

CSCI 132:

Basic Data Structures and Algorithms

Time Complexity, Big-O

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Spring 2025

Announcements

No Lab next week

Midterm Exam is a week from today
→ Review/Study Guide has been posted

Suppose you are moving across the country. You've contracted a builder to build you a brand-new house. You are trying to plan which date you should put all your belongings in the truck and move to the new house across the country. You ask the builder the following question:

How long will it take to finish building the house?

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The builder is unsure exactly when he will be done, but he offers the following answers in an enclosed envelope. You can only pick one.

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The **fastest** time he
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The **slowest** time he
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The **average** time it takes him to complete a house

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How long will it take to finish building the house?

The builder is unsure exactly when he will be done, but he offers the following answers in an enclosed envelope. You can only pick one.

(We will also assume they won't break any records for fastest/slowest time)

The **fastest** time he has completed a house in the past

"Best case scenario"

The **slowest** time he has completed a house in the past

"Worst case scenario"

The **average** time it takes him to complete a house

Average

Suppose you are moving across the country. You've contracted a builder to build you a brand-new house. You are trying to plan which date you should put all your belongings in the truck and move to the new house across the country. You ask the builder the following question:

How long will it take to finish building the house?

The builder is unsure exactly when he will be done, but he offers the following answers in an enclosed envelope. You can only pick one.

The **slowest** time he has completed a house in the past

"Worst case scenario"

If we select this option, we are **guaranteed** a date that the house will be finished by

(The house might be empty for a few days, but that's much better than having to stay in a hotel until the house is ready)

The **running time** of an algorithm is the time it takes for an algorithm to completely run from start to finish

There are a few ways we can measure running time:

- 1.

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There are a few ways we can measure running time:

~~1. Time (seconds, nanoseconds, minutes, days, etc)~~

Practical, but the hardware of the computer greatly affects the time needed

We need a way to measure running time that is independent from the hardware the computer has

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- ~~1. Time (seconds, nanoseconds, minutes, days, etc)~~
2. Number of **operations** required to complete algorithm.

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To measure the running time of an algorithm, we will count the number of operations the algorithm performs, and look at how these operations scale *as the input increases*

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When we describe the running time of an algorithm, we will represent it using **Big-O Notation**

A **primitive operation** is an operation that has a **constant** execution time

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- Assigning a value to a variable

```
int N = 3;
```

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- Assigning a value to a variable
- Performing an arithmetic operation

```
int N = 3;  
a = a + 3 * 12
```

A **primitive operation** is an operation that has a **constant** execution time

- Assigning a value to a variable
- Performing an arithmetic operation
- Comparing two numbers/values

```
int N = 3;  
a = a + 3 * 12  
if(n >= i)
```

A **primitive operation** is an operation that has a **constant** execution time

- Assigning a value to a variable
- Performing an arithmetic operation
- Comparing two numbers/values
- Accessing an element in an array (by index)

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int N = 3;  
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- Assigning a value to a variable
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- Comparing two numbers/values
- Accessing an element in an array (by index)
- Returning from a method

```
int N = 3;  
a = a + 3 * 12  
if(n >= i)  
i = arr[3]  
return
```

A **primitive operation** is an operation that has a **constant** execution time

- Assigning a value to a variable
- Performing an arithmetic operation
- Comparing two numbers/values
- Accessing an element in an array (by index)
- Returning from a method
- Printing out a value

```
int N = 3;  
a = a + 3 * 12  
if(n >= i)  
i = arr[3]  
return  
System.out.println("Hi")
```

```
public int find_element_in_array(int[] array, int s) {  
    for(int i = 0; i < array.length; i++) {  
        if(array[i] == s) {  
            return i;  
        }  
    }  
    return -1;  
}
```

This algorithm finds the location (index) of an integer **S** in an array of size **N**


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public int find_element_in_array(int[] array, int s) {  
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This algorithm finds the location (index) of an integer **S** in an array of size **N**

The number of operations this algorithm executes varies because...

```
public int find_element_in_array(int[] array, int s) {  
    for(int i = 0; i < array.length; i++) {  
        if(array[i] == s) {  
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        }  
    }  
    return -1;  
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```

This algorithm finds the location (index) of an integer **S** in an array of size **N**

The number of operations this algorithm executes varies **S** will be at different locations

```
public int find_element_in_array(int[] array, int s) {  
    for(int i = 0; i < array.length; i++) {  
        if(array[i] == s) {  
            return i;  
        }  
    }  
    return -1;  
}
```

This algorithm finds the location (index) of an integer **S** in an array of size **N**

This is a **primitive operation**, lets count how many times this operation is executed given some input

```
public int find_element_in_array(int[] array, int s) {  
    for(int i = 0; i < array.length; i++) {  
        if(array[i] == s) {  
            return i;  
        }  
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This algorithm finds the location (index) of an integer **S** in an array of size **N**

S = 5

4	6	3	5	1	8	2	9	7	10
---	---	---	---	---	---	---	---	---	----

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4 operations (5 operations including the return)

```
public int find_element_in_array(int[] array, int s) {  
    for(int i = 0; i < array.length; i++) {  
        if(array[i] == s) {  
            return i;  
        }  
    }  
    return -1;  
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```

This algorithm finds the location (index) of an integer **S** in an array of size **N**

S = ???

4	6	3	5	1	8	2	9	7	10
---	---	---	---	---	---	---	---	---	----

What is the **best-case scenario** for this algorithm (when would this have the shortest running time) ?

```
public int find_element_in_array(int[] array, int s) {  
    for(int i = 0; i < array.length; i++) {  
        if(array[i] == s) {  
            return i;  
        }  
    }  
    return -1;  
}
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This algorithm finds the location (index) of an integer **S** in an array of size **N**

S = 4

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---	---	---	---	---	---	---	---	---	----

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        if(array[i] == s) {  
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        }  
    }  
    return -1;  
}
```

This algorithm finds the location (index) of an integer **S** in an array of size **N**

S = ?

4	6	3	5	1	8	2	9	7	10
---	---	---	---	---	---	---	---	---	----

What is the **worst-case scenario** for this algorithm (when would this have the longest running time) ?

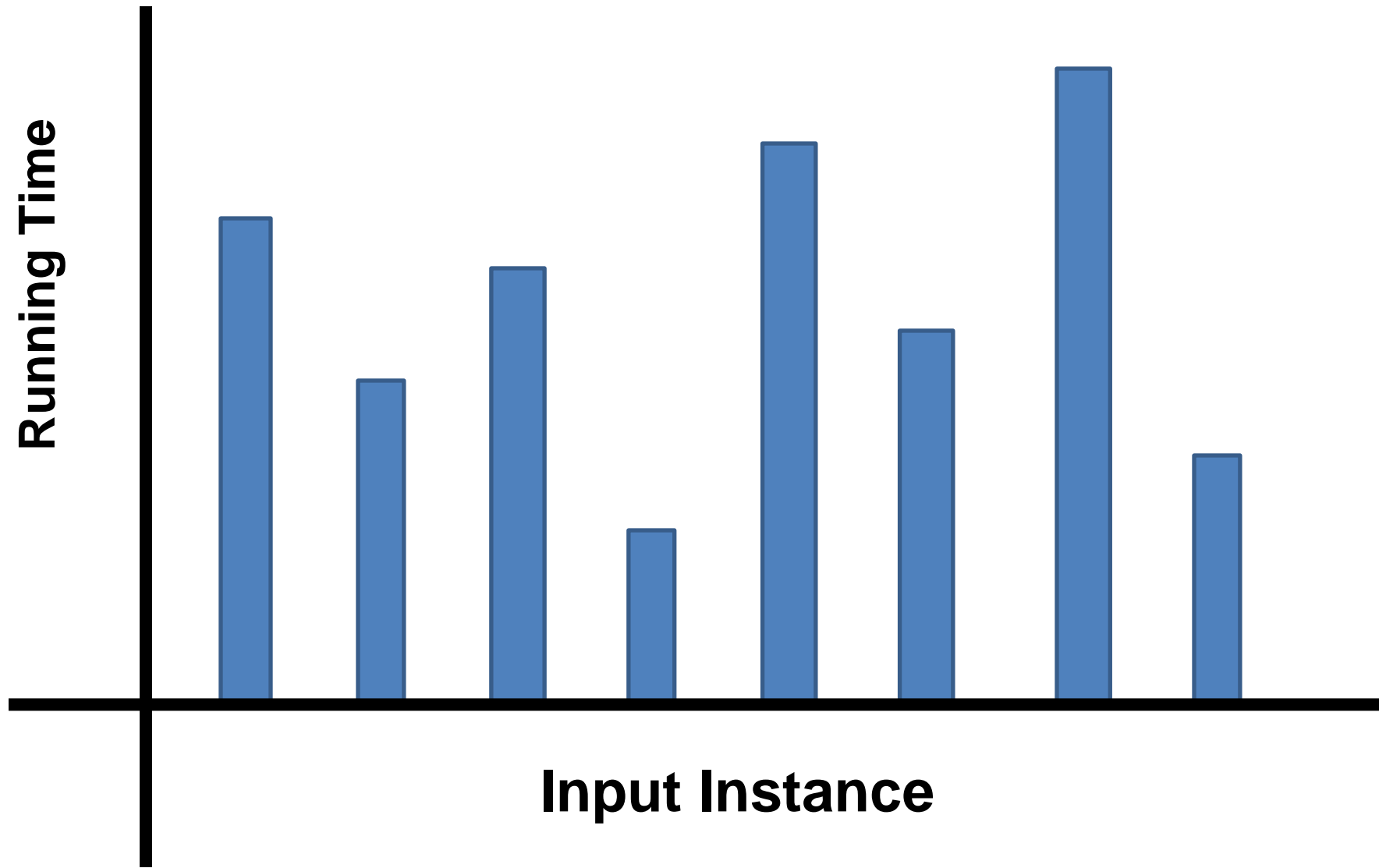
```
public int find_element_in_array(int[] array, int s) {  
    for(int i = 0; i < array.length; i++) {  
        if(array[i] == s) {  
            return i;  
        }  
    }  
    return -1;  
}
```

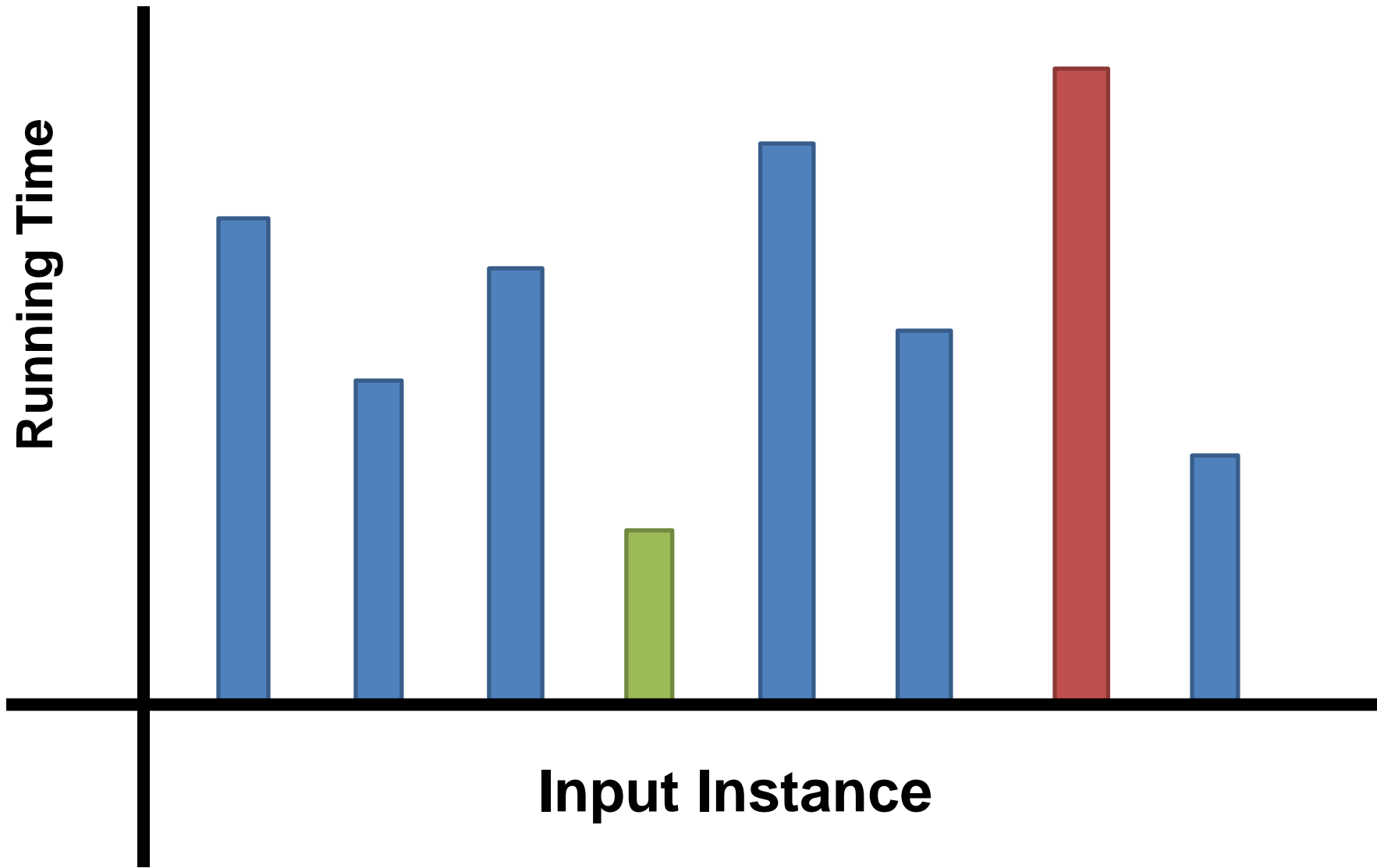
This algorithm finds the location (index) of an integer **S** in an array of size **N**

S = 11

4	6	3	5	1	8	2	9	7	10
---	---	---	---	---	---	---	---	---	----

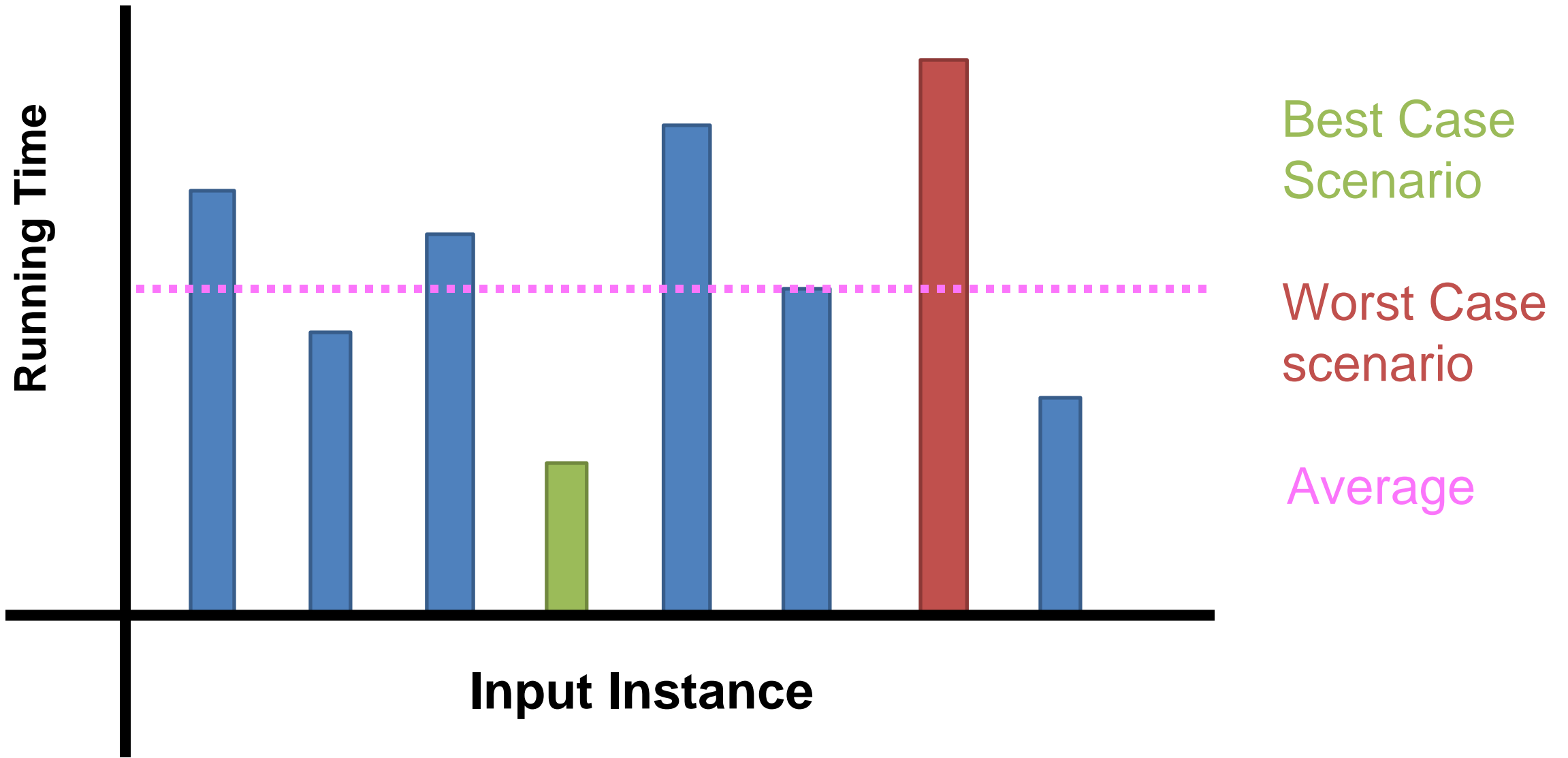
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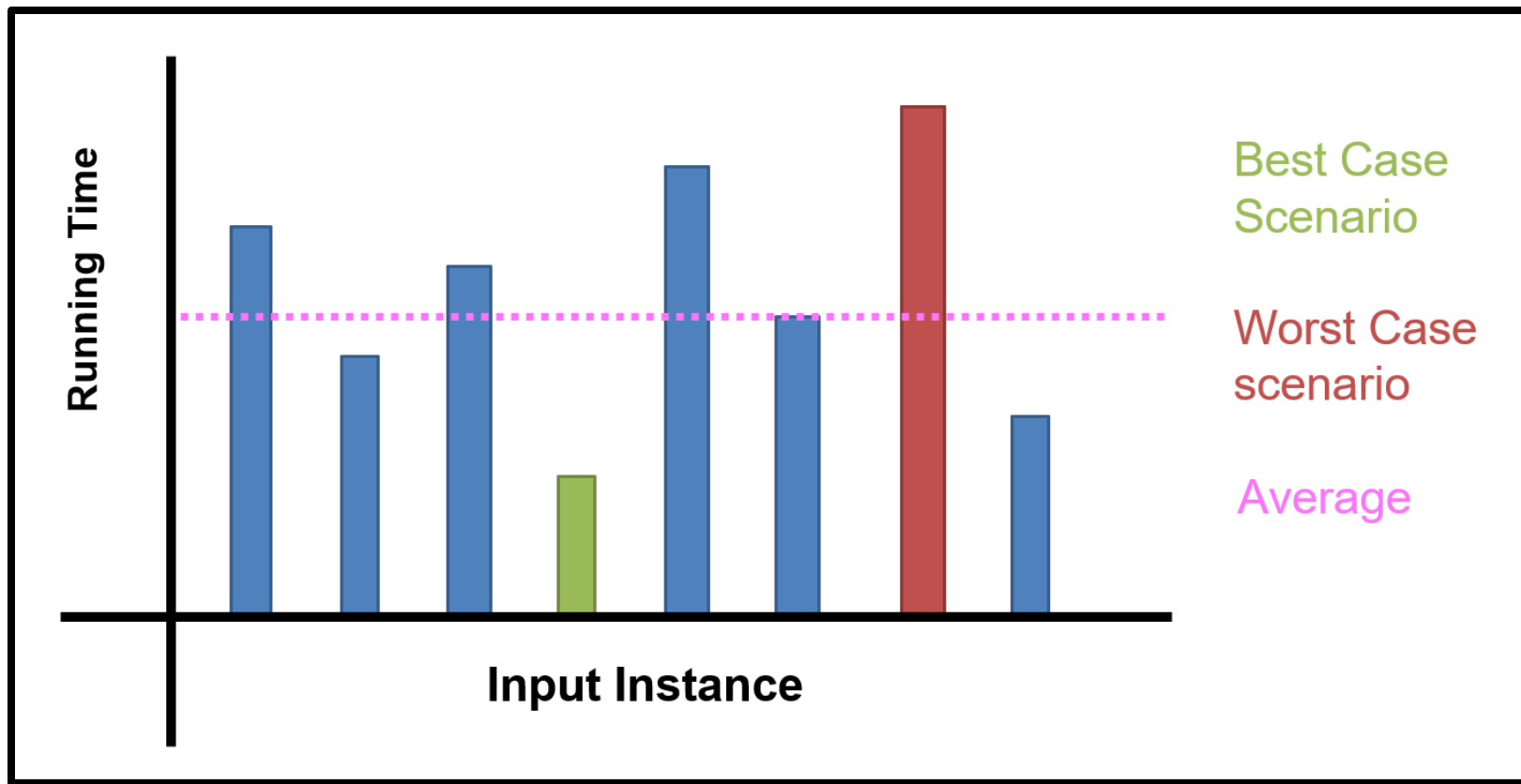




Best Case
Scenario

Worst Case
scenario







In computer science (and this class in particular), we will be focusing on stating running time in terms of **worst-case scenario**

```
public int find_element_in_array(int[] array, int s) {  
    for(int i = 0; i < array.length; i++) {  
        if(array[i] == s) {  
            return i;  
        }  
    }  
    return -1;  
}
```


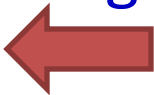
To compute the running time of this algorithm, we will go line-by-line and state the running time of each operation (worst-case scenario)


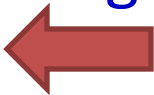
At the end, add everything up to get the total running time

```
public int find_element_in_array(int[] array, int s) {  
    for(int i = 0; i < array.length; i++) {   
        if(array[i] == s) {  
            return i;  
        }  
    }  
    return -1;  
}
```


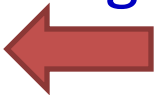

```
public int find_element_in_array(int[] array, int s) {  
    for(int i = 0; i < array.length; i++) {  N  
        if(array[i] == s) {  
            return i;  
        }  
    }  
    return -1;  
}
```

Worse case scenario, this for loop will run N times (N = size of the array)





```
public int find_element_in_array(int[] array, int s) {  
    for(int i = 0; i < array.length; i++) {  N  
        if(array[i] == s) {   
            return i;  
        }  
    }  
    return -1;  
}
```





```
public int find_element_in_array(int[] array, int s) {  
    for(int i = 0; i < array.length; i++) {  N  
        if(array[i] == s) {  1  
            return i;  
        }  
    }  
    return -1;  
}
```

This is a primitive operation, so it will always run in constant time

```
public int find_element_in_array(int[] array, int s) {  
    for(int i = 0; i < array.length; i++) {  N  
        if(array[i] == s) {  1  
            return i;   
        }  
    }  
    return -1;  
}
```



```
public int find_element_in_array(int[] array, int s) {  
    for(int i = 0; i < array.length; i++) {  N  
        if(array[i] == s) {  1  
            return i;  1  
        }  
    }  
    return -1;   
}
```

```
public int find_element_in_array(int[] array, int s) {  
    for(int i = 0; i < array.length; i++) {  N  
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        }  
    }  
    return -1;  1  
}
```

```

public int find_element_in_array(int[] array, int s) {
    for(int i = 0; i < array.length; i++) { ← N
        if(array[i] == s) { ← 1
            return i; ← 1
        }
    }
    return -1; ← 1
}

```

This whole block consists of only primitive operation, so we will group everything together and call it one single primitive operation

```

public int find_element_in_array(int[] array, int s) {
    for(int i = 0; i < array.length; i++) { ← N
        if(array[i] == s) {
            return i; } }
    }
    return -1; ← 1
}

```

Total Running Time =

```

public int find_element_in_array(int[] array, int s) {
    for(int i = 0; i < array.length; i++) { ← N
        if(array[i] == s) {
            return i; } 1
        }
    }
    return -1; ← 1
}

```

Total Running Time = $N * 1 + 1$

The if statement is inside the for loop, so we must multiply it by N
(number of time the for loop runs)

```

public int find_element_in_array(int[] array, int s) {
    for(int i = 0; i < array.length; i++) { ← N
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            return i; } 1
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```

Total Running Time = $N + 1$

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            return i; } 1
        }
    }
    return -1; ← 1
}

```

Total Running Time = $N + 1$

$O(N + 1)$
 “Big-Oh”

Big-O = Running Time in
 terms of worst-case scenario

```

public int find_element_in_array(int[] array, int s) {
    for(int i = 0; i < array.length; i++) { ← N
        if(array[i] == s) {
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        }
    }
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}

```

Total Running Time = $N + 1$

$O(N + 1)$ where N = Size of Array

“Big-Oh”

Big O Formal Definition

Let $f(n)$ and $g(n)$ be functions mapping positive integers to positive real numbers
 $f(n)$ is $O(g(n))$ if there is a real constant $c > 0$ and an integer constant $n_0 \geq 1$ such that

$$f(n) \leq c \cdot g(n), \text{ for all } n \geq n_0$$

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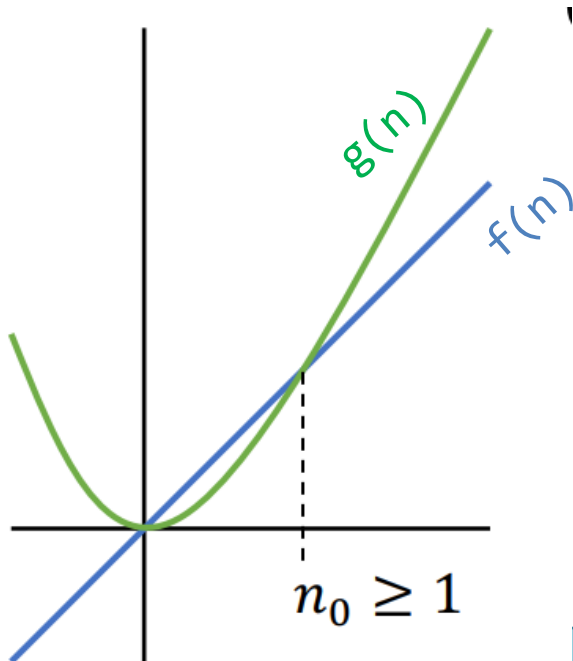
Past a certain spot, $g(n)$ dominates $f(n)$ within a multiplicative constant

Big O Formal Definition

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 $f(n)$ is $O(g(n))$ if there is a real constant $c > 0$ and an integer constant $n_0 \geq 1$ such that

$$f(n) \leq c \cdot g(n), \text{ for all } n \geq n_0$$

Past a certain spot, $g(n)$ dominates $f(n)$ within a multiplicative constant



$$\begin{aligned} \forall n \geq 1, n^2 &\geq n \\ \Rightarrow n &\in O(n^2) \end{aligned}$$

O -notation provides an upper bound on some function $f(n)$

Big-O

Notation used to describe the running time of an algorithm in terms of worse case scenario

Traits of Big-O-Notation:

In Big-O, we can drop non-dominant factors

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$$x^2 + x + 10$$

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Traits of Big-O-Notation:

In Big-O, we can drop non-dominant factors

$$x^2 + \underbrace{x + 10}$$

When X is really *really big*, these factors don't contribute very much at all

Big-O

Notation used to describe the running time of an algorithm in terms of worse case scenario

Traits of Big-O-Notation:

In Big-O, we can drop non-dominant factors

$$x^2 + \underbrace{x + 10}_{\text{non-dominant}} \in O(x^2)$$

When X is really *really big*, these factors don't contribute very much at all

x^2 is the dominating factor, so we can drop everything else

Big-O

Notation used to describe the running time of an algorithm in terms of worse case scenario

Traits of Big-O-Notation:

In Big-O, we can drop non-dominant factors

$$x^2 + x + 10 \in O(x^2)$$

When X is really *really big*, these factors don't contribute very much at all

$$\cancel{x^2 + x + 10 = O(x^2)}$$

Quick warning on notation

=

✗

∈

✓

Big-O

Notation used to describe the running time of an algorithm in terms of worse case scenario

Traits of Big-O-Notation:

In Big-O, we can drop non-dominant factors

????

```

public int find_element_in_array(int[] array, int s) {
    for(int i = 0; i < array.length; i++) { ← N
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}

```

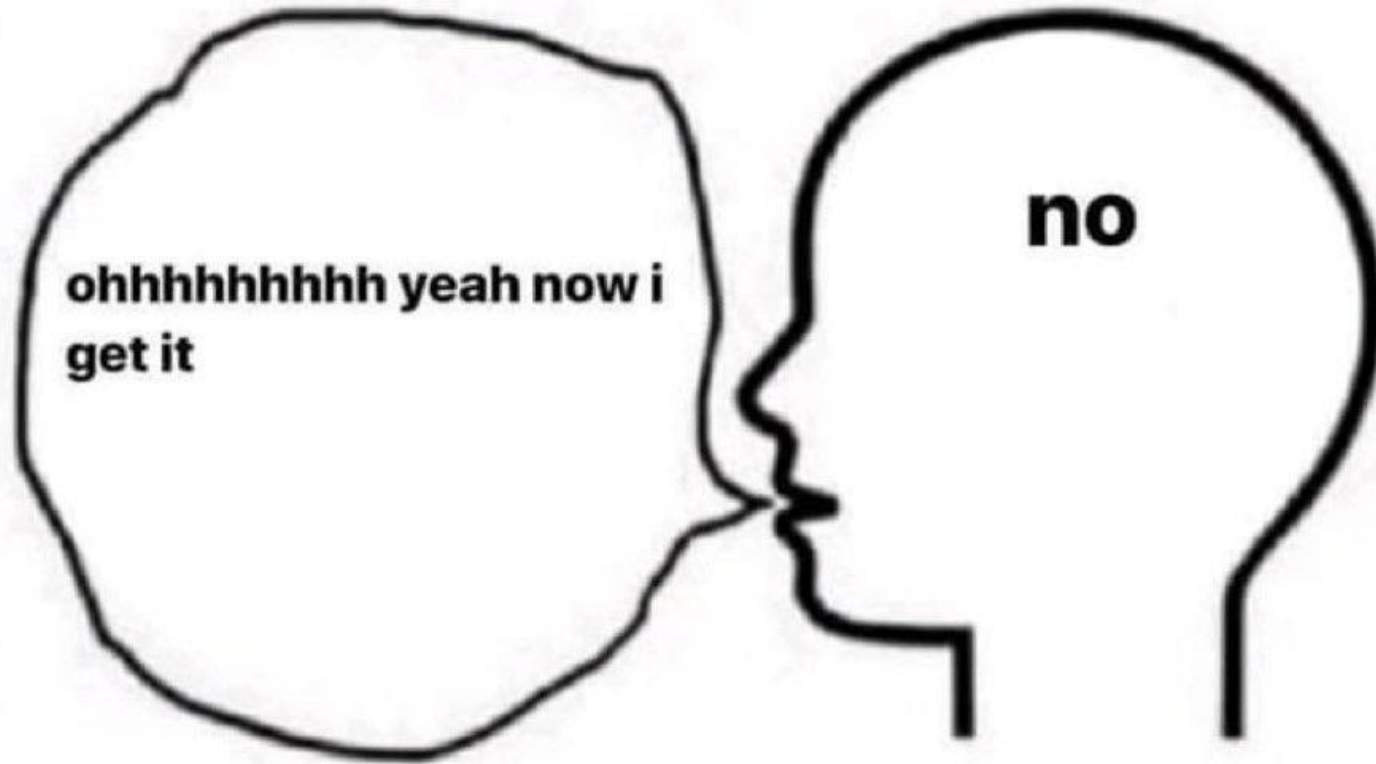
Total Running Time = $N + 1$

$O(N + 1)$ where N = Size of Array

$O(N)$ where N = Size of Array



**"do you understand it
now?"**



Algorithm Analysis: Adding value to an Array/ArrayList

```
int[] newArray = new int[myArray.length + 1];
```

Create a new array that is one spot larger

```
for(int i = 0; i < myArray.length; i++) {  
    newArray[i] = myArray[i];  
}
```

Fill new array with contents of old array

```
int new_value = 4;  
newArray[myArray.length] = new_value;  
myArray = newArray;
```

Add new value to array and update reference variable

What is the running time of this algorithm?

Algorithm Analysis: Adding value to an Array/ArrayList

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int[] newArray = new int[myArray.length + 1];
```

Create a new array that is one spot larger

```
for(int i = 0; i < myArray.length; i++) {  
    newArray[i] = myArray[i];  
}
```

Fill new array with contents of old array

```
int new_value = 4;  
newArray[myArray.length] = new_value;  
myArray = newArray;
```

Add new value to array and update reference variable

What is the running time of this algorithm?

We will find the time complexity for each operation!

Algorithm Analysis: Adding value to an Array/ArrayList

```
int[] newArray = new int[myArray.length + 1];
```



```
for(int i = 0; i < myArray.length; i++) {  
    newArray[i] = myArray[i];  
}
```

```
int new_value = 4;  
newArray[myArray.length] = new_value;  
myArray = newArray;
```

Total Running Time =

Algorithm Analysis: Adding value to an Array/ArrayList

```
int[] newArray = new int[myArray.length + 1];
```

 **O(n)**

```
for(int i = 0; i < myArray.length; i++) {  
    newArray[i] = myArray[i];  
}
```

```
int new_value = 4;  
newArray[myArray.length] = new_value;  
myArray = newArray;
```


Total Running Time = n

Algorithm Analysis: Adding value to an Array/ArrayList

```
int[] newArray = new int[myArray.length + 1];
```

 **O(n)**

```
for(int i = 0; i < myArray.length; i++) {  
    newArray[i] = myArray[i];  
}
```



```
int new_value = 4;  
newArray[myArray.length] = new_value;  
myArray = newArray;
```

Total Running Time = n

Algorithm Analysis: Adding value to an Array/ArrayList

```
int[] newArray = new int[myArray.length + 1]; ← O(n)
```

```
for(int i = 0; i < myArray.length; i++) { ← O(n)  
    newArray[i] = myArray[i]; ←  
}
```

```
int new_value = 4;  
newArray[myArray.length] = new_value;  
myArray = newArray;
```

Total Running Time = $n + n$

Algorithm Analysis: Adding value to an Array/ArrayList

```
int[] newArray = new int[myArray.length + 1]; ← O(n)
```

```
for(int i = 0; i < myArray.length; i++) { ← O(n)  
    newArray[i] = myArray[i]; ← O(1)  
}
```

```
int new_value = 4;  
newArray[myArray.length] = new_value;  
myArray = newArray;
```

Total Running Time = $n + n * 1$

Algorithm Analysis: Adding value to an Array/ArrayList

```
int[] newArray = new int[myArray.length + 1]; ← O(n)
```

```
for(int i = 0; i < myArray.length; i++) { ← O(n)  
    newArray[i] = myArray[i]; ← O(1)  
}
```

```
int new_value = 4;  
newArray[myArray.length] = new_value;  
myArray = newArray;
```

Total Running Time = $n + n * 1$

When do we add? When do multiply?

Sequential Operations = Add

Nested Operations (in a loop) = Multiply

Algorithm Analysis: Adding value to an Array/ArrayList

```
int[] newArray = new int[myArray.length + 1]; ← O(n)
```



```
for(int i = 0; i < myArray.length; i++) { ← O(n)  
    newArray[i] = myArray[i]; ← O(1)  
}
```



```
int new_value = 4; ←  
newArray[myArray.length] = new_value;  
myArray = newArray;
```

Total Running Time = $n + n * 1$

Algorithm Analysis: Adding value to an Array/ArrayList

`int[] newArray = new int[myArray.length + 1];`  **O(n)**

`for(int i = 0; i < myArray.length; i++) {`  **O(n)**
 `newArray[i] = myArray[i];`  **O(1)**
`}`

`int new_value = 4;`  **O(1)**
`newArray[myArray.length] = new_value;` 
`myArray = newArray;`

Total Running Time = $n + n * 1 + 1$

Algorithm Analysis: Adding value to an Array/ArrayList

`int[] newArray = new int[myArray.length + 1];` ← $O(n)$

`for(int i = 0; i < myArray.length; i++) {` ← $O(n)$
 `newArray[i] = myArray[i];` ← $O(1)$
`}`

`int new_value = 4;` ← $O(1)$
`newArray[myArray.length] = new_value;` ← $O(1)$
`myArray = newArray;` ← $O(1)$

Total Running Time = $n + n * 1 + 1 + 1$

Algorithm Analysis: Adding value to an Array/ArrayList

`int[] newArray = new int[myArray.length + 1];` ← $O(n)$



`for(int i = 0; i < myArray.length; i++) {` ← $O(n)$
 `newArray[i] = myArray[i];` ← $O(1)$
`}`




`int new_value = 4;` ← $O(1)$
`newArray[myArray.length] = new_value;` ← $O(1)$
`myArray = newArray;` ← $O(1)$

Total Running Time = $n + n * 1 + 1 + 1 + 1$

Algorithm Analysis: Adding value to an Array/ArrayList

`int[] newArray = new int[myArray.length + 1];`  **O(n)**



`for(int i = 0; i < myArray.length; i++) {`  **O(n)**
 `newArray[i] = myArray[i];`  **O(1)**
`}`




`int new_value = 4;`  **O(1)**
`newArray[myArray.length] = new_value;`  **O(1)**
`myArray = newArray;`  **O(1)**

$$\begin{aligned}\text{Total Running Time} &= n + n * 1 + 1 + 1 + 1 \\ &= 2n + 3\end{aligned}$$

Algorithm Analysis: Adding value to an Array/ArrayList

`int[] newArray = new int[myArray.length + 1];`  **O(n)**

`for(int i = 0; i < myArray.length; i++) {`  **O(n)**
 `newArray[i] = myArray[i];`  **O(1)**
`}`

`int new_value = 4;`  **O(1)**
`newArray[myArray.length] = new_value;`  **O(1)**
`myArray = newArray;`  **O(1)**

$$\begin{aligned}\text{Total Running Time} &= n + n * 1 + 1 + 1 + 1 \\ &= 2n + 3\end{aligned}$$

O(2n) where n is the size of the array

Big-O

Notation used to describe the running time of an algorithm in terms of worse case scenario

Traits of Big-O-Notation:

In Big-O, we can drop non-dominant factors

In Big-O, we can drop multiplicative constants

Algorithm Analysis: Adding value to an Array/ArrayList

```
int[] newArray = new int[myArray.length + 1]; ← O(n)
```

```
for(int i = 0; i < myArray.length; i++) { ← O(n)  
    newArray[i] = myArray[i]; ← O(1)  
}
```

```
int new_value = 4; ← O(1)  
newArray[myArray.length] = new_value; ← O(1)  
myArray = newArray; ← O(1)
```

When we write algorithms,
we should still be *aware of*
these coefficients

$$\begin{aligned}\text{Total Running Time} &= n + n * 1 + 1 + 1 + 1 \\ &= 2n + 3\end{aligned}$$



~~O(2n) where n is the size of the array~~ → O(n) where n is the size of the array

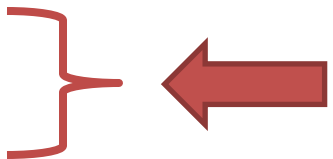
Algorithm Analysis: Adding Node to end of Singly Linked List (no `tail` pointer)

```
public void addToBack(Node newNode) {  
    if(head == null) {  
        head = newNode;  
    }  
    else {  
        Node current = head;  
        while(current.getNext() != null) {  
            current = current.getNext();  
        }  
        current.setNext(newNode);  
    }  
}
```

What is the running time of this algorithm?

Algorithm Analysis: Adding Node to end of Singly Linked List (no `tail` pointer)

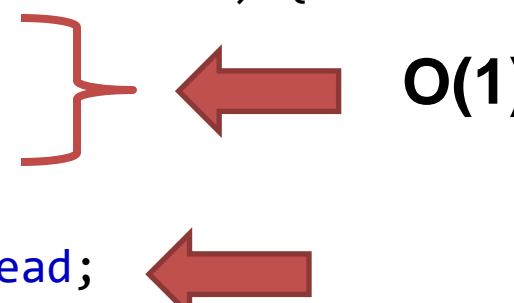
```
public void addToBack(Node newNode) {  
    if(head == null) {  
        head = newNode;  
    }  
    else {  
        Node current = head;  
        while(current.getNext() != null) {  
            current = current.getNext();  
        }  
        current.setNext(newNode);  
    }  
}
```



Total Running Time =

Algorithm Analysis: Adding Node to end of Singly Linked List (no `tail` pointer)

```
public void addToBack(Node newNode) {  
    if(head == null) {  
        head = newNode;  
    }  
    else {  
        Node current = head;  
        while(current.getNext() != null) {  
            current = current.getNext();  
        }  
        current.setNext(newNode);  
    }  
}
```



Total Running Time = 1 +

Algorithm Analysis: Adding Node to end of Singly Linked List (no `tail` pointer)

```
public void addToBack(Node newNode) {  
    if(head == null) {  
        head = newNode;  
    }  
    else {  
        Node current = head;  
        while(current.getNext() != null) {  
            current = current.getNext();  
        }  
        current.setNext(newNode);  
    }  
}
```

Diagram illustrating the algorithm analysis for adding a node to the end of a singly linked list (no `tail` pointer):

- The `if(head == null)` block is annotated with a red bracket and an arrow pointing to $O(1)$, indicating constant time complexity.
- The `while(current.getNext() != null)` loop is annotated with a red arrow pointing to $O(1)$, indicating constant time complexity.

Total Running Time = 1 + 1

Algorithm Analysis: Adding Node to end of Singly Linked List (no `tail` pointer)

```
public void addToBack(Node newNode) {  
    if(head == null) {  
        head = newNode;  
    }  
    else {  
        Node current = head;  
        while(current.getNext() != null) {  
            current = current.getNext();  
        }  
        current.setNext(newNode);  
    }  
}
```

Complexity analysis annotations:

- `if(head == null) { head = newNode; }` is annotated with $O(1)$.
- `Node current = head;` is annotated with $O(1)$.
- `while(current.getNext() != null) { current = current.getNext(); }` is annotated with $O(n)$.

Total Running Time = $1 + 1 + n$

Algorithm Analysis: Adding Node to end of Singly Linked List (no `tail` pointer)

```
public void addToBack(Node newNode) {  
    if(head == null) {  
        head = newNode;  
    }  
    else {  
        Node current = head;  
        while(current.getNext() != null) {  
            current = current.getNext();  
        }  
        current.setNext(newNode);  
    }  
}
```

Complexity analysis annotations:

- `if(head == null)`: $O(1)$
- `head = newNode`: $O(1)$
- `Node current = head`: $O(1)$
- `while(current.getNext() != null)`: $O(n)$
- `current = current.getNext()`: $O(1)$
- `current.setNext(newNode)`: $O(1)$

Total Running Time = $1 + 1 + n * 1$

Algorithm Analysis: Adding Node to end of Singly Linked List (no `tail` pointer)

```
public void addToBack(Node newNode) {  
    if(head == null) {  
        head = newNode;  
    }  
    else {  
        Node current = head;  
        while(current.getNext() != null) {  
            current = current.getNext();  
        }  
        current.setNext(newNode);  
    }  
}
```

Complexity analysis annotations:

- `if(head == null) {` and `head = newNode;` are grouped with a red bracket and an arrow pointing to **O(1)**.
- `Node current = head;` has an arrow pointing to **O(1)**.
- `while(current.getNext() != null) {` has an arrow pointing to **O(n)**.
- `current = current.getNext();` has an arrow pointing to **O(1)**.
- `current.setNext(newNode);` has an arrow pointing to **O(1)**.

Total Running Time = $1 + 1 + n * 1 + 1$

Algorithm Analysis: Adding Node to end of Singly Linked List (no `tail` pointer)

```
public void addToBack(Node newNode) {  
    if(head == null) {  
        head = newNode;  
    }  
    else {  
        Node current = head;  
        while(current.getNext() != null) {  
            current = current.getNext();  
        }  
        current.setNext(newNode);  
    }  
}
```

Complexity analysis annotations:

- `if(head == null) {` and `head = newNode;` are grouped with a red bracket and an arrow pointing to **O(1)**.
- `Node current = head;` has an arrow pointing to **O(1)**.
- `while(current.getNext() != null) {` has an arrow pointing to **O(n)**.
- `current = current.getNext();` has an arrow pointing to **O(1)**.
- `current.setNext(newNode);` has an arrow pointing to **O(1)**.

$$\begin{aligned}\text{Total Running Time} &= 1 + 1 + n * 1 + 1 \\ &= n + 3\end{aligned}$$

Algorithm Analysis: Adding Node to end of Singly Linked List (no `tail` pointer)

```
public void addToBack(Node newNode) {  
    if(head == null) {  
        head = newNode;  
    }  
    else {  
        Node current = head;  
        while(current.getNext() != null) {  
            current = current.getNext();  
        }  
        current.setNext(newNode);  
    }  
}
```

Complexity analysis annotations:

- `if(head == null) {` and `head = newNode;` are grouped with a red bracket and an arrow pointing to $O(1)$.
- `Node current = head;` has an arrow pointing to $O(1)$.
- `while(current.getNext() != null) {` has an arrow pointing to $O(n)$.
- `current = current.getNext();` has an arrow pointing to $O(1)$.
- `current.setNext(newNode);` has an arrow pointing to $O(1)$.

$$\begin{aligned}\text{Total Running Time} &= 1 + 1 + n * 1 + 1 \\ &= n + 3\end{aligned}$$

∈ $O(n)$ where n is ????

Algorithm Analysis: Adding Node to end of Singly Linked List (no `tail` pointer)

```
public void addToBack(Node newNode) {  
    if(head == null) {  
        head = newNode;  
    }  
    else {  
        Node current = head;  
        while(current.getNext() != null) {  
            current = current.getNext();  
        }  
        current.setNext(newNode);  
    }  
}
```

Complexity analysis for the code above:

- `if(head == null) { head = newNode; }` is $O(1)$.
- `Node current = head;` is $O(1)$.
- `while(current.getNext() != null) { ... }` is $O(n)$.
- `current = current.getNext();` inside the while loop is $O(1)$.
- `current.setNext(newNode);` is $O(1)$.

$$\begin{aligned}\text{Total Running Time} &= 1 + 1 + n * 1 + 1 \\ &= n + 3\end{aligned}$$

∈ $O(n)$ where n is the number of nodes in the LL

Algorithm Analysis: Adding Node to end of Singly Linked List (no `tail` pointer)

```
public void addToBack(Node newNode) {  
    if(head == null) {  
        head = newNode;  
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        while(current.getNext() != null) {  
            current = current.getNext();  
        }  
        current.setNext(newNode);  
    }  
}
```

Complexity annotations for the code above:

- `if(head == null) { head = newNode; }` is $O(1)$.
- `Node current = head;` is $O(1)$.
- `while(current.getNext() != null) { ... }` loop is $O(n)$.
- `current = current.getNext();` inside the loop is $O(1)$.
- `current.setNext(newNode);` is $O(1)$.

$$\begin{aligned}\text{Total Running Time} &= 1 + 1 + n * 1 + 1 \\ &= n + 3\end{aligned}$$

∈ $O(n)$ where n is the number of nodes in the LL

“Worst case scenario, we have to go through all the nodes in the LL to add something at the end”

Algorithm Analysis: Adding Node to end of Singly Linked List (`tail` pointer)

```
public void addToBack(Node newNode) {  
  
    if(head == null && tail == null) {  
        head = newNode;  
        tail = newNode;  
    }  
    else {  
        tail.setNext(newNode);  
        tail = newNode;  
    }  
}
```

What is the running time of this algorithm?

Algorithm Analysis: Adding Node to end of Singly Linked List (*tail* pointer)

```
public void addToBack(Node newNode) {  
  
    if(head == null && tail == null) {  
        head = newNode;  
        tail = newNode;  
    }  
    else {  
        tail.setNext(newNode);  
        tail = newNode;  
    }  
}
```

← **O(1)**

Total Running Time =

Algorithm Analysis: Adding Node to end of Singly Linked List (*tail* pointer)

```
public void addToBack(Node newNode) {
```

```
    if(head == null && tail == null) {
```

```
        head = newNode;
```

```
        tail = newNode;
```

← O(1)

```
    }
```

```
    else {
```

```
        tail.setNext(newNode);
```

```
        tail = newNode;
```




← O(1)

```
    }
```

```
}
```

Total Running Time =

Algorithm Analysis: Adding Node to end of Singly Linked List (`tail` pointer)

```
public void addToBack(Node newNode) {  
    if(head == null && tail == null) {  
        head = newNode;  O(1)  
        tail = newNode;  
    }  
    else {  
        tail.setNext(newNode);  O(1)  
        tail = newNode;  O(1)  
    }  
}
```

Total Running Time = 1 + 1 + 1

Algorithm Analysis: Adding Node to end of Singly Linked List (`tail` pointer)




```
public void addToBack(Node newNode) {  
    if(head == null && tail == null) {  
        head = newNode;           ← O(1)  
        tail = newNode;  
    }  
    else {  
        tail.setNext(newNode);    ← O(1)  
        tail = newNode;          ← O(1)  
    }  
}
```

Total Running Time = 1 + 1 + 1

∈ **O(1)**

“The number of operations required for this algorithm is the same no matter the input”

Algorithm Analysis: Adding Node to end of Singly Linked List (`tail` pointer)

```
public void addToBack(Node newNode) {  
    if(head == null && tail == null) {  
        head = newNode;  O(1)  
        tail = newNode;  
    }  
    else {  
        tail.setNext(newNode);  O(1)  
        tail = newNode;  O(1)  
    }  
}
```

Total Running Time = 1 + 1 + 1

∈ O(1)

“The number of operations required for this algorithm is the same no matter the input”

3,000,000 Nodes = 3 operations, 10 Nodes = 3 operations

Algorithm Analysis: Finding pairs that add up to a target sum

```
public static List<int[]> findPairs(int[] arr, int target) {  
    List<int[]> pairs = new LinkedList<>();  
    for (int i = 0; i < arr.length; i++) {  
        for (int j = i + 1; j < arr.length; j++) {  
            if (arr[i] + arr[j] == target) {  
                pairs.add(new int[]{arr[i], arr[j]});  
            }  
        }  
    }  
    return pairs;  
}
```

Algorithm Analysis: Finding pairs that add up to a target sum

```
public static List<int[]> findPairs(int[] arr, int target) {  
    List<int[]> pairs = new LinkedList<>();  
    for (int i = 0; i < arr.length; i++) {  
        for (int j = i + 1; j < arr.length; j++) {  
            if (arr[i] + arr[j] == target) {  
                pairs.add(new int[]{arr[i], arr[j]});  
            }  
        }  
    }  
    return pairs;  
}
```

```
int[] arr = {1, 2, 3, 4, 5, 6, 7};  
int target = 8;
```

```
pairs = { [1,7], [2,6], [3,5], [4,4], [5,3], [6,2], [7,1] }
```

Algorithm Analysis: Finding pairs that add up to a target sum


```
public static List<int[]> findPairs(int[] arr, int target) {  
    List<int[]> pairs = new LinkedList<>();  
    for (int i = 0; i < arr.length; i++) {  
        for (int j = i + 1; j < arr.length; j++) {  
            if (arr[i] + arr[j] == target) {  
                pairs.add(new int[]{arr[i], arr[j]});  
            }  
        }  
    }  
    return pairs;  
}
```

Running time?

```
int[] arr = {1, 2, 3, 4, 5, 6, 7};  
int target = 8;
```

```
pairs = { [1,7], [2,6], [3,5], [4,4], [5,3], [6,2], [7,1] }
```


Algorithm Analysis: Finding pairs that add up to a target sum

```
public static List<int[]> findPairs(int[] arr, int target) {  
    List<int[]> pairs = new LinkedList<>();  O(1)  
    for (int i = 0; i < arr.length; i++) {  
        for (int j = i + 1; j < arr.length; j++) {  
            if (arr[i] + arr[j] == target) {  
                pairs.add(new int[]{arr[i], arr[j]});  
            }  
        }  
    }  
    return pairs;  
}
```

```
int[] arr = {1, 2, 3, 4, 5, 6, 7};  
int target = 8;
```

Running time?

```
pairs = { [1,7], [2,6], [3,5], [4,4], [5,3], [6,2], [7,1] }
```

```
public static List<int[]> findPairs(int[] arr, int target) {  
    List<int[]> pairs = new LinkedList<>(); ← O(1)  
    for (int i = 0; i < arr.length; i++) { ← O(n)  
        for (int j = i + 1; j < arr.length; j++) {  
            if (arr[i] + arr[j] == target) {  
                pairs.add(new int[]{arr[i], arr[j]});  
            }  
        }  
    }  
    return pairs;  
}
```

Running time?

```
int[] arr = {1, 2, 3, 4, 5, 6, 7};  
int target = 8;
```

```
pairs = { [1,7], [2,6], [3,5], [4,4], [5,3], [6,2], [7,1] }
```

```
public static List<int[]> findPairs(int[] arr, int target) {  
    List<int[]> pairs = new LinkedList<>(); ← O(1)  
    for (int i = 0; i < arr.length; i++) { ← O(n)  
        for (int j = i + 1; j < arr.length; j++) { ← O(n)  
            if (arr[i] + arr[j] == target) {  
                pairs.add(new int[]{arr[i], arr[j]});  
            }  
        }  
    }  
    return pairs;  
}
```

Running time?

```
int[] arr = {1, 2, 3, 4, 5, 6, 7};  
int target = 8;
```

```
pairs = { [1,7], [2,6], [3,5], [4,4], [5,3], [6,2], [7,1] }
```

```
public static List<int[]> findPairs(int[] arr, int target) {  
    List<int[]> pairs = new LinkedList<>(); ← O(1)  
    for (int i = 0; i < arr.length; i++) { ← O(n)  
        for (int j = i + 1; j < arr.length; j++) { ← O(n)  
            if (arr[i] + arr[j] == target) { ← O(1)  
                pairs.add(new int[]{arr[i], arr[j]});  
            }  
        }  
    }  
    return pairs;  
}
```

Running time?

```
int[] arr = {1, 2, 3, 4, 5, 6, 7};  
int target = 8;
```

```
pairs = { [1,7], [2,6], [3,5], [4,4], [5,3], [6,2], [7,1] }
```

```

public static List<int[]> findPairs(int[] arr, int target) {
    List<int[]> pairs = new LinkedList<>(); ← O(1)
    for (int i = 0; i < arr.length; i++) { ← O(n)
        for (int j = i + 1; j < arr.length; j++) { ← O(n)
            if (arr[i] + arr[j] == target) { ← O(1)
                pairs.add(new int[]{arr[i], arr[j]});
                                O(1)          O(1)
            }
        }
    }
    return pairs;
}
    
```

Running time?

```

int[] arr = {1, 2, 3, 4, 5, 6, 7};
int target = 8;
    
```

```

pairs = { [1,7], [2,6], [3,5], [4,4], [5,3], [6,2], [7,1] }
    
```

Algorithm Analysis: Finding pairs that add up to a target sum

$n = \text{length of array}$

```
public static List<int[]> findPairs(int[] arr, int target) {  
    List<int[]> pairs = new LinkedList<>(); ← O(1)  
    for (int i = 0; i < arr.length; i++) { ← O(n)  
        for (int j = i + 1; j < arr.length; j++) { ← O(n)  
            if (arr[i] + arr[j] == target) { ← O(1)  
                pairs.add(new int[]{arr[i], arr[j]}); ← O(1)  
            }  
        }  
    }  
    return pairs; ← O(1)  
}
```

Running time?

```
int[] arr = {1, 2, 3, 4, 5, 6, 7};  
int target = 8;
```

```
pairs = { [1,7], [2,6], [3,5], [4,4], [5,3], [6,2], [7,1] }
```

Algorithm Analysis: Finding pairs that add up to a target sum

$n = \text{length of array}$

```
public static List<int[]> findPairs(int[] arr, int target) {
    List<int[]> pairs = new LinkedList<>(); ← O(1)
    for (int i = 0; i < arr.length; i++) { ← O(n)
        for (int j = i + 1; j < arr.length; j++) { ← O(n)
            if (arr[i] + arr[j] == target) { ← O(1)
                pairs.add(new int[]{arr[i], arr[j]}); ← O(1)
            }
        }
    }
    return pairs; ← O(1)
}
```

```
int[] arr = {1, 2, 3, 4, 5, 6, 7};
int target = 8;
```

```
pairs = { [1,7], [2,6], [3,5], [4,4], [5,3], [6,2], [7,1] }
```

Running time?

$O(n^2)$ where $n = \text{length of array}$

```
public int find_element_in_array(int[] array, int s) {  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
        System.out.println(array[i]);  
        System.out.println(array[i]);  
        System.out.println(array[i]);  
        System.out.println(array[i]);  
    }  
    return -1;  
}
```



```
public int find_element_in_array(int[] array, int s) {  
    for(int i = 0; i < array.length; i++) { ← O(n)  
        System.out.println(array[i]); ← O(1)  
        System.out.println(array[i]); ← O(1)  
        System.out.println(array[i]); ← O(1)  
        System.out.println(array[i]); ← O(1)  
        System.out.println(array[i]); ← O(1)  
    }  
    return -1; ← O(1)  
}
```

```
public int find_element_in_array(int[] array, int s) {  
    for(int i = 0; i < array.length; i++) { ← O(n)  
        System.out.println(array[i]); ← O(1)  
        System.out.println(array[i]); ← O(1)  
        System.out.println(array[i]); ← O(1)  
        System.out.println(array[i]); ← O(1)  
        System.out.println(array[i]); ← O(1)  
    }  
    return -1; ← O(1)  
}
```

Total Running Time: $n * 5$

$O(5n)$

$n = | \text{length of array} |$

```

public int find_element_in_array(int[] array, int s) {
    for(int i = 0; i < array.length; i++) { ← O(n)
        System.out.println(array[i]); ← O(1)
        System.out.println(array[i]); ← O(1)
        System.out.println(array[i]); ← O(1)
        System.out.println(array[i]); ← O(1)
        System.out.println(array[i]); ← O(1)
    }
    return -1; ← O(1)
}

```

Total Running Time: $n * 5$

$O(5n)$

$n = | \text{length of array} |$

To find an element in an array, we traverse the length of the array **five times** ?

```

public int find_element_in_array(int[] array, int s) {
    for(int i = 0; i < array.length; i++) { ← O(n)
        System.out.println(array[i]); ← O(1)
        System.out.println(array[i]); ← O(1)
        System.out.println(array[i]); ← O(1)
        System.out.println(array[i]); ← O(1)
        System.out.println(array[i]); ← O(1)
    }
    return -1; ← O(1)
}

```

Total Running Time: ~~$n * 5$~~

~~$O(5n)$~~

$n = | \text{length of array} |$

To find an element in an array, we traverse the length of the array **five times** ?

no

```

public int find_element_in_array(int[] array, int s) {
    for(int i = 0; i < array.length; i++) { ← O(n)
        System.out.println(array[i]);
        System.out.println(array[i]);
        System.out.println(array[i]);
        System.out.println(array[i]);
        System.out.println(array[i]);
    }
    return -1; ← O(1)
}

```

Total Running Time: n

O(n)

n = | length of array |


To find an element in an array, we traverse the length of the array **once**

When calculating the **asymptotic running time/big O notation/time complexity/running time** the thing we need to pay attention to is the amount of looping

```
public int print_array(int[] array) {  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
}
```

```
public int print_array(int[] array) {  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
    ...  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
}
```

```
public int print_array(int[] array) {  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
}
```



 $O(n)$

$O(n + n + n + \dots + n + n + n)$



```
public int print_array(int[] array) {  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
    ...  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
}
```

```
public int print_array(int[] array) {  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
}
```


 $O(n)$

$O(500n)$



```
public int print_array(int[] array) {  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
    ...  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
}
```



```
public int print_array(int[] array) {  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
}
```


$O(n)$

$O(n)$



```
public int print_array(int[] array) {  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
    ...  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
}
```

```
public int print_array(int[] array) {  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
}
```


 $O(n)$

Even though one algorithm does much more work than another, they still have the same asymptotic running time

$O(n)$



```
public int print_array(int[] array) {  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
    ...  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
    for(int i = 0; i < array.length; i++) {  
        System.out.println(array[i]);  
    }  
}
```

```
public int print_array(int[] array) {  
    for(int i = 0; i < array.length; i++)  
    {  
        System.out.println(array[i]);  
    }  
}
```



$O(n)$

```
public int print_array(int[] array) {  
    for(int i = 0; i < array.length; i++)  
    {  
        System.out.println(array[i]);  
    }  
}
```



$O(n)$

```
public int print_array(int[] array) {  
    for(int i = 0; i < array.length; i++)  
    {  
        System.out.println(array[i]);  
    }  
}
```



???

```
public int print_array(int[] array) {  
    for(int i = 0; i < array.length; i++)  
    {  
        System.out.println(array[i]);  
    }  
}
```



$O(n)$

```
public int print_array(int[] array) {  
    for(int i = 0; i < array.length; i++)  
    {  
        System.out.println(array[i]);  
    }  
}
```



$O(n)$

```
public int print_array(int[] array) {
    for(int i = 0; i < array.length; i++)
    {
        System.out.println(array[i]);
    }
}
```



$O(n)$

```
public int print_array(int[] array) {
    for(int i = 0; i < array.length; i++)
    {
        System.out.println(array[i]);
    }
}
```



$O(n)$

```
public int print_array(int[] array) {
    for(int i = 0; i < array.length; i++)
    {
        System.out.println(array[i]);
    }
}
```



???

```
public int print_array(int[] array) {
    for(int i = 0; i < array.length; i++)
    {
        System.out.println(array[i]);
    }
}
```



???

```
public int print_array(int[] array) {
    for(int i = 0; i < array.length; i++)
    {
        System.out.println(array[i]);
    }
}
```



$O(n)$

```
public int print_array(int[] array) {
    for(int i = 0; i < array.length; i++)
    {
        System.out.println(array[i]);
    }
}
```



$O(n)$

The same algorithm will have the same asymptotic running time no matter what the computer's hardware is

```
public int print_array(int[] array) {
    for(int i = 0; i < array.length; i++)
    {
        System.out.println(array[i]);
    }
}
```



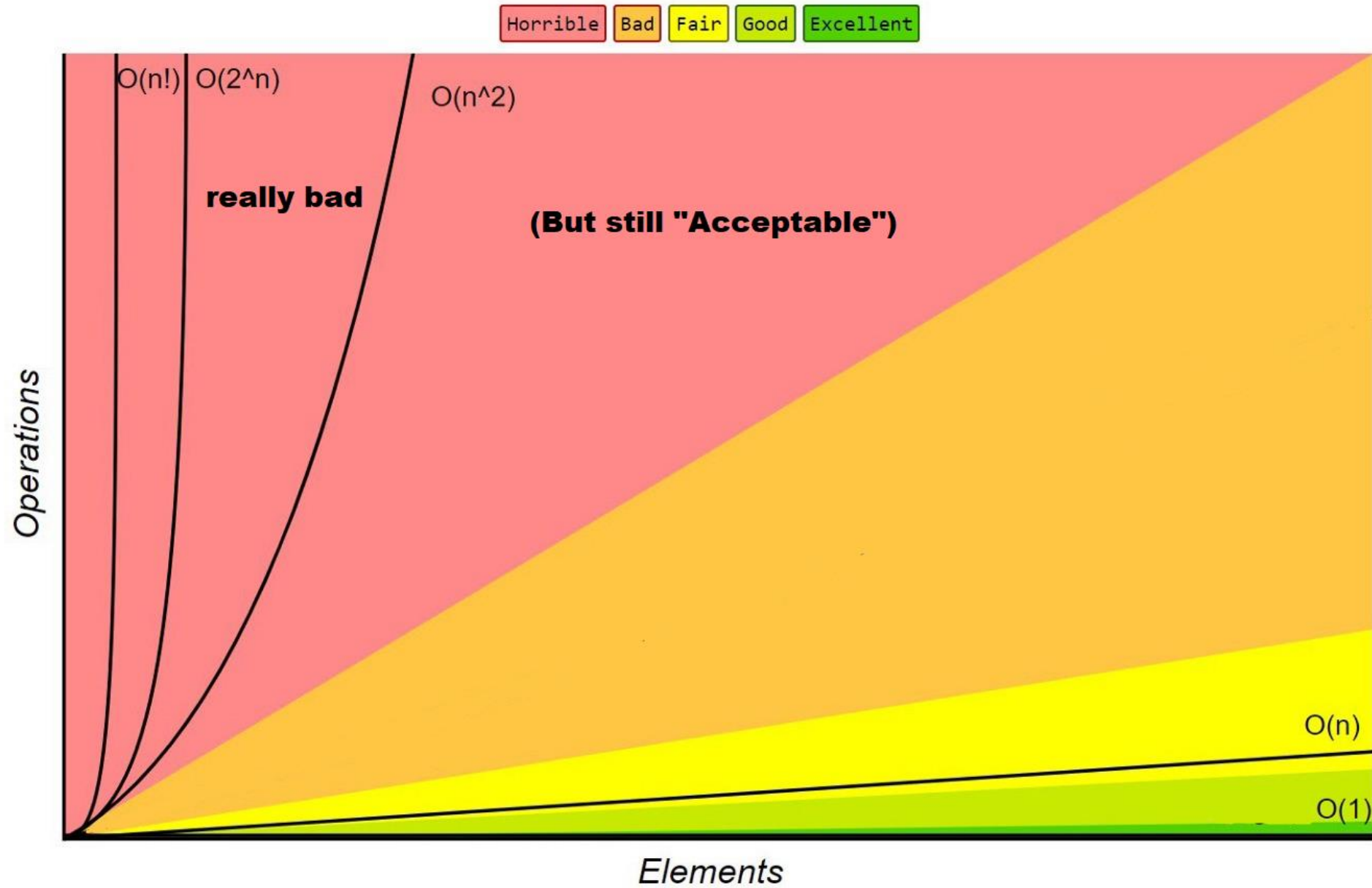
$O(n)$

```
public int print_array(int[] array) {
    for(int i = 0; i < array.length; i++)
    {
        System.out.println(array[i]);
    }
}
```



$O(n)$

Big-O Complexity Chart



Big-O Complexity Chart

“Polynomial Time”

