## FLIGHT LANDING DISTANCE ANALYSIS

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**MOTIVATION**: To reduce the risk of landing overrun.

**GOAL**: To study what factors and how they would impact the landing distance of a commercial flight.

**DATA**: Landing data (landing distance and other parameters) from 950 commercial flights (not real data set but simulated from statistical models). See two Excel files 'FAA-1.xls' (800 flights) and 'FAA-2.xls' (150 flights).

# **SUMMARY:**

I split the project into three Chapters: Data Cleaning, Analysis of relationship between variables and Regression modelling. I have summarized the methods used at each step and the results I got for all three parts below:

- Data Cleaning and Preparation: Here I tried identifying the structure of the data and got rid of abnormal observations. There were several missing values but I didn't want to get rid of those observations at the very outset of the analysis. Finally, at the end of data cleaning I had a data set with 831 observations
- Analysis of relationship between variables: I used x-y plots and correlation to understand the relationship between variables. I found that the duration variable did not have any significant correlation with the landing distance so eliminated it. Also found that the Speed variables had a high correlation.
- Regression Modelling: Developed a linear regression model with the selected variables to predict the landing distance. Found that the r-squared value was inflated due to the correlated speed variables. Identified the magnitude of correlation by using the VIF and Tolerance metrics and thus eliminated Speed\_air from the analysis as it had a large correlation with the Speed\_ground and also because the variable had close to 641 missing values. Modelled the landing distance again by compensating for the multi collinearity and got a decent predicting model with an r-squared close to .85.

Finally, I can see from the regression analysis that the factors like Speed\_ground, No\_pasg, pitch, Height and type of aircraft impact the landing distance.

Out of all the predictors, I find that Speed\_gound, pitch, height and type of aircraft are the factors majorly affecting the landing distance. Factors like no\_pasg has comparatively lesser impact on the landing distance.

## CHAPTER: 1 DATA PREPARATION AND CLEANING

## 1.1. DATA PREPARATION

Since we have the data files in the xlsx files, we first create a library called "Proj1SC" on the SAS Server (SAS on Demand for Analytics). Then import the xls files as SAS datafiles.

# 1.1.1. IMPORTING THE DATA

**CODE:** 

FILENAME REFFILE '/home/lalgudrn0/StatsComputing\_Project/FAA1.xls';

PROC IMPORT DATAFILE=REFFILE

DBMS=XLS OUT=PROJ1SC.FAA1; GETNAMES=YES;

RUN;

PROC CONTENTS DATA=PROJ1SC.FAA1; RUN;

Output Description for FAA1 file:

|   | Alph         | abetic L | let of \ | /arlables ar | nd Attribute | 8            |
|---|--------------|----------|----------|--------------|--------------|--------------|
| # | Variable     | Туре     | Len      | Format       | Informat     | Label        |
| 1 | aircraft     | Char     | 7        | \$7.         | \$7.         | aircraft     |
| 8 | distance     | Num      | 8        | BEST12.      |              | distance     |
| 2 | duration     | Num      | 8        | BEST12.      |              | duration     |
| 6 | height       | Num      | 8        | BEST12.      |              | height       |
| 3 | no_pasg      | Num      | 8        | BEST8.       |              | no_pasg      |
| 7 | pitch        | Num      | 8        | BEST12.      |              | pitch        |
| 5 | speed_air    | Num      | 8        | BEST12.      |              | speed_air    |
| 4 | speed ground | Num      | 8        | BEST13.      |              | speed ground |

FILENAME REFFILE '/home/lalgudrn0/StatsComputing\_Project/FAA2.xls';

PROC IMPORT DATAFILE=REFFILE

DBMS=XLS OUT=PROJ1SC.faa2; GETNAMES=YES;

RUN:

PROC CONTENTS DATA=PROJ1SC.faa2; RUN;

Output Description for FAA2 file:

|   | Alph         | abetic L | let of \ | /arlables ar | nd Attribute | 8            |
|---|--------------|----------|----------|--------------|--------------|--------------|
| # | Variable     | Туре     | Len      | Format       | Informat     | Label        |
| 1 | aircraft     | Char     | 7        | \$7.         | \$7.         | aircraft     |
| 7 | distance     | Num      | 8        | BEST12.      |              | distance     |
| 5 | height       | Num      | 8        | BEST12.      |              | height       |
| 2 | no_pasg      | Num      | 8        | BEST8.       |              | no_pasg      |
| 6 | pitch        | Num      | 8        | BEST12.      |              | pitch        |
| 4 | speed_air    | Num      | 8        | BEST12.      |              | speed_air    |
| 3 | speed_ground | Num      | 8        | BEST13.      |              | speed_ground |

#### 1.1.2. MERGING THE DATAFILES

The first step here is to merge the data files we have:

```
CODE:
data Proj1SC.merged;
set Proj1SC.faa1 Proj1SC.faa2;
run;
```

We would like to see how the data looks. Mainly with respect to the missing values.

#### CODE

```
proc means data = proj1sc.merged N Nmiss;
run;
```

#### **Output:**

| Variable     | Label        | N   | N Miss |
|--------------|--------------|-----|--------|
| duration     | duration     | 800 | 200    |
| no pasq on   | no pasq      | 950 | 50     |
| speed ground | speed ground | 950 | 50     |
| speed air    | speed air    | 239 | 761    |
| height       | height       | 950 | 50     |
| pitch        | pitch        | 950 | 50     |
| distance     | distance     | 950 | 50     |

As we can see, there are 1000 rows of data if we simply merge the files using concatenation technique. We want to remove the observations where there are no values at all. There are 50 such observations. We can do that by using one of the variables that is present in all rows. Using the variable "aircraft" to delete the observations, we can get this done.

#### **CODE:**

## 1.1.3. REMOVING DUPLICATES:

We find that there are a lot of duplicates in the dataset after merging. We need to remove those duplicates.

proc sort data = proj1sc.remove\_empty\_rows out= proj1sc.final nodupkey;

by aircraft no\_pasg speed\_ground speed\_air height pitch distance;

run;

proc print data = proj1sc.final; run;

#### 1.1.4. COMPUTING MISSING VALUES IN THE MERGED DATA SET:

#### CODE:

proc means data = proj1sc.final N NMISS; run;

| Variable     | Label        | N   | N Miss |  |
|--------------|--------------|-----|--------|--|
| duration     | duration     | 800 | 50     |  |
| no_pasg      | no_pasg      | 850 | 0      |  |
| speed ground | speed ground | 850 | 0      |  |
| speed_air    | speed air    | 208 | 642    |  |
| height       | height       | 850 | 0      |  |
| pitch        | pltch        | 850 | 0      |  |
| distance     | distance     | 850 | 0      |  |

We have now removed the duplicate rows from the data files and we find that the merged dataset has 850 observations.

## 1.2. DATA EXPLORATION

# 1.2.1. COMPUTING FOR THE ABNORMAL AND MISSING VALUES IN VARIABLES:

## 1. Aircraft type

proc freq data = proj1sc.final; table aircraft /nocum nopercent nofreq; where aircraft is missing; run;

*Inference*: We find that there are no missing values in the aircraft column.

## 2. Duration:

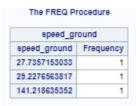
proc freq data = proj1sc.final; table duration /nocum nopercent nofreq; where duration < 40 or duration is missing; run;



*Inference*: We find that there are 5 abnormal values and 50 missing values with respect to the Duration variable.

#### 3. Speed Ground:

```
proc freq data = proj1sc.final;
table speed_ground /nocum nopercent nofreq;
where speed_ground < 30 or speed_ground >140 or speed_ground is missing;
run;
```



*Inference*: There are no missing values in Speed\_ground column but there are 3 observations with abnormal data values in it.

#### 4. Speed Air:

proc freq data = proj1sc.final; table speed\_air /nocum nopercent nofreq; where speed\_air < 30 or speed\_ground >140 or speed\_air is missing; run:



*Inference*: There are 642 missing values in Speed\_Air column and there is 1 observation with abnormal data values in it.

#### 5. Height:

proc freq data = proj1sc.final; table height /nocum nopercent nofreq; where height < 6 or height is missing; run;



*Inference*: There are no missing values in height column but there are 10 observations with abnormal data values in it.

#### **6.** Distance:

```
proc freq data = proj1sc.final;
table distance /nocum nopercent nofreq;
where distance >6000 or distance is missing or distance < 0;
run;
```



*Inference*: There are no missing values in distance column but there are 2 observations with abnormal data values in it.

#### 1.3. DATA CLEANING

## 1.3.1. DEALING WITH MISSING VALUES

Since we can see that for the variable *Speed\_*air there are 642 missing values, we cannot just delete all the observations with missing values in the dataset. We would like to explore options to find out if there is any way we can compensate for the missing observations. The possible approximations we tried and their consequences are summarized below:

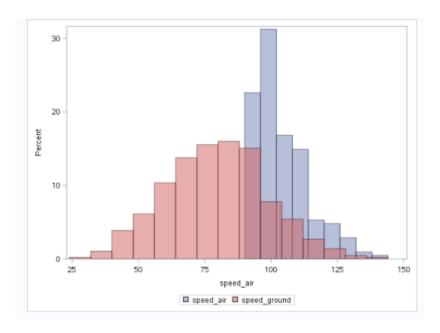
#### 1.3.1.1. EXPLORING THE DISTRIBUTION OF SPEED AIR

We want to understand the distribution of Speed\_air and see if we use Speed\_ground to make approximations for the Speed\_air values in the missing observations:

When we try plotting the records for Speed\_air and Speed\_ground, we get the following distribution:

#### CODE:

proc sgplot data = proj1sc.final; histogram speed\_air /transparency=0.5; histogram speed\_ground /transparency=0.5; run;



As we can see, the values of Speed\_Air are present only above a value of 90. But after the values appear, we can see that the distribution of Speed\_air overlaps with the distribution of Speed\_ground. This might be because the sensors measuring speed\_air are calibrated to operate only of the value is greater than 90. So, we cannot delete the observations with a value of NULL for Speed\_Air as we might be missing out on a lot of details by doing that.

#### 1.3.1.2. USING AVERAGES FOR MISSING OBSERVATIONS

We can maybe replace the missing values with the averages, but as we can see in the distribution, we do not want to make assumptions for variables at the beginning of the project.

## 1.3.2. DEALING WITH ABNORMAL VALUES

We find that the data has very few abnormal values which might skew our predictions if we use them for building a predictive model using them. But we just cannot get rid of the abnormal values. So we can store them in a Separate Dataset called "Abnormal\_Flight". We might want to use them later in our analysis.

```
NOTE: There were 21 observations read from the data set PROJISC.ABNORMAL. NOTE: 2 observations with duplicate key values were deleted.
```

But for our analysis for now, we use a data set that does not contain any abnormal values in it. By cleaning the data set of the abnormal value, we have a data set with 831 observations.

```
NOTE: There were 831 observations read from the data set PROJISC.CLEAN_5.

NOTE: The data set PROJISC.FLIGHTCLEANED has 831 observations and 8 variables.
```

## 1.4. OBSERVATIONS

In the cleaned data set that we have now, we would like to understand how that variables are distributed.

1. Let us understand how many missing values we have in the dataset:

#### CODE:

proc means data= proj1sc.FLIGHTCLEANED N NMISS; RUN;

| Variable     | Label        | N   | N MIss |
|--------------|--------------|-----|--------|
| duration     | duration     | 781 | 50     |
| no_pasg      | no_pasg      | 831 | 0      |
| speed ground | speed ground | 831 |        |
| speed air    | speed air    | 203 | 628    |
| height       | height       | 831 |        |
| pitch        | pitch        | 831 |        |
| distance     | distance     | 831 |        |

We find that in all we have 831 observations for the 8 variables.

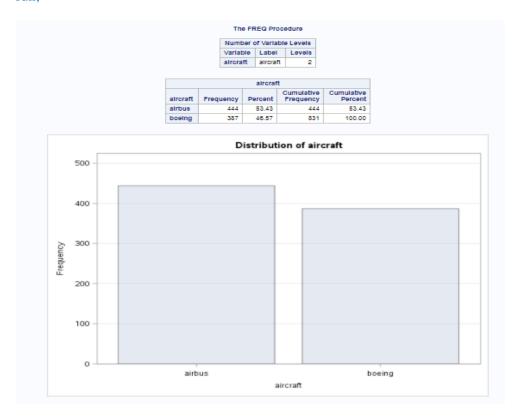
2. Now let us analyse at the variable level:

The aircraft column is of categorical type, so we use the FREQ function to estimate a frequency plot to understand the distribution of the variable.

#### CODE:

proc freq data = proj1sc.clean\_5 NLevels; table aircraft/plots = freqplot;

run;



All other variables are continuous, so we would like to perform a univariate analysis to understand the variables characteristics. But since a univariate analysis might give us a lot of

information about the measure of central tendency and spread of the variable, we can use a MEANS procedure to get a basic understanding of all the variables.

#### CODE:

proc means data= proj1sc.FLIGHTCLEANED mean stddev median q1 q3 min max; var no\_pasg speed\_ground speed\_air height pitch distance duration; run:

| Variable     | Label        | Mean        | Std Dev     | Median      | Lower Quartile | Upper Quartile | Minimum    | Maximum    |  |  |  |  |
|--------------|--------------|-------------|-------------|-------------|----------------|----------------|------------|------------|--|--|--|--|
| no_pasg      | no_pasg      | 60.0553550  | 7.4913166   | 60.0000000  | 55.0000000     | 65.0000000     | 29.0000000 | 87.0000000 |  |  |  |  |
| speed ground | speed ground | 79.5426997  | 18.7356754  | 79.7939604  | 66.1925304     | 91.9496075     | 33.5741041 | 132.784676 |  |  |  |  |
| apeed air    | speed air    | 103.4850352 | 9.7362774   | 101.1189240 | 96.1964606     | 109.3823005    | 90.0028586 | 132.911464 |  |  |  |  |
| height       | height       | 30.4578695  | 9.7848114   | 30.1670844  | 23.5298692     | 37.0143018     | 6.2275178  | 59.945963  |  |  |  |  |
| pitch        | pitch        | 4.0051609   | 0.5265690   | 4.0010380   | 3.6403979      | 4.3710717      | 2.2844801  | 5.926784   |  |  |  |  |
| distance     | distance     | 1522.48     | 896.3381524 | 1262.15     | 892.9839743    | 1937.26        | 41.7223127 | 5381.9     |  |  |  |  |
| duration     | duration     | 154.7757191 | 48.3499237  | 154.2845505 | 119.6314577    | 189.6629425    | 41.9493694 | 305.621710 |  |  |  |  |

3. Since the major problem statement focuses on the landing Distance, lets focus on understanding the distribution of the landing distance which can be useful in the analysis going forward.

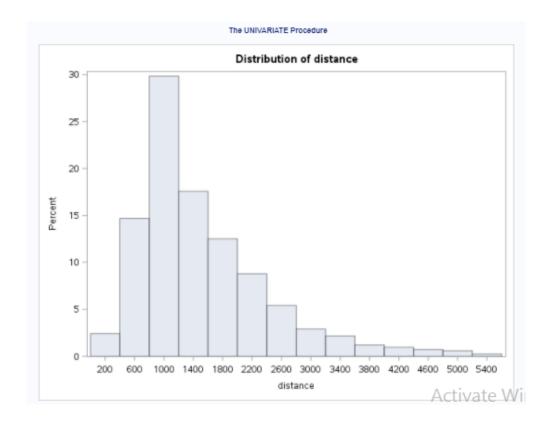
#### CODE:

proc univariate data = proj1sc.FLIGHTCLEANED;

var distance;

Histogram distance;

run;



## CHAPTER: 2 RELATIONSHIP BETWEEN VARIABLES

Now that we have cleaned the dataset, we would now like to understand the impact of every factor on the Distance variable using linear regression modelling.

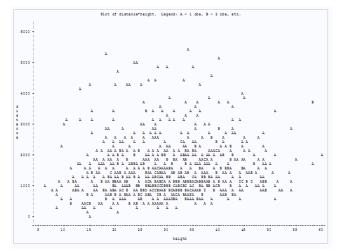
## **2.1. X-Y PLOTS:**

First, let us try plotting the distribution of Distance with respect to some of the variables we have in our data set.

## 2.1.1. DISTANCE VS HEIGHT

CODE

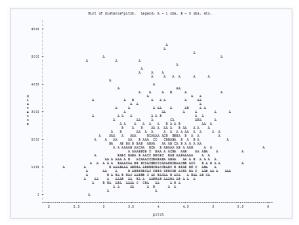
proc plot data = proj1sc.FLIGHTCLEANED;
plot distance\*height;
run;



Looking at the graph, we are not able to make any inference about the relationship between distance and height.

## 2.1.2. DISTANCE VS PITCH

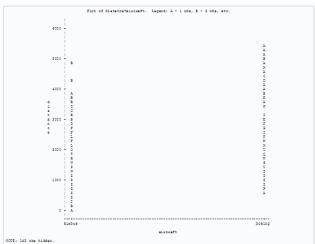
proc plot data = proj1sc.FLIGHTCLEANED;
plot distance\*pitch;
run;



Looking at the graph, we are not able to make any inference about the relationship between distance and pitch.

## 2.1.3. DISTANCE VS TYPE OF AIRCRAFT

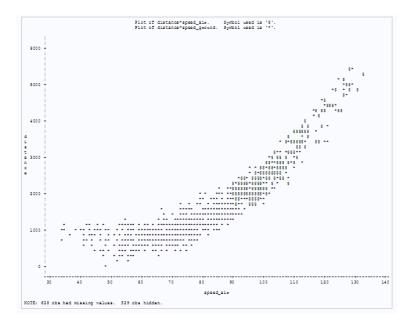
proc plot data = proj1sc.FLIGHTCLEANED;
plot distance\*aircraft;
run;



Looking at the graph, we can say that the distribution of distance between the two types of aircrafts is slightly different. So, this variable might have an impact on the prediction of landing distance.

## 2.1.4. DISTANCE VS SPEED VARIABLES

proc plot data = proj1sc.FLIGHTCLEANED; plot distance\*speed\_air = "\$" distance\*speed\_ground = "\*" / overlay; run;



Looking at the graph, we can see that the Speed\_air and Speed\_ground almost has the same relationship with the distance variable but the value of speed\_air starts only after a value of

90. One take away from the graph is that both the speed variables might be useful in predicting the landing distance.

#### 2.2. CORRELATION ANALYSIS:

Next step would be to run a correlation analysis on the data set to identify the significant variable to be considered for the prediction of distance.

#### 2.2.1. CODING THE CATEGORICAL VARIABLE

Now to run a correlation analysis, firstly let us convert the categorical variable aircraft into numeric values. Only then we will be able to run a regression analysis.

```
/* Convert the categorical variable into a numerical condition */
data proj1sc.Flight;
set proj1sc.flightcleaned;
if (aircraft = "boeing") then type = 0;
else type = 1;
drop aircraft;
run;
```

#### 2.2.2. PAIRWISE CORRELATION BETWEEN ALL VARIABLES

COMPUTING PAIRWISE CORRELATION:

proc corr data = proj1sc.flight;
var distance type no\_pasg Speed\_air Speed\_ground height pitch duration;
title "Pairwise Correlation";
run;

|                              |                           |                           | Prob >                    | orrelation Co<br> r  under H0:<br>er of Observa | Rho=0                     |                           |                           |                           |
|------------------------------|---------------------------|---------------------------|---------------------------|---|---------------------------|---------------------------|---------------------------|---------------------------|
|                              | distance                  | type                      | no_paeg                   | apeed_air                                       | speed_ground              | height                    | pitch                     | duration                  |
| distance<br>distance         | 1.00000                   | -0.23814<br><.0001<br>831 | -0.01776<br>0.6093<br>831 | 0.94210<br><.0001<br>203                        | 0.86624<br><.0001<br>831  | 0.09941<br>0.0041<br>831  | 0.08703<br>0.0121<br>831  | -0.05138<br>0.1514<br>781 |
| type                         | -0.23814<br><.0001<br>831 | 1.00000                   | 0.02269<br>0.5136<br>831  | 0.07207<br>0.3069<br>203                        | 0.04045<br>0.2441<br>831  | 0.01439<br>0.6788<br>831  | -0.35420<br><.0001<br>831 | 0.04443<br>0.2149<br>781  |
| no_pasg<br>no_pasg           | -0.01776<br>0.6093<br>831 | 0.02269<br>0.5136<br>831  | 1.00000                   | -0.00616<br>0.9305<br>203                       | -0.00013<br>0.9969<br>831 | 0.04699<br>0.1760<br>831  | -0.01793<br>0.6057<br>831 | -0.03639<br>0.3098<br>781 |
| speed_air<br>speed_air       | 0.94210<br><.0001<br>203  | 0.07207<br>0.3069<br>203  | -0.00616<br>0.9305<br>203 | 1.00000   | 0.98794<br><.0001<br>203  | -0.07933<br>0.2606<br>203 | -0.03927<br>0.5780<br>203 | 0.04454<br>0.5364<br>195  |
| speed_ground<br>speed_ground | 0.86624<br><.0001<br>831  | 0.04045<br>0.2441<br>831  | -0.00013<br>0.9969<br>831 | 0.98794<br><.0001<br>203                        | 1.00000<br>831            | -0.05761<br>0.0970<br>831 | -0.03912<br>0.2599<br>831 | -0.04897<br>0.1716<br>781 |
| height<br>height             | 0.09941<br>0.0041<br>831  | 0.01439<br>0.6788<br>831  | 0.04699<br>0.1760<br>831  | -0.07933<br>0.2606<br>203                       | -0.05761<br>0.0970<br>831 | 1.00000                   | 0.02298<br>0.5082<br>831  | 0.01112<br>0.7564<br>781  |
| pitch<br>pitch               | 0.08703<br>0.0121<br>831  | -0.35420<br><.0001<br>831 | -0.01793<br>0.6057<br>831 | -0.03927<br>0.5780<br>203                       | -0.03912<br>0.2599<br>831 | 0.02298<br>0.5082<br>831  | 1.00000                   | -0.04675<br>0.1918<br>781 |
| duration<br>duration         | -0.05138<br>0.1514<br>781 | 0.04443<br>0.2149<br>781  | -0.03639<br>0.3098<br>781 | 0.04454<br>0.5364<br>195                        | -0.04897<br>0.1716<br>781 | 0.01112<br>0.7564<br>781  | -0.04675<br>0.1918<br>781 | 1.00000<br>781            |

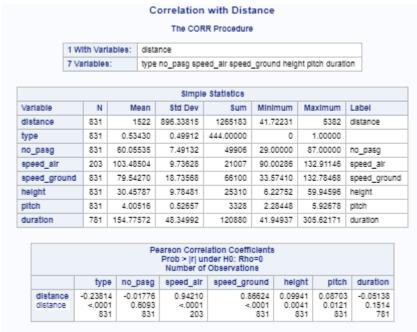
We find that the variables Speed\_air and Speed\_ground are highly correlated by the order of 98.7%. While building the model we surely need to consider their impact on inflating the predictions due to this multicollinear relationship.

#### 2.2.3. CORRELATION OF VARIABLES WITH THE DISTANCE VARIABLE

The major area of interest is in understanding the correlation of all the variables to the distance variable.

## **CORRLATION WITH DISTANCE:**

proc corr data = proj1sc.flight;
var type no\_pasg Speed\_air Speed\_ground height pitch duration;
with distance;
title "Correlation with Distance";
run;



We find that excepting the duration variable, all other variables have a significant correlation with the distance variable at 95% confidence level. Since the NULL hypothesis that rho = 0 for the distance variable cannot be rejected, we can leave the duration variable from our analysis.

## CHAPTER: 3 REGRESSION MODELLING

#### 3.1. CONSTRUCTING A MODEL WITH ALL VARIABLES

proc reg data = proj1sc.flight; model distance = type no\_pasg Speed\_air Speed\_ground height pitch; title "Regression Analysis of the Flight Dataset"; run;

|               |        | De        |               | Mod                                | EG Proc<br>el: MOD<br>able: dis | EL1  |               | ance              |       |         |       |
|---------------|--------|-----------|---------------|------------------------------------|---------------------------------|------|---------------|-------------------|-------|---------|-------|
|               |        | Number    | of Obse       | servations Read<br>servations Used |                                 |      |               |                   | 831   |         |       |
|               |        | Number o  | of Obse       |                                    |                                 |      |               |                   | 203   | 3       |       |
|               |        | Number    | of Obse       | rvatio                             | na with i                       | Miss | eing Va       | lues              | 628   | 3       |       |
|               |        |           |               |                                    |                                 |      |               |                   |       |         |       |
|               |        |           |               | _                                  | la of Va                        | rlan | C9            |                   |       |         |       |
|               | Source | 9         | DF            | _                                  |                                 |      | Mean<br>quare | F                 | /alue | Pr > F  |       |
|               | Model  |           | 6             | 1329                               | 51503 221                       |      | 58584         | 12                | 35.07 | <.0001  |       |
|               | Error  |           | 196           | 35                                 | 3516465                         |      | 17941         |                   |       |         |       |
|               | Correc | ted Total | 202           | 1364                               | 57968                           |      |               |                   |       |         |       |
|               |        | Roof MSF  |               |                                    | 33.94451                        |      | 2 0 0 0 0     |                   | 0.974 |         |       |
|               |        |           | ependent Mean |                                    |                                 |      |               | J R-Sq 0.9734     |       |         |       |
|               |        | Coeff Var |               |                                    | 74.67289 Ac<br>4.82740          |      | auj IX-a      |                   |       | -       |       |
|               | -      | 00011 141 |               |                                    | 4.02.74                         |      |               |                   |       |         |       |
|               |        |           | F             | arame                              | eter Esti                       | mat  | 98            |                   |       |         |       |
| Variable Labe |        | Label     | Label         |                                    | Parameter<br>Estimate           |      |               | Standard<br>Error |       | t Value | Pr>   |
| Interce       | ept    | Intercep  | ot            | 1                                  | -5804.                          | 2696 | 57 15         | 6.63              | 260   | -37.06  | <.000 |
| type          |        |           |               | 1                                  | -426                            | 8912 | 21 2          | 0.32              | 755   | -21.00  | <.000 |
| no_pa         | eg .   | no_pas    | 9             | 1                                  | -2.                             | 2990 | 22            | 1.34              | 357   | -1.71   | 0.088 |
| speed         | air    | speed_a   | air           | 1                                  | 88.                             | 0398 | 51            | 6.31              | 100   | 13.95   | <.000 |
| speed         | ground | speed_c   | ground        | 1                                  | -5.                             | 8978 | 52            | 6.22              | 131   | -0.95   | 0.344 |
| helght        |        | height    |               | 1                                  | 13.                             | 628  | 37            | 1.00              | 747   | 13.53   | <.000 |
|               |        |           |               | 1                                  |                                 | 6575 |               | 8.00              |       | -0.26   | 0.796 |

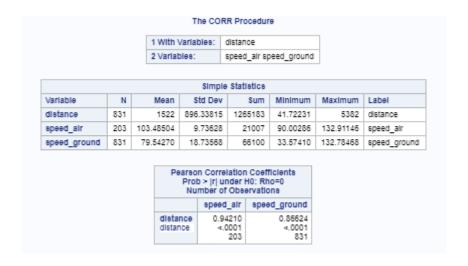
## 3.2. ANALYSIS OF RESULTS

When we try interpreting the results, we find the following two conditions:

- 1. The model has used only 203 observations out of the 831 observations in the data set. This is due to the missing values in Speed\_air variable.
- 2. We also find that despite both the speed variables having a large positive correlation with the distance, we are seeing that one of the speed variables is having a negative coefficient in the regression model which is counter intuitve. This might be due to the correlation between the speed variables. We need to explore the effect of multi collinearity on the regression model.

#### DISTANCE VS SPEED VARIABLES

proc corr data = proj1sc.flight; var speed\_air speed\_ground; with distance; run;



#### 3.3. COMPUTING VIF AND TOLERANCE:

proc reg data = proj1sc.flight;
model distance = type no\_pasg Speed\_air Speed\_ground height pitch /vif tol;
title "Regression Analysis of the Flight Dataset";
run;

|              |              |    | Paramete              | r Estimates       |         |         |           |                       |
|--------------|--------------|----|-----------------------|-------------------|---------|---------|-----------|-----------------------|
| Variable     | Label        | DF | Parameter<br>Estimate | Standard<br>Error | t Value | Pr >  t | Tolerance | Variance<br>Inflation |
| Intercept    | Intercept    | 1  | -5804.26967           | 156.63260         | -37.06  | <.0001  |           | 0                     |
| type         |              | 1  | -426.89121            | 20.32755          | -21.00  | <.0001  | 0.87877   | 1.13795               |
| no_paeg      | no_pasg      | 1  | -2.29922              | 1.34357           | -1.71   | 0.0886  | 0.99609   | 1.00392               |
| speed_air    | speed_air    | 1  | 88.03951              | 6.31100           | 13.95   | <.0001  | 0.02352   | 42.50919              |
| speed_ground | speed_ground | 1  | -5.89752              | 6.22131           | -0.95   | 0.3443  | 0.02345   | 42.63875              |
| height       | height       | 1  | 13.62837              | 1.00747           | 13.53   | <.0001  | 0.98610   | 1.01409               |
| pitch        | pitch        | 1  | -4.65754              | 18.00975          | -0.26   | 0.7962  | 0.86989   | 1.14956               |

We know that, tolerance (requested by the tol option) is the proportion of variance in a given predictor that is NOT explained by all of the other predictors, while the VIF (or Variance Inflation Factor) is simply 1 / tolerance. The VIF represents a factor by which the variance of the estimated coefficient is multiplied due to the multicollinearity in the model

A good "global" check for a multicollinearity problem is to see if the largest condition index is greater than 30.

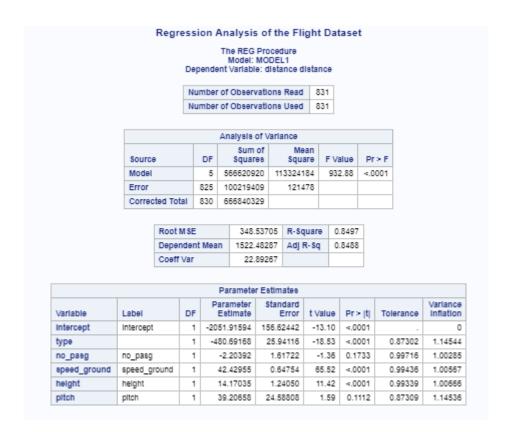
Here we find that the VIF is 42 for both the speed variables. So, we need to eliminate one of those variables to get a proper fit to the model. We also know that the speed\_air variable has 641 missing values. It is always better to fit a model with more data than less. So we can eliminate Speed\_air from our model and construct the linear regression equation.

#### 3.4. MODEL COMPENSATED FOR MULTICOLLINEARITY

/\* Final Model \*/

proc reg data = proj1sc.flight;

model distance = type no\_pasg Speed\_ground height pitch /vif tol; title "Regression Analysis of the Flight Dataset"; run;



We have the following observations:

- The model is based on all the 831 observations present in the cleaned dataset.
- Type of aircraft has a major impact on the landing distance with a coefficient of the order of 480. Which means the type of aircraft affects the landing distance by a factor of 480.
- Factors like Speed\_Ground, Height and Pitch have a positive impact on the landing distance
- The no\_pasg has a negative impact on the landing distance but the magnitude of impact is small compared to other factors

#### 3.5. JUSTIFICATION FOR VARIABLE SELECTIONS

As per the results we got in our process of understanding the variables, we made two choices with respect to the variable:

- 1. Eliminated duration variable from the list as we found that the NULL Hypothesis for rho=0 couldn't be rejected for the relationship between duration and distance
- 2. We eliminated speed\_air variable to compensate for the multicollinearity issue we had on the model due to the correlation between speed\_air and speed\_ground. We chose to eliminate speed\_air among the two variables because it has a lot of missing values and we would always want to use more data for developing the model.

#### **QUESTIONS:**

# 1. How many observations (flights) do you use to fit your final model? If not all 950 flights, why?

We used 831 observations from the data set after getting rid of the abnormal observations. Also, we have made variable selections to make sure our model is robust and is not overfitting the given dataset.

# 2. What factors and how they impact the landing distance of a flight?

We can see from the regression analysis that the factors like Speed\_ground, No\_pasg, pitch, Height and type of aircraft impact the landing distance.

Out of all the predictors, we find that Speed\_gound, pitch, height and type of aircraft are the factors majorly affecting the landing distance. Factors like no\_pasg has comparatively lesser impact on the landing distance.

## 3. Is there any difference between the two makes Boeing and Airbus?

Yes, there is a difference in the landing distance between the two types of aircrafts. We tried understanding this by plotting the distributions of landing distance and the type of aircraft. Also in the regression model, we get a coefficient of the order of 480 which means that the type of aircraft would affect the landing distance by a factor of 480.

proc univariate data = proj1sc.FLIGHTCLEANED; class aircraft; histogram distance /overlay:

histogram distance /overlay;

run;

