Smooth risk-based predictive approaches to treatment effect heterogeneity: A simulation study

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Abstract

Objective: Simulation study to compare different risk-based approaches to estimating individualized treatment effects within the RCT setting. **Study Design and Setting:** Starting from a base case scenario that assumes a true constant treatment effect, we considered a total of 66 scenarios for introducing non-constant effects and evaluating methods under different sample sizes and baseline risk prediction performance. We compared 7 methods for predicting absolute benefit: A constant treatment effect model, a risk stratified approach, a model including a linear interaction of the baseline risk linear predictor with treatment, 3 restricted cubic spline smoothing models of increasing flexibility (3, 4 and 5 knots) and an adaptive model selection method based on Akaike's Information Criterion. We evaluated performance using root mean squared error, discrimination for benefit and calibration for benefit (i.e., observed vs. predicted risk difference in treated vs. untreated). **Results:** The model including a linear interaction of the risk linear predictor with treatment had adequate performance that was robust under the majority of the simulation scenarios. Methods using restricted cubic spline smoothing required larger sample sizes and higher prediction AUC to achieve adequate performance. The adaptive approach's performance was comparable to the performance of the best model in each scenario. **Conclusion:** In most cases using a model just including a linear interaction of the risk linear predictor with treatment adequately predicts absolute benefit.

1 Introduction

- Within the setting of patient-centered outcomes research, predictive approaches for assessing heterogeneity of treatment effects (HTE) aim at the development of models predicting either individualized effects or which of two (or more) treatments is better for an individual [1]. In prior work, we divided such methods in three broader categories based on the reference class used for defining patient similarity when making individualized predictions or recommendations [2]. Risk-modeling approaches use prediction of baseline risk as the reference; treatment effect modeling approaches also model treatment-covariate interactions, in addition to risk factors; optimal treatment regime approaches focus on developing treatment assignment rules and therefore rely heavily on modeling treatment effect modifiers. Risk-modeling approaches to predictive HTE analyses provide a viable option in the absence of well-established 10 treatment effect modifiers [3,4]. In simulations, modeling of effect modifiers in the form of treatment-covariate 11 interactions often led to miscalibrated predictions of benefit, while risk-based methods proved quite robust [5]. Most often, risk-modeling approaches are carried out in two steps: first a risk prediction model is developed 13 externally or internally on the entire RCT population, "blinded" to treatment; then the RCT population is stratified using this prediction model to evaluate risk-based treatment effect variation [6]. However, even though estimates 15 at the risk subgroup level are accurate, this does not apply on the individual level, especially for patients with 16 predicted risk at the boundaries of the risk intervals. Therefore, the risk-stratified approach should be used for 17 exploring and presenting an overview of HTE, while inferences on the individual level should be made with caution. 18 We aimed to provide an overview of methods that can be used to move from a risk-stratified approach to
- a continuous one using common smoothing techniques. These methods extend the risk-based framework of predictive HTE analyses to allow predictions on the individual level, within the RCT setting. We carried out a simulation study to compare the performance of these methods under different settings of increasing non-linearity of treatment effects. Finally, we carried out an application on real data as a demonstration of the considered techniques.

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5 2 Methods

26 2.1 Simulation scenarios

- $_{
 m 27}$ In the simulated datasets of the base-case scenario treatment was allocated at random using a 50/50 split.
- For each patient we simulated 8 baseline covariates, where $x_1,\ldots,x_4\sim N(0,1)$ and $x_5,\ldots,x_8\sim B(1,0.2)$.

- ²⁹ Outcomes for patients in the control arm were generated from a logistic regression model including all baseline
- $_{
 m 30}$ covariates. Coefficient values were such, so that the prediction model had an AUC of 0.75 and an event rate
- $_{31}$ of 20% in the control arm was achieved. Outcomes in the treatment arm were created using the same logistic
- 32 regression model, including a constant treatment effect odds ratio (OR) of 0.8. The generated samples of the
- base-case scenario were of size n=4,250 (80% power for the detection of an unadjusted OR of 0.8).
- $_{34}$ We evaluated the effect of sample size considering additional scenarios with sample sizes of 1,064 and 17,000.
- 35 We also evaluated the effect of prediction performance, adjusting the baseline covariate coefficients, so that AUC
- $_{36}$ values of 0.65 and 0.80 were achieved when validating in a simulated dataset of 500,000 patients.
- 37 A true logistic regression model with a constant treatment effect (constant OR) implies that outcome risk in
- the treatment arm is a straight line parallel to the first diagonal on the log-odds scale, with distance equal to
- $\log(\mathsf{OR})$. We assessed the effect of stronger and absent relative treatment effects ($\mathsf{OR}=0.5$ or $\mathsf{OR}=1$). We
- 40 also relaxed the assumption that the line should be parallel to the diagonal, considering moderate and stronger
- 41 linear deviations. Finally, we dropped the assumption of linearity allowing for quadratic deviations.
- We also considered scenarios with treatment-covariate interactions. These scenarios include 4 weak interactions
- $_{43}$ (OR $_{t_x=1}$ /OR $_{t_x=0}=0.82$), 4 strong interactions (OR $_{t_x=1}$ /OR $_{t_x=0}=0.61$), and 2 weak and 2 strong interactions.
- 44 Combining all these different settings resulted in a simulation study of 66 scenarios. The exact settings for each
- scenario are available in the supplementary material.

46 2.2 Individualized risk-based benefit predictions

- 47 All methods assume that a risk prediction model is available and can be used to assign individualized predictions.
- 48 For the simulations we developed the prediction models internally and blinded to treatment using logistic regression
- 49 including main effects for all baseline covariates and treatment. Predictions on individuals were made setting
- 50 treatment to 0.
- 51 The stratified HTE method was suggested as an alternative to traditional subgroup analyses. Patients are
- 52 stratified into equally-sized risk strata—in this case based on risk quartiles. Absolute effects are estimated using
- the differences in event rates between treatments within risk quarters. We considered this approach as a reference,
- expecting it to perform worse than the other candidates, as its objective is not individual benefit prediction.
- 55 We also considered a set of linear methods. We fit separate models within treatment arms using only the
- 56 treatment indicator and the linear predictor of the internal risk prediction model. In the simpler case, we assume
- $_{57}$ a constant relative treatment effect (OR). Absolute benefit is then estimated from $expit(lp+\log(\mathsf{OR}))$, where

- expit $(x)=\frac{e^x}{1+e^x}$ and lp is the linear predictor of the prediction model. A different approach fits a logistic regression using treatment, risk linear predictor and their interaction within each treatment arm. In this case, absolute benefit is estimated from $\exp it(\beta_0+\beta_{lp}lp)-\exp it(\beta_0+\beta_{t_x}+(\beta_{lp}+\beta_*)lp)$. We will refer to this method as the linear interaction approach.
- Finally, we used restricted cubic splines (RCS) to relax the linearity assumption on the effect of the linear predictor [7]. We compared the results for 3, 4 and 5 knots when fitting the splines to introduce increasing flexibility to

the methods considered.

₆₅ 2.3 Evaluation metrics

66 3 Results

67 3.1 Simulations

The model including a constant relative treatment effect had the lowest median RMSE in scenarios where the base case of true constant relative treatment effect (OR = 0.8, N = 4250 and AUC = 0.75) or moderate relative deviations were considered (Figure 1; Panel A). However, when we considered strong linear and quadratic deviations from the base case the linear interaction model performed best (Figure 1; Panels B and C). Only in the case of strong quadratic deviations models including RCS smoothing (3 knots) performed equally well to the linear interaction method. Increasing the number of knots in RCS smoothing resulted in higher error rates across all scenarios. The performance of the adaptive approach was quite comparable with the best performing model in all scenarios.

When we increased the sample size (N = 17000), in all scenarios the model more in agreement with the underlying settings had the lowest error rates. Under the base case of constant relative treatment effects (OR = 0.8), the model including a constant relative treatment effect had the lowest RMSE (Figure 2; Panel A). When introducing moderate and strong linear deviations the linear interaction model performed best (Figure 2; Panels B and C). In the case of true strong quadratic deviations from the base case of constant relative effects, the more flexible RCS smoothing models (3 knots) had the lowest RMSE. Again, the increased flexibility of RCS smoothing with higher number of knots resulted in overfitting and worse performance (Figure 2; Panel D).

When we increased the true prediction AUC to 0.85, models including RCS smoothing had the lowest RMSE when strong quadratic deviations from the base case of true constant relative treatment effects were assumed (Figure 3; Panel D). However, with milder deviations, the linear interaction model had the lowest RMSE with the

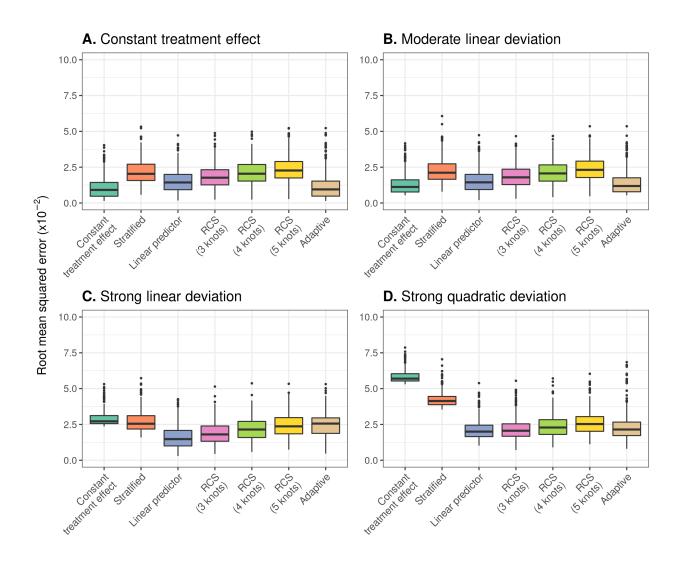


Figure 1: RMSE base case

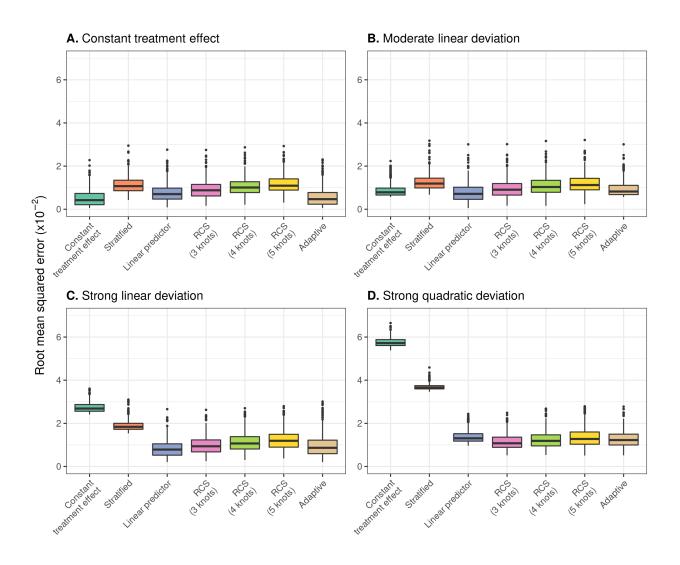


Figure 2: Sample size 17000

- ⁸⁶ RCS smoothing methods (3 knots) being a close second (Figure 3; Panels B and C). Increasing the number of
- knots of RCS smoothing resulted in increased RMSE, which was less pronounced in the case of strong quadratic
- 88 deviations.

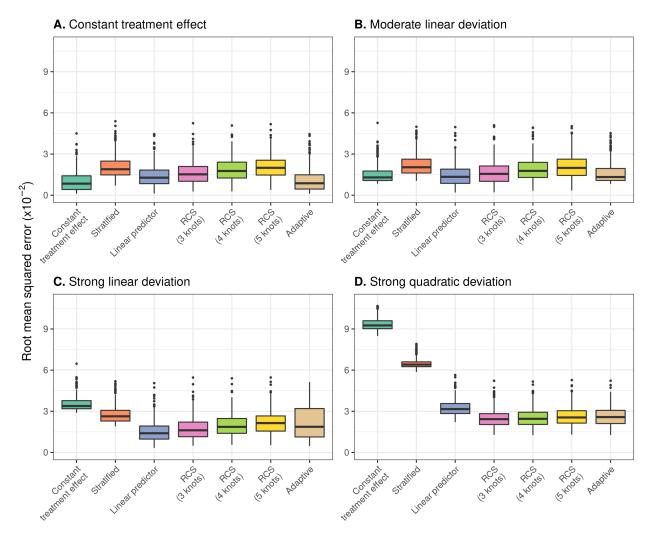


Figure 3: AUC 0.85

- 89 All candidate methods demonstrated comparable discrimination for benefit in all scenarios where linear and
- 90 quadratic deviations from the base case of constant treatment effect were considered (Figure 4). However,
- models including a linear interaction with the risk linear predictor tended to present much lower variability com-
- 92 pared to all other model-based and smoothing approaches. We also observed an increasing trend of discrimination
- 93 for benefit variability with increasing number of restricted cubic spline knots in all scenarios. This is evidence that
- the increased flexibility of these methods often led to overfitting.
- 95 When focusing on calibration for benefit, the linear interaction model had the lowest median ICI for benefit in

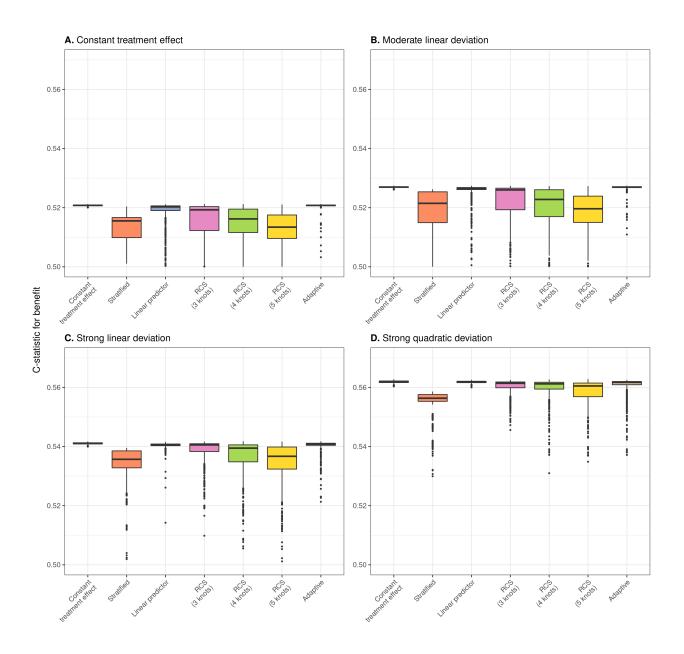


Figure 4: Discrimination for benefit base case.

- the majority of the scenarios except for the scenarios where moderate linear deviations from the base case were
- 97 considered. In that case constant treatment effect models demonstrated the best performance, very comparable
- to the linear interaction model's performance, nonetheless (Figure 5; Panels A, B, and C).

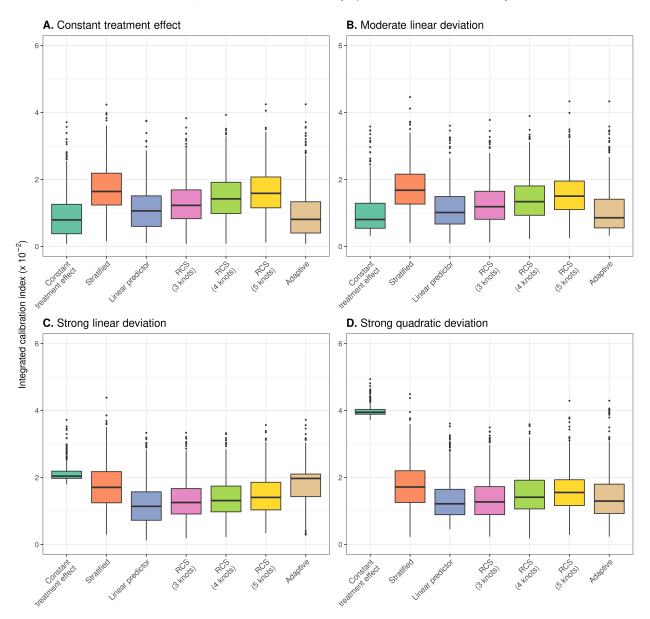


Figure 5: Calibration for benefit base case.

99 3.2 Real data

We demonstrate the different methods for individualizing treatment benefits using data from 30,510 patients with
an acute myocardial infarction (MI) included in the GUSTO-I trial. 10,348 patients were randomized to tissue

plasminogen activator (tPA) treatment and 20,162 were randomized to streptokinase. The outcome of interest was 30-day mortality, recorded for all patients.

In line with (Califf 1997; Steyerberg 2000), we fitted a logistic regression model with 6 baseline covariates, i.e. age,
Killip class, systolic blood pressure, heart rate, an indicator of previous MI, and the location of MI, to predict
30-day mortality risk. A constant effect of treatment was included in the model. When deriving risk predictions
for individuals we set the treatment indicator to 0. More information on model development can be found in the supplement.

We used the risk linear predictor to fit the the proposed methods under study for individualizing absolute benefit predictions. All methods had quite comparable results, in the sense that we predicted increasing benefits for patients with higher baseline risk predictions. In terms of c-for benefit, validated internally, all models had quite comparable performance ranging from 0.519 (RCS smoothing with 3 knots) to 0.542 (RCS smoothing with 4 knots). Similar conclusions could be drawn in terms of ICI-for-benefit which ranged from 0.0039 (linear interaction approach) to 0.0053 (RCS smoothing with 4 knots).

The adaptive approach picked the model with RCS smoothing with 4 knots, which had quite comparable performance to the smooth fit with 5 knots. However, for lower baseline risk these 2 models predicted implausible
benefits and maybe should be avoided when applying such models in practice. The linear interaction model and
the model with RCS smoothing (3 knots) made very similar predictions, while also followed quite closely the
evolution of the stratified estimates. In this case, we observed that even using a simple model with a constant
relative treatment effect can result in very similar benefit predictions as other more complex approaches.

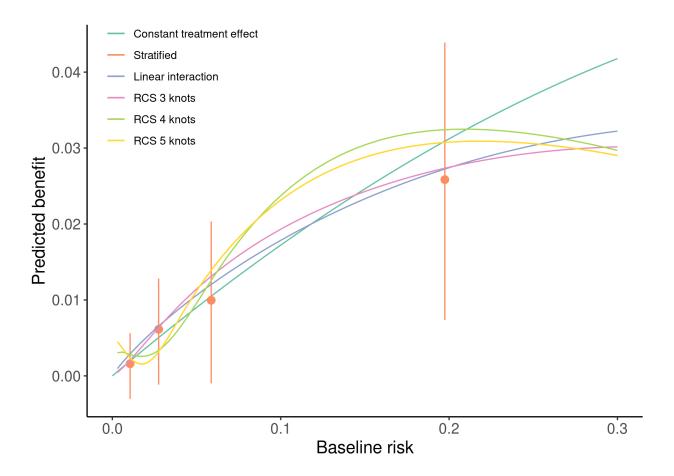


Figure 6: Caption

4 References

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