

Introduction to Econometrics

pp. 331-386

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Instrumental Variables Regression

Chapter 7 discussed several problems, including omitted variables, errors-in-variables, and simultaneous causality, that make the error term correlated with the regressor. Omitted variable bias can be addressed directly by including the omitted variable in a multiple regression, but this is only feasible if you have data on the omitted variable. And sometimes, such as when causality runs *both* from X to Y and from Y to X , so that there is simultaneous causality bias, multiple regression simply cannot eliminate the bias. If a direct solution to these problems is either infeasible or unavailable, then a new method is required.

Instrumental variables (IV) regression is a general way to obtain a consistent estimator of the unknown coefficients of the population regression function when the regressor, X , is correlated with the error term, u . To understand how IV regression works, think of the variation in X as having two parts: one part that, for whatever reason, is correlated with u (this is the part that causes the problems), and a second part that is uncorrelated with u . If you had information that allowed you to isolate the second part, then you could focus on those variations in X that are uncorrelated with u and disregard the variations in X that bias the OLS estimates. This is, in fact, what IV regression does. The information about the movements in X that are uncorrelated with u is gleaned from one or more additional variables, called **instrumental variables** or simply **instruments**. Instrumental variables regression uses these additional variables as tools or “instruments” to isolate the movements in X that are uncorrelated with u , which in turn permit consistent estimation of the regression coefficients.

The first two sections of this chapter describe the mechanics and assumptions of IV regression: why IV regression works, what is a valid instrument, and how to implement and to interpret the most common IV regression method, two stage least squares. The key to successful empirical analysis using instrumental variables is finding valid instruments, and Section 10.3 takes up the question of how to assess whether a set of instruments is valid. As an illustration, Section 10.4 uses IV regression to estimate the elasticity of demand for cigarettes. Finally, Section 10.5 turns to the difficult question of where valid instruments come from in the first place.

10.1 The IV Estimator with a Single Regressor and a Single Instrument

We start with the case of a single regressor, X , which might be correlated with the regression error, u . If X and u are correlated, then the OLS estimator is inconsistent, that is, it may not be close to the true value of the regression coefficient even when the sample is very large (see Equation (5.1)). As discussed in Section 7.2, this correlation between X and u can stem from various sources, including omitted variables, errors in variables (measurement errors in the regressors), or simultaneous causality (when causality runs “backwards” from Y to X as well as “forwards” from X to Y). Whatever the source of the correlation between X and u , if there is a valid instrumental variable, Z , then the effect on Y of a unit change in X can be estimated using the instrumental variables estimator.

The IV Model and Assumptions

The population regression model relating the dependent variable Y_i and regressor X_i is

$$Y_i = \beta_0 + \beta_1 X_i + u_i, \quad i = 1, \dots, n, \quad (10.1)$$

where as usual u_i is the error term representing omitted factors that determine Y_i . If X_i and u_i are correlated, the OLS estimator is inconsistent. Instrumental variables estimation uses an additional, “instrumental” variable Z to isolate that part of X that is uncorrelated with u_i .

Endogeneity and exogeneity. Instrumental variables regression has some specialized terminology to distinguish variables that are correlated with the population error term u from ones that are not. Variables correlated with the error term are called **endogenous** variables, while variables uncorrelated with the error term are called **exogenous** variables. The historical source of these terms traces to models with multiple equations, in which an “endogenous” variable is determined within the model while an “exogenous” variable is determined outside the model. For example, Section 7.2 considered the possibility that, if low test scores produced decreases in the student-teacher ratio because of political intervention and increased funding, then causality would run *both* from the student-teacher ratio to test scores *and* from test scores to the student-teacher ratio. This was represented mathematically as a system of two simultaneous equations (Equations (7.3) and (7.4)), one for each causal connection. As discussed in Section 7.2, because both test scores and the student-teacher ratio are determined within the model, both are correlated with the population error term u ; that is, in this example, both variables are endogenous. In contrast, an exogenous variable, which is determined outside the model, is uncorrelated with u .

The two conditions for a valid instrument. A valid instrumental variable (“instrument”) must satisfy two conditions, known as **instrument relevance** and **instrument exogeneity**:

1. **Instrument Relevance:** $\text{corr}(Z_i, X_i) \neq 0$.
2. **Instrument Exogeneity:** $\text{corr}(Z_i, u_i) = 0$.

If an instrument is relevant, then variation in the instrument is related to variation in X_i . If in addition the instrument is exogenous, then that part of the variation of X_i captured by the instrumental variable is exogenous. Thus, an instrument that is relevant and exogenous can capture movements in X_i that are exogenous. This exogenous variation can in turn be used to estimate the population coefficient β_1 .

The two conditions for a valid instrument are vital for instrumental variables regression, and we return to them (and a version of them relevant for multiple regressors and multiple instruments) repeatedly throughout this chapter.

The Two Stage Least Squares Estimator

If the instrument Z satisfies the conditions of instrument relevance and exogeneity, then the coefficient β_1 can be estimated using an IV estimator called **two stage least squares** (TSLS). As the name suggests, the two stage least squares estimator is calculated in two stages. The first stage decomposes X into two components: a

problematic component that may be correlated with the regression error, and another problem-free component that is uncorrelated with the error. The second stage uses the problem-free component to estimate β_1 .

The first stage begins with a population regression linking X and Z :

$$X_i = \pi_0 + \pi_1 Z_i + v_i, \quad (10.2)$$

where π_0 is the intercept, π_1 is the slope, and v_i is the error term. This regression provides the needed decomposition of X_i . One component is $\pi_0 + \pi_1 Z_i$, the part of X_i that can be predicted by Z_i . Because Z_i is exogenous, this component of X_i is uncorrelated with u_i , the error term in Equation (10.1). The other component of X_i is v_i , which is the problematic component of X_i that is correlated with u_i .

The idea behind TSLS is to use the problem-free component of X_i , $\pi_0 + \pi_1 Z_i$, and to disregard v_i . The only complication is that the values of π_0 and π_1 are unknown, so $\pi_0 + \pi_1 Z_i$ cannot be calculated. Accordingly, the first stage of TSLS applies OLS to Equation (10.2) and uses the predicted value from the OLS regression, $\hat{X}_i = \hat{\pi}_0 + \hat{\pi}_1 Z_i$, where $\hat{\pi}_0$ and $\hat{\pi}_1$ are the OLS estimates.

The second stage of TSLS is easy: regress Y_i on \hat{X}_i using OLS. The resulting estimators from the second stage regression are the TSLS estimators, $\hat{\beta}_0^{TSLS}$ and $\hat{\beta}_1^{TSLS}$.

Why Does IV Regression Work?

Two examples provide some intuition for why IV regression solves the problem of correlation between X_i and u_i .

Example #1: Philip Wright's problem. The method of instrumental variables estimation was first published in 1928 in an appendix to a book written by Philip G. Wright (Wright, 1928); this appendix is thought to have been written with or by his son, Sewall Wright, an important statistician. Philip Wright was concerned with an important economic problem of his day: how to set an import tariff (a tax on imported goods) on animal and vegetable oils and fats, such as butter and soy oil. In the 1920s, import tariffs were a major source of tax revenue for the United States. The key to understanding the economic effect of a tariff was having quantitative estimates of the demand and supply curves of the goods. Recall that the supply elasticity is the percentage change in the quantity supplied arising from a 1% increase in the price, and the demand elasticity is the percentage change in the quantity demanded arising from a 1% increase in the price. Philip Wright needed estimates of these elasticities of supply and demand.

To be concrete, consider the problem of estimating the elasticity of demand for butter. Recall from Key Concept 6.2 that the coefficient in a linear equation relating $\ln(Y_i)$ to $\ln(X_i)$ has the interpretation of the elasticity of Y with respect to X . In the Wrights' problem, this suggests the demand equation

$$\ln(Q_i^{\text{butter}}) = \beta_0 + \beta_1 \ln(P_i^{\text{butter}}) + u_i, \quad (10.3)$$

where Q_i^{butter} is the i^{th} observation on the quantity of butter consumed, P_i^{butter} is its price, and u_i represents other factors that affect demand, such as income and consumer tastes. In Equation (10.3), a 1% increase in the price of butter yields a β_1 percent change in demand, so β_1 is the demand elasticity.

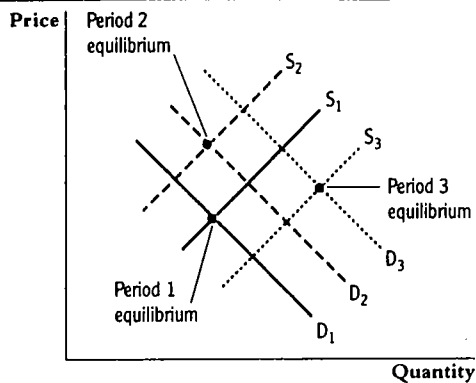
The Wrights had data on total annual butter consumption and its average annual price in the United States for 1912 to 1922. It would have been easy to use these data to estimate the demand elasticity by applying OLS to Equation (10.3), but they had a key insight: because of the interactions between supply and demand, the regressor, $\ln(P_i^{\text{butter}})$, was likely to be correlated with the error term.

To see this, look at Figure 10.1a, which shows the market demand and supply curves for butter for three different years. The demand and supply curves for the first period are denoted D_1 and S_1 , and the first period's equilibrium price and quantity are determined by their intersection. In year two, demand increases from D_1 to D_2 (say, because of an increase in income) and supply decreases from S_1 to S_2 (because of an increase in the cost of producing butter); the equilibrium price and quantity are determined by the intersection of the new supply and demand curves. In year three, the factors affecting demand and supply change again; demand increases again to D_3 , supply increases to S_3 , and a new equilibrium quantity and price are determined. Figure 10.1b shows the equilibrium quantity and price pairs for these three periods and for eight subsequent years, where in each year the supply and demand curves are subject to shifts associated with factors other than price that affect market supply and demand. This scatterplot is like the one that the Wrights would have seen when they plotted their data. As they reasoned, fitting a line to these points by OLS will estimate neither a demand curve nor a supply curve, because the points have been determined by changes in both demand and supply.

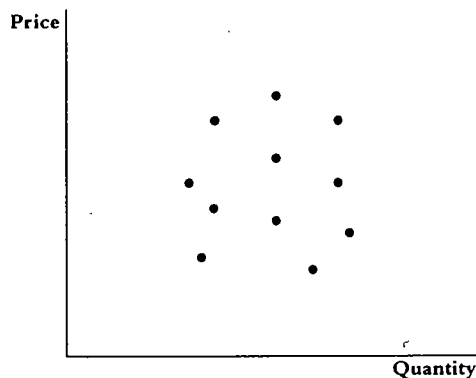
The Wrights realized that a way to get around this problem was to find some third variable that shifted supply but did not shift demand. Figure 10.1c shows what happens when such a variable shifts the supply curve, but demand remains stable. Now all of the equilibrium price and quantity pairs lie on a stable demand curve, and the slope of the demand curve is easily estimated. In the instrumental variable formulation of Wright's problem, this third variable—the instrumental

FIGURE 10.1

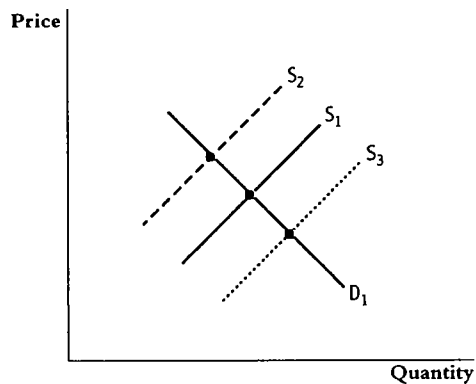
(a) Price and quantity are determined by the intersection of the supply and demand curves. The equilibrium in the first period is determined by the intersection of the demand curve D_1 and the supply curve S_1 . Equilibrium in the second period is the intersection of D_2 and S_2 , and equilibrium in the third period is the intersection of D_3 and S_3 .

**(a) Demand and Supply in Three Time Periods**

(b) This scatterplot shows equilibrium price and quantity in eleven different time periods. The demand and supply curves are hidden. Can you determine the demand and supply curves from the points on the scatterplot?

**(b) Equilibrium Price and Quantity for Eleven Time Periods**

(c) When the supply curve shifts from S_1 to S_2 to S_3 but the demand curve remains at D_1 , the equilibrium prices and quantities trace out the demand curve.

**(c) Equilibrium Price and Quantity When Only the Supply Curve Shifts**

variable—is correlated with price (it shifts the supply curve, which leads to a change in price) but is uncorrelated with u (the demand curve remains stable). The Wrights discussed several potential instrumental variables; one was the weather. For example, below-average rainfall in a dairy region could impair grazing and thus reduce butter production at a given price (it would shift the supply curve to the left and increase the equilibrium price), so dairy-region rainfall satisfies the condition for instrument relevance. But dairy-region rainfall should not have a direct influence on the demand for butter, so the correlation between dairy-region rainfall and u_i would be zero; that is, dairy-region rainfall satisfies the condition for instrument exogeneity.

Example #2: Estimating the effect on test scores of class size. Despite controlling for student and district characteristics, the estimates of the effect on test scores of class size reported in Part II still might have omitted variables bias resulting from unmeasured variables such as learning opportunities outside school or the quality of the teachers. If data on these variables are unavailable, this omitted variables bias cannot be addressed by including the variables in the multiple regressions.

Instrumental variables regression provides an alternative approach to this problem. Consider the following hypothetical example: some California schools are forced to close for repairs because of a summer earthquake. Districts close to the epicenter are most severely affected. A district with some closed schools needs to “double up” their students, temporarily increasing class size. This means that distance from the epicenter satisfies the condition for instrument relevance because it is correlated with class size. But if distance to the epicenter is unrelated to any of the other factors affecting student performance (such as whether the students are still learning English), then it will be exogenous because it is uncorrelated with the error term. Thus the instrumental variable, distance to the epicenter, could be used to circumvent omitted variables bias and to estimate the effect of class size on test scores.

The Sampling Distribution of the TSLS Estimator

The exact distribution of the TSLS estimator in small samples is complicated. However, like the OLS estimator, its distribution in large samples is simple: the TSLS estimator is consistent and is normally distributed.

Formula for the TSLS estimator. Although the two stages of TSLS make the estimator seem complicated, when there is a single X and a single instrument Z , as we assume in this section, there is a simple formula for the TSLS estimator.

Let s_{ZY} be the sample covariance between Z and Y and let s_{ZX} be the sample covariance between Z and X . As shown in Appendix 10.2, the TSLS estimator with a single instrument is

$$\hat{\beta}_1^{TSLs} = \frac{s_{ZY}}{s_{ZX}}. \quad (10.4)$$

That is, the TSLS estimator of β_1 is the ratio of the sample covariance between Z and Y to the sample covariance between Z and X .

Sampling distribution of $\hat{\beta}_1^{TSLs}$ when the sample size is large. The formula in Equation (10.4) can be used to show that $\hat{\beta}_1^{TSLs}$ is consistent and, in large samples, normally distributed. The argument is summarized here, with mathematical details given in Appendix 10.3.

The argument that $\hat{\beta}_1^{TSLs}$ is consistent combines the assumptions that Z_i is relevant and exogenous with the consistency of sample covariances for population covariances. To begin, note that because $Y_i = \beta_0 + \beta_1 X_i + u_i$ in Equation (10.1),

$$\text{cov}(Z_i, Y_i) = \text{cov}(Z_i, \beta_0 + \beta_1 X_i + u_i) = \beta_1 \text{cov}(Z_i, X_i) + \text{cov}(Z_i, u_i), \quad (10.5)$$

where the second equality follows from the properties of covariances (Equation (2.33)). By the instrument exogeneity assumption, $\text{cov}(Z_i, u_i) = 0$, and by the instrument relevance assumption, $\text{cov}(Z_i, X_i) \neq 0$. Thus, if the instrument is valid,

$$\beta_1 = \frac{\text{cov}(Z_i, Y_i)}{\text{cov}(Z_i, X_i)}. \quad (10.6)$$

That is, the population coefficient β_1 is the ratio of the population covariance between Z and Y to the population covariance between Z and X .

As discussed in Section 3.6, the sample covariance is a consistent estimator of the population covariance, that is, $s_{ZY} \xrightarrow{p} \text{cov}(Z_i, Y_i)$ and $s_{ZX} \xrightarrow{p} \text{cov}(Z_i, X_i)$. It follows from Equations (10.4) and (10.6) that the TSLS estimator is consistent:

$$\hat{\beta}_1^{TSLs} = \frac{s_{ZY}}{s_{ZX}} \xrightarrow{p} \frac{\text{cov}(Z_i, Y_i)}{\text{cov}(Z_i, X_i)} = \beta_1. \quad (10.7)$$

The formula in Equation (10.4) also can be used to show that the sampling distribution of $\hat{\beta}_1^{TSLs}$ is normal in large samples. The reason is the same as for every other least squares estimator we have considered: the TSLS estimator is an average of random variables, and when the sample size is large the central limit

theorem tells us that averages of random variables are normally distributed. Specifically, the numerator of the expression for $\hat{\beta}_1^{TSLs}$ in Equation (10.4) is $s_{ZY} = \frac{1}{n-1} \sum_{i=1}^n (Z_i - \bar{Z})(Y_i - \bar{Y})$, an average of $(Z_i - \bar{Z})(Y_i - \bar{Y})$. A bit of algebra, sketched out in Appendix 10.3, shows that because of this averaging the central limit theorem implies that, in large samples, $\hat{\beta}_1^{TSLs}$ has a sampling distribution that is approximately $N(\beta_1, \sigma_{\hat{\beta}_1^{TSLs}}^2)$, where

$$\sigma_{\hat{\beta}_1^{TSLs}}^2 = \frac{1}{n} \frac{\text{var}[(Z_i - \mu_Z)u_i]}{[\text{cov}(Z_i, X_i)]^2}. \quad (10.8)$$

Statistical inference using the large-sample distribution. The variance $\sigma_{\hat{\beta}_1^{TSLs}}^2$ can be estimated by estimating the variance and covariance terms appearing in Equation (10.8), and the square root of the estimate of $\sigma_{\hat{\beta}_1^{TSLs}}^2$ is the standard error of the IV estimator. This is done automatically in TSLS regression commands in econometric software packages. Because $\hat{\beta}_1^{TSLs}$ is normally distributed in large samples, hypothesis tests about β_1 can be performed by computing the t -statistic, and a 95% large-sample confidence interval is given by $\hat{\beta}_1^{TSLs} \pm 1.96 SE(\hat{\beta}_1^{TSLs})$.

Application to the Demand for Cigarettes

The Wrights were interested in the demand elasticity of butter, but today other commodities, such as cigarettes, figure more prominently in public policy debates. One tool in the quest for reducing illnesses and deaths from smoking—and the costs, or externalities, imposed by those illnesses on the rest of society—is to tax cigarettes so heavily that current smokers cut back and potential new smokers are discouraged from taking up the habit. But precisely how big a tax hike is needed to make a dent in cigarette consumption? For example, what would the after-tax sales price of cigarettes need to be to achieve a 20% reduction in cigarette consumption?

The answer to this question depends on the elasticity of demand for cigarettes. If the elasticity is -1 , then the 20% target in consumption can be achieved by a 20% increase in price. If the elasticity is -0.5 , then the price must rise 40% to decrease consumption by 20%. Of course, we do not know what the demand elasticity of cigarettes is in the abstract: we must estimate it from data on prices and sales. But, as with butter, because of the interactions between supply and demand, the elasticity of demand for cigarettes cannot be estimated consistently by an OLS regression of log quantity on log price.

We therefore use TSLS to estimate the elasticity of demand for cigarettes using annual data for the 48 continental U.S. states for 1985–1995 (the data are described

in Appendix 10.1). For now, all the results are for the cross section of states in 1995; results using data for earlier years (panel data) are presented in Section 10.4.

The instrumental variable, $SalesTax_i$, is the portion of the tax on cigarettes arising from the general sales tax, measured in dollars per pack (in real dollars, deflated by the Consumer Price Index). Cigarette consumption ($Q_i^{cigarettes}$) is the number of packs of cigarettes sold per capita in the state, and the price, $P_i^{cigarettes}$, is the average real price per pack of cigarettes including all taxes.

Before using TSLS it is essential to ask whether the two conditions for instrument validity hold. We return to this topic in detail in Section 10.3, where we provide some statistical tools that help in this assessment. Even with those statistical tools, judgment plays an important role, so it is useful to think about whether the sales tax on cigarettes plausibly satisfies the two conditions.

First consider instrument relevance. Because a high sales tax increases the total sales price $P_i^{cigarettes}$, the sales tax per pack plausibly satisfies the condition for instrument relevance.

Next consider instrument exogeneity. For the sales tax to be exogenous, it must be uncorrelated with the error in the demand equation; that is, the sales tax must affect the demand for cigarettes only indirectly through the price. This seems plausible: general sales tax rates vary from state to state, but they do so mainly because different states choose different mixes of sales, income, property, and other taxes to finance public undertakings. Those choices about public finance are driven by political considerations, not by factors related to the demand for cigarettes. We discuss the credibility of this assumption more in Section 10.4, but for now we keep it as a working hypothesis.

In modern statistical software, the first stage of TSLS is estimated automatically so you do not need to run this regression yourself to compute the TSLS estimator. Just this once, however, we present the first-stage regression explicitly; using data for the 48 states in 1995, this is

$$\widehat{\ln(P_i^{cigarettes})} = 4.63 + 0.031 SalesTax_i \quad (10.9)$$

(0.03) (0.005)

The R^2 of this regression is 47%, so the variation in sales tax on cigarettes explains 47% of the variance of cigarette prices across states.

In the second stage of TSLS, $\ln(Q_i^{cigarettes})$ is regressed on $\widehat{\ln(P_i^{cigarettes})}$ using OLS. The resulting estimated regression function is

$$\widehat{\ln(Q_i^{cigarettes})} = 9.72 - 1.08 \widehat{\ln(P_i^{cigarettes})}. \quad (10.10)$$

This estimated regression function is written using the regressor in the second stage, the predicted value $\widehat{\ln(P_i^{\text{cigarettes}})}$. It is, however, conventional and less cumbersome simply to report the estimated regression function with $\ln(P_i^{\text{cigarettes}})$ rather than $\widehat{\ln(P_i^{\text{cigarettes}})}$. Reported in this notation, the TSLS estimates and heteroskedasticity-robust standard errors are

$$\widehat{\ln(Q_i^{\text{cigarettes}})} = 9.72 - 1.08\ln(P_i^{\text{cigarettes}}). \quad (10.11)$$

(1.53) (0.32)

The TSLS estimate suggests that the demand for cigarettes is surprisingly elastic, in light of their addictive nature: an increase in the price of 1% reduces consumption by 1.08%. But, recalling our discussion of instrument exogeneity, perhaps this estimate should not yet be taken too seriously. Even though the elasticity was estimated using an instrumental variable, there might still be omitted variables that are correlated with the sales tax per pack. A leading candidate is income: states with higher incomes might depend relatively less on a sales tax and more on an income tax to finance state government. Moreover, the demand for cigarettes presumably depends on income. Thus we would like to reestimate our demand equation including income as an additional regressor. To do so, however, we must first extend the IV regression model to include additional regressors.

10.2 The General IV Regression Model

The general IV regression model has four types of variables: the dependent variable, Y ; problematic endogenous regressors, like the price of cigarettes, which are potentially correlated with the error term and which we will label X ; additional regressors that are not correlated with the error term, called **included exogenous variables**, which we will label W ; and instrumental variables, Z . In general, there can be multiple endogenous regressors (X 's), multiple included exogenous regressors (W 's), and multiple instrumental variables (Z 's).

For IV regression to be possible, there must be at least as many instrumental variables (Z 's) as endogenous regressors (X 's). In Section 10.1, there was a single endogenous regressor and a single instrument. Having (at least) one instrument for this single endogenous regressor was essential. Without the instrument we could not have computed the instrumental variables estimator: there would be no first-stage regression in TSLS.



The General Instrumental Variables Regression Model and Terminology

The general IV regression model is

$$Y_i = \beta_0 + \beta_1 X_{1i} + \cdots + \beta_k X_{ki} + \beta_{k+1} W_{1i} + \cdots + \beta_{k+r} W_{ri} + u_i, \quad (10.12)$$

$i = 1, \dots, n$, where:

- Y_i is the dependent variable;
- u_i is the error term, which represents measurement error and/or omitted factors;
- X_{1i}, \dots, X_{ki} are k endogenous regressors, which are potentially correlated with u_i ;
- W_{1i}, \dots, W_{ri} are r included exogenous regressors, which are uncorrelated with u_i ;
- $\beta_0, \beta_1, \dots, \beta_{k+r}$ are unknown regression coefficients;
- Z_{1i}, \dots, Z_{mi} are m instrumental variables.

The coefficients are overidentified if there are more instruments than endogenous regressors ($m > k$); they are underidentified if $m < k$; and they are exactly identified if $m = k$. Estimation of the IV regression model requires exact identification or overidentification.

The relationship between the number of instruments and the number of endogenous regressors is sufficiently important to have its own terminology. The regression coefficients are said to be **exactly identified** if the number of instruments (m) equals the number of endogenous regressors (k), that is, $m = k$. The coefficients are **overidentified** if the number of instruments exceeds the number of endogenous regressors, that is, $m > k$; and they are **underidentified** if the number of instruments is less than the number of endogenous regressors, that is,

$m < k$. The coefficients must be either exactly identified or overidentified if they are to be estimated by IV regression.

The general IV regression model and its terminology is summarized in Key Concept 10.1.

TSLS in the General IV Model

TSLS with a single endogenous regressor. When there is a single endogenous regressor X and some additional included exogenous variables, the equation of interest is

$$Y_i = \beta_0 + \beta_1 X_i + \beta_2 W_{1i} + \cdots + \beta_{1+r} W_{ri} + u_i, \quad (10.13)$$

where, as before, X_i might be correlated with the error term, but W_{1i}, \dots, W_{ri} are not.

The population first-stage regression of TSLS relates X to the exogenous variables, that is, the W 's and the instruments Z :

$$X_i = \pi_0 + \pi_1 Z_{1i} + \cdots + \pi_m Z_{mi} + \pi_{m+1} W_{1i} + \cdots + \pi_{m+r} W_{ri} + v_i, \quad (10.14)$$

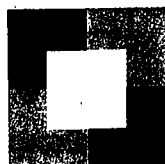
where $\pi_0, \pi_1, \dots, \pi_{m+r}$ are unknown regression coefficients and v_i is an error term.

Equation (10.14) is sometimes called the **reduced form** equation for X . It relates the endogenous variable X to all the available exogenous variables, both those included in the regression of interest (W) and the instruments (Z).

In the first stage of TSLS, the unknown coefficients in Equation (10.14) are estimated by OLS, and the predicted values from this regression are $\hat{X}_1, \dots, \hat{X}_n$.

In the second stage of TSLS, Equation (10.13) is estimated by OLS, except that X_i is replaced by its predicted values from the first stage. That is, Y_i is regressed on $\hat{X}_i, W_{1i}, \dots, W_{ri}$ using OLS. The resulting estimator of $\beta_0, \beta_1, \dots, \beta_{1+r}$ is the TSLS estimator.

Extension to multiple endogenous regressors. When there are multiple endogenous regressors X_{1i}, \dots, X_{ki} , the TSLS algorithm is similar, except that each endogenous regressor requires its own first-stage regression. Each of these first-stage regressions has the same form as Equation (10.14), that is, the dependent variable is one of the X 's and the regressors are all the instruments (Z 's) and all the included exogenous variables (W 's). Together, these first-stage regressions produce predicted values of each of the endogenous regressors.



Key Concept 10.2

Two Stage Least Squares

The TSLS estimator in the general IV regression model in Equation (10.12) with multiple instrumental variables is computed in two stages:

1. **First-stage regression(s):** Regress X_{1i} on the instrumental variables (Z_{1i}, \dots, Z_{mi}) and the included exogenous variables (W_{1i}, \dots, W_{ri}) using OLS. Compute the predicted values from this regression; call these \hat{X}_{1i} . Repeat this for all the endogenous regressors X_{2i}, \dots, X_{ki} , thereby computing the predicted values $\hat{X}_{1i}, \dots, \hat{X}_{ki}$.
2. **Second-stage regression:** Regress Y_i on the predicted values of the endogenous variables $(\hat{X}_{1i}, \dots, \hat{X}_{ki})$ and the included exogenous variables (W_{1i}, \dots, W_{ri}) using OLS. The TSLS estimators $\hat{\beta}_0^{TSLS}, \dots, \hat{\beta}_{k+r}^{TSLS}$ are the estimators from the second-stage regression.

In practice, the two stages are done automatically within TSLS estimation commands in modern econometric software.

In the second stage of TSLS, Equation (10.12) is estimated by OLS, except that the endogenous regressors (X 's) are replaced by their respective predicted values (\hat{X} 's). The resulting estimator of $\beta_0, \beta_1, \dots, \beta_{k+r}$ is the TSLS estimator.

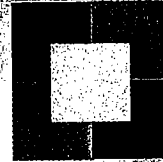
In practice, the two stages of TSLS are done automatically within TSLS estimation commands in modern econometric software. The general TSLS estimator is summarized in Key Concept 10.2.

Instrument Relevance and Exogeneity in the General IV Model

The conditions of instrument relevance and exogeneity need to be modified for the general IV regression model.

When there is one included endogenous variable but multiple instruments, the condition for instrument relevance is that at least one Z is useful for predicting X , given W . When there are multiple included endogenous variables, this condition is more complicated because we must rule out perfect multicollinearity in the population regression. Intuitively, when there are multiple included endogenous variables, the instruments must provide enough information about the exogenous movements in these variables to sort out their separate effects on Y .

The Two Conditions for Valid Instruments



Key Concept 10.3

A set of m instruments Z_{1i}, \dots, Z_{mi} must satisfy the following two conditions to be valid:

1. Instrument Relevance

- In general, let \hat{X}_{1i}^* be the predicted value of X_{1i} from the population regression of X_{1i} on the instruments (Z 's) and the included exogenous regressors (W 's), and let "1" denote a regressor that takes on the value "1" for all observations (its coefficient is the intercept). Then $(\hat{X}_{1i}^*, \dots, \hat{X}_{ki}^*, W_{1i}, \dots, W_{ni}, 1)$ are not perfectly multicollinear.
- If there is only one X , then at least one Z must enter the population regression of X on the Z 's and the W 's.

2. Instrument Exogeneity

The instruments are uncorrelated with the error term, that is,
 $\text{corr}(Z_{1i}, u_i) = 0, \dots, \text{corr}(Z_{mi}, u_i) = 0.$

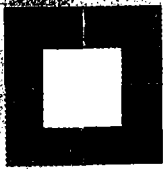
The general statement of the instrument exogeneity condition is that each instrument must be uncorrelated with the error term u_i . The general conditions for valid instruments are given in Key Concept 10.3.

The IV Regression Assumptions and Sampling Distribution of the TSLS Estimator

Under the IV regression assumptions, the TSLS estimator is consistent and has a sampling distribution that, in large samples, is approximately normal.

The IV regression assumptions. The IV regression assumptions are modifications of the least squares assumptions for the multiple regression model in Key Concept 5.4.

The first IV regression assumption modifies the conditional mean assumption in Key Concept 5.4 to apply to the included exogenous variables only. Just like the second least squares assumption for the multiple regression model, the second IV regression assumption is that the draws are i.i.d., as they are if the data are collected by simple random sampling. Similarly, the third IV assumption is that all



Key Concept 10.4

The IV Regression Assumptions

The variables and errors in the IV regression model in Key Concept 10.1 satisfy

1. $E(u_i | W_{1i}, \dots, W_{ri}) = 0$;
2. $(X_{1i}, \dots, X_{ki}, W_{1i}, \dots, W_{ri}, Z_{1i}, \dots, Z_{mi}, Y_i)$ are i.i.d. draws from their joint distribution;
3. The X 's, W 's, Z 's, and u all have nonzero, finite fourth moments;
4. The W 's are not perfectly multicollinear; and
5. The two conditions for a valid instrument in Key Concept 10.3 hold.

the variables have four moments, and the fourth IV regression assumption is that the included exogenous regressors are not perfectly multicollinear.

The fifth IV regression assumption is that the two conditions for instrument validity in Key Concept 10.3 hold. The IV regression assumptions are summarized in Key Concept 10.4.

Sampling distribution of the TSLS estimator. Under the IV regression assumptions, the TSLS estimator is consistent and normally distributed in large samples. This is shown in Section 10.1 (and Appendix 10.3) for the special case of a single endogenous regressor, a single instrument, and no included exogenous variables. Conceptually, the reasoning in Section 10.1 carries over to the general case of multiple instruments and multiple included endogenous variables. The expressions in the general case are complicated, however, and the reader is referred to Greene (2000, Chapter 9) for the details.

Inference Using the TSLS Estimator

Because the sampling distribution of the TSLS estimator is normal in large samples, the general procedures for statistical inference (hypothesis tests and confidence intervals) in regression models extend to TSLS regression. For example, 95% confidence intervals are constructed as the TSLS estimator ± 1.96 standard errors. Similarly, joint hypotheses about the population values of the coefficients can be tested using the F -statistic, as described in Section 5.7.

Calculation of TSLS standard errors. There are two points to bear in mind about TSLS standard errors. First, the standard errors reported by OLS estimation

of the second-stage regression are incorrect because they do not recognize that it is the second stage of a two-stage process. Specifically, the second-stage OLS standard errors fail to adjust for the fact that the second-stage regression uses the predicted values of the included endogenous variables. Formulas for standard errors that make the necessary adjustment are incorporated into (and automatically used by) TSLS regression commands in econometric software. Therefore this issue is not a concern in practice if you use a specialized TSLS regression command.

Second, as always the error u might be heteroskedastic. It is therefore important to use heteroskedasticity-robust versions of the standard errors, for precisely the same reason as it is important to use heteroskedasticity-robust standard errors for the OLS estimators of the multiple regression model.

Application to the Demand for Cigarettes

In Section 10.1, we estimated the elasticity of demand for cigarettes using data on annual consumption in 48 U.S. states in 1995 using TSLS with a single regressor (the logarithm of the real price per pack) and a single instrument (the real sales tax per pack). Income also affects demand, however, so it is part of the error term of the population regression. As discussed in Section 10.1, if the state sales tax is related to state income, then it is correlated with a variable in the error term of the cigarette demand equation, which violates the instrument exogeneity condition. If so, the IV estimator in Section 10.1 is inconsistent. That is, the IV regression suffers from a version of omitted variable bias. To solve this problem, we need to include income in the regression.

We therefore consider an alternative specification in which the logarithm of income is included in the demand equation. In the terminology of Key Concept 10.1, the dependent variable Y is the logarithm of consumption, $\ln(Q_i^{\text{cigarettes}})$; the endogenous regressor X is the logarithm of the real price, $\ln(P_i^{\text{cigarettes}})$; the included exogenous variable W is the logarithm of real per capita state income, $\ln(Inc_i)$; and the instrument Z is the real sales tax per pack, $SalesTax_i$. The TSLS estimates and (heteroskedasticity-robust) standard errors are

$$\widehat{\ln(Q_i^{\text{cigarettes}})} = 9.43 - 1.14\ln(P_i^{\text{cigarettes}}) + 0.21\ln(Inc_i). \quad (10.15)$$

(1.26) (0.37) (0.31)

This regression uses a single instrument, $SalesTax_i$, but in fact another candidate instrument is available. In addition to general sales taxes, states levy special taxes that apply only to cigarettes and other tobacco products. These cigarette-specific taxes ($CigTax_i$) constitute a possible second instrumental

variable. The cigarette-specific tax increases the price of cigarettes paid by the consumer, so it arguably meets the condition for instrument relevance. If it is uncorrelated with the error term in the state cigarette demand equation, it is an exogenous instrument.

With this additional instrument in hand, we now have two instrumental variables, the real sales tax per pack and the real state cigarette-specific tax per pack. With two instruments and a single endogenous regressor, the demand elasticity is overidentified, that is, the number of instruments ($SalesTax_i$ and $CigTax_i$, so $m = 2$) exceeds the number of included endogenous variables ($P_i^{cigarettes}$, so $k = 1$). We can estimate the demand elasticity using TSLS, where the regressors in the first-stage regression are the included exogenous variable, $\ln(Inc_i)$, and both instruments.

The resulting TSLS estimate of the regression function using the two instruments $SalesTax_i$ and $CigTax_i$ is

$$\widehat{\ln(Q_i^{cigarettes})} = 9.89 - 1.28\ln(P_i^{cigarettes}) + 0.28\ln(Inc_i). \quad (10.16)$$

(0.96) (0.25) (0.25)

Compare Equations (10.15) and (10.16): the standard error of the estimated price elasticity is smaller by one-third in Equation (10.16) (0.25 in Equation (10.16) versus 0.37 in Equation (10.15)). The reason the standard error is smaller in Equation (10.16) is that this estimate uses more information than Equation (10.15): in Equation (10.15), only one instrument is used (the sales tax), but in Equation (10.16), two instruments are used (the sales tax and the cigarette-specific tax). Using two instruments explains more of the variation in cigarette prices than using just one, and this is reflected in smaller standard errors on the estimated demand elasticity.

Are these estimates credible? Ultimately, credibility depends on whether the set of instrumental variables—here, the two taxes—plausibly satisfies the two conditions for valid instruments. It is therefore vital that we assess whether these instruments are valid, and it is to this topic that we now turn.

10.3 Checking Instrument Validity

Whether instrumental variables regression is useful in a given application hinges on whether the instruments are valid: invalid instruments produce meaningless results. It therefore is essential to assess whether a given set of instruments is valid in a particular application.

Assumption #1: Instrument Relevance

The role of the instrument relevance condition in IV regression is subtle. One way to think of instrument relevance is that it plays a role akin to the sample size: the more relevant the instruments—that is, the more the variation in X is explained by the instruments—the more information is available for use in IV regression. A more relevant instrument produces a more accurate estimator, just as a larger sample size produces a more accurate estimator. Moreover, statistical inference using TSLS is predicated on the TSLS estimator having a normal sampling distribution, but according to the central limit theorem the normal distribution is a good approximation in large—but not necessarily small—samples. If having a more relevant instrument is like having a larger sample size, this suggests that for the normal distribution to provide a good approximation to the sampling distribution of the TSLS estimator, the instruments should not just be relevant, but be highly relevant.

Instruments that explain little of the variation in X are called **weak instruments**. In the cigarette example, the distance of the state from cigarette manufacturing plants arguably would be a weak instrument: although a greater distance increases shipping costs (thus shifting the supply curve in and raising the equilibrium price), cigarettes are lightweight, so shipping costs are a small component of the price of cigarettes. Thus the amount of price variation explained by shipping costs, and thus distance to manufacturing plants, probably is quite small.

This section discusses why weak instruments are a problem, how to check for weak instruments, and what to do if you have weak instruments. It is assumed throughout that the instruments are exogenous.

Why weak instruments are a problem. If the instruments are weak, then the normal distribution provides a poor approximation to the sampling distribution of the TSLS estimator, even if the sample size is large. Thus there is no theoretical justification for the usual methods for performing statistical inference, even in large samples. In fact, if instruments are weak, then the TSLS estimator can be badly biased, and 95% confidence intervals constructed as the TSLS estimator ± 1.96 standard errors can contain the true value of the coefficient far less than 95% of the time. In short, if instruments are weak, TSLS is no longer reliable.

To see that there is a problem with the large-sample normal approximation to the sampling distribution of the TSLS estimator, consider the special case, considered in Section 10.1, of a single included endogenous variable, a single instrument, and no included exogenous regressor. If the instrument is valid, then $\hat{\beta}_1^{TSLS}$



Key Concept 10.5

A Rule of Thumb for Checking for Weak Instruments

The first-stage F -statistic is the F -statistic testing the hypothesis that the coefficients on the instruments Z_{1i}, \dots, Z_{mi} equal zero in the first stage of two stage least squares. When there is a single endogenous regressor, a first-stage F less than 10 indicates that the instruments are weak, in which case the TSLS estimator is biased (even in large samples), and TSLS t -statistics and confidence intervals are unreliable.

is consistent because the sample covariances s_{ZY} and s_{ZX} are consistent; that is, $\hat{\beta}_1^{TSLS} = s_{ZY}/s_{ZX} \xrightarrow{p} \text{cov}(Z_i, Y_i)/\text{cov}(Z_i, X_i) = \beta_1$ (Equation (10.7)). But now suppose that the instrument is not just weak but irrelevant, so that $\text{cov}(Z_i, X_i) = 0$. Then $s_{ZX} \xrightarrow{p} \text{cov}(Z_i, X_i) = 0$, so, taken literally, the denominator on the right-hand side of the limit $\text{cov}(Z_i, Y_i)/\text{cov}(Z_i, X_i)$ is zero! Clearly, the argument that $\hat{\beta}_1^{TSLS}$ is consistent breaks down when the instrument relevance condition fails. As shown in Appendix 10.4, this breakdown results in the TSLS estimator having a nonnormal sampling distribution, even if the sample size is very large. In fact, when the instrument is irrelevant, the large-sample distribution of $\hat{\beta}_1^{TSLS}$ is not that of a normal random variable, rather, it is the distribution of a *ratio* of two normal random variables!

While this circumstance of totally irrelevant instruments might not be encountered in practice, it raises a question: How relevant must the instruments be for the normal distribution to provide a good approximation in practice? The answer to this question in the general IV model is complicated. Fortunately, however, there is a simple rule of thumb available for the most common situation in practice, the case of a single endogenous regressor.

Checking for weak instruments when there is a single endogenous regressor. One way to check for weak instruments when there is a single endogenous regressor is to compute the F -statistic testing the hypothesis that the coefficients on the instruments are all zero in the first-stage regression of TSLS. This **first-stage F -statistic** provides a measure of the information content contained in the instruments: the more information content, the larger is the expected value of the F -statistic. One simple rule of thumb is that you do not need to worry about weak instruments if the first-stage F -statistic exceeds 10. (Why 10? See Appendix 10.4.) This is summarized in Key Concept 10.5.

A Scary Regression

One way to estimate the percentage increase in earnings from going to school for another year (the “return to education”) is to regress the logarithm of earnings against years of school using data on individuals. But if more able individuals are both more successful in the labor market and attend school longer (perhaps because they find it easier), then years of schooling will be correlated with the omitted variable, innate ability, and the OLS estimator of the return to education will be biased. Because innate ability is extremely difficult to measure and thus cannot be used as a regressor, some labor economists have turned to IV regression to estimate the return to education. But what variable is correlated with years of education but not the error term in the earnings regression—that is, what is a valid instrumental variable?

Your birthday, suggested labor economists Joshua Angrist and Alan Krueger. Because of mandatory schooling laws, they reasoned, your birthday is correlated with your years of education: if the law requires you to attend school until your 16th birthday and you turn 16 in January while you are in tenth grade, you might drop out—but if you turn 16 in July you already will have completed tenth grade. If so, your birthday satisfies the instrument relevance condition. But being born in January or July should have no *direct* effect on your earnings (other than through years of education), so your birthday satisfies the instrument exogeneity condition. They implemented this idea by using the individual’s quarter (three-month period) of birth as an instrumental variable. They used a very large sample of data from the U.S. Census (their regressions had at least 329,000 observations!), and they controlled for other variables such as the worker’s age.

But John Bound, another labor economist, was skeptical. He knew that weak instruments cause

TSLS to be unreliable and worried that, despite the extremely large sample size, the quarter of birth might be a weak instrument in some of their specifications. So when Bound and Krueger next met over lunch, the conversation inevitably turned to whether the Angrist-Krueger instruments were weak. Krueger thought not, and suggested a creative way to find out: why not rerun the regressions using a truly irrelevant instrument—replace each individual’s real quarter of birth by a fake quarter of birth, randomly generated by the computer—and compare the results using the real and fake instruments? What they found was amazing: it didn’t matter whether you used the real quarter of birth or the fake one as the instrument—TSLS gave basically the same answer!

This was a scary regression for labor econometricians. The TSLS standard error computed using the real data suggests that the return to education is precisely estimated—but so does the standard error computed using the fake data. Of course, the fake data *cannot* estimate the return to education precisely, because the fake instrument is totally irrelevant. The worry, then, is that the TSLS estimates based on the real data are just as unreliable as those based on the fake data.

The problem is that the instruments are in fact very weak in some of Angrist and Krueger’s regressions. In some of their specifications, the first-stage *F*-statistic is less than two, far less than the rule-of-thumb cutoff of 10. In other specifications, Angrist and Krueger have larger first-stage *F*-statistics, and in those cases the TSLS inferences are not subject to the problem of weak instruments. By the way, in those specifications the return to education is estimated to be approximately 8%, somewhat *greater* than estimated by OLS.¹

¹The original IV regressions are reported in Angrist and Krueger (1991), and the re-analysis using the fake instruments is published in Bound, Jaeger, and Baker (1995).

What do I do if I have weak instruments? It depends. If you have many instruments, then some of those instruments are probably weaker than others. If you have a small number of strong instruments and many weak ones, you will be better off to discard the weakest instruments and use the most relevant subset for your TSLS analysis. Your TSLS standard errors might increase when you drop weak instruments, but keep in mind that your original standard errors were not meaningful anyway!

If, however, you have only a few instruments or if the coefficients are exactly identified, then discarding weak instruments will not help. In this case, there are two recourses: find additional, stronger instruments, or use some advanced tools designed specifically for use with weak instruments. The first requires an intimate knowledge of the problem at hand and can entail redesigning the data set and the nature of the empirical study. The second requires procedures that are less sensitive to weak instruments than TSLS. One estimator that is less sensitive to weak instruments than TSLS is limited information maximum likelihood (LIML); see Hayashi (2000, Section 8.6) or Greene (2000, Chapter 16). The development of procedures that are reliable when instruments are weak is currently an area of active research.

Assumption #2: Instrument Exogeneity

If the instruments are not exogenous, then TSLS is inconsistent: the TSLS estimator converges in probability to something other than the population coefficient in the regression. After all, the idea of instrumental variables regression is that the instrument contains information about variation in X_i that is unrelated to the error term u_i . If, in fact, the instrument is not exogenous, then it cannot pinpoint this exogenous variation in X_i , and it stands to reason that IV regression fails to provide a consistent estimator. The math behind this argument is summarized in Appendix 10.4.

Can you test statistically the assumption that the instruments are exogenous? No. More precisely, suppose that you have as many instruments as endogenous regressors (the coefficients are exactly identified). Then it is impossible to develop a statistical test of the hypothesis that the instruments are in fact exogenous. That is, empirical evidence cannot be brought to bear on the question of whether these instruments satisfy the exogeneity restriction. In this case, the only way to assess whether the instruments are exogenous is to draw on expert opinion and your personal knowledge of the empirical problem at hand. For example, the Wrights' knowledge of agricultural supply and demand led them to

suggest that below average rainfall would plausibly shift the supply curve for butter but would not directly shift the demand curve.

Assessing whether the instruments are exogenous *necessarily* requires making an expert judgment based on personal knowledge of the application. If, however, there are more instruments than endogenous regressors, then there is a statistical tool that can be helpful in this process, the so-called test of overidentifying restrictions.

The overidentifying restrictions test. Suppose you have a single endogenous regressor, two instruments, and no included exogenous variables. Then you could compute two different TSLS estimators, one using the first instrument, the other using the second. These two estimators will not be the same because of sampling variation, but if both instruments are exogenous then they will tend to be close to each other. But what if these two instruments produce very different estimates? Then you might sensibly conclude that there is something wrong with one or the other of the instruments—or both. That is, it would be reasonable to conclude that one or the other, or both, of the instruments is not exogenous.

The **test of overidentifying restrictions** implicitly makes this comparison. We say implicitly, because the test is carried out without actually computing all of the different possible IV estimates. Here is the idea. Exogeneity of the instruments means that they are uncorrelated with u_i . This suggests that the instruments should be approximately uncorrelated with \hat{u}_i^{TSLS} , where $\hat{u}_i^{TSLS} = Y_i - (\hat{\beta}_0^{TSLS} + \hat{\beta}_1^{TSLS}X_{1i} + \dots + \hat{\beta}_{k+r}^{TSLS}W_{ri})$ is the residual from the estimated TSLS regression using all the instruments (approximately rather than exactly because of sampling variation). (Note that these residuals are constructed using the true X 's rather than their first-stage predicted values.) Accordingly, if the instruments are in fact exogenous, then the coefficients on the instruments in a regression of \hat{u}_i^{TSLS} on the instruments and the included exogenous variables should all be zero, and this hypothesis can be tested.

This method for computing the overidentifying restriction test is summarized in Key Concept 10.6. This statistic is computed using the homoskedasticity-only F -statistic. The test statistic is commonly called the J -statistic.

In large samples, if the instruments are not weak and the errors are homoskedastic, then, under the null hypothesis that the instruments are exogenous, the J -statistic has a chi-squared distribution with $m - k$ degrees of freedom (χ_{m-k}^2). It is important to remember that even though the number of restrictions being tested is m , the degrees of freedom of the asymptotic distribution of the J -statistic is $m - k$. The reason is that it is only possible to test the *overidentifying* restrictions, of which there are $m - k$.



Key Concept 10.6

The Overidentifying Restrictions Test (the J -Statistic)

Let \hat{u}_i^{TSLs} be the residuals from TSLS estimation of Equation (10.12). Use OLS to estimate the regression coefficients in

$$\hat{u}_i^{TSLs} = \delta_0 + \delta_1 Z_{1i} + \cdots + \delta_m Z_{mi} + \delta_{m+1} W_{1i} + \cdots + \delta_{m+r} W_{ri} + e_i, \quad (10.17)$$

where e_i is the regression error term. Let F denote the homoskedasticity-only F -statistic testing the hypothesis that $\delta_1 = \cdots = \delta_m = 0$. The overidentifying restrictions test statistic is $J = mF$. Under the null hypothesis that all the instruments are exogenous, then in large samples J is distributed χ^2_{m-k} , where $m - k$ is the “degree of overidentification,” that is, the number of instruments minus the number of endogenous regressors.

The easiest way to see that you cannot test the exogeneity of the regressors when the coefficients are exactly identified ($m = k$) is to consider the case of a single included endogenous variable ($k = 1$). If there are two instruments, then you can compute two TSLS estimators, one for each instrument, and you can compare them to see if they are close. But if you have only one instrument, then you can compute only one TSLS estimator and you have nothing to compare it to. In fact, if the coefficients are exactly identified, so that $m = k$, then the overidentifying test statistic J is exactly zero.

10.4 Application to the Demand for Cigarettes²

Our attempt to estimate the elasticity of demand for cigarettes left off with the TSLS estimates summarized in Equation (10.16), in which income was an included exogenous variable and there were two instruments, the general sales tax and the cigarette-specific tax. We can now undertake a more careful evaluation of these instruments.

²This section assumes knowledge of the material in Sections 8.1 and 8.2 on panel data with $T = 2$ time periods.

The Externalities of Smoking

Smoking imposes costs that are not fully borne by the smoker, that is, it generates externalities. One economic justification for taxing cigarettes therefore is to “internalize” these externalities. In theory, the tax on a pack of cigarettes should equal the dollar value of the externalities created by smoking that pack. But what, precisely, are the externalities of smoking, measured in dollars per pack?

Several studies have used econometric methods to estimate the externalities of smoking. The negative externalities—costs—borne by others include medical costs paid by the government to care for ill smokers, health care costs of nonsmokers associated with secondhand smoke, and fires caused by cigarettes.

But, from a purely economic point of view, smoking also has *positive* externalities, or benefits. The biggest benefit of smoking is that smokers tend to pay much more in Social Security (public pension) taxes than they ever get back. There are also large savings in nursing home expenditures on the very old—smokers tend not to live that long. Because the negative externalities of smoking occur while the smoker is alive but the positive ones accrue

after death, the net present value of the per-pack externalities (the value of the net costs per pack, discounted to the present) depend on the discount rate.

The studies do not agree on a specific dollar value of the net externalities. Some suggest the net externalities, properly discounted, are quite small, less than current taxes. In fact, the most extreme estimates suggest that the net externalities are *positive*, so smoking should be subsidized! Other studies, which incorporate costs that are probably important but difficult to quantify (such as caring for babies who are unhealthy because their mothers smoke) suggest that externalities might be \$1 per pack, possibly even more. But all the studies agree that, by tending to die in late middle age, smokers pay far more in taxes than they ever get back in their brief retirement.³

³An early calculation of the externalities of smoking was reported by Willard G. Manning et al. (1989). A calculation suggesting that health care costs would go *up* if everyone stopped smoking is presented in Barendregt et al. (1997). Other studies of the externalities of smoking are reviewed by Chaloupka and Warner (2000).

As in Section 10.1, it makes sense that the two instruments are relevant because taxes are a big part of the price of cigarettes, and shortly we will look at this empirically. First, however, we focus on the difficult question of whether the two tax variables are plausibly exogenous.

The first step in assessing whether an instrument is exogenous is to think through the arguments for why it may or may not be. This requires thinking about what factors account for the error term in the cigarette demand equation and whether these factors are plausibly related to the instruments.

Why do some states have higher per capita cigarette consumption than others? One reason might be variation in incomes across states, but state income is

included in Equation (10.16), so this is not part of the error term. Another reason is that there are historical factors influencing demand. For example, states that grow tobacco have higher rates of smoking than most other states. Could this factor be related to taxes? Quite possibly: if tobacco farming and cigarette production are important industries in a state, then these industries could exert influence to keep cigarette-specific taxes low. This suggests that an omitted factor in cigarette demand—whether the state grows tobacco and produces cigarettes—could be correlated with cigarette-specific taxes.

One solution to this possible correlation between the error term and the instrument would be to include information on the size of the tobacco and cigarette industry in the state; this is the approach we took when we included income as a regressor in the demand equation. But because we have panel data on cigarette consumption, a different approach is available that does not require this information. As discussed in Chapter 8, panel data makes it possible to eliminate the influence of variables that vary across entities (states) but do not change over time, such as the climate and historical circumstances that lead to a large tobacco and cigarette industry in a state. Two methods for doing this were given in Chapter 8: constructing data on *changes* in the variables between two different time periods, and using fixed effects regression. To keep the analysis here as simple as possible, we adopt the former approach and perform regressions of the type described in Section 8.2, based on the changes in the variables between two different years.

The time span between the two different years influences how the estimated elasticities are to be interpreted. Because cigarettes are addictive, changes in price will take some time to alter behavior. At first, an increase in the price of cigarettes might have little effect on demand. Over time, however, the price increase might contribute to some smokers' desire to quit and, importantly, it could discourage nonsmokers from taking up the habit. Thus the response of demand to a price increase could be small in the short run but large in the long run. Said differently, for an addictive product like cigarettes, demand might be inelastic in the short run, that is, it might have a short-run elasticity near zero, but it might be more elastic in the long run.

In this analysis, we focus on estimating the long-run price elasticity. We do this by considering quantity and price changes that occur over ten-year periods. Specifically, in the regressions considered here, the ten-year change in log quantity, $\ln(Q_{i,1995}^{\text{cigarettes}}) - \ln(Q_{i,1985}^{\text{cigarettes}})$, is regressed against the ten-year change in log price, $\ln(P_{i,1995}^{\text{cigarettes}}) - \ln(P_{i,1985}^{\text{cigarettes}})$, and the ten-year change in log income, $\ln(Inc_{i,1995}) - \ln(Inc_{i,1985})$. Two instruments are used: the change in the sales tax over ten years, $SalesTax_{i,1995} - SalesTax_{i,1985}$, and the change in the cigarette-specific tax over ten years, $CigTax_{i,1995} - CigTax_{i,1985}$.

TABLE 10.1 Two Stage Least Squares Estimates of the Demand for Cigarettes Using Panel Data for 48 U.S. States

Dependent variable: $\ln(Q_{i,1995}^{cigarettes}) - \ln(Q_{i,1985}^{cigarettes})$			
Regressor	(1)	(2)	(3)
$\ln(P_{i,1995}^{cigarettes}) - \ln(P_{i,1985}^{cigarettes})$	-0.94** (0.21)	-1.34** (0.23)	-1.20** (0.20)
$\ln(Inc_{i,1995}) - \ln(Inc_{i,1985})$	0.53 (0.34)	0.43 (0.30)	0.46 (0.31)
Intercept	0.21 (0.13)	0.45** (0.14)	0.37** (0.12)
Instrumental variable(s)	Sales tax	Cigarette-specific tax	Both sales tax and cigarette-specific tax
First-stage <i>F</i> -statistic	33.70	107.20	88.60
Overidentifying restrictions <i>J</i> -test and <i>p</i> -value	-	-	4.93 (0.026)

These regressions were estimated using data for 48 U.S. states (48 observations on the ten-year differences). The data are described in Appendix 10.1. The *J*-test of overidentifying restrictions is described in Key Concept 10.6 (its *p*-value is given in parentheses), and the first-stage *F*-statistic is described in Key Concept 10.5. Individual coefficients are statistically significant at the *5% level or **1% significance level.

The results are presented in Table 10.1. As usual, each column in the table presents the results of a different regression. All regressions have the same regressors, and all coefficients are estimated using TSLS; the only difference between the three regressions is the set of instruments used. In column (1), the only instrument is the sales tax; in column (2), the only instrument is the cigarette-specific tax; and in column (3), both taxes are used as instruments.

In IV regression, the reliability of the coefficient estimates hinge on the validity of the instruments, so the first things to look at in Table 10.1 are the diagnostic statistics assessing the validity of the instruments.

First, are the instruments relevant? The first-stage *F*-statistics in the three regressions are 33.7, 107.2, and 88.6, so in all three cases the first-stage *F*-statistics exceed 10. We conclude that the instruments are not weak, so that we can rely on the standard methods for statistical inference (hypothesis tests, confidence intervals) using the estimated coefficients and standard errors.

Second, are the instruments exogenous? Because the regressions in columns (1) and (2) each have a single instrument and a single included endogenous

regressor, the coefficients in those regressions are exactly identified. Thus we cannot deploy the J -test in either of those regressions. The regression in column (3), however, is overidentified because there are two instruments and a single included endogenous regressor, so there is one ($m - k = 2 - 1 = 1$) overidentifying restriction. The J -statistic is 4.93; this has a χ^2_1 distribution, so the 5% critical value is 3.84 (Appendix Table 3) and the null hypothesis that both the instruments are exogenous is rejected at the 5% significance level (this deduction can be made directly from the p -value of 0.026, reported in the table).

The reason the J -statistic rejects is that the two instruments produce rather different estimated coefficients. When the only instrument is the sales tax (column (1)), the estimated price elasticity is -0.94 , but when the only instrument is the cigarette-specific tax, the estimated price elasticity is -1.34 . Recall the basic idea of the J -statistic: if both instruments are exogenous, then the two TSLS estimators using the individual instruments are consistent and differ from each other only because of random sampling variation. If, however, one of the instruments is exogenous and one is not, then the estimator based on the endogenous instrument is inconsistent, which is detected by the J -statistic. In this application, the difference between the two estimated price elasticities is sufficiently large that it is unlikely to be the result of pure sampling variation, so the J -statistic rejects the null hypothesis that both the instruments are exogenous.

The J -statistic rejection means that the regression in column (3) is based on invalid instruments (the instrument exogeneity condition fails). What does this imply about the estimates in columns (1) and (2)? The J -statistic rejection says that at least one of the instruments is endogenous, so there are three logical possibilities: the sales tax is exogenous but the cigarette-specific tax is not, in which case the column (1) regression is reliable; the cigarette-specific tax is exogenous but the sales tax is not, so the column (2) regression is reliable; or neither tax is exogenous, so neither regression is reliable. The statistical evidence cannot tell us which possibility is correct, so we must use our judgment.

We think that the case for the exogeneity of the general sales tax is stronger than for the cigarette-specific tax, because the political process can link changes in the cigarette-specific tax to changes in the cigarette market and smoking policy. For example, if smoking decreases in a state because it becomes out of fashion, there will be fewer smokers and a weakened lobby against cigarette-specific tax increases, which in turn could lead to higher cigarette-specific taxes. Thus, changes in tastes (which are part of u) could be correlated with changes in cigarette-specific taxes (the instrument). This suggests discounting the IV estimates that use the cigarette-only tax as an instrument. This suggests adopting only the price elasticity estimated using the general sales tax as an instrument, -0.94 .

The estimate of -0.94 indicates that cigarette consumption is not very inelastic: an increase in price of 1% leads to a decrease in consumption of 0.94%. This may seem surprising for an addictive product like cigarettes. But remember that this elasticity is computed using changes over a ten-year period, so it is a long-run elasticity. This estimate suggests that increased taxes can make a substantial dent in cigarette consumption, at least in the long run.

When the elasticity is estimated using five-year changes from 1985 to 1990, rather than the ten-year changes reported in Table 10.1, the elasticity (estimated with the general sales tax as the instrument) is -0.79 ; for changes from 1990 to 1995, the elasticity is -0.68 . These estimates suggest that demand is less elastic over horizons of five years than ten. This finding of greater price elasticity at longer horizons is consistent with the large body of research on cigarette demand. Demand elasticity estimates in that literature typically fall in the range -0.3 to -0.5 , but these are mainly short-run elasticities; some recent studies suggest that the long-run elasticity could be perhaps twice the short-run elasticity.⁴

10.5 Where Do Valid Instruments Come From?

In practice the most difficult aspect of IV estimation is finding instruments that are both relevant and exogenous. There are two main approaches, which reflect two different perspectives on econometric and statistical modeling.

The first approach is to use economic theory to suggest instruments. For example, the Wrights' understanding of the economics of agricultural markets led them to look for an instrument that shifted the supply curve but not the demand curve; this in turn led them to consider weather conditions in agricultural regions. One area where this approach has been particularly successful is the field of financial economics. Some economic models of investor behavior involve statements about how investors forecast, which then imply sets of variables that are uncorrelated with the error term. Those models sometimes are nonlinear in the data and in the parameters, in which case the IV estimators discussed in this chapter cannot be used. An extension of IV methods to nonlinear models, called generalized method of moments estimation, is used instead. Economic theories are, however, abstractions that often do not take into account the nuances and details necessary for analyzing a particular data set. Thus this approach does not always work.

⁴If you are interested in learning more about the economics of smoking, see Chaloupka and Warner (2000) and Gruber (2001).

The second approach to constructing instruments is to look for some exogenous source of variation in X arising from what is, in effect, a random phenomenon that induces shifts in the endogenous regressor. For example, in our hypothetical example in Section 10.1, earthquake damage increased average class size in some school districts, and this variation in class size was unrelated to potential omitted variables that affect student achievement. This approach typically requires knowledge of the problem being studied and careful attention to the details of the data, and is best explained through examples.

Three Examples

We now turn to three empirical applications of IV regression that provide examples of how different researchers used their expert knowledge of their empirical problem to find instrumental variables.

Does putting criminals in jail reduce crime? This is a question only an economist would ask. After all, a criminal cannot commit a crime outside jail while in prison, and the fact that some criminals are caught and jailed serves to deter others. But the magnitude of the combined effect—the change in the crime rate associated with a 1% increase in the prison population—is an empirical question.

One strategy for estimating this effect is to regress crime rates (crimes per 100,000 members of the general population) against incarceration rates (prisoners per 100,000), using annual data at a suitable level of jurisdiction (for example, U.S. states). This regression could include some control variables measuring economic conditions (crime increases when general economic conditions worsen), demographics (youths commit more crimes than the elderly), and so forth. There is, however, a serious potential for simultaneous causality bias that undermines such an analysis: if the crime rate goes up and the police do their job, there will be more prisoners. On the one hand, increased incarceration reduces the crime rate; on the other hand, an increased crime rate increases incarceration. As in the butter example in Figure 10.1, because of this simultaneous causality an OLS regression of the crime rate on the incarceration rate will estimate some complicated combination of these two effects. This problem cannot be solved by finding better control variables.

This simultaneous causality bias, however, can be eliminated by finding a suitable instrumental variable and using TSLS. The instrument must be correlated with the incarceration rate (it must be relevant), but it must also be uncorrelated with the error term in the crime rate equation of interest (it must be exogenous). That is, it must affect the incarceration rate but be unrelated to any of the unobserved factors that determine the crime rate.

Where does one find something that affects incarceration but has no direct effect on the crime rate? One place is exogenous variation in the capacity of existing prisons. Because it takes time to build a prison, short-term capacity restrictions can force states to release prisoners prematurely or otherwise reduce incarceration rates. Using this reasoning, Levitt (1996) suggested that lawsuits aimed at reducing prison overcrowding could serve as an instrumental variable, and he implemented this idea using panel data for the U.S. states from 1972 to 1993.

Are variables measuring overcrowding litigation valid instruments? Although Levitt did not report first-stage F -statistics, the prison overcrowding litigation slowed the growth of prisoner incarcerations in his data, suggesting that this instrument is relevant. To the extent that overcrowding litigation is induced by prison conditions but not by the crime rate or its determinants, this instrument is exogenous. Because Levitt breaks down overcrowding legislation into several types, and thus has several instruments, he is able to test the overidentifying restrictions and fails to reject them using the J -test, which bolsters the case that his instruments are valid.

Using these instruments and TSLS, Levitt estimated the effect on the crime rate of incarceration to be substantial. This estimated effect was three times larger than the effect estimated using OLS, suggesting that OLS suffered from large simultaneous causality bias.

Does cutting class sizes increase test scores? As we saw in the empirical analysis of Part II, schools with small classes tend to be wealthier, and their students have access to enhanced learning opportunities both in and out of the classroom. In Part II, we used multiple regression to tackle the threat of omitted variables bias by controlling for various measures of student affluence, ability to speak English, and so forth. Still, a skeptic could wonder whether we did enough: if we left out something important, our estimates of the class size effect would still be biased.

This potential omitted variables bias could be addressed by including the right control variables, but if these data are unavailable (some, like outside learning opportunities, are hard to measure) then an alternative approach is to use IV regression. This regression requires an instrumental variable correlated with class size (relevance) but uncorrelated with the omitted determinants of test performance that make up the error term, such as parental interest in learning, learning opportunities outside the classroom, quality of the teachers and school facilities, etc. (exogeneity).

Where does one look for an instrument that induces random, exogenous variation in class size, but is unrelated to the other determinants of test performance?

Hoxby (2000) suggested biology. Because of random fluctuations in timings of births, the size of the incoming kindergarten class varies from one year to the next. Although the actual number of children entering kindergarten might be endogenous (recent news about the school might influence whether parents send a child to a private school), she argued that the *potential* number of children entering kindergarten—the number of four-year-olds in the district—is mainly a matter of random fluctuations in the birth dates of children.

Is potential enrollment a valid instrument? Whether it is exogenous depends on whether it is correlated with unobserved determinants of class size. Surely biological fluctuations in potential enrollment are exogenous, but potential enrollment also fluctuates because parents with young children choose to move into an improving school district and out of one in trouble. If so, an increase in potential enrollment could be correlated with unobserved factors such as the quality of school management, rendering this instrument invalid. Hoxby addressed this problem by reasoning that growth or decline in the potential student pool for this reason would occur smoothly over several years, whereas random fluctuations in birth dates would produce short-term “spikes” in potential enrollment. Thus, she used as her instrument not potential enrollment, but the deviation of potential enrollment from its long-term trend. These deviations satisfy the criterion for instrument relevance (the first-stage F -statistics all exceed 100). She makes a good case that this instrument is exogenous, but, as in all IV analysis, the credibility of this assumption is ultimately a matter of judgment.

Hoxby implemented this strategy using detailed panel data on elementary schools in Connecticut in the 1980s and 1990s. The panel data set permitted her to include school fixed effects, which, in addition to the instrumental variables strategy, attacks the problem of omitted variables bias at the school level. Her TSLS estimates suggested that the effect on test scores of class size is small; most of her estimates were statistically insignificantly different from zero.

Does aggressive treatment of heart attacks prolong lives? New aggressive treatments for victims of heart attacks (technically, acute myocardial infarctions, or AMI) hold the potential for saving lives. Before a new medical procedure—in this example, cardiac catheterization⁵—is approved for general use, it goes through clinical trials, a series of randomized controlled experiments designed to measure its effects and side effects. But strong performance in a clinical trial is one thing; actual performance in the real world is another.

⁵Cardiac catheterization is a procedure in which a catheter, or tube, is inserted into a blood vessel and guided all the way to the heart to obtain information about the heart and coronary arteries.

A natural starting point for estimating the real-world effect of cardiac catheterization is to compare patients who received the treatment to those who did not. This leads to regressing the length of survival of the patient against the binary treatment variable (whether the patient received cardiac catheterization) and other control variables that affect mortality (age, weight, other measured health conditions, etc.). The population coefficient on the indicator variable is the increment to the patient's life expectancy provided by the treatment. Unfortunately, the OLS estimator is subject to bias: cardiac catheterization does not "just happen" to a patient randomly; rather, it is performed because the doctor and patient decide that it might be effective. If their decision is based in part on unobserved factors relevant to health outcomes not in the data set, then the treatment decision will be correlated with the regression error term. If the healthiest patients are the ones who receive the treatment, the OLS estimator will be biased (treatment is correlated with an omitted variable), and the treatment will appear more effective than it really is.

This potential bias can be eliminated by IV regression using a valid instrumental variable. The instrument must be correlated with treatment (must be relevant) but must be uncorrelated with the omitted health factors that affect survival (must be exogenous).

Where does one look for something that affects treatment but not the health outcome, other than through its effect on treatment? McClellan, McNeil, and Newhouse (1994) suggested geography. Most hospitals in their data set did not specialize in cardiac catheterization, so many patients were closer to "regular" hospitals that did not offer this treatment than to cardiac catheterization hospitals. McClellan, McNeil, and Newhouse therefore used as an instrumental variable the difference between the distance from the AMI patient's home to the nearest cardiac catheterization hospital and the distance to the nearest hospital of any sort; this distance is zero if the nearest hospital is a cardiac catheterization hospital, otherwise it is positive. If this relative distance affects the probability of receiving this treatment, then it is relevant. If it is distributed randomly across AMI victims, then it is exogenous.

Is relative distance to the nearest cardiac catheterization hospital a valid instrument? McClellan, McNeil, and Newhouse do not report first-stage F -statistics, but they do provide other empirical evidence that it is not weak. Is this distance measure exogenous? They make two arguments. First, they draw on their medical expertise and knowledge of the health care system to argue that distance to a hospital is plausibly uncorrelated with any of the unobservable variables that determine AMI outcomes. Second, they have data on some of the additional variables that affect AMI outcomes, such as the weight of the patient, and in their sample

distance is uncorrelated with these *observable* determinants of survival; this, they argue, makes it more credible that distance is uncorrelated with the *unobservable* determinants in the error term as well.

Using 205,021 observations on Americans aged at least 64 who had an AMI in 1987, McClellan, McNeil, and Newhouse reached a striking conclusion: their TSLS estimates suggest that cardiac catheterization has a small, possibly zero effect on health outcomes, that is, cardiac catheterization does not substantially prolong life. In contrast, the OLS estimates suggest a large positive effect. They interpret this difference as evidence of bias in the OLS estimates.

McClellan, McNeil, and Newhouse's IV method has an interesting interpretation. The OLS analysis used actual treatment as the regressor, but because actual treatment is itself the outcome of a decision by patient and doctor, they argue that the actual treatment is correlated with the error term. Instead, TSLS uses *predicted* treatment, where the variation in predicted treatment arises because of variation in the instrumental variable: patients closer to a cardiac catheterization hospital are more likely to receive this treatment.

This interpretation has two implications. First, the IV regression actually estimates the effect of the treatment not on a "typical" randomly selected patient, but rather on patients for whom distance is an important consideration in the treatment decision. The effect on those patients might differ from the effect on a typical patient, which provides one explanation of the greater estimated effectiveness of the treatment in clinical trials than in McClellan, McNeil, and Newhouse's IV study. Second, it suggests a general strategy for finding instruments in this type of setting: find an instrument that affects the probability of treatment, but does so for reasons that are unrelated to the outcome except through their effect on the likelihood of treatment. Both these implications have applicability to experimental and "quasi-experimental" studies, the topic of Chapter 11.

10.6 Conclusion

From the humble start of estimating how much less butter people will buy if its price rises, IV methods have evolved into a general approach for estimating regressions when one or more variables are correlated with the error term. Instrumental variables regression uses the instruments to isolate variation in the endogenous regressors that is uncorrelated with the error in the regression of interest; this is the first stage of two stage least squares. This in turn permits estimation of the effect of interest in the second stage of two stage least squares.

Successful IV regression requires valid instruments, that is, instruments that are both relevant (not weak) and exogenous. If the instruments are weak, then the TSLS estimator can be biased, even in large samples, and statistical inferences based on TSLS t -statistics and confidence intervals can be misleading. Fortunately, when there is a single endogenous regressor it is possible to check for weak instruments simply by checking the first-stage F -statistic.

If the instruments are not exogenous, that is, if one or more instruments is correlated with the error term, then the TSLS estimator is inconsistent. If there are more instruments than endogenous regressors, then instrument exogeneity can be examined by testing the overidentifying restrictions. However, the core assumption—that there are at least as many exogenous instruments as there are endogenous regressors—cannot be tested. It is therefore incumbent on both the empirical analyst and the critical reader to use their own understanding of the empirical application to evaluate whether this assumption is reasonable.

The interpretation of IV regression as a way to exploit known exogenous variation in the endogenous regressor can be used to guide the search for potential instrumental variables in a particular application. This interpretation underlies much of the empirical analysis in the area that goes under the broad heading of program evaluation, in which experiments or quasi-experiments are used to estimate the effect of programs, policies, or other interventions on some outcome measure. A variety of additional issues arises in those applications, for example the interpretation of IV results when, as in the cardiac catheterization example, different “patients” might have different responses to the same “treatment.” These and other aspects of empirical program evaluation are taken up in Chapter 11.

Summary

1. Instrumental variables regression is a way to estimate regression coefficients when one or more regressor is correlated with the error term.
2. Endogenous variables are correlated with the error term in the equation of interest; exogenous variables are uncorrelated with this error term.
3. For an instrument to be valid, it must (1) be correlated with the included endogenous variable and (2) be exogenous.
4. IV regression requires at least as many instruments as included endogenous variables.
5. The TSLS estimator has two stages: first, the included endogenous variables are regressed against the included exogenous variables and the instruments; second, the

- dependent variable is regressed against the included exogenous variables and the predicted values of the included endogenous variables from the first-stage regression(s).
6. Weak instruments (instruments that are nearly uncorrelated with the included endogenous variables) make the TSLS estimator biased and TSLS confidence intervals and hypothesis tests unreliable.
 7. If an instrument is not exogenous, then the TSLS estimator is inconsistent.

Key Terms

instrumental variables (IV) regression (331)	overidentification (342)
instrumental variable (instrument) (331)	underidentification (342)
endogenous variable (333)	reduced form (343)
exogenous variable (333)	first-stage regression (344)
instrument relevance condition (333)	second-stage regression (344)
instrument exogeneity condition (333)	weak instruments (349)
two stage least squares (333)	first-stage F -statistic (350)
included exogenous variables (341)	test of overidentifying restrictions (353)
exact identification (342)	

Review the Concepts

- 10.1 In the demand curve regression model of Equation (10.3), is $\ln(P_i^{\text{butter}})$ positively or negatively correlated with the error, u_i ? If β_1 is estimated by OLS, would you expect the estimated value to be larger or smaller than the true value of β_1 ? Explain.
- 10.2 In the study of cigarette demand in this chapter, suppose that we used as an instrument the number of trees per capita in the state. Is this instrument relevant? Is it exogenous? Is it a valid instrument?
- 10.3 In his study of the effect of incarceration on crime rates, suppose that Levitt had used the number of lawyers per capita as an instrument. Is this instrument relevant? Is it exogenous? Is it a valid instrument?
- 10.4 In their study of the effectiveness of cardiac catheterization, McClellan, McNeil, and Newhouse (1994) used as an instrument the difference in distance to cardiac catheterization and regular hospitals. How could you determine whether this instrument is relevant? How could you determine whether this instrument is exogenous?