# Hypothesis Testing

Ryan Miller



#### Outline

- ▶ Video #1
  - Null Models
- ▶ Video #2
  - p-values
- ► Video #3
  - ► An Example
- ► Video #4
  - Decision Errors
- ► Video #5
  - p-value Misconceptions

#### Introduction

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  - Central Limit theorem gave us a Normal model for the sampling distribution of the sample average, which we could use to find a confidence interval estimate

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- Last week, we focused on the sample average (proportion) as a random variable
  - Central Limit theorem gave us a Normal model for the sampling distribution of the sample average, which we could use to find a confidence interval estimate
- Confidence intervals can be used to statistically assess the variability inherent to sample data
  - However, this week we'll learn about complimentary approach, known as hypothesis testing, that also uses the Central Limit theorem to evaluate the statistical variability in an observed outcome

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- 16 infants repeatedly watched demonstrations of two scenarios
  - A "helper" toy assisting the main character
  - A "hinderer" toy blocking the main character
- ▶ When given the choice, 14 of 16 infants chose the "helper" toy

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- Could the majority have chosen the "helper" toy due to a confounding variable like the toy's color or shape?
  - No, recall that these were randomly assigned
- Could the majority have chosen the "helper" toy due to some type of bias?
  - Probably not, measurement of this outcome is pretty clear-cut

Ideally, statisticians are left to decide between two explanations: random chance/variability or a real relationship

At this point, the remaining step is to try and rule out random chance as a viable explanation. To do so, statisticians apply the following logic:

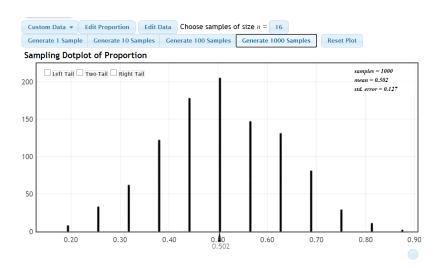
- 1) Identify a suitable **null model** for the outcome of interest
- 2) Calculate the probability of seeing the outcome that occurred in the sample data if the null model were true
- 3) If this probability is sufficiently small, rule out random chance as an explanation

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  - Under this null model, we can investigate what outcomes could occur by random chance alone
- One approach is to use simulation by generating many different repititions of 16 coin flips on StatKey
- Another approach is to use Central Limit theorem to determine the distribution of sample proportions under the null model

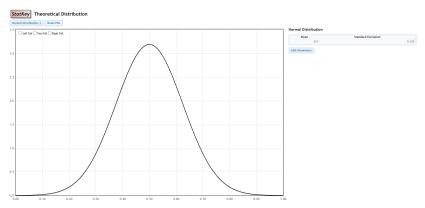
### The Simulation Approach





## The CLT Approach

Note that according to CLT,  $SE = \sqrt{.5*.5/16} = 0.125$ 



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  - In our example, we observed a sample proportion of  $\hat{p}=14/16=0.875$ , which appears to be a very unlikely outcome under the null model
- ▶ In the next video, we'll introduce the *p*-value as a statistical tool to more precisely measure the degree of incompatibility between the observed data and the null model

#### *p*-values

- Probability theory allows us to quantify how compatible/incompatible the sample data are with a null model
  - ► The **p-value** is defined as the probability of seeing an outcome at least as extreme as what was observed in our sample if the null model were true

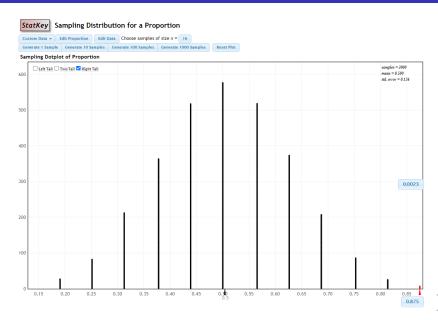
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- ► The *smaller* the *p*-value, the *more incompatible* the sample data are with the null model, and thus the stronger the evidence is against random chance as a viable explanation

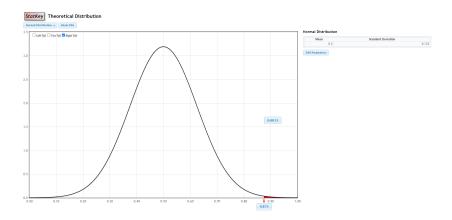
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- The smaller the p-value, the more incompatible the sample data are with the null model, and thus the stronger the evidence is against random chance as a viable explanation
  - For example, a p-value of 0.01 indicates a 1/100 chance of seeing results as extreme as the sample data if the null model were true (high degree of incompatibility)
  - $\triangleright$  A p-value of 0.2 indicates a 1/5 chance of seeing results as extreme as the sample data (low degree of incompatibility)

#### The Simulated Null Distribution



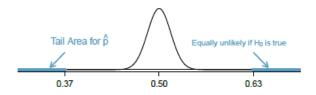
### The CLT Null Distribution





### Two-sided p-values

- ► The p-values (0.0023 and 0.0013) we calculated using the simulated/CLT null distributions aren't actually the ones that a researcher would report in an scientific journal
  - Instead, they are a special case known as a *one-sided p-*value, which are rarely used by statisticians
- Instead, two-sided p-values tend to be prefered:



▶ The practical implication is that we must double the one-sided tail area to find all areas of the null distribution that are as unlikely as the observed outcome in our sample



### Alternative Hypotheses

There are many reason why statisticians prefer two-sided *p*-values, and one is the notion that any null model should be paired with a *complementary* alternative:

$$H_0: p = 0.5$$

$$H_A: p \neq 0.5$$

Under this setup, an observed sample proportion that is either very large or very small would provide substantial evidence against the null model

#### p-values as a Measure of Evidence

Ronald Fisher, creator of the *p*-value, and described by his peers as "a genius who almost single-handedly created the foundations of modern statistical science", suggests the following guidelines:

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- Many scientific fields use  $\alpha=0.05$  as a "significance threshold" for *rejecting* a null hypothesis
- ▶ Thus, *p*-values < 0.05 are described as "statistically significant"



# Arguments Against "Statistical Significance"

- p < 0.05 is an arbitrary cutoff that shouldn't distract you from the main idea behind p-values
- ► That is, a *p*-value of 0.0001 doesn't tell you the same thing as a *p*-value of 0.04, even though both are "statistically significant"

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- ➤ That is, a *p*-value of 0.0001 doesn't tell you the same thing as a *p*-value of 0.04, even though both are "statistically significant"
- When reporting results you should always include the p-value itself, not just whether it met some arbitrary significance threshold
  - Imagine your weather app only telling you: "it's cold" or "it's not cold"
  - ► This is bad because "cold" is subjective, it's better to provide the temperature and let you decide for yourself

### Closing Remarks

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  - ► The two-sided *p*-value is found by multiplying the relevant one-sided tail-area by 2
- ➤ You should think of the *p*-value as a measure of incompatibility between the null model and the observed data
  - A smaller *p*-value suggests lower compatibility (ie: it's likely that the null model is wrong)

### How to Conduct a Hypothesis Test

The key steps in any hypothesis test are as follows:

- 1) State the null and alternative hypotheses
- 2) Find the null distribution (the distribution of possible outcomes that could occur if the null hypothesis were true)
- 3) Using the null distribution, locate the estimate observed in the sample data to find the *p*-value
- 4) Use the *p*-value to make a conclusion

We'll now go through a full example of this process

### Example

According to Wikipedia, babies born 15-weeks prematurely have a 70% survival rate. A recent study of babies born at Johns Hopkins University found that 31 of 39 (79.5%) babies born 15-weeks early survived. Does this study provide statistically compelling evidence that Wikipedia's claim is wrong?

### Step 1 - State the Hypotheses

In order to evaluate whether the sample data are incompatible with Wikipedia's claim, we begin by assuming that Wikipedia's claim is true:

$$H_0: p = 0.7$$

$$H_A : p \neq 0.7$$

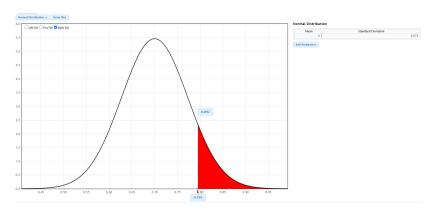
### Step 2 - Find the Null Distribution

Central Limit theorem suggests we might use a Normal model to tell us which sample proportions we might expect to see if the  $H_0: p = 0.7$  is true:

$$\hat{p} \sim N\left(0.7, \sqrt{\frac{0.7(1-0.7)}{39}}\right)$$

In words, the expected value of our null model is 0.7 and the standard error is  $\sqrt{\frac{0.7(1-0.7)}{39}}=0.073$ 

## Step 3 - Locate the Sample Estimate to find the *p*-value



Remember we need to double this area to get a two-sided p-value of 0.184



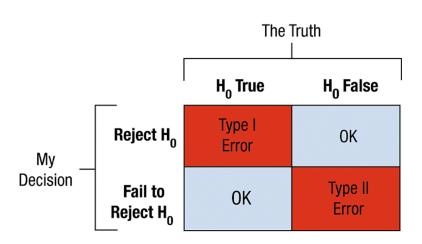
#### Step 4 - Make a Conclusion

Based upon the p-value of 0.184, there is a roughly 1 in 5 chance of seeing a sample proportion like this one (31 of 39) if Wikipedia's claim of 70% survival is correct. Therefore, we conclude these data do not provide sufficient evidence to disprove Wikipedia's claim.

#### Decision Thresholds

- ► The final step in a hypothesis test is to use the *p*-value to make a decision
  - Many scientific fields use  $\alpha = 0.05$  as a "significance threshold" for *rejecting* a null hypothesis
- lacktriangle More generally, we could let lpha denote a decision threshold
  - ▶ If p-value  $\leq \alpha$  we'd reject  $H_0$  in favor of the alternative
  - If p-value  $> \alpha$  we'd decide there isn't enough evidence to reject  $H_0$

#### Decision Errors





#### Example #1

- Consider a jury trial for Person A
  - $ightharpoonup H_0$ : Person A is not guilty vs.  $H_A$ : Person A is guilty
- ▶ In words, what would a Type I and Type II error represent?

# Example #1 (solution)

- A Type I error would mean that Person A is not guilty ( $H_0$  is true), but the jury decides they are guilty (reject  $H_0$ )
- ▶ A Type II error would mean that Person A is guilty ( $H_0$  is false), but the jury decides they are not guilty (not enough evidence to reject  $H_0$ )

### Example #2

- Consider a clinical trial evaluating a new medication for disease
  B
  - ▶  $H_0$ : The medication doesn't cure disease B vs.  $H_A$ : The medication cures disease B
- ▶ In words, what would a Type I and Type II error represent?

# Example #2 (solution)

- A Type I error would mean the new medication is not effective (H<sub>0</sub> is true), but the study concludes it cures disease B (reject H<sub>0</sub>)
- A Type II error would mean the new medication cures disease B (H₀ is false), but the study concludes it is ineffective (not enough evidence to reject H₀)

#### **Error Rates**

- **b** By design, using a *decision threshold* of  $\alpha$  means the probability of making a Type I error (when  $H_0$  is true) is  $\alpha$ 
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- If we wanted to reduce the rate of Type I errors, we might consider a more stringent threshold of  $\alpha = 0.01$ 
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#### Error Rates and Study Replication

- ▶ The decision threshold of  $\alpha = 0.05$  is very widely used because it is thought to balance the rates of Type I and Type II errors
- While we'd expect a Type I error in 5% of studies, if others are repeating the same research the chance of two independent studies both resulting in a Type I error is very small
  - ightharpoonup 0.05\*0.05 = 0.0025 (or 1/400)

#### Error Rates and Multiple Tests

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- As an example, consider a genetic association study testing differences in the expression levels of 7129 genes across two patients with two different types of leukemia
  - ► This single study involves 7129 different hypothesis tests
  - If all of the tests used  $\alpha = 0.05$ , and none of the genes were related to the type of leukemia, we'd expect to see 356 "statistically significant" genes

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- As you'd expect, it is wise to use a more stringent significance threshold in this type of study (one involving many different related hypotheses)

# The Bonferroni Adjustment

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- $\triangleright$  A simple fix is to divide the desired Type I error rate,  $\alpha$ , by the number of hypothesis tests, h, to get an adjusted significance threshold ( $\alpha^* = \alpha/h$ )
- This procedure is known as the "Bonferroni Adjustment" and it will limit the *entire study's* Type I error rate to  $\alpha$  (known as the family-wise error rate)
  - For the Leukemia example (involving 7129 different genes), we might use an adjusted significance threshold of  $\alpha^* = 0.05/7139 = 0.00007$  if we wanted to limit the probability of making at least one Type I error to 5%

- Hypothesis testing is a decision making tool, but it isn't perfect
  - ► Type I errors occur when the null hypothesis is *true*, but the data say to *reject it*
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  - There is a trade-off between using more/less stringent values of  $\alpha$  (lowering  $\alpha$  will reduce the chances of making a Type I error but increase the likelihood of making a Type II error)
- Performing a large number of hypothesis tests within a single study can be problematic

# Hypothesis Testing Misconceptions

- ▶ We've now introduced the general framework for hypothesis testing, which is based upon using the p-value as a measure of evidence against a null hypothesis
- Unfortunately, p-values are frequently misunderstood and are often used incorrectly
  - ► The misuse of *p*-values has become such a problem that *Basic* and *Applied Social Psychology* has banned their use (source)

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- Unfortunately, p-values are frequently misunderstood and are often used incorrectly
  - The misuse of *p*-values has become such a problem that *Basic* and *Applied Social Psychology* has banned their use (source)
- ► However, it is my belief that *p*-values, if used properly, are an important statistical tool
  - But in order to be used properly, you need to be aware of the mistakes that others are making

- ► Let's consider a silly example where the NBA's Steph Curry and myself compete by each shooting 5 three-point shots
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  - ▶ I make 2 of 5, and Steph makes 5 of 5
- ► We might use a hypothesis test to evaluate the null hypothesis that we're both equally good three-point shooters (ie:
  - $H_0: p_{Miller} = p_{Curry}$ 
    - ► The *p*-value for this scenario is 0.17
    - Does that mean we are equally good 3-pt shooters?

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- ► The p-value measures the strength of evidence against the null hypothesis
  - In a sample involving only 5 shots, there isn't enough data to provide sufficient evidence against the null hypothesis
  - ► A lack of evidence does not mean the null hypothesis is likely to be correct

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- It might seem professionals would easily avoid the mistake highlighted in that silly Steph Curry example, but unfortunately it happens quite often
- ▶ In 2006, the Woman's Health Initiative evaluated the relationship between low-fat diets and reduced risk of breast cancer risk and found a p-value of 0.07
  - ► The NY Times ran the headline: "Study Finds Lowfat Diets Won't Stop Cancer or Heart Disease"
  - The article described the study's results as: "The death knell for the belief that reducing the percentage of fat in the diet is important for health"
- In reality, these results simply indicates insufficient evidence linking dietary fat and breast cancer, it's very possible there is a small benefit but we cannot rule out random chance

# Comments - "Proving" the Null Hypothesis

- ► Hypothesis testing is not designed to "prove" a null hypothesis, so you should never use it to try and do so
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  - The null hypothesis is intended to be a "straw man" that researchers want to "knock down"
- ▶ The closest thing to "proving" a null hypothesis is a *very* narrow confidence interval around the null value
  - This interval estimate would suggest the only plausible values for the parameter of interest are extremely close to what the null hypothesis suggests

### Comments - Confidence Intervals vs. Hypothesis Tests

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  - A confidence interval provides a range of plausible estimates for a population characteristic
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- ightharpoonup Consider  $H_0$ : p=0.5, and suppose our sample produces a 95% CI estimate for p of (0.53, 0.63)
  - ▶ This interval says that it is *not plausible* that p = 0.5, so we expect the hypothesis test to have a p-value < 0.05 (based upon the 95% confidence level)

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- Again consider  $H_0$ : p = 0.5, but now suppose a different sample leads to a sample proportion of  $\hat{p} = 0.53$  and a p-value of 0.11, we'd expect the 95% confidence interval estimate from this sample to suggest that 0.5 is a plausible value (ie: the 95% CI would contain 0.5)



- Confidence intervals and hypothesis tests lead to similar conclusions, but provide complementary information
- In the 1980s, AstraZeneca developed Prilosec, a very successful medication for healing erosive esophagitis (heart burn)
  - In the 2001, just before the company's patent on *Prilosec* was about to expire, AstraZeneca developed a new drug, Nexium

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  - ▶ In the 2001, just before the company's patent on *Prilosec* was about to expire, *AstraZeneca* developed a new drug, *Nexium*
- ► To get *Nexium* approved by the FDA, *AstraZeneca* conducted a large randomized experiment comparing it to *Prilosec* 
  - The experiment resulted in a *p*-value < 0.001, well below significance threshold of  $\alpha = 0.05$  used by the FDA
- After its approval, AstraZeneva spent millions of dollars marketing Nexium and it soon became one of the top selling drugs in the world, leading to billions in profits

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  - Omeprazole (Prilosec)
  - Esomeprazole (Nexium)
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- Critics of the pharmaceutical industry argue the results of the Nexium study were not clinically significant, meaning the differences in the two drugs aren't substantial enough to be influencing clinical practices

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- A very small p-value does not mean an observed relationship is large, meaningful, or important
  - The p-value is a tool for evaluating how plausible it is for an observed relationship to be explained by random chance
- ▶ With enough data, it is possible to show small/inconsequential relationships are unlikely to occur by chance alone
  - This doesn't mean those relationships have any real-world significance
  - Reporting confidence intervals along side hypothesis test results is one way to address this shortcoming

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  - ▶ Instead, a large *p*-value only means there is insufficient evidence in the sample

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  - ► Instead, a large p-value only means there is insufficient evidence in the sample
- ► A small or significant *p*-value does not mean the observed relationship is important or meaningful
  - Instead, a small p-value only means the sample data are unlikely to have occurred by random chance alone if the null model were true