$\begin{array}{c} \text{COMPLEX NETWORKS - SPRING 2024} \\ \text{HOMEWORK 3} \end{array}$

INSTRUCTOR: JIA LIU SOLUTION BY: RENAN MONTEIRO BARBOSA

- DUE on 03/23/2025 11:59pm C.T.
- You can write on the separate work sheet or type your quiz. (Word or Latex or similar)
- If you use the handwriting, Solutions must be neat, clear and legible.
- If you need to scan you quiz, save it as a PDF file. Do not use jpeg, png, jpg etc. Do not submit more than one file.
- Please check your scanned file before submission. Make sure it is readable, correct order, properly oriented. Make sure it does include all pages.
- Please name your file as follows: LastnameInitials-MAP5990quiz1.pdf. If your name is Alan David Roberts, file name is RobertsAD-MAP5990quiz1.pdf.
- Try to keep the file size less than 4MB.
- You can resubmit the quiz if you want. Please specify which one is the one to be graded. Otherwise I will grade the most recent version.
- DO NOT EMAIL me the quiz. All quizzes are submitted via Canvas.

Date: 03/23/2025.

(1) Consider the adjacency matrix A of a directed network of size N=4 given by

$$A = \left[\begin{array}{cccc} 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{array} \right]$$

In the following we will indicate with **1** the column vector with elements $i_i = 1$ for $i = 1, 2, \dots, N$ and we will indicate with **I**the identity matrix.

- (a) Draw the network
- (b) Calculate the eigenvector centrality using its definition.
- (c) Calculate the Kate centrality.
- (d) Calculate the PageRank centrality.

Answers:

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- (a) Draw the network.
- (b) Calculate the eigenvector centrality using its definition.
- (c) Calculate the Kate centrality.
- (d) Calculate the PageRank centrality.

(2) Consider the adjacency matrix A of a directed network of size N=4 given by

$$A = \left[\begin{array}{cccc} 0 & 1 & 1 & 0 \\ 1 & 0 & 0 & 1 \\ 1 & 0 & 0 & 1 \\ 0 & 1 & 1 & 0 \end{array} \right]$$

In the following we will indicate with **1** the column vector with elements $i_i = 1$ for $i = 1, 2, \dots, N$ and we will indicate with **I**the identity matrix.

- (a) Draw the network
- (b) Calculate the degree centrality.

- (a) Draw the network
- (b) Calculate the degree centrality.



(4) Study the real-world complex networks on Neuman's website http://www-personal.umich.edu/mejn/netdata/, choose five real-world networks listed in the table and fill the table:

Network	directed or not	node#	edge#	community#
Karate				
Dolphin				
Les Miserable				
American College Football				
Power Grid				

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- (5) Choose one network from the previous question:
 - (a) Use Gephi to plot the network. Make sure to use centrality and communities so that you can show the properties of the network.
 - (b) Use Gephi to find the largest two nodes with the betweenness centrality, degree centrality, and pagerank centrality. Use the table to report your data.

- (a) Use Gephi to plot the network.
- (b) Use Gephi to find the largest two nodes