The background image is a surreal landscape. It features a vast field of green, mound-like structures arranged in a precise grid pattern. These mounds are partially submerged in a shallow layer of blue liquid, which reflects the sky. In the upper center, a black flagpole with a red flag stands. In the middle ground, a small black sphere is visible. The sky is filled with soft, white clouds. A dark, semi-transparent rectangular box is overlaid on the left side of the image, containing the title and names.

# Crazy Putting Phase 3

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# The challenge

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1. Implement collision detection.
2. Improve the bot to handle complex terrains like mazes.
3. Having a random error in the initial position and velocity of the ball, including an analysis of the impact on the bot's performance.
4. Allow for balls that can both fly and bounce, as well as improvements to the bot so it can handle these new options.
5. Handling different (unknown) coefficients of friction and making sure the bot can handle them.

# Table of contents

1. Game Engine
2. Physics
3. Bots
4. Conclusion



# Game Engine

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We have made our own OpenGL-based game engine with support for the following features:

Dynamic terrain generation

Real-time editing

Collision detection

Realistic lighting

Water with special effects (du/dv maps, reflections, depth effect)

3D model support (.obj)

Third person camera

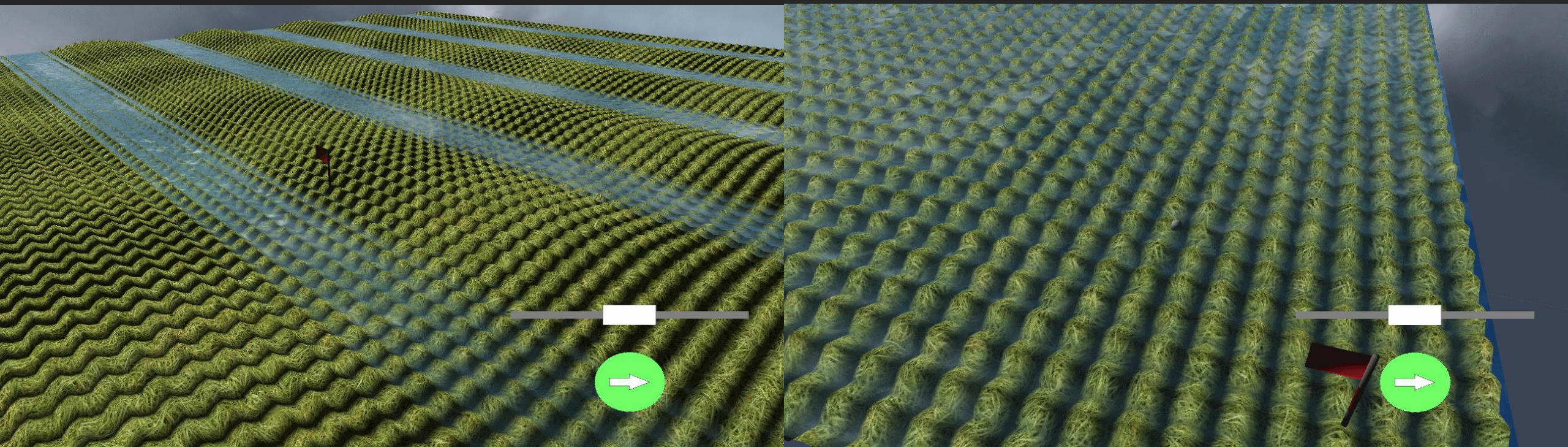




# Terrain generation

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Given a mathematical function with the variables  $x$  and  $y$  we can generate a terrain during runtime.

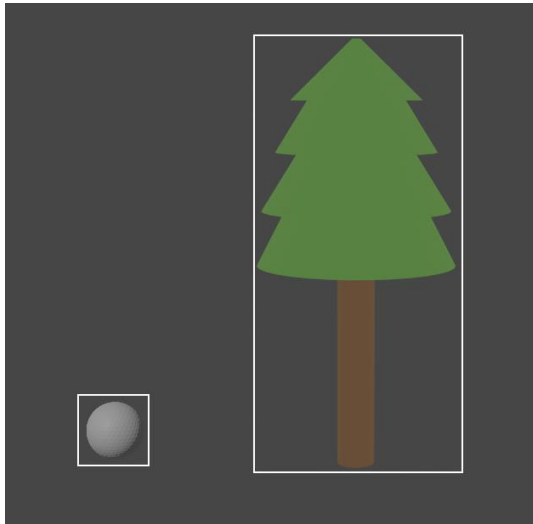


# Collision detection

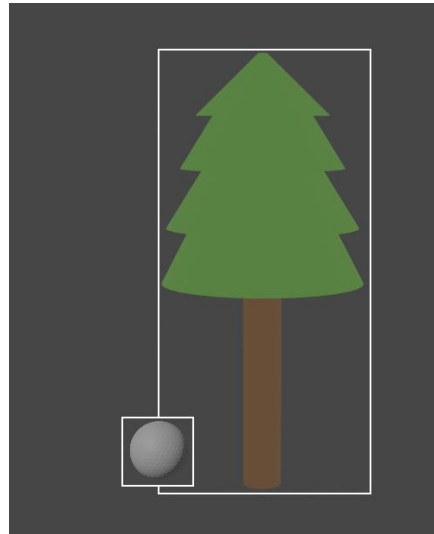
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Stages:

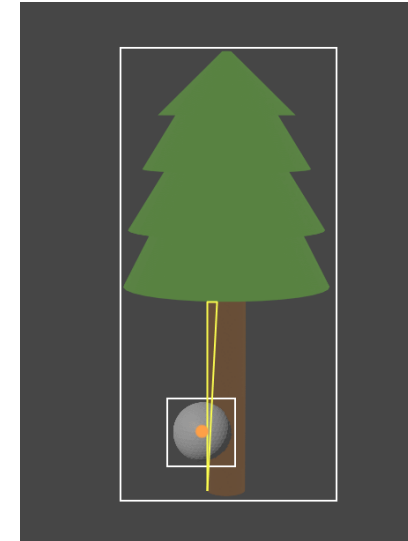
1. Check if the smallest possible box around an object, that still contains every point making up the model, overlaps with that of the ball.
2. Check if the actual mesh is colliding with the ball



No collision



Possible collision

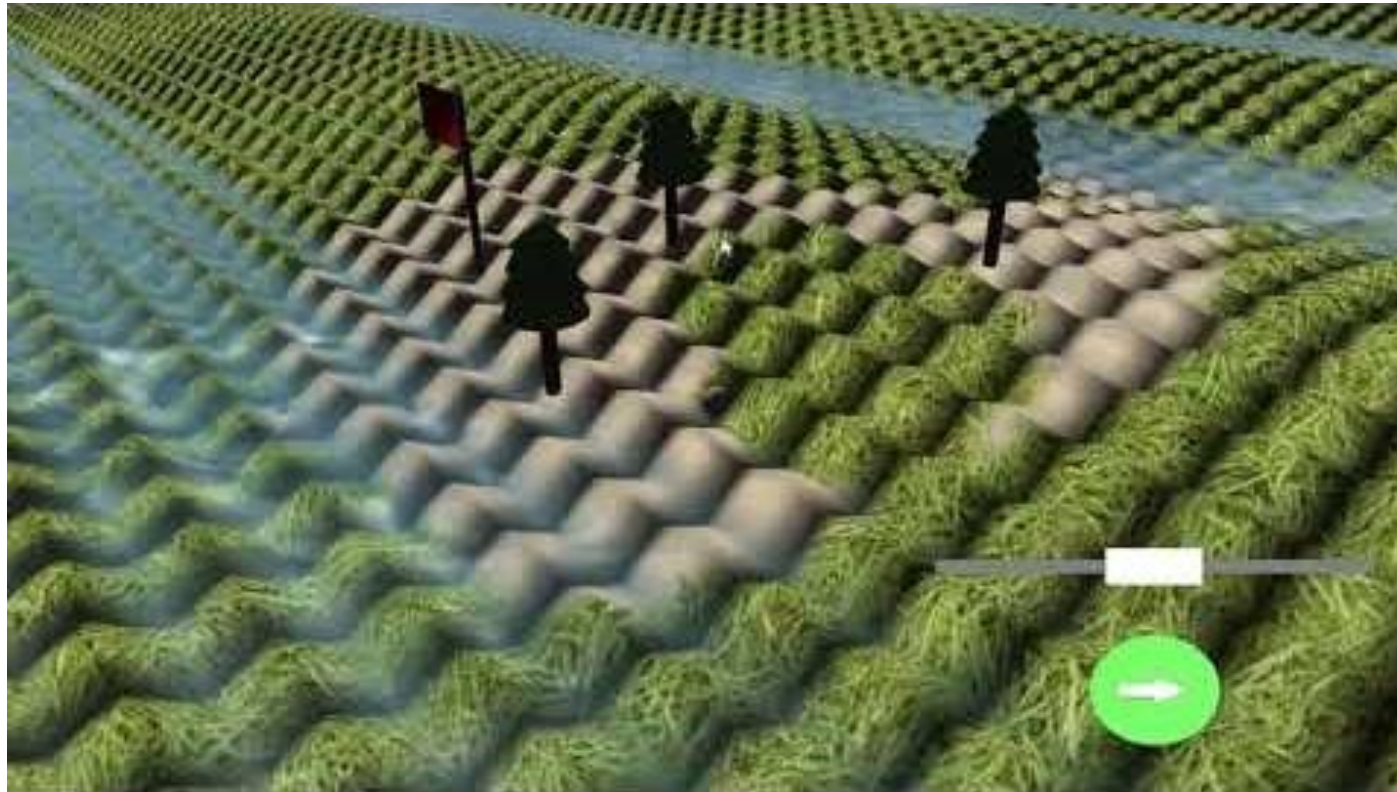


Collision



# Live saving and loading

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# Our solvers

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Last period we rewrote the entire physics engine to improve the interaction with the game. We also added 1 solver to improve the accuracy of our calculations.

❖ Classical 4<sup>th</sup> order Runge-Kutta



# The formulas

## Classical 4<sup>th</sup>-order Runge-Kutta

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$$k_1 = v(t)$$

$$l_1 = a(p(t), v(t))$$

$$k_2 = v(t) + l_1 \frac{1}{2} \Delta t$$

$$l_2 = a\left(p(t) + k_1 \frac{1}{2} \Delta t, k_2\right)$$

$$k_3 = v(t) + l_2 \frac{1}{2} \Delta t$$

$$l_3 = a\left(p(t) + k_2 \frac{1}{2} \Delta t, k_3\right)$$

$$k_4 = p(t) + l_3 \Delta t$$

$$l_4 = a(p(t) + k_3 \Delta t, k_2)$$

$$p(t + \Delta t) = p(t) + \frac{1}{6} \Delta t (k_1 + 2k_2 + 2k_3 + k_4)$$

$$v(t + \Delta t) = v(t) + \frac{1}{6} \Delta t (l_1 + 2l_2 + 2l_3 + l_4)$$

# Flying and bouncing balls

---

```
process(double deltaTime, (Vector position, Vector velocity))
```

```
  FOR time=0 TO time=deltaTime
```

```
    IF !isFlying(position)
```

```
      THEN velocity = redirectVelocity(position, velocity)
```

```
      calculate next position and velocity
```

```
      update position and velocity
```

```
  return (position, velocity)
```



Bouncing ball video



# Flying acceleration

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❖ In the horizontal directions:

$$F_{net} = -F_D \quad \rightarrow \quad ma = -\frac{1}{2}C_D\rho A\dot{x}^2$$

$$a = -\frac{C_D\rho A\dot{x}^2}{2m}$$

$$\rightarrow \quad a = -\frac{C_D\rho A\dot{y}^2}{2m}$$

❖ In the vertical direction:

$$F_{net} = -F_g - F_D \rightarrow \quad ma = -mg - \frac{1}{2}C_D\rho A\dot{z}^2$$

$$a = -g - \frac{C_D\rho A\dot{z}^2}{2m}$$

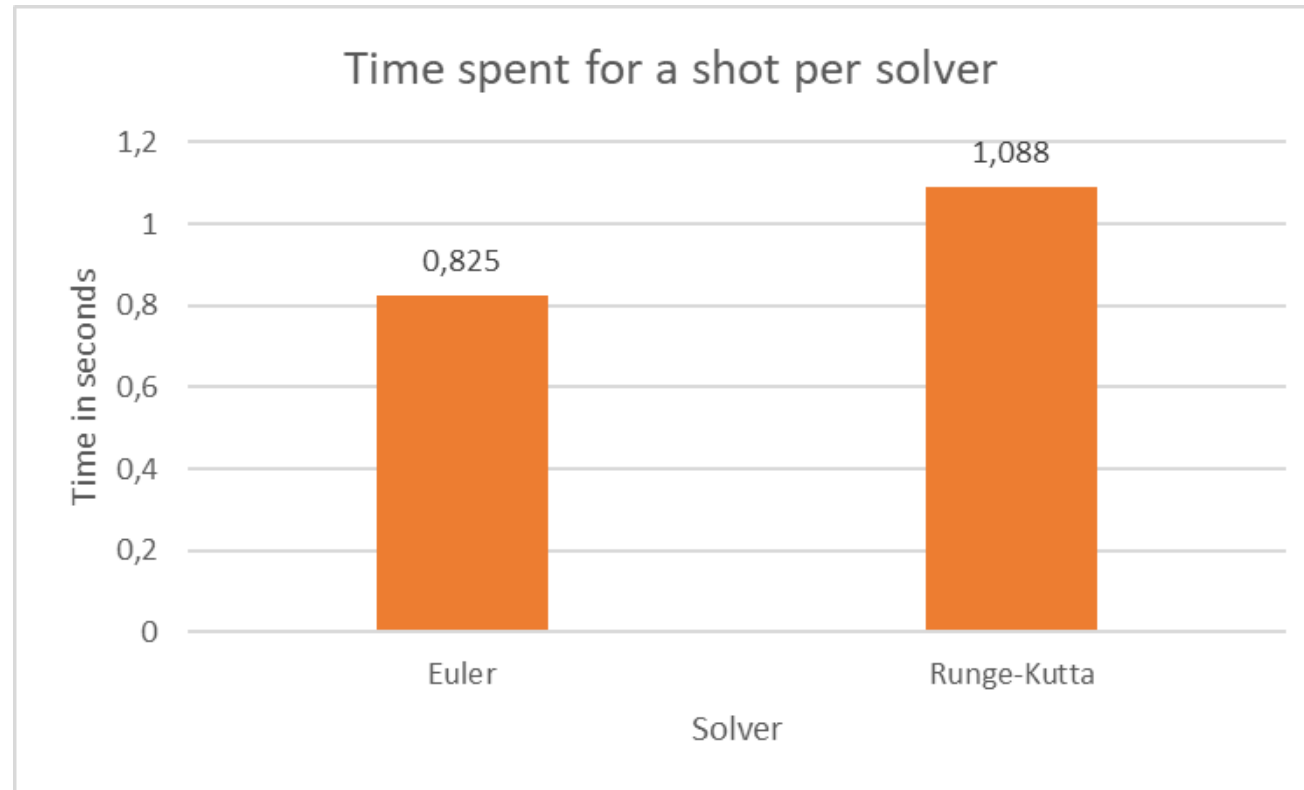
# Precision experiment

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# Speed experiment

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# Bots

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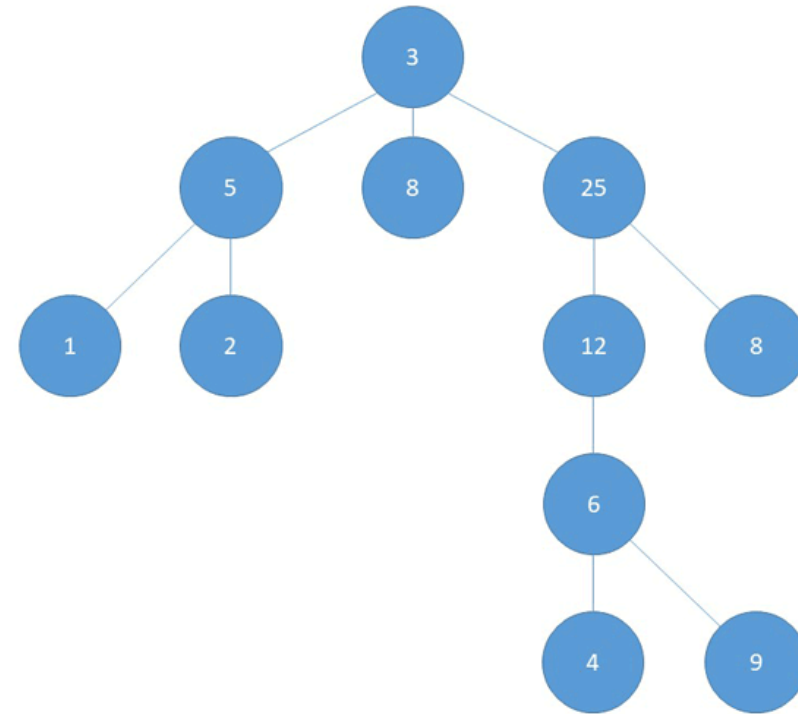
- ❖ Random error
- ❖ Different coefficients of frictions

# Single Shot Bot

- ❖ Finds the location of the flag
- ❖ Computes shots in the area of the flag and stores the successful ones
- ❖ For each successful shot stored, it aims to try the perfect velocity
- ❖ If there is an obstacle between the ball and the flag, it will shoot the ball with a wider angle
- ❖ If no hole in one solution is possible, it won't find a solution.
- ❖  $O(\text{maxVelocity} / (\text{degree step} * \text{velocity step}))$

# BFS Graph Bot

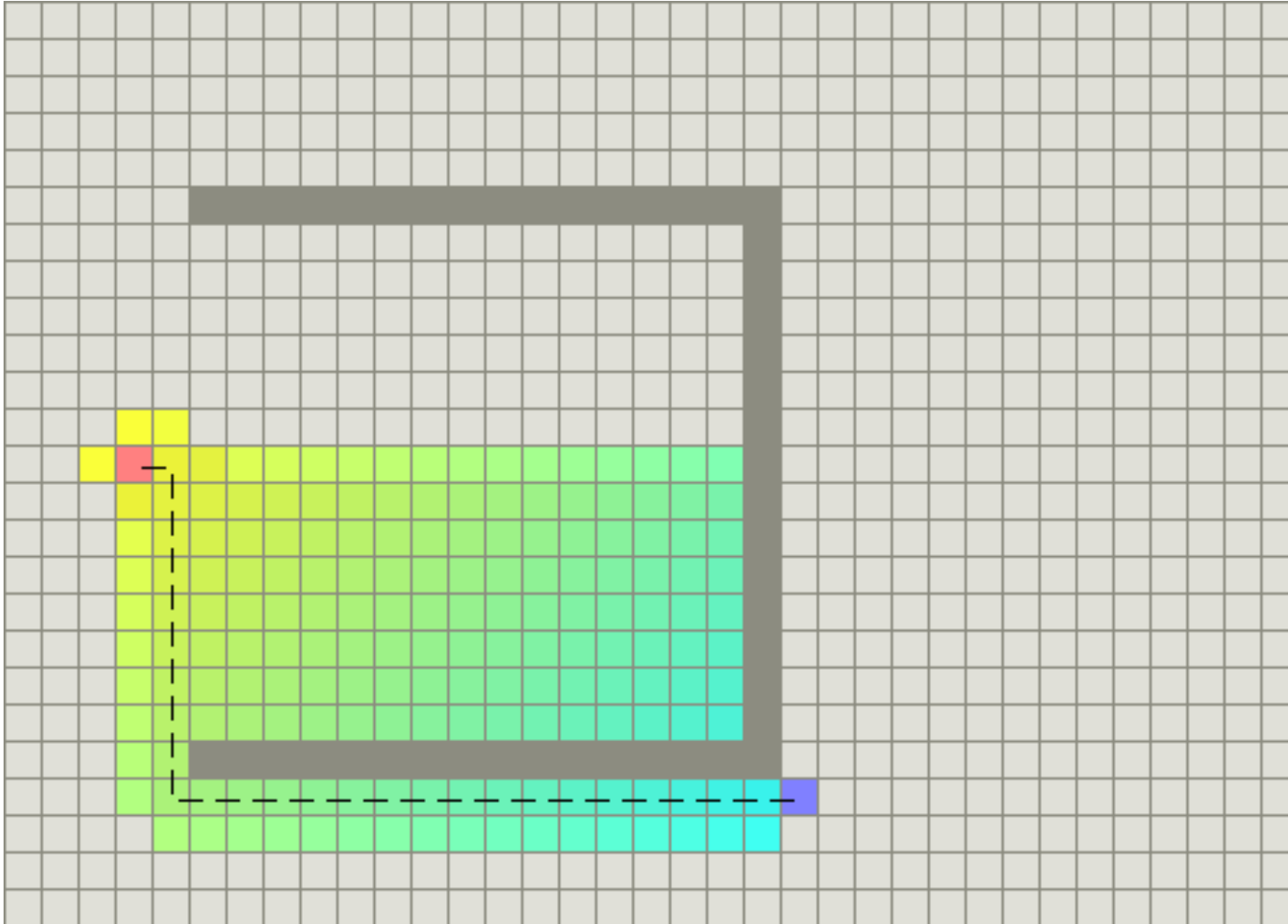
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Olivera Popović. (2020). Breadth-First Search [gif]. Stack Abuse  
<https://stackabuse.com/graphs-in-java-breadth-first-search-bfs/>

$O(\text{grid} * \text{the number of outgoing shots} * \text{shot complexity} + \text{grid})$





From <http://theory.stanford.edu/~amitp/GameProgramming/AStarComparison.html> by Stanford, date unknown

# A\* Bot

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# Experiments

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# Conclusion

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- ❖ Graphics engine
- ❖ Collision detection
- ❖ Physics solvers
- ❖ Flying and bouncing balls
- ❖ AI





# Questions

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