03 - Formulae and Functions

Dr. Robert Lowe

Division of Mathematics and Computer Science
Maryville College





Outline

Formulae

2 Functions





Outline

Formulae

2 Functions





Formulae

Area of a Circle	Circumference of a Circle	Area of a Rectangle	Perimeter of a Rectangle
πr^2	$2\pi r$	$l \times w$	$2 \times I + 2 \times W$
Area of a Triangle	Surface Area of a Sphere	Volume of a Sphere	Quadratic Formula
1/2 bh	$4\pi r^2$	$\frac{4}{3}\pi r^3$	$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2}$
2		3	2a
_			2a

 $\pi = 3.141592653589793238462643383279...$

• A formula is a way of writing down a generic computation so it can be repeated as many times as needed.



Formulae

Area of a Circle	Circumference of a Circle	Area of a Rectangle	Perimeter of a Rectangle
πr^2	$2\pi r$	$l \times w$	$2 \times I + 2 \times W$
Area of a Triangle	Surface Area of a Sphere	Volume of a Sphere	Quadratic Formula
$\frac{1}{2}bh$	$4\pi r^2$	$\frac{4}{3}\pi r^3$	$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

 $\pi = 3.141592653589793238462643383279...$

- A formula is a way of writing down a generic computation so it can be repeated as many times as needed.
- Letters serve as placeholders for numbers. (We refer to these as variables.)





Formulae

Area of a Circle	Circumference of a Circle	Area of a Rectangle	Perimeter of a Rectangle
πr^2	$2\pi r$	$l \times w$	$2 \times I + 2 \times W$
Area of a Triangle	Surface Area of a Sphere	Volume of a Sphere	Quadratic Formula
$\frac{1}{2}bh$	$4\pi r^2$	$\frac{4}{3}\pi r^3$	$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

 $\pi = 3.141592653589793238462643383279...$

- A formula is a way of writing down a generic computation so it can be repeated as many times as needed.
- Letters serve as placeholders for numbers. (We refer to these as variables.)
- To apply a formula, we just fill in the numbers.







1
$$A = \pi r^2$$





1
$$A = \pi r^2$$

$$A = 3.14 \times (4 \text{cm})^2$$





1
$$A = \pi r^2$$

$$A = 3.14 \times (4 \text{cm})^2$$

$$A = 3.14 \times 16 \text{cm}^2$$





- **1** $A = \pi r^2$
- $A = 3.14 \times (4 \text{cm})^2$
- $A = 3.14 \times 16 \text{cm}^2$
- $A = 50.24 \text{cm}^2$





- **1** $A = \pi r^2$
- $A = 3.14 \times (4 \text{cm})^2$
- $A = 3.14 \times 16 \text{cm}^2$
- $A = 50.24 \text{cm}^2$
- **6** $C = 2\pi r$





- **1** $A = \pi r^2$
- 2 $A = 3.14 \times (4 \text{cm})^2$
- **3** $A = 3.14 \times 16 \text{cm}^2$
- $A = 50.24 \text{cm}^2$
- **6** $C = 2\pi r$
- **6** $C = 2 \times 3.14 \times 4$ cm





- **1** $A = \pi r^2$
- $A = 3.14 \times (4 \text{cm})^2$
- **3** $A = 3.14 \times 16 \text{cm}^2$
- $A = 50.24 \text{cm}^2$
- **6** $C = 2\pi r$
- **6** $C = 2 \times 3.14 \times 4$ cm
- $C = 6.28 \times 4$ cm





- **1** $A = \pi r^2$
- $A = 3.14 \times (4 \text{cm})^2$
- $A = 3.14 \times 16 \text{cm}^2$
- $A = 50.24 \text{cm}^2$
- **6** $C = 2\pi r$
- **6** $C = 2 \times 3.14 \times 4$ cm
- $C = 6.28 \times 4$ cm
- 8 C = 25.12cm













2
$$P = 2 \times 120 \text{yd} + 2 \times 53\frac{1}{3} \text{yd}$$





$$P = 2 \times I + 2 \times w$$

2
$$P = 2 \times 120 \text{yd} + 2 \times 53\frac{1}{3} \text{yd}$$

$$P = 240 \text{yd} + 2 \times 53 \frac{1}{3} \text{yd}$$





2
$$P = 2 \times 120 \text{yd} + 2 \times 53\frac{1}{3} \text{yd}$$

$$P = 240 \text{yd} + 2 \times 53 \frac{1}{3} \text{yd}$$

$$P = 240 \text{yd} + 106 \frac{2}{3} \text{yd}$$





2
$$P = 2 \times 120 \text{yd} + 2 \times 53\frac{1}{3} \text{yd}$$

$$P = 240 \text{yd} + 2 \times 53 \frac{1}{3} \text{yd}$$

$$P = 240 \text{yd} + 106 \frac{2}{3} \text{yd}$$

6
$$P = 346\frac{2}{3}$$
yd





$$P = 2 \times I + 2 \times w$$

2
$$P = 2 \times 120 \text{yd} + 2 \times 53\frac{1}{3} \text{yd}$$

$$P = 240 yd + 2 \times 53\frac{1}{3} yd$$

$$P = 240 \text{yd} + 106 \frac{2}{3} \text{yd}$$

6
$$P = 346\frac{2}{3}$$
yd





$$P = 2 \times I + 2 \times w$$

2
$$P = 2 \times 120 \text{yd} + 2 \times 53\frac{1}{3} \text{yd}$$

$$P = 240 yd + 2 \times 53\frac{1}{3} yd$$

$$P = 240 \text{yd} + 106 \frac{2}{3} \text{yd}$$

6
$$P = 346\frac{2}{3}$$
yd

$$A = 120 \text{yd} \times 53\frac{1}{3} \text{yd}$$





$$P = 2 \times I + 2 \times w$$

2
$$P = 2 \times 120 \text{yd} + 2 \times 53\frac{1}{3} \text{yd}$$

3
$$P = 240 \text{yd} + 2 \times 53\frac{1}{3} \text{yd}$$

$$P = 240 \text{yd} + 106 \frac{2}{3} \text{yd}$$

6
$$P = 346\frac{2}{3}$$
yd

$$A = 120 \text{yd} \times 53\frac{1}{3} \text{yd}$$

8
$$A = 6,400 \text{yd}^2$$









1
$$S = 4\pi r^2$$





1
$$S = 4\pi r^2$$

②
$$S = 4 \times 3.14 \times (5in)^2$$





1
$$S = 4\pi r^2$$

2
$$S = 4 \times 3.14 \times (5in)^2$$

3
$$S = 4 \times 3.14 \times 25 \text{in}^2$$





1
$$S = 4\pi r^2$$

2
$$S = 4 \times 3.14 \times (5in)^2$$

3
$$S = 4 \times 3.14 \times 25 \text{in}^2$$

$$S = 12.56 \times 25 \text{in}^2$$



1
$$S = 4\pi r^2$$

$$S = 4 \times 3.14 \times (5in)^2$$

3
$$S = 4 \times 3.14 \times 25 \text{in}^2$$

$$S = 12.56 \times 25 \text{in}^2$$

5
$$S = 314 \text{in}^2$$





1
$$S = 4\pi r^2$$

$$S = 4 \times 3.14 \times (5in)^2$$

3
$$S = 4 \times 3.14 \times 25 \text{in}^2$$

$$S = 12.56 \times 25 \text{in}^2$$

5
$$S = 314 \text{in}^2$$

6
$$A = \frac{4}{3}\pi r^3$$

1
$$S = 4\pi r^2$$

$$S = 4 \times 3.14 \times (5in)^2$$

3
$$S = 4 \times 3.14 \times 25 \text{in}^2$$

$$S = 12.56 \times 25 \text{in}^2$$

5
$$S = 314 \text{in}^2$$

6
$$A = \frac{4}{3}\pi r^3$$

$$A = \frac{4}{3} \times 3.14 \times (5in)^3$$





1
$$S = 4\pi r^2$$

2
$$S = 4 \times 3.14 \times (5in)^2$$

3
$$S = 4 \times 3.14 \times 25 \text{in}^2$$

$$S = 12.56 \times 25 \text{in}^2$$

6
$$S = 314 \text{in}^2$$

6
$$A = \frac{4}{3}\pi r^3$$

$$A = \frac{4}{3} \times 3.14 \times (5in)^3$$

3
$$A = \frac{4}{3} \times 3.14 \times 125 \text{in}^3$$





1
$$S = 4\pi r^2$$

$$S = 4 \times 3.14 \times (5in)^2$$

3
$$S = 4 \times 3.14 \times 25 \text{in}^2$$

$$S = 12.56 \times 25 \text{in}^2$$

6
$$S = 314 \text{in}^2$$

6
$$A = \frac{4}{3}\pi r^3$$

$$A = \frac{4}{3} \times 3.14 \times (5in)^3$$

3
$$A = \frac{4}{3} \times 3.14 \times 125 \text{in}^3$$

$$A \approx 1.33 \times 3.14 \times 125 \text{in}^3$$





1
$$S = 4\pi r^2$$

2
$$S = 4 \times 3.14 \times (5in)^2$$

3
$$S = 4 \times 3.14 \times 25 \text{in}^2$$

$$S = 12.56 \times 25 \text{in}^2$$

5
$$S = 314 \text{in}^2$$

6
$$A = \frac{4}{3}\pi r^3$$

$$A = \frac{4}{3} \times 3.14 \times (5in)^3$$

$$A = \frac{4}{3} \times 3.14 \times 125 \text{in}^3$$

9
$$A \approx 1.33 \times 3.14 \times 125 \text{in}^3$$

1
$$A \approx 4.18 \times 125 \text{in}^3$$





1
$$S = 4\pi r^2$$

2
$$S = 4 \times 3.14 \times (5in)^2$$

3
$$S = 4 \times 3.14 \times 25 \text{in}^2$$

$$S = 12.56 \times 25 \text{in}^2$$

5
$$S = 314 \text{in}^2$$

6
$$A = \frac{4}{3}\pi r^3$$

$$A = \frac{4}{3} \times 3.14 \times (5in)^3$$

$$A = \frac{4}{3} \times 3.14 \times 125 \text{in}^3$$

9
$$A \approx 1.33 \times 3.14 \times 125 \text{in}^3$$

1
$$A \approx 4.18 \times 125 \text{in}^3$$





Outline

Formulae

2 Functions





 A function is a rule which shows how one set maps onto another. (Usually we mean one set of numbers onto another set of values.)





- A function is a rule which shows how one set maps onto another. (Usually we mean one set of numbers onto another set of values.)
- Algebraic functions are written like a formula

$$f(x) = x + 2$$





- A function is a rule which shows how one set maps onto another. (Usually we mean one set of numbers onto another set of values.)
- Algebraic functions are written like a formula

$$f(x) = x + 2$$

• f applies x + 2 to the given value. For example:

$$f(2) = 2 + 2$$

$$f(2) = 4$$





- A function is a rule which shows how one set maps onto another. (Usually we mean one set of numbers onto another set of values.)
- Algebraic functions are written like a formula

$$f(x) = x + 2$$

• f applies x + 2 to the given value. For example:

$$f(2) = 2 + 2$$

$$f(2) = 4$$

• Note that f(x) is the notation that means "Function of x" and not $f \cdot x$.





Write each of the geometric formulae from the previous section as a function.

Area of a Circle

Area of a Triangle

Circumference of a Circle

Surface Area of A Sphere

Area of a Rectangle

Volume of a Sphere





Write each of the geometric formulae from the previous section as a function. Area of a Circle

 \bullet πr^2

Area of a Triangle

Circumference of a Circle

Surface Area of A Sphere

Area of a Rectangle

Volume of a Sphere





Write each of the geometric formulae from the previous section as a function.

- Area of a Circle

Area of a Triangle

2 $A(r) = \pi r^2$

Circumference of a Circle

Surface Area of A Sphere

Area of a Rectangle

Volume of a Sphere





Write each of the geometric formulae from the previous section as a function.

Area of a Circle

$$1 \pi r^2$$

2
$$A(r) = \pi r^2$$

Circumference of a Circle

 $\bigcirc 2\pi r$

Surface Area of A Sphere

Area of a Rectangle

Volume of a Sphere



Write each of the geometric formulae from the previous section as a function.

Area of a Circle

2
$$A(r) = \pi r^2$$

Circumference of a Circle

$$\bigcirc 2\pi r$$

2
$$c(r) = 2\pi r$$

Area of a Rectangle

Volume of a Sphere



Write each of the geometric formulae from the previous section as a function.

Area of a Circle

$$1 \pi r^2$$

2
$$A(r) = \pi r^2$$

Circumference of a Circle

$$\bigcirc 2\pi r$$

Surface Area of A Sphere

2
$$c(r) = 2\pi r$$

Area of a Rectangle

$$1 \times w$$

Volume of a Sphere



Write each of the geometric formulae from the previous section as a function.

Area of a Circle

$$\bigcirc$$
 πr^2

2
$$A(r) = \pi r^2$$

Circumference of a Circle

$$\bigcirc 2\pi r$$

Surface Area of A Sphere

2
$$c(r) = 2\pi r$$

Area of a Rectangle

$$1 \times w$$

$$A(I, w) = I \times w$$



Write each of the geometric formulae from the previous section as a function.

Area of a Circle

$$1 \pi r^2$$

2
$$A(r) = \pi r^2$$

Circumference of a Circle

$$\bigcirc 2\pi r$$

2
$$c(r) = 2\pi r$$

Area of a Rectangle

$$\bigcirc 1 \times w$$

$$A(I, w) = I \times w$$

$$P(l, w) = 2 \times l + 2 \times w$$



Write each of the geometric formulae from the previous section as a function.

- Area of a Circle
- **2** $A(r) = \pi r^2$

Circumference of a Circle

- $\bigcirc 2\pi r$
- $c(r) = 2\pi r$

Area of a Rectangle

- $1 \times w$

Perimeter of a Rectangle

$$P(l, w) = 2 \times l + 2 \times w$$

Area of a Triangle

Surface Area of A Sphere





Write each of the geometric formulae from the previous section as a function.

Area of a Circle

- $\mathbf{0} \pi \mathbf{r}^2$
- **2** $A(r) = \pi r^2$

Circumference of a Circle

- $\bigcirc 2\pi r$
- $c(r) = 2\pi r$

Area of a Rectangle

- \bigcirc $1 \times w$

Perimeter of a Rectangle

$$P(l, w) = 2 \times l + 2 \times w$$

Area of a Triangle

- **2** $A(b,h) = \frac{1}{2}bh$

Surface Area of A Sphere





Write each of the geometric formulae from the previous section as a function.

Area of a Circle

- **2** $A(r) = \pi r^2$

Circumference of a Circle

- $\bigcirc 2\pi r$
- $c(r) = 2\pi r$

Area of a Rectangle

- $1 \times w$
- $A(I, w) = I \times w$

Perimeter of a Rectangle

$$P(l, w) = 2 \times l + 2 \times w$$

Area of a Triangle

- **2** $A(b,h) = \frac{1}{2}bh$

Surface Area of A Sphere

 $0 4\pi r^2$





Write each of the geometric formulae from the previous section as a function.

Area of a Circle

- $\mathbf{0} \pi r^2$
- **2** $A(r) = \pi r^2$

Circumference of a Circle

- $\bigcirc 2\pi r$
- **2** $c(r) = 2\pi r$

Area of a Rectangle

- $1 \times W$

Perimeter of a Rectangle

$$P(l, w) = 2 \times l + 2 \times w$$

Area of a Triangle

- **2** $A(b,h) = \frac{1}{2}bh$

Surface Area of A Sphere

- $0 4\pi r^2$
- **2** $S(r) = 4\pi r^2$





Write each of the geometric formulae from the previous section as a function.

Area of a Circle

- \bullet πr^2
- **2** $A(r) = \pi r^2$

Circumference of a Circle

- $\bigcirc 2\pi r$
- **2** $c(r) = 2\pi r$

Area of a Rectangle

- $1 \times w$
- $A(I, w) = I \times w$

Perimeter of a Rectangle

$$P(l, w) = 2 \times l + 2 \times w$$

Area of a Triangle

- **2** $A(b,h) = \frac{1}{2}bh$

Surface Area of A Sphere

- **1** $4\pi r^2$
- 2 $S(r) = 4\pi r^2$

$$0 \frac{4}{3} \pi r^3$$





Write each of the geometric formulae from the previous section as a function.

Area of a Circle

- \bullet πr^2
- **2** $A(r) = \pi r^2$

Circumference of a Circle

- $\bigcirc 2\pi r$
- **2** $c(r) = 2\pi r$

Area of a Rectangle

- $1 \times w$

Perimeter of a Rectangle

$$P(l, w) = 2 \times l + 2 \times w$$

Area of a Triangle

- **2** $A(b,h) = \frac{1}{2}bh$

Surface Area of A Sphere

- $0 4\pi r^2$
- 2 $S(r) = 4\pi r^2$

- 2 $V(r) = \frac{4}{3}\pi r^3$





In the first half of a basketball game, team A scored 60 points and team B scored 70 points. In the second half, team A scores 7 points per minute and team B scores 8 points per minute.





In the first half of a basketball game, team A scored 60 points and team B scored 70 points. In the second half, team A scores 7 points per minute and team B scores 8 points per minute.



In the first half of a basketball game, team A scored 60 points and team B scored 70 points. In the second half, team A scores 7 points per minute and team B scores 8 points per minute.

- $s_a(x) = 60 + 7x$
- 2 $s_a(24) = 60 + 7 \cdot 24$





In the first half of a basketball game, team A scored 60 points and team B scored 70 points. In the second half, team A scores 7 points per minute and team B scores 8 points per minute.

- 2 $s_a(24) = 60 + 7 \cdot 24$
- 3 $s_a(24) = 60 + 168$





In the first half of a basketball game, team A scored 60 points and team B scored 70 points. In the second half, team A scores 7 points per minute and team B scores 8 points per minute.

2
$$s_a(24) = 60 + 7 \cdot 24$$

3
$$s_a(24) = 60 + 168$$

$$s_a(24) = 228$$



In the first half of a basketball game, team A scored 60 points and team B scored 70 points. In the second half, team A scores 7 points per minute and team B scores 8 points per minute.

$$s_a(x) = 60 + 7x$$

2
$$s_a(24) = 60 + 7 \cdot 24$$

3
$$s_a(24) = 60 + 168$$

$$s_a(24) = 228$$





In the first half of a basketball game, team A scored 60 points and team B scored 70 points. In the second half, team A scores 7 points per minute and team B scores 8 points per minute.

2
$$s_a(24) = 60 + 7 \cdot 24$$

3
$$s_a(24) = 60 + 168$$

$$s_a(24) = 228$$

2
$$s_b(24) = 70 + 8 \cdot 24$$





In the first half of a basketball game, team A scored 60 points and team B scored 70 points. In the second half, team A scores 7 points per minute and team B scores 8 points per minute.

2
$$s_a(24) = 60 + 7 \cdot 24$$

$$s_a(24) = 60 + 168$$

$$s_a(24) = 228$$

1
$$s_b(x) = 70 + 8x$$

2
$$s_b(24) = 70 + 8 \cdot 24$$

$$s_b(24) = 70 + 192$$





In the first half of a basketball game, team A scored 60 points and team B scored 70 points. In the second half, team A scores 7 points per minute and team B scores 8 points per minute.

2
$$s_a(24) = 60 + 7 \cdot 24$$

3
$$s_a(24) = 60 + 168$$

$$s_a(24) = 228$$

2
$$s_b(24) = 70 + 8 \cdot 24$$

$$s_b(24) = 70 + 192$$

$$s_b(24) = 262$$





In the first half of a basketball game, team A scored 60 points and team B scored 70 points. In the second half, team A scores 7 points per minute and team B scores 8 points per minute.

2
$$s_a(24) = 60 + 7 \cdot 24$$

3
$$s_a(24) = 60 + 168$$

$$s_a(24) = 228$$

2
$$s_b(24) = 70 + 8 \cdot 24$$

$$s_b(24) = 70 + 192$$

$$s_b(24) = 262$$



