

# **Tutorial 2: A simple charged system**

June 7, 2017

# **Contents**

1	Introduction	1
2	Basic set up	2
3	Equilibration	4
4	Running the simulation	6
5	Analysis	6
6	Task - Real units	8
7	2D Electrostatics and Constraints	8

# 1 Introduction

This tutorial introduces some of the basic features of ESPResSo for charged systems by constructing a simulation script for a simple salt crystal. In the subsequent task, we use to a more realistic force-field for a NaCl crystal. Finally, we introduce constraints and 2D-Electrostatics to simulate a molten salt in a parallel plate capacitor. We assume

that the reader is familiar with the basic concepts of Python and MD simulations. The code pieces can be copied step by step into a python script file, which then can be run using pypresso <file> from the ESPResSo build directory. Note that you might have to correct erroneous line breaks. Compile espresso with the following features in your myconfig.hpp to be set throughout the whole tutorial:

```
#define EXTERNAL_FORCES
#define CONSTRAINTS
#define MASS
#define ELECTROSTATICS
#define LENNARD_JONES
```

# 2 Basic set up

The script for the tutorial can be found in your build directory at \doc\tutorials\python\02-charged\_system\nacl.py. We start with setting up all the relevant simulation parameters in one place:

```
# System parameters
n_part = 200
n_ionpairs = n_part/2
density = 0.7
time_step = 0.01
temp = 1.0
gamma = 1.0
l_bjerrum = 1.0
num_steps_equilibration = 1000
num_configs = 100
integ_steps_per_config = 1000
# Particle parameters
                                 0, "Cation": 1}
           = {"Anion":
types
            = {"Anion": n_ionpairs, "Cation": n_ionpairs}
numbers
            = {"Anion": -1.0, "Cation": 1.0}
charges
            = {"Anion":
                              1.0, "Cation": 1.0}
lj_sigmas
lj_epsilons = {"Anion":
                              1.0, "Cation": 1.0}
WCA_cut = 2.**(1. / 6.)
            = {"Anion":
                         WCA_cut * lj_sigmas["Anion"],
lj_cuts
               "Cation": WCA_cut * lj_sigmas["Cation"]}
```

These variables do not change anything in the simulation engine, but are just standard Python variables. They are used to increase the readability and flexibility of the script. The box length is not a parameter of this simulation, it is calculated from the number of particles and the system density. This allows to change the parameters later easily,

e. g. to simulate a bigger system. We use dictionaries for all particle related parameters, which is less error-prone and readable as we will see later when we actually need the values. The parameters here define a purely repulsive, equally sized, monovalent salt.

The simulation engine itself is modified by changing the espressomd. System() properties. We create an instance system and set the box length, periodicity and time step. The skin depth skin is a parameter for the link-cell system which tunes its performance, but shall not be discussed here. Further, we activate the Langevin thermostat for our NVT ensemble with temperature temp and friction coefficient gamma.

```
# Setup System
system = espressomd.System()
box_1 = (n_part / density)**(1. / 3.)
system.box_1 = [box_1, box_1, box_1]
system.periodicity = [1, 1, 1]
system.time_step = time_step
system.cell_system.skin = 0.3
system.thermostat.set_langevin(kT=temp, gamma=gamma)
```

We now fill this simulation box with particles at random positions, using type and charge from our dictionaries. Using the length of the particle list system.part for the id, we make sure that our particles are numbered consecutively. The particle type is used to link non-bonded interactions to a certain group of particles.

Before we can really start the simulation, we have to specify the interactions between our particles. We already defined the Lennard-Jones parameters at the beginning, what is left is to specify the combination rule and to iterate over particle type pairs. For simplicity, we implement only the *Lorentz-Berthelot* rules. We pass our interaction pair to system.non\_bonded\_inter[\*,\*] and set the pre-calculated LJ parameters epsilon, sigma and cutoff. With shift="auto", we shift the interaction potential to the cutoff so that  $U_{LJ}(r_{cutoff}) = 0$ .

```
def combination_rule_epsilon(rule, eps1, eps2):
    if rule=="Lorentz":
```

```
return (eps1*eps2)**0.5
    else:
        return ValueError("No combination rule defined")
def combination_rule_sigma(rule, sig1, sig2):
    if rule == "Berthelot":
        return (sig1+sig2)*0.5
    else:
        return ValueError("No combination rule defined")
# Lennard-Jones interactions parameters
for s in [["Anion", "Cation"],
          ["Anion", "Anion"],
["Cation", "Cation"]]:
        lj_sig = combination_rule_sigma(
                "Berthelot",
                lj_sigmas[s[0]],lj_sigmas[s[1]])
        lj_cut = combination_rule_sigma(
                "Berthelot",
                lj_cuts[s[0]],lj_cuts[s[1]])
        lj_eps = combination_rule_epsilon(
                "Lorentz",
                lj_epsilons[s[0]],lj_epsilons[s[1]])
        system.non_bonded_inter[types[s[0]], types[s[1]]].
   lennard_jones.set_params(epsilon = lj_eps, sigma = lj_sig,
   cutoff = lj_cut, shift = "auto")
```

# 3 Equilibration

With randomly positioned particles, we most likely have huge overlap and the strong repulsion will cause the simulation to crash. The next step in our script therefore is a suitable LJ equilibration. This is known to be a tricky part of a simulation and several approaches exist to reduce the particle overlap. Here, we use a highly damped system (huge gamma in the thermostat) and cap the forces of the LJ interaction. We use system .analysis.mindist to get the minimal distance between all particles pairs. This value is used to progressively increase the force capping. This results in a slow increase of the force capping at strong overlap. At the end, we reset our thermostat to the target values and deactivate the force cap by setting it to zero.

```
print("\n--->Lennard Jones Equilibration")
max_sigma = max(lj_sigmas.values())
min_dist = 0.0
cap = 10.0
#Warmup Helper: Cold, highly damped system
system.thermostat.set_langevin(kT=temp*0.1, gamma=gamma*50.0)
```

ESPResSo uses so-called actors for electrostatics, magnetostatics and hydrodynamics. This ensures that unphysical combinations of algorithms are avoided, for example simultaneous usage of two electrostatic interactions. Adding an actor to the system also activates the method and calls necessary initialization routines. Here, we define a  ${\rm P^3M}$  object with parameters Bjerrum length and rms force error . This automatically starts a tuning function which tries to find optimal parameters for  ${\rm P^3M}$  and prints them to the screen:

Before the production part of the simulation, we do a quick temperature equilibration. For the output, we gather all energies with system.analysis.energy(), calculate the temperature from the ideal part and print it to the screen along with the total and Coulomb energies. We integrate for a certain amount of steps with system.integrator.run(100).



Figure 1: VMD Snapshot of the salt system

# 4 Running the simulation

Now we can integrate the particle trajectories for a couple of time steps. Our integration loop basically looks like the equilibration:

Additionally, we append all particle configurations in the core with system.analysis. append() for a very convenient analysis later on.

# 5 Analysis

Now, we want to calculate the averaged radial distribution functions  $g_{++}(r)$  and  $g_{+-}(r)$  with the rdf() command from system.analysis:

```
print("\n--->Analysis")
# Calculate the averaged rdfs
rdf_bins = 100
r_min = 0.0
r_max = system.box_1[0]/2.0
r,rdf_00 = system.analysis.rdf(rdf_type='<rdf>',
```

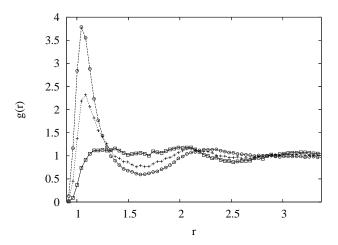


Figure 2: Radial distribution functions  $g_{++}(r)$  between equal charges (rectangles) and  $g_{+-}(r)$  for opposite charges (circles). The plus symbols denote g(r) for an uncharged system.

The shown rdf() commands return the radial distribution functions for equally and oppositely charged particles for specified radii and number of bins. In this case, we calculate the averaged rdf of the stored configurations, denoted by the chevrons in rdf\_type='<rdf'' would simply calculate the rdf of the current particle configuration. The results are two NumPy arrays containing the r and g(r) values. Finally we write the data into a file with standard python output routines.

Fig. 2 shows the resulting radial distribution functions. In addition, the distribution for a neutral system is given, which can be obtained from our simulation script by simply

not adding the P<sup>3</sup>M actor to the system. To view your own results, run gnuplot in a Terminal window and plot the simulation data:

```
p 'rdf.data' u 1:2 w lp t 'g(r) ++' , '' u 1:3 w lp t 'g(r) +-'
```

#### 6 Task - Real units

So far, the system has arbitrary units and is not connected to any real physical system. Simulate a proper NaCl crystal with the force field parameter taken from:

- R. Fuentes-Azcatl and M. Barbosa, Sodium Chloride,  $NaCl/\epsilon$ : New Force Field,
- J. Phys. Chem. B, 2016, 120(9), pp 2460-2470

	q/e	$\sigma/{ m \AA}$	$(\epsilon/k_{\rm B})/{ m K}$	$m/\mathrm{u}$
Na	+1	2.52	17.44	22.99
Cl	-1	3.85	192.45	35.453

Use the following system parameters:

Temperature	$298 \mathrm{~K}$
Friction Coeff.	$10 \text{ ps}^{-1}$
Density	$1.5736 \text{ uÅ}^{-3}$
Bjerrum length(298 K)	439.2 Å
Time step	2 fs

To make your life more easy, don't try to equilibrate randomly positioned particles, but set them up in a crystal structure close to equilibrium. If you do it right, you don't even need the Lennard-Jones equilibration. To speed things up, don't go further than 1000 particles and use a  $P^3M$  accuracy of  $10^{-2}$ . Your RDF should look like the plot in figure 3. When you get stuck, you can look at the solution script \doc\tutorials\python\02-charged\_system\nacl\_units.py (or nacl\_units\_vis.py with visualization).

#### 7 2D Electrostatics and Constraints

In this section, we use the parametrized NaCl system from the last task to simulate a molten salt in a parallel plate capacitor with and without applied electric field. We have to extend our simulation by several aspects:

#### Confinement

ESPResSo features a number of basic shapes like cylinders, walls or spheres to simulate confined systems. Here, we use to walls at z = 0 and  $z = L_z$  for the parallel plate setup  $(L_z$ : Box length in z-direction).

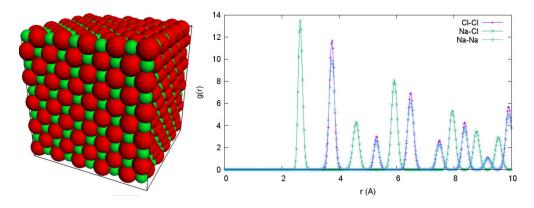


Figure 3: Snapshot and RDF of the parametrized NaCl crystal.

#### **2D-Electrostatics**

ESPResSo also has a number of ways to account for the unwanted electrostatic interaction in the now non-periodic z-dimension. We use the 3D-periodic  $P^3M$  algorithm in combination with the *Electrostatic Layer Correction* (ELC). ELC subtracts the forces caused by the periodic images in the z-dimension. Another way would be to use the explicit 2D-electrostatics algorithm MMM2D, also available in ESPResSo.

#### **Electric Field**

The simple geometry of the system allows us to treat an electric field in z-direction as a homogeneous force. Note that we use inert walls here and don't take into account the dielectric contrast caused by metal electrodes.

#### **Parameters**

For our molten NaCl, we use a temperature 100 K above the melting point (1198.3 K) and an approximated density of  $\rho = 1.1138 \text{ uÅ}^{-3}$  found in

Janz, G. J., Thermodynamic and Transport Properties of Molten Salts: Correlation Equations for Critically Evaluated Density, Surface Tension, Electrical Conductance, and Viscosity Data, *J. Phys. Chem. Ref. Data*, 17, Suppl. 2, 1988.

Let's walk through the python script. We need additional imports for the wall shapes and the ELC algorithm:

```
from espressond import *
from espressond.shapes import *
from espressond import electrostatics
from espressond import electrostatic_extensions
import numpy
```

If we target a liquid system, we should not set up the particles in a lattice, as this introduces unwanted structure in the starting configuration. We define our system size

by the number of particles and the density. The system parameters lead to the following values:

```
system = espressomd.System()
print("\n--->Setup system")
# System parameters
n_part = 500
n_ionpairs = n_part/2
density = 1.1138
time_step = 0.001823
temp = 1198.3
gamma = 50
\#1_bjerrum = 0.885^2 * e^2/(4*pi*epsilon_0*k_B*T)
l_bjerrum = 130878.0 / temp
wall_margin = 0.5
Ez = 0
num_steps_equilibration = 3000
num_configs = 200
integ_steps_per_config = 100
```

We save the force field parameters in python dictionaries, now with parameters for the walls:

```
# Particle parameters
                              0, "Na": 1, "Electrode": 2}
           = {"Cl":
types
numbers
           = {"Cl": n_ionpairs, "Na": n_ionpairs}
charges
           = {"Cl":
                          -1.0, "Na": 1.0}
           = {"Cl":
                           3.85, "Na": 2.52,
                                             "Electrode": 3.37}
lj_sigmas
lj_epsilons = {"Cl":
                         192.45, "Na": 17.44, "Electrode": 24.
   72}
            = {"Cl":
lj_cuts
                            3.0 * lj_sigmas["C1"],
               "Na":
                            3.0 * lj_sigmas["Na"],
               "Electrode": 3.0 * lj_sigmas["Electrode"]}
                      35.453, "Na": 22.99, "Electrode": 12.01}
            = {"Cl":
masses
```

To finally calculate the box size, we take into account the diameter of the electrode interaction. Additionally, ELC needs a particle-free gap in the z-direction behind the wall.

```
# Setup System
box_l = (n_ionpairs * sum(masses.values()) / density)**(1. / 3.)
box_z = box_l + 2.0 * (lj_sigmas["Electrode"]+wall_margin)
box_volume = box_l * box_l * box_z
```

```
elc_gap = box_z * 0.15
system.box_l = [box_l, box_l, box_z + elc_gap]
system.periodicity = [1, 1, 1]
system.time_step = time_step
system.cell_system.skin = 0.3
system.thermostat.set_langevin(kT=temp, gamma=gamma)
```

In the next snippet, we add the walls to our system. Our constraint takes two arguments: First the shape, in our case a simple plane defined by its normal vector and the distance from the origin, second the particle\_type, which is used to set up the interaction between particles and constraints.

Now we place the particles at random position without overlap with the walls:

```
# Place particles
for i in range(n_ionpairs):
    p = numpy.random.random(3)*box_1
    p[2] += lj_sigmas["Electrode"]
    system.part.add(id=len(system.part), type=types["Cl"], pos=
    p, q=charges["Cl"], mass=masses["Cl"])
for i in range(n_ionpairs):
    p = numpy.random.random(3)*box_1
    p[2] += lj_sigmas["Electrode"]
    system.part.add(id=len(system.part), type=types["Na"], pos=
    p, q=charges["Na"], mass=masses["Na"])
```

The scheme to set up the Lennard-Jones interaction is the same as before, extended by the Electrode-Ion interactions:

```
# Lennard-Jones interactions parameters

def combination_rule_epsilon(rule, eps1, eps2):
    if rule=="Lorentz":
        return (eps1*eps2)**0.5
    else:
        return ValueError("No combination rule defined")

def combination_rule_sigma(rule, sig1, sig2):
    if rule=="Berthelot":
        return (sig1+sig2)*0.5
    else:
        return ValueError("No combination rule defined")
```

Next is the Lennard-Jones Equilibration. Here we use an alternative way to get rid of the overlap: ESPResSo features a routine for energy minimization with similar features as in the manual implementation used before. Basically it caps the forces and limits the displacement during integration.

As described, we use  $P^3M$  in combination with ELC to account for the 2D-periodicity. ELC is also added to the actors of the system and takes  $gap\ size$  and  $maximum\ pairwise\ errors$  as arguments.

For now, our electric field is zero, but we want to switch it on later. Here we run over all particles and set an external force on the charges caused by the field:

```
for p in system.part:
    p.ext_force = [0,0,Ez * p.q]
```

This is followed by our standard temperature equilibration:

In the integration loop, we like to measure the density profile for both ion species along the z-direction. We use a simple histogram analysis to accumulate the density data.

```
print("\n--->Integration")
bins=100
z_dens_na = numpy.zeros(bins)
z_dens_cl = numpy.zeros(bins)
system.time = 0.0
cnt = 0
for i in range(num_configs):
    energy = system.analysis.energy()
    temp_measured = energy['ideal'] / ((3.0 / 2.0) * n_part)
    print("t={0:.1f}, E_total={1:.2f}, E_coulomb={2:.2f},
          T={3:.4f}".format(system.time, energy['total'],
          energy['coulomb'], temp_measured))
    system.integrator.run(integ_steps_per_config)
    for p in system.part:
        bz = int(p.pos[2]/box_z*bins)
        if p.type == types["Na"]:
            z_dens_na[bz] += 1.0
        elif p.type == types["C1"]:
            z_dens_cl[bz] += 1.0
    cnt += 1
```

Finally, we calculate the average, normalize the data with the bin volume and save it to a file using NumPy's savetxt command.

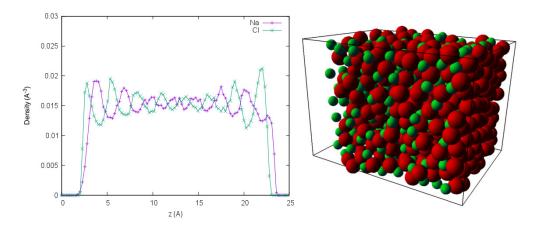


Figure 4: Snapshot and densities along the z-Axis with applied electric field for the ion species.

```
print("\n--->Written z_density.data")
print("\n--->Done")
```

The resulting density plot is very noisy due to insufficient sampling, but should show a slight depletion of the smaller Na atoms at the walls. Now try to put in an electric field that represents an applied voltage of 15 V between the walls and compare the results. The density data (see figure 4) should show strong layering at the walls, decaying towards the system center. The complete script is at

 $\verb|\doc\tutorials|| python \verb|\02-charged_system|| nacl_units_confined.py. |$ 

In the interactive script nacl\_units\_confined\_vis.py, you can increase/decrease the electric field with the keys t/g (at your own risk).