Pure Spin Current Injection in Hydrogenated Graphene Structures

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I. INTRODUCTION

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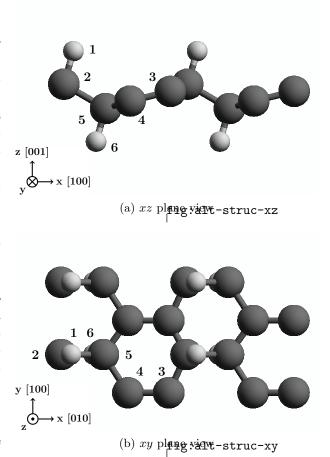
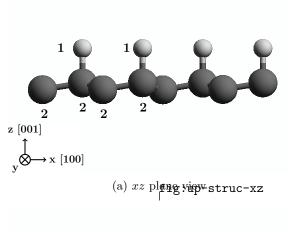


FIG. 1. Alt structurefig:alt-struc

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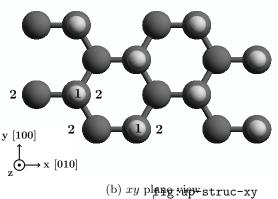


FIG. 2. Up structure fig:up-struc

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TT. THEORY

sec:theory

Pure spin-current

sec:theory-pure_spin_current

The spin density injection current K^{ab} with speed along direction a and spin polarization along b is defined as

$$\dot{K} = \mu^{\rm abcd}(\omega) E^{\rm c}(\omega) E^{\rm d*}(\omega) \qquad \begin{array}{c} {\rm eq:dotk} \\ {\rm (1)} \end{array}$$

where

$$\mu^{\text{abcd}}(\omega) = \frac{\pi e^2}{\hbar^2} \int \frac{d^3 K}{8\pi^3} \sum_{vcc'}^{'} \text{Re} \left[K_{cc'}^{\text{ab}} (r_{vc'}^{\text{c}} r_{cv}^{\text{d}} + r_{vc'}^{\text{d}} r_{cv}^{\text{c}}) \right] \delta(\omega - \omega_{cv})$$

$$\stackrel{\text{eq:mu}}{=} (2)$$

rent pseudotensor. The ' in the sum means that only covers these states.

is the corresponding spin density injection cur- c and c' are quasi degenerate states and the sum

speed at which the spin polarized in the b direction incident beam reaches the xy plane with a po-

Now we define the spin velocity, \mathcal{V}^{ab} as the tion moves along the a direction when a normal larization angle α . Then,

$$\begin{split} \mathcal{V}^{\mathrm{ab}}(\omega) &= \frac{2}{\hbar} \frac{\mu^{\mathrm{abxx}}(\omega) E^2(\omega) \cos^2(\alpha) + \mu^{\mathrm{abyy}}(\omega) E^2(\omega) \sin^2(\alpha) + 2\mu^{\mathrm{abxy}}(\omega) E^2(\omega) \cos(\alpha) \sin(\alpha)}{\xi^{\mathrm{xx}}(\omega) E^2(\omega) \cos^2(\alpha) + \xi^{\mathrm{yy}}(\omega) E^2(\omega) \sin^2(\alpha)}, \\ &= \frac{2}{\hbar} \frac{\mu^{\mathrm{abxx}}(\omega) \cos^2(\alpha) + \mu^{\mathrm{abyy}}(\omega) \sin^2(\alpha) + \mu^{\mathrm{abxy}}(\omega) \sin(2\alpha)}{\xi^{\mathrm{xx}}(\omega) \cos^2(\alpha) + \xi^{\mathrm{yy}}(\omega) \sin^2(\alpha)}. \end{split} \qquad \qquad \text{eq: vab}$$

For an angle $\alpha = \frac{\pi}{4}$ this expression can be reduced to

$$\mathcal{V}^{ab}(\omega) = \frac{2}{\hbar} \frac{\mu^{abxx}(\omega) + \mu^{abyy}(\omega) + 2\mu^{abxy}(\omega)}{\xi^{xx}(\omega) + \xi^{yy}(\omega)}.$$
eq: vab-90deg

В. Fixing spin

sec:theory-fixspin

Considering that we have 2D structures we can fix the spin direction along the x, y, and zCartesian coordinates and then define the magnitude of the spin velocity $|\mathcal{V}_{\sigma^b}|$ in a fixed angle γ_b as

$$\begin{split} |\mathcal{V}_{\sigma^{b}}|(\omega) &= \sqrt{(\mathcal{V}^{ax}(\omega))^{2} + (\mathcal{V}^{ay}(\omega))^{2}}, & \text{(5)} \\ \gamma_{b}(\omega) &= \tan^{-1}\left(\frac{\mathcal{V}^{ay}(\omega)}{\mathcal{V}^{ax}(\omega)}\right), & \text{eq:gamma-ang} \end{split}$$

where the angle is measured in the counterclockwise direction from the positive x axis.

Fixing velocity.

sec:theory-fixvel

In a similar way we can fix the velocity in the xy plane along x and y directions and define $|\mathcal{V}^{\mathbf{a}}|$

$$|\mathcal{V}^{a}|(\omega) = \sqrt{(\mathcal{V}^{ax}(\omega))^2 + (\mathcal{V}^{ay}(\omega))^2 + (\mathcal{V}^{az}(\omega))^2}_{\substack{eq: vv-mag}},$$

and the corresponding polar and azimuthal angles θ and φ as

$$\begin{split} \theta(\omega) &= \cos^{-1}\left(\frac{\mathcal{V}^{\mathrm{az}}(\omega)}{|\mathcal{V}^{\mathrm{a}}(\omega)|}\right), \quad 0 \leq \theta \leq \pi, \quad (8) \\ \varphi(\omega) &= \tan^{-1}\left(\frac{\mathcal{V}^{\mathrm{ay}}(\omega)}{\mathcal{V}^{\mathrm{ax}}(\omega)}\right), \quad 0 \leq \varphi \leq 2\pi. \quad (9) \end{split}$$

Layer	Atom	Position [Å]		
No.	type	x	y	z
1	Н	-0.61516	-1.42140	1.47237
2	\mathbf{C}	-0.61516	-1.73300	0.39631
3	\mathbf{C}	0.61516	1.73300	0.15807
4	\mathbf{C}	0.61516	0.42201	-0.15814
5	\mathbf{C}	-0.61516	-0.37396	-0.39632
6	Н	-0.61516	-0.68566	-1.47237

TABLE I. Unit cell of alt structure. Layer division, atom types and positions for the alt structure. The structure unit cell was divided in six layers corresponding each one to atoms in different z positions. The corresponding layer atom position is depicted in Fig. 1 with the corresponding number of layer to 11

Layer-by-layer analysis.

sec:theory-layer

For a layered system we have that the total contribution of Eqns. (5) and (7) is given¹ by

$$\begin{split} |\mathcal{V}_{\sigma^{\mathrm{b}}}(\omega)| = & \ell_{\mathrm{eff}} \sum_{\ell=1}^{N_{\mathrm{eff}}} |\mathcal{V}_{\sigma^{\mathrm{b}}}(\ell|\omega)|^{\mathrm{eq:vs-layer}} \\ |\mathcal{V}^{\mathrm{a}}(\omega)| = & \ell_{\mathrm{eff}} \sum_{\ell=1}^{N_{\mathrm{eff}}} |\mathcal{V}^{\mathrm{a}}(\ell|\omega)|^{\mathrm{eq:vv-layer}} \\ (11) \end{split}$$

III. RESULTS

sec:results

We preset the results for \mathcal{V}^{ab} for the $C_{16}H_8$ alt and C₁₆H₈-up structures being both noncentrosymmetric semi-infinite carbon systems with 50% hydrogenation in different arrangements. The alt system has alternating hydrogen atoms

Layer	Atom	Position [Å]				
No.	type	x	y	\overline{z}		
1	Η	-0.61516	-1.77416	0.73196		
1	Η	0.61518	0.35514	0.73175		
2	\mathbf{C}	-0.61516	-1.77264	-0.49138		
2	\mathbf{C}	-0.61516	-0.35600	-0.72316		
2	\mathbf{C}	0.61516	0.35763	-0.49087		

TABLE II. Unit cell of *up* structure. Layer division, atom types and positions for the *up* structure. The structure unit cell was divided in two layers corresponding to hydrogen and carbon atoms. The corresponding layer atom position is depicted in Fig. 2 with the corresponding number of layer_up-unitcell

on the upper and bottom sides of the carbon sheet, while the up system has H only on the upper side. We take the hexagonal carbon lattice to be on the xy plane for both structures, and the carbon-hydrogen bonds on the perpendicular xz plane, as depicted in Figs. 1 and 2.

Using the ABINIT code² we calculated the self- consistent ground state and the Kohn-Sham states using density functional theory in the local density approximation (DFT-LDA) with a planewave basis. We used Hartwigsen-Goedecker-Hutter (HGH) relativistic separable dual-space Gaussian pseudopotentials³ including the spin-orbit interaction for calculating $\mathcal{V}^{a}(\omega)$.

The convergence parameters for the calculations of our results corresponding to the alt and up structures are cutoff energies of 65 Ha and 40 Ha, respectively. The energy eigenvalues and matrix elements were calculated using 14452 k points and 8452 k points in the irreducible Brillouin zone (IBZ) and present LDA energy band gaps of 0.72 eV and 0.088 eV, respectively for the alt and up structures. As mentioned in⁴, using DFT the LDA is only one method of many other that can be used to calculate the electronic structure of materials. Also it is known that all methods predict a different band gap than the obtained in the experiment. A correction for the band gap energy value can be calculated by other ab-initio methods such as the GW approximation⁵ being this outside the scope of this paper.

The structures presented here where divided

into layers to analyze the he layer-by-layer contribution for $\mathcal{V}^{\mathrm{ab}}$ response. The *alt* structure was divided in six layers corresponding the first one to the top hydrogen atoms, from the second to the forth to carbon atoms in different z positions, and the sixth and last one to the bottom hydrogen atoms. The up structure was divided into two layers, the first one comprised by the top hydrogen atoms and the second by the carbon atoms. The layer divisions and atom positions for the unit cells are shown in Tables I and II.

IV. FIXING SPIN

sec:res-fixspin

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A. Fixing velocity

sec:res-fixvel

Alt structure.

For the alt structure we analyzed the energy range from $0.6\,\mathrm{eV}$ to $1.0\,\mathrm{eV}$ where we found the most intense response for $|\mathcal{V}^{\mathrm{x}}|$ and $|\mathcal{V}^{\mathrm{a}}|$. In Fig. 3 we present the $|\mathcal{V}^{\mathrm{a}}|$ spectra resulting from evaluate Eq. (7) using different polarization angles α in Eq. (3) for the $C_{16}H_8$ -alt structure. We can see that the onset of the response is when the energy of the incoming light is the same of the gap energy. From this picture we can see that for the zone between the energy range of $0.90\,\mathrm{eV}$ - $0.93\,\mathrm{eV}$ and polarization angles between 120° and 150° is the zone where the maximum

360

315

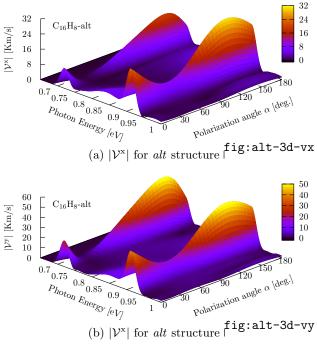
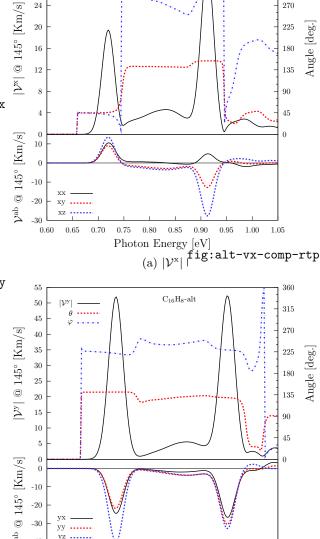


FIG. 3. $|\mathcal{V}^{x}|$ response for $C_{16}H_{8}$ -alt structure. The maximum response zone is localized for an energy range from $0.90 \,\mathrm{eV}$ to $0.93 \,\mathrm{eV}$ and for a polarization angle of the incoming beam from 120° to 150°_{15} alt-3d

response for both, $|\mathcal{V}^x|$ and $|\mathcal{V}^y|$ is kept. We also found that the absolute maximum of the response is obtained when the energy of the incoming bean is 0.912 eV and the polarization angle is $\alpha = 145^{\circ}$. In the top frames of Figs. 4(a) and 4(b) we present the results for $|\mathcal{V}^{x}|$ and $|\mathcal{V}^{y}|$ (left scale) fixing the polarization angle to 145° for the alt structure vs the photon energy and the corresponding polar φ and azimuthal θ angles (right scale). Also in the bottom frames of Figs. 4(a) and 4(b) we present the decomposition of $|\mathcal{V}^{x}|$ and $|\mathcal{V}^{y}|$ in the corresponding components \mathcal{V}^{xx} , \mathcal{V}^{xy} , \mathcal{V}^{xz} and \mathcal{V}^{yx} , \mathcal{V}^{yy} \mathcal{V}^{yz} with α fixed to 145°. Making the analysis for the components and angles for $|\mathcal{V}^{x}|$ depicted in Fig. 4(a) we can see that for an incoming beam energy of 0.720 eV the components contributions are similar having values of $V^{xx} = 10.5 \,\mathrm{Km/s}$, $\mathcal{V}^{xy} = 9.1 \,\mathrm{Km/s}$, and $\mathcal{V}^{xz} = 13.5 \,\mathrm{Km/s}$ resulting in a total spin-velocity $|\mathcal{V}^x| = 19.4 \,\mathrm{Km/s}$ and spin polar and azimuthal angles $\varphi = 45.8^{\circ}$ and $\theta = 40.7^{\circ}$, respectively. In the other hand, for an energy of the incoming beam equal to 0.912 eV we found that the contribution of the compo-



 $C_{16}H_8$ -alt

28

FIG. 4. Most intense responses of $|\mathcal{V}^x|$ and $|\mathcal{V}^y|$ and the corresponding three components for the *alt* structure. Both maxima where obtained for a polarization angle $\alpha = 145^{\circ}$.

0.80

0.85

 $\begin{array}{c} {\rm Photon\; Energy\; [eV]} \\ {\rm (b)\; |\mathcal{V}^y|} \end{array} \\ {\rm fig:alt-vy-comp-rtp} \\$

0.65

0.60

nents are $V^{xx} = 4.8 \,\mathrm{Km/s}$ $V^{xy} = -12.8 \,\mathrm{Km/s}$, and $V^{xz} = -27.7 \,\mathrm{Km/s}$ having a mayor response coming from the xz component and resulting in a spin- velocity magnitude $|V^x| = 30.9 \,\mathrm{Km/s}$ being this the absolute maximum fixing the spin-velocity in the x direction. Then, the components give us polar and azimuthal angles with

values of $\varphi = 153.8^{\circ}$ and $\theta = 290.4^{\circ}$. This angles and its variation with the incoming energy beam are presented in the right scale of the top frame of Fig 4(a). Finally we have that since the onset of the response till an energy of the incoming bean of $0.744\,\mathrm{eV}$ the three components of $|\mathcal{V}^{\mathrm{x}}|$ are positive while for the range from 0.746 eV to $0.886\,\mathrm{eV}$ the \mathcal{V}^xx component is positive but the \mathcal{V}^{xy} and \mathcal{V}^{xz} components change in direction. This is due to a change in the spin polarization direction. Finally after the energy value of 0.886 eV the response decreases and goes to zero. Making now the analysis for $|\mathcal{V}^{y}|$ depicted in Fig. 4(b) we have that for an incoming energy beam of $0.720\,\mathrm{eV}$ the yz component have a major contribution than the yx and yy components having values of $V^{yx} = -24.6 \,\mathrm{Km/s}$, $\mathcal{V}^{yy} = -21.8 \,\mathrm{Km/s}$, and $\mathcal{V}^{yz} = -40.2 \,\mathrm{Km/s}$ resulting in a total spin-velocity $|\mathcal{V}^{y}| = 51.9 \,\mathrm{Km/s}$ and spin polar and azimuthal angles $\varphi = 140.7^{\circ}$ and $\theta = 221.6^{\circ}$, respectively. Also, for an energy of the incoming beam of 0.912 eV we found that the contribution of the components are $\mathcal{V}^{xx} = -26.7 \,\mathrm{Km/s} \,\mathcal{V}^{xy} = -30.6 \,\mathrm{Km/s}, \text{ and}$ $\mathcal{V}^{xz} = -32.9 \,\mathrm{Km/s}$ having all the three components similar contributions and resulting in a spin- velocity magnitude $|\mathcal{V}^{y}| = 52.3 \,\mathrm{Km/s}$ being this the absolute maximum spin-velocity for the velocity fixed to the y direction and being 1.7 times more intense than the maximum of $|\mathcal{V}^{x}|$. The components then give us the polar and azimuthal angles with values of $\varphi = 129.0^{\circ}$ and $\theta = 228.9^{\circ}$, respectively. This angles and the corresponding variation is presented in the right sale of the top frame of Fig. 4(b). We also have that the three components of $|\mathcal{V}^{y}|$ are negative keeping the same spin polarization since the onset of the response to a energy of the incoming beam of 0.886 eV when the response decreases and goes to zero. From the bottom frames of Fig. 4 we can see that for the alt structure the most intense component of $|\mathcal{V}^{x}|$ and $|\mathcal{V}^{y}|$ corresponds to V^{yz} which has a value of -40.2 Km/s for an energy incident beam of 0.72 eV. This component and the corresponding layer by layer contribution is depicted in Fig. 5. From this figure we have that for the energy range from 0.70 eV to 0.74 eV the fifth and sixth layers corresponding to the bottom carbon and hydrogen num-

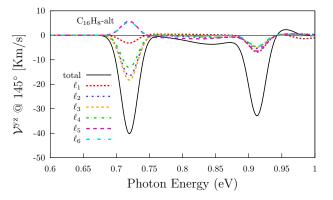
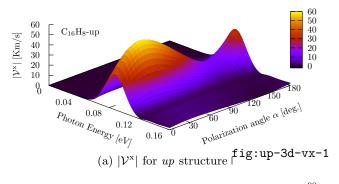


FIG. 5. Layer-by-layer contribution of V^{yz} for the *alt* structure. fig:alt-vyz-lay



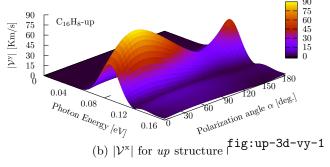


FIG. 6. $|\mathcal{V}^{x}|$ response for $C_{16}H_8$ -up structure. The maximum response zone is localized for an energy range from $0.04\,\mathrm{eV}$ to $0.12\,\mathrm{eV}$ and for a polarization angle of the incoming beam from 25° to 150° : up-3d-1

bered with 5 and 6 in Fig. 1 have contributions in opposite direction than the other 4 layers resulting in a total response $\mathcal{V}^{yz} = -40.2 \,\mathrm{Km/s}$ for an incoming beam energy of $0.72 \,\mathrm{eV}$. In the other hand, for the energy range from $0.88 \,\mathrm{eV}$ to $0.95 \,\mathrm{eV}$ the response for the all six layers the responses are in the same direction resulting in a total response $\mathcal{V}^{yz} = -32.89 \,\mathrm{Km/s}$ for an incoming beam with energy of $0.912 \,\mathrm{eV}$.

Up structure.

6

40

30

20

10

Polarization angle α [deg.]

Polarization angle α [deg.]

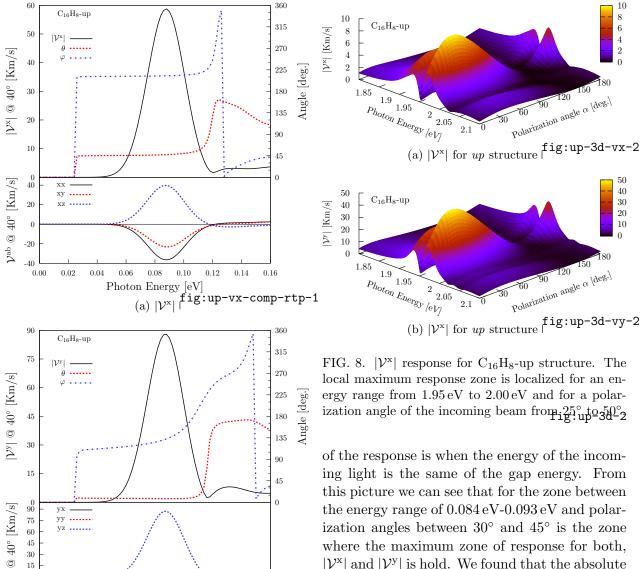


FIG. 7. Most intense responses of $|\mathcal{V}^{x}|$ and $|\mathcal{V}^{y}|$ and the corresponding three components for the up structure. Both maxima where obtained for a polarization angle $\alpha = 40^{\circ}$. fig:up-vab-comp-rtp-1

0.08

0.10

0.12

Photon Energy [eV] (b) $|\mathcal{V}^y|$ fig:up-vy-comp-rtp-1

0.14

0.06

60 45

30

15 $\gamma_{
m ap}$ 0

-15

0.00

0.02

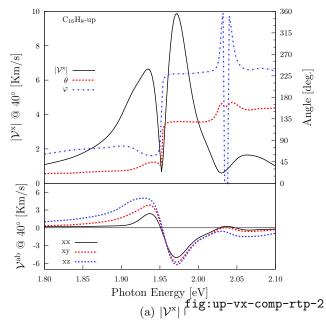
0.04

For the *up* structure we first analyzed the energy range from 0.00 eV to 0.16 eV where we found the most intense response for \mathcal{V}^{x} and $|\mathcal{V}^{y}|$. In Fig. 6 we present the V^a spectra resulting from evaluate again Eq. (7) using different polarization angles α in Eq. (3) but now for the $C_{16}H_8$ -up structure. We can see that the onset

FIG. 8. $|\mathcal{V}^{x}|$ response for $C_{16}H_{8}$ -up structure. The local maximum response zone is localized for an energy range from 1.95 eV to 2.00 eV and for a polarization angle of the incoming beam from 25° up 30° 2

of the response is when the energy of the incoming light is the same of the gap energy. From this picture we can see that for the zone between the energy range of 0.084 eV-0.093 eV and polarization angles between 30° and 45° is the zone where the maximum zone of response for both, $|\mathcal{V}^{x}|$ and $|\mathcal{V}^{y}|$ is hold. We found that the absolute maximum of the response is obtained when the polarization angle is $\alpha = 40^{\circ}$ and the energy of the incoming beam is 0.088 eV. In the top frames of Figs. 7(a) and 7(b) we present the results of $|\mathcal{V}^{x}|$ and $|\mathcal{V}^{y}|$ (left scale) fixing the polarization angle to $\alpha = 40^{\circ}$ for the up structure vs photon energy and the corresponding polar φ and azimuthal θ angles (right scale). In the bottom frames of same figures we present the decomposition of $|\mathcal{V}^{x}|$ and $|\mathcal{V}^{y}|$ in the corresponding \mathcal{V}^{xx} , \mathcal{V}^{xy} , \mathcal{V}^{xz} , and \mathcal{V}^{yx} , \mathcal{V}^{yy} , \mathcal{V}^{yz} components with α fixed to 40° .

From Fig. 7(a) we have that for an incoming bean with energy of 0.088 eV the three components have similar contributions and have values of $\mathcal{V}^{xx} = -36.5 \,\mathrm{Km/s}$, $\mathcal{V}^{xy} = -23.2 \,\mathrm{Km/s}$, and $V^{xz} = 39.8 \,\mathrm{Km/s}$ resulting in a value of



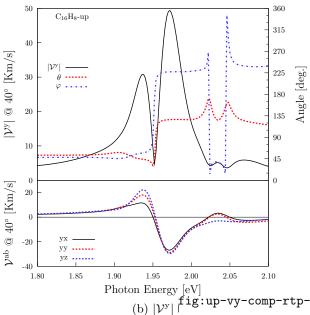
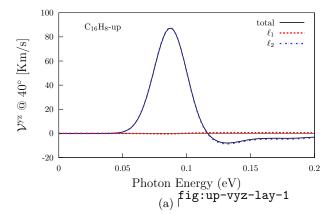


FIG. 9. Intense responses of $|\mathcal{V}^{x}|$ and $|\mathcal{V}^{y}|$ and the corresponding three components for the up structure. Both maxima where obtained for a polarization angle $\alpha = 40^{\circ}$. fig:up-vab-comp-rtp-2

 $|\mathcal{V}^{x}| = 58.7 \,\mathrm{Km/s}$ being this value the absolute maximum obtained when the spin-velocity is fixed in the x direction. To this value corresponds a polar and azimuthal angles of $\varphi = 47.4$ and $\theta = 212.5$, respectively. Now, from Fig. 7(b) we have that the yx and yy components have less contributions for the total response than the yzand for the same incoming beam energy have

values of $V^{yx} = -7.9 \,\mathrm{Km/s} \,V^{yy} = 8.6 \,\mathrm{Km/s}$, and $V^{yz} = 87.2 \,\mathrm{Km/s}$ resulting in a value of the total response of $|\mathcal{V}^{y}| = 87.9 \,\mathrm{Km/s}$ being this value the absolute maximum obtained when the spinvelocity is fixed in the y direction and being 1.5 times more intense than $|\mathcal{V}^{x}|$ and corresponding spin polar and azimuthal angles $\varphi = 7.6$ $\theta = 132.7$, respectively. We also found that since the onset of the response till an energy for the incoming beam of 0.118 eV the components of both, $|\mathcal{V}^{x}|$ and $|\mathcal{V}^{y}|$ have no change in the spin polarization direction. Finally, after this energy value both goes to zero. Also there is another energy range of interest for an incoming energy beam from 1.80 eV to 2.10 eV presented in Fig. 8 where two local maxima of $|\mathcal{V}^x|$ and fig:up-vx-comp-rtp-2 $|\mathcal{V}^{y}|$ are obtained for the up structure resulting from evaluate Eqns. (7) and (3). From this figure we have that for the zone between the energy ranges from 1.92 eV to 1.94 eV and from $1.96\,\mathrm{eV}$ to $1.98\,\mathrm{eV}$ and angles from 30° to 45° those maxima zones are hold. We found that the maxima are obtained when the polarization angle is fixed to 40° and the corresponding energies are 1.934 eV and 1.972 eV. Again, in the top frames of Figs. 9(a) and 9(b) we present the results of $|\mathcal{V}^{x}|$ and $|\mathcal{V}^{y}|$ (left scale) fixing the polarization angle to $\alpha = 40^{\circ}$ vs the photon energy and the corresponding polar φ and azimuthal θ angles (right scale) for the up structure. In the bottom frames of same figures we present the three components xx, xy, xz, and yx, yy, yz corresponding to $|\mathcal{V}^{x}|$ and $|\mathcal{V}^{y}|$ fixing the polarization angle to 40°. We found that Photon Energy [eV] the polarization angle to 40°. We found that (b) $|\mathcal{V}^{y}|$ fig:up-vy-comp-rtp-2 for both cases, $|\mathcal{V}^{x}|$ and $|\mathcal{V}^{y}|$, the corresponding components have similar contributions and for an incoming energy beam of 1.934 eV have values of $V^{xx} = 2.3 \,\mathrm{Km/s}$, $V^{xy} = 3.8 \,\mathrm{Km/s}$, $\mathcal{V}^{xz} = 4.9 \,\mathrm{Km/s}$, and $\mathcal{V}^{yx} = 11.5 \,\mathrm{Km/s}$, $\mathcal{V}^{yy} =$ $17.0 \,\mathrm{Km/s}, \,\mathcal{V}^{\mathrm{yz}} = 20.4 \,\mathrm{Km/s}$ resulting in a in values of $|\mathcal{V}^{x}| = 6.6 \,\mathrm{Km/s} \,|\mathcal{V}^{y}| = 28.7 \,\mathrm{Km/s}$ being $|\mathcal{V}^{y}|$ 4.3 times more intense than $|\mathcal{V}^{x}|$ for this photon energy. The responses have polar and azimuthal spin polarization angels $\varphi = 42.0^{\circ}$ and $\theta = 58.7^{\circ}$ for $|\mathcal{V}^{x}|$ and $\varphi = 45.2^{\circ}$ and $\theta = 56.0^{\circ}$ for $|\mathcal{V}^{y}|$. Alike, for an incoming energy beam of 1.972 eV all the components of $|\mathcal{V}^{x}|$ and $|\mathcal{V}^{y}|$ have similar contributions having values of $\mathcal{V}^{xx} = -5.0 \,\mathrm{Km/s}$, $\mathcal{V}^{xy} = -5.8 \,\mathrm{Km/s}$,



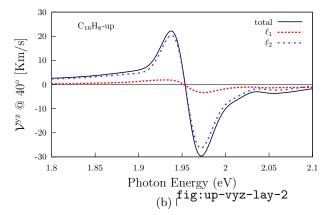


FIG. 10. Layer-by-layer contribution of \mathcal{V}^{yz} for the up structure. fig:up-vyz-lay

 $\mathcal{V}^{xz} = -6.2 \,\mathrm{Km/s}$, and $\mathcal{V}^{yx} = -26.8 \,\mathrm{Km/s}$, $\mathcal{V}^{yy} = -28.9 \,\mathrm{Km/s}$, $\mathcal{V}^{yz} = -29.7 \,\mathrm{Km/s}$ result-

ing in a in values of $|\mathcal{V}^x| = 9.9 \,\mathrm{Km/s} \,|\mathcal{V}^y| =$ $49.4 \,\mathrm{Km/s}$ being $|\mathcal{V}^{\mathrm{y}}| 5.0$ times more intense than $|\mathcal{V}^{x}|$ for this photon energy. The responses have polar and azimuthal spin polarization angles $\varphi =$ $129.0^{\circ} \theta = 229.1^{\circ} \text{ or } |\mathcal{V}^{x}| \text{ and } \varphi = 127.0^{\circ} \text{ and }$ $\theta = 227.1^{\circ}$ for $|\mathcal{V}^{y}|$. Finally we have that all the tree components of $|\mathcal{V}^{x}|$ and $|\mathcal{V}^{y}|$ keep the spin polarization positive till an energy of the incoming beam equal to 1.954 eV when the spin polarization changes the direction and after an energy for the incoming beam equal to 2.05 eV both responses goes to zero. From the bottom frames of Figs. 7 and 9 we can see that for the up structure again the most intense component of $|\mathcal{V}^{x}|$ and $|\mathcal{V}^{y}|$ corresponds to \mathcal{V}^{yz} which has a value of 87.2 Km/s for an energy incident beam of 0.088 eV and -29.7 Km/s for an energy incident beam of 1.972 eV. This component and the corresponding layer by layer contribution is depicted in Fig. 10s. From this figure we have that for the energy range from 0 eV to 0.2 eV the response comes from the second layer composed by carbon atoms presented in Tab. II and denoted by the number 2 in Fig. 2. In the other hand, the response for the energy range from 1.8 eV to 2.1 eV almost all the response comes from the carbon atoms having a leaser contribution from the hydrogen layer.

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