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- 1.2 Polyphony
- 1.3 Musical Time
- 1.4 Repetition

2 Meta-languages for Abstraction and Structure

- 2.1 Description, Instantiation, and Interpretation
- 2.2 Grammar and Syntax
- 2.2.1 Grammar of Natural Languages
- 2.2.2 Grammar-Based Music Theories
- 2.3 Formal Logic and Type Theory
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- 3.2 Motivations For Using Type Theory
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- 4.1.1 A Plan for Modular Theories that Work Together
- **4.1.2** Relating General Principles to Style Specific Constraints
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A Process Algebra For Metered Part II Polyphony

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- **6.5.1** Without Syntactical Constraints
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- 6.6 A Formal Model of Structural Repetition
- 6.6.1 Typed Holes and Arrows: A Functional Interpretation of Templates
- **6.6.2** Repetition structure as Higher-Order Templates
- **6.6.3** Repetition-Syntax-Material Decomposition
- **6.6.4** Cross-Domain Analogies of Repetition Structure

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6.7 Encoding and Generating Instances of Galant Schemata

6.8 Sampling Metered Polyphony with Repetition Constraint

6.9 Compression by Exploiting Structural Repetition