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{revtex4}
\usepackage{amsmath}      % need for subequations
\usepackage{graphicx}     % need for figures
\usepackage{verbatim}    % useful for program listings
\usepackage{color}        % use if color is used in text
\usepackage{subfigure}    % use for side-by-side figures
\usepackage{hyperref}     % use for hypertext links, including those to external
                          % documents and URLs

\usepackage[dvipsnames]{xcolor}
\usepackage{multirow}
\usepackage{soul}
%\usepackage[inline]{showlabels}
% \input{/Users/bms/util/definitions}
%\input{/Users/reinaldo/Documents/tex_files/bmsdefinitions.tex}
\def\tama{10cm}
\raggedbottom             % don't add extra vertical space

\begin{document}

\title{Pure Spin Current Injection in Hydrogenated Graphene Structures}
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\date{\today}

\begin{abstract}
We present a theoretical study of spin-velocity injection (SVI) of a pure spin
current (PSC) induced by a linearly polarized light that impinges normally on
the surface of two 50\% hydrogenated noncentrosymmetric two-dimensional (2D)
graphene structures. The first structure, hydrogenated at only one side,
labeled Up, also known as graphone, and the second, one-labelled Alt, is
25\% hydrogenated at both sides. The hydrogenation opens an energy gap in both
structures. We analyze two possibilities: the first, one is by the spin is fixeding
the spin
along a chosen direction, and the resulting SVI is calculated.
In the Ssecondly, we choose the SVI direction along
the surface plane, and calculate the resulting
spin orientation. This is done by changing the energy
 $\hbar\omega$  and polarization angle  $\alpha$  of the incoming light. The
results are calculated within a full electronic band structure scheme using the
Density Functional Theory (DFT) in the Local Density Approximation (LDA). The
maxima of the spin-velocities are reached when  $\hbar\omega=0.084$  eV and
 $\alpha=35^\circ$  for the Up structure, and  $\hbar\omega=0.720$  eV and
 $\alpha=150^\circ$  for the Alt geometry. We find a speed of 668 Km/s and
645 Km/s for the Up and the Alt structures, respectively, when the spin points
perpendicularly to the surface. Also, the response is maximized by
fixing the spin-velocity direction
along a high symmetry axis, obtaining a speed of 688 Km/s
with the spin pointing at  $13^\circ$  from the surface normal, for the Up,
and 906 Km/s and the spin pointing at  $60^\circ$  from the surface normal, for

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the Alt systems. These speed values are of order of magnitude larger than those of bulk semiconductors, such as CdSe and GaAs, thus making the hydrogenated graphene structures excellent candidates for spintronics applications.

\maketitle

\section{Introduction}
\label{sec:introduction}

Spintronics is an emerging research field of electronics in which the manipulation and transport of spin of electrons in a solid state materials is central, adding a new degree of freedom to conventional charge manipulation.\cite{wolfSC04,fabianAPS07} At present, there is an increasing interest in attaining the same level of control over the transport of spin at micro- or nano-scales, as it has been done for the flow of charge in typical 3D-bulk based electronic devices.\cite{awschalomNP2007} Several semiconductor spintronics devices have been proposed \cite{majumdarAPL06, dattaAPL90,gotteNat16,pershinPRB08}, and some of them require spin polarized electrical current \cite{awschalomSSBM13} or pure spin current (PSC). One of the difficulties in creating measurable spin current and development of PSC based semiconductor devices is the fact that the spin relaxation time in conventional semiconducting materials is short to enable the spin transport, thus resulting in a non-observable spin current.\cite{murakamiSc03} For PSC there is no net motion of charge; spin-up electrons move in a given direction, while spin-down electrons travel in the opposite one. This effect can be due to one-photon absorption of linearly polarized light by a semiconductor, with filled valence bands and empty conduction bands, illuminated by light with photon energy larger than the energy gap. This phenomenon can be due to spin injection,\cite{malPRB03} Hall Effects,\cite{sinovaPRB04} interference of two optical beams,\cite{bhatPRL00, najmaiePRB03} or one photon absorption of linearly polarized light\cite{bhatPRL05}. The last effect has been observed in gallium arsenide (GaAs),\cite{zhaoPRL2006, stevensPRL03} aluminum-gallium arsenide (AlGaAs),\cite{stevensPRL03} and Co₂FeSi.\cite{kimuraNGPAM12}

The spin velocity injection (SVI) is an optical effect that quantifies the velocity at which

a PSC moves along the direction $\hat{\mathbf{a}}$, with the spin of the electron polarized along the direction $\hat{\mathbf{b}}$. One photon absorption of polarized light produces an even distribution of electrons in \mathbf{k} space, regardless of the symmetry of the material, resulting in a null electrical current.\cite{bhatPRL05} Then, the electrons excited to the conduction bands at opposite \mathbf{k} points will result in opposite spin polarizations producing no net spin injection in centrosymmetric materials.\cite{bhatPRL05}

If the crystalline structure of the material is noncentrosymmetric, the spin polarization injected at a given \mathbf{k} point not necessarily vanishes.\cite{alvaradoPRL85,schmiedeskampPRL88} Therefore, since the velocities of electrons at opposite \mathbf{k} points are opposite, a PSC will be produced.

Graphene, an allotrope of carbon with hexagonal 2D lattice structure, demonstrates properties such as fractional quantum Hall effect at room temperature, excellent thermal transport properties, excellent conductivity\cite{heerscheNat07} and strength \cite{geimNM07, reinaNL08},

novoselov2S07, balandinNL08}, being a perfect platform for two-dimensional (2D) electronic systems; however, numerous important ~~most~~ electronic applications are disabled by the absence of a semiconducting gap. Recent studies demonstrate that a narrow band gap can be opened in graphene by applying an electric field, \cite{zhangN09} reducing the surface area, \cite{hanPRL07} or applying uniaxial strain. \cite{niACSN08} Another possibility to open the gap is by doping; this has been successfully achieved using nitrogen, \cite{weiNL2009} boron-nitrogen, \cite{guoIJ11} silicon, \cite{colettiPRB10} noble-metals, \cite{varykhalovPRB10} and hydrogen. \cite{eliasS09, guisingerNL09, samarakoonACSN10} Depending on the percentage of hydrogenation and spatial arrangements of the hydrogen-carbon bonds, hydrogenated graphene demonstrates different structural configurations and a tunable electron gap, as it has been proven in Ref. \onlinecite{shkrebtiPSSC12}. In this paper, we ~~present-offer~~ two 50\% hydrogenated graphene noncentrosymmetric structures, both ~~presenting-demonstrating~~ a discernible band gap. The first one, labelled as the Up structure, also known as graphone, \cite{gmitraPRL13} has hydrogen atoms bonded to the carbon layer only on the upper side of the structure; we consider here the magnetic isomer of graphone, with the so-called ``chair'' structure shown in Fig. \ref{fig:up-struc}. In contrast, the Alt structure, shown in Fig. \ref{fig:alt-struc}, has hydrogen alternating on the upper and bottom sides of the carbon sheet. \cite{zapataPSB2016}

Both the Up and the Alt structures are noncentrosymmetric, and therefore, they are good candidates in which SVI can be induced. In this article, we address theoretically the ~~SVI-spin velocity injection~~ by one-photon absorption of linearly polarized light, analyzing in our structures, two possible scenarios of practical interest. The first case is by fixing the spin of the electrons along z , i.e., perpendicular to the surface plane, with the resulting velocity directed along the surface of the structures in the xy plane. In the second case we fix the SVI velocity along the x or y direction, and then, the resulting spin is directed outward of the xy plane.

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\begin{figure}[ht!]
  \centering
  \includegraphics[width=5cm]{figures/fig1}
  \caption{
    Top (top panel) and side (bottom panel) views of the Up
    structure along with the
    Cartesian  $x$ ,  $y$ , and  $z$  directions. The dark (light) spheres
    are the C (H) atoms.
    The primitive hexagonal unit cell is also shown.
    {\color{red}Anatoli: we are confused about the primitive hexagonal
    unit cell shown. For instance, according to us, if we take C2 and
    apply the red arrow, it will end up in the site of C4, but these C
    atoms according to Table \ref{tab:up-unitcell} are not equivalent, or are they? I am
    absolutely sure that the two atoms are equivalent, this structure, e.g., has the same
    symmetry as graphane. They might be slightly not equivalent since the calculations
```

have been done for twice-bigger unit cell. And after your question I have left only three numbers after comma, five is too much and they are below the error in the coordinate determination

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_}}
\label{fig:up-struc}
\end{figure}
\begin{figure}[ht!]
\centering
\includegraphics[width=5cm]{figures/fig2}
\caption{
Top (top panel) and side (bottom panel) views of the Alt
structure along with the
Cartesian  $x$ ,  $y$ , and  $z$  directions. The dark (light) spheres
are the C (H) atoms.
The primitive hexagonal-rectangular unit cell is also shown.
}
\label{fig:alt-struc}
\end{figure}

```

This paper is organized as follows. In Section \ref{sec:theory} we ~~present~~-outline the formalism and the main expressions that describe PSC and SVI. In Section \ref{sec:results} we describe the numerical details and discuss the corresponding SVI spectra for the Up and Alt structures. Finally, we summarize our findings in Section \ref{sec:conclusions}.

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\section{Theory}
\label{sec:theory}

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In this section, we summarize the theoretical approach, involved in calculation of the spin velocity injection (SVI) resulting from the pure spin current (PSC).

To calculate the velocity of the spin injection $\hat{V}^{\mathrm{a}\mathrm{b}}(\omega)$ along the direction $\hat{\mathbf{a}}$, at which the spin moves in a polarized state along direction $\hat{\mathbf{b}}$,

~~we~~ start with the operator that describes the electronic SVI, ~~is~~ written as

$$\begin{aligned} \hat{K}^{\mathrm{a}\mathrm{b}} &= \\ \frac{1}{2} &\left(\hat{v}^{\mathrm{a}} \hat{S}^{\mathrm{b}} + \hat{S}^{\mathrm{b}} \hat{v}^{\mathrm{a}} \right) \end{aligned}$$

~~where~~ Here $\hat{\mathbf{v}} = [\hat{\mathbf{r}}, \hat{H}_0]/i\hbar$ is the velocity operator, with $\hat{\mathbf{r}}$ being the position operator and \hat{H}_0 the unperturbed ground state Hamiltonian; the Roman superscripts indicate Cartesian coordinates. To obtain the expectation value of $\hat{K}^{\mathrm{a}\mathrm{b}}$, we use the length gauge for the perturbing Hamiltonian, written as

$$\hat{H}_{\text{p}} = -e \hat{\mathbf{r}} \cdot \mathbf{E}(t)$$

where the applied electric field of the beam of light is given by

$$\mathbf{E}(t) =$$

$$\{\mathbf{E}(\omega)e^{-i\omega t} + \{\mathbf{E}^*(\omega)e^{i\omega t}$$

.
 \end{align}

In order to calculate the response of the system to $\{\mathbf{E}(t)\}$, one needs to take into account the excited coherent superposition of the spin-split conduction bands inherent to the noncentrosymmetric semiconductors considered in this work.

To include the coherence, we follow Ref.~\onlinecite{nastosPRB07} and use a multiple

scale approach that solves the equation of motion for the single particle density matrix $\{\rho\}_{mn}(\{\mathbf{k}\};t)$, leading to

% just for comments to think about, not to introduce the suggestions right away:
% above we have rho mn, below rho cc'
% time variable has disappeared below. And rho cc' contains a and b labels,
% which are not Cartesian

$$\begin{aligned} & \frac{\partial \rho_{cc'}(\mathbf{k})}{\partial t} = \\ & \frac{e^2 E^{\mathrm{a}}(\omega) E^{\mathrm{b*}}(\omega)}{i \hbar^2} \\ & \sum_{\mathbf{v}} r^{\mathrm{a}}_{\mathbf{cv}}(\mathbf{k}) r^{\mathrm{b}}_{\mathbf{vc}}(\mathbf{k}) \left(\frac{1}{\omega - \omega_{\mathbf{cv}}(\mathbf{k}) - i \epsilon} \right. \\ & \left. - \frac{1}{\omega - \omega_{\mathbf{cv}}(\mathbf{k}) + i \epsilon} \right) \end{aligned}$$

,
 \end{align}

where we assumed that the conduction bands c and c' are quasi-degenerate states, and we take $\epsilon \rightarrow 0$ at the end of the calculation. The spin-splitting of the valence (v) bands is very small, and is neglected throughout this work.\cite{nastosPRB07} The matrix elements of any operator \mathcal{O} are given by $\mathcal{O}_{nm}(\mathbf{k}) = \langle n | \mathbf{k} | \hat{\mathcal{O}} | m | \mathbf{k} \rangle$, where $\langle 0 | n | \mathbf{k} \rangle = \hbar \omega_n(\mathbf{k})$ with $\hbar \omega_n(\mathbf{k})$ being the energy of the electronic band n and m at point $\{\mathbf{k}\}$ in the

irreducible Brillouin zone (IBZ), $|n | \mathbf{k} \rangle$ is the Bloch state, and $\omega_{nm}(\mathbf{k}) = \omega_n(\mathbf{k}) - \omega_m(\mathbf{k})$. Using $\mathcal{O} = \mathrm{Tr}(\hat{\rho} \hat{\mathcal{O}})$ for the expectation value of an observable \mathcal{O} , where Tr denotes the trace, we obtain

$$\begin{aligned} \mathcal{O} = & \int \frac{d^3 k}{8\pi^3} \sum_{cc'} \rho_{cc'}(\mathbf{k}) \\ & \mathcal{O}_{c'c}(\mathbf{k}), \end{aligned}$$

where we used the closure relationship $\sum_n |n | \mathbf{k} \rangle \langle n | \mathbf{k} | = 1$, where n goes over all v and c states, and the fact that $\rho_{vn}(\mathbf{k}) = \rho_{nv}(\mathbf{k}) = 0$ for $n=c, c'$. Therefore, using Eqs. \eqref{z.4}

and \eqref{z.5}, the rate of change of \mathcal{O} , $\dot{\mathcal{O}} = \mathrm{Tr}(\dot{\hat{\rho}} \hat{\mathcal{O}})$, is given by

$$\begin{aligned} \dot{\mathcal{O}} = & \frac{e^2}{\hbar^2} \int \frac{d^3 k}{8\pi^3} \sum_{cc'} \mathcal{O}_{c'c}(\mathbf{k}) \\ & r^{\mathrm{a}}_{\mathbf{cv}}(\mathbf{k}) r^{\mathrm{b}}_{\mathbf{vc}}(\mathbf{k}) \left(\frac{1}{\omega - \omega_{\mathbf{cv}}(\mathbf{k}) - i \epsilon} - \frac{1}{\omega - \omega_{\mathbf{cv}}(\mathbf{k}) + i \epsilon} \right) \\ & E^{\mathrm{a}}(\omega) E^{\mathrm{b*}}(\omega) \end{aligned}$$

\label{eq:dotO}

\end{align}

The prime symbol '\$'\$ in the sum means that \$c\$ and \$c'\$ are quasi-degenerate states, and the sum only covers these states. Replacing \$\hat{\mathcal{O}} \rightarrow \hat{K}^{\mathrm{ab}}\$, in the above expression, one can show that

$$\begin{aligned} \dot{K}^{\mathrm{ab}}(\omega) &= \mu^{\mathrm{abcd}}(\omega) E^{\mathrm{c}}(\omega) E^{\mathrm{d*}}(\omega), \\ \text{\label{eq:dotk}} \end{aligned}$$

where the repeated Cartesians upperscripts are summed, and

$$\begin{aligned} \mu^{\mathrm{abcd}}(\omega) &= \frac{\pi e^2}{\hbar^2} \int \frac{d^3k}{8\pi^3} \sum'_{\mathrm{vcc}} \delta(\omega - \omega_{\mathrm{cv}}(\mathbf{k})) \mathrm{Re} \left[K^{\mathrm{ab}}_{\mathrm{cc}}(\mathbf{k}) \right. \\ &\quad \left. r^{\mathrm{c}}_{\mathrm{vc}}(\mathbf{k}) r^{\mathrm{d}}_{\mathrm{cv}}(\mathbf{k}) + (c \leftrightarrow d) \right] \\ \text{\label{eq:mu}} \end{aligned}$$

is the pseudotensor that describes the rate of change of the PSC process in

semiconductors. To derive what we presented above we used \$K^{\mathrm{ab}}_{\mathrm{nm}}(-\mathbf{k}) = K^{\mathrm{ab*}}_{\mathrm{nm}}(\mathbf{k})\$, which follows from time-reversal invariance. Since \$\mu^{\mathrm{abcd}}(\omega)\$ is real, we have that \$\mu^{\mathrm{abcd}}(\omega) = \mu^{\mathrm{abdc}}(\omega)\$. We point out that Eq.~\eqref{eq:mu} is identical to Eq. (3) of Bhat et al., \cite{bhatPRL05} derived using the semiconductor optical Bloch equations. Using the closure relation,

$$\begin{aligned} K^{\mathrm{ab}}_{\mathrm{cc}}(\mathbf{k}) &= \frac{1}{2} \sum_{\mathrm{l=v,c}} \left(v^{\mathrm{a}}_{\mathrm{cl}}(\mathbf{k}) S^{\mathrm{b}}_{\mathrm{lc}}(\mathbf{k}) + S^{\mathrm{b}}_{\mathrm{cl}}(\mathbf{k}) v^{\mathrm{a}}_{\mathrm{lc}}(\mathbf{k}) \right) \\ \text{\label{eq:velspimatelem}} \end{aligned}$$

We define the spin velocity injection (SVI) as

$$\mathcal{V}^{\mathrm{ab}}(\omega) \equiv \frac{\dot{K}^{\mathrm{ab}}(\omega)}{(\hbar/2) \cdot n(\omega)},$$

which gives the velocity, along direction \$\hat{\mathbf{a}}\$, at which the spin moves in a

polarized state along direction \$\hat{\mathbf{b}}\$.

The carrier injection rate \$\dot{n}(\omega)\$ is written as \cite{nastosPRB07}

$$\begin{aligned} \dot{n}(\omega) &= \xi^{\mathrm{ab}}(\omega) E^{\mathrm{c}}(\omega) E^{\mathrm{d*}}(\omega) \\ \text{\label{eq:dotn}} \end{aligned}$$

where the tensor

$$\begin{aligned} & \xi^{\mathrm{ab}}(\omega) \\ & = \\ & \frac{2\pi e^2}{\hbar^2} \int \frac{d^3k}{8\pi^3} \sum_{\mathbf{vc}} \mathbf{r}^{\mathrm{a}}_{\mathbf{vc}}(\mathbf{k}) \mathbf{r}^{\mathrm{b}}_{\mathbf{cv}}(\mathbf{k}) \delta(\omega - \omega_{\mathbf{cv}}(\mathbf{k})), \end{aligned}$$

is related to the imaginary part of the linear optical response tensor by $\mathrm{Im}[\epsilon^{\mathrm{ab}}(\omega)] = 2\pi \epsilon_0 \hbar \xi^{\mathrm{ab}}(\omega)$.

The function $V^{\mathrm{ab}}(\omega)$ allows us to quantify two very important aspects of PSC. On one hand, we can fix the spin direction along $\hat{\mathbf{b}}$ and calculate the resulting electron velocity. On the other hand, we can fix the velocity of the electron along $\hat{\mathbf{a}}$ and study the

resulting direction along which the spin is polarized. To this end, the additional advantage of 2D structures, besides being noncentrosymmetric, is that we can use an incoming linearly polarized light at normal incidence, and use the direction of the polarized electric field to control $V^{\mathrm{ab}}(\omega)$. Indeed, writing $\mathbf{E}(\omega) = E_0(\omega)(\cos\alpha\hat{\mathbf{x}} + \sin\alpha\hat{\mathbf{y}})$, where α is the polarization angle, we obtain from Eq. \eqref{eq:vab-w} that

$$\begin{aligned} & \mathcal{V}^{\mathrm{ab}}(\omega, \alpha) \\ & = \\ & \frac{2}{\hbar \xi(\omega)} \left(\mu^{\mathrm{abxx}}(\omega) \cos^2\alpha + \mu^{\mathrm{abyy}}(\omega) \sin^2\alpha + \mu^{\mathrm{abxy}}(\omega) \sin 2\alpha \right) \end{aligned}$$

,
 $\label{eq:vab-aw}$
 \end{align}
 $\end{widetext}$

since for the structures chosen in this article, $\xi^{\mathrm{xx}}(\omega) = \xi^{\mathrm{yy}}(\omega) \equiv \xi(\omega)$, and $\xi^{\mathrm{xy}}(\omega) = 0$. Next, we identify two options for $V^{\mathrm{ab}}(\omega)$.

Fixing the spin polarization $\label{sec:theory-fixspin}$

Analyzing the SVI, Eq. \eqref{eq:vab-aw}, we calculate the magnitude of the electron velocity along the plane of the structure, with the spin polarized along $\hat{\mathbf{b}}$ direction as

$$\begin{aligned} & \mathcal{V}_{\sigma^{\mathrm{b}}}(\omega, \alpha) \\ & \equiv \\ & \sqrt{[\mathcal{V}^{\mathrm{xb}}(\omega, \alpha)]^2 + [\mathcal{V}^{\mathrm{yb}}(\omega, \alpha)]^2} \\ & , \end{aligned}$$

$\label{eq:vs-mag}$

```

\end{equation}
and define the angle at which the velocity is directed on the  $xy$  plane as
\begin{equation}
\gamma_{\sigma^{\mathrm{b}}}(\omega, \alpha)
=
\tan^{-1} \left( \frac{\mathcal{V}^{\mathrm{yb}}(\omega, \alpha)}{\mathcal{V}^{\mathrm{xb}}(\omega, \alpha)} \right)
.
\label{eq:gamma-ang}
\end{equation}
We also define two special angles
\begin{equation}
\gamma_{\sigma^{\mathrm{b}}}^{\parallel}(\omega, \alpha) = \alpha,
\label{eq:gamma-par}
\end{equation}
and
\begin{equation}
\gamma_{\sigma^{\mathrm{b}}}^{\perp}(\omega, \alpha) = \alpha \pm 90^{\circ},
\label{eq:gamma-perp}
\end{equation}
corresponding to the electron velocity being parallel or perpendicular to the
incoming light polarization direction, respectively.
The subscript  $\sigma^{\mathrm{b}}$ 
denotes the spin along  $\hat{\mathbf{b}}$ .

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\subsection{Fixing the electron velocity.}\label{sec:theory-fixvel}

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Fixing the calculated velocity along $\mathbf{a}=x$ or $\mathbf{a}=y$, we
define its corresponding magnitude as

```

\begin{align}
\mathcal{V}_{\mathbf{a}}(\omega, \alpha) &\equiv \\
&\sqrt{
[\mathcal{V}^{\mathrm{ax}}(\omega, \alpha)]^2 +
[\mathcal{V}^{\mathrm{ay}}(\omega, \alpha)]^2 +
[\mathcal{V}^{\mathrm{az}}(\omega, \alpha)]^2
},
\label{eq:vv-mag}
\end{align}

```

from where we see that the spin would be oriented in the xyz system of
coordinates by along the ~~defined~~ polar angle, defined as

```

\begin{equation}
\theta_{\mathbf{a}}(\omega, \alpha) =
\cos^{-1} \left( \frac{\mathcal{V}^{\mathrm{az}}(\omega, \alpha)}{\mathcal{V}_{\mathbf{a}}(\omega, \alpha)} \right),
\quad 0 \leq \theta \leq \pi,
\label{eq:polar-ang}
\end{equation}

```

and ~~an~~ the azimuthal angle

```

\begin{equation}
\varphi_{\mathbf{a}}(\omega, \alpha) =
\tan^{-1} \left( \frac{\mathcal{V}^{\mathrm{ay}}(\omega, \alpha)}{\mathcal{V}^{\mathrm{ax}}(\omega, \alpha)} \right),
\quad 0 \leq \varphi \leq 2\pi.
\label{eq:azimuthal-ang}
\end{equation}

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\section{Results}
\label{sec:results}

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\begin{table}[t]

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\center
\begin{tabular}{ccccc}\\
\hline
\quad Atom \quad & \multicolumn{3}{c}{Position (\AA)} & \\
\cline{2-4}
\quad type \quad & $x$ & $y$ & $z$ & \\
\hline
H$_1$ & -0.61516 & -1.77416 & 0.73196 & \\
H$_2$ & 0.61518 & 0.35514 & 0.73175 & \\
C$_1$ & -0.61516 & -1.77264 & -0.49138 & \\
C$_2$ & -0.61516 & -0.35600 & -0.72316 & \\
C$_3$ & 0.61516 & 0.35763 & -0.49087 & \\
C$_4$ & 0.61518 & 1.77416 & -0.73196 & \\
\hline
\end{tabular}
\caption{
Atomic positions in the unit cell of the Up structure shown
in Fig. \ref{fig:up-struc}.
}
\label{tab:up-unitcell}
\end{table}
\begin{table}[t]
\center
\begin{tabular}{ccccc}\\
\hline
\quad Atom \quad & \multicolumn{3}{c}{Position (\AA)} & \\
\cline{2-4}
\quad type \quad & $x$ & $y$ & $z$ & \\
\hline
H$_1$ & -0.61516 & -1.42140 & 1.47237 & \\
C$_1$ & -0.61516 & -1.73300 & 0.39631 & \\
C$_2$ & 0.61516 & 1.73300 & 0.15807 & \\
C$_3$ & 0.61516 & 0.42201 & -0.15814 & \\
C$_4$ & -0.61516 & -0.37396 & -0.39632 & \\
H$_2$ & -0.61516 & -0.68566 & -1.47237 & \\
\hline
\end{tabular}
\caption{
Atomic positions in the unit cell of the Alt structure
shown in Fig. \ref{fig:alt-struc}.
}
\label{tab:alt-unitcell}
\end{table}

```

We present the calculated results of $\mathcal{V}_{\sigma^{\mathrm{b}}}(\omega, \alpha)$ and $\mathcal{V}_{\mathrm{a}}(\omega, \alpha)$ for the Up and Alt structures, both noncentrosymmetric 2D carbon systems with 50% hydrogenation, which are differently structurally arranged. We remind that the Up structure has hydrogen atoms only on the upper side of the carbon sheet, while the Alt structure has alternating hydrogen atoms on the upper and bottom sides. We take the carbon lattice to be along the xy plane for both structures, and the carbon-hydrogen bonds are outward the plane, they are perpendicular to xz plane for the Up structure, as depicted in Figs. \ref{fig:up-struc}, and off the normal for the Alt structure \ref{fig:alt-struc}. The coordinates for the Up and Alt unit cells of the structures are presented in Tables \ref{tab:up-unitcell} and \ref{tab:alt-unitcell}, respectively.

We calculated the self-consistent ground state and the Kohn-Sham states within

density functional theory in the local density approximation (DFT-LDA), with a planewave basis using the ABINIT code \cite{gonzeCPC09}. We used Hartwigsen-Goedecker-Hutter (HGH) relativistic separable dual-space Gaussian pseudopotentials \cite{hartwigsenPRB98}, including the spin-orbit interaction needed to calculate $\mu^{\mathrm{abcd}}(\omega, \alpha)$ ~~presented from~~ Eq. \eqref{eq:mu}.

The convergence parameters for the calculations, corresponding to the Up and Alt structures are cutoff energies up to 65 eV, resulting in LDA energy band gaps of 0.084 eV and 0.718 eV, respectively, and 14452 \mathbf{k} points in the IBZ

where the energy

eigenvalues and matrix elements were calculated;

to integrate $\mu^{\mathrm{abcd}}(\omega)$ and $\xi^{\mathrm{ab}}(\omega)$ the linearized analytic tetrahedron method (LATM) has been used. \cite{nastosPRB07}

We neglect the anomalous velocity term

$\hbar(\boldsymbol{\sigma} \times \nabla V)/4m^2c^2$, where V is the crystal potential, in $\hat{\mathbf{v}}$ of Eq. \eqref{z.1}, as this term is known to give small contribution to PSC. \cite{bhatPRL05} Therefore, $[\hat{\mathbf{v}}, \hat{\mathbf{S}}] = 0$, and Eq. \eqref{z.1} reduces to $\hat{K}^{\mathrm{ab}} = \hat{v}^{\mathrm{a}} \hat{S}^{\mathrm{b}} = \hat{S}^{\mathrm{b}} \hat{v}^{\mathrm{a}}$.

Finally, the prime in the sum of Eq. \eqref{eq:mu} is restricted to quasi-degenerated conduction bands c and c' that are closer than 30 meV to each other, which is both typical laser-pulse energy width and the thermal

room-temperature energy level broadening. \cite{nastosPRB07}

room-temperature energy level broadening. \cite{nastosPRB07}

\subsection{SVI: Spin velocity injection}

\label{sec:res-spin_velocity}

\begin{figure}[t]

\centering

\includegraphics[width=\tama]{figures/fig3}

\caption Spin velocity +injection $\mathcal{V}^{\mathrm{ab}}(\omega, \alpha)$

\it vs. photon energy $\hbar\omega$, for the angles α that maximize the signal. The

largest velocity are at the low energy regions of the spectra for the Alt and Up structures, becoming different from zero at the energy gap of each

structure. In the high energy regions, the values of

$\mathcal{V}^{\mathrm{ab}}(\omega, \alpha)$ are also very large compared to the 3D case of CdSe and GaAs, shown at the bottom panel.)

\label{fig:vab-str-comp}

\end{figure}

In Fig. \ref{fig:vab-str-comp}, we show $\mathcal{V}^{\mathrm{ab}}(\omega, \alpha)$ \it vs. $\hbar\omega$ for the

velocity and spin

directions

$\hat{\mathbf{a}}$ and $\hat{\mathbf{b}}$, and for the angle α , at which the signal is maximized, for the Up and Alt structures, and for CdSe and GaAs bulk systems, shown for comparison. As expected from

Eq. \eqref{eq:mu},

$\mathcal{V}^{\mathrm{ab}}(\omega, \alpha)$ starts rising becomes different from zero right at the

corresponding energy gap of each system. For the 2D structures considered, the spectrum contains two narrow energy regions with strong response, while for the bulk systems, the spectra covers a rather wide energy range, but with a much weaker response. For the Up structure, at $\mathbf{ab} = yz$ and $\alpha = 35^\circ$ the response is maximized, which means that an incoming light

their corresponding polarization angle α and energy $\hbar\omega$. }

\label{tab:vab-str-comp}

\end{table}

\subsection{Fixing spin}

\label{sec:res-fixspin}

\begin{figure}[t]

\centering

\includegraphics[width=\tama]{figures/fig4}

\caption{Color online. For the Up structure, the top panel shows $\mathcal{V}_{\sigma^{\mathrm{z}}}(\omega, \alpha)$ {\it vs.} $\hbar\omega$ and α , and the bottom panel shows $\gamma_{\sigma^{\mathrm{z}}}(\omega, \alpha)$ (right scale, red line), and $\mathcal{V}_{\sigma^{\mathrm{z}}}(\omega, \alpha)$ (left scale, black solid line), {\it vs.} α , for $\hbar\omega=0.084$ eV, i.e. along the ridge shown in the 3D plot. }

\label{fig:up-vs-z-w1}

\end{figure}

\begin{figure}[t]

\centering

\includegraphics[width=\tama]{figures/fig5}

\caption{For the Up structure, the top panel shows $\mathcal{V}_{\sigma^{\mathrm{z}}}(\omega, \alpha)$ {\it vs.} $\hbar\omega$ and α , and the bottom panel shows $\gamma_{\sigma^{\mathrm{z}}}(\omega, \alpha)$ (right scale, red line, long dashes), and $\mathcal{V}_{\sigma^{\mathrm{z}}}(\omega, \alpha)$ (left scale, black solid line), {\it vs.} α , for $\hbar\omega=1.954$ eV, i.e. along the highest ridge shown in the 3D plot. }

\label{fig:up-vs-z-w2}

\end{figure}

In this subsection, we calculate $\mathcal{V}_{\sigma^{\mathrm{z}}}(\omega, \alpha)$, Eq. \eqref{eq:vs-mag}, for the case with the spin fixed along z , i.e.

directed perpendicularly to the surface of the Up and Alt structures. Also, we calculate $\gamma_{\sigma^{\mathrm{z}}}(\omega, \alpha)$ from Eq.

\eqref{eq:gamma-ang}, which determines the direction of the injected electrons movement along the surface of each structure. We mention that we have also analyzed the cases when the spin is directed along x or y , finding similar qualitative results to those presented below.

{\color{red}Anatoli: stop here!! I have not gone through the rest!!}

\subsubsection{Up structure}\label{up:fs}

In the top panel of Fig. \ref{fig:up-vs-z-w1}, we plot

$\mathcal{V}_{\sigma^{\mathrm{z}}}(\omega, \alpha)$ {\it vs.}

$0.080 \leq \hbar\omega \leq 0.096$ eV (similar energy range for the Up structure shown in the left panel of Fig.~\ref{fig:vab-str-comp}) and

$0^\circ \leq \alpha \leq 180^\circ$. We see a broad peak that reaches the maximum of $\mathcal{V}_{\sigma^{\mathrm{z}}}(\omega, \alpha) = 739.7$ Km/s at

$\alpha=35^\circ$ and $\hbar\omega=0.084$ eV. The variation of $\mathcal{V}_{\sigma^{\mathrm{z}}}(\omega, \alpha)$ as a function of α ,

which comes from the interplay of the μ tensor components as multiplied by the trigonometric functions of Eq.~\eqref{eq:vab-aw}, gives a

sizable set of values between 739.7 Km/s and 165.4 Km/s, for

$0.084 \leq \hbar\omega \leq 0.090$ eV. In the bottom panel, we show

$\mathcal{V}_{\sigma^{\mathrm{z}}}(\omega, \alpha)$ {\it vs.} α (left scale, black line), at $\hbar\omega=0.084$ eV, thus following the ridge in the 3D

plot of the top panel. Also, we plot the corresponding velocity angle $\gamma_{\sigma^z}(\omega, \alpha)$ (right scale, red line), where it is very interesting to see that $\gamma_{\sigma^z}(\omega, \alpha)$ is centered at 64.55° with a rather small deviation of only $\pm 0.03^\circ$, for the whole range of α . This result means that for $\hbar\omega=0.084$ eV and for all values of α , the electrons, with the chosen spin pointing along z , will move at the angle of $\gamma_{\sigma^z}(\omega, \alpha) \sim 64.5^\circ$ with respect to the x direction, with the range of high speeds $V_{\sigma^z}(\omega, \alpha)$ shown in the figure. Also, from Eq. \eqref{eq:gamma-par} we find that $\gamma^{\parallel}_{\sigma^z}(\omega, \alpha) = \alpha = 64.56^\circ$, with $V_{\sigma^z}(\omega, \alpha) = 631.1$ Km/s (see green arrow), and that from Eq. \eqref{eq:gamma-perp}, $\gamma^{\perp}_{\sigma^z}(\omega, \alpha) = \alpha - 90^\circ = 64.50^\circ$, gives $\alpha = 154.50^\circ$, with $V_{\sigma^z}(\omega, \alpha) = 191.5$ Km/s (see blue arrow). Thus, at $\hbar\omega=0.084$ eV, an incident field, polarized at $\alpha \sim 65.5^\circ$ or $\sim 154.5^\circ$, injects electrons with their spin polarized along z , which move parallel or perpendicular to the incident electric field, with a speed of 631.14 Km/s or 191.5 Km/s, respectively.

Now, we analyze the results for the second energy range of the Up structure shown in the top right panel of Fig. \ref{fig:vab-str-comp}. In the top panel of Fig. \ref{fig:up-vs-z-w2}, we plot $V_{\sigma^z}(\omega, \alpha)$ {\it vs.} $1.950 \leq \hbar\omega \leq 1.960$ eV and $0^\circ \leq \alpha \leq 180^\circ$. We see two broad peaks that maximize at $\alpha = 35^\circ$ and $\hbar\omega = 1.954$ eV, with a value of $V_{\sigma^z}(\omega, \alpha) = 193.5$ Km/s, and at $\alpha = 35^\circ$ and $\hbar\omega = 1.957$ eV, with a value of $V_{\sigma^z}(\omega, \alpha) = 170.6$ Km/s. We only analyze the highest maximum in the bottom panel, where we show $V_{\sigma^z}(\omega, \alpha)$ {\it vs.} α (left scale, black line), at $\hbar\omega = 1.954$ eV, thus following the highest ridge shown in the 3D plot of the top panel. Also, we plot the corresponding velocity angle $\gamma_{\sigma^z}(\omega, \alpha)$ (right scale, red line), where in this case we see that the values of $\gamma_{\sigma^z}(\omega, \alpha)$ have more dispersion, as a function of α , than for the lower energy range shown in the bottom panel of Fig. \ref{fig:up-vs-z-w1}. However, $\gamma_{\sigma^z}(\omega, \alpha) \sim 77.8^\circ$ is nearly constant from $\alpha = 0^\circ$ up to $\alpha \sim 85^\circ$. In this case, we find that $\gamma^{\parallel}_{\sigma^z}(\omega, \alpha) = \alpha = 78.0^\circ$, with $V_{\sigma^z}(\omega, \alpha) = 115.0$ Km/s (as indicated by green arrow), and that from Eq. \eqref{eq:gamma-perp}, $\gamma^{\perp}_{\sigma^z}(\omega, \alpha) = \alpha - 90^\circ = 167.8^\circ$, gives $\alpha = 77.8^\circ$, with $V_{\sigma^z}(\omega, \alpha) = 65.6$ Km/s (see blue arrow). Thus, through the correct choice of $\hbar\omega$ and α we could inject electrons, in this case with their spin polarized along z , which move parallel or perpendicular to the incident electric field, with sizable speeds.

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\begin{figure}[tb]
\centering
\includegraphics[width=\tama]{figures/fig6}
\caption{Color online. For the Alt structure, the top panel shows  $V_{\sigma^z}(\omega, \alpha)$  {\it vs.}  $\hbar\omega$  and  $\alpha$ , and the bottom panel shows  $\gamma_{\sigma^z}(\omega, \alpha)$  (right scale, red line), and  $V_{\sigma^z}(\omega, \alpha)$  (left scale, black line), {\it vs.}  $\alpha$ , for  $\hbar\omega=0.720$  eV, i.e. along the ridge shown in the 3D plot.}
\label{fig:alt-vs-z}
```


For the Up structure, we find once again that $\alpha=35^\circ$ maximizes the response. In Fig. \ref{fig:up-vab-comp-rtp-1}, we plot $\mathcal{V}_{\mathrm{a}}(\omega, \alpha)$ (left scale, black line), $\theta_{\mathrm{a}}(\omega, \alpha)$ (right scale, red line), and $\varphi_{\mathrm{a}}(\omega, \alpha)$, (right scale, blue line), {\it vs.} $\hbar\omega$, for $\mathrm{a}=x, y$. We see that for $\hbar\omega=0.084$ eV, the response has a maximum of $\mathcal{V}_{\mathrm{x}}(\omega, \alpha)=431.7$ Km/s at $\theta_{\mathrm{x}}(\omega, \alpha)=42.5^\circ$, and $\varphi_{\mathrm{x}}(\omega, \alpha)=208.3^\circ$, and $\mathcal{V}_{\mathrm{y}}(\omega, \alpha)=687.9$ Km/s at $\theta_{\mathrm{y}}(\omega, \alpha)=13.9^\circ$, and $\varphi_{\mathrm{y}}(\omega, \alpha)=82.1^\circ$. This means that the spin is directed upward the third quadrant of the xy plane when the electron moves along x , and is almost parallel to the xy plane in the first quadrant when it moves along y . Also from this figure, we see that when the electron moves along x , the spin direction is almost constant for all the energies across the peak of the response, having $42.5^\circ < \theta_{\mathrm{x}}(\omega, \alpha) < 53.7^\circ$ and $208.3^\circ < \varphi_{\mathrm{x}}(\omega, \alpha) < 215.7^\circ$. When the electron moves along y , the spin polar angle has again small variations, $11.3^\circ < \theta_{\mathrm{y}}(\omega, \alpha) < 13.9^\circ$, but the azimuthal angle varies significantly, $82.1^\circ < \varphi_{\mathrm{y}}(\omega, \alpha) < 182.4^\circ$.

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\begin{figure}[t]
\centering
\includegraphics[width=\tama]{figures/fig8}
\caption{The Up structure: the spin velocity  $\mathcal{V}_{\mathrm{a}}(\omega, \alpha)$  (left scale, black line), the polar angle  $\theta_{\mathrm{a}}(\omega, \alpha)$  (right scale, red line), and the azimuthal angle  $\varphi_{\mathrm{a}}(\omega, \alpha)$ , (right scale, blue line), {\it vs.}  $\hbar\omega$ , for  $\alpha=35^\circ$ , and  $\mathrm{a}=x$  or  $\mathrm{a}=y$  is shown. }
\label{fig:up-vx-vy-w2}
\end{figure}
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In Fig. \ref{fig:up-vx-vy-w2}, we plot $\mathcal{V}_{\mathrm{a}}(\omega, \alpha)$ {\it vs.} $\hbar\omega$, in the range where there two local maxima with opposite sign at $\hbar\omega=1.954$ eV and $\hbar\omega=1.957$ eV occur. The first is the largest of the two, with $\mathcal{V}_{\mathrm{x}}(\omega, \alpha)=61.2$ Km/s, $\theta_{\mathrm{x}}(\omega, \alpha)=48.3^\circ$, and $\varphi_{\mathrm{x}}(\omega, \alpha)=54.3^\circ$, for the electron moving along x ; and $\mathcal{V}_{\mathrm{y}}(\omega, \alpha)=293.2$ Km/s, $\theta_{\mathrm{y}}(\omega, \alpha)=49.8^\circ$, and $\varphi_{\mathrm{y}}(\omega, \alpha)=51.9^\circ$ for the electron moving along y . For the peak at $\hbar\omega=1.957$ eV, we obtain $\theta_{\mathrm{x}}(\omega, \alpha)=129.8^\circ$ and $\varphi_{\mathrm{x}}(\omega, \alpha)=231.7^\circ$, with $\mathcal{V}_{\mathrm{x}}(\omega, \alpha)=54.6$ Km/s and $\theta_{\mathrm{y}}(\omega, \alpha)=129.3^\circ$; and $\varphi_{\mathrm{y}}(\omega, \alpha)=230.7^\circ$, with $\mathcal{V}_{\mathrm{y}}(\omega, \alpha)=263.7$ Km/s. We remark that these angles are almost constant for all the energy values across the peak of these two local maxima, for which the spin is directed upward in the first quadrant of the xy plane when the electron moves along either x or y directions.

\subsubsection{Alt structure}

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\begin{figure}[tb]
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\centering
\includegraphics[width=\tama]{figures/fig9}
\caption{The Alt structure: the velocity  $\mathcal{V}_{\mathrm{a}}$ 
( $\omega, \alpha$ )$ (left scale, black line), the polar angle  $\theta_{\mathrm{a}}$ 
( $\omega, \alpha$ )$ (right scale, red line), and the azimuthal angle
 $\varphi_{\mathrm{a}}$  ( $\omega, \alpha$ )$, (right scale, blue line), {\it vs.}
 $\hbar\omega$ , for  $\alpha=150^\circ$ , and  $\mathrm{a}=x$  or  $\mathrm{a}=y$  are
shown. }
\label{fig:alt-vx-vy-w1}
\end{figure}

```

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\begin{figure}[tb]
\centering
\includegraphics[width=\tama]{figures/fig10}
\caption{The Alt structure:  $\mathcal{V}_{\mathrm{a}}$ 
( $\omega, \alpha$ )$ (left scale, black line), the polar angle  $\theta_{\mathrm{a}}$ 
( $\omega, \alpha$ )$ (right scale, red line), and the azimuthal angle
 $\varphi_{\mathrm{a}}$  ( $\omega, \alpha$ )$, (right scale, blue line), {\it vs.}
 $\hbar\omega$ , for  $\alpha=150^\circ$ , and  $\mathrm{a}=x$  or  $\mathrm{a}=y$  are
shown.}
\label{fig:alt-vx-vy-w2}
\end{figure}

```

In Figs. \ref{fig:alt-vx-vy-w1} and \ref{fig:alt-vx-vy-w2}, we plot \mathcal{V}_{a} (ω, α)\$ (left scale, black line), θ_{a} (ω, α)\$ (right scale, red line), and φ_{a} (ω, α)\$, (right scale, blue line), {\it vs.} $\hbar\omega$ in two different ranges, and for $\mathrm{a}=x, y$. In this case, $\alpha=150^\circ$ maximizes both \mathcal{V}_{x} (ω, α)\$ and \mathcal{V}_{y} (ω, α)\$, as a function of α . In Fig. \ref{fig:alt-vx-vy-w1}, the absolute maximum \mathcal{V}_{x} (ω, α) = 301.7\$, Km/s is at $\hbar\omega=0.720$ \$, eV , θ_{x} (ω, α) = 44.5° and φ_{x} (ω, α) = 51.2° ; and \mathcal{V}_{y} (ω, α) = 905.6\$, Km/s at θ_{y} (ω, α) = 119.7° and φ_{y} (ω, α) = 163.4° . Thus, the spin is directed upward the fourth quadrant of the xy plane when the spin velocity is directed along x , while it is directed downward the second quadrant when the spin velocity is directed along y . Finally, in Fig. \ref{fig:alt-vx-vy-w1}, the absolute maximum is at $\hbar\omega=0.911$ \$, eV at \mathcal{V}_{x} (ω, α) = 276.3\$, Km/s, θ_{x} (ω, α) = 154.6° , and φ_{x} (ω, α) = 292.3° , and \mathcal{V}_{y} (ω, α) = 468.6\$, Km/s at θ_{y} (ω, α) = 129.2° , and φ_{y} (ω, α) = 228.3° , implying that the spin is directed downward the fourth quadrant of the xy plane when the spin velocity is directed along x , while is directed downward the third quadrant when the spin velocity is directed along y .

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\section{Conclusions}
\label{sec:conclusions}

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We reported the results of an *ab initio* calculations for the spin velocity injection (SVI) due to the one-photon absorption of the linearly polarized light in the Up and Alt 2D 50% hydrogenated graphene structures. Different possible arrangements of the of the spin injection have been considered: we made the calculations for the cases when the spin is polarized in z direction or when the velocity is directed along x or y . To the best

of our knowledge, this effect has been previously reported in this 2D partially hydrogenated structures. We have shown that the SVI demonstrates an anisotropic behavior, which is very sensitive to the symmetry of the structures of interest. We have found that the Up structure shows the strongest response for the spin directed along z , resulting in the velocity $V_{\sigma^z}(\omega, \alpha) = 668.0 \text{ km/s}$ for the incoming photon energy of 0.084 eV . Also, the Alt structure has the strongest response when the spin moves along y direction, resulting in $V^y(\omega, \alpha) = 905.6 \text{ km/s}$ for the incoming photon energy of 0.720 eV . The speed values obtained here are of the same order of magnitude as those of Ref.~\onlinecite{najmaiePRB03} in unbiased semiconductor quantum well structures, while they are of order of magnitude higher compared to 3D bulk materials. The spin relaxation time in pure and doped graphene is long enough in the order from nanoseconds to milliseconds. \cite{wojtaszekPRB13,ertlerPRB09} Therefore, according to our results, due to the high spin velocity transport both structures considered are the excellent candidates for the development of spintronics devices that require pure spin current (PSC).

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% journal={Phys. E: Low-dim. Sys.},
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