

The Stacking Scheme

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Say we obtain the following results, using three different estimators:

Estimator	Estimated RMSE	Prediction
Method 1	ϵ_1	\vec{y}_1
Method 2	ϵ_2	\vec{y}_2
Method 3	ϵ_3	\vec{y}_3

Since a better performance is indicated by a lower estimated rmse ϵ_i , we form the following stacking scheme, which gives more weights to better forming estimators:

$$\begin{aligned}\vec{y}_{\text{Stacked}} &= \frac{1}{2s} [(s - \epsilon_1) \vec{y}_1 + (s - \epsilon_2) \vec{y}_2 + (s - \epsilon_3) \vec{y}_3], \\ s &= \epsilon_1 + \epsilon_2 + \epsilon_3\end{aligned}\tag{1}$$

Check: suppose under the most rare but ideal situation ¹ that

$$\vec{y}_1 = \vec{y}_2 = \vec{y}_3 = \vec{y}_{\text{Test}}$$

then by (1)

$$\begin{aligned}\vec{y}_{\text{Stacked}} &= \frac{1}{2s} (s - \epsilon_1 + s - \epsilon_2 + s - \epsilon_3) \vec{y}_{\text{Test}} \\ &= \frac{1}{2s} (3s - s) \vec{y}_{\text{Test}} \\ &= \vec{y}_{\text{Test}}\end{aligned}$$

which is the desired result.

¹It is possible although improbable.