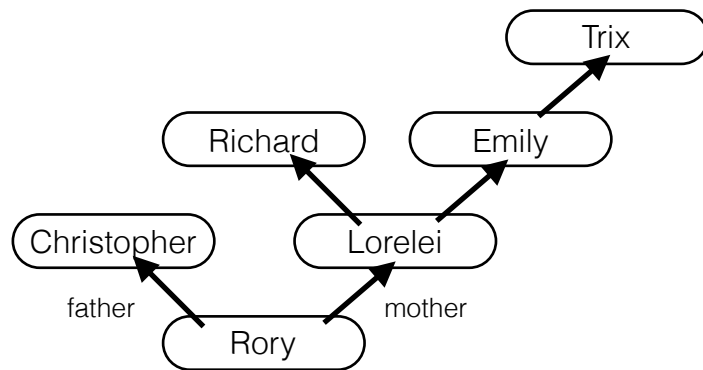
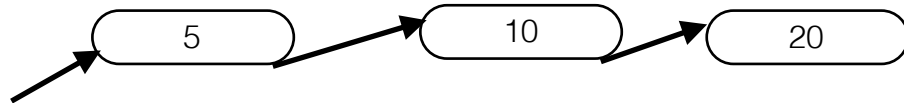


Objectives: Merge sort review; recursion: practice and more advanced;

Up next: MP7; Extra credit?



1. Write a tail recursive with a string accumulator method and a wrapper method to return the father with the longest name. Only consider the male lineage.



2. How can we insert links to create a *sorted* linked list?

```

list = new LinkedList(10,null);
list = list.insert(20);
list = list.insert(5);
public LinkedList(int newValue, LinkedList newNext)
    { ... } //constructor
  
```

Write a function that takes an int and inserts in order:

```

public LinkedList insert(LinkedList list, int value) {
    if (list == null || value < list.value)
        return new LinkedList(value, list);
    else {
        list.next = insert(list.next, value);
        return list;
    }
}
  
```

3a. **Merge Sort review:**

```

static void mergeSort(int[] data, int lo, int hi) {
    if (lo >= hi) return;
    int mid = (lo + hi) / 2;

    mergeSort(data,?,                );
    mergeSort(data,?,                );

    int size = hi - lo + 1;
    int[] temp = new int[size];

    merge(data,temp,lo,mid+1,hi);

    for (int i = 0; i < size; i++) data[i+lo] = temp[i];
}

public static void merge(int[] a, int []tempArray,
                        int lower, int mid, int upper){

    int tempIndex=0;
    int leftLo = lower;
    int leftHi = mid-1;
    int rightLo = mid;
    int rightHi = upper;

    }
  
```

3b. How many levels does the merge sort activation diagram have (roughly)? Why?

3c. At each level of the tree ($j = 0, 1, 2, \dots$), how many subproblems are there (as a function of N)?

3d. At each level of the tree ($j = 0, 1, 2, \dots$), how many values are in the array passed into the recursive activation (as a function of N)?

4. Write a recursive song in ABA format:

```
// Recursive method to create the pitches for son
// Assume pitches in array have all been initialized to 440.0;

public static void createSong(double[] pitches, int lo, int hi,
double augment) {

    // divide the range of subarray into thirds and work on each
    third

    int oneThird = (hi - lo + 1) / 3;

}
}
```

5. You have an array of doubles. You want to search between indices 'lo' and 'hi'.

Write a recursive method to find the largest product of two neighboring values. e.g. findPair({ 1.0 , 1.0 , 7.5 , 4.0, 4.1 , 3.5 },0,5) returns 30.0 (7.5 * 4.0), which is largest product of two neighboring values.

```
public static double findPair(double[] array, int lo,
                                int hi) {
```

Write a FORWARD recursive method to find the first index of the largest product of two neighboring values. e.g. findPair({ 1.0 , 1.0 , 7.5 , 4.0, 4.1 , 3.5 },0,5) returns 2 because 7.5x4.0=30.0 is largest product of two neighboring values.

```
public static int findPair(double[] array, int lo, int hi) {
```