



~~■~~ Data $\xrightarrow{\text{space}} \xrightarrow{\text{time}}$

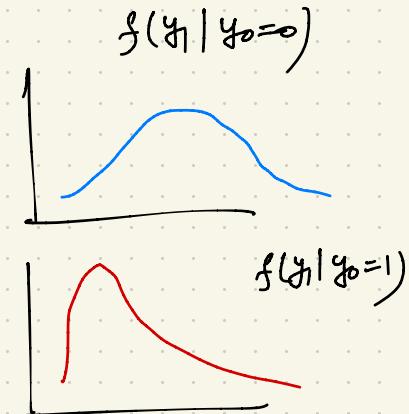
$$\underline{X} = [y_0 \ y_1(s-1, t) \ y_1(s, t-1)] \sim y(s, t)$$

GCM
 obs

~~■~~ Fit $\xrightarrow{Y_1 \sim \underline{X}}$

④ Let's say $s=1$,
i.e. $y_1(s-1, t)$ is not available

Further, let's drop the time variable too,
then $X = y_0$



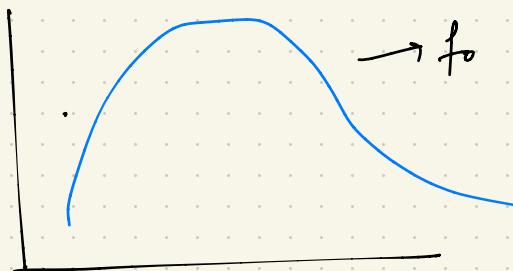
Predict:

From the fitted model we have

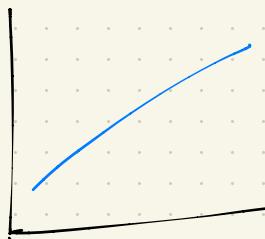
$$f_0 = f(y_1 | y_0=0), \quad f_1 = f(y_1 | y_0=1)$$

$$F_0 = F(y_1 | y_0=0), \quad F_1 = F(y_1 | y_0=1)$$

also F_0^{-1} and F_1^{-1}

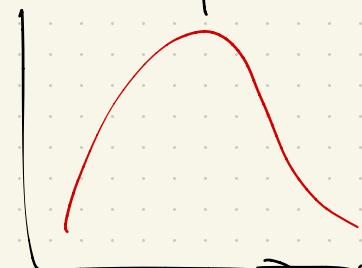


$$\downarrow F_0 \text{ (pointwise)}$$



$$\xrightarrow{F_1^{-1} \text{ (pointwise)}}$$

calibrated
density of \hat{y}_1



$$\hat{y}_1 \sim Y_1, \quad y_0 = 1$$

$$\hat{y}_1 \sim F_1^{-1} F_0(Y_1), \quad y_0=0 \rightarrow \text{calibration}$$

■ For $\delta = 2$

→ Fit is identical.

→ For predictions, replace

$y_1(t, t)$ by $\hat{y}_1(t, t)$ from the previous model

→ calibrate

■ If $y_1(s, t^{-1})$ is a covariate

→ Fit is identical

→ Predict in sequence:

$$\hat{y}_1(t=1) = F_1^{-1} F_0(y_1(t=1))$$

$$\hat{y}_1(t=2) = F_1^{-1} F_0(\hat{y}_1(t=1))$$

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