$$\hat{S}^{+} = \left(\sqrt{2S - \hat{a}^{\dagger}\hat{a}}\right)\hat{a}, 
\hat{S}^{-} = \hat{a}\sqrt{2S - \hat{a}^{\dagger}\hat{a}}, 
\hat{S}^{z} = S - \hat{a}^{\dagger}\hat{a},$$