

CSCI 132:

Basic Data Structures and Algorithms

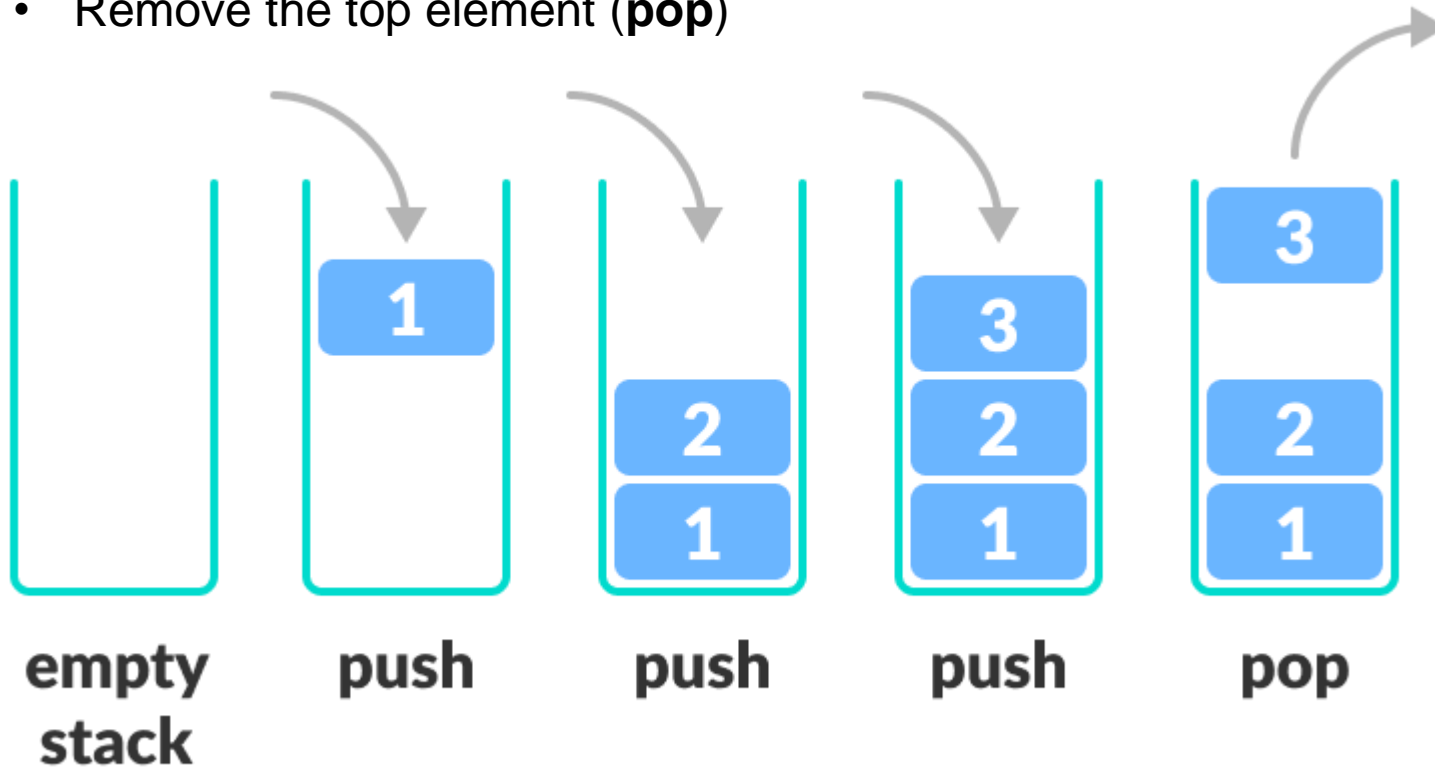
Stacks (Linked List implementation)

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A **stack** is a data structure that can hold data, and follows the **last in first out (LIFO)** principle

We can:

- Add an element to the top of the stack (**push**)
- Remove the top element (**pop**)



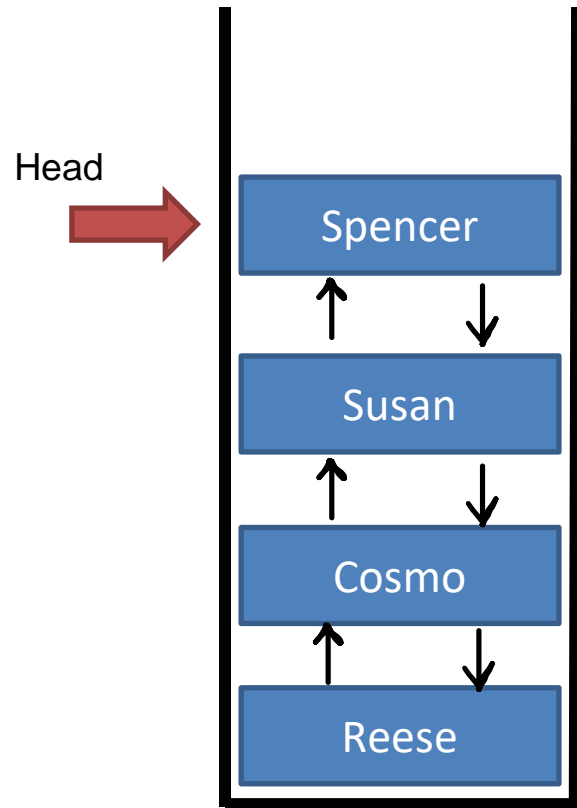
We can implement a Stack using an Array, or a linked List

Stack Implementation (Linked List)

We will import the Linked List Library (we will not write our own linked list class)

To Do List:

- Push()
- Pop()
- Peek()
- IsEmpty()



If we don't know how big our stack needs to be ahead of time, then using a linked list will be a better choice than an array/arraylist

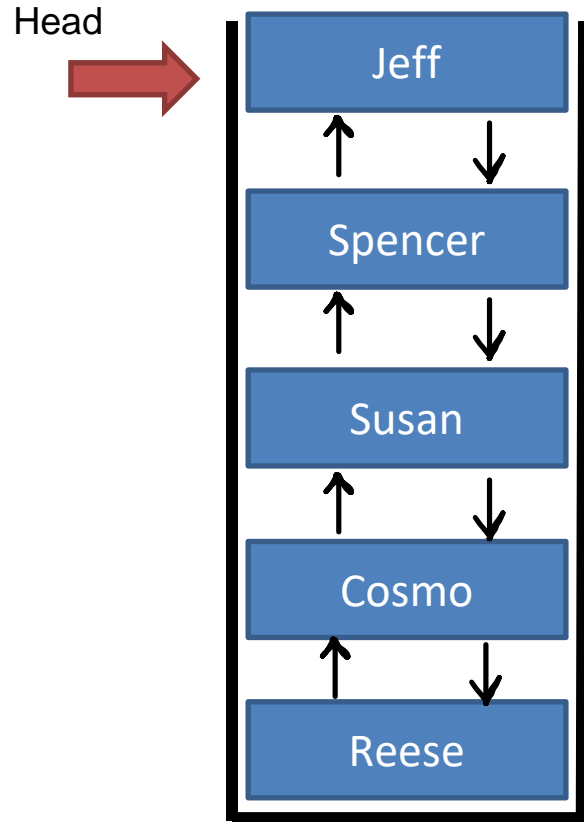
The top of the stack will be the head of the linked list

Stack Implementation (Linked List)

We will import the Linked List Library (we will not write our own linked list class)

To Do List:

- Push()
- Pop()
- Peek()
- IsEmpty()



```
stack.push("Jeff")
```

Whenever we add something to the stack, we add the element to the front of the linked list

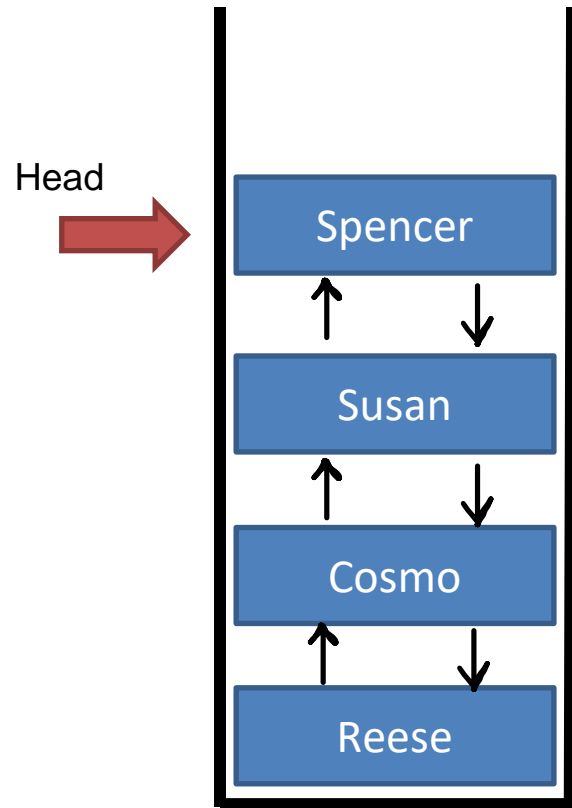
The top of the stack will be the head of the linked list

Stack Implementation (Linked List)

We will import the Linked List Library (we will not write our own linked list class)

To Do List:

- Push()
- Pop()
- Peek()
- IsEmpty()



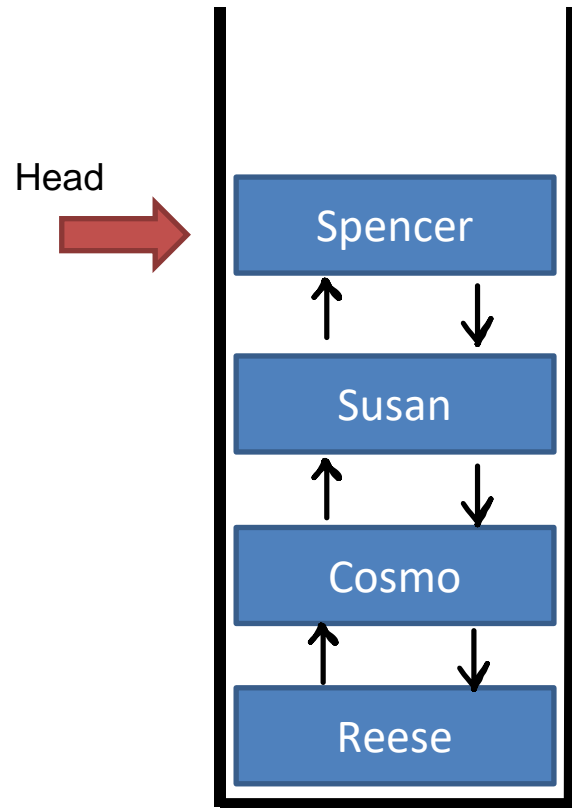
`stack.pop()`

Whenever we remove an element from the stack (`pop()`), we always remove the head node of the linked list

The top of the stack will be the head of the linked list

Stack Implementation (Linked List)

We will import the **Linked List Library** (we will not write our own linked list class)



```
public void push(newElement){  
    addToFront(newElement);  
    size++  
}
```

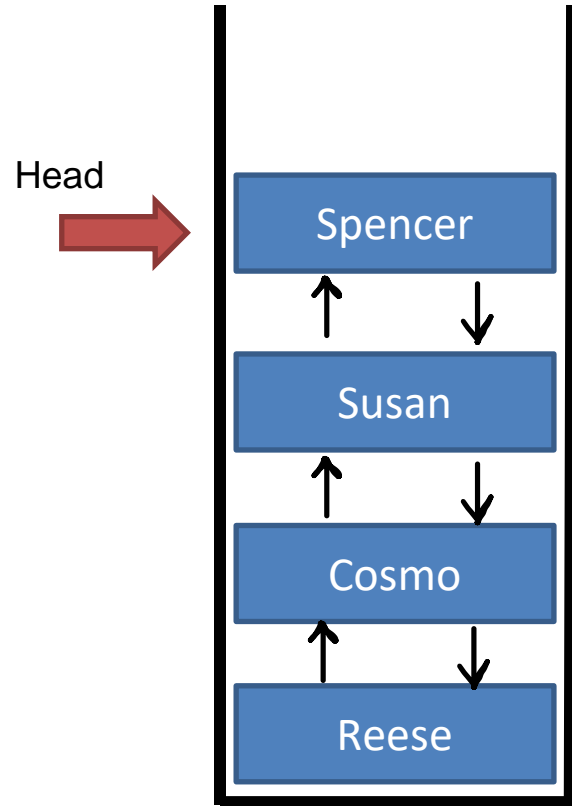
To Do List:

- Push()
- Pop()
- Peek()
- IsEmpty()

When we use a linked list, we are no longer restricted by a fixed size

Stack Implementation (Linked List)

We will import the Linked List Library (we will not write our own linked list class)



```
public void push(newElement){  
  
    addToFront(newElement);  
    size++  
    top_of_stack = head  
  
}  
  
public void pop(){  
    If size == 0:  
        return  
    Else:  
        removeFront()  
        size--  
        top_of_stack = head  
  
}
```

To Do List:

- Push()
- Pop()
- Peek()
- IsEmpty()

When we use a linked list, we are no longer restricted by a fixed size

Stack Runtime Analysis

(Array Implementation)

```
public StackArray() {
    data = new VideoGame[8];
    top_of_stack = -1;
    size = 0;
}
```

Algorithm	w/ Array	w/ Linked List
Creation		
Push()		
Pop()		
peek()		
Print()		

(Linked List Implementation)

```
public StackLinkedList() {
    data = new LinkedList<VideoGame>();
    top_of_stack = null;
    this.size = 0;
}
```


Stack Runtime Analysis

(Array Implementation)

```
public StackArray() {
    data = new VideoGame[8]; O(n)
    top_of_stack = -1; O(1)
    size = 0; O(1)
}
```

Total Running time: $O(n)$ $n = |array|$

Algorithm	w/ Array	w/ Linked List
Creation	$O(n)$	$O(1)$
Push()		
Pop()		
peek()		
Print()		

(Linked List Implementation)

```
public StackLinkedList() {
    data = new LinkedList<VideoGame>(); O(1)
    top_of_stack = null; O(1)
    this.size = 0; O(1)
}
```

Total Running time: $O(1)$

Stack Runtime Analysis

(Array Implementation)

```
public StackArray() {
    data = new VideoGame[8]; O(n)
    top_of_stack = -1; O(1)
    size = 0; O(1)
}
```

Total Running time: $O(n)$ $n = |array|$

Algorithm	w/ Array	w/ Linked List
Creation	$O(n)$	$O(1)$
Push()		
Pop()		
peek()		
Print()		

(Linked List Implementation)

```
public StackLinkedList() {
    data = new LinkedList<VideoGame>(); O(1)
    top_of_stack = null; O(1)
    this.size = 0; O(1)
}
```

Total Running time: $O(1)$

Stack Runtime Analysis

Algorithm	w/ Array	w/ Linked List
Creation	$O(n)$	$O(1)$
Push()		
Pop()		
peek()		
Print()		

(Array Implementation)

```
public void push(VideoGame newVideoGame) {  
  
    if(this.size == this.data.length) {  
        return;  
    }  
    else {  
        This.top_of_stack++;  
        data[this.top_of_stack] = newVideoGame;  
        this.size++;  
    }  
}
```

Stack Runtime Analysis

(Array Implementation)

Algorithm	w/ Array	w/ Linked List
Creation	O(n)	O(1)
Push()	O(1)	
Pop()		
peek()		
Print()		

```
public void push(VideoGame newVideoGame) {  
  
    if(this.size == this.data.length) { O(1)  
        return; O(1)  
    }  
    else {  
        this.top_of_stack++; O(1)  
        data[this.top_of_stack] = newVideoGame; O(1)  
        this.size++; O(1)  
    }  
}
```

Total Running Time: O(1)

Stack Runtime Analysis

Algorithm	w/ Array	w/ Linked List
Creation	$O(n)$	$O(1)$
Push()	$O(1)$	
Pop()		
peek()		
Print()		

(Linked List Implementation)

```
public void push(VideoGame newVideoGame) {  
  
    data.addFirst(newVideoGame);  
    this.top_of_stack = this.data.getFirst();  
    this.size++;  
  
}
```

Stack Runtime Analysis

Algorithm	w/ Array	w/ Linked List
Creation	$O(n)$	$O(1)$
Push()	$O(1)$	$O(1)$
Pop()		
peek()		
Print()		

(Linked List Implementation)

```
public void push(VideoGame newVideoGame) {  
  
    data.addFirst(newVideoGame);  $O(1)$   
    this.top_of_stack = this.data.getFirst();  $O(1)$   
    this.size++;  $O(1)$   
  
}
```

Total Running Time: $O(1)$

Stack Runtime Analysis

(Array)

```
public void pop() {
    if(this.size == 0) {
        return;
    }
    else {
        this.data[this.top_of_stack] = null;
        this.top_of_stack--;
        this.size--;
    }
}
```

Algorithm	w/ Array	w/ Linked List
Creation	O(n)	O(1)
Push()	O(1)	O(1)
Pop()		
peek()		
Print()		

```
public void pop() { (Linked List)
    if(this.size == 0) {
        return;
    }
    else {
        this.data.removeFirst();
        this.top_of_stack = this.data.getFirst();
        this.size--;
    }
}
```

Stack Runtime Analysis

(Array)

```
public void pop() {
    if(this.size == 0) { O(1)
        return; O(1)
    }
    else {
        this.data[this.top_of_stack] = null; O(1)
        this.top_of_stack--; O(1)
        this.size--; O(1)
    }
}
```

Total Running Time: O(1)

Algorithm	w/ Array	w/ Linked List
Creation	O(n)	O(1)
Push()	O(1)	O(1)
Pop()	O(1)	O(1)
peek()		
Print()		

```
public void pop() { (Linked List)
    if(this.size == 0) { O(1)
        return;O(1)
    }
    else { O(1)
        this.data.removeFirst(); O(1)
        this.top_of_stack = this.data.getFirst();O(1)
        this.size--; O(1)
    }
}
```

Total Running Time: O(1)

Stack Runtime Analysis

(Array)

```
public VideoGame peek() {
    if(this.size != 0) {
        return this.data[this.top_of_stack];
    }
    else {
        return null;
    }
}
```

Algorithm	w/ Array	w/ Linked List
Creation	O(n)	O(1)
Push()	O(1)	O(1)
Pop()	O(1)	O(1)
peek()		
Print()		

(Linked List)

```
public VideoGame peek() {
    if(this.size != 0) {
        return this.top_of_stack;
    }
    else {
        return null;
    }
}
```

Stack Runtime Analysis

(Array)

```
public VideoGame peek() {
    if(this.size != 0) { O(1)
        return this.data[this.top_of_stack]; O(1)
    }
    else {
        return null; O(1)
    }
}
```

Total Running Time: O(1)

Algorithm	w/ Array	w/ Linked List
Creation	O(n)	O(1)
Push()	O(1)	O(1)
Pop()	O(1)	O(1)
peek()	O(1)	O(1)
Print()		

(Linked List)

```
public VideoGame peek() {
    if(this.size != 0) { O(1)
        return this.top_of_stack; O(1)
    }
    else { O(1)
        return null; O(1)
    }
}
```

Total Running Time: O(1)

Stack Runtime Analysis

(Array)

```
public void printStack() {
    for(int i = this.size-1; i >= 0; i--) {
        this.data[i].printInfo();
    }
}
```

Algorithm	w/ Array	w/ Linked List
Creation	O(n)	O(1)
Push()	O(1)	O(1)
Pop()	O(1)	O(1)
peek()	O(1)	O(1)
Print()		

(Linked List)

```
public void printStack() {
    for(int i = 0; i < this.data.size(); i++) {
        this.data.get(i).printInfo();
    }
}
```

Stack Runtime Analysis

(Array)

```
public void printStack() {
    for(int i = this.size-1; i >= 0; i--) {
        this.data[i].printInfo();
    }
}
```

Algorithm	w/ Array	w/ Linked List
Creation	O(n)	O(1)
Push()	O(1)	O(1)
Pop()	O(1)	O(1)
peek()	O(1)	O(1)
Print()		

Both of these for loops go through the stack and print out all N elements → O(n) where n = # of elements in the stack

(Linked List)

```
public void printStack() {
    for(int i = 0; i < this.data.size(); i++) {
        this.data.get(i).printInfo();
    }
}
```

Stack Runtime Analysis

(Array)

```
public void printStack() {  
    for(int i = this.size-1; i >= 0; i--) {  
        this.data[i].printInfo();  
    }  
}
```

Algorithm	w/ Array	w/ Linked List
Creation	$O(n)$	$O(1)$
Push()	$O(1)$	$O(1)$
Pop()	$O(1)$	$O(1)$
peek()	$O(1)$	$O(1)$
Print()	$O(n)$	$O(n)$

Total Running Time: $O(n)$

(Linked List)

```
public void printStack() {  
    for(int i = 0; i < this.data.size(); i++) {  
        this.data.get(i).printInfo();  
    }  
}
```

The .get() method actually runs in linear time ($O(n)$)

Total Running Time: $O(n^2)$

n = # of elements in the stack

Stack Runtime Analysis

(Array)

```
public void printStack() {  
    for(int i = this.size-1; i >= 0; i--) {  
        this.data[i].printInfo();  
    }  
}
```

Algorithm	w/ Array	w/ Linked List
Creation	O(n)	O(1)
Push()	O(1)	O(1)
Pop()	O(1)	O(1)
peek()	O(1)	O(1)
Print()	O(n)	O(n)

Total Running Time: O(n)

(Linked List)

```
public void printStack() {  
    for(VideoGame each : this.data) {  
        each.printInfo();  
    }  
}
```

Total Running Time: O(n)

n = # of elements in the stack

Stack Runtime Analysis

Algorithm	w/ Array	w/ Linked List
Creation	$O(n)$	$O(1)$
Push()	$O(1)$	$O(1)$
Pop()	$O(1)$	$O(1)$
peek()	$O(1)$	$O(1)$
Print()	$O(n)$	$O(n)$

Takeaways: Adding and removing elements from a stack runs in constant time ($O(1)$) *(we like algorithms that run in constant time!!)*

Stack Runtime Analysis

Algorithm	w/ Array	w/ Linked List
Creation	$O(n)$	$O(1)$
Push()	$O(1)$	$O(1)$
Pop()	$O(1)$	$O(1)$
peek()	$O(1)$	$O(1)$
Print()	$O(n)$	$O(n)$

Takeaways: Adding and removing elements from a stack runs in constant time ($O(1)$) *(we like algorithms that run in constant time!!)*

Downside: Stacks operate in a LIFO structure, which might not be ideal for some data

Stack Runtime Analysis

Algorithm	w/ Array	w/ Linked List
Creation	$O(n)$	$O(1)$
Push()	$O(1)$	$O(1)$
Pop()	$O(1)$	$O(1)$
peek()	$O(1)$	$O(1)$
Print()	$O(n)$	$O(n)$

With an array, our stack size is limited by the size of the array

With a linked list, our stack can grow infinitely*

Stack Runtime Analysis

Algorithm	w/ Array	w/ Linked List
Creation	$O(n)$	$O(1)$
Push()	$O(1)$	$O(1)$
Pop()	$O(1)$	$O(1)$
peek()	$O(1)$	$O(1)$
Print()	$O(n)$	$O(n)$

Arrays are more memory efficient (contiguous memory), but there might be a lot of unused space in an array (not ideal)

Stack Runtime Analysis

Algorithm	w/ Array	w/ Linked List
Creation	$O(n)$	$O(1)$
Push()	$O(1)$	$O(1)$
Pop()	$O(1)$	$O(1)$
peek()	$O(1)$	$O(1)$
Print()	$O(n)$	$O(n)$

Do you know how big the stack needs to be?

Yes → Array

No → Linked List

Program 3