Example R and Stata code for a Mendelian randomization analysis

Sanderson et al.

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Example R and Stata code to perform a multivariable Mendelian randomization (MVMR) analysis

R. code

• Read in the data

```
suppressPackageStartupMessages({
   library(tidyverse)
   library(haven)
   library(remotes)
})
dat <- read_dta("https://raw.github.com/remlapmot/mrrobust/master/dodata.dta")
dat <- dat %>% filter(ldlcp2 < 1e-8)</pre>
```

Example code using the MendelianRandomization package

• Install the package and load it into memory

library(MendelianRandomization)

• Convert our data frame to the required class

```
datfmt <- mr_mvinput(
  bx = as.matrix(cbind(dat$ldlcbeta, dat$hdlcbeta, dat$tgbeta)),
  bxse = as.matrix(cbind(dat$ldlcse, dat$hdlcse, dat$tgse)),
  by = dat$chdbeta,
  byse = dat$chdse,
  exposure = "exposure",
  outcome = "outcome",
  snps = "snp",
  effect_allele = dat$a1,
  other_allele = dat$a2,
  eaf = NA
)</pre>
```

• Fit an MVMR/MVIVW model

```
mvivwfit <- mr_mvivw(datfmt)</pre>
mvivwfit
## Multivariable inverse-variance weighted method
## (variants uncorrelated, random-effect model)
## Number of Variants : 73
##
   ______
##
##
     Exposure Estimate Std Error 95% CI p-value
## exposure_1 0.429 0.061 0.309, 0.548 0.000
## exposure_2 -0.194 0.131 -0.451, 0.062 0.138
## exposure_3 0.226 0.123 -0.016, 0.468 0.067
## Residual standard error = 1.490
## Heterogeneity test statistic = 155.3766 on 70 degrees of freedom, (p-value = 0.0000)
  • Fit an MVMR-Egger model
mvmreggerfit <- mr_mvegger(datfmt)</pre>
mvmreggerfit
## Multivariable MR-Egger method
## (variants uncorrelated, random-effect model)
##
## Orientated to exposure : 1
## Number of Variants : 73
##
      Exposure Estimate Std Error 95% CI
                                              p-value
##
    exposure_1 0.567 0.100 0.371, 0.764 0.000
##
    exposure_2 -0.136 0.133 -0.398, 0.125 0.306
##
    exposure_3 0.274 0.125 0.030, 0.518
                                                0.028
    (intercept) -0.009 0.005 -0.020, 0.001
##
                                                0.084
## Residual standard error = 1.469
## Heterogeneity test statistic = 148.9290 on 69 degrees of freedom, (p-value = 0.0000)
Example code using the MVMR and RMVMR packages
  • Install the package and load it into memory
if (!requireNamespace("MVMR", quietly = TRUE)) {
```

• Create a data object of the required structure

remotes::install_github("WSpiller/MVMR")

}

library(MVMR)

```
r_input <- format_mvmr(
    BXGs = dat[,c("ldlcbeta","hdlcbeta","tgbeta")],
    BYG = dat$chdbeta,
    seBXGs = dat[,c("ldlcse","hdlcse","tgse")],
    seBYG = dat$chdse,
    RSID = dat$rsid
)</pre>
```

• Fit an MVMR model

##

```
mvmrfit <- ivw_mvmr(r_input)

##

## Multivariable MR

##

## Estimate Std. Error t value Pr(>|t|)

## exposure1 0.4286200 0.0609661 7.030464 1.099077e-09

## exposure2 -0.1941989 0.1308289 -1.484372 1.421994e-01

## exposure3 0.2260456 0.1232828 1.833554 7.097168e-02
```

• Conditional F-statistics for instrument strength (Sanderson, Spiller, and Bowden 2021)

Residual standard error: 1.49 on 70 degrees of freedom

```
## Warning in strength_mvmr(r_input): Covariance between effect of genetic variants on each exposure
## not specified. Fixing covariance at 0.

##
## Conditional F-statistics for instrument strength
##
## exposure1 exposure2 exposure3
## F-statistic 126.7447 35.29937 39.32731

##
## exposure1 exposure2 exposure3
## F-statistic 126.7447 35.29937 39.32731
```

• Fit a radial MVMR model

```
if (!requireNamespace("RMVMR", quietly = TRUE)) {
    remotes::install_github("WSpiller/RMVMR")
}
library(RMVMR)

rmvmr_input <- mrmvinput_to_rmvmr_format(datfmt)

rmvmr_fit <- ivw_rmvmr(rmvmr_input, summary = TRUE)</pre>
```

```
##
## Radial Multivariable MR
##
## Estimate Std. Error t value Pr(>|t|)
## exposure1 0.4286200 0.0609661 7.030464 1.099077e-09
## exposure2 -0.1941989 0.1308289 -1.484372 1.421994e-01
## exposure3 0.2260456 0.1232828 1.833554 7.097168e-02
##
## Residual standard error: 1.49 on 70 degrees of freedom
```

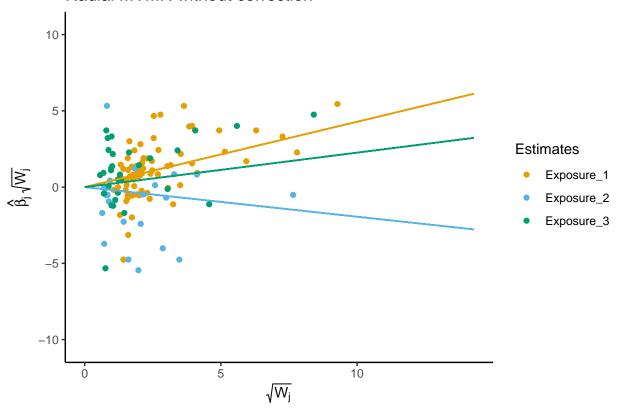
rmvmr_fit\$coef

```
## Estimate Std. Error t value Pr(>|t|)
## exposure1 0.4286200 0.0609661 7.030464 1.099077e-09
## exposure2 -0.1941989 0.1308289 -1.484372 1.421994e-01
## exposure3 0.2260456 0.1232828 1.833554 7.097168e-02
```

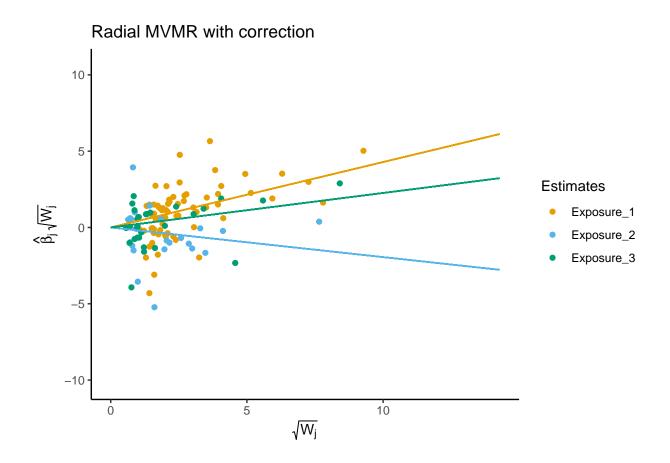
• Plot the radial MVMR models

```
plt_rmvmr <- plot_rmvmr(rmvmr_input, rmvmr = rmvmr_fit)
plt_rmvmr$p1</pre>
```

Radial MVMR without correction



plt_rmvmr\$p2



• Heterogeneity statistics

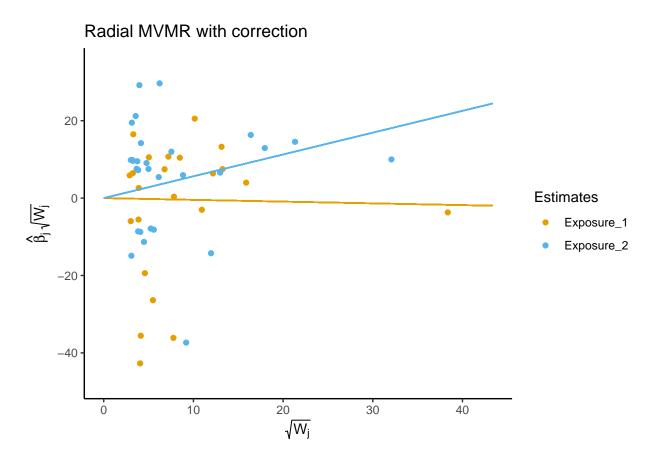
```
pleio_rmvmr <- pleiotropy_rmvmr(rmvmr_input, rmvmr = rmvmr_fit)</pre>
pleio_rmvmr$gq
##
              q_statistic
                                p_value
## Exposure_1
                 76.37356 2.812609e-01
## Exposure_2
                 59.58894 8.243650e-06
## Exposure_3
                 45.88633 1.308596e-02
head(pleio_rmvmr$qdat)
                 wj corrected_beta
                                                       qj_p ref_exposure
##
       snp
                                             qj
## 1 snp_1 2.414215
                          0.3141338 0.031643343 0.85881269
                                                              Exposure_1
## 2 snp_2 3.938760
                          0.3821443 0.008507667 0.92650973
                                                              Exposure_1
## 3 snp_3 3.246657
                         -0.6057993 3.473998077 0.06234046
                                                              Exposure_1
## 4 snp_4 2.001191
                         0.3273484 0.020524059 0.88608310
                                                              Exposure_1
## 5 snp_5 9.278826
                          0.5414293 0.118081748 0.73112437
                                                              Exposure 1
## 6 snp_6 1.317671
                          1.0713541 0.544339092 0.46064001
                                                              Exposure_1
```

• Conditional F-statistics for instrument strength (Sanderson, Spiller, and Bowden 2021)

```
str_rmvmr <- strength_rmvmr(rmvmr_input)</pre>
```

Warning in MVMR::strength_mvmr(r_input, gencov): Covariance between effect of genetic variants on ## each exposure not specified. Fixing covariance at 0.

```
str_rmvmr$plot[[1]]
```



str_rmvmr\$stat[[2]]

NULL

Stata code

• Load the Statamarkdown package to enable Stata code chunks in an R Markdown file

```
if (!requireNamespace("Statamarkdown", quietly = TRUE)) {
   remotes::install_github("Hemken/Statamarkdown")
}
library(Statamarkdown)
```

• Read in the data and create an indicator variable to select observations with p-value between the genotype and LDL-C < 10-8

```
use https://raw.github.com/remlapmot/mrrobust/master/dodata, clear
gen byte sel1 = (ldlcp2 < 1e-8)</pre>
```

Example code using the mrrobust package

• Install the mrrobust package using the github package

```
// Note: output suppressed
net install mrrobust, from("https://raw.github.com/remlapmot/mrrobust/master/")
mrdeps
```

• Fit and MVMR model with phenotypes LDL-c and HDL-c (Burgess, Dudbridge, and Thompson 2015).

```
mvmr chdbeta ldlcbeta hdlcbeta [aw=1/(chdse^2)] if sel1==1
```

```
Number of genotypes = 73
                                              Number of phenotypes = 2
                                         Standard errors: Random effect
                                       Residual standard error = 1.514
         Coef. Std. Err. z P>|z| [95% Conf. Interval]
chdbeta |
   ldlcbeta | .4670719
                      .0581901
                                 8.03
                                        0.000
                                                .3530214
                                                           .5811224
   hdlcbeta | -.2930048 .1211822
                                  -2.42 0.016
                                                -.5305175
                                                           -.0554921
```

• Additionally include a third phenotype – triglycerides.

```
mvmr chdbeta ldlcbeta hdlcbeta tgbeta [aw=1/(chdse^2)] if sel1==1
```

```
Number of genotypes = 73
                                        Number of phenotypes = 3
                                   Standard errors: Random effect
                                  Residual standard error = 1.490
         1
              Coef. Std. Err.
                                          [95% Conf. Interval]
                              z P>|z|
______
chdbeta
      ldlcbeta |
             .42862 .0609661 7.03 0.000
                                          .3091286
                                                    .5481113
  hdlcbeta | -.1941989 .1308289
                             -1.48
                                   0.138
                                          -.4506189
                                                    .0622211
                   .1232828
                            1.83 0.067
                                          -.0155842
    tgbeta | .2260456
                                                    .4676755
```

• Report the QA statistic for instrument validity and the conditional F-statistics for instrument strength for each phenotype (Sanderson et al. 2019; Sanderson, Spiller, and Bowden 2021).

mvmr chdbeta ldlcbeta hdlcbeta tgbeta [aw=1/(chdse^2)] if sel1==1, gxse(ldlcse hdlcse tgse)

> e hdlcse tgse)

Number of genotypes = 73 Number of phenotypes = 3 Standard errors: Random effect Residual standard error = 1.490

	Coef.					Interval]
hdlcbeta	.42862 1941989 .2260456	.0609661 .1308289 .1232828	7.03 -1.48 1.83	0.000 0.138 0.067	.3091286 4506189 0155842	.5481113 .0622211 .4676755

 Q_A statistic for instrument validity; chi2(70) = 152.88 (p = 0.0000)

Conditional F-statistics for instrument strength:

 $F_x1 = 130.31$ (ldlcbeta)

 $F_x2 = 36.29$ (hdlcbeta)

 $F_x3 = 40.44$ (tgbeta)

• Fit an MVMR-Egger regression (Rees, Wood, and Burgess 2017), orienting the model with respect to the first phenotype in the main *varlist*.

mrmvegger chdbeta ldlcbeta hdlcbeta tgbeta [aw=1/(chdse^2)] if sel1==1

MVMR-Egger model oriented wrt: ldlcbeta

Number of genotypes = 73

Number of phenotypes = 3

Residual standard error = 1.469

	Coef.	Std. Err.	z	P> z	[95% Conf.	Interval]
chdbeta						
ldlcbeta	.5672993	.1002611	5.66	0.000	.370791	.7638075
hdlcbeta	1364113	.1332727	-1.02	0.306	3976209	.1247983
tgbeta	.2739803	.1246927	2.20	0.028	.0295871	.5183735
_cons	0093655	.0054187	-1.73	0.084	019986	.001255

We can also orient the model with respect to HDL-C.

mrmvegger chdbeta ldlcbeta hdlcbeta tgbeta [aw=1/(chdse^2)] if sel1==1, orient(2)

> t(2)

MVMR-Egger model oriented wrt: hdlcbeta

Number of genotypes = 73

Number of phenotypes = 3

Residual standard error = 1.501

 	Coef.	Std. E	rr.	z			Interval]
i							
1	.4286398	.06140	56	6.98	0.000	.308287	.5489926
-	.1989637	.154190	09	-1.29	0.197	5011723	.1032449
1	.2256794	.12432	21	1.82	0.069	0179875	.4693463
l	.0002155	.00362	18	0.06	0.953	006883	.0073141
	 -	+	 .4286398 .06140 1989637 .15419 .2256794 .12432	 .4286398 .0614056 1989637 .1541909 .2256794 .1243221	.4286398 .0614056 6.98 1989637 .1541909 -1.29 .2256794 .1243221 1.82	.4286398 .0614056 6.98 0.000 1989637 .1541909 -1.29 0.197 .2256794 .1243221 1.82 0.069	.4286398 .0614056 6.98 0.000 .308287 1989637 .1541909 -1.29 0.1975011723 .2256794 .1243221 1.82 0.0690179875

Or we can orient the model with respect to triglycerides.

```
mrmvegger chdbeta ldlcbeta hdlcbeta tgbeta [aw=1/(chdse^2)] if sel1==1, orient(3)
```

> t(3)

assertthat

R session information for reproducibility

```
library(sessioninfo)
session_info()
```

```
- Session info ------
setting value
version R version 4.1.1 (2021-08-10)
      Windows 10 x64
system x86_64, mingw32
ui
       RTerm
language (EN)
collate English_United Kingdom.1252
ctype
       English_United Kingdom.1252
       Europe/London
tz
date
        2021-09-22
                  * version date lib source
package
arrangements
                   1.1.9 2020-09-13 [1] CRAN (R 4.1.0)
```

0.2.1 2019-03-21 [1] CRAN (R 4.1.0)

```
2020-12-09 [1] CRAN (R 4.1.0)
backports
                          1.2.1
                          0.7.9
                                  2021-07-27 [1] CRAN (R 4.1.0)
broom
cellranger
                          1.1.0
                                  2016-07-27 [1] CRAN (R 4.1.0)
                                  2021-07-17 [1] CRAN (R 4.1.0)
cli
                          3.0.1
codetools
                          0.2-18
                                  2020-11-04 [2] CRAN (R 4.1.1)
                          2.0 - 2
                                  2021-06-24 [1] CRAN (R 4.1.0)
colorspace
                          1.0.2
                                  2020-08-27 [1] CRAN (R 4.1.0)
conquer
                          1.4.1
                                  2021-02-08 [1] CRAN (R 4.1.0)
crayon
curl
                          4.3.2
                                   2021-06-23 [1] CRAN (R 4.1.0)
                                  2021-02-21 [1] CRAN (R 4.1.0)
data.table
                          1.14.0
DBI
                          1.1.1
                                   2021-01-15 [1] CRAN (R 4.1.0)
                                  2021-04-06 [1] CRAN (R 4.1.0)
                          2.1.1
dbplyr
DEoptimR
                          1.0 - 9
                                  2021-05-24 [1] CRAN (R 4.1.0)
digest
                                  2020-10-24 [1] CRAN (R 4.1.0)
                          0.6.27
                        * 1.0.7
                                  2021-06-18 [1] CRAN (R 4.1.0)
dplyr
ellipsis
                          0.3.2
                                  2021-04-29 [1] CRAN (R 4.1.0)
                          0.14
                                  2019-05-28 [1] CRAN (R 4.1.0)
evaluate
fansi
                          0.5.0
                                  2021-05-25 [1] CRAN (R 4.1.0)
                          2.1.0
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farver
fastmap
                          1.1.0
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forcats
                        * 0.5.1
                                  2021-01-27 [1] CRAN (R 4.1.0)
foreach
                          1.5.1
                                  2020-10-15 [1] CRAN (R 4.1.0)
                                  2020-07-31 [1] CRAN (R 4.1.0)
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                          0.1.0
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generics
                        * 3.3.5
                                  2021-06-25 [1] CRAN (R 4.1.0)
ggplot2
glmnet
                          4.1 - 2
                                  2021-06-24 [1] CRAN (R 4.1.0)
                          1.4.2
                                  2020-08-27 [1] CRAN (R 4.1.0)
glue
                          0.6-2
                                  2021-01-07 [1] CRAN (R 4.1.0)
gmp
                          0.3.0
                                  2019-03-25 [1] CRAN (R 4.1.0)
gtable
haven
                        * 2.4.3
                                  2021-08-04 [1] CRAN (R 4.1.0)
highr
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hms
                          1.1.0
                                  2021-05-17 [1] CRAN (R 4.1.0)
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                                  2021-09-08 [1] CRAN (R 4.1.1)
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httr
                          1.4.2
                                  2020-07-20 [1] CRAN (R 4.1.0)
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                          1.0.13
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                          0.4.2
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jsonlite
                          1.7.2
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                                  2019-09-22 [1] CRAN (R 4.1.0)
```

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                         5.86
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                         2.5.1
R6
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readxl
remotes
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                                 2018-06-08 [1] CRAN (R 4.1.0)
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                         0.4.11
                                 2021-04-30 [1] CRAN (R 4.1.0)
rlang
rmarkdown
                         2.11
                                 2021-09-14 [1] CRAN (R 4.1.1)
                       * 0.2
                                 2021-06-28 [1] Github (wspiller/rmvmr@5b1198b)
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                         0.93-8
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                         0.13
                                 2020-11-12 [1] CRAN (R 4.1.0)
                         1.0.1
                                 2021-07-26 [1] CRAN (R 4.1.0)
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                                 2020-05-11 [1] CRAN (R 4.1.0)
                       * 1.1.1
                                 2018-11-05 [1] CRAN (R 4.1.0)
sessioninfo
shape
                         1.4.6
                                 2021-05-19 [1] CRAN (R 4.1.0)
SparseM
                         1.81
                                 2021-02-18 [1] CRAN (R 4.1.0)
Statamarkdown
                       * 0.7.0
                                 2021-09-15 [1] Github (Hemken/Statamarkdown@a68a8b9)
                         1.7.4
stringi
                                 2021-08-25 [1] CRAN (R 4.1.1)
                       * 1.4.0
                                 2019-02-10 [1] CRAN (R 4.1.0)
stringr
survival
                         3.2-13 2021-08-24 [2] CRAN (R 4.1.1)
tibble
                       * 3.1.4
                                 2021-08-25 [1] CRAN (R 4.1.1)
tidyr
                       * 1.1.3
                                 2021-03-03 [1] CRAN (R 4.1.0)
                                 2021-04-30 [1] CRAN (R 4.1.0)
tidyselect
                         1.1.1
tidyverse
                       * 1.3.1
                                 2021-04-15 [1] CRAN (R 4.1.0)
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                         0.1.2
                                 2021-07-20 [1] CRAN (R 4.1.0)
utf8
                         1.2.2
                                 2021-07-24 [1] CRAN (R 4.1.0)
vctrs
                         0.3.8
                                 2021-04-29 [1] CRAN (R 4.1.0)
viridisLite
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                                 2021-04-13 [1] CRAN (R 4.1.0)
                         2.4.2
                                 2021-04-18 [1] CRAN (R 4.1.0)
withr
xfun
                         0.26
                                 2021-09-14 [1] CRAN (R 4.1.1)
xm12
                         1.3.2
                                 2020-04-23 [1] CRAN (R 4.1.0)
yaml
                         2.2.1
                                 2020-02-01 [1] CRAN (R 4.1.0)
```

- [1] C:/Users/eptmp/Documents/R/win-library/4.1
- [2] C:/Program Files/R/R-4.1.1/library

Stata session information for reproducibility

```
about
ado describe mrrobust

Stata/MP 16.1 for Windows (64-bit x86-64)
Revision 08 Jul 2021
```

Total physical memory: 32.00 GB Available physical memory: 20.07 GB

Copyright 1985-2019 StataCorp LLC

Stata license: Unlimited-user 2-core network, expiring 21 Jan 2022

Serial number: 501609352178 Licensed to: Tom Palmer

University of Bristol

[89] package mrrobust from https://raw.github.com/remlapmot/mrrobust/master

TITLE

'mrrobust': Stata package for two-sample Mendelian randomization analyses

DESCRIPTION/AUTHOR(S)

Author: Tom Palmer

Distribution-Date: 20210917

INSTALLATION FILES

m\mrmedian.ado

m\mrmedian.sthlp

m\mrmedianobs.ado

m\mrmedianobs_work.ado

m\mrmedianobs.sthlp

m\mregger.ado

m\mregger.sthlp

m\mrrobust.sthlp

m\mreggerplot.ado

m\mreggerplot.sthlp

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References

- Burgess, S, F Dudbridge, and SG Thompson. 2015. "Multivariable Mendelian randomization: the use of pleiotropic genetic variants to estimate causal effects." *American Journal of Epidemiology* 181: 251--260. https://doi.org/10.1093/aje/kwu283.
- Rees, J, A Wood, and S Burgess. 2017. "Extending the MR-Egger method for multivariable Mendelian randomization to correct for both measured and unmeasured pleiotropy." Statistics in Medicine 36: 4705–18. https://doi.org/10.1002/sim.7492.
- Sanderson, E, G Davey Smith, F Windmeijer, and J Bowden. 2019. "An examination of multivariable Mendelian randomization in the single-sample and two-sample summary data settings." *International Journal of Epidemiology* 48: 713–27. https://doi.org/10.1093/ije/dyy262.
- Sanderson, E, W Spiller, and J Bowden. 2021. "Testing and Correcting for Weak and Pleiotropic Instruments in Two-Sample Multivariable Mendelian Randomization." Statistics in Medicine. https://doi.org/10.1002/sim.9133.