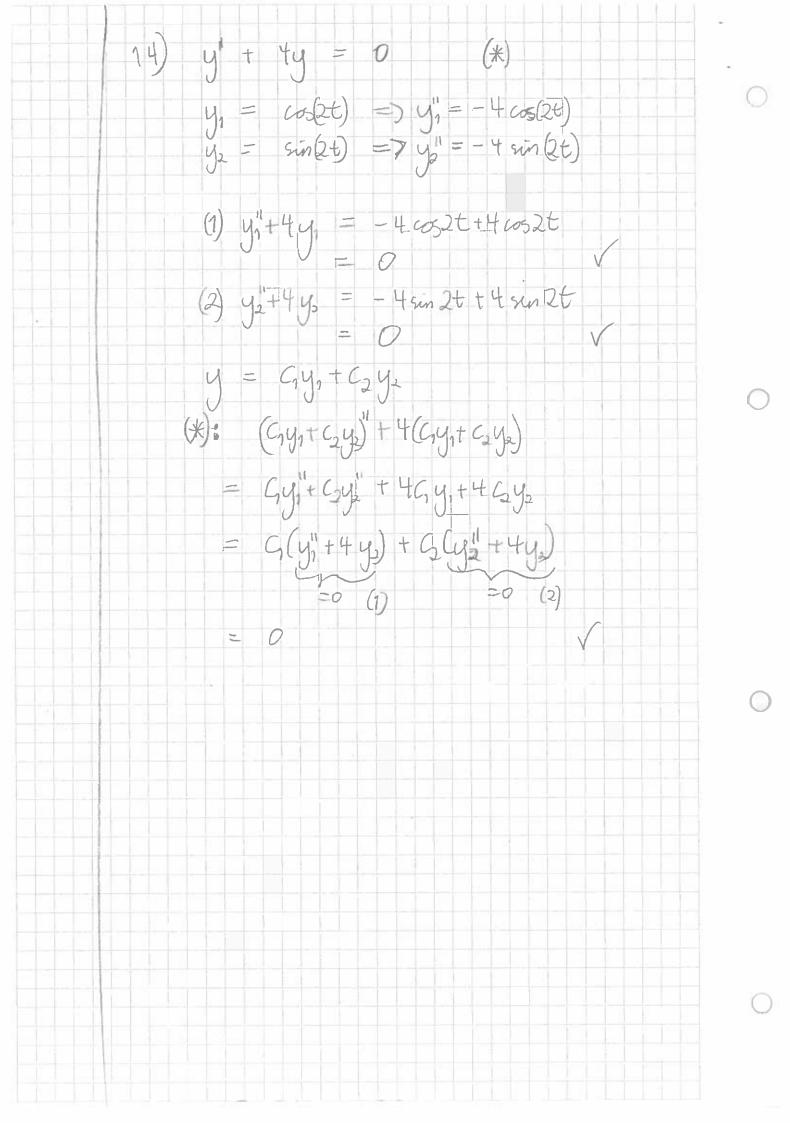
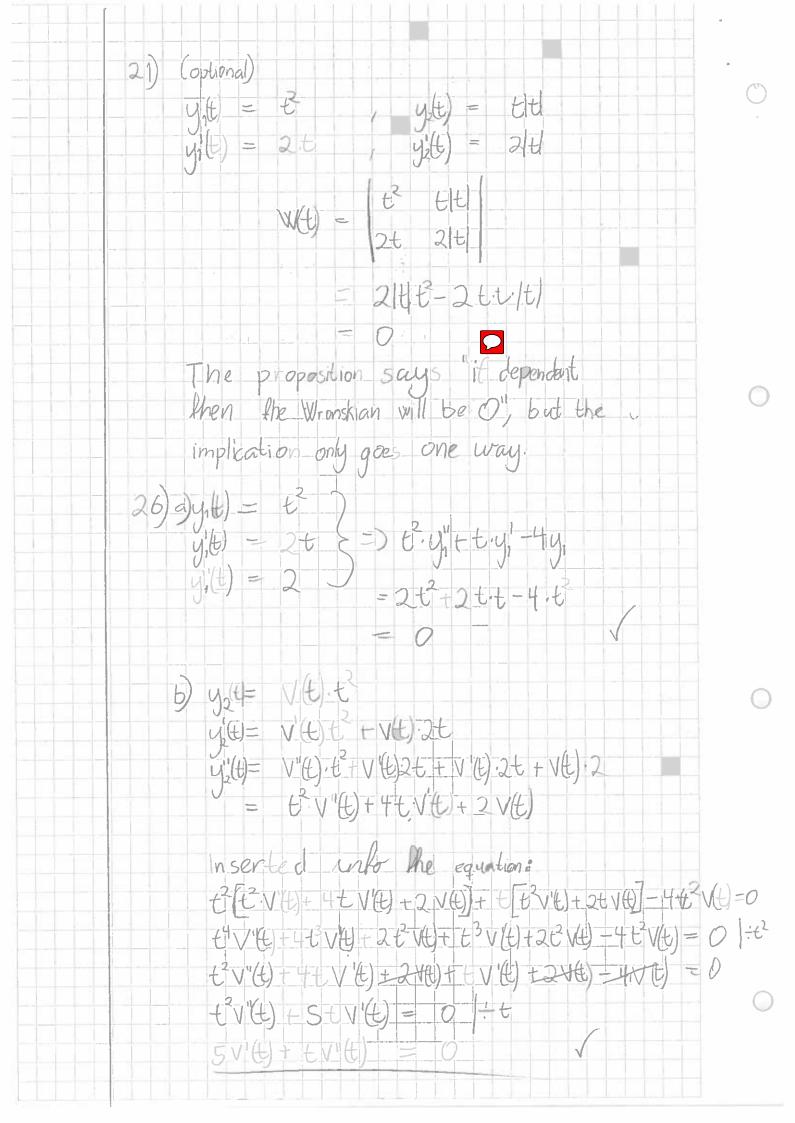
Wing 3 Rendell Cale linear and homogeneous: 8 linear (and inhogeneous): 1,2,4,6 nonlinear: 3,5,7 (13) $y''_1 - y'_1 - 6y = 0$ $(e^{3t})' - (e^{3t})' - 6e^{3t} = 0$ 9et-3et-62t= 0 y2-y2-6y2=0 $(e^{2t})'' - (e^{-2t})' - 6e^{2t} = 0$ 4e2+2e2-602=0 $(C_1y_1+C_2y_2)'-(C_1y_1+C_2y_2)'-G(C_1y_1+C_2y_2)=0$ (=) Cy + Czy - Cy - Cy - 6Cy - 6Czy = 0 $(=) C_1(y_1'-y_1'-6y_1) + C_2(y_2'-y_2'-6y_2) = 0$ as shown in (1) as shown in (2) G. O+C2. O

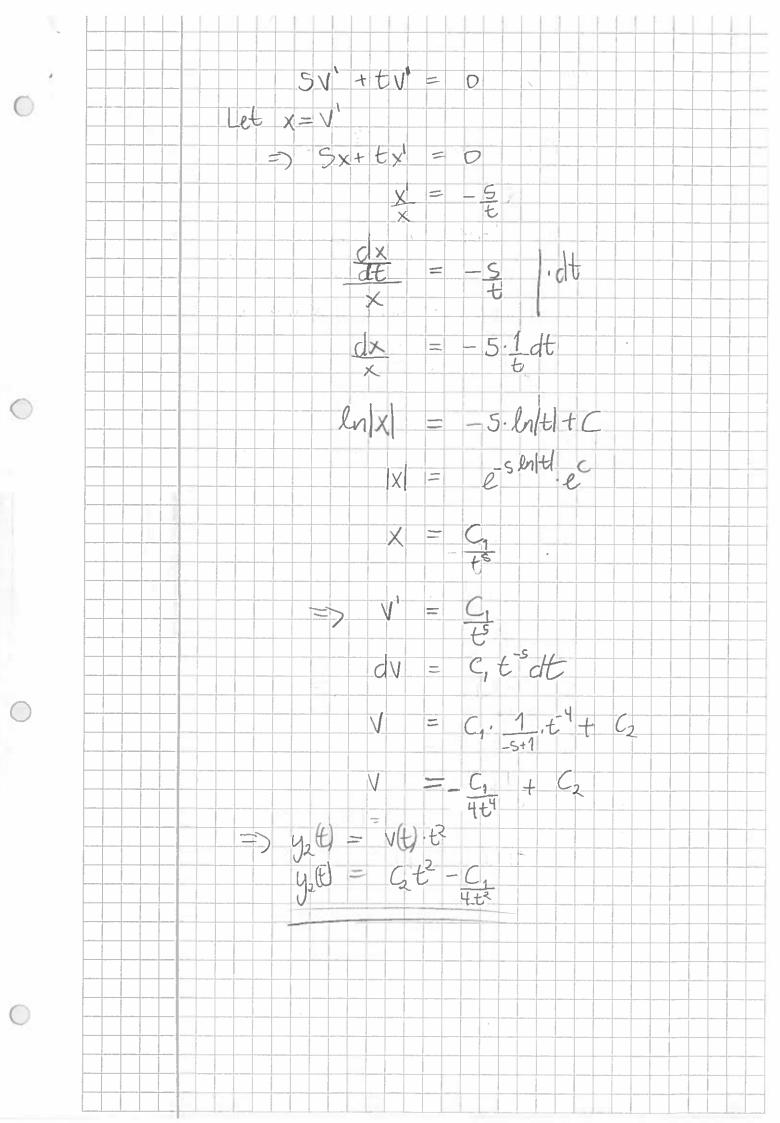


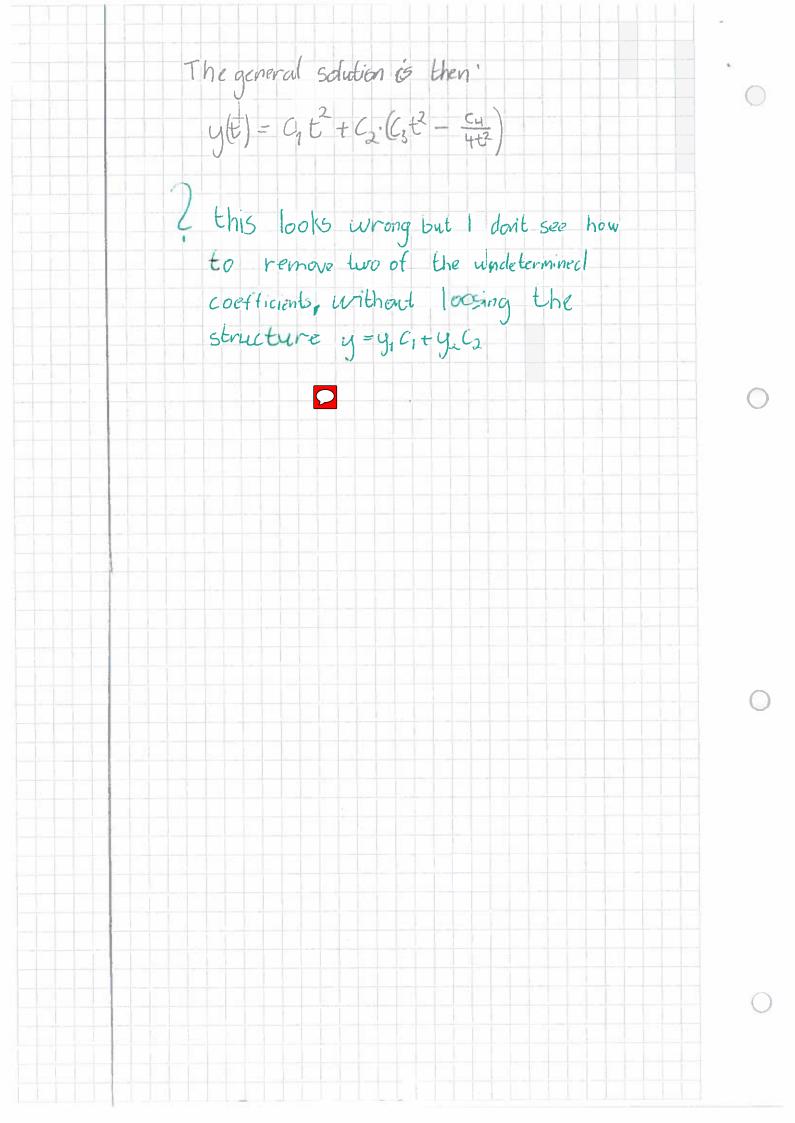
17) et is not a constant multiple of et so they are linearly independent, $W(t) = \begin{bmatrix} e^{-t} & e^{2t} \\ -\bar{e}^{t} & 2\bar{e}^{t} \end{bmatrix}$ e 2 2 - e (-e) e (2 2 to 2t) = e 7 0 Since WE) 70, y and y, are breakly independent. 19 cos(3t) is a phase-shifed version of sir(3t), and thus one can be constant multiple of the other, so they are Linearly independent. W(t) = cost sinst -35 m3t 3003t = cos3t).3cos(3+)-(sin3t)(3sin3t)) = 3 cos23t + 3 sin2Bt Since W(t) 7 0, y, and your linearly independent.

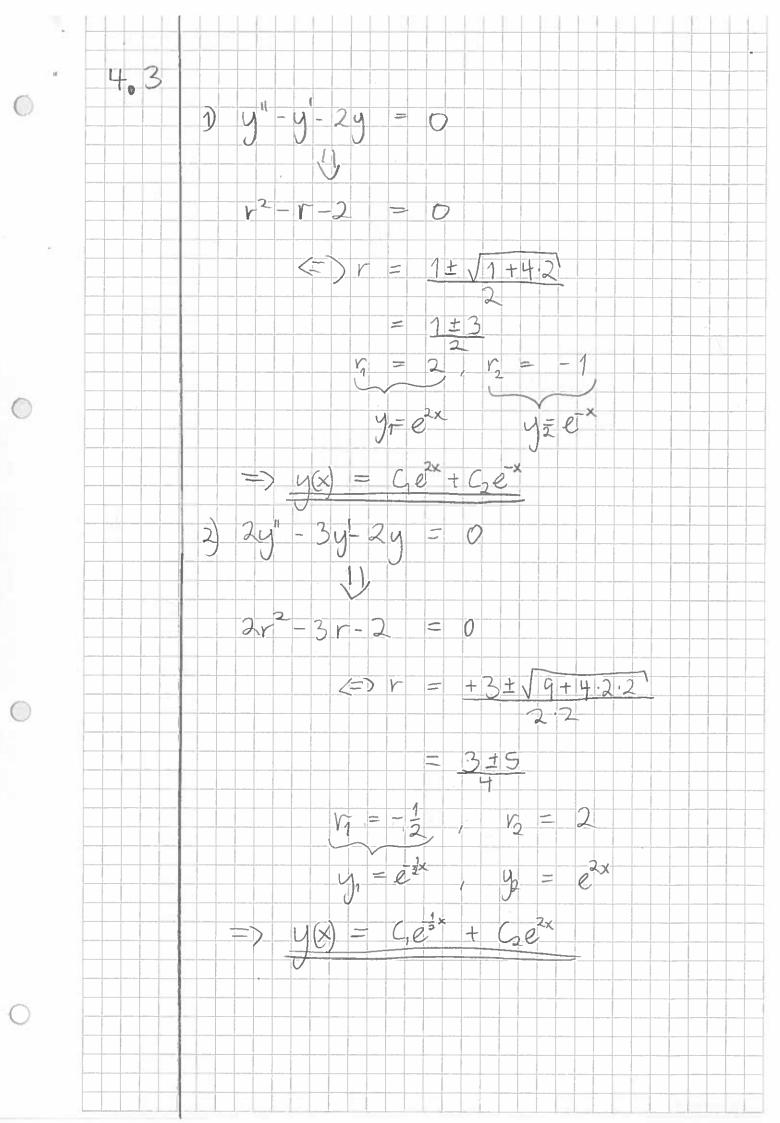
Same as with (18); you and you contain a common factor of et, but the tria functions are viol constant multiples of each other so whey are linearly independent. y1 = e2t cay3t) y! = -2e26 cos(3t) -3@24 sin(3t) 1/2 = e 2t sin Bt y= -2e2t sin(bt) +3e2t. cos(3+) $W(t) = \begin{cases} y_1 & y_2 \\ y_1 & y_2 \end{cases}$ e cost (-2e sinst) + 3e2 cost) - e 2 sin3t) (-2 e cos3t)-3e su3t) = e2t e2t (-2co-3t) w.(3t) + 3co-8t) +. e = = (2 52 (3 t) cos(3t) + 3 sin (3t)) = e4t (-2663t) Fin(3t) + 25in(3t) 658t +3cos23t)+3sin(34)) Since W(t) = 3et + 0, y, and y, are linearly independent

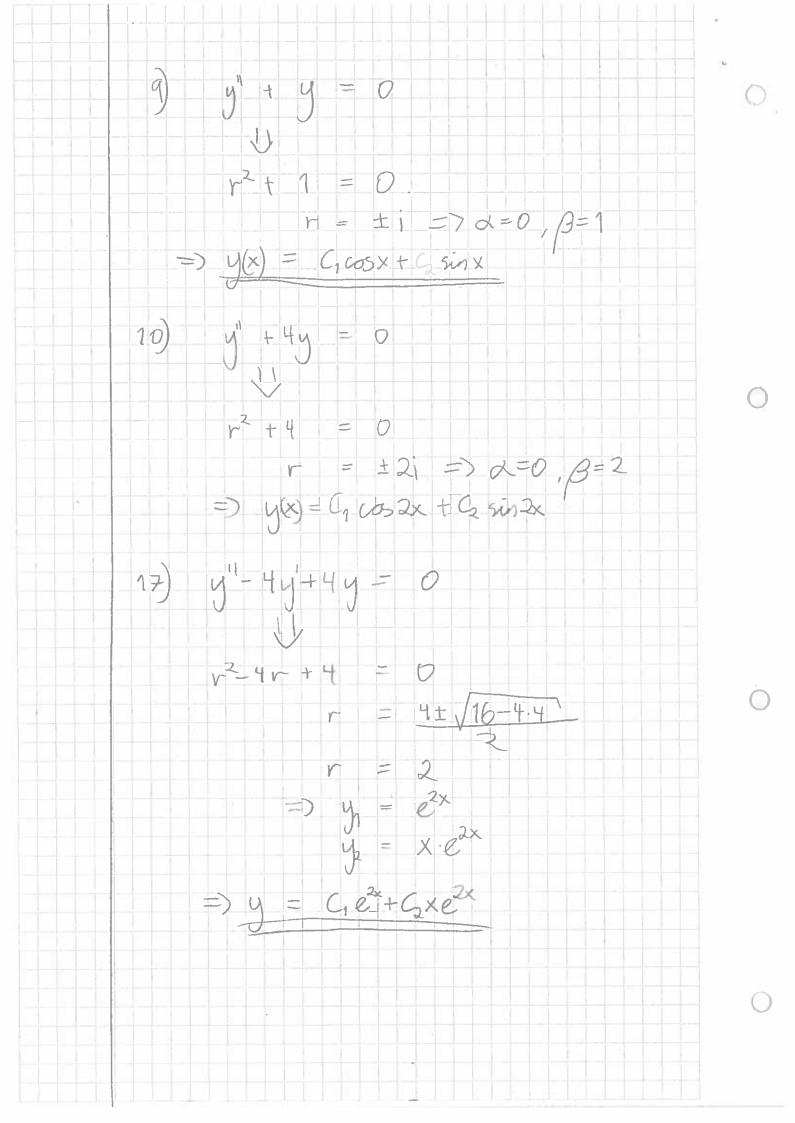
Here y(t) = y(t) it so they are obviously linearly independent, $y(t) = e^{3t}$ $y(t) = -3e^{3t}$ $y(t) = te^{3t}$ $y(t) = t \cdot (3e^{3t} + e^{3t} = (1-3t)e^{3t}$ $= e^{-3t} \cdot (1-3t) e^{3t} - te^{-3t} \cdot (-3)e^{-3t}$ $= e^{-6t} \cdot (1-3t+3t)$ $= e^{-6t} \neq 0$ Since W(t)=est + 0, y, and y, are linearly independent.

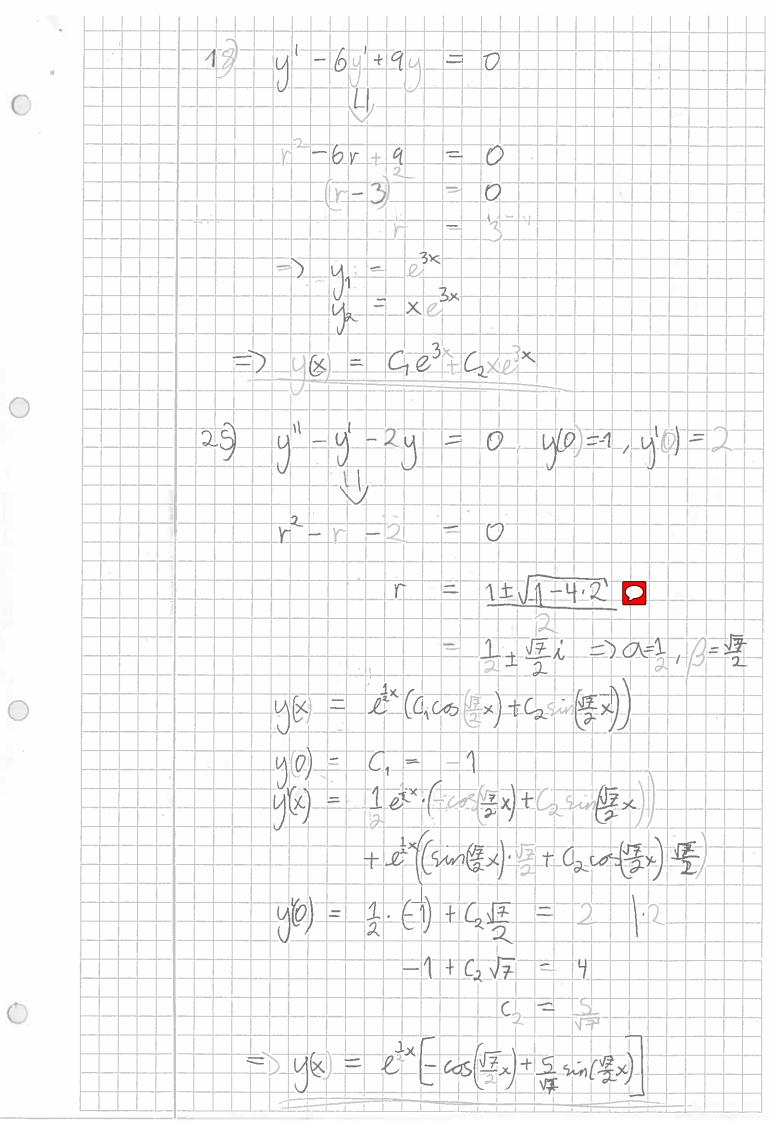


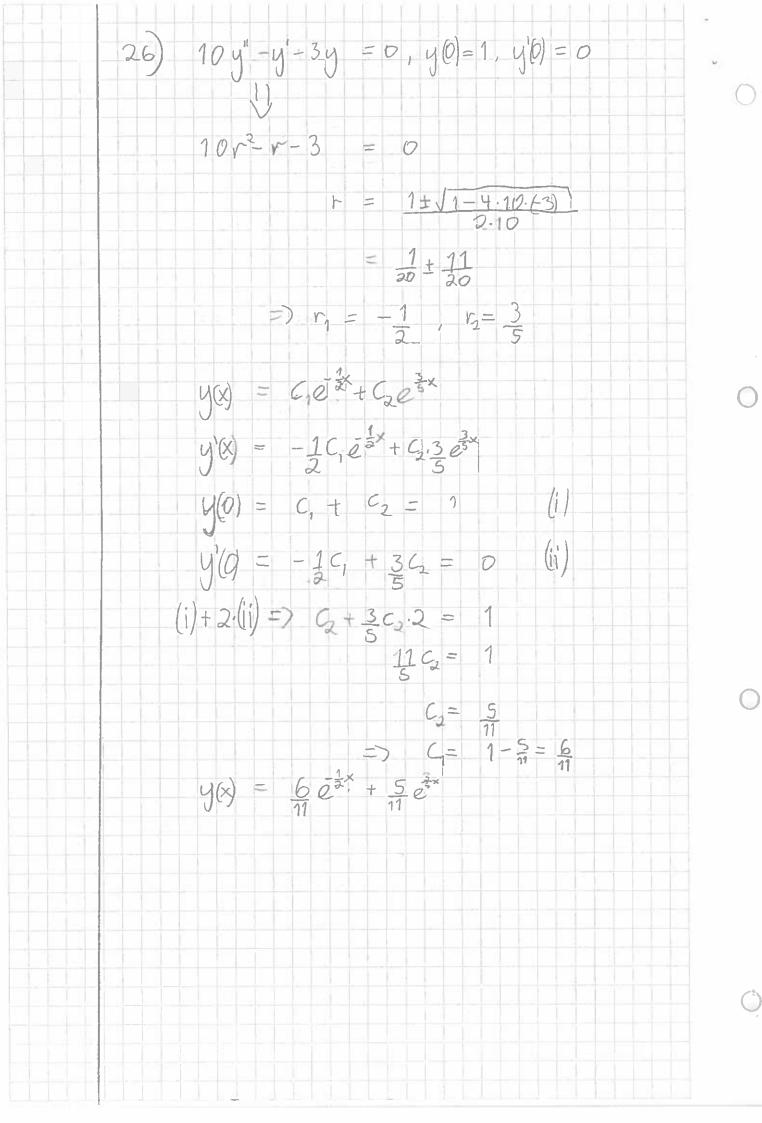




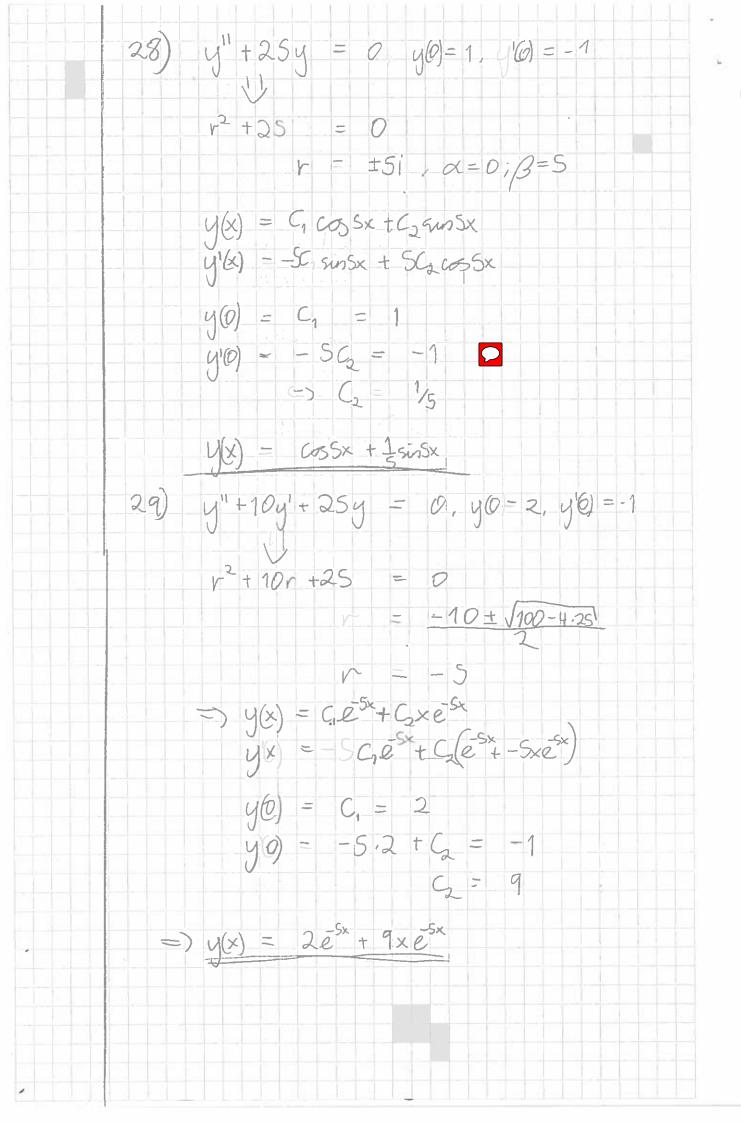




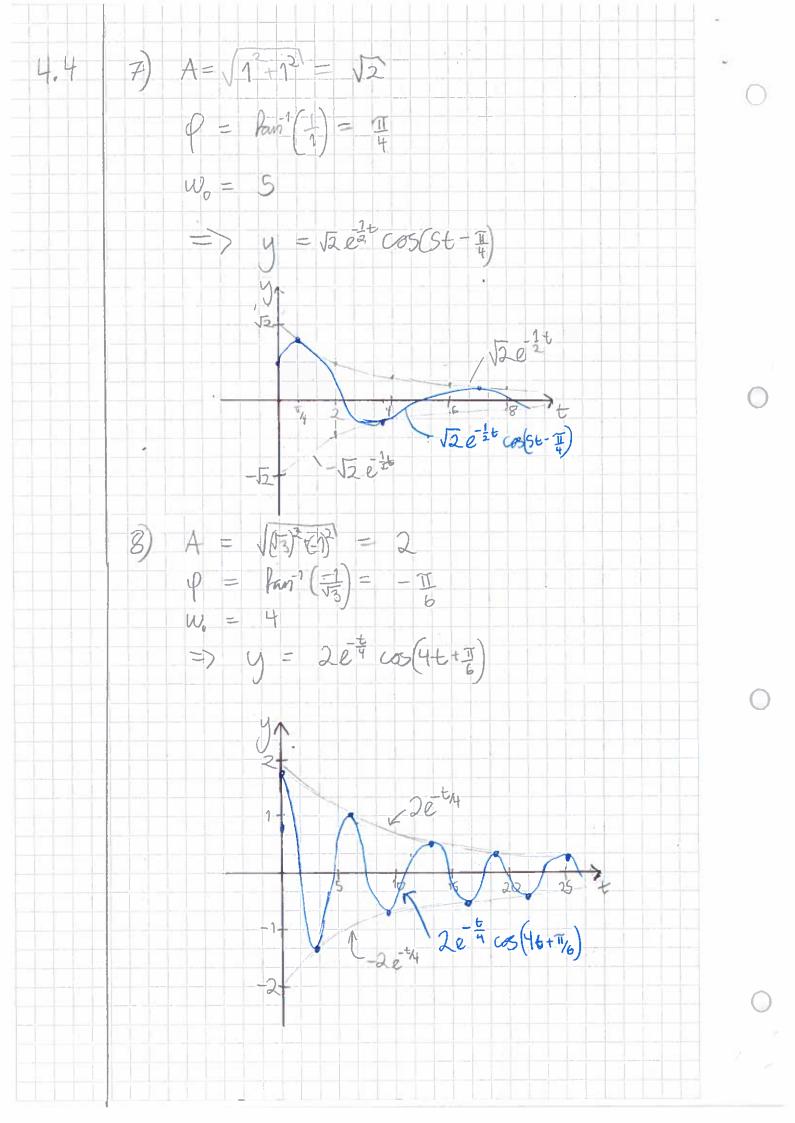


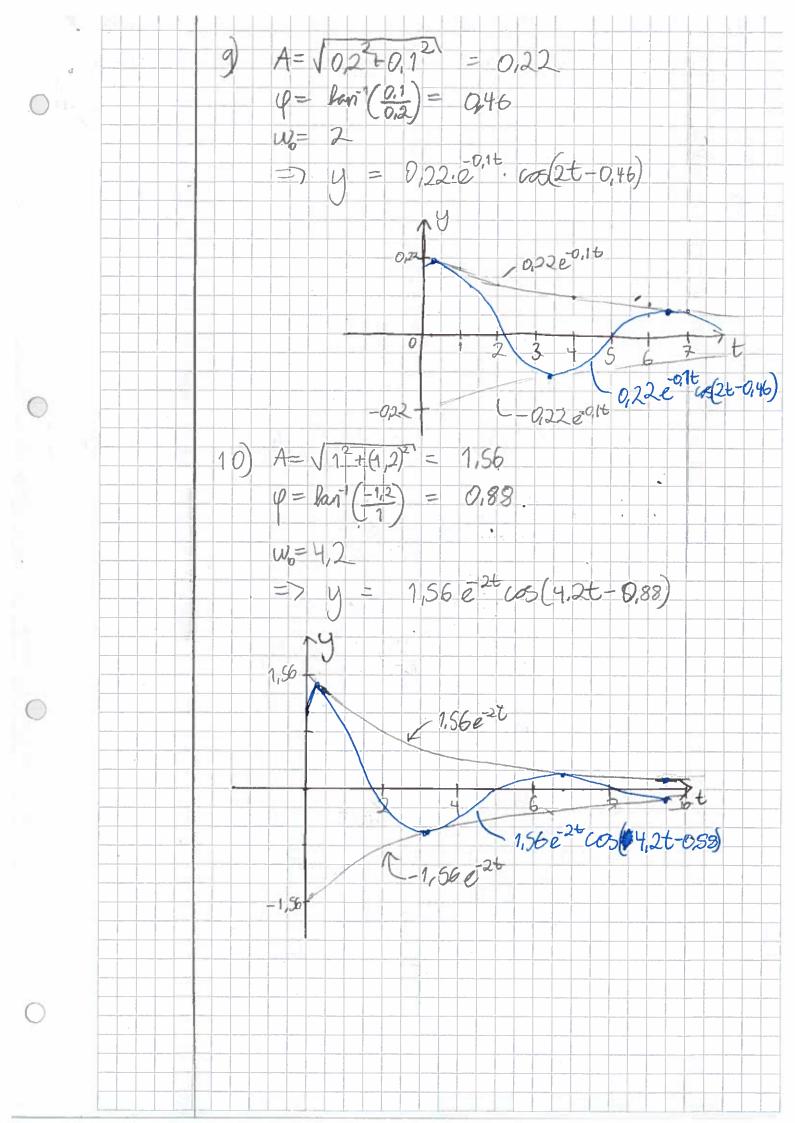


(27) y'' - 2y' + 17y = 0, y(0) = -2, y(0) = 3 $r = 2 \pm \sqrt{4 - 4.17}$ $= 1 \pm 2 \sqrt{1-17}$ $= 1 \pm 4i = 3 = 1, \beta = 4$ = 2 + 3 = 4 + 3 = 4 = 1 = 2 + 3 = 4 = 1 = 2 + 3 = 4 = 1 = 2 + 3 = 4 = 1 = 3 + 3 = 1 = 3 + 3 = $y(x) = e\left[c_1 \cos 4x + c_2 \sin 4x\right]$ te[4c.(-sntx)+4c2costx] $y(0) = c_1 = -2$ $y(0) = -2 + 4c_2 = 3$ =) y(x) = e.[-2cos4x + 5 sin+x]



then $y'=t \times 1e^{it} + e^{it} = (t \times 1) e^{it}$ $y''=(t \times 1) \cdot e^{it} + (t \times 1) (e^{it})'$ $=\lambda_1e^{\lambda_1t}+(t\lambda_1+1)\lambda_1e^{\lambda_1t}$ $= (\lambda_1 + (\lambda_1 + \lambda_2) e^{\lambda_1 t}$ $= (\lambda_1^2 + 1 + 2\lambda_1)e^{\lambda_1 t}$ $=\lambda(\lambda, \pm 1)e^{\lambda \pm}$ inserted into the equation: y" tpy tqy = 0 (x2t+2h)et+p(tx,+)et+qtex=0 $\lambda_1 t + 2\lambda_1 + p\lambda_1 t + p + q t = 0$ If $\lambda^2 + p\lambda + q = 0$ has a double root, then p-49 = 0 and the solution is and $q = p^2$ So (*) becomes -8) ++2 = +p.(-1)++p+p2+= P2 - P - P + 10+ 026 = 0 This shows that y=tent is a solution,





13)
$$2 | x^n + K x = 0$$
, $x(0) = 0$, $x(0) = V_0$
 $3 | x^2 + K = 0$
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(2) $i_{2} = 2 V_{0}$ $V_{0} = \sqrt{10 \cdot k^{2}} = \sqrt{10 \cdot 8^{2}} = \sqrt{10 \cdot 8^{2}}$ Ker 32 og Vo er 8 $m x'' + Kx = 0, x(0) = x_0, x(0) = V_0$ 14) $X'' + \frac{K}{m} \times =$ $V^2 + \frac{K}{m} = 0$ $|r| = \pm \sqrt{\frac{K}{m}} i$ $= \int x(t) = C_1 \cos(\frac{K}{m}t) + C_2 \sin(\frac{K}{m}t)$ $= \int x(t) = -C_1 \int_{m}^{K} \sin(\frac{K}{m}t) + C_2 \int_{m}^{K} \cos(\frac{K}{m}t)$ $X(0) = C_1 = X_0$ $X(0) = C_2 \cdot \sqrt{\frac{K}{m}} = V_0$ $= C_2 \cdot \sqrt{\frac{K}{m}} = V$ $A = \sqrt{x_0^2 + \frac{mv_0^2}{K}}$

