

1. (25 points) List all of the super-keys of the relation  $R(A, B, C, D, E)$  with keys  $ABD$  and  $ACE$ . (That is, the relation has two keys: the aggregate key  $ABD$ , and the aggregate key  $ACE$ .)

2. (25 points) What is the closure of  $\{A, B\}$  with respect to  $R(A, B, C, D, E, F, G)$  if  $R$  has the following functional dependencies?

(a)  $G \rightarrow CDE \quad A \rightarrow F \quad BF \rightarrow ABC \quad FC \rightarrow G$

(b)  $D \rightarrow A \quad C \rightarrow D \quad A \rightarrow B \quad AB \rightarrow C$

3. (25 points) For each of the following questions, if the schema  $R(A, B, C, D, E)$  is in BCNF or 3NF with respect to the given the functional dependencies, draw a circle around BCNF or 3NF (or both) as appropriate. Show your work!

(a) BCNF      3NF       $AB \rightarrow C \quad A \rightarrow B \quad A \rightarrow DE \quad C \rightarrow D$

(b) BCNF      3NF       $E \rightarrow BCD \quad D \rightarrow AE \quad B \rightarrow CD$

4. (25 points) Use the algorithm given in class to compute the 3NF for  $R(A, B, C, D, E)$  with the following FDs.

(a)  $A \rightarrow BC \quad B \rightarrow C \quad E \rightarrow D$

(b)  $A \rightarrow BC \quad E \rightarrow BCD \quad B \rightarrow CD$