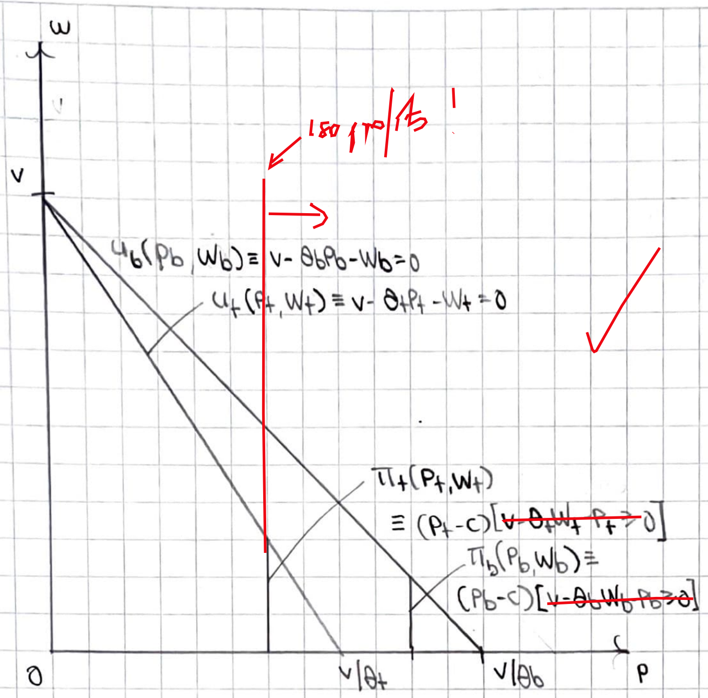


The firm's optimisation problem is

$\max_{P_b, W_b, P_t, W_t} (1-\lambda)(P_b - c) + \lambda(P_t - c)$ subject to

$PC_b: v - \theta_b P_b - W_b \geq 0$

$PC_t: v - \theta_t P_t - W_t \geq 0$

$IC_b: v - \theta_b P_b - W_b \geq v - \theta_b P_t - W_t$

$IC_t: v - \theta_t P_t - W_t \geq v - \theta_t P_b - W_b$

$P_b^+: P_b \geq 0$, $P_t^+: P_t \geq 0$, $W_b^+: W_b \geq 0$, $W_t^+: W_t \geq 0$

supposing without loss of generality that consumers have reservation utility 0

b ~~Four~~

$v - \theta_b P_b - W_b \geq_1 v - \theta_b P_t - W_t \geq_2 v - \theta_t P_t - W_t \geq_3 0$

$\geq_1$ follows from IC_b, $\geq_2$ from $\theta_b < \theta_t$ (supposing $P_t \neq 0$)

$\geq_3$ from PC_t

$\Rightarrow v - \theta_b P_b - W_b > v - \theta_t P_t - W_t$, i.e. PC_b does not bind.

Suppose for reductio that at the optimum $\hat{P}_b, \hat{W}_b, \hat{P}_t, \hat{W}_t$, PC_t does not bind, i.e. $v - \theta_t \hat{P}_t - \hat{W}_t > 0$. Then, for sufficiently small ε (such that PC_b and PC_t continues to hold) $P_b' = \hat{P}_b + \varepsilon$, $P_t' = \hat{P}_t + \varepsilon$ is such that all constraints hold and $\pi' > \hat{\pi}$. So $\hat{P}_b, \hat{W}_b, \hat{P}_t, \hat{W}_t$ is not an optimum. By reductio, PC_t binds at the optimum, and tourists are indifferent between travelling and not travelling.

c Suppose for reductio that at the optimum, IC_b does not bind, i.e. $v - \theta_b \hat{P}_b - \hat{W}_b > v - \theta_b \hat{P}_t - \hat{W}_t$. Then, for sufficiently small ε (such that PC_b and IC_b continue to hold), $P_b' = \hat{P}_b + \varepsilon$ is such that all constraints hold and $\pi' > \hat{\pi}$. ~~So the candidate~~ By reductio, IC_b binds at the optimum, and business men are indifferent between buying at W_b and at W_t.

~~Suppose for reductio that $\hat{W}_b \neq 0$.~~ IC_b binds, i.e.

$v - \theta_b \hat{P}_b - \hat{W}_b = v - \theta_b \hat{P}_t - \hat{W}_t \Leftrightarrow \theta_b \hat{P}_b + \hat{W}_b = \theta_b \hat{P}_t + \hat{W}_t \Leftrightarrow$

$\theta_b(\hat{P}_b - \hat{P}_t) = \hat{W}_t - \hat{W}_b \Rightarrow \theta_t(\hat{P}_b - \hat{P}_t) > \hat{W}_t - \hat{W}_b \Rightarrow$

$v - \theta_t \hat{P}_b - \hat{W}_b < v - \theta_t \hat{P}_t - \hat{W}_t$, i.e. IC_t does not bind.

Date

Suppose for reductio that $\hat{w}_b \neq 0$. Then for sufficiently small ε (such that IC_t continues to hold), $w_b' = \hat{w}_b - \varepsilon$, $p_b' = \hat{p}_b + \varepsilon/\theta_b$ is such that ~~v-θbwb~~ $v - \theta_b \hat{p}_b - w_b = v - \theta_b p_b' - w_b'$, so it is trivial that PC_b, PC_t, and IC_b continue to hold (and IC_t holds by construction of ε), and $\pi' > \hat{\pi}$. By reductio, $\hat{w}_b = 0$.

You could do it along the IC_b constraint!

Businessmen buy at $\hat{w}_b = 0$ and are indifferent ~~to~~ between buying at this time and buying when tourists do at $\hat{w}_t$.

d

d Given that PC_t binds, $v-\theta_t\hat{p}_t-\hat{w}_t=0$, $(\hat{p}_t,\hat{w}_t)$ lies on the indifference curve $u_t(p_t,w_t)=0$. Given that IC_b binds, $v-\theta_b\hat{p}_b-\hat{w}_b = v-\theta_b\hat{p}_t-\hat{w}_t$, $(\hat{p}_b,\hat{w}_b)$ lies on the indifference $u_b(p_b,w_b)=u_b(\hat{p}_t,\hat{w}_t)$, i.e. the indifference curve that crosses $(\hat{p}_t,\hat{w}_t)$. Given that $\hat{w}_b=0$, $(\hat{p}_b,\hat{w}_b)$ lies on the intersection of that indifference curve with the p axis.

How could we know this is the right method rather than Lagrangian?

The Lagrangian works but it is more tedious, we are assuming necessary and sufficient conditions so finding a solution is all we need. These arguments help to find the solution quicker.

$\hat{w}_t = v-\theta_t\hat{p}_t$

$v-\theta_b\hat{p}_b-\hat{w}_b = v-\theta_b\hat{p}_t-\hat{w}_t \Rightarrow \theta_b\hat{p}_b-\hat{w}_b=\theta_b\hat{p}_t+\hat{w}_t$

$\Rightarrow \theta_b\hat{p}_b = \theta_b\hat{p}_t + v-\theta_t\hat{p}_t \Rightarrow \hat{p}_b = \hat{p}_t + v/\theta_b - \theta_t/\theta_b\,\hat{p}_t$

$\hat{\pi} = (1-\lambda)\hat{\pi}_b + \lambda\hat{\pi}_t$

$= (1-\lambda)(\hat{p}_t + v/\theta_b - \theta_t/\theta_b\,\hat{p}_t - c) + \lambda(\hat{p}_t - c)$

~~At the optimum, the following FOC holds~~

$d\hat{\pi}/d\hat{p}_t = (1-\lambda)(1-\theta_t/\theta_b)+\lambda \gtreqless 0 \Rightarrow$

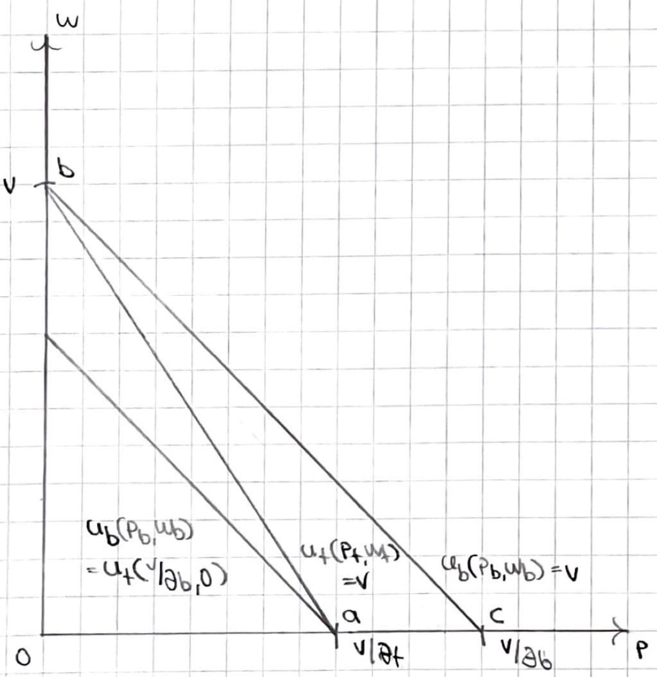
$1-(1-\lambda)(\theta_t/\theta_b) = 0 \Rightarrow$

$1-\lambda = \theta_b/\theta_t \Rightarrow \lambda = 1-\theta_b/\theta_t$

it is a linear function! it might not be equal to 0!

Suppose $\lambda > 1-\theta_b/\theta_t$, then $d\hat{\pi}/d\hat{p}_t>0$, the firm maximises profit by choosing the maximum feasible (i.e. subject to the above constraints) $\hat{p}_t$, namely v/θ_t. Then $\hat{w}_t=0$, $\hat{p}_b=\hat{p}_t=v/\theta_t$, $\hat{w}_b=0$. This is the pooling equilibrium. $\hat{\pi}=(v/\theta_t - c)$ Very good

Suppose $\lambda<1-\theta_b/\theta_t$, then $d\hat{\pi}/d\hat{p}_t>0$, the firm maximises profit by choosing the minimum feasible $\hat{p}_t$, namely 0. Then $\hat{w}_t = v$, $\hat{p}_b = v/\theta_b$, $\hat{w}_b=0$. This is the separating equilibrium. Suppose that indifferent tourists do not buy. $\hat{\pi} = (1-\lambda)(v/\theta_b - c)$



The pooling eqm is a, the separating eqm is points b and c. Very good

e If $c > v/\theta_b$, then $c>v/\theta_t$, $\hat{\pi}<0$ in either eqm, the firm should choose ~~p_b,p_t~~ high p_b, p_t, w_b, w_t such that no consumers buy.

Data

If $v/\theta_t < c < v/\theta_b$, then only the ~~po~~ separating eqm is profitable, the firm should choose $p_b = v/\theta_b$, $w_b = 0$ and high p_t, w_t such that no tourists buy. ✓ maybe just p_b, w_b.

If $c < v/\theta_t < v/\theta_b$ the airline does not serve tourists iff

$(1-\lambda)(v/\theta_b - c) > (v/\theta_t - c) \Leftrightarrow$ ← explain!

$\Leftrightarrow (1-\lambda)v/\theta_b - v/\theta_t > -c + (1-\lambda)c \Leftrightarrow$

$(1-\lambda)v/\theta_b - v/\theta_t > -\lambda c \Leftrightarrow$

$c > \cancel{\tfrac{1-\lambda}{\lambda}}\ \frac{\lambda-1}{\lambda} \, v/\theta_b + \frac{v}{\lambda \theta_t} \Leftrightarrow$

$c > \frac{\lambda-1}{\lambda} \, v/\theta_b + \frac{1}{\lambda} \, v/\theta_t$

Marginal cost exceeds ~~the~~ some weighted average of the maximum price each type is willing and able to pay

Very good work.