## Graphing and Projection Using Linear Functions

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## **Linear Functions**

• Recall that a linear pattern can be written recursively:

$$P_n = P_{n-1} + (P_2 - P_1)$$

• Suppose we carry this out for some arbitrary number of iterations:

$$P_x = P_{x-1} + (P_2 - P_1)$$

$$P_x = (P_{x-2} + (P_2 - P_1)) + (P_2 - P_1)$$

$$P_x = ((P_{x-3} + (P_2 - P_1)) + (P_2 - P_1)) + (P_2 - P_1)$$
...
$$P_x = ((P_1 + \ldots + (P_2 - P_1)) + (P_2 - P_1)) + (P_2 - P_1)$$

• Regrouping by using the associative property of addition, we get:

$$P_x = P_1 + (P_2 - P_1) + \ldots + (P_2 - P_1)$$

Where  $(P_2 - P_1)$  is repeated x times.

• By the definition of multiplication, this gives us:

$$P_x = P_1 + x(P_2 - P_1)$$

• Moreover, because each iteration increases n by 1, we can make the claim that  $P_2 - P_1$  is the slope because:

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

• This gives us:

$$P_x = P_1 + xm$$

• If we want to standardize the starting point to be where x=0 on a cartesian plane, we can do this as:

$$P_x = b + xm$$

Where  $b = P_0$ .

• This gives us the familiar equation of a line:

$$y = mx + b$$

• Of course, b is rarely given to us, so we must solve for this:

$$y = mx + b$$
$$y - b = mx$$
$$-b = mx - y$$
$$b = -mx + y$$

Therefore:

$$b = y - mx$$

- We find b by substituting an arbitrary (x, y) pair into the above.
- Thus we can write a linear pattern as a function:

$$f(x) = mx + b$$

## **Graphing Linear Funcions**

- To graph a linear function, simply choose two points and draw them on the graph.
- Draw a straight line through both points.
- This will project the linear function backwards and forewards.
- We can also make predictions based on the numeric value of the linear function.
- Also, we can use a spreadsheet to find the equation of a line from a data series by using the "trendline" feature.