Smooth risk-based predictive approaches to treatment effect heterogeneity: A simulation study

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Abstract

Objective: Simulation study to compare different risk-based approaches to estimating individualized treatment effects within the RCT setting. **Study Design and Setting:** Starting from a base case scenario that assumes a true constant treatment effect, we considered a total of 66 scenarios for introducing non-constant effects and evaluating methods under different sample sizes and baseline risk prediction performance. We compared 7 methods for predicting absolute benefit: A constant treatment effect model, a risk stratified approach, a model including a linear interaction of the baseline risk linear predictor with treatment, 3 restricted cubic spline smoothing models of increasing flexibility (3, 4 and 5 knots) and an adaptive model selection method based on Akaike's Information Criterion. We evaluated performance using root mean squared error, discrimination for benefit and calibration for benefit (i.e., observed vs. predicted risk difference in treated vs. untreated). **Results:** The model including a linear interaction of the risk linear predictor with treatment had adequate performance that was robust under the majority of the simulation scenarios. Methods using restricted cubic spline smoothing required larger sample sizes and higher prediction AUC to achieve adequate performance. The adaptive approach's performance was comparable to the performance of the best model in each scenario. **Conclusion:** In most cases using a model just including a linear interaction of the risk linear predictor with treatment adequately predicts absolute benefit.

1 Introduction

- Within the setting of patient-centered outcomes research, predictive approaches for assessing heterogeneity of treatment effects (HTE) aim at the development of models predicting either individualized effects or which of two (or more) treatments is better for an individual [1]. In prior work, we divided such methods in three broader categories based on the reference class used for defining patient similarity when making individualized predictions or recommendations [2]. Risk-modeling approaches use prediction of baseline risk as the reference; treatment effect modeling approaches also model treatment-covariate interactions, in addition to risk factors; optimal treatment regime approaches focus on developing treatment assignment rules and therefore rely heavily on modeling treatment effect modifiers. Risk-modeling approaches to predictive HTE analyses provide a viable option in the absence of well-established 10 treatment effect modifiers [3,4]. In simulations, modeling of effect modifiers in the form of treatment-covariate 11 interactions often led to miscalibrated predictions of benefit, while risk-based methods proved quite robust [5]. Most often, risk-modeling approaches are carried out in two steps: first a risk prediction model is developed 13 externally or internally on the entire RCT population, "blinded" to treatment; then the RCT population is stratified using this prediction model to evaluate risk-based treatment effect variation [6]. However, even though estimates 15 at the risk subgroup level are accurate, this does not apply on the individual level, especially for patients with 16 predicted risk at the boundaries of the risk intervals. Therefore, the risk-stratified approach should be used for 17 exploring and presenting an overview of HTE, while inferences on the individual level should be made with caution. 18 We aimed to provide an overview of methods that can be used to move from a risk-stratified approach to
- a continuous one using common smoothing techniques. These methods extend the risk-based framework of predictive HTE analyses to allow predictions on the individual level, within the RCT setting. We carried out a simulation study to compare the performance of these methods under different settings of increasing non-linearity of treatment effects. Finally, we carried out an application on real data as a demonstration of the considered techniques.

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5 2 Methods

26 2.1 Simulation scenarios

- $_{
 m 27}$ In the simulated datasets of the base-case scenario treatment was allocated at random using a 50/50 split.
- For each patient we simulated 8 baseline covariates, where $x_1,\ldots,x_4\sim N(0,1)$ and $x_5,\ldots,x_8\sim B(1,0.2)$.

- ²⁹ Outcomes for patients in the control arm were generated from a logistic regression model including all baseline
- $_{
 m 30}$ covariates. Coefficient values were such, so that the prediction model had an AUC of 0.75 and an event rate
- $_{31}$ of 20% in the control arm was achieved. Outcomes in the treatment arm were created using the same logistic
- 32 regression model, including a constant treatment effect odds ratio (OR) of 0.8. The generated samples of the
- base-case scenario were of size n=4,250 (80% power for the detection of an unadjusted OR of 0.8).
- $_{34}$ We evaluated the effect of sample size considering additional scenarios with sample sizes of 1,064 and 17,000.
- 35 We also evaluated the effect of prediction performance, adjusting the baseline covariate coefficients, so that AUC
- $_{36}$ values of 0.65 and 0.80 were achieved when validating in a simulated dataset of 500,000 patients.
- 37 A true logistic regression model with a constant treatment effect (constant OR) implies that outcome risk in
- the treatment arm is a straight line parallel to the first diagonal on the log-odds scale, with distance equal to
- $\log(\mathsf{OR})$. We assessed the effect of stronger and absent relative treatment effects ($\mathsf{OR}=0.5$ or $\mathsf{OR}=1$). We
- 40 also relaxed the assumption that the line should be parallel to the diagonal, considering moderate and stronger
- 41 linear deviations. Finally, we dropped the assumption of linearity allowing for quadratic deviations.
- We also considered scenarios with treatment-covariate interactions. These scenarios include 4 weak interactions
- $_{43}$ (OR $_{t_x=1}$ /OR $_{t_x=0}=0.82$), 4 strong interactions (OR $_{t_x=1}$ /OR $_{t_x=0}=0.61$), and 2 weak and 2 strong interactions.
- 44 Combining all these different settings resulted in a simulation study of 66 scenarios. The exact settings for each
- scenario are available in the supplementary material.

46 2.2 Individualized risk-based benefit predictions

- 47 All methods assume that a risk prediction model is available and can be used to assign individualized predictions.
- 48 For the simulations we developed the prediction models internally and blinded to treatment using logistic regression
- 49 including main effects for all baseline covariates and treatment. Predictions on individuals were made setting
- 50 treatment to 0.
- 51 The stratified HTE method was suggested as an alternative to traditional subgroup analyses. Patients are
- 52 stratified into equally-sized risk strata—in this case based on risk quartiles. Absolute effects are estimated using
- the differences in event rates between treatments within risk quarters. We considered this approach as a reference,
- expecting it to perform worse than the other candidates, as its objective is not individual benefit prediction.
- 55 We also considered a set of linear methods. We fit separate models within treatment arms using only the
- 56 treatment indicator and the linear predictor of the internal risk prediction model. In the simpler case, we assume
- $_{57}$ a constant relative treatment effect (OR). Absolute benefit is then estimated from $expit(lp+\log(\mathsf{OR}))$, where

- $\exp \operatorname{it}(x) = \frac{e^x}{1+e^x}$ and Ip is the linear predictor of the prediction model. A different approach fits a logistic regression using treatment, risk linear predictor and their interaction within each treatment arm. In this case, absolute benefit is estimated from $expit(\beta_0 + \beta_{lp}lp) - expit(\beta_0 + \beta_{t_x} + (\beta_{lp} + \beta_*)lp)$. We will refer to this method as the linear interaction approach.
- Finally, we used restricted cubic splines (RCS) to relax the linearity assumption on the effect of the linear predictor [7]. We compared the results for 3, 4 and 5 knots when fitting the splines to introduce increasing flexibility to 63 the methods considered.

2.3 **Evaluation metrics**

3 Results

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3.1 Simulations

Under the base case of constant relative treatment effect, the model assuming a constant treatment effect had the lowest median RMSE, regardless of true prediction AUC and sample size. Linear interaction models demonstrated comparable performance. Among the RCS smoothing methods, the one fitted with 3 knots always performed best, while the increased flexibility achieved when increasing the knots resulted in overfitting and worse performance. 71 The adaptive approach under all scenarios performed similar to the model with smaller RMSE in all scenarios. When we introduced deviations from the base case of constant relative treatment effects, while keeping fixed both the sample size (N = 4250) and the true prediction AUC (0.75) the linear interaction model had the lowest 74 RMSE (Figure 1; Panels A, D, and G). When these deviations were moderate (Figure 1; Panel A) the constant treatment effect model had comparable performance to the linear interaction model. This can be attributed to the fact that such deviations are quite mild and absolute benefits maintain similar patterns across baseline risk. On the contrary, when strong quadratic deviations were considered the constant effect model's RMSE sharply increased, while the more flexible method of RCS smoothing (3 knots) preformed very well (Figure 1; Panel G). Again, increasing the number of knots increased RMSE, indicating overfitting. When we increased the true prediction AUC to 0.85, models including RCS smoothing had the lowest RMSE

when strong quadratic deviations from the base case of constant relative treatment effects were assumed (Figure 1; Panel H). However, with milder deviations, the linear interaction model had the lowest RMSE with the RCS

smoothing methods (3 knots) being a close second (Figure 1; Panels B and E). Increasing the number of knots of RCS smoothing resulted in increased RMSE, which was less pronounced in the case of strong quadratic deviations.

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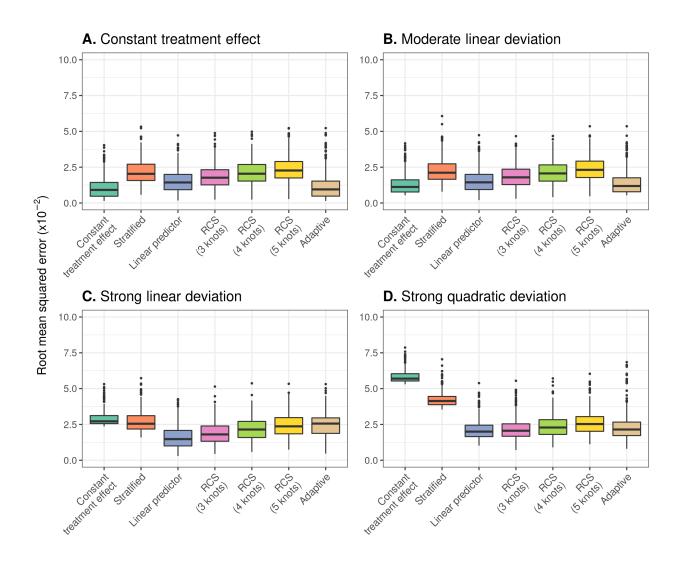


Figure 1: RMSE base case

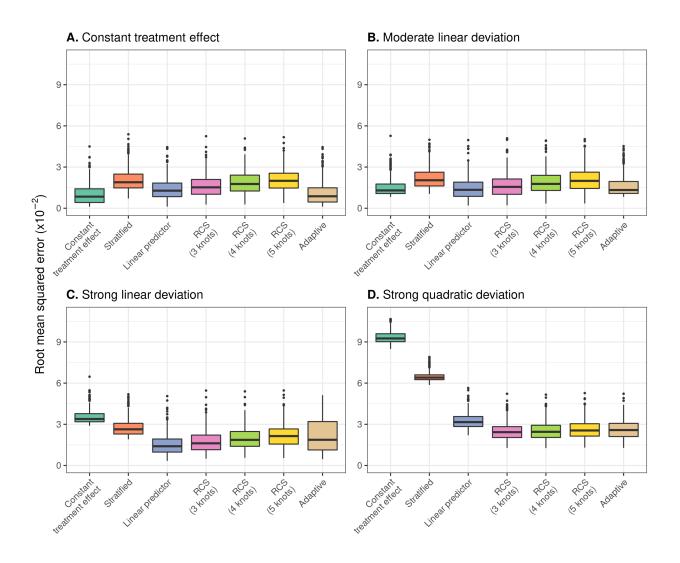


Figure 2: AUC 0.85

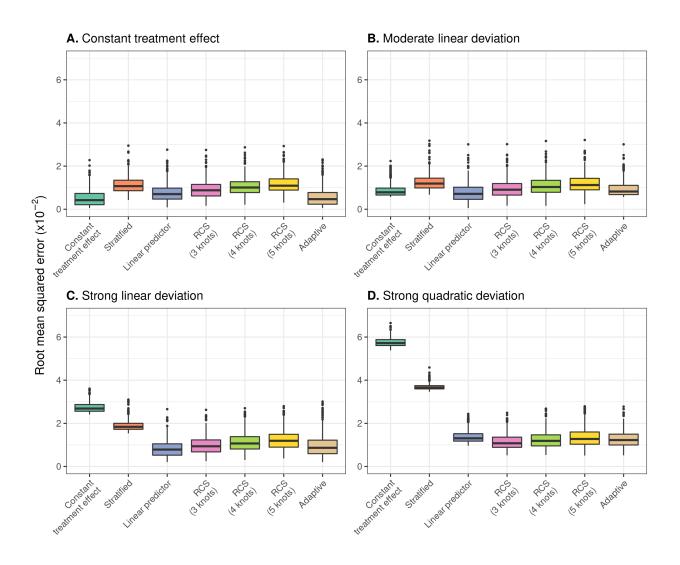


Figure 3: Sample size 17000

- 86 We observed similar results when we increased the sample size to 17000, while keeping the true prediction AUC
- constant at 0.75 (Figure 1; Panels C, F, and I).
- 88 When focusing on the different scenarios where true treatment-covariate interactions were considered all methods
- 89 had similar RMSE performance. In case of strong treatment-covariate interactions the constant effect model had
- 90 slightly increased RMSE (0.096; [0.092, 0.103]) compared to the other methods. The linear interaction model
- with the risk linear predictor had the lowest RMSE (0.088; [0.08, 0.095]).
- 92 All candidate methods demonstrated comparable discrimination for benefit in all scenarios where linear and
- 93 quadratic deviations from the base case of constant treatment effect were considered (Figure 4). However,
- models including a linear interaction with the risk linear predictor tended to present much lower variability com-
- 95 pared to all other model-based and smoothing approaches. We also observed an increasing trend of discrimination
- 96 for benefit variability with increasing number of restricted cubic spline knots in all scenarios. This is evidence that
- 97 the increased flexibility of these methods often led to overfitting.
- 98 When focusing on calibration for benefit, the linear interaction model had the lowest median ICI for benefit in
- 99 the majority of the scenarios except for the scenarios where moderate linear deviations from the base case were
- 100 considered. In that case constant treatment effect models demonstrated the best performance, very comparable
- to the linear interaction model's performance, nonetheless (Figure 5; Panels A, B, and C).

02 3.2 Real data

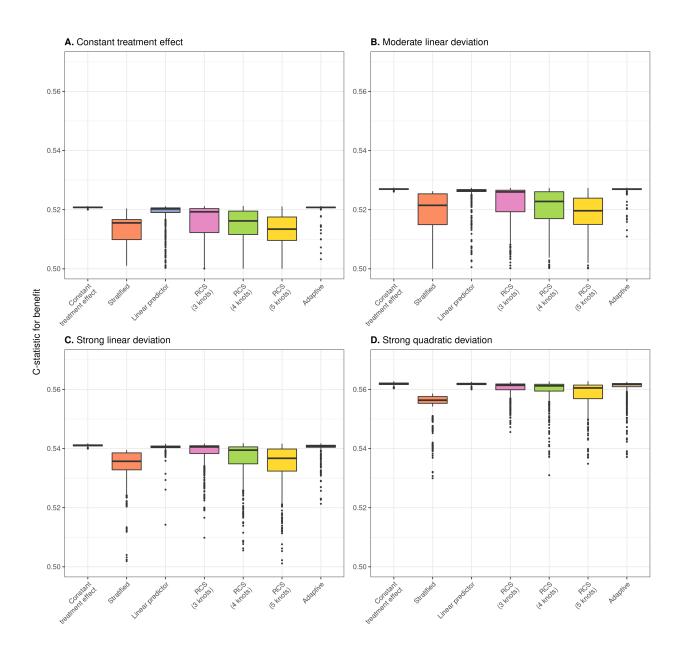


Figure 4: Discrimination for benefit base case.

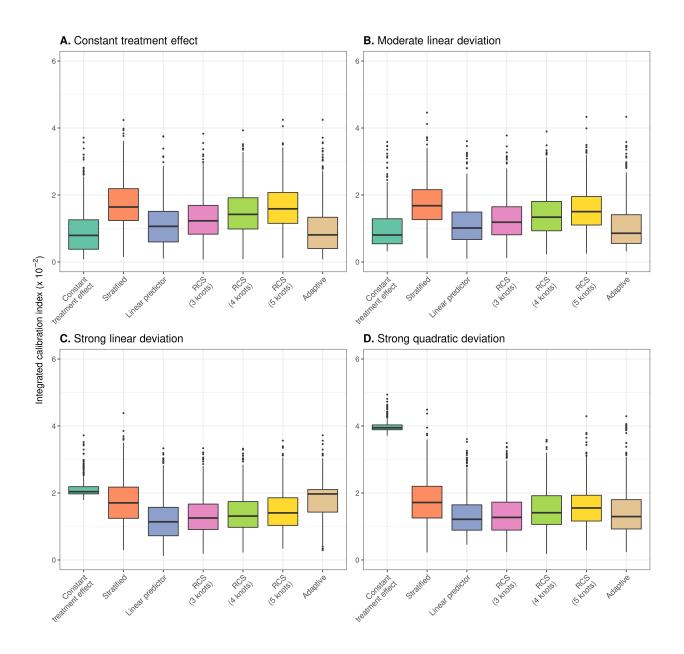


Figure 5: Calibration for benefit base case.

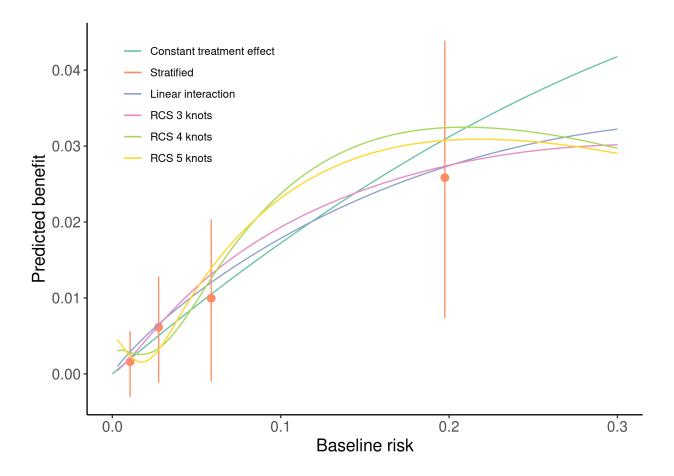


Figure 6: Caption

3 4 References

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