

	A	B	C
$R \equiv$	7	3	5
	4	1	2
	2	9	8

	D	B	E
$S \equiv$	2	1	5
	9	3	6
	8	7	8

	X	Y
$T \equiv$	a	b
	d	e
	g	h

1. (30 points) What is $\pi_{A,B}(R \bowtie S) \times T$?

Solution:

	A	B	C	D	E
$R \bowtie S =$	4	1	2	2	5
	7	3	5	9	6

	A	B
$\pi_{A,B}(R \bowtie S) =$	4	1
	7	3

	A	B	X	Y
$\pi_{A,B}(R \bowtie S) \times T =$	4	1	a	b
	7	3	a	b
	4	1	d	e
	7	3	d	e
	4	1	g	h
	7	3	g	h

2. (30 points) What is $\sigma_{A < 7}(R) \cup \rho_{D=A, E=C} \sigma_{D > 5}(S)$?

Solution:

	A	B	C
$\sigma_{A < 7}(R) =$	4	1	2
	2	9	8

	D	B	E
$\sigma_{D > 5}(S) =$	9	3	6
	8	7	8

	A	B	C
$\sigma_{A < 7}(R) \cup \rho_{D=A, E=C} \sigma_{D > 5}(S) =$	4	1	2
	2	9	8
	9	3	6
	8	7	8

3. (40 points) Write an expression using the relations R, S, T that has the following value.

Z	Q	W
a	b	7
a	b	1
a	b	3

Solution: A solution is $\rho_{X=Z, Y=Q, B=W} \sigma_{X=a}(T) \times \pi_B(S)$