

Game Theory Problem Set 3

	L	R
T	<u>$3+\epsilon_2$</u> , 0	0
B	0, <u>$3+\epsilon_1$</u>	0

Best responses underlined.

By inspection, (T,L) and (B,R) are the only pure strategy Nash equilibria where players play mutual best responses.

Suppose that there is some NE where P1 mixes. P1 plays a mixed strategy, and plays action T with probability p and action B with probability $1-p$. Then, $\pi_1(T, \sigma_2^*) = \pi_1(B, \sigma_2^*)$, $q = (3+\epsilon_1)(1-q)$, where q is the probability that strategy of player 2 σ_2^* at U^* assigns to L such that P1 has no profitable deviation $q = \frac{3+\epsilon_1}{4+\epsilon_1}$. Then P2 plays a mixed strategy at U^* , so $\pi_2(L, \sigma_1^*) = \pi_2(R, \sigma_1^*)$, $(3+\epsilon_2)p = 1-p$, $p = \frac{1}{4+\epsilon_2}$. So $U^* = (\frac{1}{4+\epsilon_2} T + (1-\frac{1}{4+\epsilon_2}) B, qL + (1-q)R)$ is a mixed strategy NE where $p = \frac{1}{4+\epsilon_2}$ and $q = \frac{3+\epsilon_1}{4+\epsilon_1}$. From the above argument if P1 mixes, so does P2. By symmetry, if P2 mixes, so does P1. Then, there are no hybrid NE.

Let σ^* denote the pure BNE where P1 plays T if $\epsilon_1 < \epsilon_1^*$ and B otherwise and P2 plays L if $\epsilon_2 > \epsilon_2^*$ and R otherwise.

ϵ_1^* and ϵ_2^* is the convention

$$\pi_1(T, \sigma_2^*) = P(\epsilon_2 > \epsilon_2^*) \times 1 + P(\epsilon_2 < \epsilon_2^*) \times 0$$

$$= \frac{\epsilon_2^*}{\epsilon} (1 - \frac{\epsilon_2^*}{\epsilon})$$

$$\pi_1(B, \sigma_2^*) = P(\epsilon_2 > \epsilon_2^*) \times 0 + P(\epsilon_2 < \epsilon_2^*) \times (3+\epsilon_1)$$

$$= \frac{\epsilon_2^*}{\epsilon} (3+\epsilon_1)$$

$$\pi_1(T, \sigma_2^*) \geq \pi_1(B, \sigma_2^*) \text{ iff}$$

$$1 - \frac{\epsilon_2^*}{\epsilon} \geq \frac{\epsilon_2^*}{\epsilon} (3+\epsilon_1)$$

$$1 \geq \frac{\epsilon_2^*}{\epsilon} (4+\epsilon_1)$$

$$4+\epsilon_1 \leq \frac{\epsilon}{\epsilon_2^*}$$

$$\epsilon_1 \leq \frac{\epsilon}{\epsilon_2^*} - 4$$

Since σ^* is a BNE, P1 has no profitable deviation from σ^* , so under σ^* P1 plays T if $\pi_1(T, \sigma_2^*) \geq \pi_1(B, \sigma_2^*)$ iff $\epsilon_1 \leq \frac{\epsilon}{\epsilon_2^*} - 4$ iff $\epsilon_1 < \frac{\epsilon}{\epsilon_2^*} - 4$, so $\epsilon_1^* = \frac{\epsilon}{\epsilon_2^*} - 4$

$\pi_1(B, \sigma_2^*)$ iff $\epsilon_1 < \frac{\epsilon}{\epsilon_2^*} - 4$ iff $\epsilon_1 < \frac{\epsilon}{\epsilon_2^*} - 4$, so $\epsilon_1^* = \frac{\epsilon}{\epsilon_2^*} - 4$

$$\pi_2(L, \sigma_1^*) = P(\epsilon_1 < \epsilon_1^*) \times (3+\epsilon_2) + P(\epsilon_1 > \epsilon_1^*) \times 0$$

$$= \frac{\epsilon_1^*}{\epsilon} (3+\epsilon_2)$$

$$\pi_2(R, \sigma_1^*) = P(\epsilon_1 < \epsilon_1^*) \times 0 + P(\epsilon_1 > \epsilon_1^*) \times 1$$

$$= 1 - \frac{\epsilon_1^*}{\epsilon}$$

$$\pi_2(L, \sigma_1^*) \geq \pi_2(R, \sigma_1^*) \text{ iff}$$

$$\frac{\epsilon_1^*}{\epsilon} (3+\epsilon_2) \geq 1 - \frac{\epsilon_1^*}{\epsilon}$$

$$\frac{\epsilon_1^*}{\epsilon} (3+\epsilon_2) \geq 1$$

$$3+\epsilon_2 \geq \frac{\epsilon}{\epsilon_1^*}$$

$$\epsilon_2 \geq \frac{\epsilon}{\epsilon_1^*} - 3$$

$$\epsilon_2^* = \frac{\epsilon}{\epsilon_1^*} - 3$$

By substitution,

$$\epsilon_1^* = \frac{\epsilon}{(\frac{\epsilon}{\epsilon_1^*} - 3) - 4} - 4$$

$$= \frac{\epsilon}{\frac{\epsilon}{\epsilon_1^*} - 7} - 4$$

Supposing that the BNE is symmetric, i.e. $\epsilon_1^* = \epsilon_2^*$,

$$\begin{aligned} \varepsilon_1^* &= \bar{\varepsilon} / \varepsilon_1^* - 4, \\ (\varepsilon_1^* + 4) \varepsilon_1^* &= \bar{\varepsilon} \\ (\varepsilon_1^* + 2)^2 &= \bar{\varepsilon} + 4 \\ \varepsilon_1^* &= -2 + \sqrt{\bar{\varepsilon} + 4} \text{ or } -2 - \sqrt{\bar{\varepsilon} + 4} \text{ (reject since } \varepsilon_1^* \in [0, \bar{\varepsilon}]) \\ \text{Then } \varepsilon_2^* &= \varepsilon_1^* = -2 + \sqrt{\bar{\varepsilon} + 4}. \\ \varepsilon_2^* &= \bar{\varepsilon} / \varepsilon_2^* - 4, \text{ so P.2 has no profitable deviation, and} \\ x^* &\text{ is a BNE.} \end{aligned}$$

Can show symmetric NE by multiplying to get $\varepsilon_1^* \varepsilon_2^* = \dots$, $\varepsilon_2^* \varepsilon_1^* = \dots$, then $\varepsilon_1 = \varepsilon_2$

c Let p and q denote the ex ante probability that P.1 plays T and the ex ante probability that P.2 plays C respectively.

$$\begin{aligned} p &= P(\varepsilon_1 < \varepsilon_1^*) = \varepsilon_1^* / \bar{\varepsilon} = -2 + \sqrt{\bar{\varepsilon} + 4} / \bar{\varepsilon} \\ &= (-2 + \sqrt{\bar{\varepsilon} + 4}) \times (-2 + \sqrt{\bar{\varepsilon} + 4}) / \bar{\varepsilon} (\sqrt{\bar{\varepsilon} + 4} + 2) \\ &= \frac{1}{\sqrt{\bar{\varepsilon} + 4} + 2} \end{aligned}$$

$$q = P(\varepsilon_2 > \varepsilon_2^*) = 1 - \varepsilon_2^* / \bar{\varepsilon} = 1 - \frac{1}{\sqrt{\bar{\varepsilon} + 4} + 2}$$

$$\lim_{\bar{\varepsilon} \rightarrow 0} p = 1/4$$

$$\lim_{\bar{\varepsilon} \rightarrow 0} q = 3/4$$

The ex ante probability distributions of ~~the~~ induced by the pure NE of the perturbed game converge to the probability distribution of the mixed NE in the unperturbed game (where $\varepsilon_1 = \varepsilon_2 = 0$), where from the result in (a), $p = 1/4 + \varepsilon_2 = 1/4$, $q = 3/4 + \varepsilon_1/4 + \varepsilon_1 = 3/4$.

d Mixed NE are difficult to justify because at the mixed NE, each player has equal ~~to~~ for each player, each of the actions he mixes ~~to~~ yields equal expected payoff, so each player has no incentive to mix over these actions in any particular way.

Harsanyi's purification theorem is that the probability distributions induced by the pure BNE of the perturbed game in which players use threshold strategies converges ~~to~~, as the perturbation vanishes, to the probability distribution of the mixed NE in the unperturbed strategic form game.

Harsanyi's purification theorem ~~can be interpreted~~ justifies mixed NE in the sense that the players who mix can be understood as responding to an unobservable, vanishingly small payoff shock, i.e. a whim.

Can solve w/ L'Hopital's rule

there are limits rules

No strict reason to play any mixed strategy \rightarrow unsatisfactory

"some small fact not modeled in the game" players don't actually randomise, but choose based on $\varepsilon_1, \varepsilon_2$, but it appears that they randomise to others

Alt interpretation \rightarrow different types of people

Harsanyi: any game is a simplification, so there are unmodelled shocks

2a. Players: $N = \{S, G\}$

Actions: $A_S = \{L, R\}$, $A_G = \{l, r\}$

States: $\Sigma = \{SH, SR\}$

Signals: $t_S(SH) = SH$, $t_S(SR) = SR$, $t_G(SH) = t_G(SR)$

Beliefs: $\frac{P_S(SH|t_S) + P_S(SR|t_S)}{P_S(SH|t_S) + P_S(SR|t_S)} =$

$$P_G(t_S = SH | t_G) = P_G(t_S = SR | t_G) = 1/2$$

Payoffs:

	l	r		l	r
L	0.3	0	L	0.4	0.2
	0.7	1		0.6	0.8
R	0.2	0.4	R	0	0.3
	0.8	0.6		1	0.7
	SH			SR	

Best responses underlined

In a Bayesian ~~strategic~~ game, player i's strategy is a type-contingent plan of action. Since G has only one type, its strategy σ_G is some action ~~or~~ $a_G \in A_G = \{l, r\}$ or some probability distribution over A_G . S's strategy σ_S is some pair $(\sigma_{SH}, \sigma_{SR})$ where S plays σ_{SH} if $t_S = SH$ and σ_{SR} if $t_S = SR$, and each of σ_{SH} and σ_{SR} is some action $a_S \in A_S = \{L, R\}$ or some probability distribution over A_S .

By inspection of the payoff tables above, S's best response $B_S(a_G) = (R, R)$ if $a_G = l$.

$$B_S(\sigma_G) = (R, R) \text{ if } \sigma_G = l \\ (L, L) \text{ if } \sigma_G = r$$

G's best response

$$B_G(\sigma_S) = \begin{cases} l & \text{if } \sigma_S = (R, R) \\ r & \text{if } \sigma_S = (L, L) \\ \{l, r\} & \text{if } \sigma_S = (R, R) \text{ or } (L, R) \text{ or } (R, L) \end{cases}$$

The payoff table can be rewritten as

	l	r
L	0.35	0.1
	0.65	0.9
R	0.15	0.15
	0.85	0.85
RE	0.1	0.35
	0.9	0.65
RT	0.3	0.3
	0.7	0.7

By inspection, there are no mutual best responses in pure strategies, so there is no pure BNE.

this works because ex ante BR corresponds with interim BR (captured in Eso notes w/ 2)

Let σ^* be a hybrid BNE where G ~~mixes~~ mixes l and r, then $\sigma_G^* = \sigma^*$ let q be the probability σ_G^* assigns to l and $1-q$ be the probability it assigns to r.

$$\pi_S(L, \sigma_G^*; t_S = SH) = 0.7q + (1-q) = 1 - 0.3q$$

$$\pi_S(R, \sigma_G^*; t_S = SH) = 0.8q + 0.6(1-q) = 0.6 + 0.2q$$

$$\pi_S(L, \sigma_G^*; t_S = SR) = 0.6q + 0.8(1-q) = 0.8 - 0.2q$$

$$\pi_S(R, \sigma_G^*; t_S = SR) = q + 0.7(1-q) = 0.7 + 0.3q$$

σ^* is a BNE only if G has no profitable deviation

$$\text{which is iff } \pi_G(l, \sigma_S^*; t_G) = \pi_G(r, \sigma_S^*; t_G)$$

RL dominated by LR
G never mixes against LL, RR

Give intuition

Suppose σ_t plays $\sigma_t = (L, L)$
 $E_G(\pi_G(l, \sigma_t; t_{st})) = 0.35 <$
 $E_G(\pi_G(r, \sigma_t; t_{st})) = 0.1$ from σ^*
 so G can profitably deviate by reallocating probability mass from r to l

By symmetry, if σ_t plays $\sigma_t = (R, R)$, G can profitably deviate by reallocating probability mass from l to r.

Suppose σ_t plays $\sigma_t = (L, R)$
 $E_G(\pi_G(l, \sigma_t; t_{st})) = \frac{1}{2}[0.3q + 0(1-q)] + \frac{1}{2}[0q + 0.3(1-q)]$
 $= 0.15q + 0.15 - 0.15q$
 $= 0.15$

$E_G(\pi_G(r, \sigma_t; t_{st})) = \frac{1}{2}[0.3q + 0(1-q)] + \frac{1}{2}[0q + 0.3(1-q)]$
 $= \frac{1}{2}[0.3q + 0.3(1-q)] = 0.15$

$E_G(\pi_G(r, \sigma_t; t_{st})) = \frac{1}{2}(0) + \frac{1}{2}(0.3) = 0.15$
 Then G has no incentive to deviate for any q.

$\pi_{st}(LR, \sigma_t^*; t_{st} = SL) =$
 $\pi_{st}(\sigma_t, \sigma_t^*; t_{st} = SL) = 0.7q + 1(1-q) = 1 - 0.3q >$
 $\pi_{st}(\sigma_t, \sigma_t^*; t_{st} = SL) = 0.8q + 0.6(1-q) = 0.6 + 0.2q$
 where σ_t^* is a pure strategy of σ_t that yields a different action given t_{st} , and
 $\pi_{st}(\sigma_t, \sigma_t^*; t_{st} = SR) = q + 0.7(1-q) = 0.7 + 0.3q >$
 $\pi_{st}(\sigma_t, \sigma_t^*; t_{st} = SR) = 0.6q + 0.8(1-q) = 0.8 - 0.2q$
 $1 - 0.3q > 0.6 + 0.2q, 0.4 > 0.2q, 0.5q > 0.1, q > 0.2$
 $0.7 + 0.3q > 0.8 - 0.2q, 0.5q > 0.1, q > 0.2$
 so $\sigma^* = (LR, q \cdot l + (1-q) \cdot r)$ is a hybrid BNE
 for all $q \in (0.2, 0.8)$

c Argue: "show", more is required

Devote
 P_L the prob that ~~type~~ SL chooses L
 P_R the prob that SR chooses R
 Then find $\pi_G(L), \pi_G(R)$
 Then $P_L + P_R = 1$
 Solve for q
 σ_t SL and SR are each indiff.
 Then ~~if~~ σ_t is mixing between LR, ~~RL~~,
 but $\pi_{st}(LR) > \pi_{st}(RL)$, so no eqm

Suppose that σ_t plays $\sigma_t = (R, L)$
 $E_G(\pi_G(l, \sigma_t; t_{st})) = \frac{1}{2}(0.2) + \frac{1}{2}(0.4) = 0.3$
 $E_G(\pi_G(r, \sigma_t; t_{st})) = \frac{1}{2}(0.4) + \frac{1}{2}(0.2) = 0.3$
 Then G has no incentive to deviate for any q.
 σ_t has no incentive to deviate if
 $\pi_{st}(\sigma_t, \sigma_t^*; t_{st} = SL) > \pi_{st}(\sigma_t', \sigma_t^*; t_{st} = SL)$
 $0.6 + 0.2q > 1 - 0.3q$
 $0.5q > 0.4$
 $q > 0.8$
 $\pi_{st}(\sigma_t, \sigma_t^*; t_{st} = SR) > \pi_{st}(\sigma_t', \sigma_t^*; t_{st} = SR)$
 $0.8 - 0.2q > 0.7 + 0.3q$
 $0.1 > 0.5q$
 $q < 0.2$
 so σ_t always has incentive to deviate, there are
 no hybrid BNE where σ_t plays pure strategy RL and
 G mixes.

c Suppose that some type L σ_t mixes at equilibrium.
 Then, by definition of NE, this SL has no profitable
 deviation. Then, the payoff to this SL from ~~SL~~
 L and the payoff from R are equal. This is possible
 only if G mixes l and r and assigns high
 probability to l. If G so mixes, then ~~an~~ SR a
 type R σ_t has ~~strictly~~ higher payoff from R than
 from L, and so always chooses R. Then G is
 very ~~badly~~ off enjoys low payoff against SR
 and fails to maximise his expected payoff, so it is
 not an equilibrium.

3. ~~Player~~

All strategy profiles $s^* = (x^*, y^*)$ where $x^* + y^* = 1$ are pure NE. $(1, 1)$ is also a pure NE. "degenerate" \rightarrow "both players do sth ridiculous"

$$u_1(x, y) = \begin{cases} x^\alpha & \text{if } x+y \leq z \\ 0 & \text{otherwise} \end{cases}$$

$$u_2(y, x) = \begin{cases} y^\alpha & \text{if } x+y \leq z \\ 0 & \text{otherwise} \end{cases}$$

$$E_1[u_1(x, y)] = \begin{cases} 0 & \text{if } x+y > 1 \\ (P(x+y \leq z)) x^\alpha & \text{otherwise} \end{cases}$$

$$= \begin{cases} 0 & \text{if } x+y > 1 \\ \frac{1-(x+y)^{1-\alpha}}{1-\alpha} & \text{otherwise} \end{cases}$$

By symmetry

$$E_2[u_2(y, x)] = \begin{cases} 0 & \text{if } x+y > 1 \\ \frac{1-(x+y)^{1-\alpha}}{1-\alpha} & \text{otherwise} \end{cases}$$

Suppose

Supposing that

Suppose given that $z \in [0, 1]$, $F(z) = (x+y)$ $F(z=1) = 1, \infty$

$F(z)$ the expected utility function simplifies to $\min \{ \dots, 0 \}$

$$E_1[u_1(x, y)] = [1 - (x+y)^\alpha] x^\alpha$$

By symmetry,

$$E_2[u_2(y, x)] = [1 - (x+y)^\alpha] y^\alpha$$

Argue that at eqm, $x+y \leq 1$ (rule out degenerate eqm)

c FOCs:

$$\frac{\partial}{\partial x} E_1[u_1(x, y)] = \frac{\partial}{\partial x} [1 - (x+y)^\alpha] x^\alpha = 0$$

$$\frac{\partial}{\partial y} E_2[u_2(y, x)] = \frac{\partial}{\partial y} [1 - (x+y)^\alpha] y^\alpha = 0$$

$$\alpha [1 - (x+y)^\alpha] \alpha x^{\alpha-1} - n(x+y)^{n-1} x^\alpha = 0$$

$$\alpha [1 - (x+y)^\alpha] = n(x+y)^{n-1} x^\alpha$$

$$\alpha [1 - (x+y)^\alpha] = n y (x+y)^{n-1}$$

$$2\alpha [1 - (x+y)^\alpha] = n(x+y)^\alpha$$

$$2\alpha = (2\alpha + n)(x+y)^\alpha$$

$$x+y = \left(\frac{2\alpha}{2\alpha+n} \right)^{1/\alpha}$$

~~$x=y=1$~~

$$x=y = \alpha [1 - (x+y)^\alpha] / n(x+y)^{n-1}$$

$$x=y = \frac{1}{2} \left(\frac{2\alpha}{2\alpha+n} \right)^{1/\alpha}$$

$$\text{Optimal demands are } x^* = y^* = \frac{1}{2} \left(\frac{2\alpha}{2\alpha+n} \right)^{1/\alpha}$$

d Suppose $z \sim u(0, 1)$ then $F(z) = z$ for $z \in [0, 1]$

Plug in $n=1$

$$E_1[u_1(x, y)] = [1 - (x+y)] x^\alpha$$

$$E_2[u_2(y, x)] = [1 - (x+y)] y^\alpha$$

FOCs:

$$\frac{\partial}{\partial x} E_1[u_1(x, y)] = 0$$

$$\frac{\partial}{\partial y} E_2[u_2(y, x)] = 0$$

$$[1 - x - y] \alpha x^{\alpha-1} - x^\alpha = 0$$

$$[1 - x - y] \alpha - x = 0$$

$$(\alpha+1)x = (1-y)\alpha$$

$$x = \frac{\alpha}{\alpha+1} (1-y)$$

By symmetry,

$$y = \frac{\alpha}{\alpha+1} (1-x)$$

$$x=y = (1-x-y)\alpha$$

$$x = \frac{\alpha}{\alpha+1} (1-x) \rightarrow \text{By substitution } y=x$$

$$x = \frac{\alpha}{\alpha+1} - \frac{\alpha x}{\alpha+1}$$

$$\frac{2\alpha+1}{\alpha+1} x = \frac{\alpha}{\alpha+1}$$

$$x=y = \frac{\alpha}{2\alpha+1}$$

As players become more risk averse, the marginal utility of money decreases more rapidly, & decreases. Each player's demand decreases.

Differentiate

$$e \ln x^* = \frac{1}{2} \ln \left(\frac{1}{2} \left(\frac{2\alpha}{2\alpha+n} \right)^n \right) \\ = \frac{1}{2} \ln \frac{1}{2} + \frac{1}{n} \ln 2\alpha - \frac{1}{n} \ln(2\alpha+n) \\ = \frac{1}{n} [\ln 2\alpha - \ln 2 - \ln(2\alpha+n)]$$

let $f(n) = [\ln 2\alpha - \ln 2 - \ln(2\alpha+n)]$ and $g(n) = n$

$$f'(n) = -\frac{1}{2\alpha+n}, g'(n) = 1$$

$$\lim_{n \rightarrow \infty}$$

$$\ln x^* = \ln \left(\frac{1}{2} \left(\frac{2\alpha}{2\alpha+n} \right)^n \right) \\ = \ln \frac{1}{2} + \frac{1}{n} \ln 2\alpha - \frac{1}{n} \ln(2\alpha+n)$$

let $f(n) = \ln 2\alpha - \ln(2\alpha+n)$ and $g(n) = n$

$$f'(n) = -\frac{1}{2\alpha+n}, g'(n) = 1$$

$$\lim_{n \rightarrow \infty} \frac{1}{n} \ln 2\alpha - \frac{1}{n} \ln(2\alpha+n)$$

$$= \lim_{n \rightarrow \infty} \frac{f'(n)}{g'(n)} \text{ by "Hopital's rule"}$$

$$= \lim_{n \rightarrow \infty} -\frac{1}{2\alpha+n}$$

$$= 0$$

$$\lim_{n \rightarrow \infty} \ln x^* = \lim_{n \rightarrow \infty} \ln \frac{1}{2} + \lim_{n \rightarrow \infty} \frac{1}{n} \ln 2\alpha - \frac{1}{n} \ln(2\alpha+n)$$

(by sum rule)
 $= \ln \frac{1}{2}$

$$\lim_{n \rightarrow \infty} x^* = e^{\lim_{n \rightarrow \infty} \ln x^*} = \frac{1}{2}$$

By symmetry, $\lim_{n \rightarrow \infty} y^* = \frac{1}{2}$.

As n increases, the probability distribution of z narrows, z converges in probability to 1. This can be interpreted as a "perturbation" in z becoming This can be interpreted as a perturbation of the original full information game becoming vanishingly small. This process identifies the risk dominant equilibrium in the original game in (a).

Are we expected to know Hopital's rule?

This perturbation seems unrealistic because there is no uncertainty and size of the prize

Shocks in global game are correlated
 Shocks in purification are independent and private

4a State space $\Omega = \{K, C, B\}$

State space $\Omega = \{Kcb, Ccb, Bcb, Kcv, Ccv, Bcv\}$

where in each K-state, the sauce is ketchup, in each C-state the sauce is chocolate, in each B-state the sauce is Bechamel, in each cb state Charlie is colourblind, and in each cv state Charlie has colour vision.

Only need 1 state

"only need 5" \rightarrow merge Bcb and Bcv

C's knowledge that C is cb is not relevant

b $P_i = (\{Kcb, Ccb\}, \{Bcb\}, \{Kcv\}, \{Ccv\}, \{Bcv\})$

$P_A = (\{Kcb, Ccb, Kcv, Ccv\}, \{Bcb, Bcv\})$

c ~~Bcb and Bcv~~ let the event that the cup contains Bechamel sauce be $B = \{Bcb, Bcv\}$. Player i knows

~~Bcb and Bcv~~ ~~Bcb~~ in state ω iff $P_i(\omega) \subseteq B$.

By inspection, C knows B in states Bcb and Bcv.

$K_C(B) = \{Bcb, Bcv\}$

d By inspection, A knows $K_A(B)$ in states Bcb and Bcv.

e By inspection, let choc be the event that the cup contains chocolate sauce.

By inspection, $K_C(\text{choc}) = \{Kcv\}$

f By inspection, $K_A(K_C(\text{choc})) = \emptyset$, A never knows that C knows that choc.

