GE YOOIEW SET 3 la educ; = 10.36 - 0.0945ibs;+0.131 meduc; + 0.210 feduc; + 4; 0=722 we might expect that the more sidings or person has, the 1855 a person with more sibilings and receive four sport fourer years in education for several reasons. Families with more unidozen are cerens - 1885 p able to invest financial and other resource in the education of each child, cetens parious. This is because the a finite pool of resources must be shared among a langer number of children. Additionary, families with many anildren may require the older children to unter the warforce early to support the family Pirancially. Furner, families with many children are disproportionately low income, and hence 1885 alone to invest in their children's education. The coefficient on silvs is expected to be negerice. 5.60 has to increase by 10.044 = ,0.6 nothern for reduce predicted years of education by one year. The magnitude of the coefficient is relatively small. Acceptable to use "educ", "Meduc" etc? 6 on average, an increase in medic by 1 or better to give what they mean in your increases is associated with a 0.131 year increase in educ, holding silos. Enlish; and feduc constant. The coefficient of medic in the given regression gives a reliable estimate of for how a mother's educational attainment (couscily) influences that of her son only if the other causal determinants of the latter are not systematically related to the former. This is unitely. The 3003 educational attainment is likely to be affected by the country regim lary he grows up in, and the quality of educations the education system there likewise for the mother. The country (region) city that mother and son grow up in are likely to

pe lercheq:

The sone rever of educational attainment is also likely to be the affected by the rever of house hold wealth. Chewas for the mother. If the mather grows up in a wealthy howsehold, the same is likely to be the for the son.

- < E(8000,) = 10.36 0.094(0) + 0.131(12)+0.210(13)
 = 14.452
 - E(educ B)= 10.36-0.094(0)+0.131(16)+0.210(16)
 = 15.816

E(educ_8-educ_4) = 15.816-14.452 = 1.364 &

The predicted difference of years of education between B and A is 1.369 years.

d Houseword in come, querity of education sque squerity of houseword system), houseword querity of houseword system), houseword uscutty, might effect educ and are an likely to be corrected with sion, needed, and feduc.

bozitions being to comment a higher band. So yield to be compared order

on average, an increase in arge a one year increase in age is associated with a \$0.51 increase in the house wage rate.

The coefficient of ope consistently estimates a cousal effect only if the other cousal overeminants of uspe, coptured in it; are not systematically related to ope. This is animology.

wage is likely to be affected by the time at which a worker enter the labour force. Workers who enter the labour force during a boom are likely to have higher wafes than workers who enter the labour force during a slump, even later on in their careers. A workers ofe is likely to be related to the time at which he enter the workforce.

5 the coefficient on female is negletive and relatively large. In the sam

On overego, a female worker: hours vage

is \$3.81 less than a mare corter's havily uage.

c The estimated coefficient on degree gives a consider reliable estimate of the causal effect of having a university degree on earnings only if the other determinants of earnings, captured in it; the are not systematically related to degree. This is unlikely.

A worker's earnings are likely to be affected by the coapitate ability, conscientousness, country (region (city (and hence economic opportunity). These factors are likely to be related to whether or hat a worker has a university degree.

To obtain a better estimate of this causal effect, data should be callected on these other factors, and a a multivaritie regression model should be fit on the expanded dataset

The coefficient of degree in the resulting model gives the relationship between house using a cond the part of degree that is unconsected with female, age, agenitive ability, conscients where are no other confounding factors, this coefficient reliably estimates the course effect of degree on using.

₹ No.

Given that total hours recorded over the four activities must add up to 168 hours, thre four represents are perfectly multicalinear. Study is perfectly predicted by sleep, whit, and leisure. The component of study not predicted by sleep, work, and visure is a constant o, that has a covariance with score and a variance. B, is untefined as there is no unique solution to the acs minimisation prodem.

a NO.

is not possible to vory assept without varying at least one of sleep, work, and leasure.

c Score : Po + R, study + B25188P+B2 work + u

Sports all 163 hours a uset 10 lossure.

increase in study & (steep, or work) by one hour and a corresponding decrease in letture is a stacked with a B. (Bz or Bz) HERRE change in score.

since study, work, cort seep, and work are not perfectly multicolline out, there is a unique solution to the OS minimisation problem.

4 (Q4 C=E(Y-bo-b,X,-b2X2)2 3C(3bo=2E(Y-bo-b,X,-b2X2\(-1)) =-2E(Y-bo-b,X,-b2X2\(X,1)) =-2E(Y-bo-b,X,-b2X2\(X,1)) =-2E(Y-bo-b,X,-b2X2\(X,2))

FOG: E(Y & BX BX) =0 Po- E(Y) BE(X) BE(X) E(Y- 65 - 6, X, - 6, X) - 0 E(5, 5) 6, E(Y) -

(= B₀ + B₁X₁ + B₂X₂ + U

Since E(U) = 0,

E(Y - B₀ + A₁E(X₁) + B₂E(X₂).

E(Y - B₀ - B₁X₁ - B₂X₂) = 0

- ΣΕ(Y - B₀ - B₁X₁ - B₂X₂) = 0

∂((∂b₀ = 0))

 $COC(Y,X_1) = E(Y-A_0-B_1X_1-B_2X_2 = U$ $COU(U,X_1) = E(X_1M) - E(X_1)E(U)$ SinQle E(U) = 0, $COU(U,X_1) = E(X_1U) = E = 0$ $= E(Y-B_0-B_1X_1-B_2X_2X_1)$

- 2E(Y-Bo yB,X,-B,X2)(X,)=0

By 34mmetry, - DE(Y-Bo-B,X,-R1×2(X1)=0

(Bo, B, Bz) school, Foce: Oclope=Oclop.

- Oclope=o hence some the population.

linear regression problem.

```
50 E (UIX, X2) = 0
  0-(0)==((3K, ,Xx)=)=0
  Eq 11E
   BY CIE
   E(u)= E(E(u|X, X2)) = E(0) = 0
   CO_{(X_{i},U)} = E(X_{i}U) - E(X_{i}) = E(U)
                        (Since E(U)=0)
              = E(X,U)
   DIE
              = E(E(X,a(X,))
              >E(E(X,(X,)E(U(X,))
              = E(0)
              = 0
   By symmetry, con (x2, u)=0
b NO.
   Let the population linear regression of 7 on
   X, alone be Y= 8' + 3', \( x, + u)
   Bo', B' = argmin & bo b' E(4- bo-b'x1)2
   Bo, B. , B2 = argmin bo b, b2 E(4-b0-b,x,-b2x2)2
   CA the population linear regression of X, on
   X2 60 X, = TO+ T(X2+ X,
   文= メ、- ガローガノメ2
  B: - co
            it can be shown that
   B' = con(x,x,) hor(x,)
   B, = ca (4, x,) /vax (2,)
      = (con(Y,X,)-T,2con(Y,X2)/
        ( var(x1) - 12 var (x2) - 21, cov(x, x2)
   H 5 not necessarily the case that B = Bi
   B. captures only the relationship between the The doesn't feel quite precise enough
   component of X, unconsected with Xz and Y,
   while B' captures the entire relationship
   between x, and x,
& E(X:0:1X:) = E(X:1X:) E(0:1X:) (Since give, X; X; X; S
               -con fixed)
              = 0 (since E(uilxi)=0)
   E[ [ X , x , x , x , x , x , x ]
   = \sum_{i=1}^{n} E(X_i u_i (X_i, ..., X_n))
   2 E1/ 0
   = Ziz, x; E(u; |x, ..., xn) (since given x; x; is found)
 D E [ξη (χ;-Χ)(ν;-ν) | χ,... χη]
  = Z? (X; -X)E(U; -ù |X, ..., Xn)
  = E? (X;-X)(E(U; |X, ... Xn)-U)
   = £i²'-(X:-X)¤
```

```
· - ~ (\(\int_{i=1}^n \times_i - n\overline{\chi}\)
c ca (又山)=天) (大山)-
           = 1/2 E's xin! - (1/2 1/2/1/2/2/1/2)
                                                 RTP $ = (cà(x,1)-cà(x,u))/vàr(x)
 Cý (x,4)= NE50 xxx - (NExx) X (NE16,41)
 COCXY)= CON (X, Bo+ BX+U)
           = - Buck + Car(X,a)
       - cor(x,a) hour(x)
  rac(x) = ((μ)Σίς, χίζ - ((μΣί)ς, χί)2
 Car (x/4)/var (x)
 = [1/15;2/x, (1/15;2/x; X/1/5;2, (4;)]/
   [ 1/1 5/2/ X2 - (1/15/8/8/3/1)2]
 cg(x,4)-cg(x'm) - (水をじ(x:-n:))
 = ME ?(x:(x:-ui) - X(7-a)
 = 1/2 x; (60 +B,Xi) - X (B0+B,X)
  = KENBUR - BX
  = B((1/25, X; - X=)
  = # B, var (X)
  CONCAY HOUR
  £; = cà (x, y) hà (x) = B, + cà (x, u) hà (x)
d =($;) = =($;) + =(cà(x,u)/vàr(x))
       - Bit.
       = B, + E[ E(Z): (x-x)(u,-u) |x,...,xn) hat (x)] > 15 this step lepitimate?
       [(x) w/0]3 + 13=
        =B.
てきこの(メソ)が(メ)
  (*X) 2 = 1 (*x / *X) ( 2 = * &
     = cot (6x, coffee) (voir (6x)
      = aboà (x,4)/bevar(x)
      (メかいと)からくる)=
      = (C/6) A,
  Bo= F- B.X
  25 = FX - BX
      = a7+c - (G/6) B, (bx)
       2+ KA2- 72 =
      = a Botc
6 St = [ n-K-1 En (7: - Bo - BR; ) ] ]12
  50x = [n-k-1 E1=( (x, *- B* - B* x; )] 1/2
     = [n-k-1 Ein (ali+c-(000+c)-(96)B, (0x)) ]1/2
     = [ n-K-1 E= (a/1 - a/6 - a/2) 2 ]1/8
      = al[n-K+ Eizi (Y; - Bo- B)X; 8 ]1/2
      = asa
```

SER increases from the Exist's sample to the Exist, xist 3 sample by a factor a equivalent to the saciling factor of T. Transaction of T by c and

scaling of x by factor to have no effect on the error 10 - 25 - 25,2x since the pomper is excurry offser by an increase from 20 to 25 and the latter is excitty offset by a station of dece change from B. to B. 6 Total sum of squares TES = 20, (4:-4)2 128x= ZU (X'x - Lx)s = 512, (axite-67 + c)) = 5,5, (0x; -0x)s = 02 Engl(4:-4)2 = Q2 TES Jum of squared residuals 55R = ((N-K-1/52))2 35R* = ((n-K-1)(5{x))2 = ((1-k-1)(ast)) = azzse R3 = 1- 228/182 R2 * = (- 55 Px /755 * = 1- 02 558 / 02755 =1- 552/755 = RZ Since R2 is a relative measure of the variability of Y (4) around & (74), it is not affected by any of the trease thear tranto the scaling & 4 to 44 8 4-80+BX1; +BX21+41 YI = 30 + \$, XI; + \$> XZ; + Q; X 11= TTO + TT, X21 = X17 X1= 10 + 17, X2, + X1 ×ή- Χ; πο π, Χε, 100 mg (3K, X2) (car (x2) 一元。一天一元又一 TO - X1- Th X2 - X1 - B2 X21 - ILI - CO + B1 TO + B2 X21 + B1 X11 + B2 X21 + CU - Yo + B. X .: + B. X .: + Q. X .: + - B.CO. (X1, X1) by while bilinearity of con, since to is a constant -constant,

Yi = Bo+B, X1; + B2X2; + U; Yi = Bo + B, Xi; + B2 Xzi + Q; 11X + 15X 21 + 07 = 11X
11X + 15X 21 + 07 = 11X where 13 = 00 (X1, X2) (X2) $e^{\vec{X}_z}\hat{\pi} - \vec{X} = o\hat{\pi}$ 15×27 - 07 - 11× = 11× = X1 - (X1 - 1/2) - 1/2 = = (X11-X1) - T(x(X21-X2) Yi = る。+ る、(前o+元xi+元), きxzi+近; = (\$0+#B, #0) + B, \$1, + (B2+B, #2) x2; +U; = Vo+ \$, Xi + Y2 X2: + 1; で、ダインか = cà (76+8,×1+72×2+0,×1) = = = ((Y0+ B, X11+ Y2X21+Q1XX11)) - EP. (7,+B, X1+ 15, X2; +0;) E12, X1; = E ? (Yo Xi + B(Xi) + Y2X2, Xi + G; Xi) = 100+012 xz+ NO + B, E/E, X1, 1 = X1 JOSE X1 + 3, 212 (X1) + 12 X2 212 (8 X1) ER. (70 X1 $= \mathcal{E}_{2}^{n} \left(\gamma_{0} \ddot{X}_{11}^{n} + \beta_{1} (\ddot{X}_{11}^{n})^{2} + \gamma_{2} \chi_{21} \ddot{X}_{11}^{n} + \mathring{U}_{1} \ddot{X}_{11}^{n} \right)$ $= \gamma_{0} \mathcal{E}_{12}^{n} \ddot{X}_{11}^{n} + \beta_{1} \mathcal{E}_{22}^{n} (\ddot{X}_{11}^{n})^{2} + \gamma_{2} \mathcal{E}_{12}^{n} \chi_{21} \ddot{X}_{11}^{n} + \mathcal{E}_{12}^{n} (\mathring{U}_{1} \ddot{X}_{11}^{n})$ (公文)公公,底: 為:= 命(Y,文1) 命(文1)