

ELEC 4700  
Assignment 4  
Circuit Modeling

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## Part 1: Circuit MNA Modeling

Component stamps were created as separate functions in MatLab to add values to the respective cells in the G, C and b matrices respective of where the components are located in the circuit. Solving for the voltage matrix where  $V = (G + sC) \backslash b$  gives the G, C and b matrices given in Figure 2, and the gain of the circuit in the DC response is given in Figure 1.

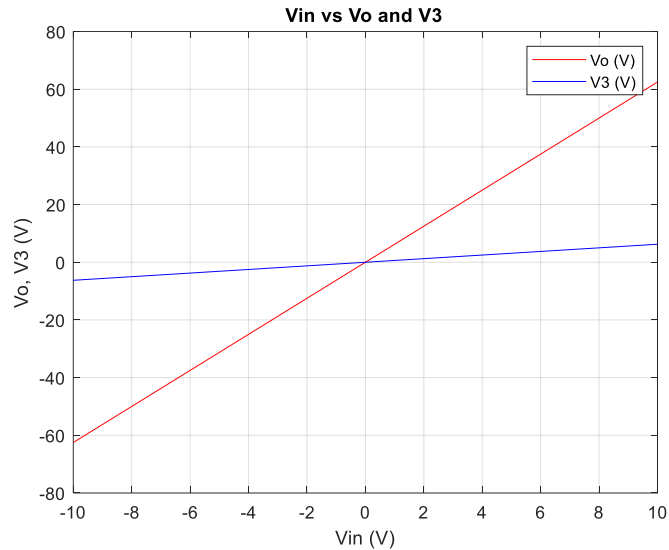


Figure 1: DC Gain

G =

1.0000	-1.0000	0	0	0	0	0	1.0000
-1.0000	1.5000	0	0	0	1.0000	0	0
0	0	0.1000	0	0	-1.0000	0	0
0	0	0	10.0000	-10.0000	0	1.0000	0
0	0	0	-10.0000	10.0010	0	0	0
0	1.0000	-1.0000	0	0	0	0	0
0	0	-10.0000	1.0000	0	0	0	0
1.0000	0	0	0	0	0	0	0

C =

0.2500	-0.2500	0	0	0	0	0	0
-0.2500	0.2500	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	-0.2000	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0

b =

```

0
0
0
0
0
0
0
0
0
10

```

Figure 2: G, C, b matrices

Next the AC frequency response can be modelled, as shown in figure 3.

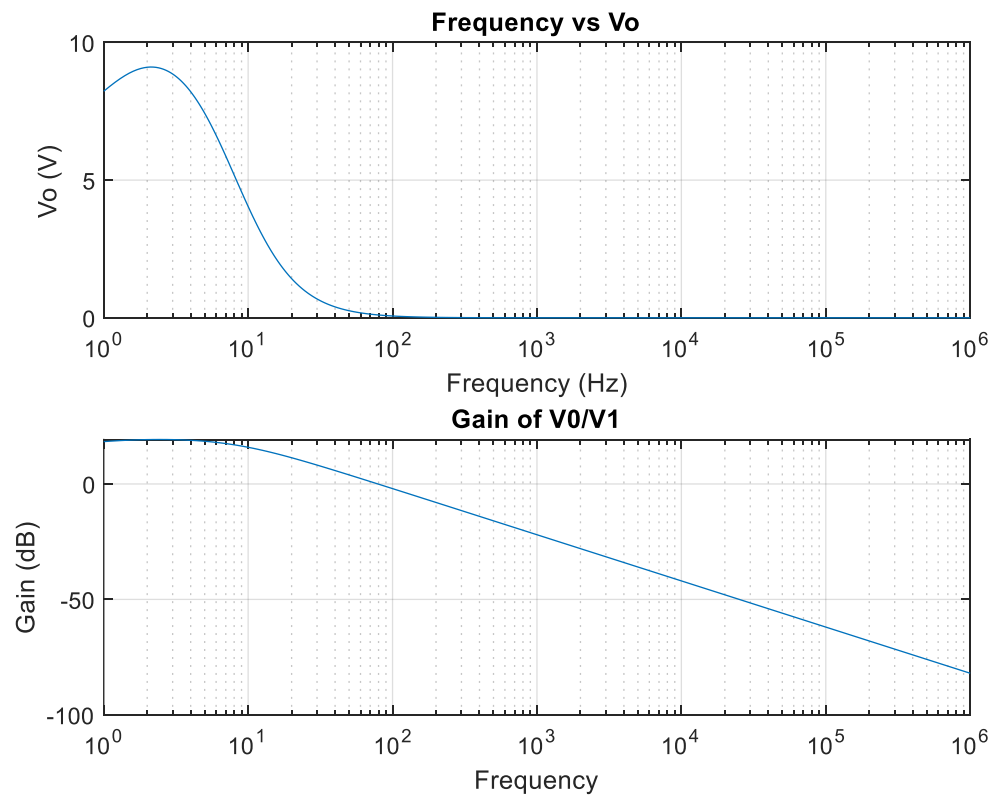


Figure 3: Frequency Response

Finally, random perturbations in the C matrix can be modelled, as shown in Figure 4.

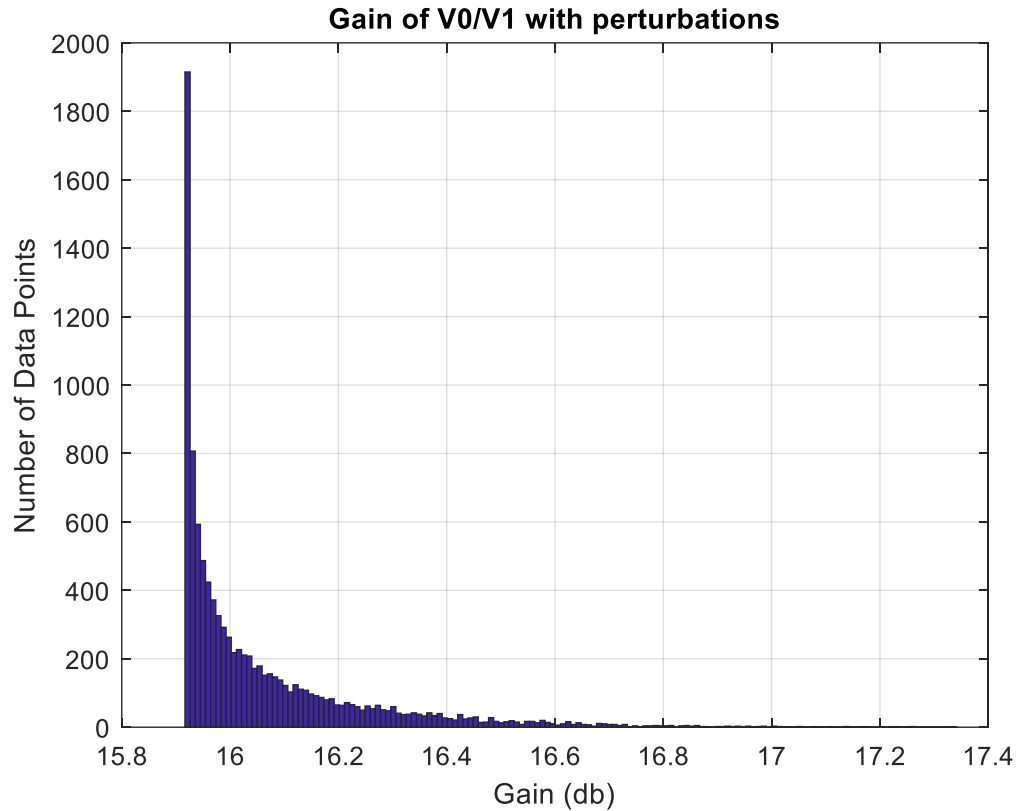


Figure 4: Perturbations in C

## Part 2: Transient Circuit Simulation

The circuit acts as a low pass filter with an amplifier. The low frequency responses will be amplified, while the high frequencies have no output.

A step response is shown in Figure 5, sinusoidal response in Figure 6 and Gaussian pulse in Figure 7.

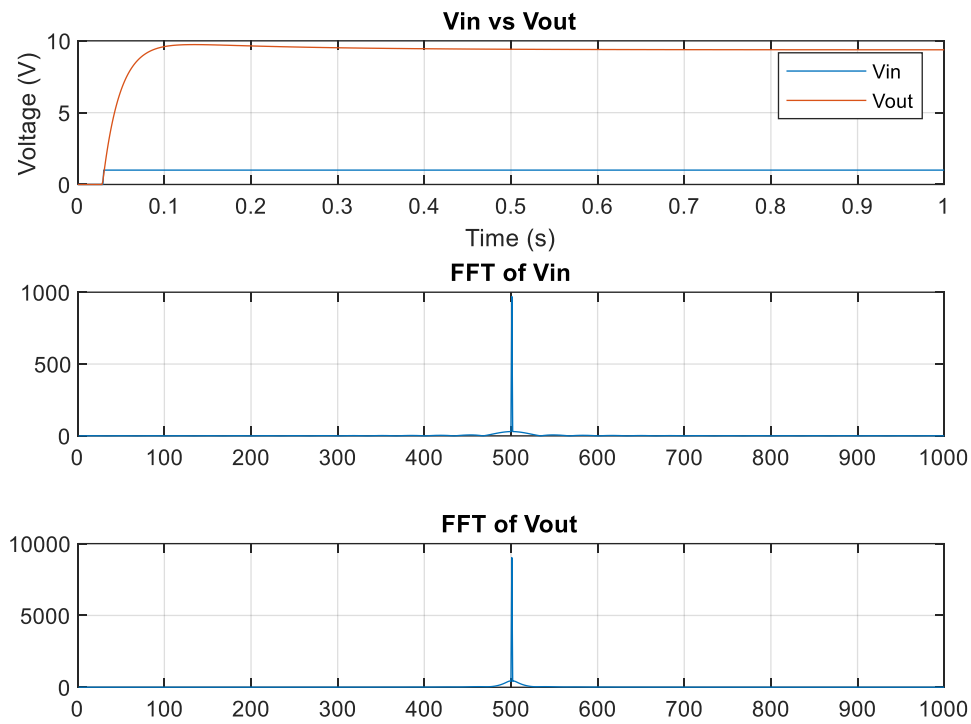


Figure 5: Step Response

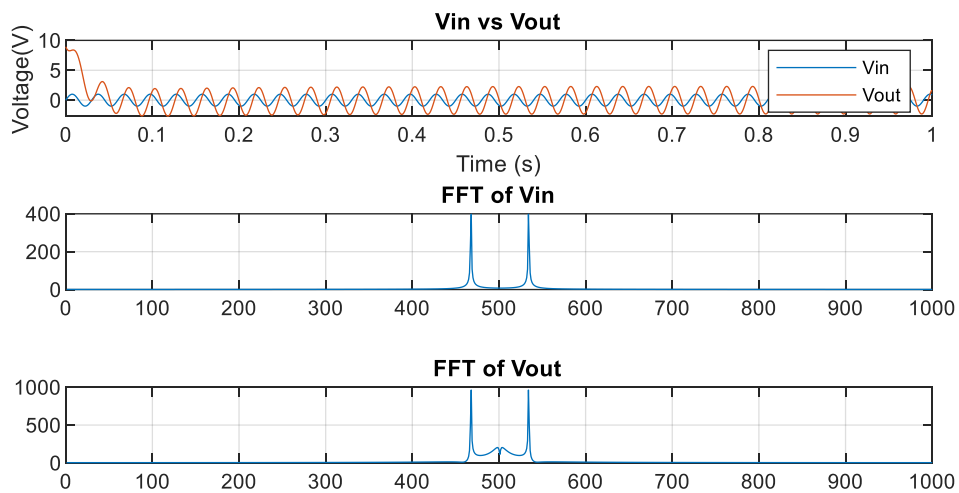


Figure 6: Sinusoidal Response

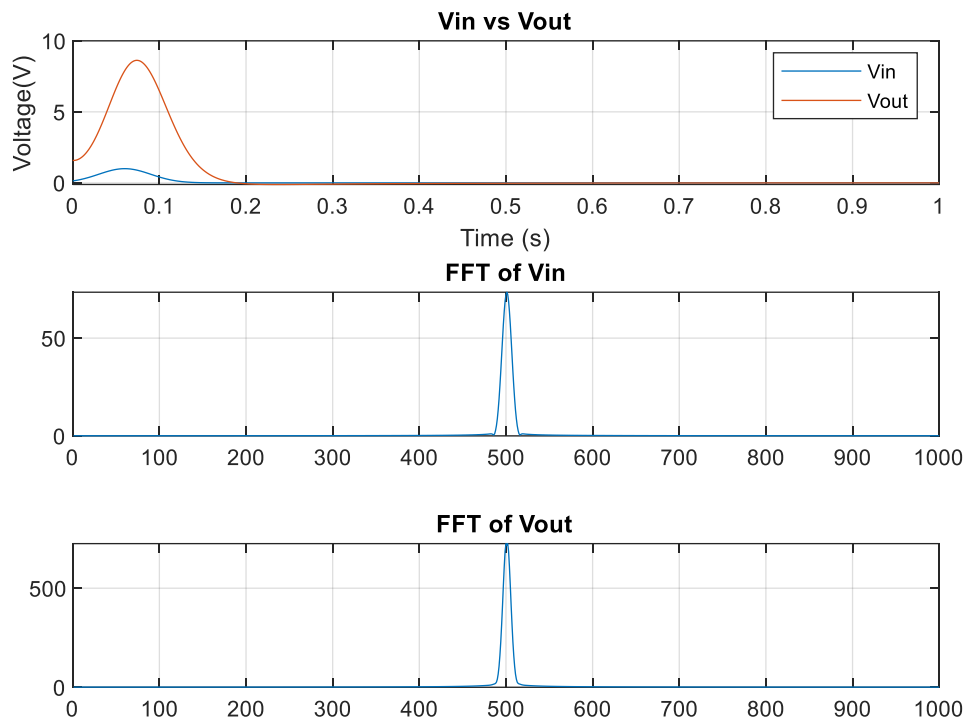


Figure 7: Gaussian Pulse Response

### Part 3: Circuit with Noise

With the addition of noise in the circuit, the C matrix has been updated, as shown below:

```

2.5000e-01  -2.5000e-01      0      0      0      0
-2.5000e-01   2.5000e-01      0      0      0      0
      0      0  1.0000e-05      0      0      0
      0      0      0      0      0      0
      0      0      0      0      0      0
      0      0      0      0      0  -2.0000e-01
      0      0      0      0      0      0
      0      0      0      0      0      0

```

Columns 7 through 8

```

      0      0
      0      0
      0      0
      0      0
      0      0
      0      0
      0      0
      0      0

```

Figure 8: C Matrix

There is also a new FFT response, shown below:

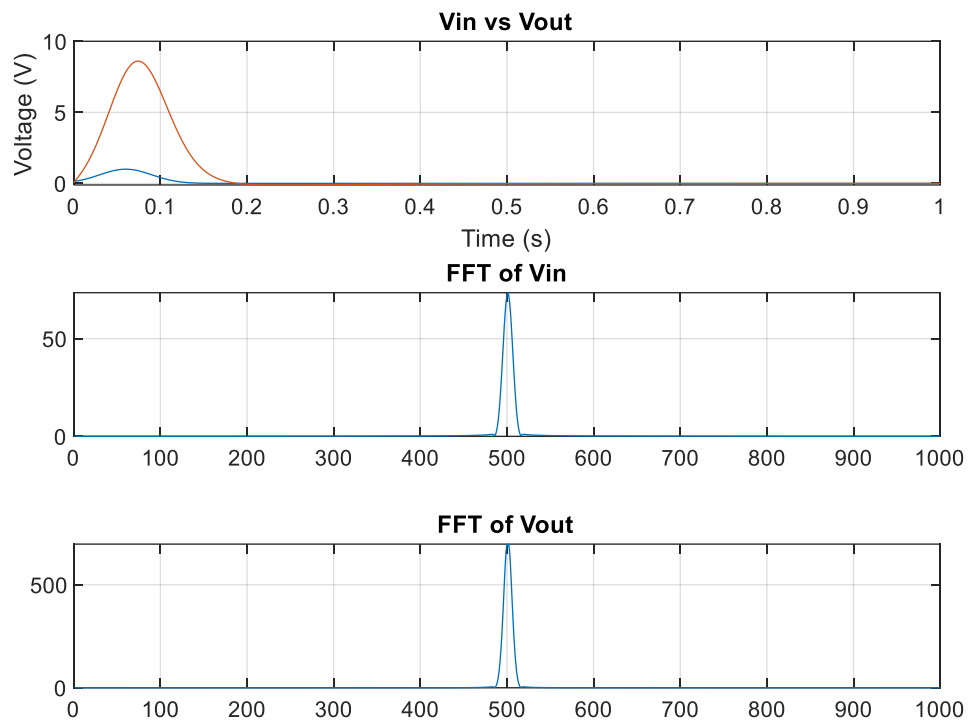


Figure 9: FFT Response

There is also noise in the circuit now, so a distribution can be modelled:



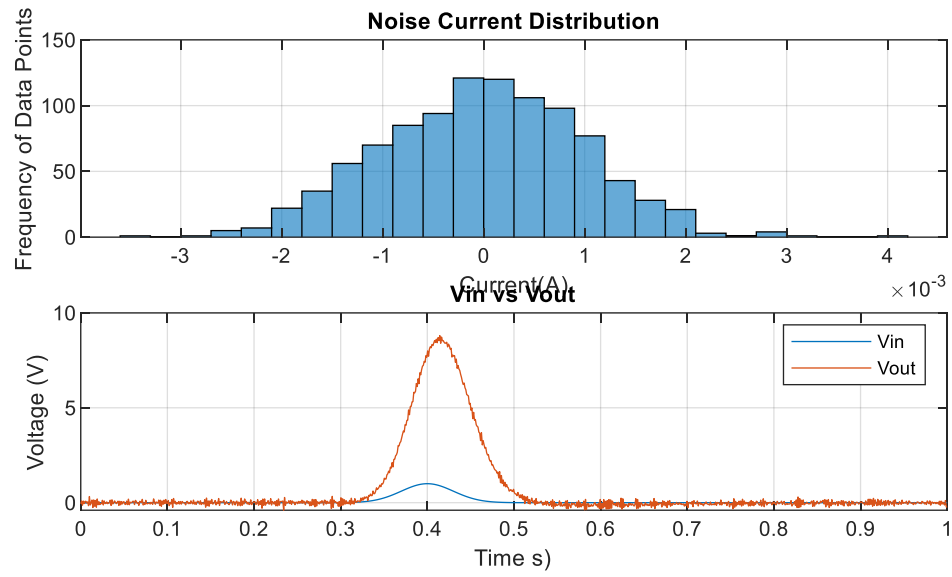


Figure 10: Noise Distribution