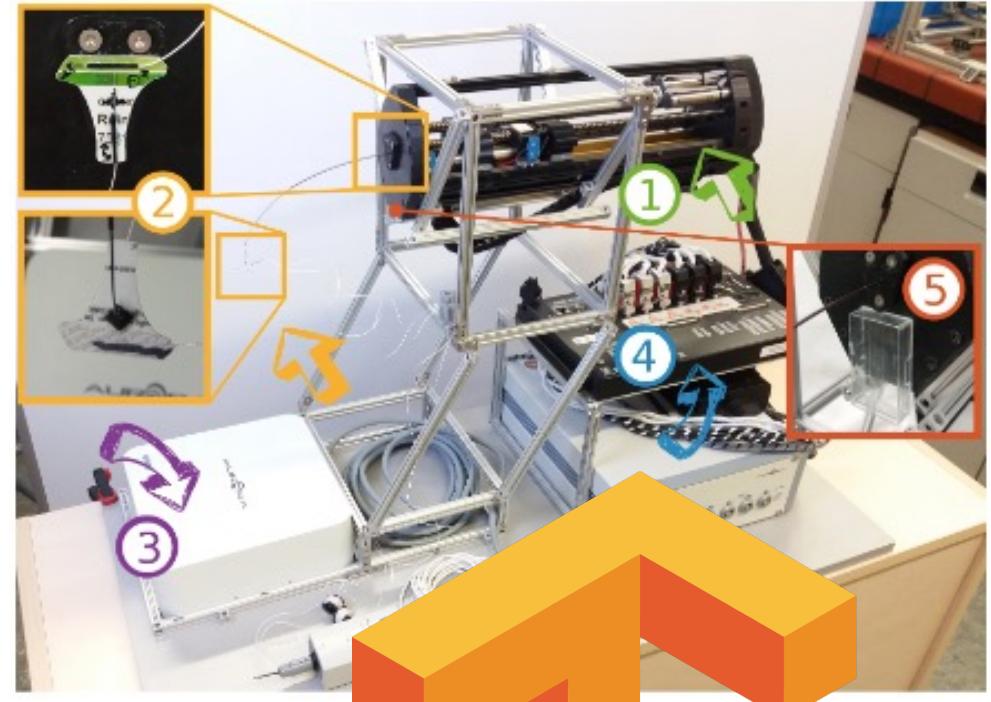


OPEN PROJECT

Reinhard Grassmann

MY BACKGROUND AND EXPERIENCE



CONCENTRIC TUBE CONTINUUM ROBOTS



2006 to 2020



36 different CTCR prototypes



61.1% only used for single publication



Different prototypes per laboratory



Webster et al. ISER 2019



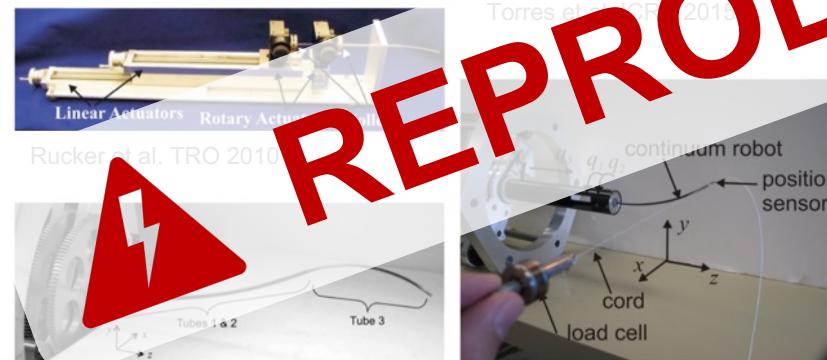
Morimoto et al. RA-L 2017



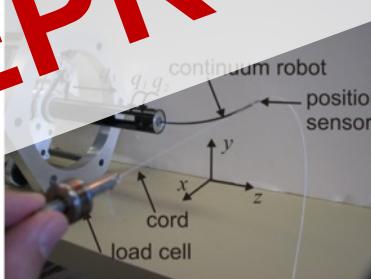
Rucker et al. TRO 2010



Dupont et al. TRO 2009



Torres et al. ICR 2015



Mahvash & Dupont. IROS 2010



Amato et al. ICRA 2010



Grassmann et al. IROS 2018



Burgner et al. IROS 2011



Ponten et al. SPIE 2017



OPEN  **PROJECT**

Hardware

Software

Blog

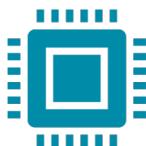
ACTUATION MODULE



- high-torque brushless DC motor
- high resolution optical encoder
- low-gear-ratio transmission



proprioceptive sensing
torque control



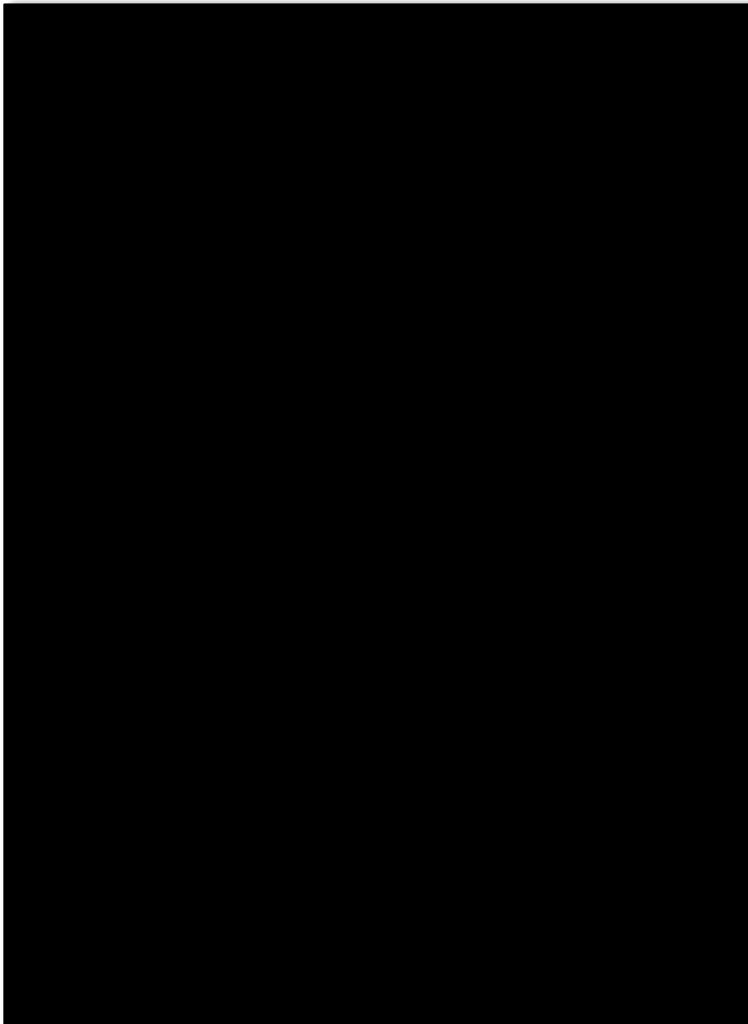
10 kHz low-level μ -controller
1 kHz high-level controller



modular
coupling to tubes/wires, tendons/rods



ONE ACTUATION MODULE



OPENCR PROJECT

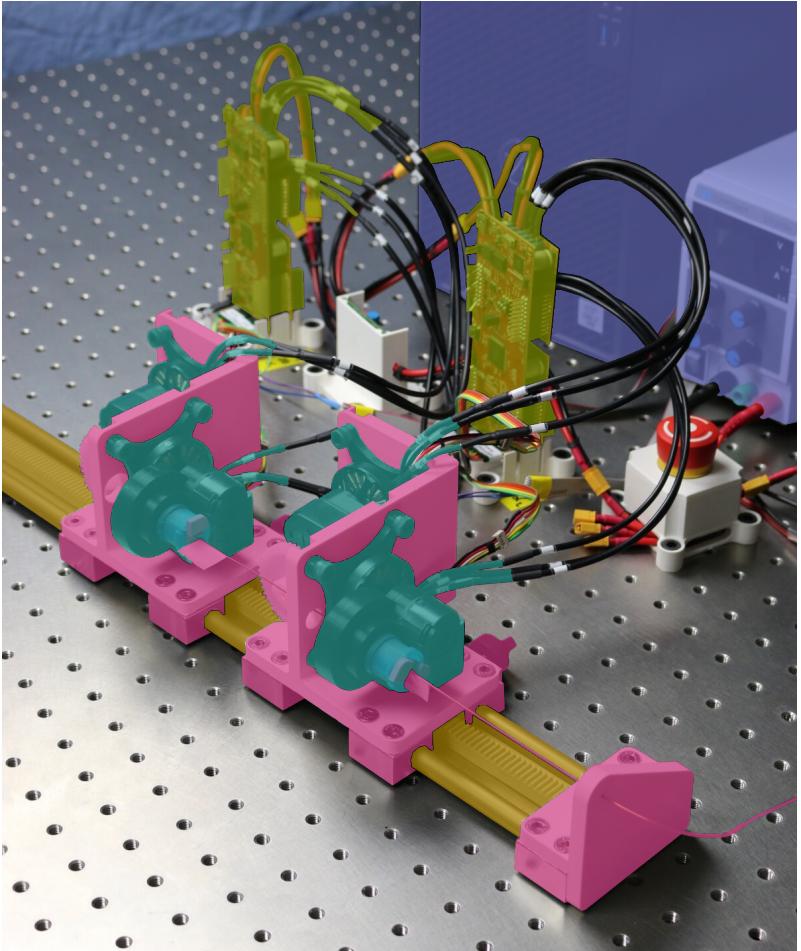
Modular Actuation Unit
Assembly Instructions



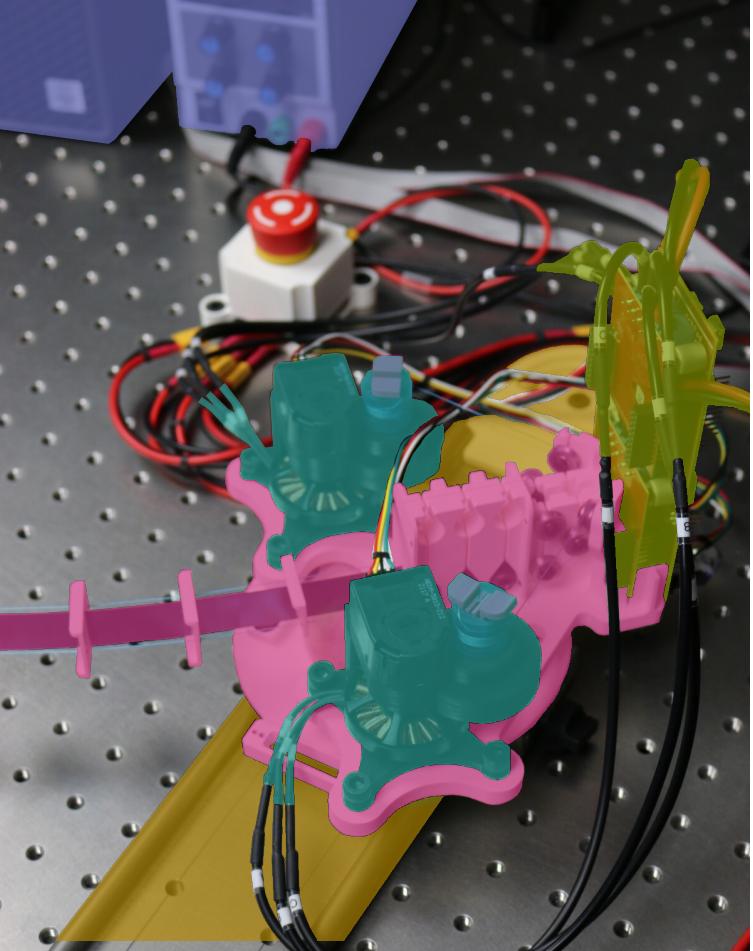
TO CREATE THEM ALL



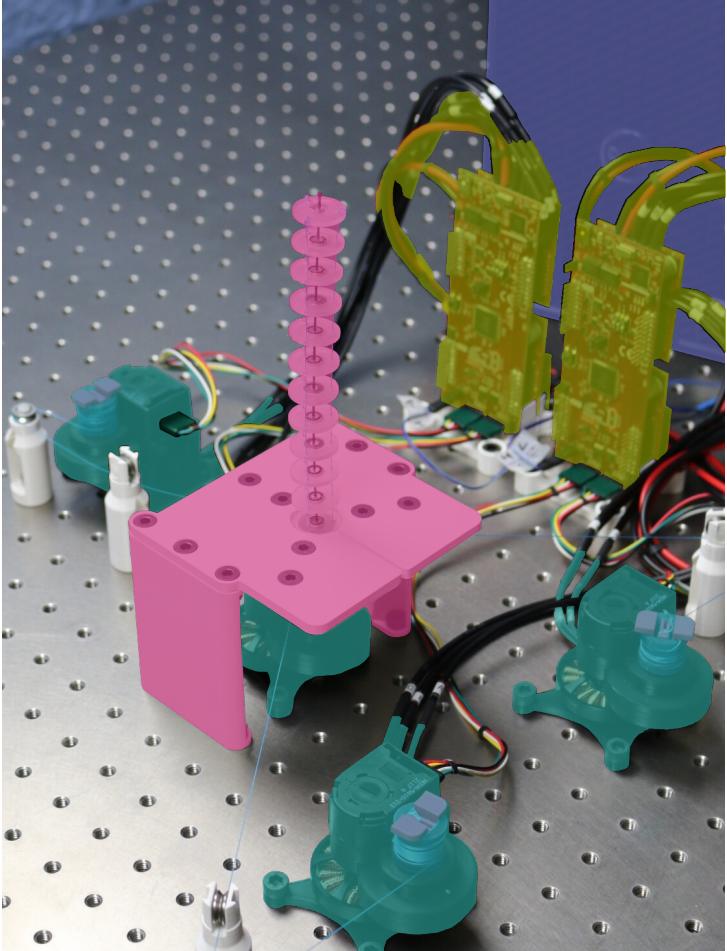
CONCENTRIC TUBE



PLANAR TENDON-DRIVEN



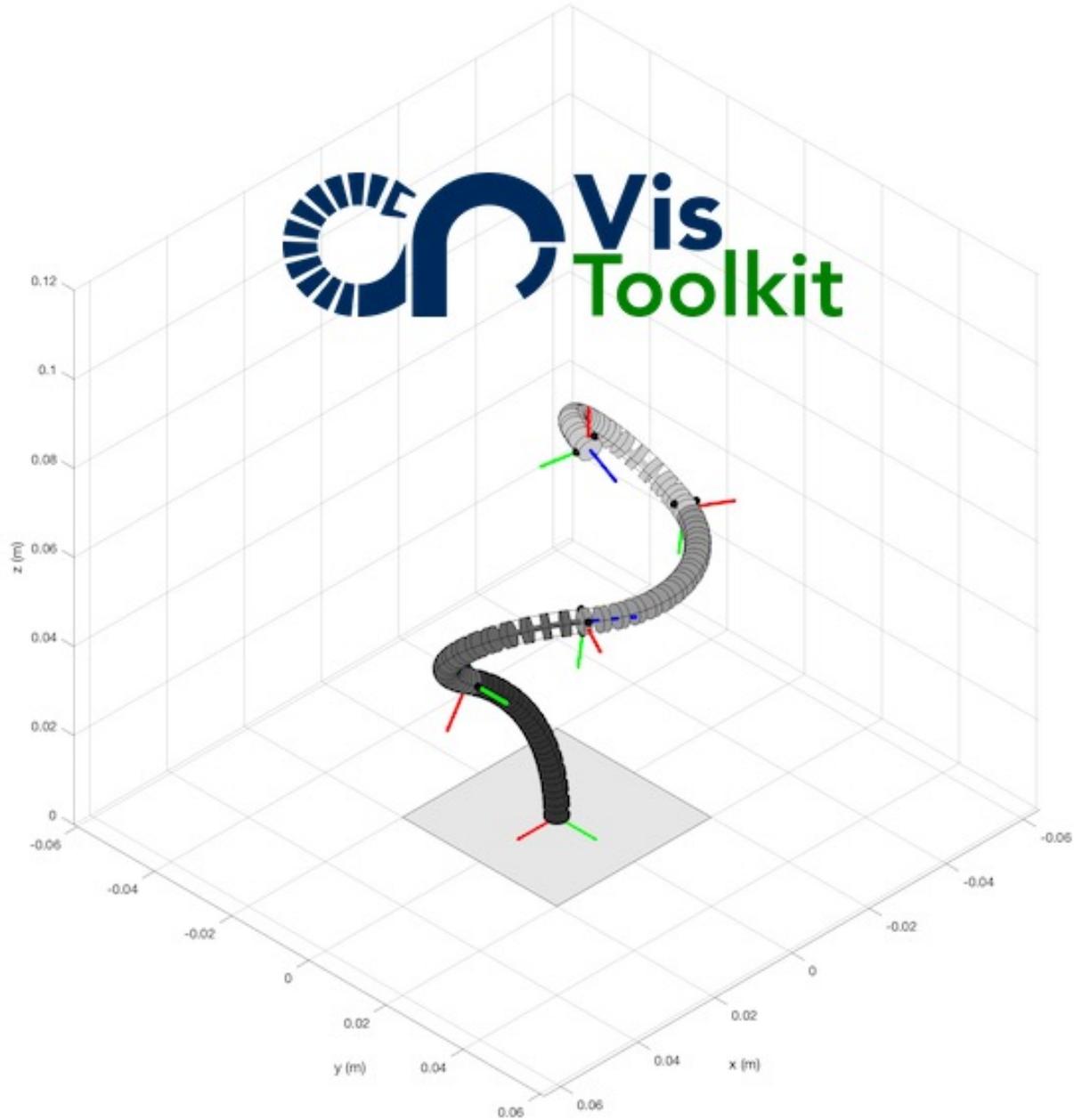
SPATIAL TENDON-DRIVEN



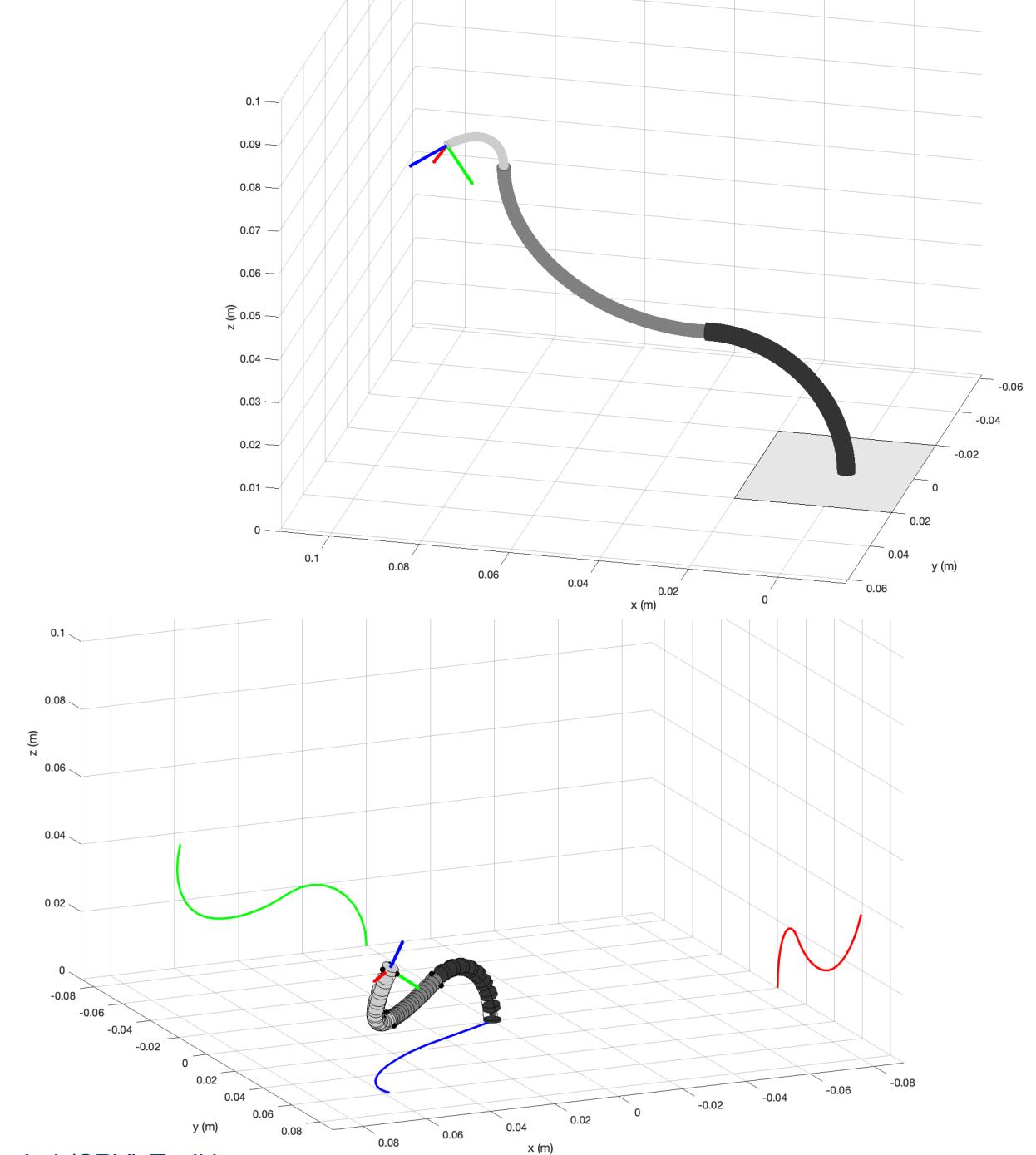
OPEN  **PROJECT**

Hardware

Software



CRV
Vis
Toolkit



PHYSICS-BASED MODELING PERFORMANCE BENCHMARK



Guidelines



Comparison
modeling performance



C++ and Matlab
implementations

frontiers
in Robotics and AI

ORIGINAL RESEARCH
published: 02 February 2021
doi: 10.3389/frobt.2020.630245

How to Model Tendon-Driven Continuum Robots and Benchmark Modelling Performance

Priyanka Rao *, Quentin Peyron, Sven Lilge and Jessica Burgner-Kahrs

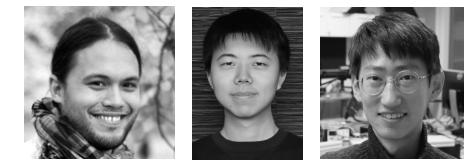
Continuum Robotics Laboratory, Department of Mathematical and Computational Sciences, University of Toronto Mississauga, Mississauga, ON, Canada

Tendon actuation is one of the most prominent actuation principles for continuum robots. To date, a wide variety of modelling approaches has been derived to describe the deformations of tendon-driven continuum robots. Motivated by the need for a comprehensive overview of existing methodologies, this work summarizes and outlines state-of-the-art modelling approaches. In particular, the most relevant models are classified based on backbone representations and kinematic as well as static assumptions. Numerical case studies are conducted to compare the performance of representative modelling approaches from the current state-of-the-art, considering varying robot parameters and scenarios. The approaches show different performances in terms of accuracy and computation time. Guidelines for the selection of the most suitable approach for given designs of tendon-driven continuum robots and applications are deduced from these results.

OPEN ACCESS

Edited by:
Matteo Cianchetti,

LEARNING-BASED MODELING FIRST DATASET AND BENCHMARK



100k
joint space and task space



Effective representations
Sampling guidelines



Benchmark
FK: 0.4% w.r.t. length

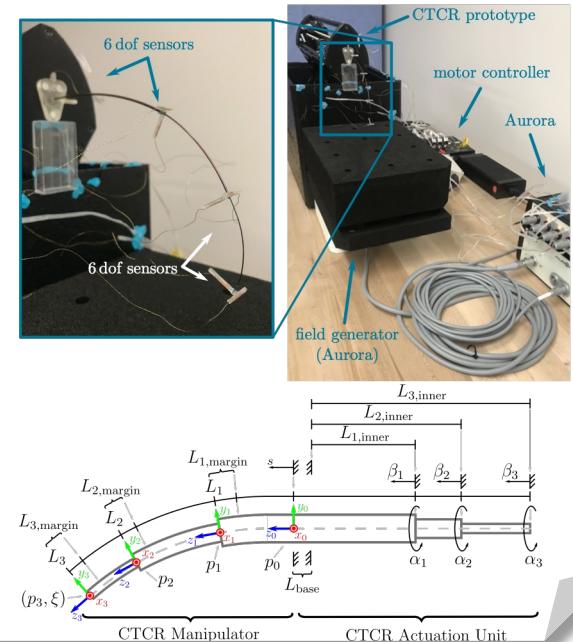
2022 IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS)
October 23-27, 2022, Kyoto, Japan

A Dataset and Benchmark for Learning the Kinematics of Concentric Tube Continuum Robots

Reinhard M. Grassmann¹, Student Member, IEEE, Ryan Zeyuan Chen¹, Student Member, IEEE,
Nan Liang², Student Member, IEEE, and Jessica Burgner-Kahrs¹, Senior Member, IEEE

Abstract—Establishing a physics-based model capturing the kinetostatic behavior of concentric tube continuum robots is challenging as elastic interactions between the flexible tubes constituting the robot result in a highly non-linear problem. The Goldstandard physics-based model using the Cosserat theory of elastic rods achieves reasonable approximations with 1.5 – 3 % with respect to the robot's length, if well-calibrated. Learning-based models of concentric tube continuum robots have been shown to outperform the Goldstandard model with approximation errors below 1 %. Yet, the merits of learning-based models remain largely unexplored as no common dataset and benchmark exist.

In this paper, we present a dataset captured from a three-tube concentric tube continuum robot for use in learning-based kinematics research. The dataset consists of 100 000 joint configurations and the corresponding four 6 dof sensors in $SE(3)$ measured with an electromagnetic tracking system (github.com/ContinuumRoboticsLab/CRL-Dataset-CTCR-Pose). With our dataset, we empower the continuum robotics and machine learning community to advance the field. We share our insights and lessons learned on joint space representation, shape representation in task space, and sampling strategies. Furthermore, we provide benchmark results for learning the forward kinematics using a simple, shallow feedforward neural network. The benchmark results for the tip error are 0.74 mm w.r.t. position (0.4 % of total robot length) and 6.49° w.r.t. orientation.



OPEN  **PROJECT**

Hardware

Software

Blog

**Jessica Burgner-Kahrs**

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Continuum Robotics 101

2022-10-21 • 8 minute read

We are starting our 101 blog post series. In this category, we will present introductory concepts in continuum robotics targeted at novices who have prior knowledge in fundamental robotics and in serial manipulators. The material is based off the [Continuum Robotics](#) course I taught at Leibniz University Hannover in 2017 and 2018 and the [Introduction to Continuum Robotics](#) I am teaching at the University of Toronto since 2021.

Today, we are looking at two questions

How can we identify a continuum robot? What differentiates continuum robots from other robot types?

On this page

- [Four Examples](#)
- [Example 1: Bionic Motion Robot](#)
- [Example 2: Snake-arm Robot](#)
- [Example 3: Multi-articulated Instruments](#)
- [Example 4: Soft Finger Gripper](#)
- [Definition](#)
- [Summary](#)
- [References](#)

**Jessica Burgner-Kahrs**

Professor. Roboticist.

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The First Continuum Robot

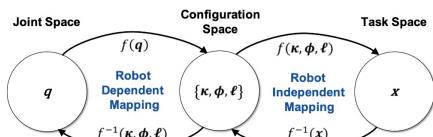
2022-11-01 • less than 1 minute read

The very first continuum robot was developed by two students at Stanford University in 1965, Victor Scheinman and Larry Leifer. Named after the Norwegian term for *snake*, the *Orm* is a pneumatically actuated robot arm. Motion is achieved by a total 28 inflatable pneumatic bellow actuators sandwiched between seven metal disks. Each actuator could be fully inflated or deflated by setting or resetting a bit in a computer word. The design was abandoned because the robot's motion was difficult to control at that time.

**Constant Curvature Kinematics Framework**

2022-12-02 • 8 minute read

Today, we dive deeper into the common constant curvature kinematics framework. We look at the mappings between joint and configuration space, i.e. the **robot dependent mapping**, and between configuration and task space, i.e. the **robot independent mapping**.

**On this page**

- [Robot Dependent Mapping](#)
- [Robot Independent Mapping](#)
- [Geometry of Circular Arcs](#)
- [Frenet-Serret Frames](#)
- [Parallel Transport Frames](#)
- [Concatenation of Arcs](#)
- [References](#)

**Algorithmic Motion Planning Meets Minimally-Invasive Robotic Surgery - Part 2**

2024-01-14 • 7 minute read

A Case Study of Inspection Using the CRISP Robot

In certain medical applications, physicians may want to inspect some region of interest for diagnostic purposes completing the procedure as fast as is safely possible to reduce costs and improve patient outcomes, especially if the patient is under anesthesia during the procedure. For example, the needle-diameter Continuum Reconfigurable Incisionless Surgical Parallel (CRISP) robot^{1,2} was suggested to assist in the diagnosis of the cause of a

- [A Case Study of Inspection Using the CRISP Robot](#)
- [Inspection Planning](#)
- [What makes it challenging](#)
- [IRIS - Incremental Random Inspection-roadmap Search](#)
- [References](#)

101
history
research
hands-on
opinion

**Alan Kuntz**

Assistant Professor.

📍 University of Utah, USA
[Email](#)
[Website](#)
[LinkedIn](#)

Introduction to Motion Planning for Continuum Robots - Part 2

2023-06-28 • 10 minute read

Today, we continue our introduction to motion planning for continuum robots. If you have missed Part 1 of the intro, look at [last week's blog post](#) before you continue here!

What makes motion planning particularly challenging for continuum robots?

First, let's discuss one of the primary differences between continuum robots and more "traditional" robots (for lack of a better term)—modeling.

On this page

- [What makes motion planning particularly challenging for continuum robots?](#)
- [How has the community overcome these challenges?](#)
- [Modeling accuracy \(or lack thereof\)](#)
- [Computation speed \(or lack thereof\)](#)
- [So what's next?](#)
- [Leveraging learned models](#)

**Priyanka Rao**

PhD Candidate.

📍 University of Toronto, Canada
[Email](#)

Getting Started on a Model for Tendon-driven Continuum Robots

2023-01-06 • 4 minute read

As you've been reading so far, there are multiple facets to [continuum robot modeling](#). We will pick up this thread today and follow it into the world of modeling tendon-driven continuum robots. We will be narrowing our focus on modeling the forward mapping from actuation inputs such as tendon tension or displacements to the final backbone shape in task space.



- [Three Steps to a Model](#)
- [Step 1: Selecting the Backbone Parameterization](#)
- [Step 2: Deriving the Force and Moment Equilibrium Equations](#)
- [Step 3: Writing the Constitutive Equations](#)
- [Getting Started with Your TDCR Model](#)
- [References](#)

Continuum Robotics 101

Turn 42 DoF into 2 DoF — overcoming the troublesome interdependency between arbitrary numbers of tendons/cables/bellows. Enabling effective algorithms on the **2 DoF manifold** embedded in the n dof joint space thanks to the proposed **Clarke transform**.

Actuation Constraints in Continuum Robotics Revisited:
2 dof Manifold and Clarke Transform

Reinhard M. Grassmann, Anastassia Senyk, and Jessica Burgner-Kahrs

Motivation

- Every displacement-actuated continuum robot is subject to actuation constraints
- Solution exists for $n = 3$ and $n = 4$ actuators
- How to deal with n actuators?
- Can we identify the manifold of the joint space?

Approach

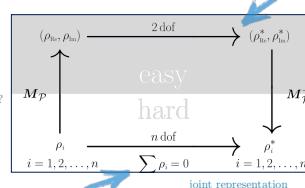
- Revisit the actuation constraints
- Analogy to Kirchhoff's current law and Field-Oriented Control
- Clark transformation

Results

- Direct sampling without branching
- Consideration of actuators using tendons, cables, rods, and even bellows
- Better joint control
- Found a suitable displacement representation
- Generalize Clarke transformation to n phases
- 2 dof manifold identified
- Identify the linear one-to-one mapping

Conclusion

- Clarke transform to transform your inputs and outputs
- Utilize the 2 dof manifold
- Mandatory even for low dimensional problems ($n = 3$)
- Useful for pneumatic/tendon/cable/backbone actuated continuum robots (including soft robots)

**generalized Clarke Transformation**

$$M_P = \begin{bmatrix} \cos(0) & \cos\left(\frac{2\pi}{n}\right) & \cdots & \cos\left(\frac{(n-1)\pi}{n}\right) \\ \sin(0) & \sin\left(\frac{2\pi}{n}\right) & \cdots & \sin\left(\frac{(n-1)\pi}{n}\right) \end{bmatrix}$$

$$\begin{bmatrix} \kappa_x \\ \kappa_y \end{bmatrix} = \begin{bmatrix} \kappa \cos(\theta) \\ \kappa \sin(\theta) \end{bmatrix} = \frac{1}{L - \beta} \begin{bmatrix} M_P & \text{diag}(1/d_i) \rho \end{bmatrix}$$

removes L removes ψ_i removes d_i

robot-depending mapping

$$\rho = (L - \beta) \text{diag}(d_i) M_P^{-1} \begin{bmatrix} \kappa_x \\ \kappa_y \end{bmatrix}$$

adds L adds d_i adds ψ_i

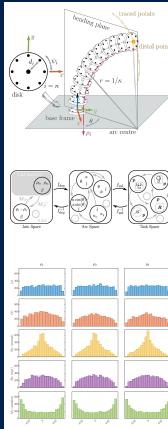


Fig. 3. Distributions for different sampling methods.

COMPUTATION TIME IN SECONDS AND NUMBER OF ITERATIONS FOR DIFFERENT SAMPLING METHODS. EACH METHOD IS RUN 1000 TIMES. THE MEAN COMPUTATION TIME AND STANDARD DEVIATION ARE REPORTED FOR THE WALL CLOCK TIME AND THE NUMBER OF ITERATIONS IS REPORTED AS THE MEAN NUMBER OF ITERATIONS. THE NUMBER OF COMPUTATIONS IN A SINGLE LOGIC CYCLE IS THE NUMBER OF SAMPLING IN A SINGLE LOGIC CYCLE.

method	time in sec	factor	std. dev.	success rate
SO	14.8 ± 3.6	14.1	N/A	9.8 %
SO	10.0 ± 1.5	10.0	± 0.5	99.0 %
SO	10.0 ± 1.5	45.0	± 0.5	92.0 %

M2 (unrolled)

M2 (rotated)

M2 (sheared)

M2 (scaled)

M2 (rotated)

OPEN  **PROJECT**

Hardware

Software

Blog



<https://crl.utm.toronto.ca>

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