\$\(\frac{3\xi\part(\xi-1)\xi\ri\xi\ri\xi\ri\xi\ri\xi\ri\xi\ri\xi\ri\xi\ri\xi\ri\xi\ri\xi\ri\xi\ri\xi\ri\xi\ri\xi\ri\xi\ri\xi\xi\ri\xi\xi\ri\xi\ri\xi\ri\xi\xi\ri\xi\ri\xi\ri\xi\ri\xi\ri\xi\ri\xi\ri\

The expected proportion of T players increases in each period for all Pc, Pt (Supposing Pt <1). This is because, for E>D, T strictly dominates C and for E>D, TT+>TC, SO \$ the population of T players grows faster than the population of C players. Supposing that E is sufficiently small, the charge in the population of D players has negligible effect on the total population, SO soft the charge in proportion of T players is determined entirely by the relative growth of the C and T populations.

But time normal indefinite, so cannot treat & as negligible.

The egin to the all T is egin not enterely stable because if T dominates, C does just as well and can take over by mutation, than D mutation will summe.

Deterministry meuhanics  H -1 0  D 2 1  D 2 1  D 2 1  D 2 1  D 2 1  D 2 1  D 2 1  D 2 1  D 2 1  D 2 1  D 2 1  D 2 1  D 2 1  D 2 1  D 2 1  D 3 1  D 4 10 10 10 10 10 10 10 10 10 10 10 10 10	
Be Best responses underlined. By inspection, the only	
Be Best responses under insect By inspection, the only	
Be Best responses underlined. By inspection, the only	
Be Best responses underlined. By inspection, the only	
Be Best responses underlined. By inspection, the only	
Be Best responses underlined. By inspection, the only pure ME are (H,D) and (D,H).	
Best responses underlined. By inspection, the only	
pure HE are (H,D) and (D,H).	
Suppose that there is a mixed ME o* = (0*, 0*)	
where of assigns probability p to H and probability	
1-p to D. Then, by definition of ME, A has no	
profitches deciction, then $\pi_1(H) = \pi_1(D)$ , $\frac{1}{2}$	
-9+2(1-9)=1-9, where 9 is the probability of assigns	
to H. 2-39=1-9, 1=29, 9=42. Then, by difficition of NE.	
(Q)-17-17-18-18-18-18-18-18-18-18-18-18-18-18-18-	
P2 ras in profitable devication, then T12(H)=T15(D),	
-p+2(1-p)=1-p, p=1/2. The only moved HE is (3*, 52*) where 5* = 15H+1/20 and 5=15H+1/20.	
angle of - 121/11/20 allo of 2	
B. Co and I a mine so the D. B.	
From the above argument, if or mixes, so does p2. By	
Symmetry, it to mixes, 30 does the so there are no	
hyprid NE.	
2-2-50	
By definition of ESS, the only count on is an ESS iff	
(J*, J*) is an NE . so the only conditate ESS is	
13H+13D. Denote this strategy of.  If mutants do no wouse glevi	inst condence Ese
200100000000000000000000000000000000000	1 11 am Solves than
T(4,0*)=T(0,0*)=1/2, so any pure or moved "Mutants do word equins	1 1001R1
Stra (potentially & degenerate) moved strategy of candidate \$25 does against	N OUN
= 2/H+ (1-12)D i= a bast response +0 0%.	
$\mu(a, a, b, c) = -b_{1,5} + 5b_{1}(1-b_{1}) + (1-b_{1})_{5} = -b_{1,5} + 5b_{1,5}$	
$=-p'^2+2p'-2p'^2+(-2p'+p'^2)$	
$=-2\phi^2+1$	
$\pi(\alpha_*'\alpha_i) = -\overline{\beta}b_i + (i-b_i) + \overline{\beta}(i-b_i)$	
= 3/2-26'	
$\pi(\sigma^*, \sigma') > \pi(\sigma', \sigma') \Leftrightarrow 36-2\phi^2 + 1$	
\$\frac{2p'^2-2p'+1/2}{2} > 0	
↔ 2(k'-1/2)2 >0	
⇔ 8'+ 1/2	
50 f 0' \$ 5 * (i.e. p' + 1/2) is a best response to	
σ* then π(σ*, σ') > π(σ', σ'). By definition of	
ESS, 0* 15 an ESS.	
b (et ∩H(t), nD(t), n(t), T(t), T(t), P(t)=PH(t), and PO(t)	
be defined in the conventional adjuster to denote the	
scale factor	
$\Omega_{H}(t+t) = \Omega_{H}(t) + \lambda \Omega_{H}(t) \pi_{H}(t) = \Omega_{H}(t) (1 + \lambda \pi_{H}(t))$	
$\Omega(t+t) = \Omega(t) + \lambda \Omega(t) \sum_{x \in \{H_1 \cap \mathcal{F}\}} P_x(t) \pi_x(t)$	
$= o(t)(1+\lambda(P_{H}(t)\pi_{H}(t)+P_{O}(t)\pi_{O}(t))$	
$= O(+)(1+\lambda(b(+)+b(+)+b(+)))$	of the pulse with the w
-11(1) 17 (10) 11(1) 2 (1) 2 (1) 2 (1) 2 (1)	
$\pi_{H}(t) = \frac{1}{p} + 2(1-p) = 2-3p - p(t) + 2(1-p(t)) = 2-3p(t)$	
$\pi_{\mathcal{D}}(t) : 1 - \mathcal{P}(t)$	
nH(++1) = nH(+)(1+ (2-3p(+))) can the replicator equations	too given without prom
	0.100
$= n(t)(1+(-2p(t)^2+1)x)$	

Replicator equation  $\dot{p} = p(1-p)\left(\pi_{H}(p) - \pi_{d}(p)\right)$   $= p(1-p)\left(3-3p-(1-p)\right)$   $= p(1-p)\left(1-2p\right)$   $\dot{p} = 0 \text{ iff } p = 0, p = 1, or p = 1/2$   $\dot{p} = 0 \text{ for } p = 0, p = 1, or p = 1/2$   $\dot{p} > 0 \text{ for } p \in (0, 1/2), \dot{p} < 0 \text{ for } p \in (1/2, 1)$ For all initial  $p \neq 0, 1$ , the process evolves to p = 1/2, (0, 0) = 1/2 (0, 0) = 1/2

Let the aperariph of  $\pi$  denote either Ran cet  $\pi x$  denote the expected payoff to from playing action x to a four player if Y=R and a column player if Y=C.

 $\frac{\pi_{H}^{2}(q)=2-3q}{p=p(1-p)(\pi_{H}^{2}(q)-\pi_{H}^{2}(q))=p(1-p)(\pi_{H}^{2}(q)-\pi_{H}^{2}(q))=p(1-p)(1-2q)}$   $\frac{\pi_{H}^{2}(q)=2-3q}{p=p(1-q)(\pi_{H}^{2}(q)-\pi_{H}^{2}(q))=p(1-q)(1-2q)}$ 

P evalues to & 1 and 9 evolves to 0 Then P > Po > 1/2 9, < 90 x 1/2 so p, > 0, 9, x 0 The & state evalues to (H,D)

 $P_0=Q_0$   $P_0=P_0(1-2P_0)$ ,  $Q_0=Q_0(1-2Q_0)=P_0(1-2P_0)$   $P_0=Q_0$ , then  $P_0=Q_0$ ,  $P_0=Q_0$ , and so on.  $P_0=Q_0$ , then  $P_0=Q_0$ ,  $P_0=Q_0$ , and  $P_0=Q_0$ .  $P_0=Q_0$ , then  $P_0=Q_0$ ,  $P_0=Q$ 

iii 9595%2,  $\dot{p}_0>0$ ,  $\dot{q}_0>0$ ,  $\dot{p}_0>\dot{q}_0$ Suppose 94%2, then  $\dot{p}_1>0$ ,  $\dot{q}_1=0$ Suppose 94%2 1000000 1000000 1000000 100000 1000000 1000000 100000 100000 100000 1000000

in the long run, each population prays are the strategy, and both populations play different that each offer plays I with certainty and the other plays I with certainty) the that each population plays is that to which it to prays with greater initial frequency than the other population. The ayminetic statation equilibrium is whitely in the long run a whitely because it is in some sense which to the population's and vulnerable to minor thy minor shock to the population's stategies such that ptq sense sees the results in the "divergent" evolution path.

Comment on this coinciding with result in (a) No mutation is modelled in the representation of the presence of mutations, endpoints are stable ESS => stability wholer represent synamic

can be represented graphically ? Fist

This corresponds to actual thank and actual box saws as opposed to thankish monkey and thankish points

if there is some group identifier that

8t 0 0 Hb

0 0 1 0

dest responses underlined. By inspection, the pure NE are (Br, Br), (C,C), and (Br, Br) where Hayers hay mutual best responses.

Stochastic evening

p Each bout HE is an absorbit consebonds to an closorping, i.e. if (at as) (denoting the strategy biogije muece ti bionie of ang to bionie or) is a pure NE, then the state six x= (xa= N, xa; =0, xa; =0), y= (ya= N, ya=0, ya;=0) is an absorbing state, i.e. remains unchanged in all subsequent periods. Where at Supprese that some such state is reached in period t. At the start of period ++1, some han players and some Earny biciders objects their strotteries to pret respond to the distribution of strategies in period to the Some Row players update their strategies to best respond to as and some Column players applicate their strategies to best respond to a. By definition of ME, a to a best response to as and as are mutual best respon LEADONZEZ " 20 the ribactive broiters, auctorises one unchanged. Then the state is unavayed. By induction, the state reinains unchanged in all subsequent periods.

Suppose that some strategy profile is not an ME, then the column's strategy or column is not playing a best response to Row's strategy.

Playing a best response to Row's strategy.

Suppose without loss of generality that the former is true. Suppose that in period t, the corresponding state is reached. With non-zero probability, at least one Row player apactes his strategy at the start of period the to best respond to Column. These Row player's strategies change since they were not previously playing a best response.

Then the state changes, so it is not an absorbing state.

At the exact of period tt, with non-zero

probability, and at team one player from the mixing population is streets updated his strately. Such players are indifferent between the pute actions that their population's corresponding strategy moves over. So with non-zero probability, and this player changes his strategy. Then the state changes, so it is not an absorbing state.

consequently a state is an absorbing state ist it corresponds to some pure NE.

c consider some arbitrary inition state—to period in period . At the start of period ++1, with non-zero probability, all and only players from one population update their strategies, and with nonzero pour pinty, an such players choose the same, strategy, which best responds to the other population's \* strategy distribution in period +. then, the apaciting population in period ++1, each wemper of the abacting population plays a common strategy. At the start of period pure strategy. At the start of period ++2, with non-zero probability, all and only players from from the non-updating population in the update their strategies, and each of these players anouses the unique best pure best response to the pure strategy chosen by each player from the other thi-upsating-population. So the state in t+2 is an absorbing state that corresponds to a pure ME, and remains unananged in all subsequent periods.

thank At any period t, there is a non-sero
productively that at period to and all subsequent
periods, the an absorbing state will have been
recared. Once reached, an absorbing state
remarks unanaged in all subsequent periods. Then,
as the number of periods increases, the probability of
being in an absorbing state approaches in the
process necessarily converges to an absorbing state.

Br 0 b

Best responses underlined. By inspection the only pure ME are (c,c) and (Br,Bt). By the argumen result given in (c,c) and (Br,Bt). By the argumen result absorbing states are the two which correspond to these pure ME, normally  $(x_1, x_2, x_3, x_4, x_5)$   $(x_2, x_4, x_5)$   $(x_3, x_4, x_5)$  and  $(x_4, x_5)$   $(x_4, x_5)$   $(x_5, x_6, x_5)$   $(x_5, x_6, x_5)$   $(x_5, x_6, x_6)$   $(x_6, x_6)$   $(x_6$ 

C is risky, Br and B+ are safe

Suppose that best reply dynamics are deterministic, then if  $\frac{p^2 + 6a}{p^2 + 6a}$  and  $\frac{p^2 + 6a}{p^2 + 6a}$  of other cition of  $(p^2 + 1, p^2 + 1)$  includes  $\frac{p^2 + 6a}{p^2 + 6a}$  by  $\frac{p^2 + 6a}{p^2 + 6a}$  by an analogous argument, the bosin of other cition of  $(p^2 + 0, p^2 + 0)$  includes  $\frac{p^2 + 6a}{p^2 + 6a}$ ,  $\frac{p^2 + 6a}{p^2 + 6a}$ .

For simplicity, we thegree to consider the consider best response dynamics where  $p^R$  to and  $p^C < p^R$ , or where  $p^R$  to and  $p^C < p^R$ .

The pathintum volume of uncorrected errors required to leave the boosts of  $(p^2=1, p^2=1)$  and enter the boosts of  $(p^2=0, p^2=0)$  is M(1-a)+M(1-b). The pathintum number of uncorrected errors required to leave  $(p^2=0, p^2=0)$  and enter the boost of  $(p^2=1, p^2=1)$  is Ma+Mo. The tatter is  $(p^2=0, p^2=0)$  is more likely in the long run than  $(p^2=1, p^2=1)$  if  $M(2-a-b) < M(a+b) \Leftrightarrow a+b>1$ 

pso prob go left is a function of

prob go left is a function of

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Pareto inferior more likely

citien sufficiently small & all that matters is the number of mistakes

the evol ont come heurs towards but

