Supplementary material II-S7

Statistical analyses and R outputs related to the main figure Fig. 2

A. Model shape selection

Tree species richness effect on soil microbial facets and functions. For each soil microbial facets and functions, we tested the shape of the relationship using the 'lm' function and the following relations: linear (i.e. $y \sim x$), quadratic (i.e. $y \sim x^2$), polynomial (i.e. $y \sim x + x^2 + x^3$) and logarithmic (i.e. $y \sim \log(x)$). The models were ordered by AIC and considered different when the difference of AIC was higher than 4. When several models had a comparable fit (difference of AIC below 4) the simplest model was chosen (i.e. linear < logarithmic < quadratic < polynomial).

Microbial biomass

Total microbial biomass

Name	Model	AIC	BIC	R2	R2_adjusted	RMSE	Sigma
polynomial	$y \sim \text{poly}(x, \text{degree} = 3)$	2886	2901	0.098	0.079	4013.930	4069.297
linear	$y \sim x$	2889	2898	0.056	0.050	4105.131	4133.153
quadratic	$y \sim x^2$	2889	2898	0.056	0.050	4105.131	4133.153
\log	$y \sim \log(x)$	2893	2902	0.027	0.021	4167.715	4196.163

Active microbial biomass

Name	Model	AIC	BIC	R2	$R2_adjusted$	RMSE	Sigma
polynomial	$y \sim poly(x, degree = 3)$	1768	1783	0.049	0.029	91.784	93.050
linear	$y \sim x$	1770	1779	0.010	0.003	93.621	94.260
quadratic	$y \sim x^2$	1770	1779	0.010	0.003	93.621	94.260
log	$y \sim \log(x)$	1771	1780	0.001	-0.006	94.060	94.702

Microbial taxonomic profile

Bacteria to fungi ratio

Name	Model	AIC	BIC	R2	R2_adjusted	RMSE	Sigma
log	$y \sim \log(x)$	207	216	0.016	0.010	0.477	0.480
linear	$y \sim x$	207	216	0.015	0.008	0.477	0.480
quadratic	$y \sim x^2$	207	216	0.015	0.008	0.477	0.480
polynomial	$y \sim \text{poly}(x, \text{degree} = 3)$	211	226	0.017	-0.004	0.476	0.483

Bacterial Shannon diversity

Name	Model	AIC	BIC	R2	R2_adjusted	RMSE	Sigma
log	$y \sim \log(x)$	388	397	0.060	0.053	0.881	0.887
polynomial	$y \sim poly(x, degree = 3)$	391	406	0.069	0.050	0.876	0.888
linear	$y \sim x$	391	400	0.044	0.037	0.888	0.894
quadratic	$y \sim x^2$	391	400	0.044	0.037	0.888	0.894

Fungal Shannon diversity

Name	Model	AIC	BIC	R2	R2_adjusted	RMSE	Sigma
log	$y \sim \log(x)$	-98	-89	0.000	-0.006	0.170	0.171
linear	$y \sim x$	-98	-89	0.000	-0.007	0.170	0.171
quadratic	$y \sim x^2$	-98	-89	0.000	-0.007	0.170	0.171
polynomial	$y \sim poly(x, degree = 3)$	-97	-82	0.014	-0.006	0.169	0.171

Microbial functional profile

Catabolism functional genes

Name	Model	AIC	BIC	R2	R2_adjusted	RMSE	Sigma
log	$y \sim \log(x)$	566	575	0.010	0.003	1.604	1.615
linear	$y \sim x$	566	575	0.007	0.000	1.607	1.618
quadratic	$y \sim x^2$	566	575	0.007	0.000	1.607	1.618
polynomial	$y \sim \text{poly}(x, \text{ degree} = 3)$	569	584	0.014	-0.007	1.601	1.624

Functional genes evenness

Name	Model	AIC	BIC	R2	$R2_adjusted$	RMSE	Sigma
\log	$y \sim \log(x)$	-455	-446	0.003	-0.003	0.051	0.051
linear	$y \sim x$	-455	-446	0.003	-0.004	0.051	0.051
quadratic	$y \sim x^2$	-455	-446	0.003	-0.004	0.051	0.051
polynomial	$y \sim \text{poly}(x, \text{ degree} = 3)$	-452	-437	0.011	-0.010	0.051	0.051

Microbial physiological potential

Substrate-induced respiration efficiency

Name	Model	AIC	BIC	R2	R2_adjusted	RMSE	Sigma
linear	y ~ x	41	50	0.071	0.064	0.272	0.274
quadratic	$y \sim x^2$	41	50	0.071	0.064	0.272	0.274
\log	$y \sim \log(x)$	42	51	0.063	0.057	0.274	0.275
polynomial	$y \sim poly(x, degree = 3)$	45	60	0.072	0.053	0.272	0.276

${\bf Substrate\text{-}induced\ respiration\ response\ range}$

Name	Model	AIC	BIC	R2	R2_adjusted	RMSE	Sigma
log	$y \sim \log(x)$	340	349	0.005	-0.002	0.749	0.754
linear	$y \sim x$	341	350	0.003	-0.003	0.750	0.755
quadratic	$y \sim x^2$	341	350	0.003	-0.003	0.750	0.755
polynomial	$y \sim poly(x, degree = 3)$	345	360	0.004	-0.017	0.749	0.760

${\bf Microbial\ respiration}$

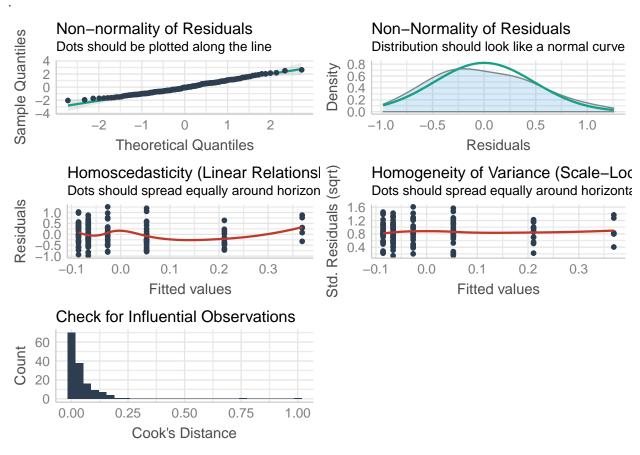
Name	Model	AIC	BIC	R2	R2_adjusted	RMSE	Sigma
linear	y ~ x	149	157	0.023	0.017	0.392	0.394
quadratic	$y \sim x^2$	149	157	0.023	0.017	0.392	0.394
\log	$y \sim \log(x)$	150	159	0.015	0.009	0.393	0.396
polynomial	$y \sim \text{poly}(x, \text{degree} = 3)$	151	166	0.035	0.015	0.389	0.395

B. Model quality check

Tree species richness effect on soil microbial facets and functions. The relation was tested using the "lm" function in R. Model statistical assumptions were tested using the "check_model" function from the R package "performance".

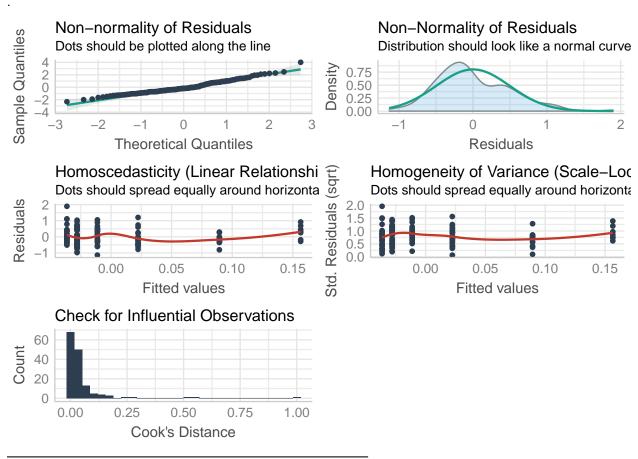
Microbial biomass

Total microbial biomass



Explanatory	Estimate	SE	t.value	p.value
(Intercept)	-0.106	0.054	-1.96	0.051
Tree species richness	0.02	0.007	2.95	0.004

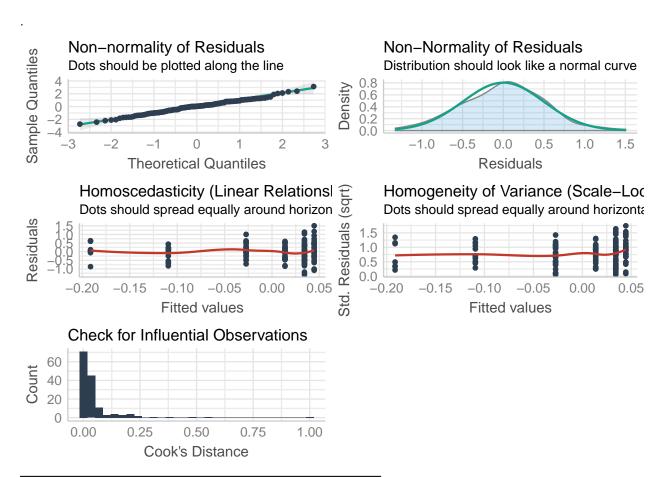
Active microbial biomass



Explanatory	Estimate	SE	t.value	p.value
(Intercept)	-0.045	0.055	-0.81	0.417
Tree species richness	0.008	0.007	1.22	0.224

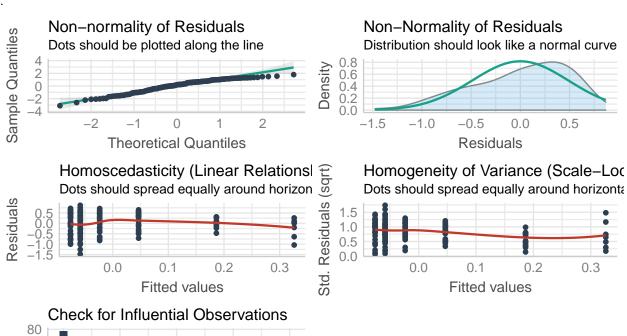
Microbial taxonomic profile

Bacteria to fungi ratio



Explanatory	Estimate	SE	t.value	p.value
(Intercept)	0.055	0.055	1	0.32
Tree species richness	-0.01	0.007	-1.5	0.137

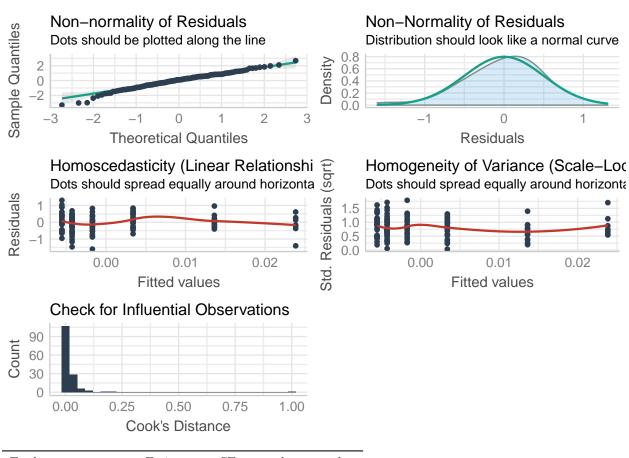
Bacterial Shannon diversity



nt	80 60 40 20	Check	ior milc	ientiai C	oservau	ons
		0.00	0.25	0.50	0.75	1.00
	Cook's Distance					

Explanatory	Estimate	SE	t.value	p.value
(Intercept)	-0.093	0.054	-1.72	0.087
Tree species richness	0.017	0.007	2.59	0.011

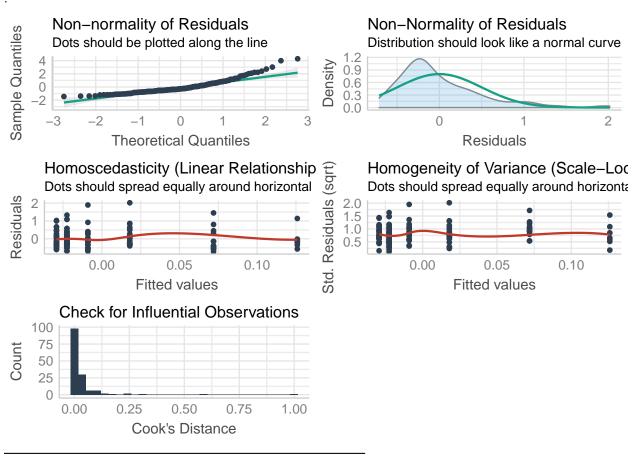
Fungal Shannon diversity



Explanatory	Estimate	SE	t.value	p.value
(Intercept)	-0.007	0.055	-0.12	0.902
Tree species richness	0.001	0.007	0.18	0.854

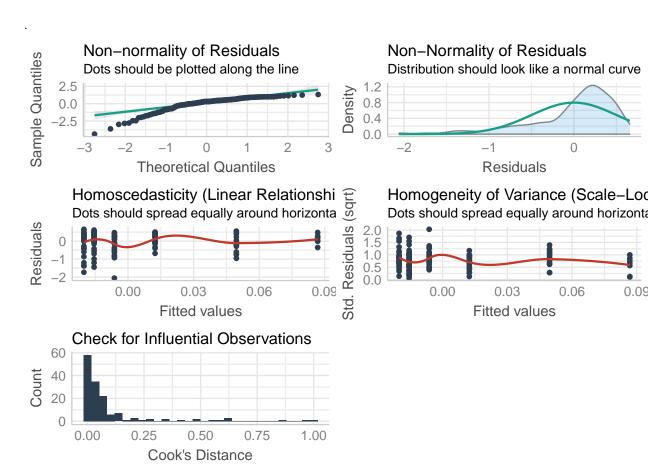
Microbial functional profile

Catabolism functional genes



Explanatory	Estimate	SE	t.value	p.value
(Intercept)	-0.036	0.055	-0.65	0.515
Tree species richness	0.007	0.007	0.98	0.329

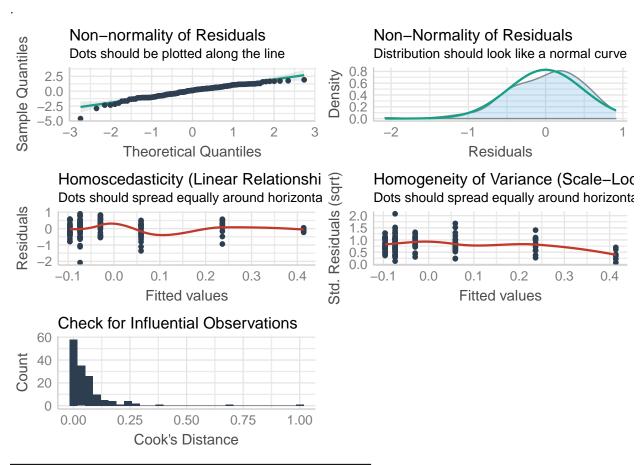
Functional genes evenness



Explanatory	Estimate	SE	t.value	p.value
(Intercept)	-0.025	0.055	-0.45	0.654
Tree species richness	0.005	0.007	0.67	0.501

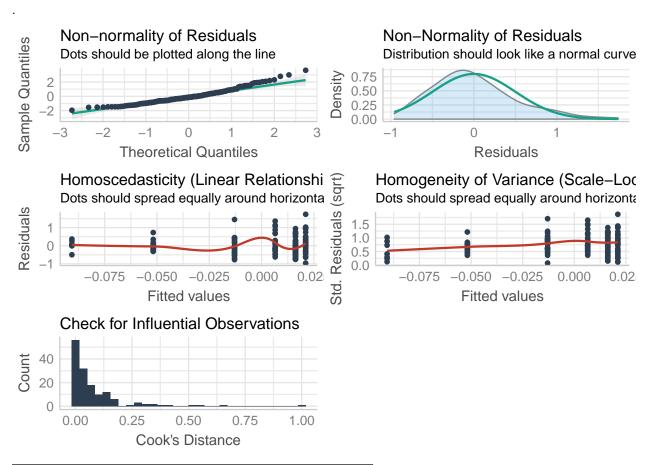
Microbial physiological potential

Substrate-induced respiration efficiency



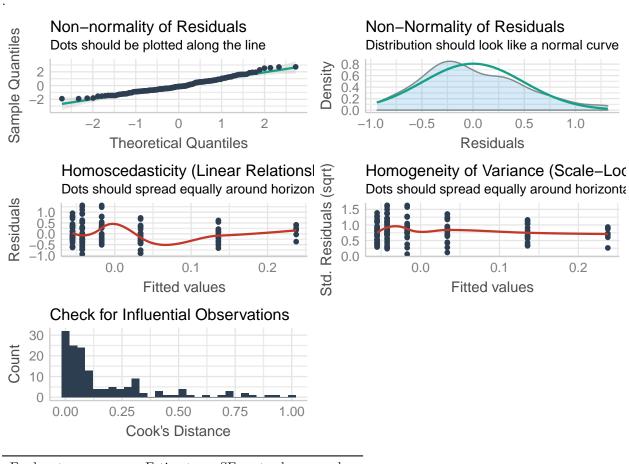
Explanatory	Estimate	SE	t.value	p.value
(Intercept)	-0.118	0.053	-2.22	0.028 0.001
Tree species richness	0.022	0.007	3.33	0.0

Substrate-induced respiration response range



Explanatory	Estimate	SE	t.value	p.value
(Intercept)	0.026	0.055	0.47	0.639
Tree species richness	-0.005	0.007	-0.7	0.482

Microbial respiration



Explanatory	Estimate	SE	t.value	p.value
(Intercept)	-0.068	0.055	-1.24	0.216
Tree species richness	0.013	0.007	1.86	0.064