THE STATA JOURNAL

Editor

H. Joseph Newton Department of Statistics Texas A & M University College Station, Texas 77843 979-845-3142; FAX 979-845-3144 jnewton@stata-journal.com

Associate Editors

Christopher F. Baum Boston College

Rino Bellocco

Karolinska Institutet, Sweden and Univ. degli Studi di Milano-Bicocca, Italy

A. Colin Cameron

University of California-Davis

David Clayton

Cambridge Inst. for Medical Research

Mario A. Cleves

Univ. of Arkansas for Medical Sciences

William D. Dupont Vanderbilt University

Charles Franklin

University of Wisconsin-Madison

Joanne M. Garrett

University of North Carolina

Allan Gregory

Queen's University

James Hardin

University of South Carolina

Ben Jann

ETH Zürich, Switzerland

Stephen Jenkins

University of Essex

Ulrich Kohler

WZB, Berlin

Stata Press Production Manager

Stata Press Copy Editor

Editor

Nicholas J. Cox Department of Geography Durham University South Road Durham City DH1 3LE UK

n.j.cox@stata-journal.com

Jens Lauritsen

Odense University Hospital

Stanley Lemeshow

Ohio State University

J. Scott Long

Indiana University

Thomas Lumley

University of Washington-Seattle

Roger Newson

Imperial College, London

Marcello Pagano

Harvard School of Public Health

Sophia Rabe-Hesketh

University of California-Berkeley

J. Patrick Royston

MRC Clinical Trials Unit, London

Philip Ryan

University of Adelaide

Mark E. Schaffer

Heriot-Watt University, Edinburgh

Jeroen Weesie

Utrecht University

Nicholas J. G. Winter

University of Virginia

Jeffrey Wooldridge

Michigan State University

Lisa Gilmore

Gabe Waggoner

Copyright Statement: The Stata Journal and the contents of the supporting files (programs, datasets, and help files) are copyright © by StataCorp LP. The contents of the supporting files (programs, datasets, and help files) may be copied or reproduced by any means whatsoever, in whole or in part, as long as any copy or reproduction includes attribution to both (1) the author and (2) the Stata Journal.

The articles appearing in the Stata Journal may be copied or reproduced as printed copies, in whole or in part, as long as any copy or reproduction includes attribution to both (1) the author and (2) the Stata Journal.

Written permission must be obtained from StataCorp if you wish to make electronic copies of the insertions. This precludes placing electronic copies of the Stata Journal, in whole or in part, on publicly accessible web sites, fileservers, or other locations where the copy may be accessed by anyone other than the subscriber.

Users of any of the software, ideas, data, or other materials published in the Stata Journal or the supporting files understand that such use is made without warranty of any kind, by either the Stata Journal, the author, or StataCorp. In particular, there is no warranty of fitness of purpose or merchantability, nor for special, incidental, or consequential damages such as loss of profits. The purpose of the Stata Journal is to promote free communication among Stata users.

The Stata Journal, electronic version (ISSN 1536-8734) is a publication of Stata Press. Stata and Mata are registered trademarks of StataCorp LP.

Stata tip 38: Testing for groupwise heteroskedasticity

Christopher F. Baum Department of Economics Boston College Chestnut Hill, MA 02467 baum@bc.edu

A natural source of heteroskedasticity in many kinds of data is group membership: observations in the sample may be a priori defined as members of groups, and the variance of a series may differ considerably across groups. This concept will also apply to the errors from a linear regression. The assumption of homoskedasticity in the relationship may reasonably hold within each group, but not between groups. This assumption most commonly arises in cross-sectional datasets. In economic data, for instance, the groups may correspond to firms in different industries or workers in different occupations. It could also apply in a time-series context: for instance, the variance of daily temperature may not be constant over the four seasons. In any case, a test for heteroskedasticity of this sort should take this a priori knowledge into account.

How might we test for groupwise heteroskedasticity in a variable or in the errors from a regression? In the context of regression, if we can argue that each group's regression equation satisfies the classical assumptions (including that of homoskedasticity), the s^2 computed by regress (see [R] regress) is a consistent estimate of the group-specific variance of the disturbance process. For two groups, an F test may be constructed, with the larger variance in the numerator; the degrees of freedom are the residual degrees of freedom of each group's regression. Conducting an F test is easy if both groups' residuals are stored in one variable, with a group variable indicating group membership (in this case 1 or 2). The third form of sdtest may then be used, with the by(groupvar) option, to conduct the F test.

What if there are more than two groups across which we wish to test for equality of disturbance variance, for instance, a set of 10 industries? We may then use the robvar command (see [R] sdtest), which like sdtest expects to find one variable containing each group's residuals, with a group membership variable identifying them. The by(groupvar) option is used here as well. The test conducted is that of Levene (1960) labeled as W_0 , which is robust to nonnormality of the error distribution. Two variants of the test proposed by Brown and Forsythe (1974), which uses more robust estimators of central tendency (e.g., median rather than mean), W_{50} and W_{10} , are also computed.

We illustrate groupwise heteroskedasticity with state-level data: 1 observation per year for each of the six states in the New England region of the United States for 1981–2000. We first apply robvar to the state-level population series to examine whether the variance of population is constant across states.

C. F. Baum 591

- . use http://www.stata-press.com/data/imeus/NEdata
- . robvar pop, by(state)

	Summary of pop						
state	Mean	Std. Dev.	Freq.				
CT	3276614.5	81452.212	20				
MA	6030915.5	178354.76	20				
ME	1212718.1	46958.538	20				
NH	1094238.9	94362.302	20				
RI	1000209.9	29548.701	20				
VT	562960.65	31310.625	20				
Total	2196276.3	1931629.4	120				
WO = 13.856	6324 df(5, 1	14) Pr > F	= 0.0000000				
W50 = 11.820	0938 df(5, 1	14) Pr > F	= 0.0000000				
W10 = 13.306	6895 df(5, 1	14) Pr > F	= 0.00000000				

All forms of the test clearly reject the hypothesis of homoskedasticity across states' population series: hardly surprising when the standard deviation of Massachusetts' (MA) population is six times that of Rhode Island (RI).

We now fit a linear trend model to state disposable personal income per capita, dpipc, by regressing that variable on year. The residuals are tested for equality of variances across states with robvar.

. regr	ess	dpipo	year
--------	-----	-------	------

Source	SS	df		MS		Number of obs F(1, 118)		120 440.17
Model Residual	3009.33617 806.737449	1 118		.33617 675804		Prob > F	=	0.0000 0.7886 0.7868
Total	3816.07362	119	32.0	678456		5		2.6147
dpipc	Coef.	Std.	Err.	t	P> t	[95% Conf.	Int	terval]
year _cons	.8684582 -1710.508	.0413		20.98 -20.76	0.000	.7864865 -1873.673		9504298 547.343

- . predict double eps, residual
- . robvar eps, by(state)

		state	Summary of Residuals Mean Std. Dev.					Freq.		
		CT	4	.167853	1.35	96266		20		
		MA	1	.618796	.865	50138		20		
		ME	-2.	9841056	.937	97625		20		
		NH	.5	1033312	.611	39299		20		
		RI		8927223	.634	08722		20		
		VT	-2.	4201543	.714	70977		20		
		Total	-6.	063e-14	2.60	37101		120		
WO	=	4.3882	2072	df(5,	114)	Pr >	F =	0.00108562		
W50	=	3.2989	9851	df(5,	114)	Pr >	F =	0.00806751		
W10	=	4.2536	3245	df(5,	114)	Pr >	F =	0.00139064		

592 Stata tip 38

The hypothesis of equality of variances is soundly rejected by all three robvar test statistics, with the residuals for Connecticut, Massachusetts, and Maine possessing a standard deviation considerably larger than those of the other three states.

References

Brown, M. B., and A. B. Forsythe. 1974. Robust tests for the equality of variances. *Journal of the American Statistical Association* 69: 364–367.

Levene, H. 1960. Robust tests for equality of variances. In *Contributions to Probability and Statistics: Essays in Honor of Harold Hotelling*, ed. I. Olkin, S. G. Ghurye, W. Hoeffding, W. G. Madow, and H. B. Mann, 278–292. Menlo Park, CA: Stanford University Press.