## **Exponential Functions**

October 18, 2019

## 1 Exponential Patterns

- Not all growth or decay models are linear.
- Consider the following pattern

| x | y      |
|---|--------|
| 1 | 10     |
| 2 | 11     |
| 3 | 12.1   |
| 4 | 13.31  |
| 5 | 14.641 |

- Is this pattern linear?
- How can we characterize this pattern?

## 2 Formulae for Exponential Pattern

- A pattern is exponential if the response variable increases by the same rate each time the explanatory variable increases by 1.
- Recursive Formula:

$$P_n = (1+r)P_{n-1}$$

• Explicit Formula:

$$P_n = (1+r)^n P_0$$

- ullet In both of the above, r is a percent written as a decimal.
- What is the recursive formula for the pattern in the previous section?
- What is the explicit formula for the pattern in the previous section?
- Graph this pattern. What is its shape like?

## 3 Sample Problems

- 1. The current population of box turtles in the Maryville College Woods is approximately 300 turtles. Assuming that the population increases by 5% every year, create a chart showing the turtle population over the next 10 years.
- 2. Draw a graph of the turtle population.
- 3. Amoeba are single celled organisms which reproduce by mitosis. An amoeba undergoes mitosis every 30 minutes. That is, it divides into two amoeba. If you have a culture that contains 100 Amoeba, how many will it contain in 24 hours (assuming none die)?