$$\int d\phi \, \boldsymbol{S}(\vec{q}_T, \vec{v}_t, \mu) =$$

$$\sum_{X_s} f_{X_s}(\vec{q}_T') \int_{X_s} \underbrace{\int_{t, (1, -\hat{v}_t)}^{t, (1, +\hat{v}_t)} \underbrace{\int_{t, (1, -\hat{v}_t)}^{t} \underbrace{\int_{t, (1,$$