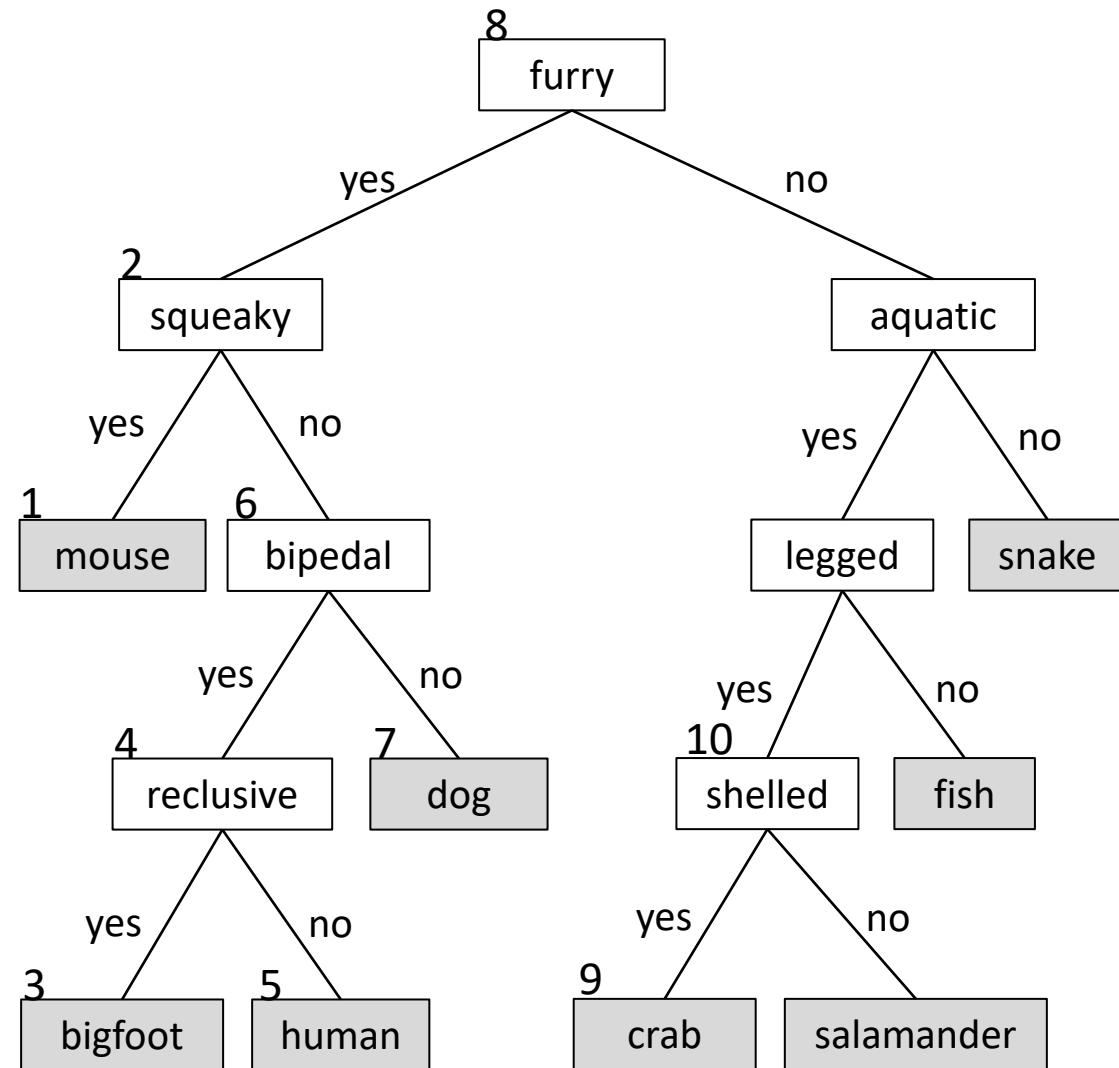


```
public class Node {  
    private String text;  
    private Node yesChild;  
    private Node noChild;  
    private Node parent;  
    private int tag;  
    ...  
}
```

Save to file:

1. Do inorder traversal of tree and assign sequential integer tag values.

File read/writing

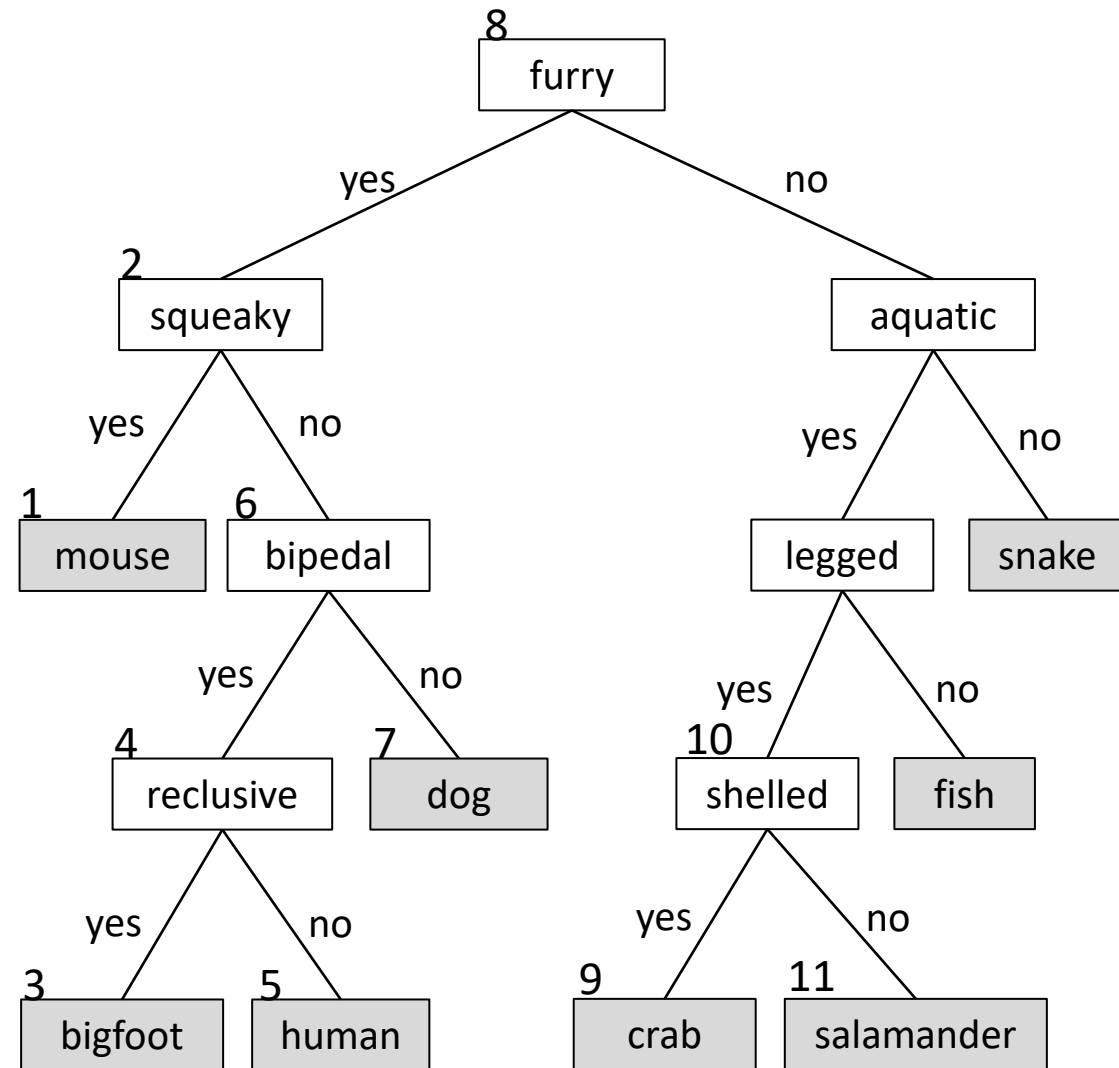


```
public class Node {  
    private String text;  
    private Node yesChild;  
    private Node noChild;  
    private Node parent;  
    private int tag;  
    ...  
}
```

Save to file:

1. Do inorder traversal of tree and assign sequential integer tag values.

File read/writing

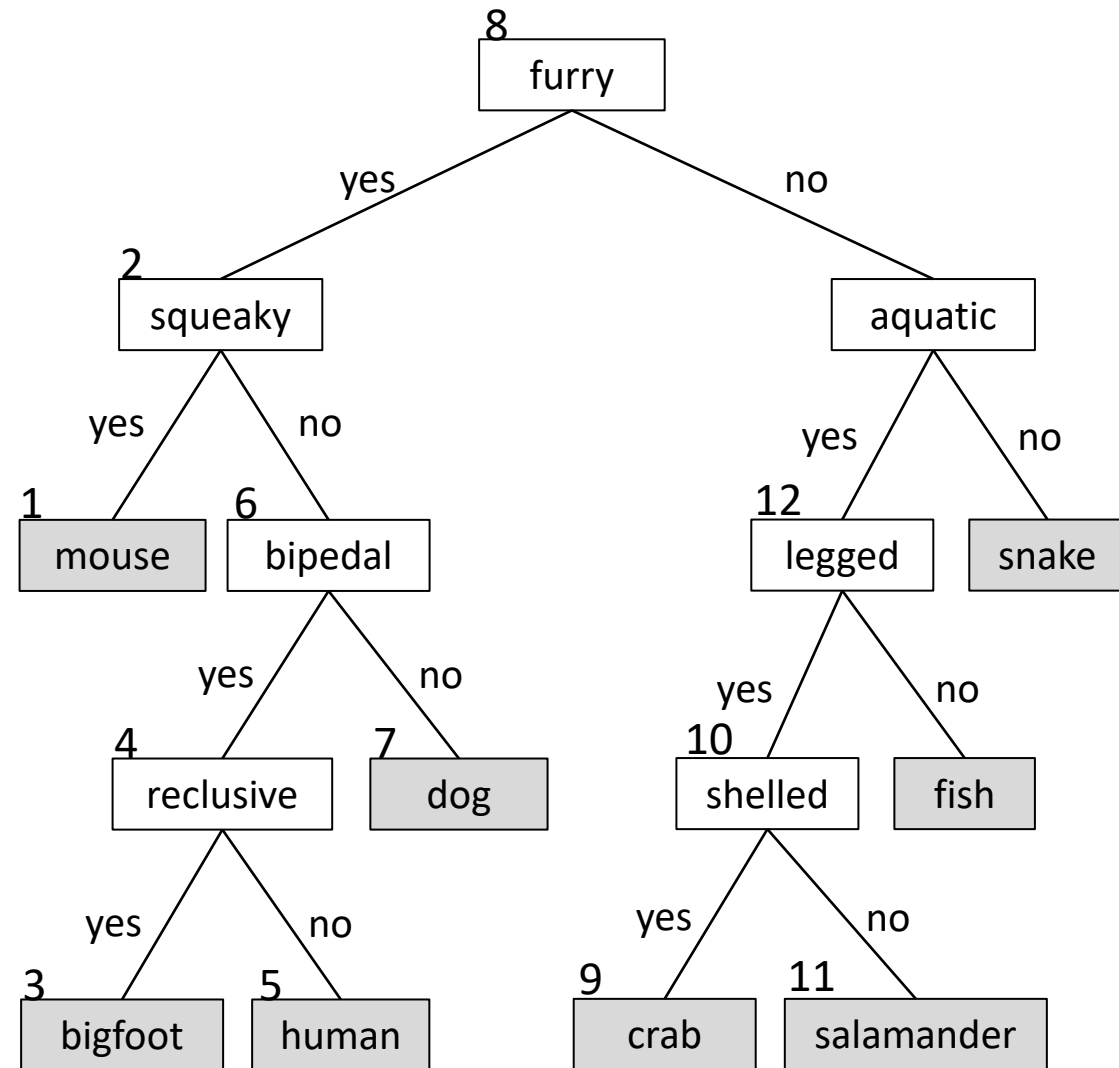


```
public class Node {  
    private String text;  
    private Node yesChild;  
    private Node noChild;  
    private Node parent;  
    private int tag;  
    ...  
}
```

Save to file:

1. Do inorder traversal of tree and assign sequential integer tag values.

File read/writing

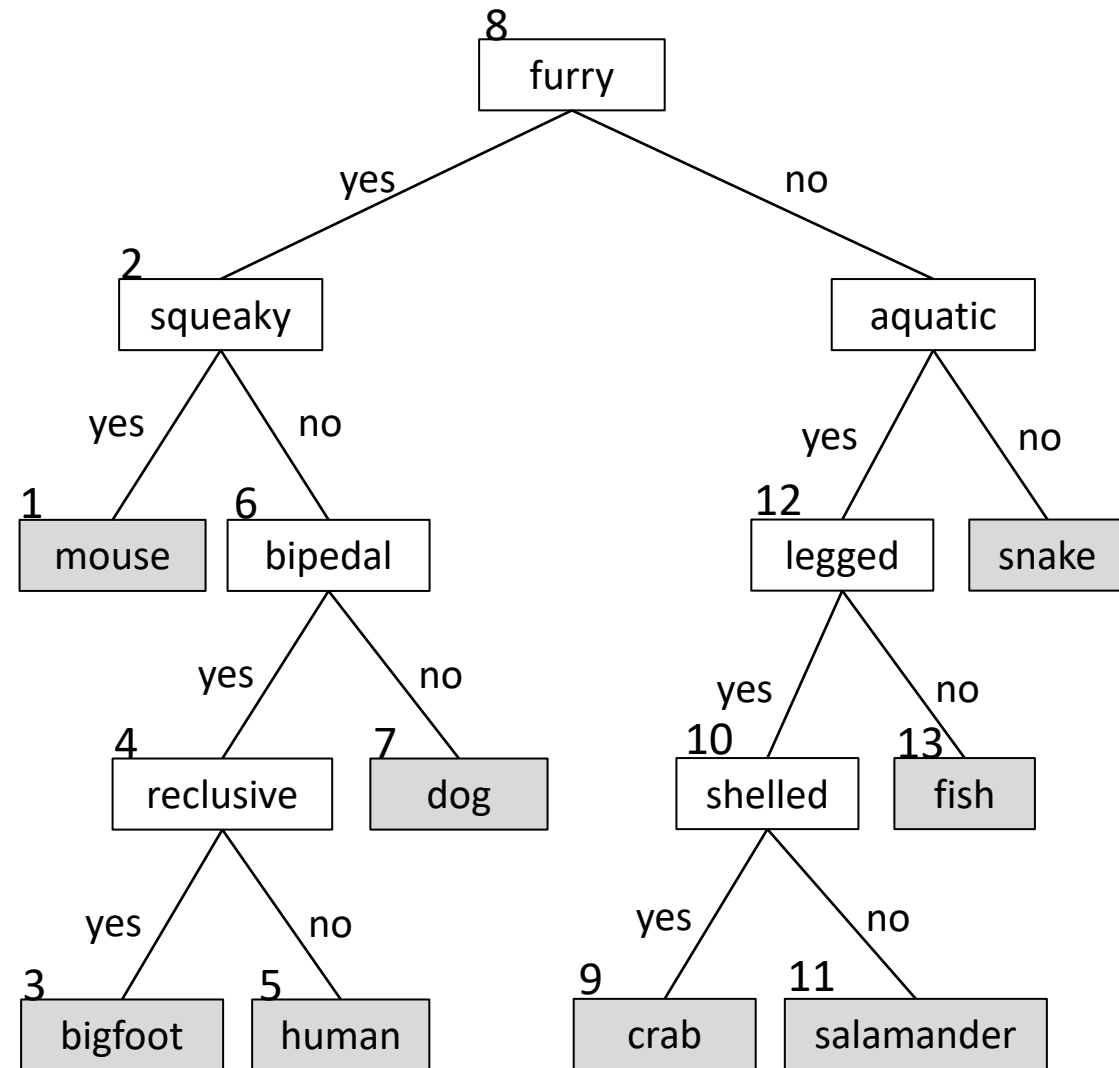


```
public class Node {  
    private String text;  
    private Node yesChild;  
    private Node noChild;  
    private Node parent;  
    private int tag;  
    ...  
}
```

Save to file:

1. Do inorder traversal of tree and assign sequential integer tag values.

File read/writing

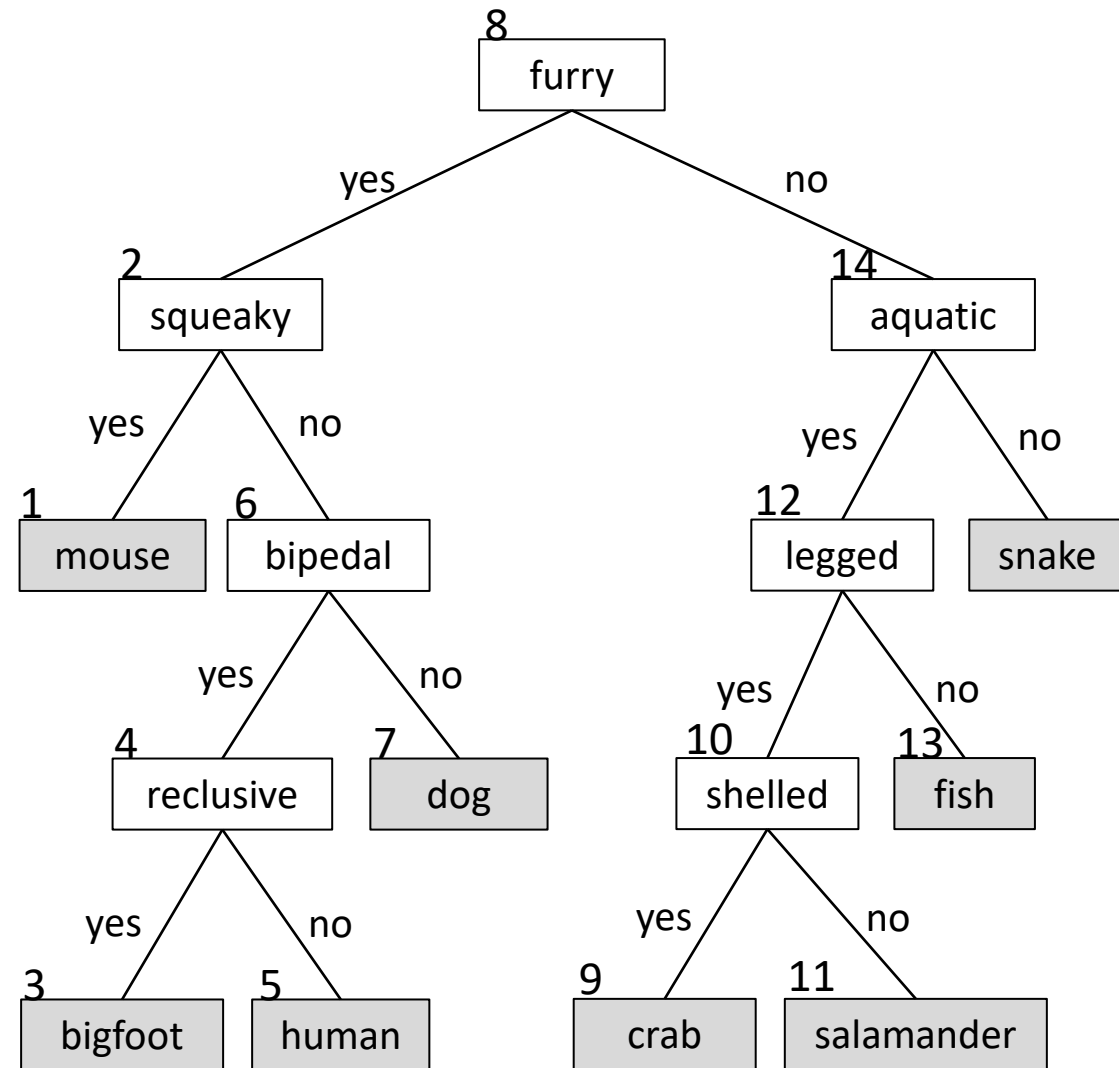


```
public class Node {  
    private String text;  
    private Node yesChild;  
    private Node noChild;  
    private Node parent;  
    private int tag;  
    ...  
}
```

Save to file:

1. Do inorder traversal of tree and assign sequential integer tag values.

File read/writing

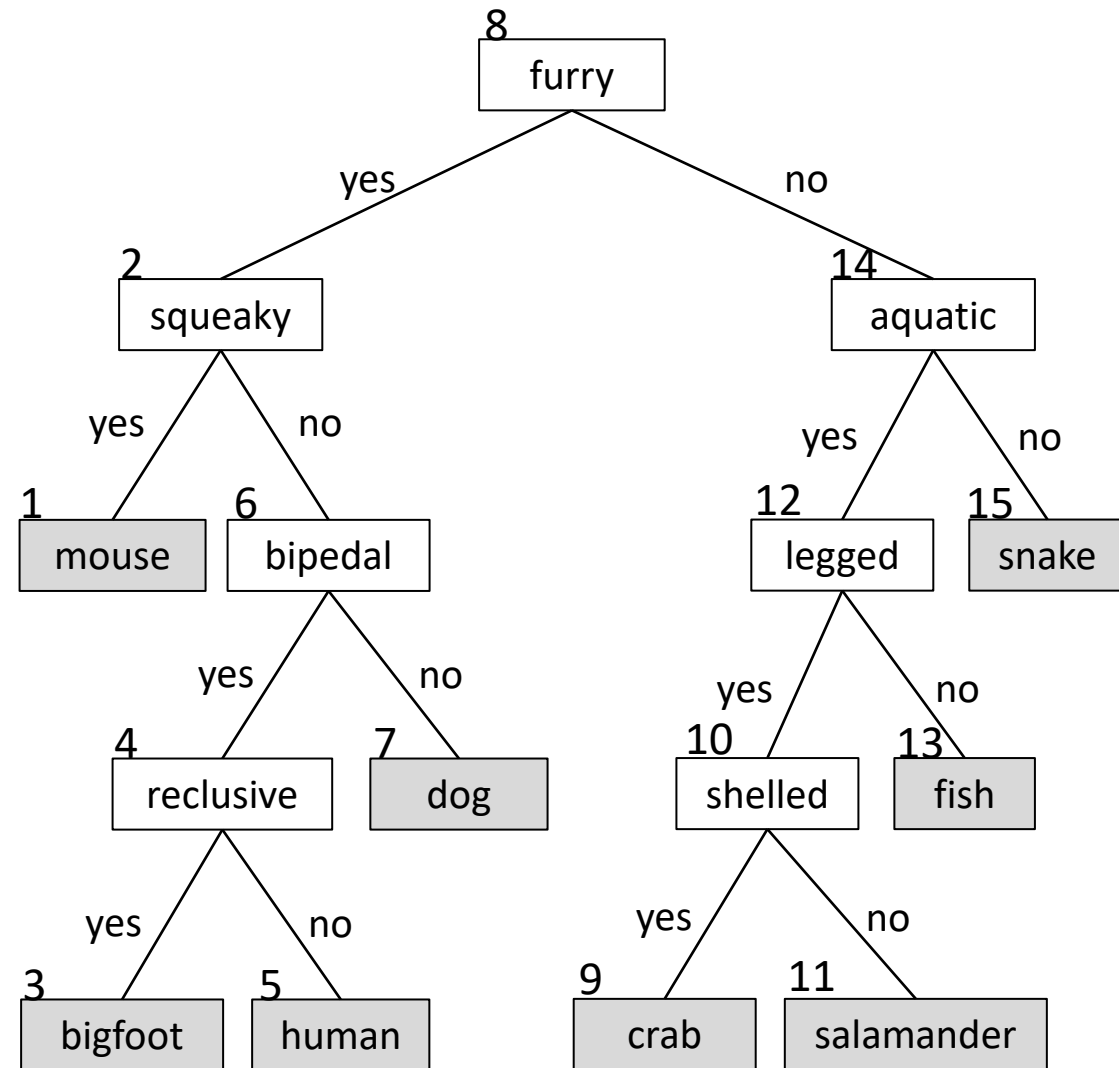


```
public class Node {  
    private String text;  
    private Node yesChild;  
    private Node noChild;  
    private Node parent;  
    private int tag;  
    ...  
}
```

Save to file:

1. Do inorder traversal of tree and assign sequential integer tag values.

File read/writing

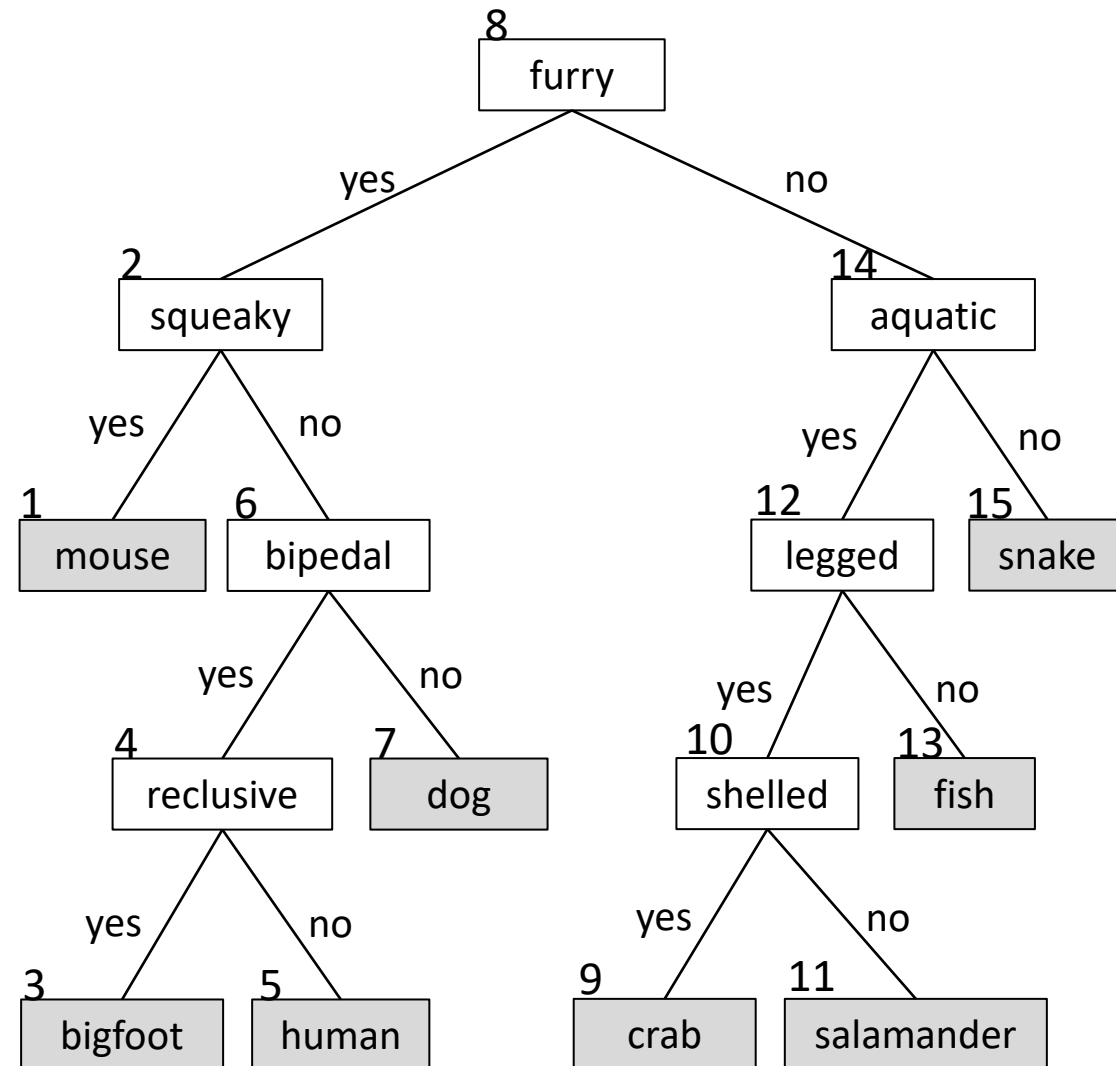


```
public class Node {  
    private String text;  
    private Node yesChild;  
    private Node noChild;  
    private Node parent;  
    private int tag;  
    ...  
}
```

Save to file:

1. Do inorder traversal of tree and assign sequential integer tag values.

File read/writing



```

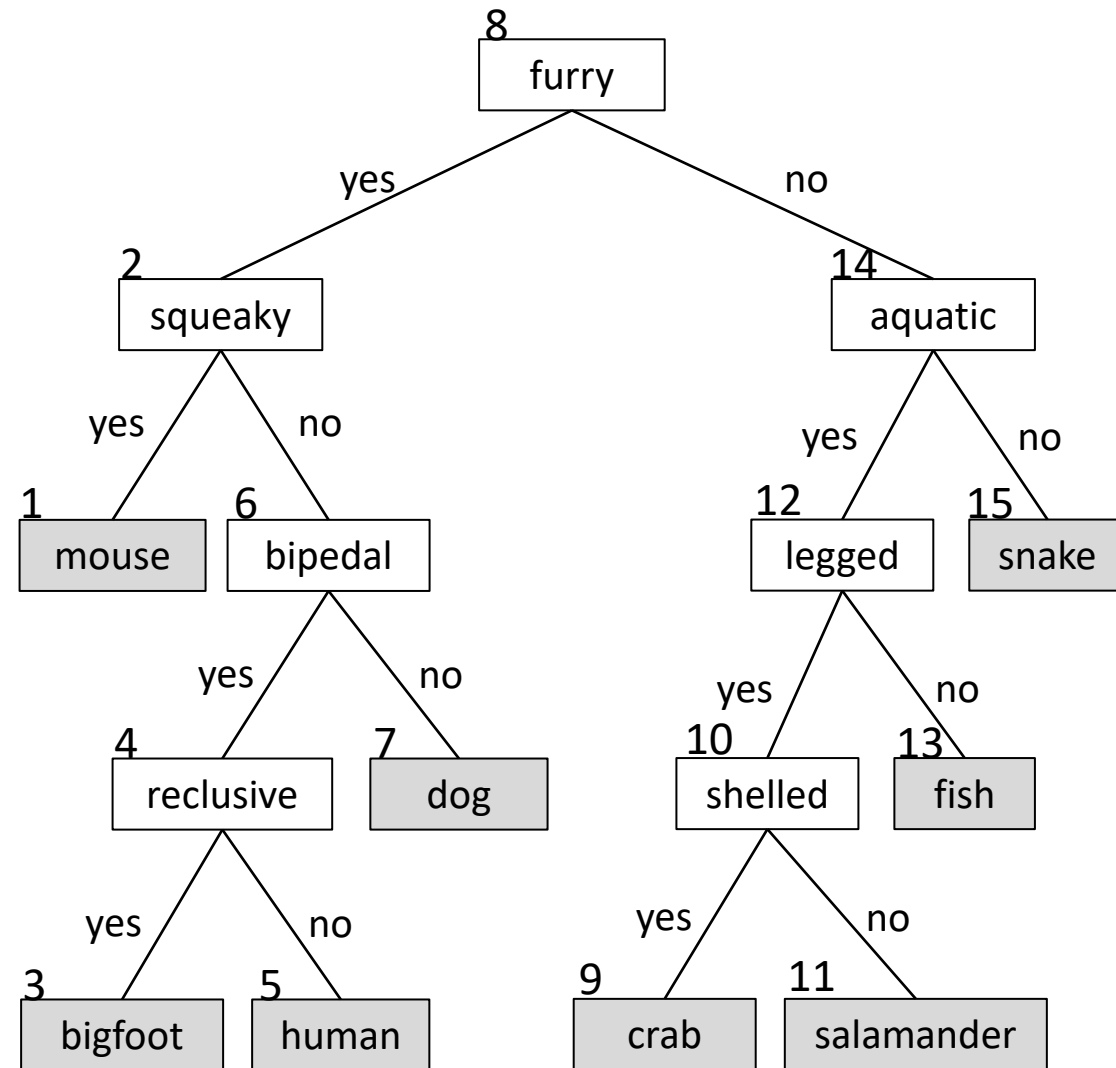
public class Node {
    private String text;
    private Node yesChild;
    private Node noChild;
    private Node parent;
    private int tag;

    ...
}
  
```

Save to file:

1. Do inorder traversal of tree and assign sequential integer tag values.
2. Do breadth first traversal and write tag and text values to file. E.g. 8-furry,2-squeaky,14-aquatic,1-mouse,6-bipedal,...

File read/writing



```

public class Node {
    private String text;
    private Node yesChild;
    private Node noChild;
    private Node parent;
    private int tag;

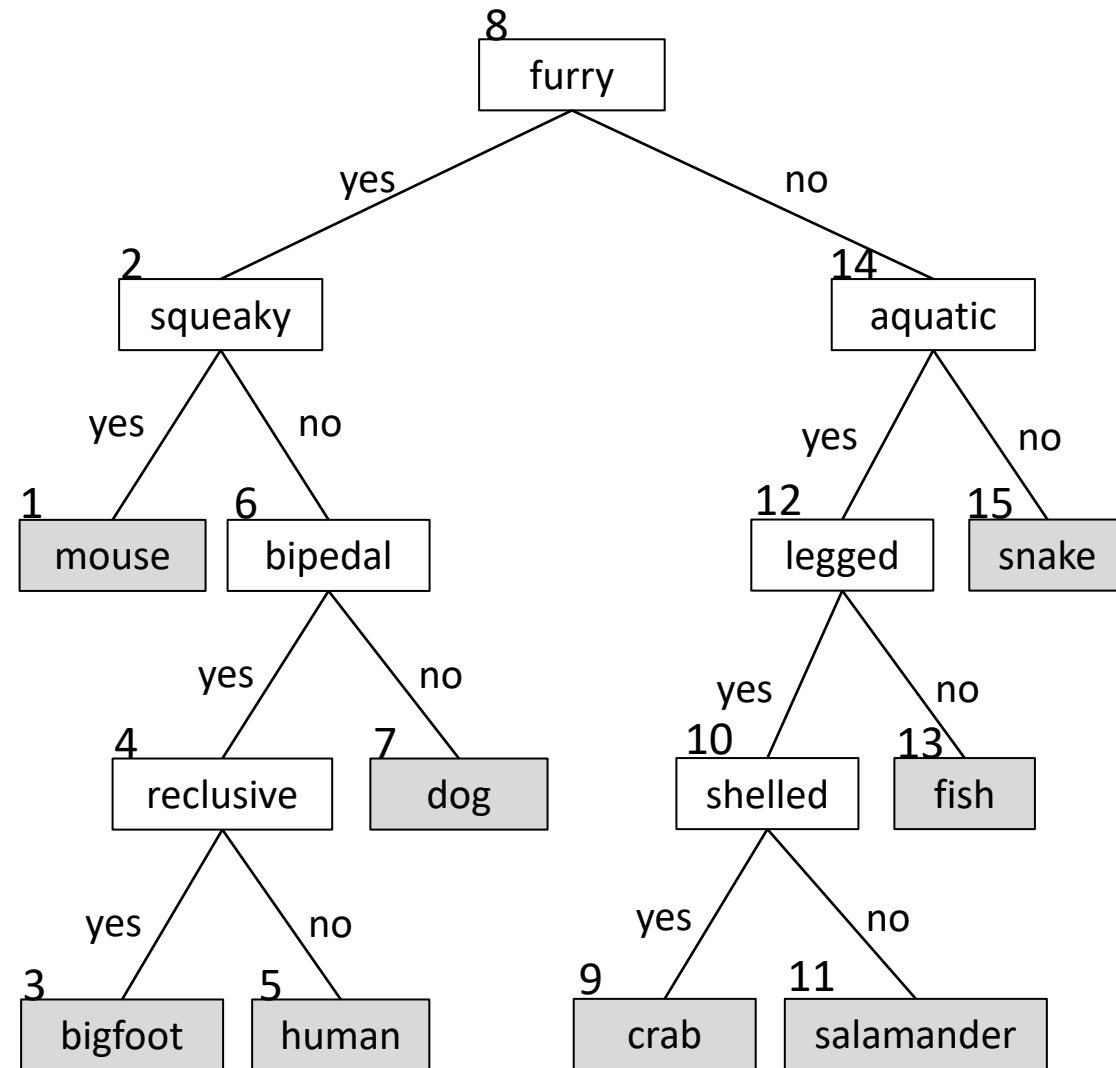
    ...
}
  
```

Save to file:

1. Do inorder traversal of tree and assign sequential integer tag values.
2. Do breadth first traversal and write tag and text values to file. E.g. 8-furry,2-squeaky,14-aquatic,1-mouse,6-bipedal,...

Build from file:

File read/writing



File read/writing

```

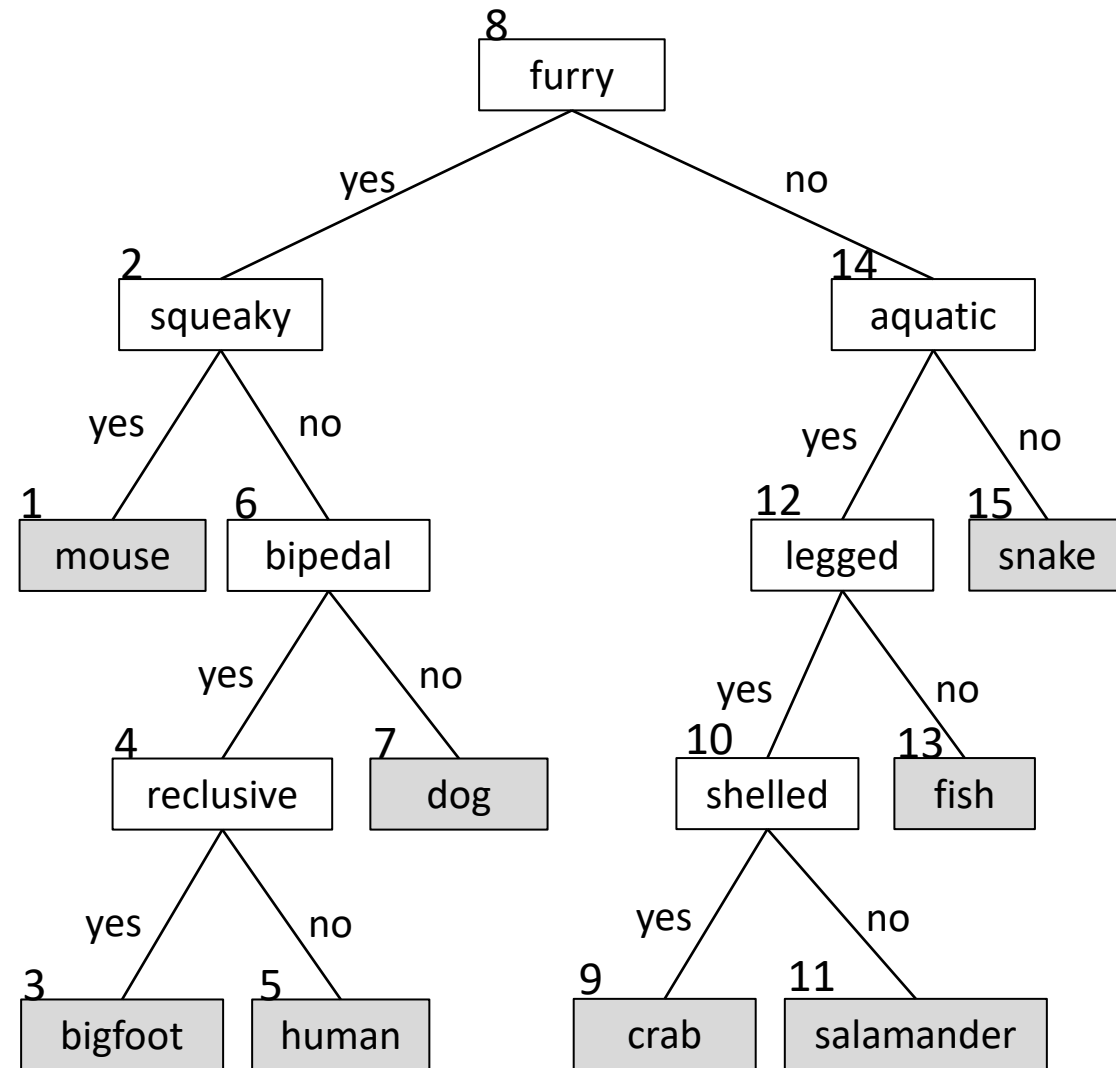
public class Node {
    private String text;
    private Node yesChild;
    private Node noChild;
    private Node parent;
    private int tag;
    ...
}
  
```

Save to file:

1. Do inorder traversal of tree and assign sequential integer tag values.
2. Do breadth first traversal and write tag and text values to file. E.g. 8-furry,2-squeaky,14-aquatic,1-mouse,6-bipedal,...

Build from file:

1. Parse input on commas to get each entry.
2. Parse each entry on dash to get tag value and text value.



File read/writing

```

public class Node {
    private String text;
    private Node yesChild;
    private Node noChild;
    private Node parent;
    private int tag;

    ...
}
  
```

Save to file:

1. Do inorder traversal of tree and assign sequential integer tag values.
2. Do breadth first traversal and write tag and text values to file. E.g. 8-furry,2-squeaky,14-aquatic,1-mouse,6-bipedal,...

Build from file:

1. Parse input on commas to get each entry.
2. Parse each entry on dash to get tag value and text value.
3. Use BST insert method to put tag/text where it should be.

