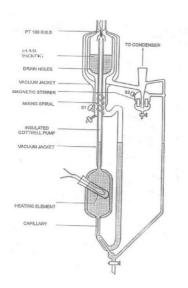
1 Objectives

- 1. Determine the vapour-liquid equilibrium data for the acetone (A) benzene (B) homogeneous mixture
- 2. Check the thermodynamic consistency of the data using the Gibbs Duhem Equation
- 3. Present the thermodynamic characteristics and constants of Van-Laar equation for the system

2 Procedure

- 1. Prepare 9 solutions of acetone and benzene having different volume fraction of acetone.
- 2. Measure the refractive index of the solutions using a refractometer, take three readings for each solution of acetone and benzene.
- 3. Now prepare a solution by adding approximately 480 ml of acetone and 120 ml of benzene so that the solution level is same as the level of cotrell pump.
- 4. Now pour the solution in the still and put the voltage value to 120V and wait for it to reach a steady temperature.
- 5. Put the voltage value to 80-85V when it starts boiling.
- 6. Dispose off the liquid and vapor solution collected by cotrell pump and condenser i.e purge the obtained liquid and vapor solution once..
- 7. Collect the liquid and vapour solution and put the voltage value to zero and measure their refractive index.
- 8. Remove some amount of solution from the still and add some benzene to it and set the voltage value to 120 and then repeat step 5, 6.
- 9. Take four such readings by removing some amount of the solution and adding the same amount of the benzene to it every time.

3 Set-Up Assembly



4 Results

4.1 Raw Data

Table 1: Properties of Components

Property	Acetone	Benzene
Density	729 kg/m ³	879 kg/m ³
Molar mass	58.08 g	78.11 g
Boiling Point	56.2 °C	81.1 °C
R.I at 30 °C	1.3545	1.4951

Table 2: Calibration Curve Data

Volume of Acetone (ml)	Volume of Benzene (ml)	Average Refractive Index
1	0	1.35797411
0.9	0.1	1.37092574
0.8	0.2	1.38415097
0.7	0.3	1.39765855
0.6	0.4	1.41145763
0.5	0.5	1.42555774
0.4	0.6	1.43996884
0.3	0.7	1.45470134
0.3	0.8	1.46976611
0.1	0.9	1.48517451
0	1	1.50093845

Table 3: Experimental Data

Sample	Temp	Vapour phase				Liqu	iid Phase		
ID	_	RI (1)	RI(2)	RI(3)	Average RI	RI(1)	RI(2)	RI(3)	Average RI
1	58.2	1.376541	1.375044	1.375344	1.375643	1.3827	1.381831	1.385324	1.38329467
						29			
2	59.9	1.395104	1.396002	1.395803	1.39563633	1.4037	1.407579	1.408178	1.40651467
						87			
3	60.8	1.404485	1.399895	1.400693	1.401691	1.4343	1.436621	1.436222	1.435723
						26			
4	63.0	1.407679	1.414266	1.414665	1.41220333	1.4440	1.441611	1.443507	1.44304133
						06			
5	65.2	1.431531	1.431831	1.429635	1.430999	1.4494	1.450194	1.450793	1.45016067
						95			
6	68.1	1.442809	1.445703	1.446701	1.445071	1.4730	1.473747	1.472649	1.473148
						48			

4.2 Derived Data

4.2.1 Mol Fraction from Vol Fraction

We calculated the mole fractions from the volume ratios as follows:

$$\frac{V_A}{V_B} = \beta \text{ (say)}$$

$$\frac{m_A/\rho_A}{m_B/\rho_B} = \beta$$

$$\frac{m_A}{m_B} = \beta \frac{\rho_A}{\rho_B}$$

$$\frac{n_A M_A}{n_B M_B} = \beta \frac{\rho_A}{\rho_B}$$

$$\frac{n_A}{n_B} = \beta \frac{\rho_A}{\rho_B} \frac{M_B}{M_A}$$

$$\Rightarrow n_B = \frac{\rho_B M_A}{\beta \rho_A M_B} n_A$$

$$\therefore x_A = \frac{n_A}{n_A + n_B}, \text{ we get :}$$

$$x_A = \frac{n_A}{n_A + \frac{\rho_B M_A}{\beta \rho_A M_B}} n_A = \frac{\beta \rho_A M_B}{\beta \rho_A M_B + \rho_B M_A}$$

$$(1)$$

For the first value of $\beta = 9$, the above formula yielded $x_A = 0.909$. The *average* refractive index (RI) was plotted against x_A and a linear regression was carried out.

Table 4: Mole fraction calculated from linear regression

Sample ID	Refractive Index		Mole	Mole	
	Vapour	Liquid	fraction of Vapour of	fraction of Liquid of	
			Acetone	Acetone	
1	1.375643	1.38329467	0.87641051	0.822889	
2	1.39563633	1.40651467	0.73656211	0.66047087	
3	1.401691	1.435723	0.69421122	0.45616584	
4	1.41220333	1.44304133	0.62068006	0.40497592	
5	1.430999	1.45016067	0.48920905	0.35517795	
6	1.445071	1.473148	0.3907789	0.19438727	

4.2.2 Saturation Pressure from Antoine's Equation:

The form of Antoine's equation obtained from Smith and Van-Ness is as follows:

$$ln Psat(kPa) = A - \frac{B}{T(^{\circ}C) + C}$$
(2)

The constants for A (acetone) are: A = 14.3145; B = 2756.22; C = 228.060 while for B (benzene) they are: A = 13.7819; B = 2726.81; C = 217.572

4.2.3 Activity Coefficient from Modified Raoult's Law:

The statement of the Modified Raoult's Law reads:

$$x_{A}\gamma_{A}P_{A}^{sat} = y_{A}\pi_{A}$$

$$\implies \gamma_{A} = \frac{y_{A}\pi_{A}}{x_{A}P_{A}^{sat}}$$
(3)

Table 5: Activity Coefficient and Saturation Pressure

Sample ID	Mole Fraction of		Temperature (°C)	Saturation Pressure	Saturation Pressure	Activity coefficient	Activity coefficient
	Acetone in	Acetone		of	of	of	of_
	Vapour	In Liquid		Acetone	Benzene	Acetone	Benzene
	Phase (y1)	Phase (x1)		(atm)	(atm)	(γ ₁)	(γ_2)
1	0.87641051	0.822889	58.2	1.08114159	0.4909635	0.98510777	1.42130314
2	0.73656211	0.66047087	59.9	1.14474676	0.52102362	0.97419587	1.48916831
3	0.69421122	0.45616584	60.8	1.17961343	0.5375436	1.29011718	1.04602332
4	0.62068006	0.40497592	63.0	1.26842971	0.57975479	1.2082928	1.09957988
5	0.48920905	0.35517795	65.2	1.36250982	0.62466361	1.01090151	1.26811053
6	0.3907789	0.19438727	68.1	1.49493862	0.68820318	1.34474496	1.09883362

4.2.4 Van-Laar Constants from Data:

The Van-Laar constants are given by:

$$a = \log \gamma_A \left[1 + \frac{x_B \log \gamma_B}{x_A \log \gamma_A} \right]^2$$

$$b = \log \gamma_B \left[1 + \frac{x_A \log \gamma_A}{x_B \log \gamma_B} \right]^2$$
(4)

Table 6: Calculation of excess Gibbs free energy

Sample ID	Mole Fraction of Acetone in Liquid Phase (x1)	Mole Fraction of Benzene In Liquid Phase (x2)	Activity coefficient of Acetone (y1)	Activity coefficient of Benzene (γ ₂)	G _E /RT =x ₁ lny ₁ + x ₂ lny ₂
1	0.822889	0.177111	0.98510777	1.42130314	0.04992084
2	0.66047087	0.33952913	0.97419587	1.48916831	0.11793991
3	0.45616584	0.54383416	1.29011718	1.04602332	0.14067069
4	0.40497592	0.59502408	1.2082928	1.09957988	0.13310942
5	0.35517795	0.64482205	1.01090151	1.26811053	0.15701433
6	0.19438727	0.80561273	1.34474496	1.09883362	0.13350677

5 Observations:

- The refractive index of the mixture shows a linear relation with the volume (and thus mole) fraction of acetone. As the mol fraction of acetone decreases, the refractive index increases.
- As the mole fraction of acetone (more volatile component) decreases, the VLE temperature increases.

6 Hypothesis & Conclusion:

One hypothesis made at the start was that data follows thermodynamic consistency. The way to check that is by the integral test (Gibb's-Duhem Equation):

$$\int_0^1 \ln \frac{\gamma_A}{\gamma_B} dx_a = 0 \tag{5}$$

To that extent, $\ln (\gamma_a/\gamma_b)$ v/s x_a was plotted and the area bound was measured. The value deviated from 0 and thus, thermodynmic consistency is **not** followed.

Some part might be because of experimental error, and it could be rectified by taking more data points.

Another aim was to calculate the Van-Laar constants. For experiment run (ie each VLE established), the constants were calculated using the formulae mentioned above. The values came out as:

Table 7: Van-Laar Constants calculated from data

Temperature of VLE	a	b
58.2	-0.24528301	0.22597255
59.9	-1.21972077	0.30300295
60.8	0.37331584	1.48697511
63	0.57097702	0.52717326
65.2	18.02423931	0.24962263
68.1	1.5925	0.29139089

It is expected that the Van-Laar constants should stay the same irrespective of the temperature/mol fraction of the VLE for the same mixture components. However, there is a clear deviation in both a & b once again proving thermodynamic inconsistency.

7 Solve

```
[1]: import numpy as np
import matplotlib.pyplot as plt
from sklearn.linear_model import LinearRegression
from scipy import interpolate
```

- A = Acetone
- B = Benzene

```
[2]: rho_A = 729 # kg/m^3
rho_B = 879 # kg/m^3

# ? Molecular weight
M_A = 58.08 # g/mol
M_B = 78.11 # g/mol
```

7.1 Calibration curve

```
[3]:
         # Volume ratio
         VR = [9/1, 8/2, 7/3, 6/4, 5/5, 4/6, 3/7, 2/8, 1/9]
         VR = np.array(VR)
         VR = VR * (rho_A / M_A) / (rho_B / M_B)
         VR_A = [(r / (r+1.0)) \text{ for } r \text{ in } VR]
         VR_A = [1.0, *VR_A, 0.0]
         \# x = [0, 0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, 1]
         x_A = np.array(VR_A)
         print("Mole fraction of Acetone: ", x_A)
         RI_1 = [1.351791, 1.364765, 1.38243, 1.400394, 1.416661, 1.437419,
         1.443108, 1.454685, 1.471052, 1.484525, 1.491711]
         RI_2 = [1.351891, 1.364765, 1.382929, 1.399296, 1.415763,
         1.43732, 1.445004, 1.4472, 1.471551, 1.483427, 1.492709]
         RI_3 = [1.351691, 1.364066, 1.383827, 1.400593, 1.417459, 1.440513,
         1.443607, 1.454884, 1.471351, 1.484425, 1.49201]
         y = np.mean([RI_1, RI_2, RI_3], axis=0)
```

```
Mole fraction of Acetone: [1. 0.90940653 0.81689935 0.72241717 0.62589606 0.5272693 0.42646723 0.32341707 0.21804277 0.11026481 0. ]
```

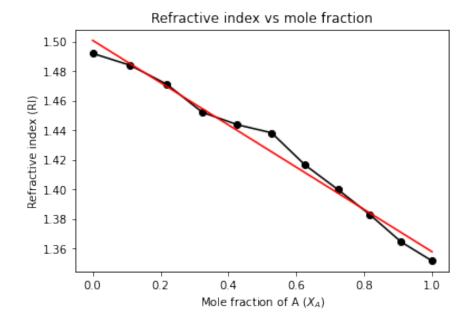
```
[4]: reg = LinearRegression().fit(x_A.reshape(-1, 1), y)
m = reg.coef_
c = reg.intercept_
```

```
y_pred = m*x_A + c

plt.title('Refractive index vs mole fraction')
plt.xlabel('Mole fraction of A ($X_A$)')
plt.ylabel('Refractive index (RI)')
plt.plot(x_A, y, 'o-k')
plt.plot(x_A, y_pred, '-r')

print(f"slope: {reg.coef_}, intercept: {reg.intercept_}")
```

slope: [-0.14296434], intercept: 1.5009384465620594



```
T = [58.2, 59.9, 60.8, 63.0, 65.2, 68.1]
T = np.array(T)
T += 273.15

RI_vap_1 = [1.376541, 1.395104, 1.404485, 1.407679, 1.431531, 1.442809]
RI_vap_2 = [1.375044, 1.396002, 1.399895, 1.414266, 1.431831, 1.445703]
RI_vap_3 = [1.375344, 1.395803, 1.400693, 1.414665, 1.429635, 1.446701]
RI_vap = np.mean([RI_vap_1, RI_vap_2, RI_vap_3], axis=0)
Y_A = (RI_vap - c) / m
Y_B = 1 - Y_A
RI_liq_1 = [1.382729, 1.403787, 1.434326, 1.444006, 1.449495, 1.473048]
RI_liq_2 = [1.381831, 1.407579, 1.436621, 1.441611, 1.450194, 1.473747]
RI_liq_3 = [1.385324, 1.408178, 1.436222, 1.443507, 1.450793, 1.472649]
```

```
RI_liq = np.mean([RI_liq_1, RI_liq_2, RI_liq_3], axis=0)
X_A = (RI_liq - c) / m
X_B = 1 - X_A

print("Average mole fraction of vapour A (at various temp):", Y_A)
print("Average mole fraction of liquid A (at various temp):", X_A)
```

Average mole fraction of vapour A (at various temp): [0.87641051 0.73656211 0.69421122 0.62068006 0.48920905 0.3907789]

Average mole fraction of liquid A (at various temp): [0.822889 0.66047087 0.45616584 0.40497592 0.35517795 0.19438727]

7.2 Calculate P_{sat}

• Antoine Equation: $log_{10}(P) = A - \frac{B}{T+C}$

7.2.1 Acetone

- A = 4.42448
- B = 1312.253
- C = -32.445
- reference: Ambrose, Sprake, et al., 1974

7.2.2 Benzene

- A = 4.725
- B = 1660.652
- C = -1.461
- reference: Eon, Pommier, et al., 1971

```
[6]: log10_Psat_A = 4.424 - 1312.25 / (T - 32.44)
Psat_A = np.power(10, log10_Psat_A)
print("Saturation pressure of Acetone:", Psat_A)

log10_Psat_B = 4.725 - 1660.65 / (T - 1.46)
Psat_B = np.power(10, log10_Psat_B)
print("Saturation pressure of Benzene:", Psat_B)
```

Saturation pressure of Acetone: [1.08114159 1.14474676 1.17961343 1.26842971 1.36250982 1.49493862]
Saturation pressure of Benzene: [0.49096359 0.52102362 0.5375436 0.57975479 0.62466361 0.68820318]

```
[7]: gamma_A = (Y_A * 1) / (Psat_A * X_A)
ln_gamma_A = np.log(gamma_A)
print("ln(gamma_A):", ln_gamma_A)

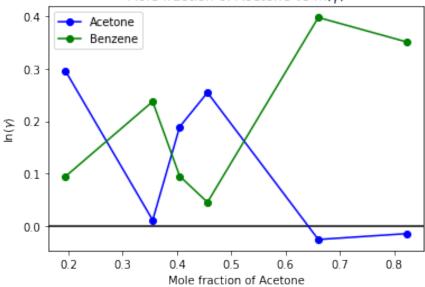
# Psat_B *= 1.3
gamma_B = (Y_B * 1) / (Psat_B * X_B)
```

```
ln_gamma_B = np.log(gamma_B)
    print("ln(gamma_B):", ln_gamma_B)

ln(gamma_A): [-0.01500423 -0.0261429     0.25473305     0.18920846     0.01084251
    0.2962044 ]
    ln(gamma_B): [0.35157418     0.39821779     0.04499565     0.09492817     0.23752803     0.09424926]

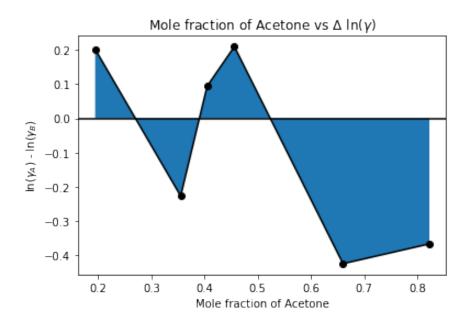
[8]:    plt.axhline(y=0, color='k')
    plt.plot(X_A, ln_gamma_A, 'o-b', label="Acetone")
    plt.plot(X_A, ln_gamma_B, 'o-g', label="Benzene")
    plt.legend()
    plt.xlabel("Mole fraction of Acetone")
    plt.ylabel("ln($\gamma$)")
    plt.title("Mole fraction of Acetone vs ln($\gamma$)")
    plt.show()
```

Mole fraction of Acetone vs $ln(\gamma)$



```
delta_ln_gamma = ln_gamma_A-ln_gamma_B

plt.axhline(y=0, color='k')
   plt.plot(X_A, delta_ln_gamma, 'o-k')
   plt.xlabel("Mole fraction of Acetone")
   plt.ylabel("ln($\gamma_A$) - ln($\gamma_B$)")
   plt.title("Mole fraction of Acetone vs $\Delta$ ln($\gamma$)")
   plt.fill_between(X_A, 0, delta_ln_gamma)
   plt.show()
```



```
spline = interpolate.interp1d(X_A, delta_ln_gamma, kind='cubic')

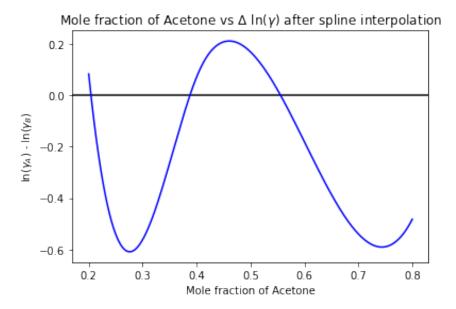
x_inter = np.linspace(0.2, 0.8, 300)
y_inter = spline(x_inter)

plt.axhline(y=0, color='k')
plt.plot(x_inter, y_inter, '-b')
plt.title("Mole fraction of Acetone vs $\Delta$ ln($\gamma$) after spline_\text{\text{\text{\text{otter}}}}
interpolation")
plt.xlabel("Mole fraction of Acetone")
plt.ylabel("ln($\gamma_A$) - ln($\gamma_B$)")

area = 0
for i in range(len(x_inter)-1):
    area += (y_inter[i])*(x_inter[i+1]-x_inter[i])

print("Area:", area)
```

Area: -0.14447233309865778



```
[11]: alpha = (X_B * ln_gamma_B) / (X_A * ln_gamma_A)
    a = ln_gamma_A * (1 + alpha)**2
    b = ln_gamma_B * (1 + 1.0/alpha)**2

print(f"Van Laar coeffecients")
    print(f"a: {a}")
    print(f"b: {b}")
```

Van Laar coeffecients

a: [-0.24528301 -1.21972077 0.37331584 0.57097702 18.02423931 1.5925]

b: [0.22597255 0.30300295 1.48697511 0.52717326 0.24962263 0.29139089]

```
[12]: residual = X_A * ln_gamma_A + X_B * ln_gamma_B
print('Residual: ', residual)
```

Residual: [0.04992084 0.11793991 0.14067069 0.13310942 0.15701433 0.13350677]

```
[13]: K_A = Y_A / X_A print ("K_A: " , K_A)
```

K_A: [1.06504098 1.11520756 1.52183956 1.5326345 1.37736322 2.01031122]