

(a) DISAPROVE

For separable ~~the~~ filters, it can be represented as product of two vectors.

$$\begin{bmatrix} 0 & 1 & 0 \\ 1 & -4 & 1 \\ 0 & 1 & 0 \end{bmatrix}$$

$$= A \times B$$

$$= \begin{bmatrix} a \\ b \\ c \end{bmatrix} \times \begin{bmatrix} c & d & f \end{bmatrix}$$

$$= \begin{bmatrix} ac & ad & af \\ bc & bd & bf \\ ec & ed & ef \end{bmatrix}$$

$$ac = 0 \quad (a = 0 \text{ or } c = 0) \quad af = 0 \quad (a = 0 \text{ or } f = 0)$$

But if $a = 0$ then $ad \neq 1$, if $f = 0$, $bf \neq 1$

So no vector A & B exist
∴ Laplacian is not a separable
filter.

(b) If a filter mask is a separable
filter, we can express it as
1-D convolution by associativity
of convolution.

But Laplacian Mask is not a
separable Mask.