# Homogeneous Spiking Neural P Systems with Structural Plasticity

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$$\Pi = (0, \sigma_1, \dots, \sigma_m, syn, out)$$

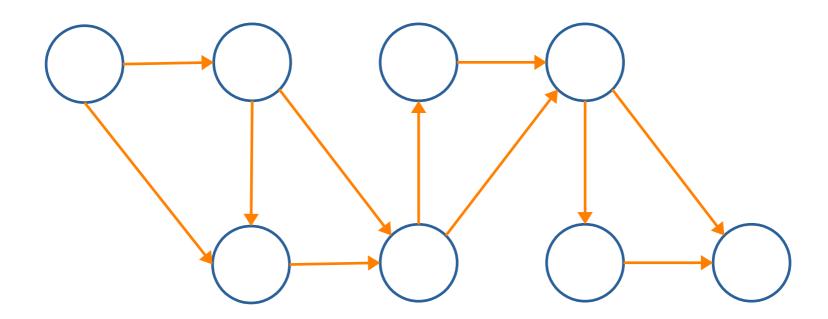
Neurons:  $\sigma_1, \dots, \sigma_m$ 





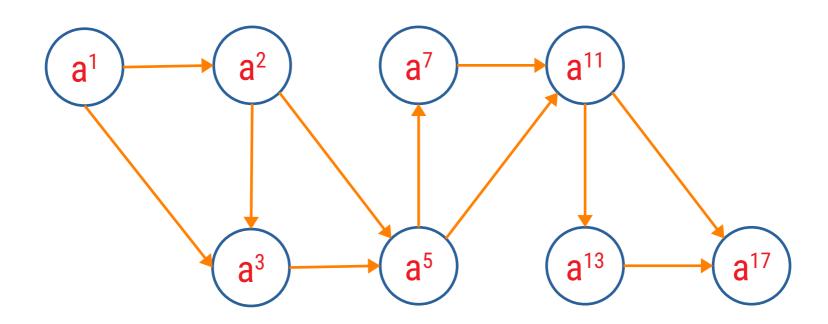
$$\Pi = (0, \sigma_1, \dots, \sigma_m, syn, out)$$

Synapses: syn



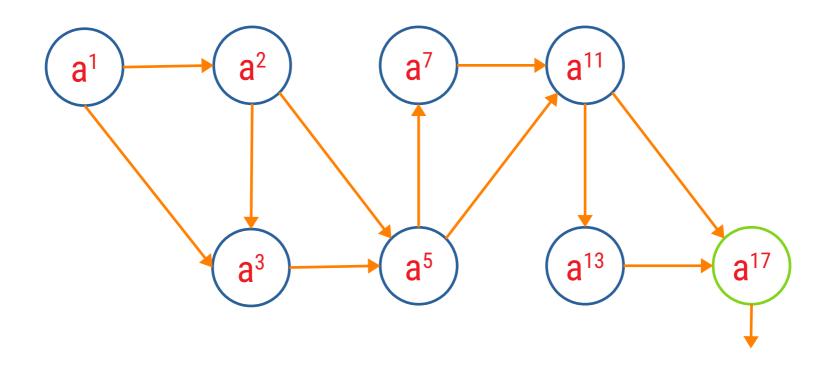
$$\Pi = (0, \sigma_1, \dots, \sigma_m, syn, out)$$

Spike: a Alphabet:  $O = \{a\}$  Multiset of Spikes:  $a^i$ 



$$\Pi = (0, \sigma_1, \dots, \sigma_m, syn, out)$$

Output Neuron: out



$$\Pi = (0, \sigma_1, ..., \sigma_m, syn, out)$$

Spiking Rule : E /  $a^c \rightarrow a$ 

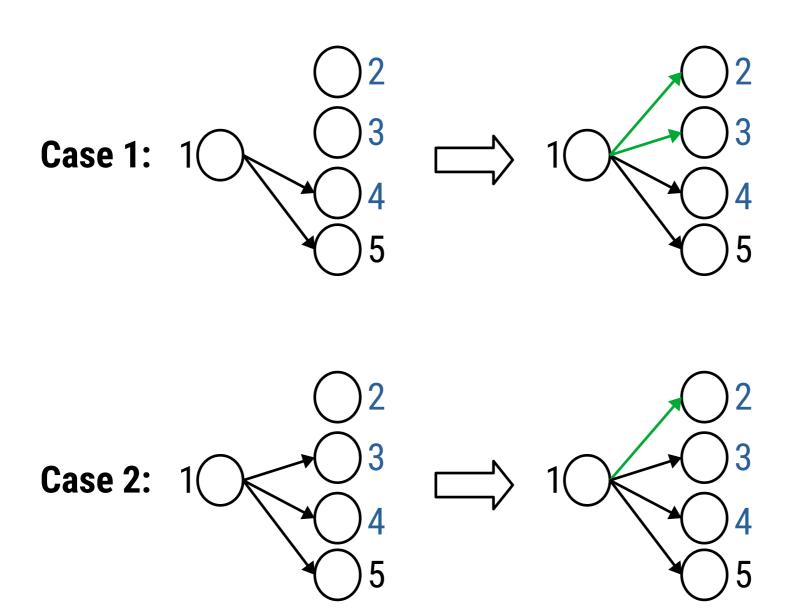
Plasticity Rule : E /  $a^c \rightarrow \alpha k(N)$ 

#### N – target neurons

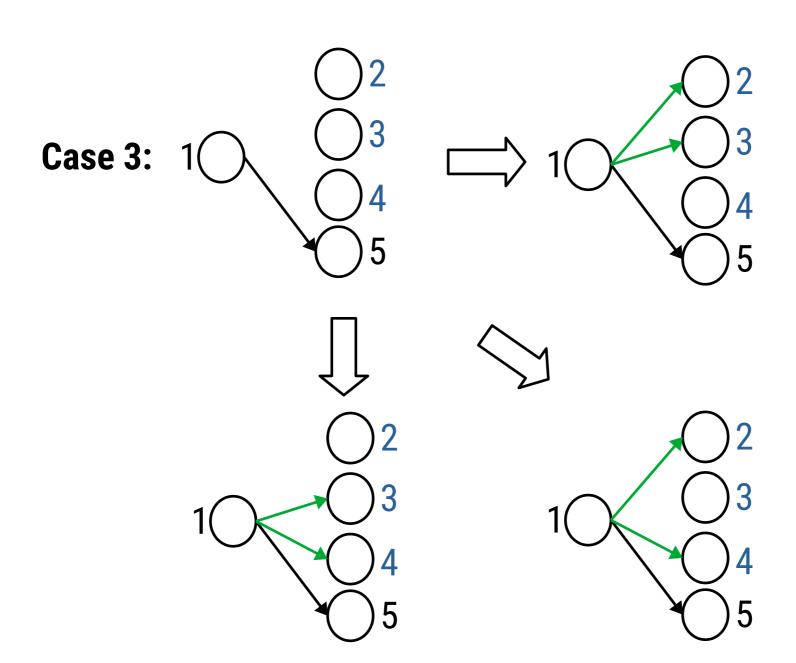
$$\alpha \in \{+, -, \pm, \mp\}$$

- +k add k synapses
- -k delete k synapses
- **±k** add then delete k synapses
- $\mp$  k delete then add k synapses

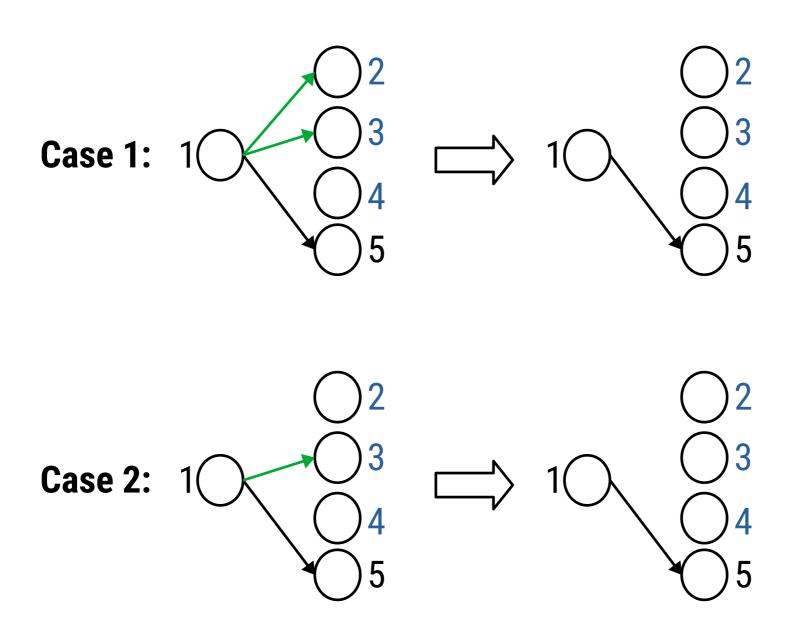
In neuron 1: E /  $a^c \rightarrow +2(\{2,3,4\})$ 



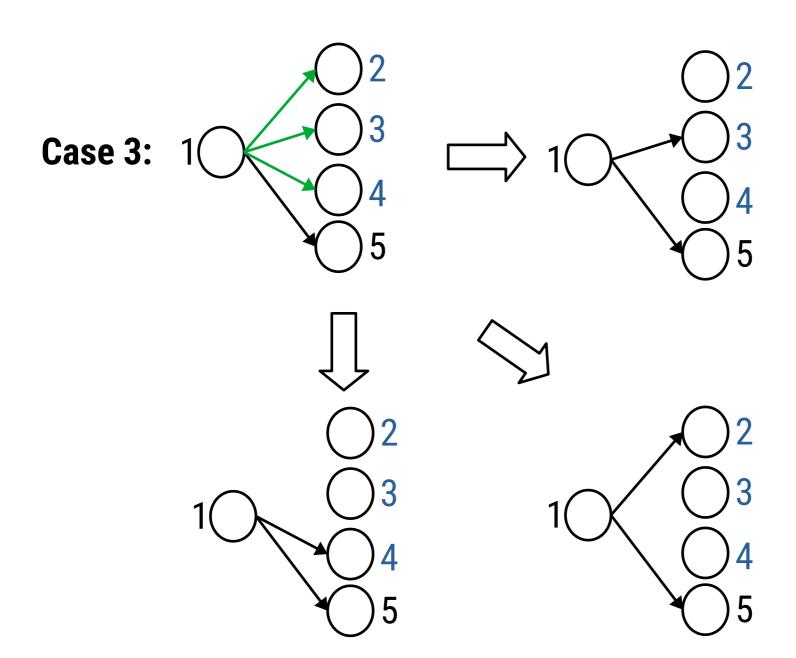
In neuron 1: E /  $a^c \rightarrow +2(\{2,3,4\})$ 



In neuron 1: E /  $a^c \rightarrow -2(\{2,3,4\})$ 

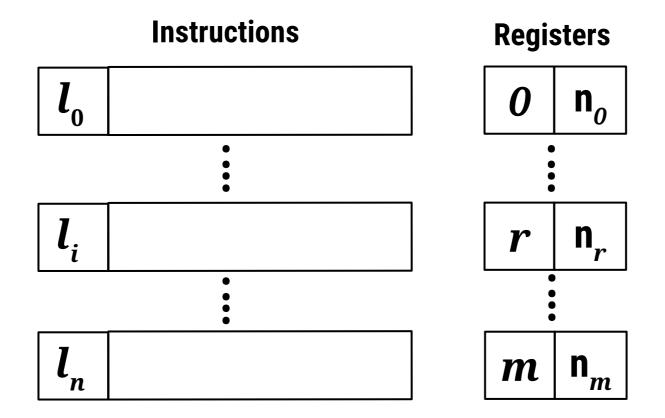


In neuron 1: E /  $a^c \rightarrow -2(\{2,3,4\})$ 

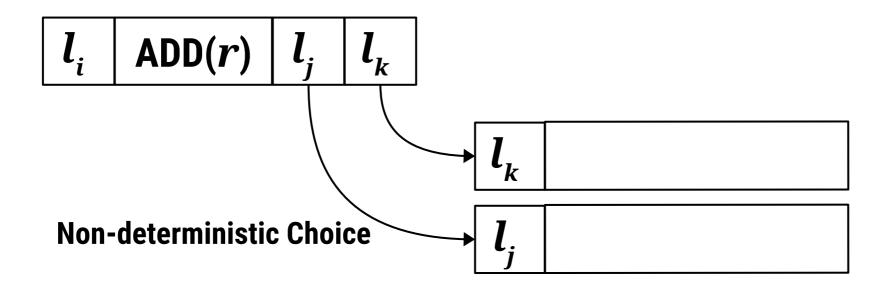


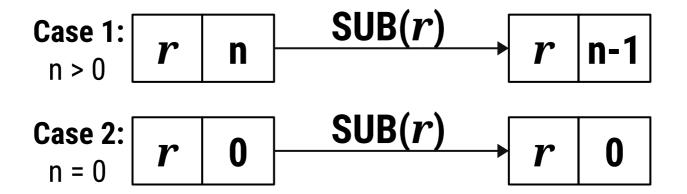
Plasticity rules as forgetting rules.

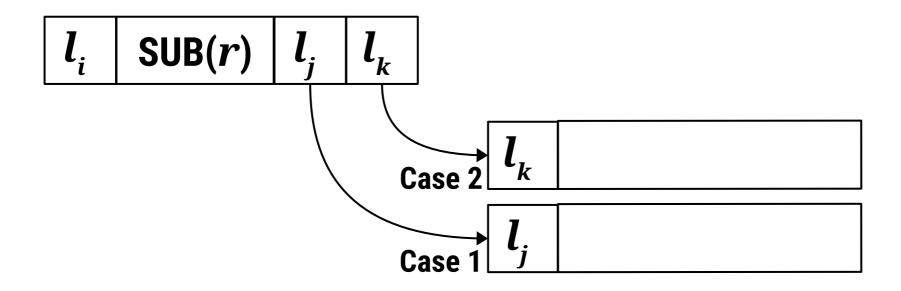
Case 1: 1 
$$\longrightarrow$$
 2 In neuron 1: E /  $a^c \rightarrow +1(\{2\})$ 











 $l_h$  Halt

#### **Representing Numbers**

n
Z + 3n
10<sup>n-1</sup>1

Number (in Register)
Spike Count
Spike Train

**Z** is some constant spike count.

#### **Common Rule Set for All Neurons**

Rule 0:  $a^{X+1}/a^1 \rightarrow \lambda$ 

Rule 1:  $a^{X+2}/a^2 \rightarrow \lambda$ 

Rule 2:  $a^{X+2}/a^2 \rightarrow a$ 

Rule 3:  $a^{Y+1}/a^1 \rightarrow \lambda$ 

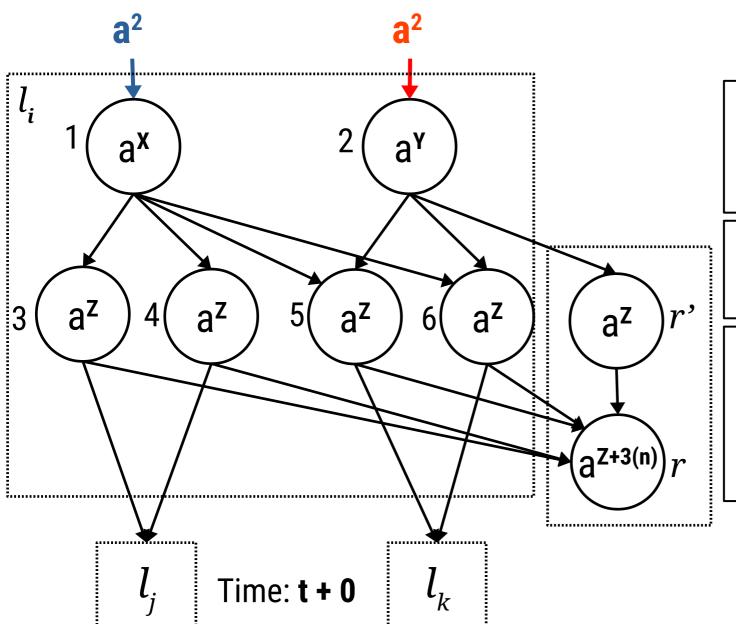
Rule 4:  $a^{Y+2}/a^2 \rightarrow a$ 

Rule 5:  $a^{Z+1}/a^1 \rightarrow a$ 

Rule 6:  $a^{Z+2}/a^2 \rightarrow \lambda$ 

Rule 7:  $a^{Z+1} (a^3)^+/a^4 \to \lambda$ 

 $l_i$  ADD(r)  $l_j$   $l_k$ 



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Rule 2:  $a^{X+2}/a^2 \rightarrow a$ 

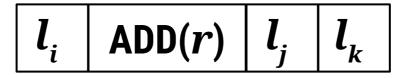
Rule 3:  $a^{Y+1}/a^1 \rightarrow \lambda$ 

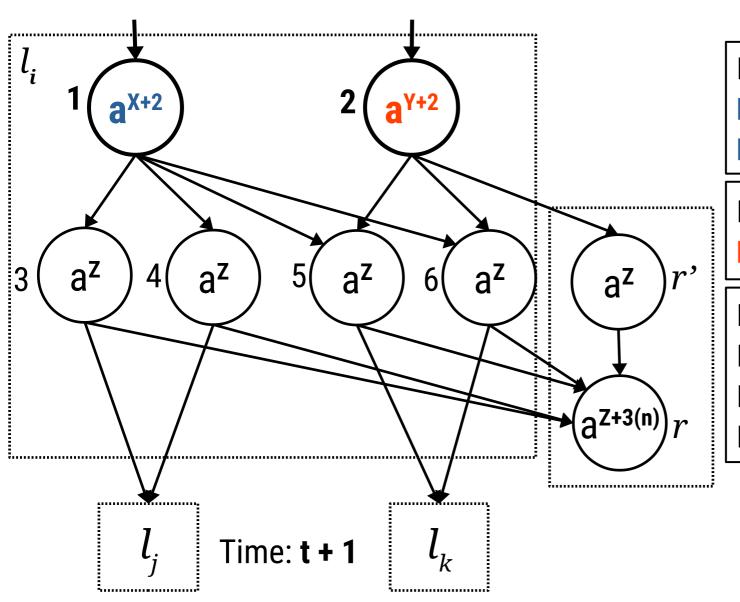
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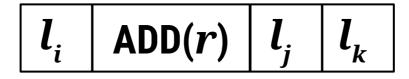
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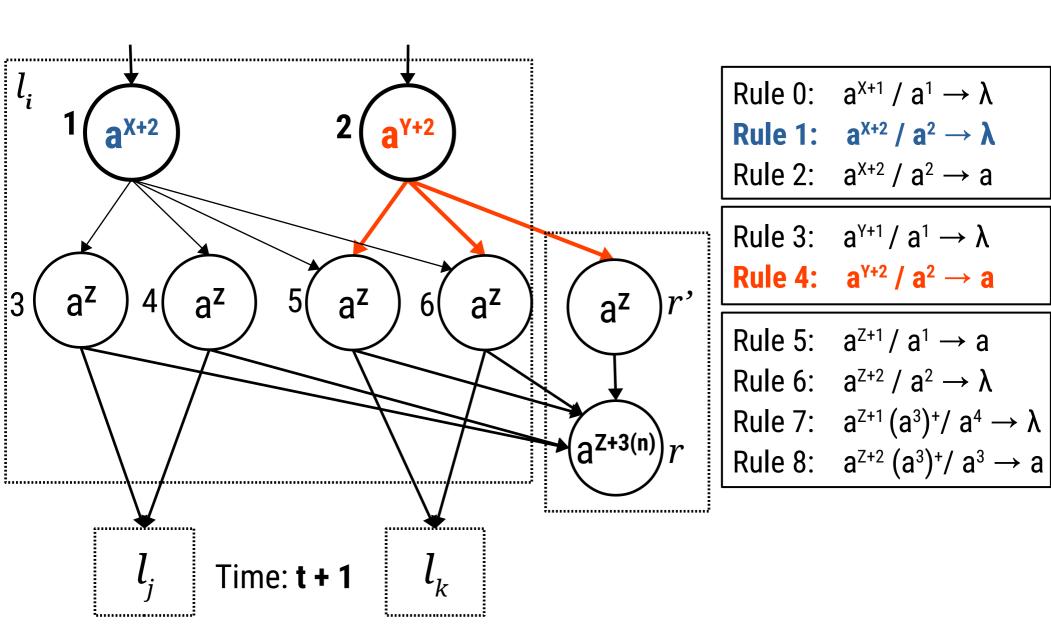
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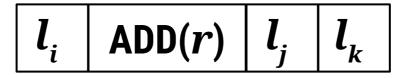
Rule 6:  $a^{Z+2}/a^2 \rightarrow \lambda$ 

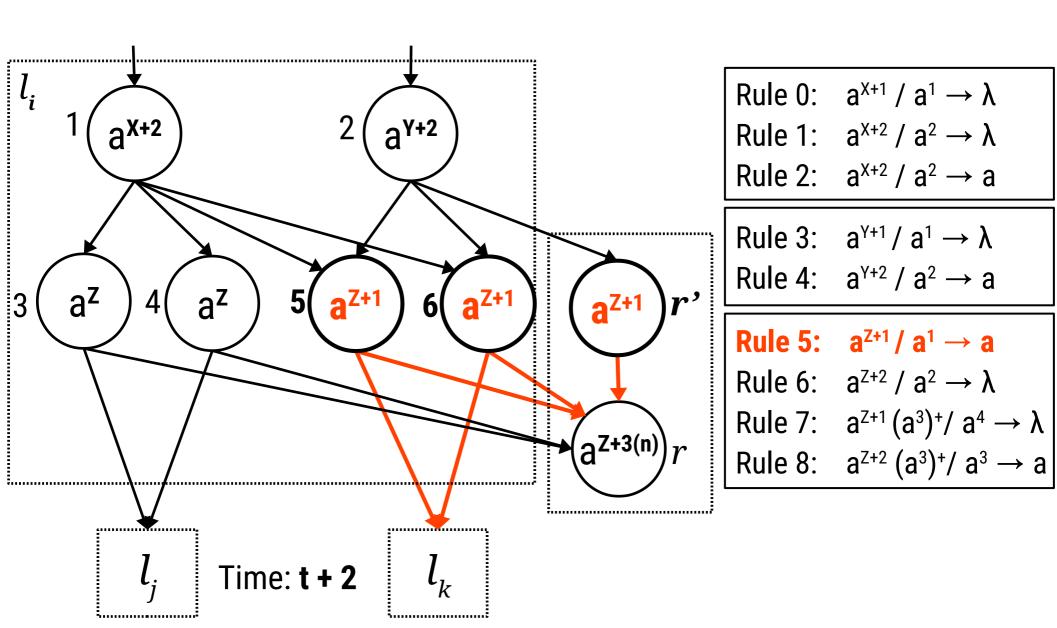
Rule 7:  $a^{Z+1}(a^3)^+/a^4 \to \lambda$ 



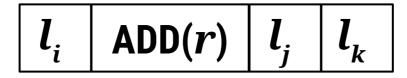


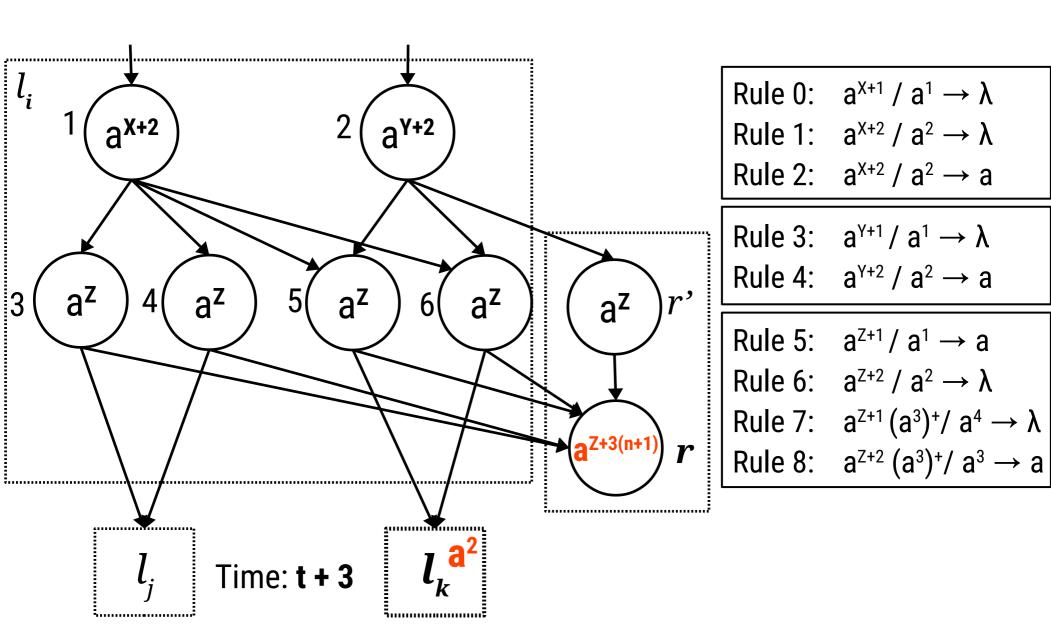
Case 1: Rule 1 is activated.



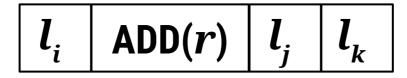


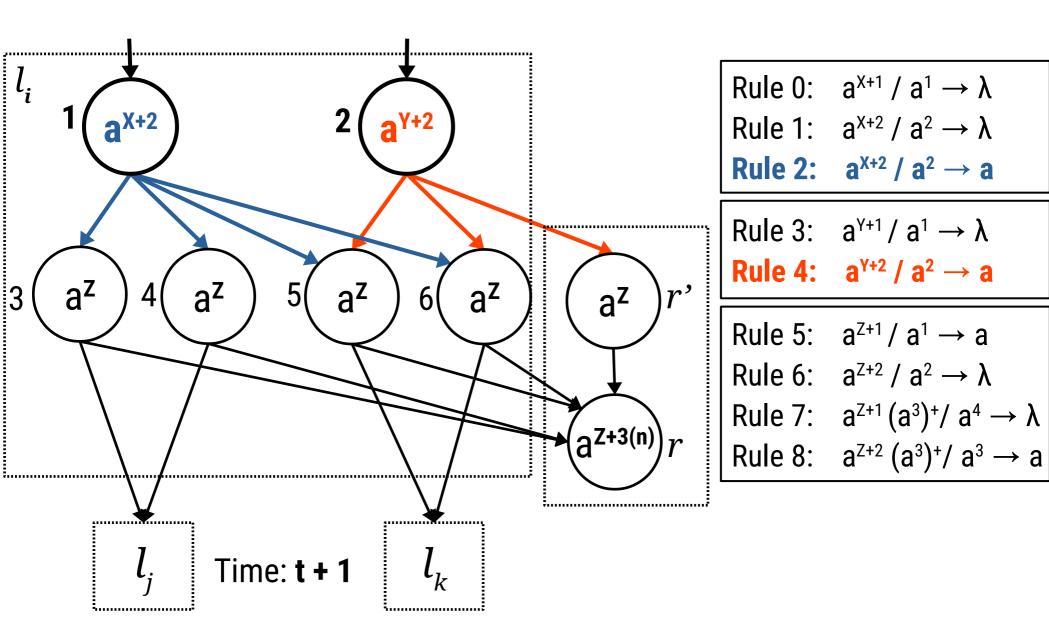
Case 1: Rule 1 is activated.





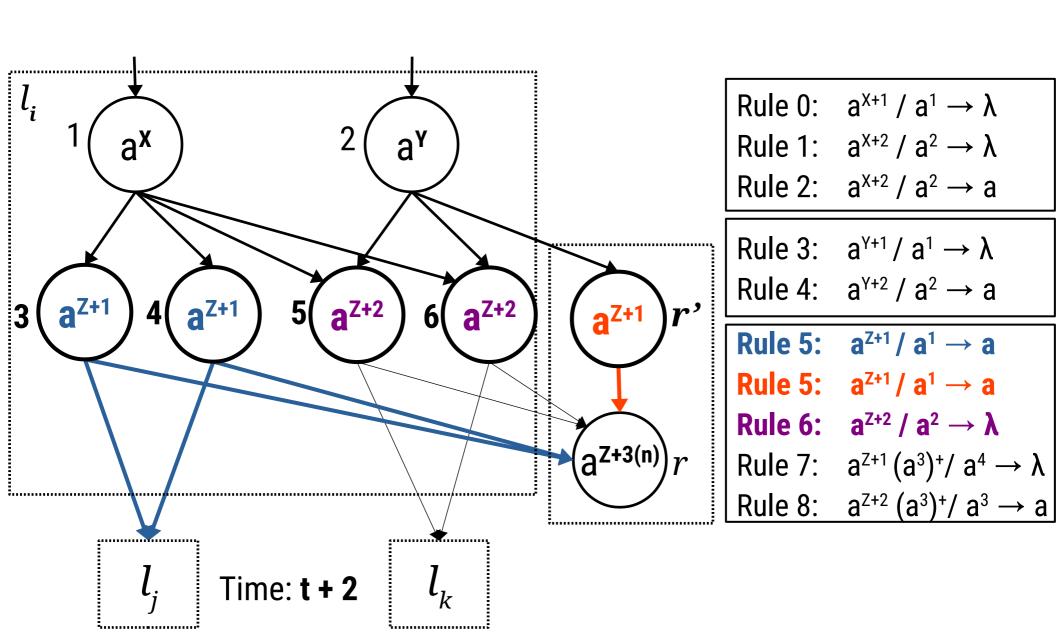
Case 1: Rule 1 is activated.



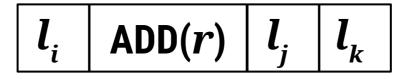


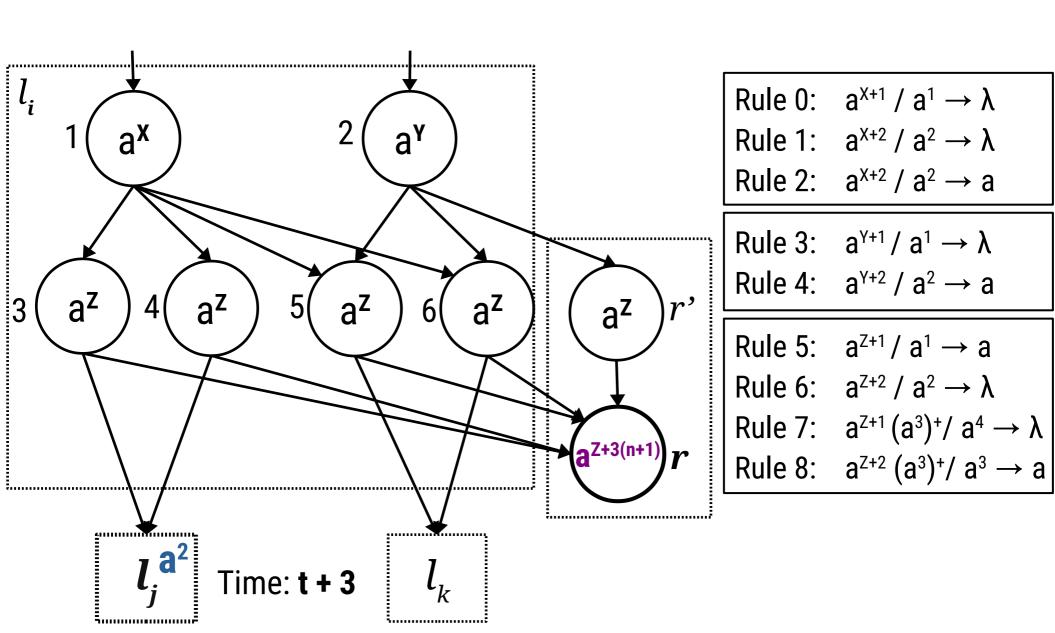
Case 2: Rule 2 is activated.

 $\begin{bmatrix} l_i & ADD(r) & l_j & l_k \end{bmatrix}$ 

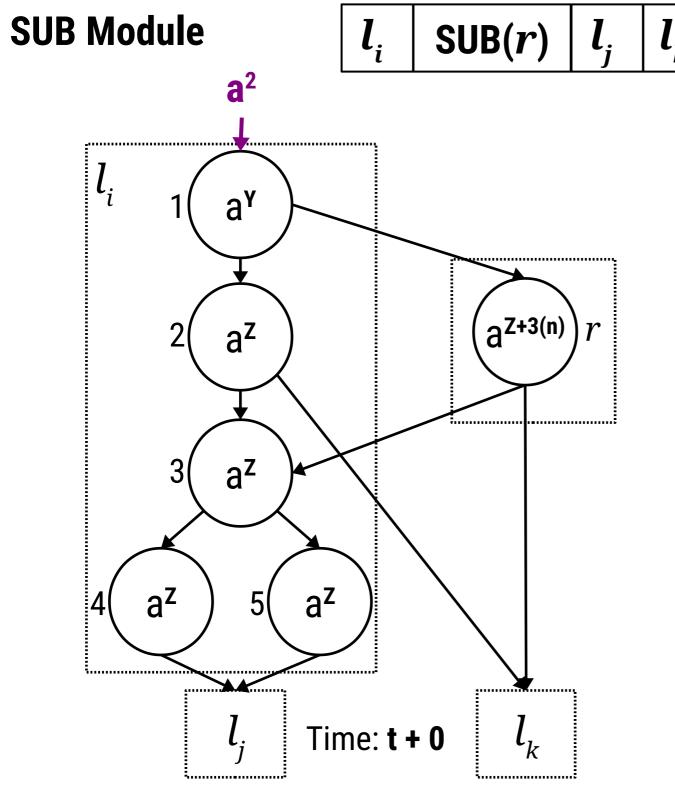


Case 2: Rule 2 is activated.





Case 2: Rule 2 is activated.



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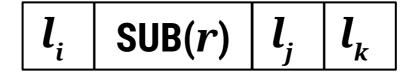
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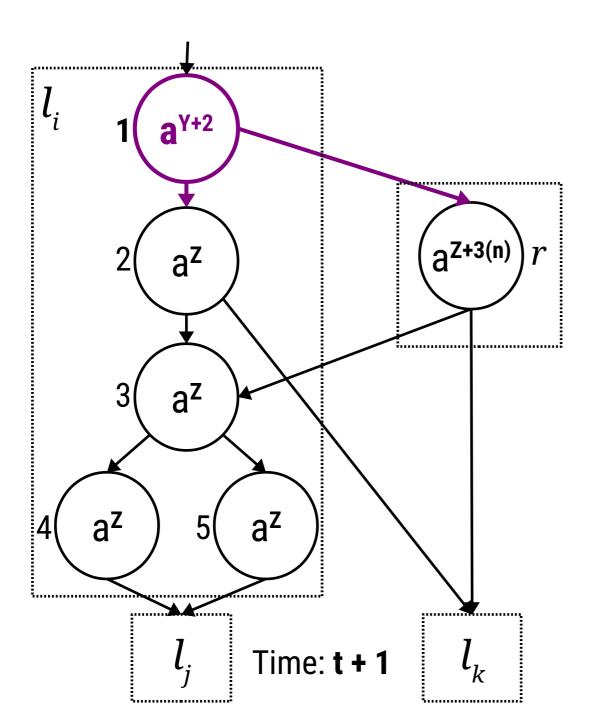
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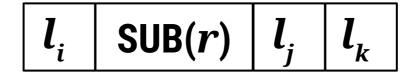
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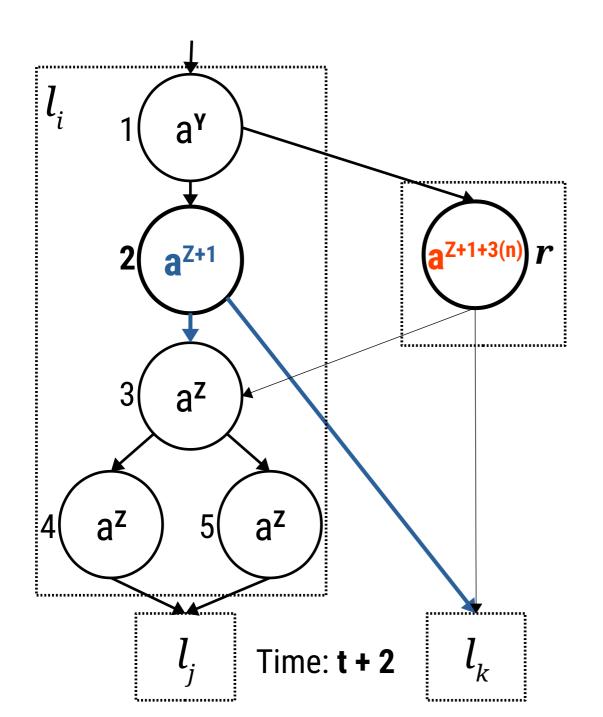
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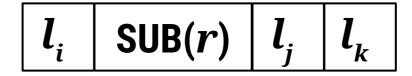
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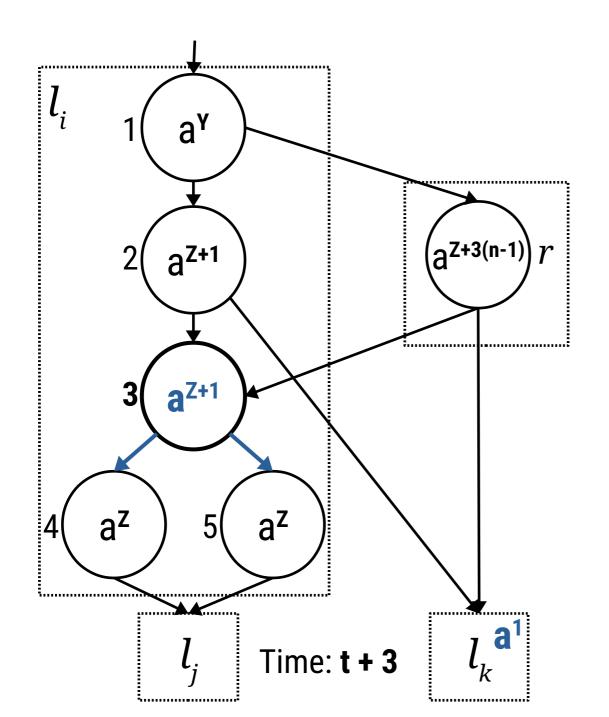
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Rule 8:  $a^{Z+2} (a^3)^+/a^3 \rightarrow a$ 





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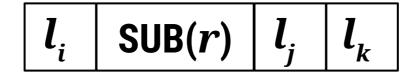
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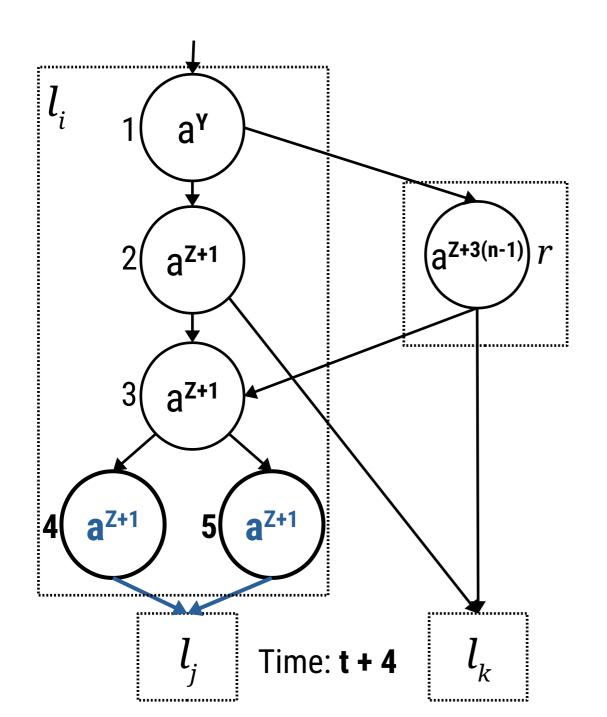
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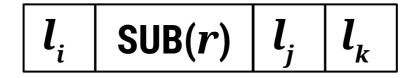
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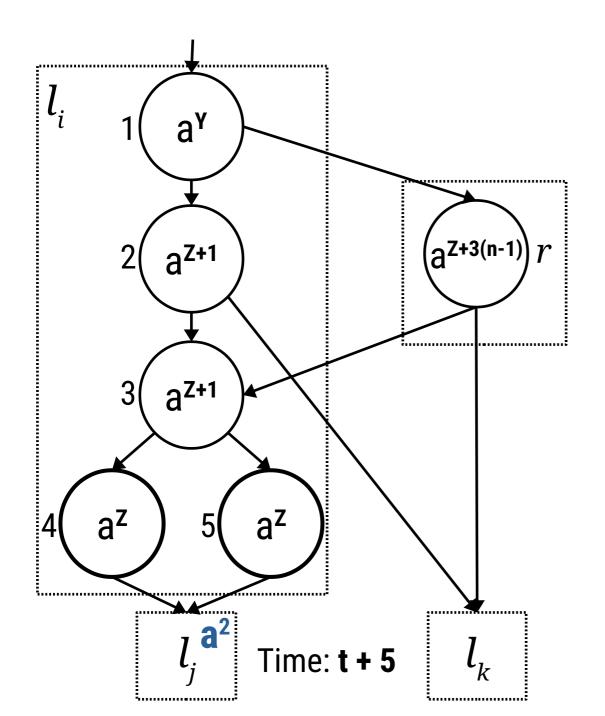
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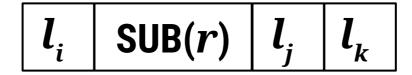
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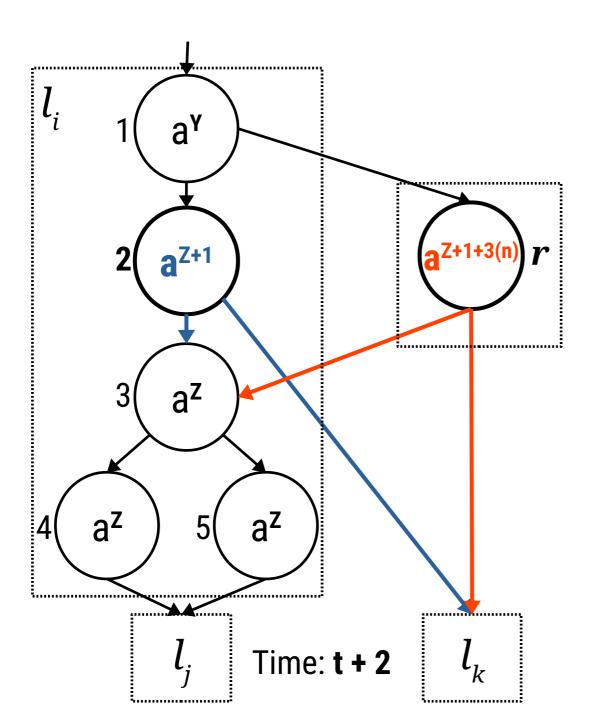
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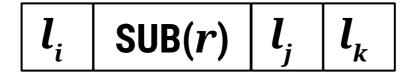
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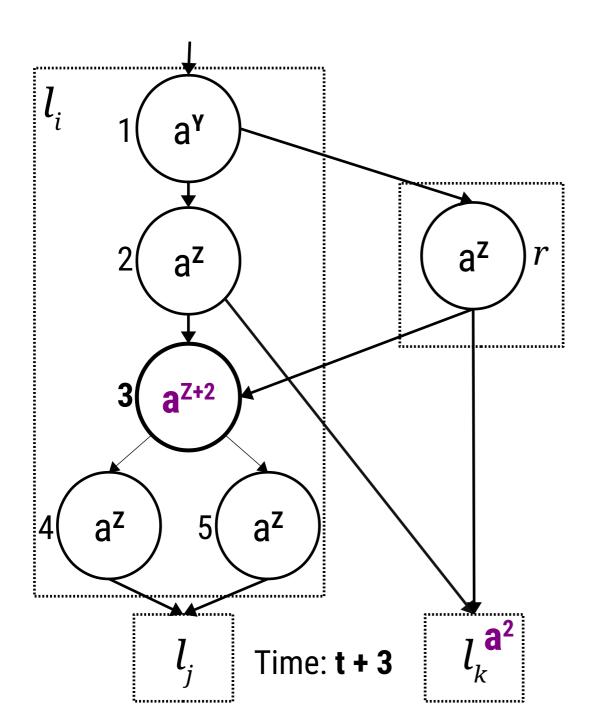
Rule 6:  $a^{Z+2}/a^2 \rightarrow \lambda$ 

Rule 7:  $a^{Z+1}(a^3)^+/a^4 \to \lambda$ 

Rule 8:  $a^{Z+2} (a^3)^+/a^3 \rightarrow a$ 

**Case 2:** n = 0





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Rule 1:  $a^{X+2}/a^2 \rightarrow \lambda$ 

Rule 2:  $a^{X+2}/a^2 \rightarrow a$ 

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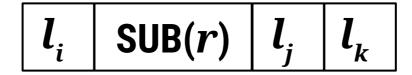
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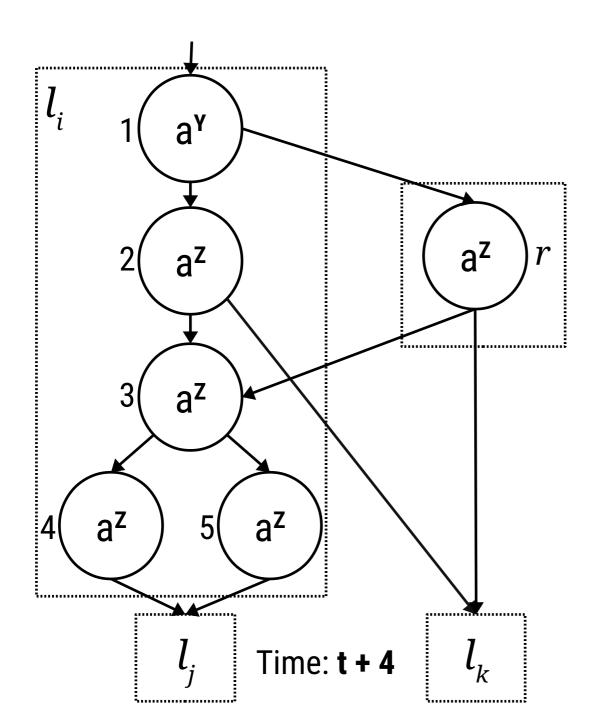
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Rule 1:  $a^{X+2}/a^2 \rightarrow \lambda$ 

Rule 2:  $a^{X+2}/a^2 \rightarrow a$ 

Rule 3:  $a^{Y+1}/a^1 \rightarrow \lambda$ 

Rule 4:  $a^{Y+2}/a^2 \rightarrow a$ 

Rule 5:  $a^{Z+1}/a^1 \rightarrow a$ 

Rule 6:  $a^{Z+2}/a^2 \rightarrow \lambda$ 

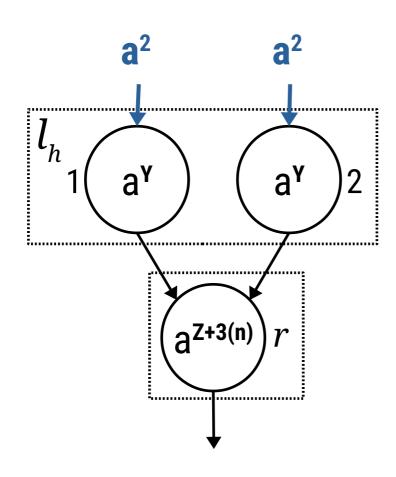
Rule 7:  $a^{Z+1}(a^3)^+/a^4 \to \lambda$ 

Rule 8:  $a^{Z+2} (a^3)^+/a^3 \rightarrow a$ 

**Case 2:** n = 0

#### **HALT Module**

 $l_h$  HALT



Time: **t + 0** 

Rule 0:  $a^{X+1} / a^1 \rightarrow \lambda$ 

Rule 1:  $a^{X+2}/a^2 \rightarrow \lambda$ 

Rule 2:  $a^{X+2}/a^2 \rightarrow a$ 

Rule 3:  $a^{Y+1}/a^1 \rightarrow \lambda$ 

Rule 4:  $a^{Y+2}/a^2 \rightarrow a$ 

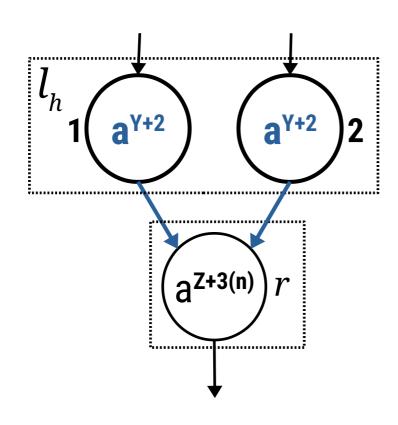
Rule 5:  $a^{Z+1}/a^1 \rightarrow a$ 

Rule 6:  $a^{Z+2} / a^2 \rightarrow \lambda$ 

Rule 7:  $a^{Z+1}(a^3)^+/a^4 \to \lambda$ 

#### **HALT Module**

 $l_h$  HALT



Time: **t + 1** 

Rule 0:  $a^{X+1}/a^1 \rightarrow \lambda$ 

Rule 1:  $a^{X+2}/a^2 \rightarrow \lambda$ 

Rule 2:  $a^{X+2}/a^2 \rightarrow a$ 

Rule 3:  $a^{Y+1}/a^1 \rightarrow \lambda$ 

Rule 4:  $a^{Y+2}/a^2 \rightarrow a$ 

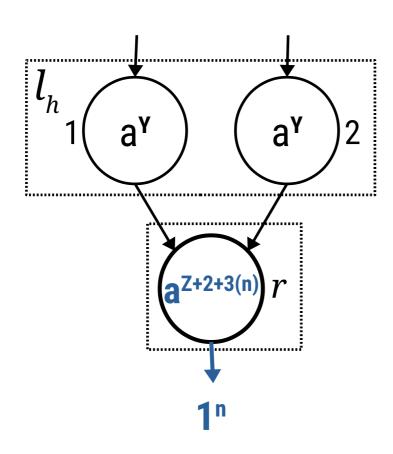
Rule 5:  $a^{Z+1}/a^1 \rightarrow a$ 

Rule 6:  $a^{Z+2} / a^2 \rightarrow \lambda$ 

Rule 7:  $a^{Z+1}(a^3)^+/a^4 \to \lambda$ 

#### **HALT Module**

 $l_h$  HALT



Time: **t + 2** 

to

Time: t + n + 1

Rule 0:  $a^{X+1}/a^1 \rightarrow \lambda$ 

Rule 1:  $a^{X+2}/a^2 \rightarrow \lambda$ 

Rule 2:  $a^{X+2}/a^2 \rightarrow a$ 

Rule 3:  $a^{Y+1}/a^1 \rightarrow \lambda$ 

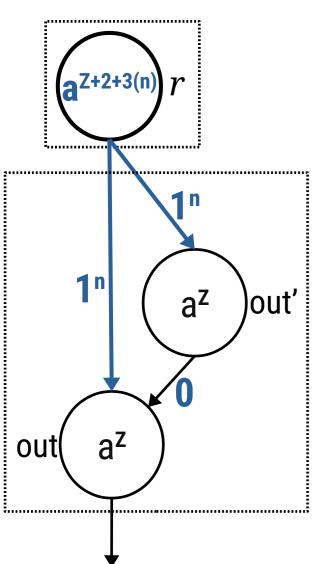
Rule 4:  $a^{Y+2}/a^2 \rightarrow a$ 

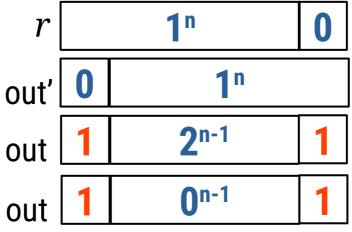
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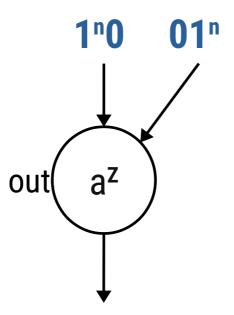
Rule 6:  $a^{Z+2} / a^2 \rightarrow \lambda$ 

Rule 7:  $a^{Z+1}(a^3)^+/a^4 \to \lambda$ 

#### **OUTPUT Module**







Rule 0:  $a^{X+1} / a^1 \rightarrow \lambda$ 

Rule 1:  $a^{X+2}/a^2 \rightarrow \lambda$ 

Rule 2:  $a^{X+2}/a^2 \rightarrow a$ 

Rule 3:  $a^{Y+1}/a^1 \rightarrow \lambda$ 

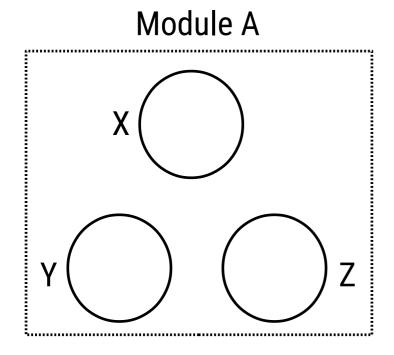
Rule 4:  $a^{Y+2} / a^2 \rightarrow a$ 

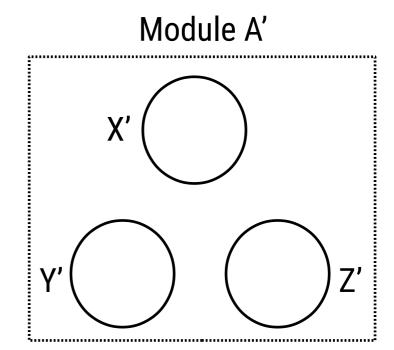
Rule 5:  $a^{Z+1}/a^1 \rightarrow a$ 

Rule 6:  $a^{Z+2}/a^2 \rightarrow \lambda$ 

Rule 7:  $a^{Z+1}(a^3)^+/a^4 \to \lambda$ 

**Discussion:** On why plasticity rules are only used as forgetting rules.





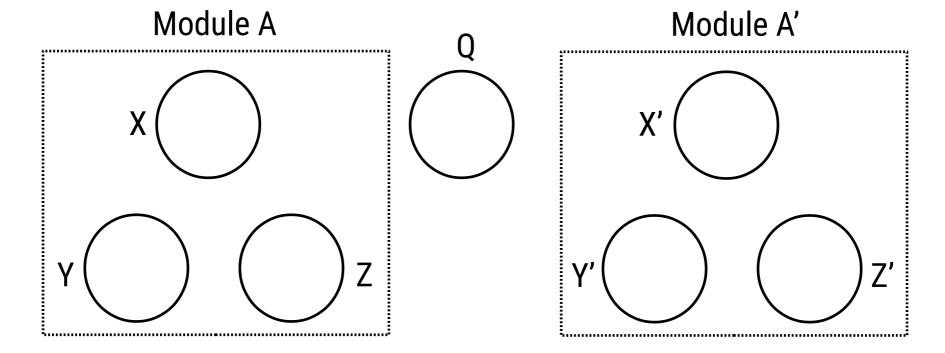
In neuron X:

Rule 1: E /  $a^c \rightarrow +2(\{Y,Z\})$ 

In neuron X':

Rule 1': E /  $a^c \to +2(\{Y',Z'\})$ 

Neuron X' can not reuse Rule 1 of neuron X. Neuron X can not reuse Rule 1' of neuron X'. **Discussion:** On why plasticity rules are only used as forgetting rules.



In neuron X:

Rule 1: E /  $a^c \rightarrow -1(\{Q\})$ 

Rule 1: E /  $a^c \rightarrow \lambda$ 

In neuron X':

Rule 1': E /  $a^c \to -1(\{Q\})$ 

Rule 1': E /  $a^c \rightarrow \lambda$ 

#### **Discussion:** On "translating" rules

Rule 0: 
$$a^{1} / a^{1} \rightarrow \lambda$$
  
Rule 1:  $a^{2} / a^{2} \rightarrow \lambda$   
Rule 2:  $a^{2} / a^{2} \rightarrow a$ 

1 Rule 0:  $a^{1} / a^{1} \rightarrow \lambda$   
Rule 1:  $a^{2} / a^{2} \rightarrow \lambda$   
Rule 2:  $a^{2} / a^{2} \rightarrow a$ 

2 Rule 3:  $a^{1} / a^{1} \rightarrow a$   
Rule 4:  $a^{2} / a^{2} \rightarrow \lambda$ 

2 Rule 3:  $a^{X+1} / a^{1} \rightarrow a$   
Rule 4:  $a^{X+2} / a^{2} \rightarrow \lambda$ 

X > 2

You can easily create a common set of rules by "translating" different rule sets then combining them and adding the appropriate initial spike counts to the neurons.

#### **Discussion:** On "translating" rules

Rule 0:  $a^{X+1}/a^1 \rightarrow \lambda$ 

Rule 1:  $a^{X+2}/a^2 \rightarrow \lambda$ 

Rule 2:  $a^{X+2}/a^2 \rightarrow a$ 

Rule 3:  $a^{Y+1}/a^1 \rightarrow \lambda$ 

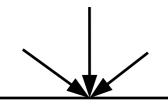
Rule 4:  $a^{Y+2}/a^2 \rightarrow a$ 

Rule 5:  $a^{Z+1}/a^1 \rightarrow a$ 

Rule 6:  $a^{Z+2} / a^2 \rightarrow \lambda$ 

Rule 7:  $a^{Z+1}(a^3)^+/a^4 \to \lambda$ 

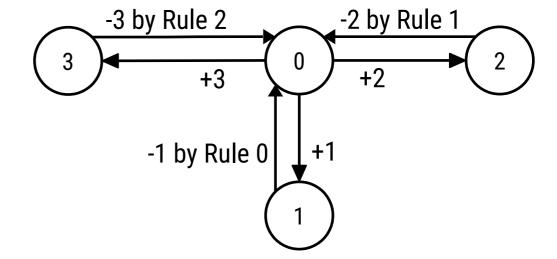
#### **Discussion:** On combining rules

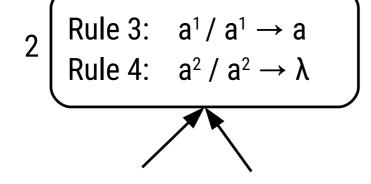


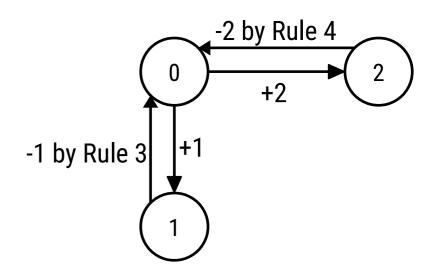
Rule 0:  $a^1 / a^1 \rightarrow \lambda$ 

Rule 1:  $a^2 / a^2 \rightarrow \lambda$ 

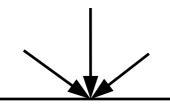
Rule 2:  $a^3 / a^3 \rightarrow a$ 







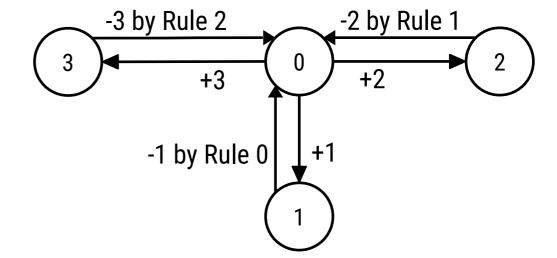
#### **Discussion:** On combining rules

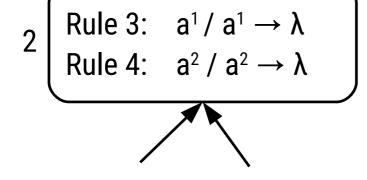


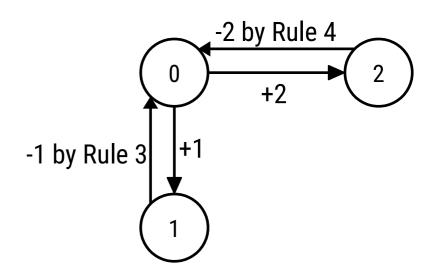
Rule 0:  $a^1 / a^1 \rightarrow \lambda$ 

Rule 1:  $a^2 / a^2 \rightarrow \lambda$ 

Rule 2:  $a^3 / a^3 \rightarrow a$ 







## **End of Presentation. Thank you!**

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