

Model Predictive Control Project

Rubric Points

- **The Model:**

In this project, kinematic model is used which is based on vehicles kinematics. The kinematic model takes into consideration the following:

1. Vehicle's x-coordinate(x)
2. Vehicle's y-coordinate(y)
3. Vehicle's orientation (ψ)
4. Vehicles velocity(v)
5. Cross-track error(cte)
6. Orientation error($epsi$)

as state. These are described by the following equations:

$$x_{t+1} = x_t + v_t * \cos(\psi_t) * dt$$

$$y_{t+1} = y_t + v_t * \sin(\psi_t) * dt$$

$$\psi_{t+1} = \psi_t + \frac{v_t}{L_f} * \delta_t * dt$$

$$v_{t+1} = v_t + a_t * dt$$

$$cte_{t+1} = f(x_t) - y_t + (v_t * \sin(e\psi_t) * dt)$$

$$e\psi_{t+1} = \psi_t - \psi_{des_t} + (\frac{v_t}{L_f} * \delta_t * dt)$$

Here t denotes the previous time-step and $t+1$ denotes the current time-step. The model uses the above equations to calculate the state $[x, y, \psi, v, cte, e\psi]$ and actuations (throttle and steering angle) for the current time-step from the previous time-step.

- **Time-step Length and Elapsed Duration (N & dt):**

The values chosen for N and dt are:

N	dt
20	0.05

This combination of values was chosen by trial and error method. The combination was chosen because it produced considerably stable behavior of the vehicle.

- **Polynomial Fitting and MPC Preprocessing:**

A three-degree polynomial curve is chosen because two-degree polynomial would not fit properly to the curves and zig-zag turns of the road, and a four or five-degree polynomial may lead to over-fitting as well as overhead computational cost.

The waypoints are preprocessed by transforming them to vehicle's coordinate system (lines 105 – 110 in *main.cpp*). This is done because now fitting the polynomial to the waypoints becomes simple as the vehicle is at origin (0,0) and orientation angle ψ is zero.

- **Model Predictive Control with Latency:**

The MPC handles a 100 milliseconds latency delay. This delay is introduced in the beginning, before calling `MPC::Solve()` in lines 123 – 129 of *main.cpp*. We estimate the new state $[x, y, \psi, v, cte, e\psi]$ of the vehicle after 100 milliseconds and then proceed with calculations in `MPC::Solve()` so that we predict the actuations after 100 milliseconds.

An alteration in the equation of ϵ which, as given in the lesson as

$$\epsilon = (\psi_0 - \psi_{sides0}) - v \cdot \Delta / L_f \cdot dt$$

is changed to

$$\epsilon = (\psi_{sides0} - \psi_0) - v \cdot \Delta / L_f \cdot dt$$

in accordance to [this](#) thread in discussion forum.