Sorting Algorithms and Complexity

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Outline

- Intuitive Sorting
- Sorting Algorithms
- Time Complexity





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Activity: Sort your cards

- Layout the cards in front of you.
- Using some technique which looks at one or two cards at once, put the cards into sorted order.
- Repeat this a few times, until you are conscious of how you do it.





Activity: How did you sort?

- Think about how you sorted your cards.
- Try to write down the general idea about how it was done.





Activity: Produce Pseudocode of your technique

- Create a directory labs/week10
- In this directory, using your favorite editor, create a file named mysort.txt
- Write pseudocode to describe the sorting method that you used.
- Compare sorting methods with your neighbors. Who's sort looks better?





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- Some of the first algorithms to be studied in terms of complexity were sorting algorithms.
- Many "official" sorting algorithms exist.
- These include:
 - Selection Sort
 - Bubble Sort
 - Merge Sort





Selection Sort

```
selction_sort(ar)
  for i = 0 to ar
    min=i
    for j = i+1 to ar.size()-1
        if ar[j] < ar[min]
            min = j
        end if
    end for
    swap ar[i] and ar[j]
end for</pre>
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Carry out selection sort with your cards.





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- Carry out selection sort with your cards.
- Intuitively, what is selection sort doing?



Bubble Sort

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bubble_sort(ar)
    do
        swapped = false
        for i=0 to ar.size()-2
        if ar[i+1] < ar[i]
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    while swapped</pre>
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- Carry out selection sort with your cards.
- Intuitively, what is bubble sort doing?



Merge Sort

```
merge sort(ar)
    if ar.size() <= 1
        ret.un
    end if
    mid = ar.size() / 2
    merge_sort(ar[0..mid])
    merge_sort(ar[mid+1 .. ar.size()-1)
merge(left, right)
    While left and right are not empty
        take the smallest of the first element in
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Activity: Compare Sorting Algorithms

Which sorting method seemed closer to what you did?





Activity: Compare Sorting Algorithms

- Which sorting method seemed closer to what you did?
- Which sorting method seemed more efficient?





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- We typically evaluate an algorithm based on how long it will take to execute.
- The standard is to rate the algorithm by the number of steps necessary to solve a problem of n size.





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- Usually, we can't find the exact f(n), and even if we could, this would not be all that meaningful.
- We instead compute an asymptotic bound.
- An algorithm is O(g(n)) if $f(n) \le cg(n)$ for some constant c for all n above some threshold.
- Intuitively, O(g(n)) gives us the "worst case" run time.





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 - n log n O(nlg(n))
 - Quadratic O(n²)
 - Exponential O(2ⁿ)
- Using a spreadsheet, let's see how these functions relate to each other.





Selection Sort Complexity

Find the time complexity of the following:

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selction_sort(ar)
  for i = 0 to ar
    min=i
    for j = i+1 to ar.size()-1
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    end for
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  end for</pre>
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Bubble Sort Complexity

Find the time complexity of the following:

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bubble_sort(ar)
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       swapped = false
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        if ar[i+1] < ar[i]
            swap ar[i+1] and ar[i]
            swapped = true
        end if
       end for
   while swapped</pre>
```





Merge Sort Complexity

Find the time complexity of the following:

```
merge_sort(ar)
    if ar.size() <= 1
        ret.un
    end if
    mid = ar.size() / 2
    merge_sort(ar[0..mid])
    merge sort(ar[mid+1 .. ar.size()-1)
merge(left, right)
    While left and right are not empty
        take the smallest of the first element in
        left and right
    end while
                                   4 □ > 4 □ > 4 □ > 4 □ > ...
```

Activity: What is the complexity of your search algorithm?

- Compute the time complexity of your own sorting algorithm.
- Include your runtime and justification of your complexity in your text file.





Activity: Code a Sorting Algorithm

- Code your favorite sorting algorithm.
- Your program should do the following:
 - Ask for 10 numbers, which it adds to a vector.
 - Run your sorting algorithm.
 - Print the sorted vector.



