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# **Theory and Background**

## **Part I**



# **1 Core Aspects of Tonal Compositions**

**1.1 Structured Tonal Motion**

**1.2 Polyphony**

**1.3 Musical Time**

**1.4 Form and Repetition**





## **2 Meta-languages for Abstraction and Structure**

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### **5.3 Stationary and Transitory Processes**

### **5.4 Temporal Abstractions**

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### **5.6 Comparison with Existing Theories**



# **6 Timely Processes**

## **6.1 Challenges in Combining Tonal Structure and Metrical Structure**

**Irregular proportions of the deeper levels**

**Passing Note in a Triple Meter**

**Accented Passing Notes**

**Suspensions**

**Interruptions**

## **6.2 Schenkerian Approaches to Rhythm**

**6.2.1 Rhythmic Equilibrium**

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### **6.7.4 Cross-Domain Analogies of Repetition Structure**



# **Computational Experiments** **Part IV**



## 6.8 Encoding and Generating Instances of Galant Schemata

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## **6.9 Sampling Metered Polyphony with Repetition Constraint**

## **6.10 Compression by Exploiting Structural Repetition**

