

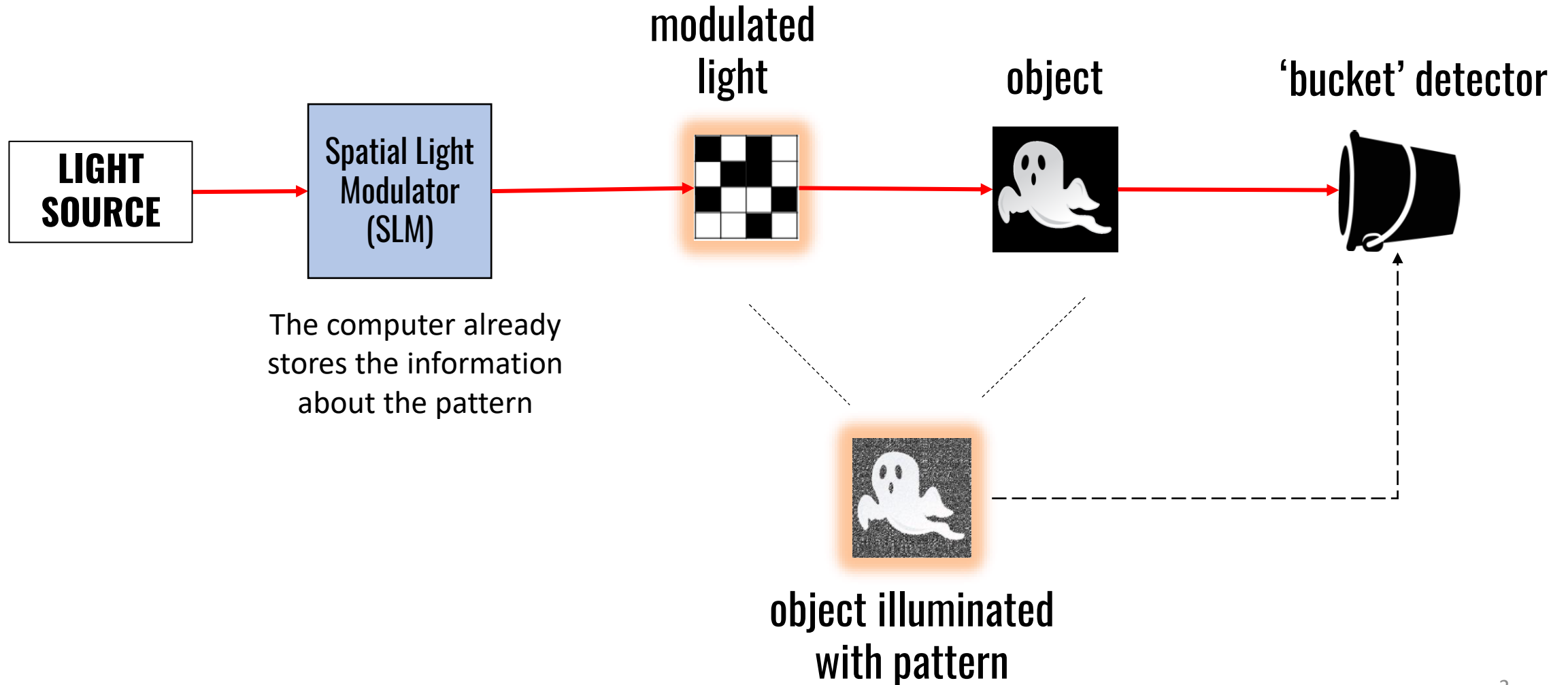
# Ghost Imaging

Physics 305 Computational Imaging

Acknowledgement: Slides are from presentation by Dr. Ritz Ann Aguilar

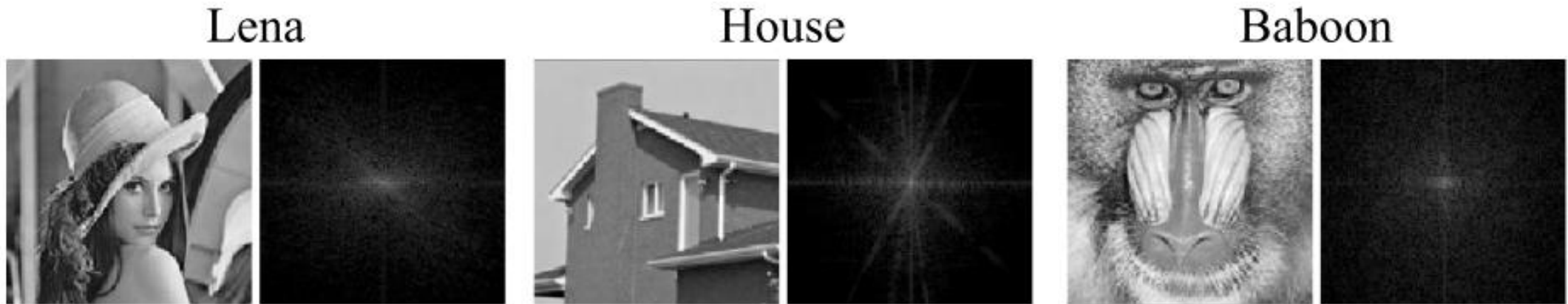
# GHOST IMAGING: COMPUTATIONAL

## a.k.a Single-Pixel Imaging



# Fourier Ghost Imaging (FGI)

- Uses the knowledge of Fourier Transform
- Utilizes knowledge that most of the information of natural images is concentrated in **low** spatial frequency bands



[1] Marcellin M W, JPEG2000: Image Compression Fundamentals, Standards and Practice vol 1 (Springer), 2002

[2] Bian et al., 2016, Efficient single pixel imaging in Fourier space, Journal of Optics, 2016

# Fourier Ghost Imaging (FGI)

- Project sinusoidal patterns onto the object. Sinusoidal pattern intensity is given by

$$I_n(x, y; f_x, f_y) = a + b \cdot \cos(2\pi(f_x x + f_y y) + n\phi) \quad (1)$$

- For 3-bucket algorithm, we set the phase shift to  $\Delta\Phi = \frac{2\pi}{3}$  and  $n = 0, 1, 2$ .
- Total intensity of reflected light from the object with reflectance  $R(x, y)$  is

$$E_n(f_x, f_y) = \iint R(x, y) I_n(x, y; f_x, f_y) dx dy \quad (2)$$

- Total response of the detector is

$$S_n(f_x, f_y) = S_r + k E_n(f_x, f_y) \quad (3)$$

where  $S_r$  is ambient light,  $k$  is a scale factor.

- Substituting (1) into (3) we get detector output

$$D_n(f_x, f_y) = D_b + ak \iint R(x, y) dx dy + bk \iint R(x, y) \cdot \cos(2\pi(f_x x + f_y y) + n\phi) dx dy \quad (5)$$

# Fourier Ghost Imaging (FGI)

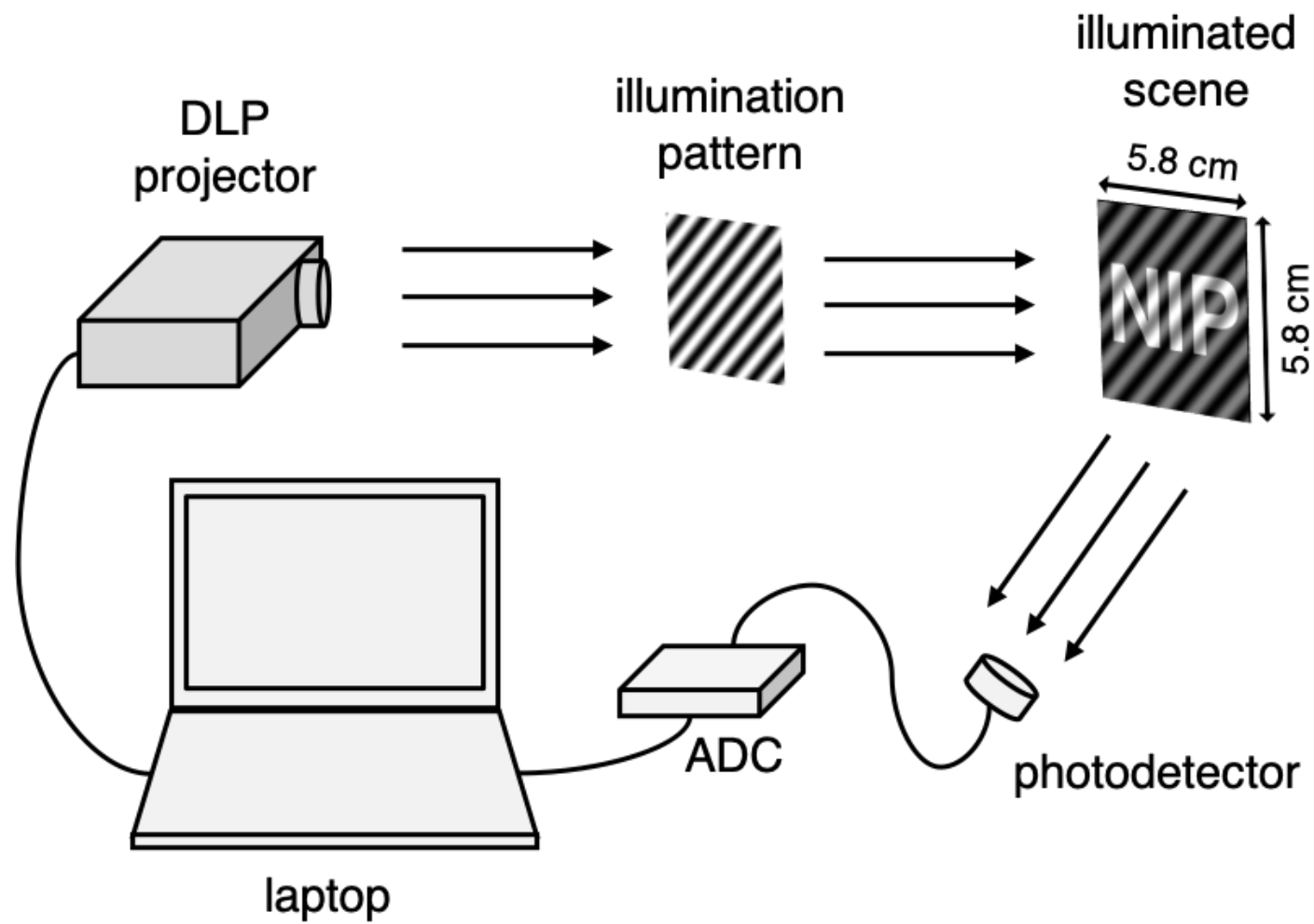
Arrange as follows:

$$\begin{aligned} & \frac{1}{3} [2S_0 - S_1 - S_2] + \frac{\sqrt{3}}{3} j \cdot [S_2 - S_1] \\ &= bk \iint R(x, y) \cdot \left\{ \cos \left( 2\pi(f_x x + f_y y) \right) - j \cdot \sin \left( 2\pi(f_x x + f_y y) \right) \right\} dx dy \\ &= bk \iint R(x, y) \cdot \exp[-j2\pi(f_x x + f_y y)] dx dy \\ &\propto \mathcal{F}\{R(x, y)\} \end{aligned}$$

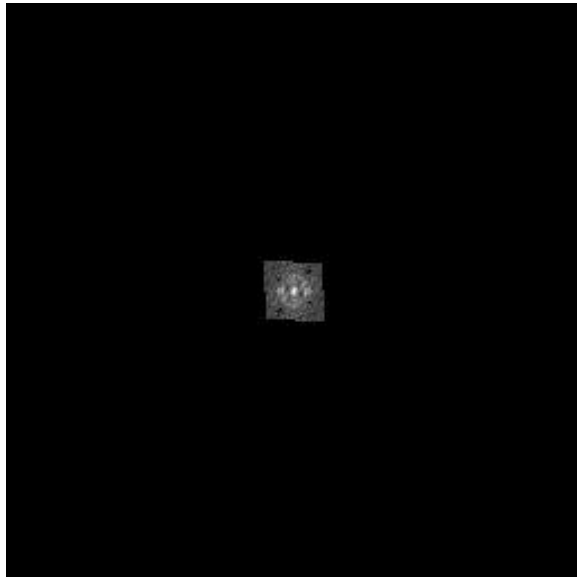
Total reflectivity of the object:

$$R(x, y) \propto \mathcal{F}^{-1} \left\{ \frac{1}{3} [2S_0 - S_1 - S_2] + \frac{\sqrt{3}}{3} j \cdot [S_2 - S_1] \right\}$$

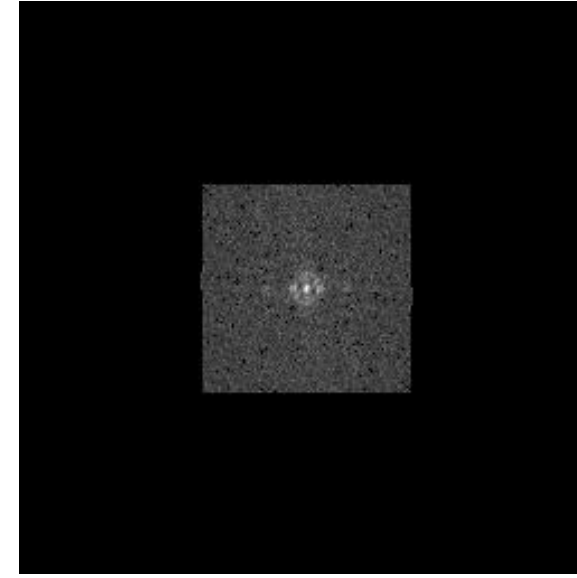
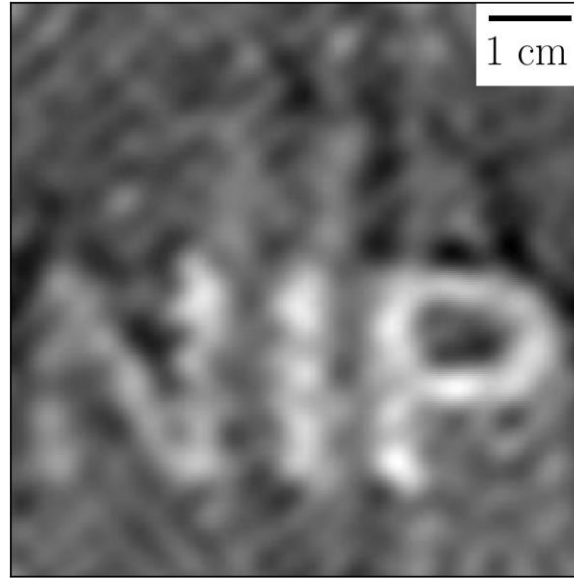
# Setup



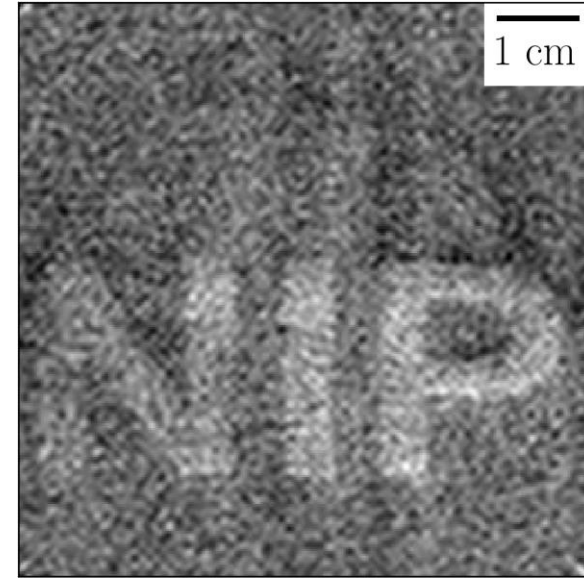
# Experiment Results



1% Spectral Coverage

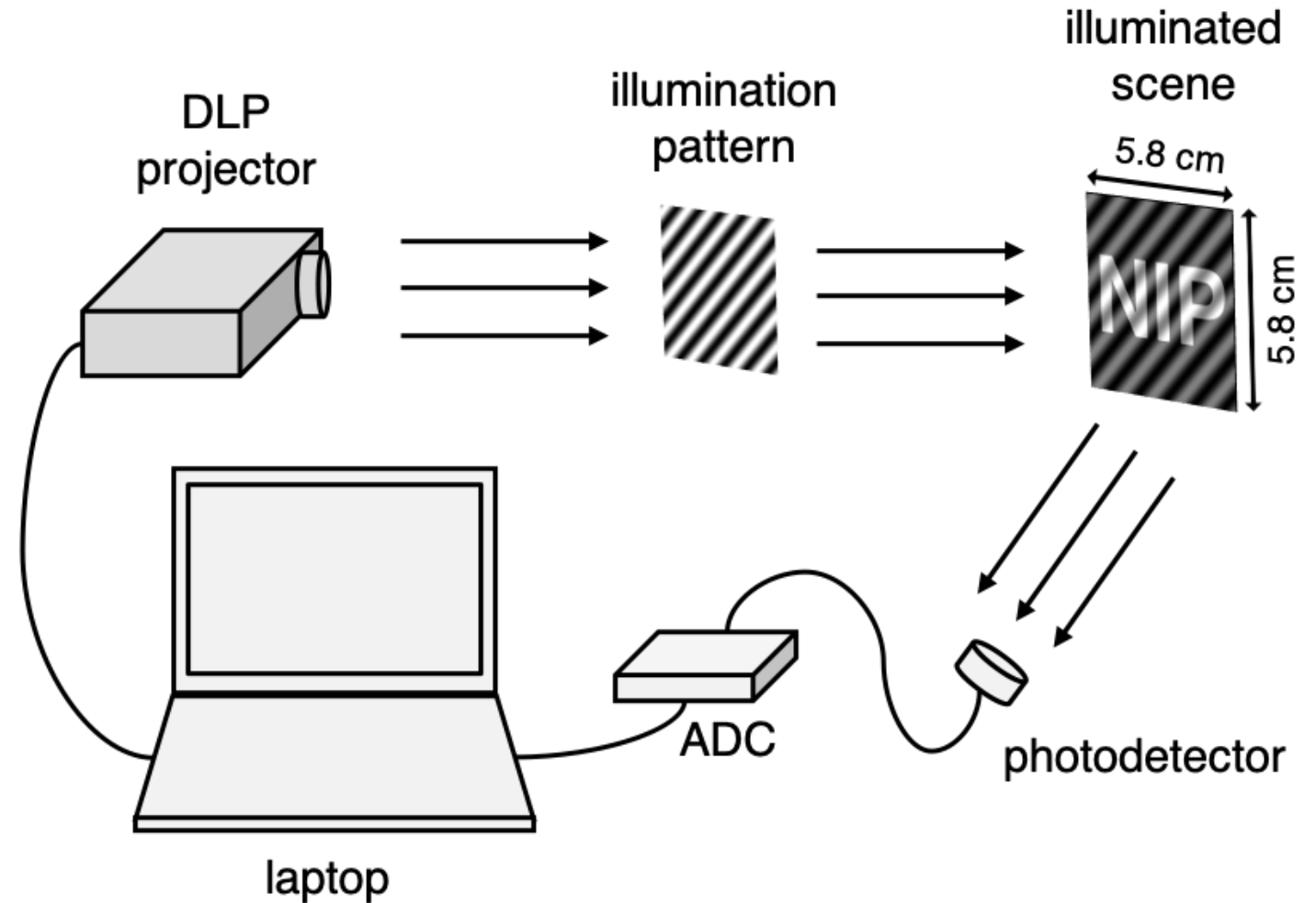


10% Spectral Coverage



# Class Activity (Activity 5)

- We will rebuild the Computational Ghost Imaging Setup of Dr Ritz Ann Aguilar and we will capture images for FGI reconstruction
- Group the class into the following:
  - Photodetector group
  - Projector group
  - Computation group





# Group Assignments

## Photodetector Group

- Will calibrate and program a light-dependent resistor (LDR) to capture signals
- Vince, Linus, Jem, Janelle, Christian V.

## Projector Group

- Will generate the sinusoidal patterns for projection
- Nina, Lem, Celso, Christian B., Reinier

## Computation Group

- Will reconstruct the image from the signals captured by LDR
- Don Ver, Ryan, Rene, JC, Hazel

# Reference

- Aguilar, R. A., Hermosa, N., & Soriano, M. N. (2019). Low-cost Fourier ghost imaging using a light-dependent resistor. *American Journal of Physics*, 87(12), 976-981.