

Homogeneous Spiking Neural P Systems with Structural Plasticity

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20th Conference on Membrane Computing

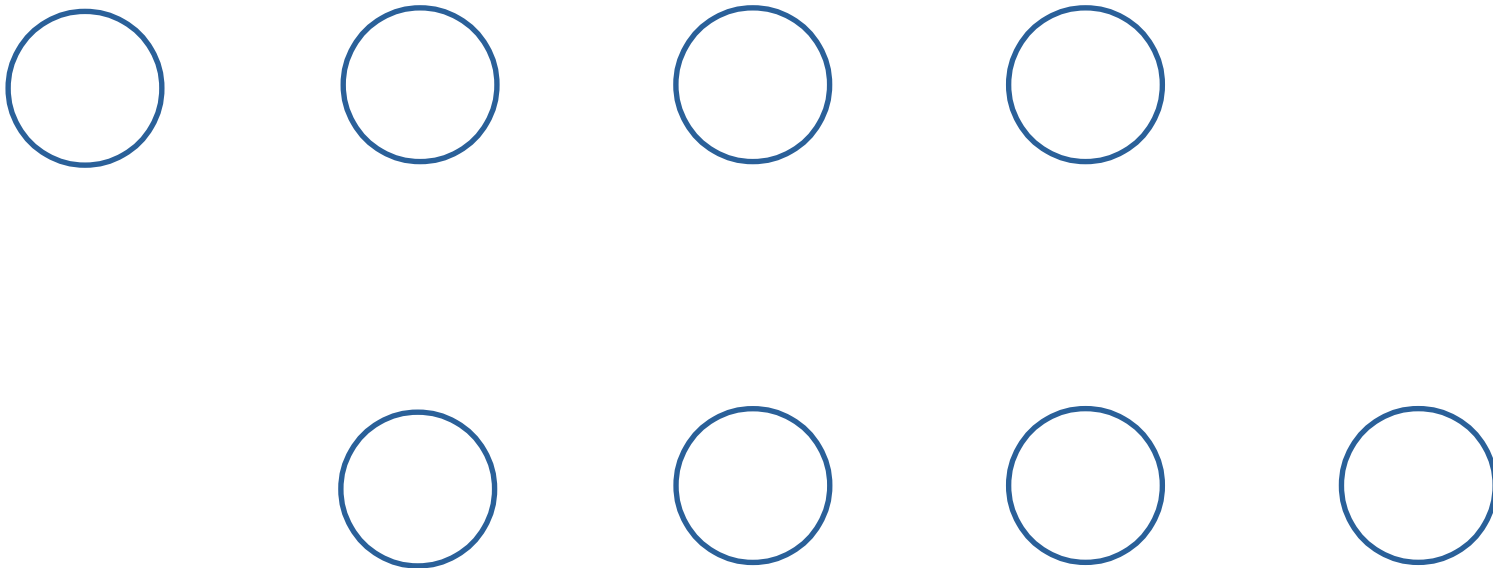
Curtea de Argeș, Romania

08 August 2019

Spiking Neural P Systems with Structural Plasticity (SNPSP System)

$$\Pi = (\textcolor{red}{0}, \textcolor{blue}{\sigma}_1, \dots, \textcolor{blue}{\sigma}_m, \textcolor{orange}{syn}, \textcolor{green}{out})$$

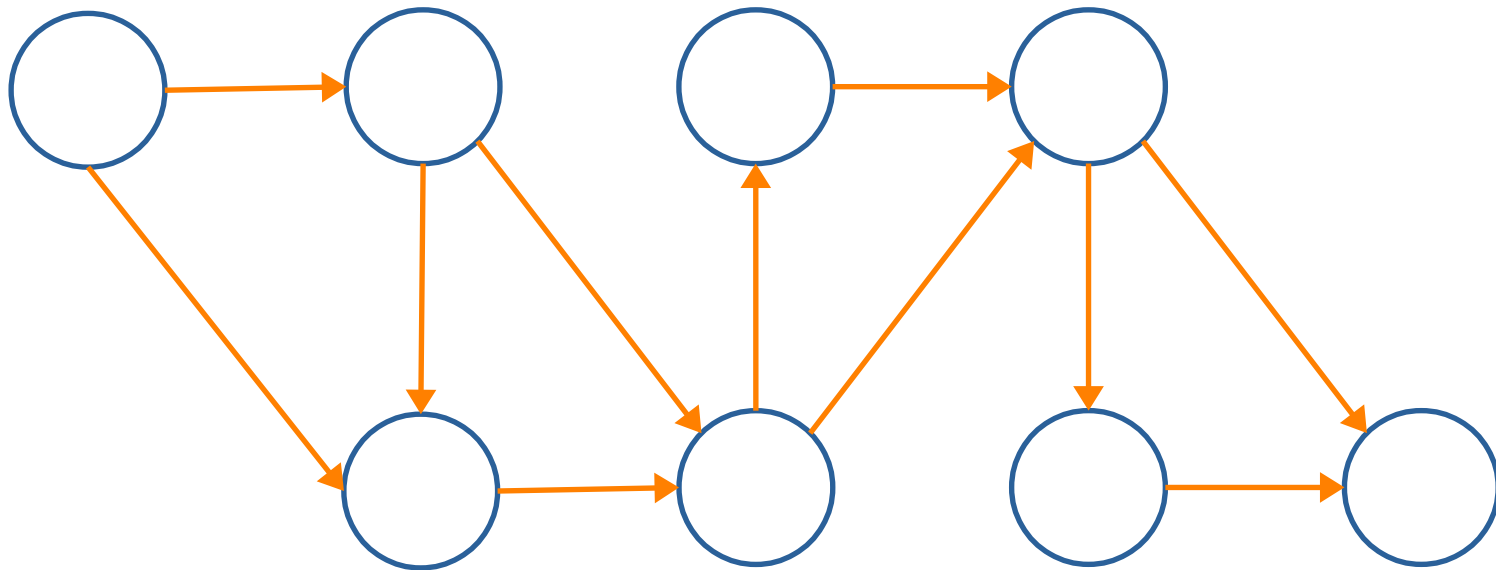
Neurons: $\textcolor{blue}{\sigma}_1, \dots, \textcolor{blue}{\sigma}_m$



Spiking Neural P Systems with Structural Plasticity (SNPSP System)

$$\Pi = (\mathbf{0}, \sigma_1, \dots, \sigma_m, \textit{syn}, \textit{out})$$

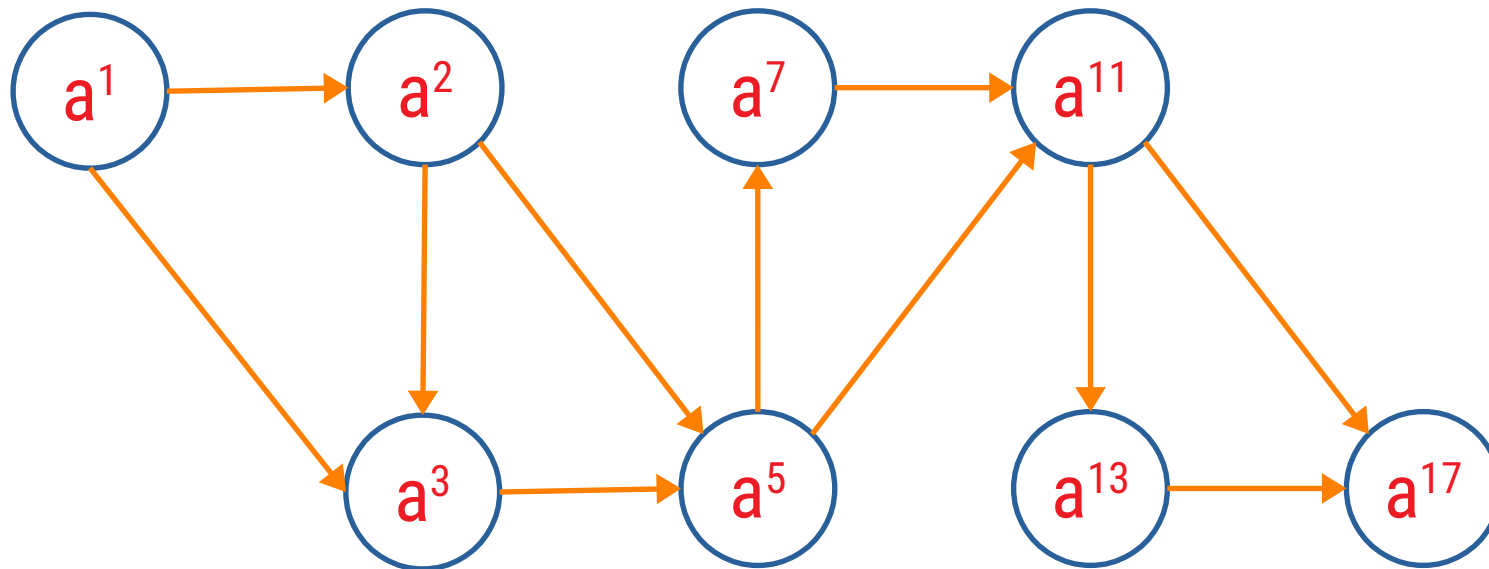
Synapses: *syn*



Spiking Neural P Systems with Structural Plasticity (SNPSP System)

$$\Pi = (0, \sigma_1, \dots, \sigma_m, \text{syn}, \text{out})$$

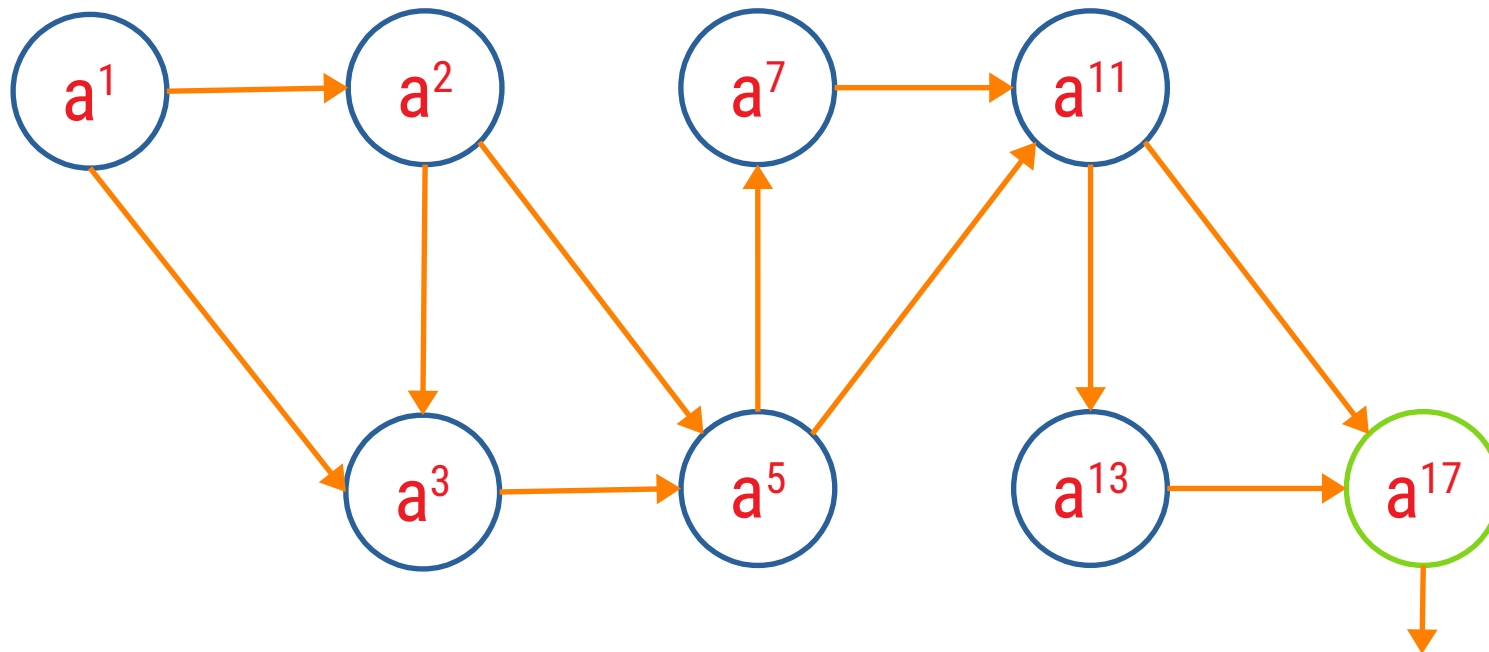
Spike: a
Alphabet: $0 = \{a\}$
Multiset of Spikes: a^i



Spiking Neural P Systems with Structural Plasticity (SNPSP System)

$$\Pi = (\mathbf{0}, \sigma_1, \dots, \sigma_m, \textit{syn}, \textit{out})$$

Output Nueron: *out*



Spiking Neural P Systems with Structural Plasticity (SNPSP System)

$$\Pi = (0, \sigma_1, \dots, \sigma_m, syn, out)$$

Spiking Rule : $E / a^c \rightarrow a$

Plasticity Rule : $E / a^c \rightarrow \alpha k(N)$

N – target neurons

$$\alpha \in \{+, -, \pm, \mp\}$$

$+k$ – add k synapses

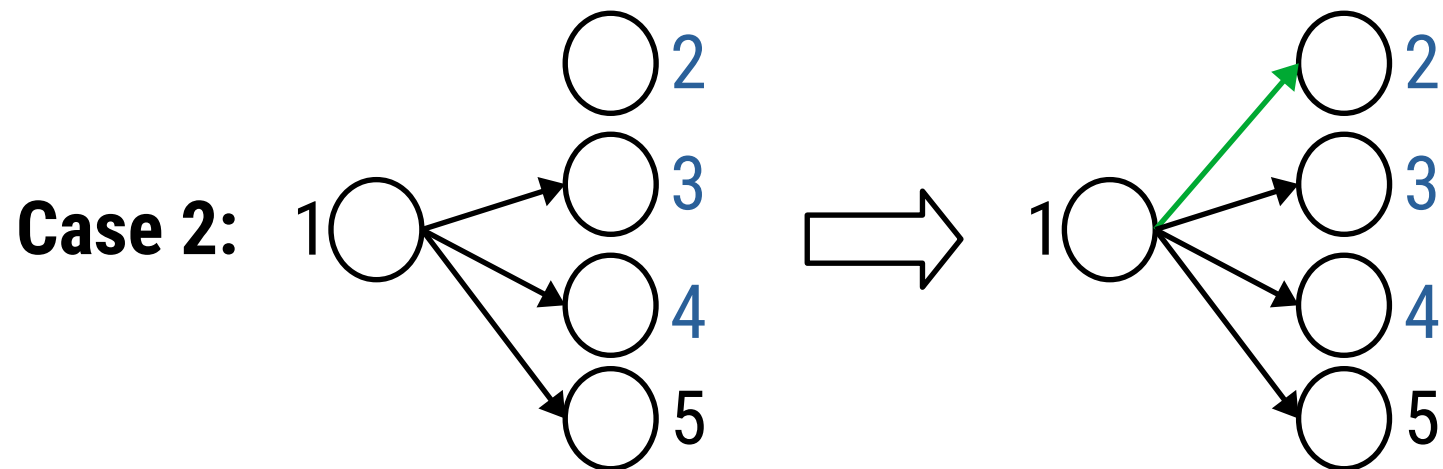
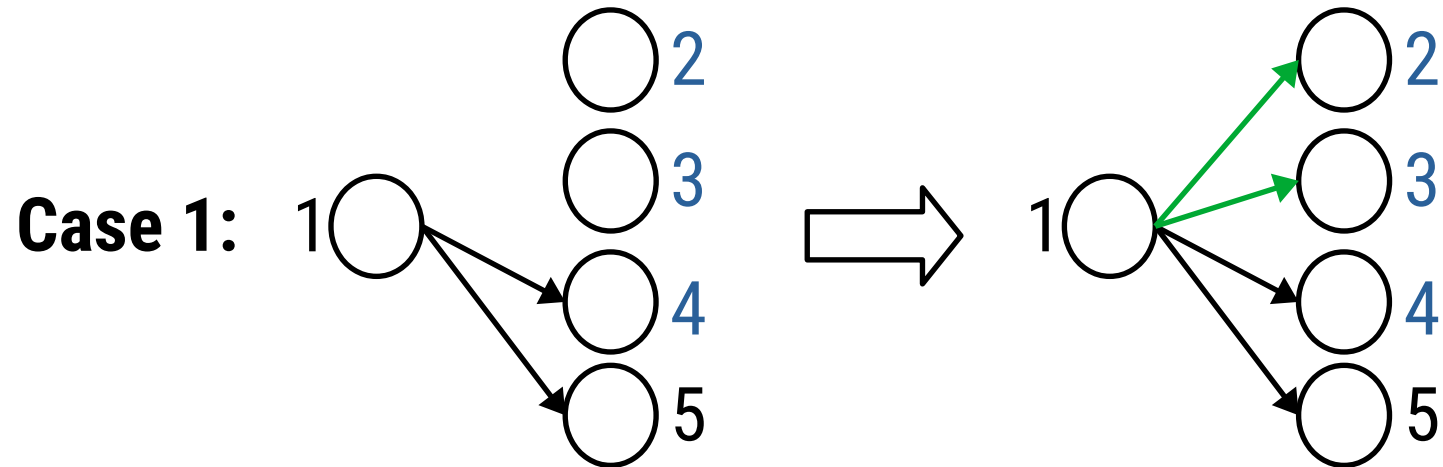
$-k$ – delete k synapses

$\pm k$ – add then delete k synapses

$\mp k$ – delete then add k synapses

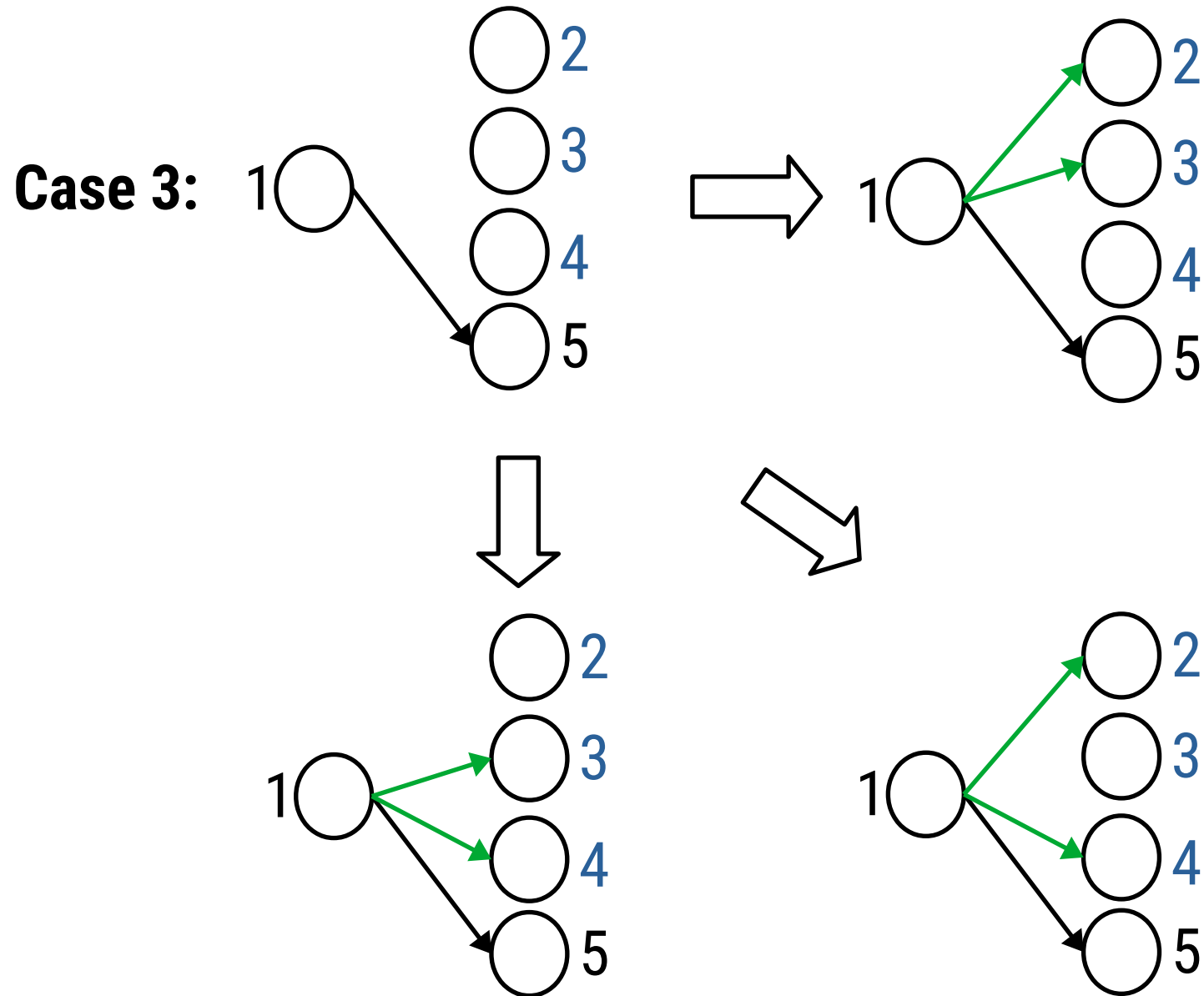
Plasticity Rule: $E / a^c \rightarrow \text{ak}(N)$

In neuron 1: $E / a^c \rightarrow +2(\{2,3,4\})$



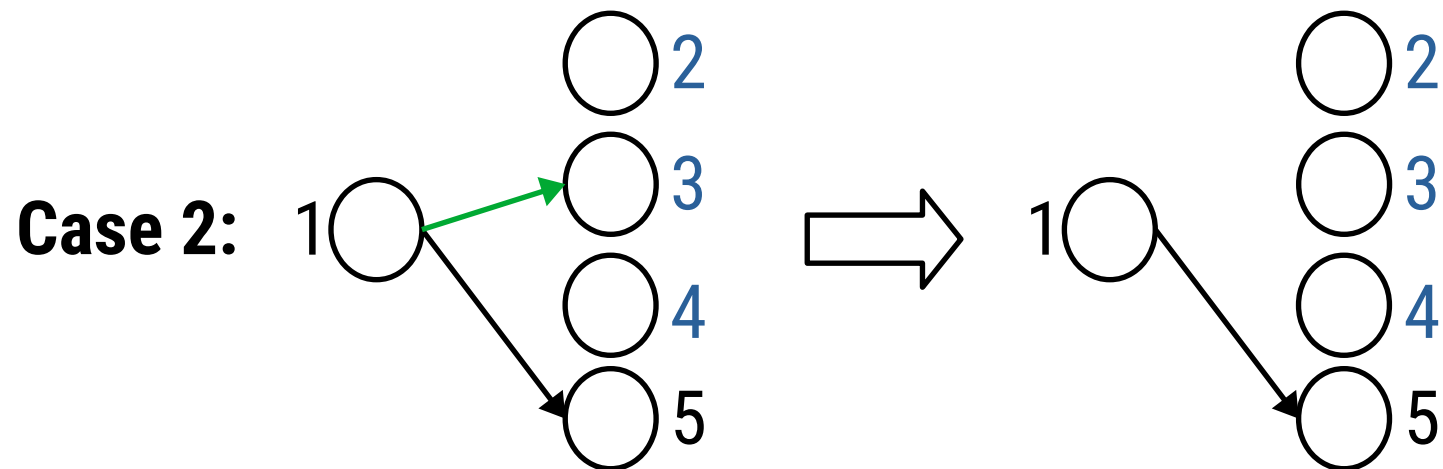
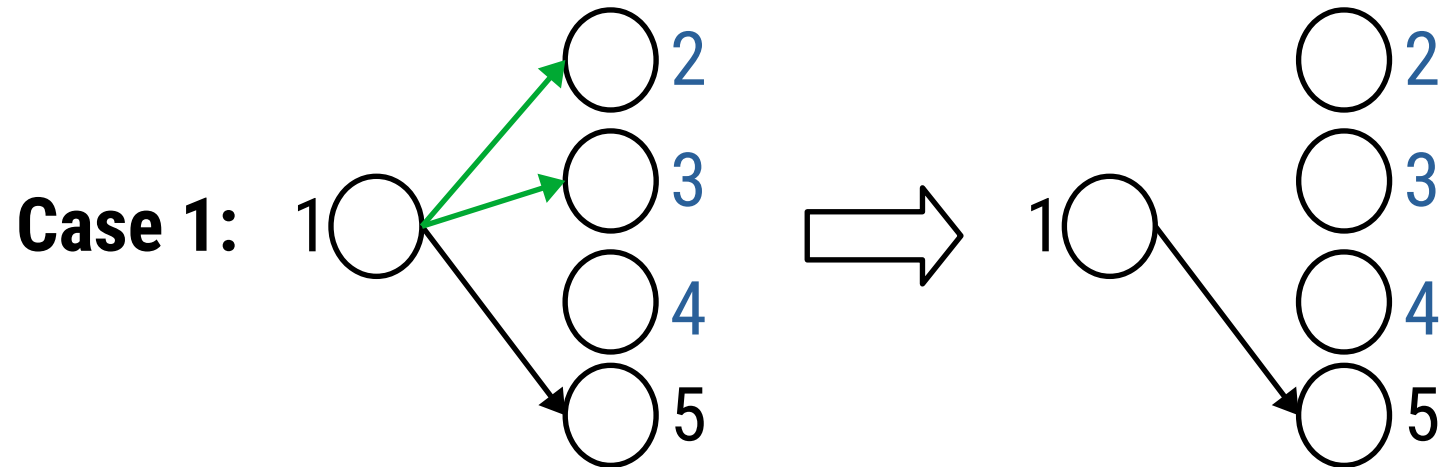
Plasticity Rule: $E / a^c \rightarrow \text{ak}(N)$

In neuron 1: $E / a^c \rightarrow +2(\{2,3,4\})$



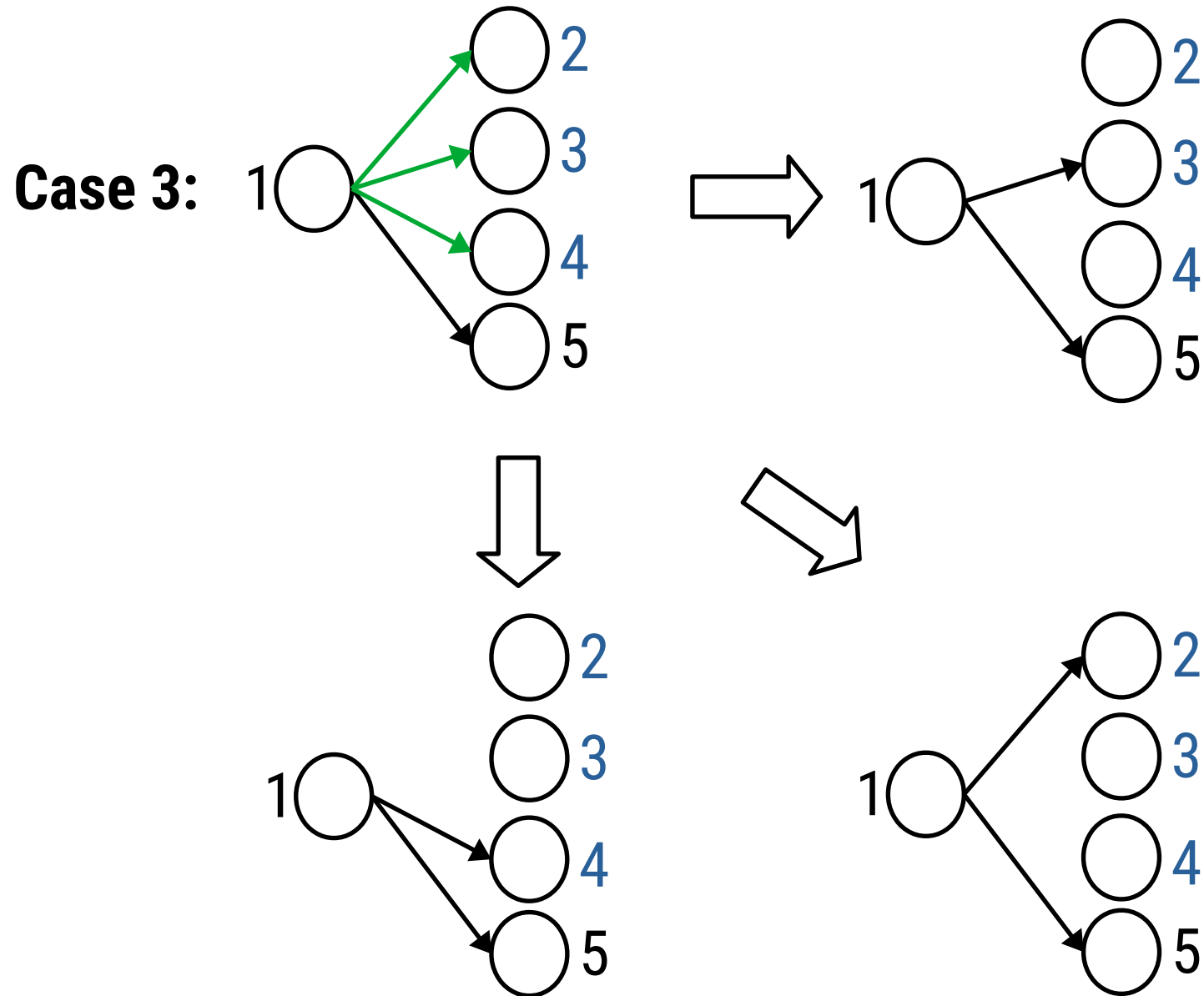
Plasticity Rule: $E / a^c \rightarrow \text{ak}(N)$

In neuron 1: $E / a^c \rightarrow -2(\{2,3,4\})$



Plasticity Rule: $E / a^c \rightarrow \text{ak}(N)$

In neuron 1: $E / a^c \rightarrow -2(\{2,3,4\})$



Plasticity Rule: $E / a^c \rightarrow \text{ak}(\text{N})$

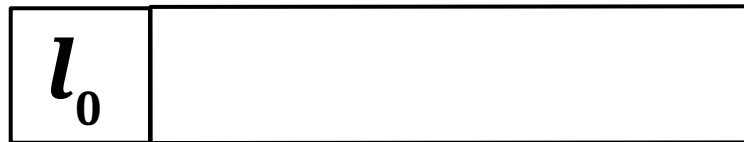
Plasticity rules as forgetting rules.

Case 1: $1 \bigcirc \longrightarrow \bigcirc 2$ In neuron 1: $E / a^c \rightarrow +1(\{2\})$

Case 2: $1 \bigcirc \quad \bigcirc 2$ In neuron 1: $E / a^c \rightarrow -1(\{2\})$

Register Machines

Instructions



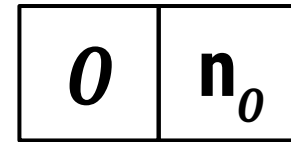
⋮



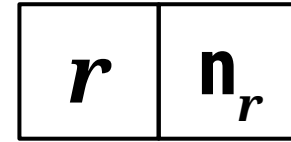
⋮



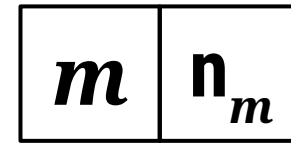
Registers



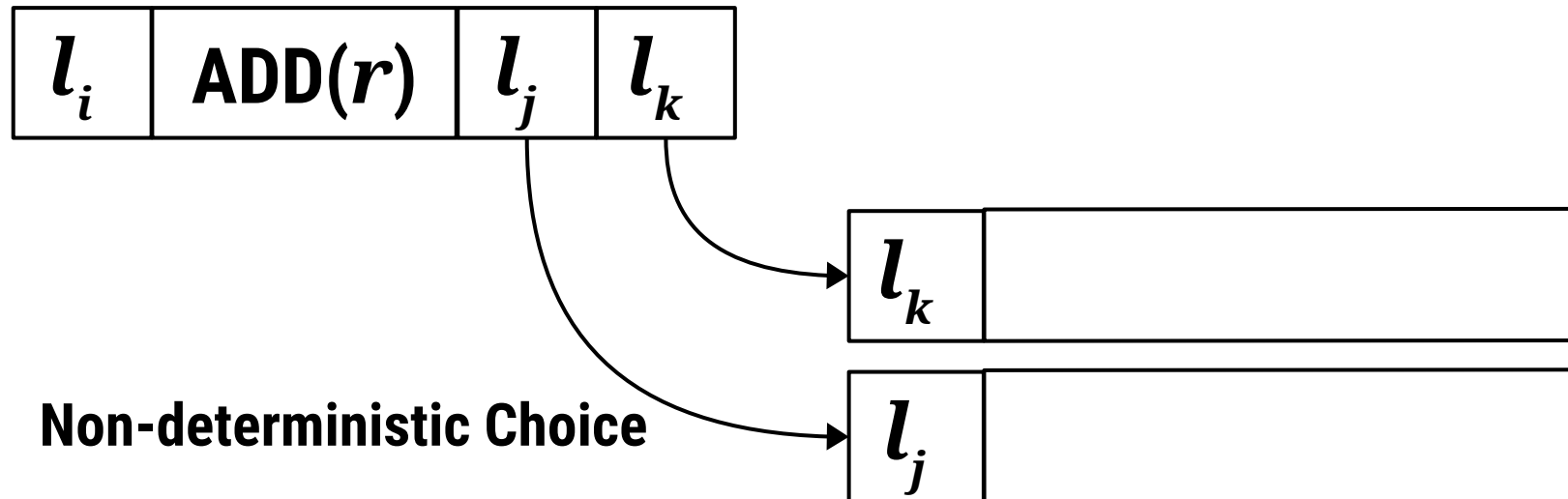
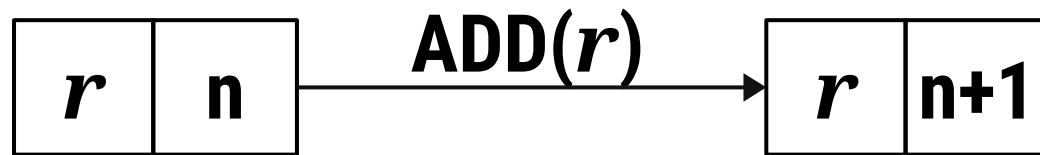
⋮



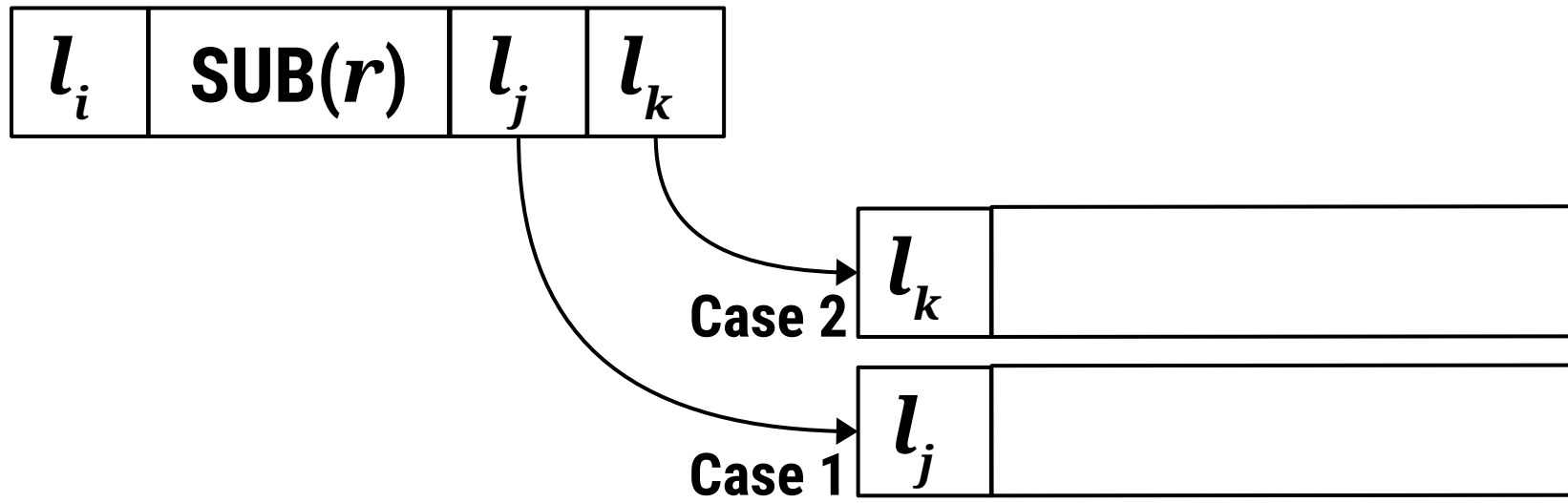
⋮



Register Machines



Register Machines



Register Machines



Representing Numbers

n

Number (in Register)

$Z + 3n$

Spike Count

Z is some constant spike count.

$10^{n-1}1$

Spike Train

Common Rule Set for All Neurons

$$\text{Rule 0: } a^{X+1} / a^1 \rightarrow \lambda$$

$$\text{Rule 1: } a^{X+2} / a^2 \rightarrow \lambda$$

$$\text{Rule 2: } a^{X+2} / a^2 \rightarrow a$$

$$\text{Rule 3: } a^{Y+1} / a^1 \rightarrow \lambda$$

$$\text{Rule 4: } a^{Y+2} / a^2 \rightarrow a$$

$$\text{Rule 5: } a^{Z+1} / a^1 \rightarrow a$$

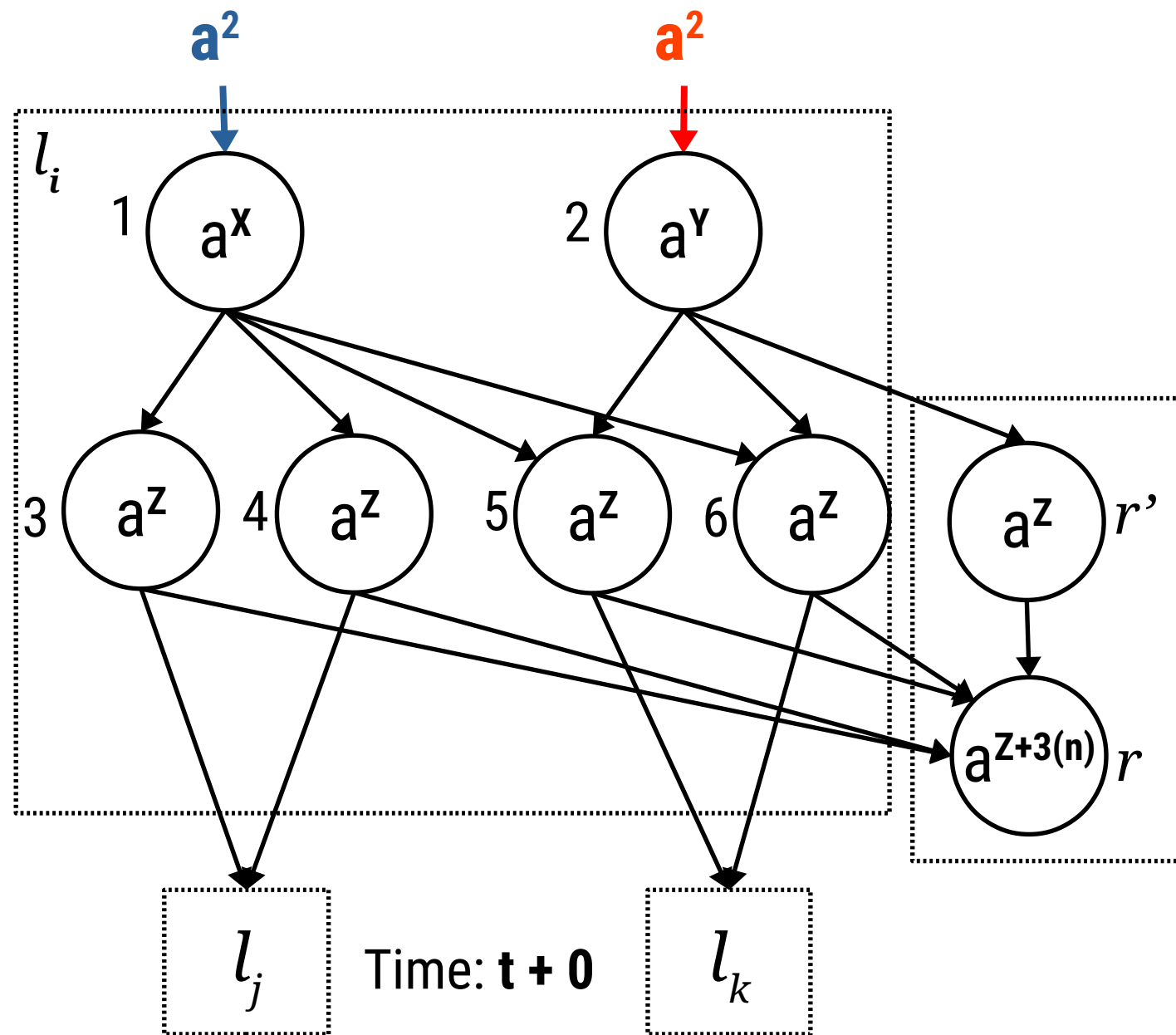
$$\text{Rule 6: } a^{Z+2} / a^2 \rightarrow \lambda$$

$$\text{Rule 7: } a^{Z+1} (a^3)^+ / a^4 \rightarrow \lambda$$

$$\text{Rule 8: } a^{Z+2} (a^3)^+ / a^3 \rightarrow a$$

ADD Module

l_i	ADD(r)	l_j	l_k
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Rule 0: $a^{x+1} / a^1 \rightarrow \lambda$

Rule 1: $a^{x+2} / a^2 \rightarrow \lambda$

Rule 2: $a^{x+2} / a^2 \rightarrow a$

Rule 3: $a^{y+1} / a^1 \rightarrow \lambda$

Rule 4: $a^{y+2} / a^2 \rightarrow a$

Rule 5: $a^{z+1} / a^1 \rightarrow a$

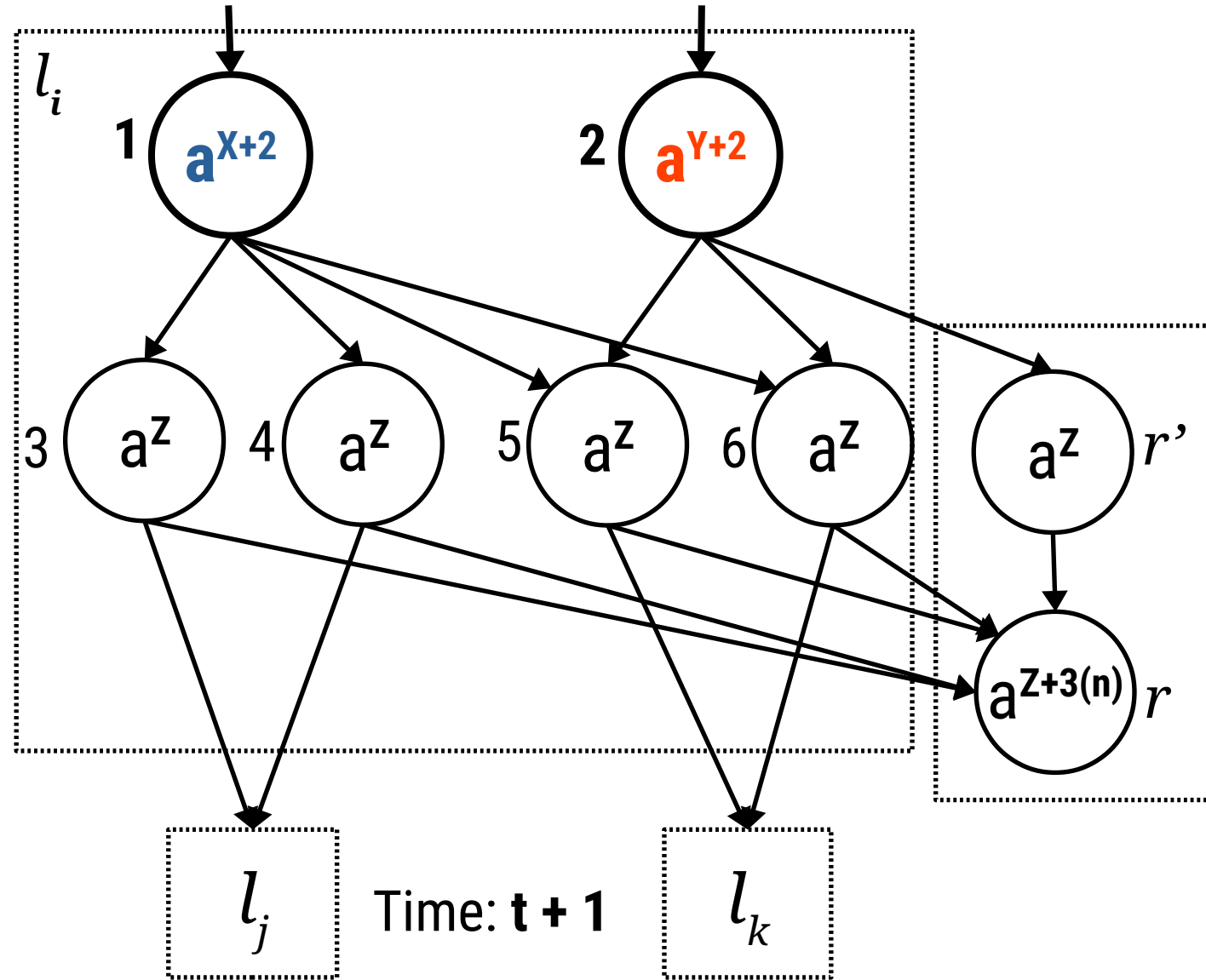
Rule 6: $a^{z+2} / a^2 \rightarrow \lambda$

Rule 7: $a^{z+1} (a^3)^+ / a^4 \rightarrow \lambda$

Rule 8: $a^{z+2} (a^3)^+ / a^3 \rightarrow a$

ADD Module

l_i	ADD(r)	l_j	l_k
-------	------------	-------	-------



Rule 0: $a^{X+1} / a^1 \rightarrow \lambda$

Rule 1: $a^{X+2} / a^2 \rightarrow \lambda$

Rule 2: $a^{X+2} / a^2 \rightarrow a$

Rule 3: $a^{Y+1} / a^1 \rightarrow \lambda$

Rule 4: $a^{Y+2} / a^2 \rightarrow a$

Rule 5: $a^{Z+1} / a^1 \rightarrow a$

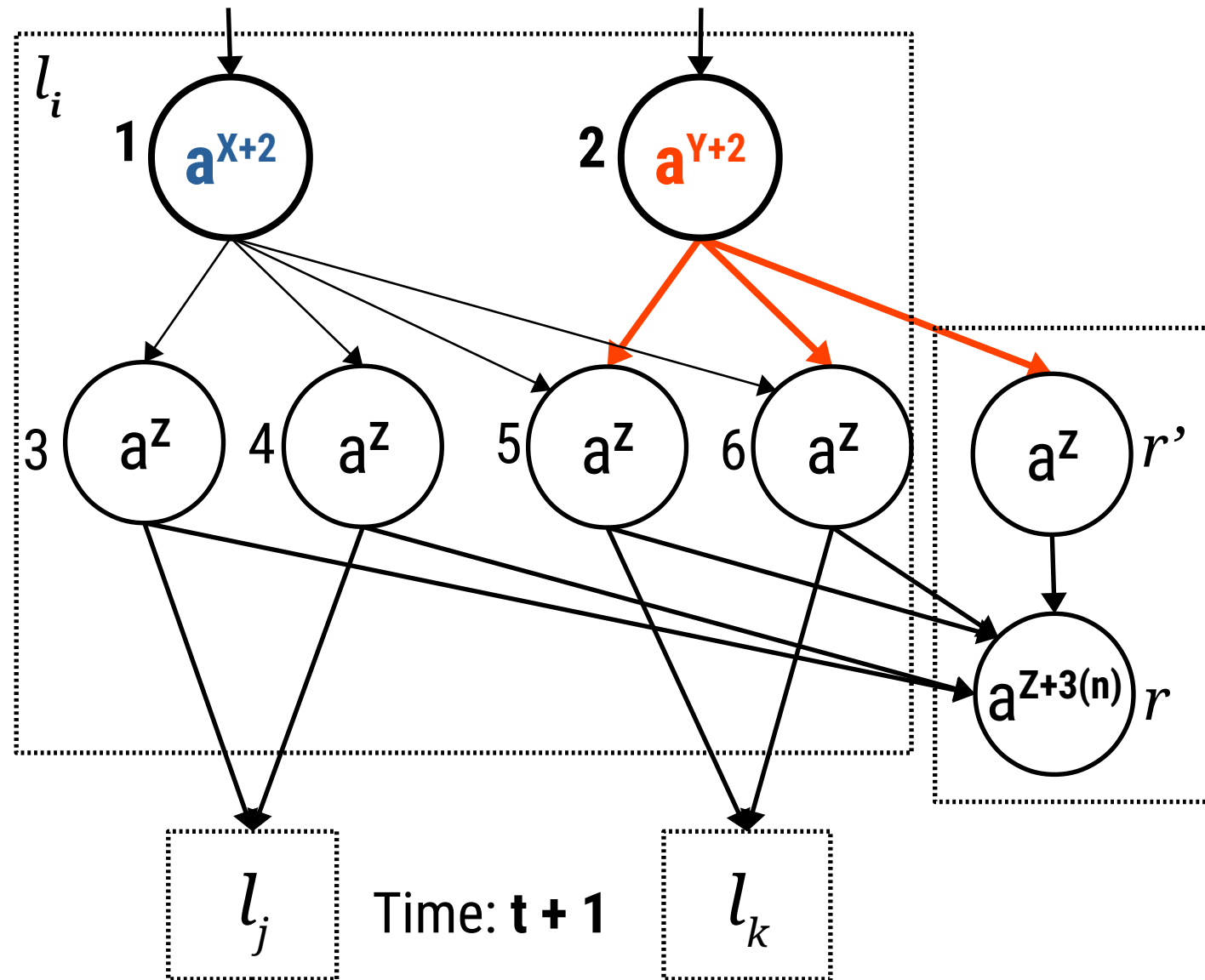
Rule 6: $a^{Z+2} / a^2 \rightarrow \lambda$

Rule 7: $a^{Z+1} (a^3)^+ / a^4 \rightarrow \lambda$

Rule 8: $a^{Z+2} (a^3)^+ / a^3 \rightarrow a$

ADD Module

l_i	ADD(r)	l_j	l_k
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Rule 0: $a^{X+1} / a^1 \rightarrow \lambda$

Rule 1: $a^{X+2} / a^2 \rightarrow \lambda$

Rule 2: $a^{X+2} / a^2 \rightarrow a$

Rule 3: $a^{Y+1} / a^1 \rightarrow \lambda$

Rule 4: $a^{Y+2} / a^2 \rightarrow a$

Rule 5: $a^{Z+1} / a^1 \rightarrow a$

Rule 6: $a^{Z+2} / a^2 \rightarrow \lambda$

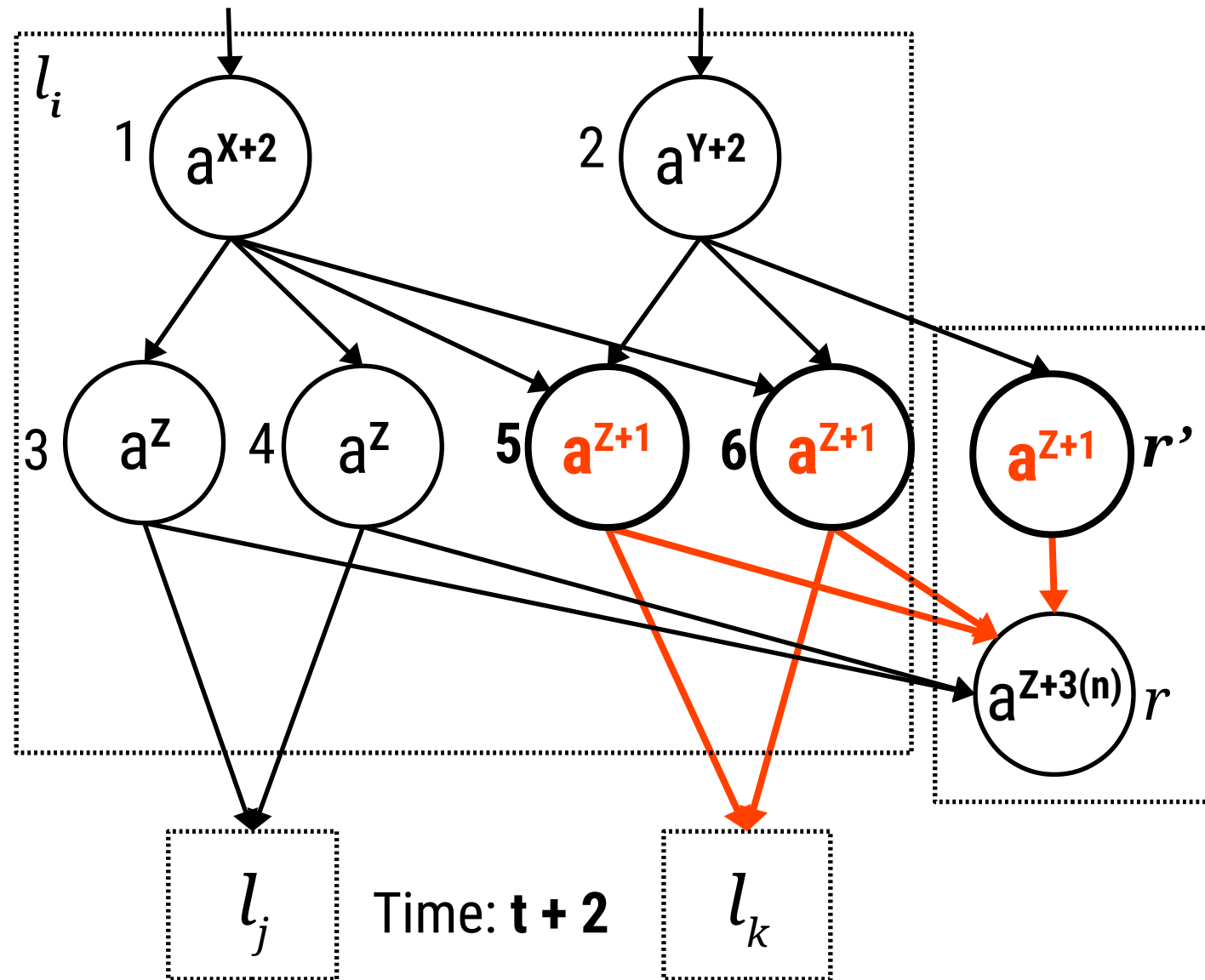
Rule 7: $a^{Z+1} (a^3)^+ / a^4 \rightarrow \lambda$

Rule 8: $a^{Z+2} (a^3)^+ / a^3 \rightarrow a$

Case 1: Rule 1 is activated.

ADD Module

l_i	ADD(r)	l_j	l_k
-------	----------------------------	-------	-------



Rule 0: $a^{x+1} / a^1 \rightarrow \lambda$

Rule 1: $a^{x+2} / a^2 \rightarrow \lambda$

Rule 2: $a^{x+2} / a^2 \rightarrow a$

Rule 3: $a^{y+1} / a^1 \rightarrow \lambda$

Rule 4: $a^{y+2} / a^2 \rightarrow a$

Rule 5: $a^{z+1} / a^1 \rightarrow a$

Rule 6: $a^{z+2} / a^2 \rightarrow \lambda$

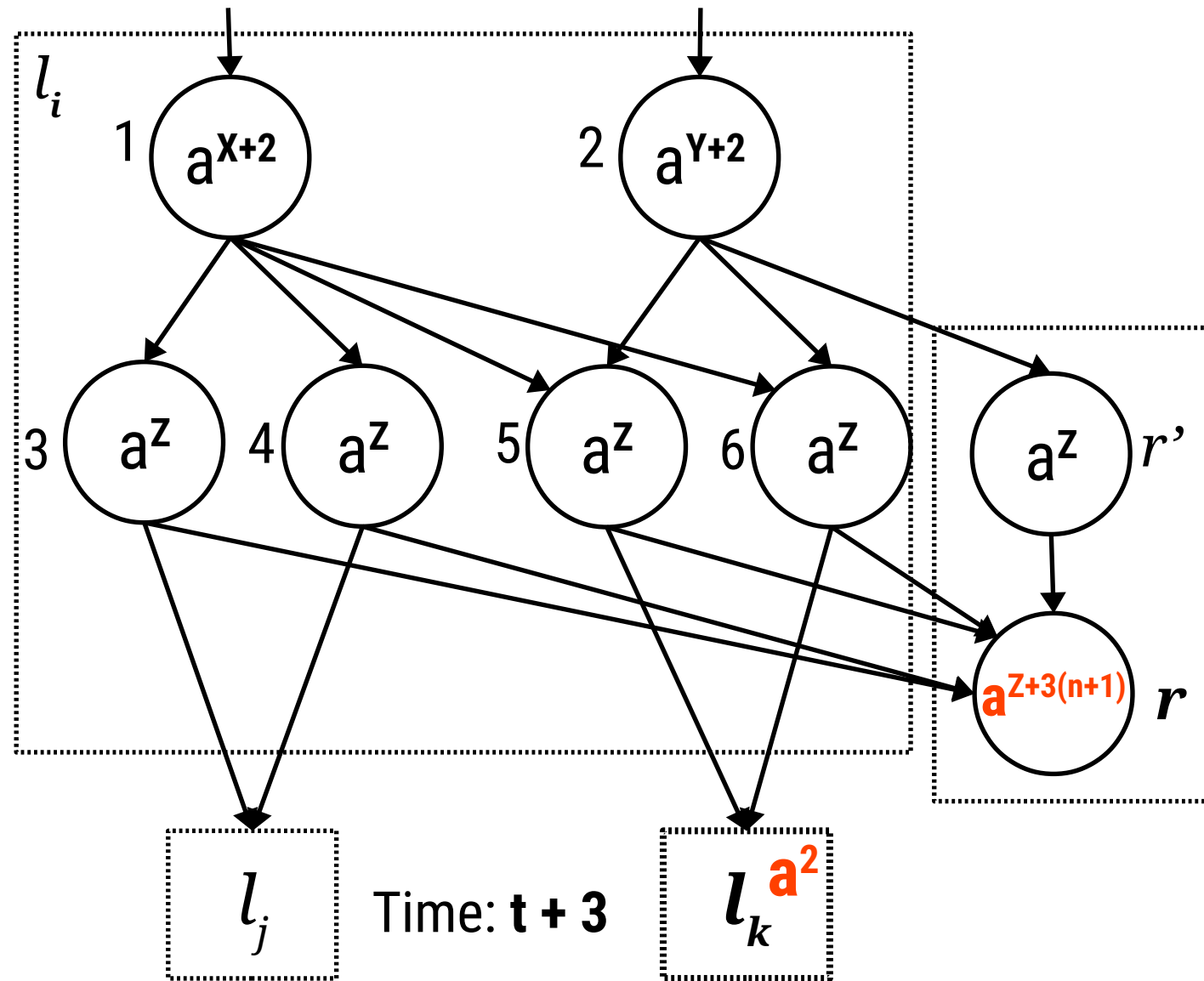
Rule 7: $a^{z+1} (a^3)^+ / a^4 \rightarrow \lambda$

Rule 8: $a^{z+2} (a^3)^+ / a^3 \rightarrow a$

Case 1: Rule 1 is activated.

ADD Module

l_i	ADD(r)	l_j	l_k
-------	----------------------------	-------	-------



Rule 0: $a^{x+1} / a^1 \rightarrow \lambda$

Rule 1: $a^{x+2} / a^2 \rightarrow \lambda$

Rule 2: $a^{x+2} / a^2 \rightarrow a$

Rule 3: $a^{y+1} / a^1 \rightarrow \lambda$

Rule 4: $a^{y+2} / a^2 \rightarrow a$

Rule 5: $a^{z+1} / a^1 \rightarrow a$

Rule 6: $a^{z+2} / a^2 \rightarrow \lambda$

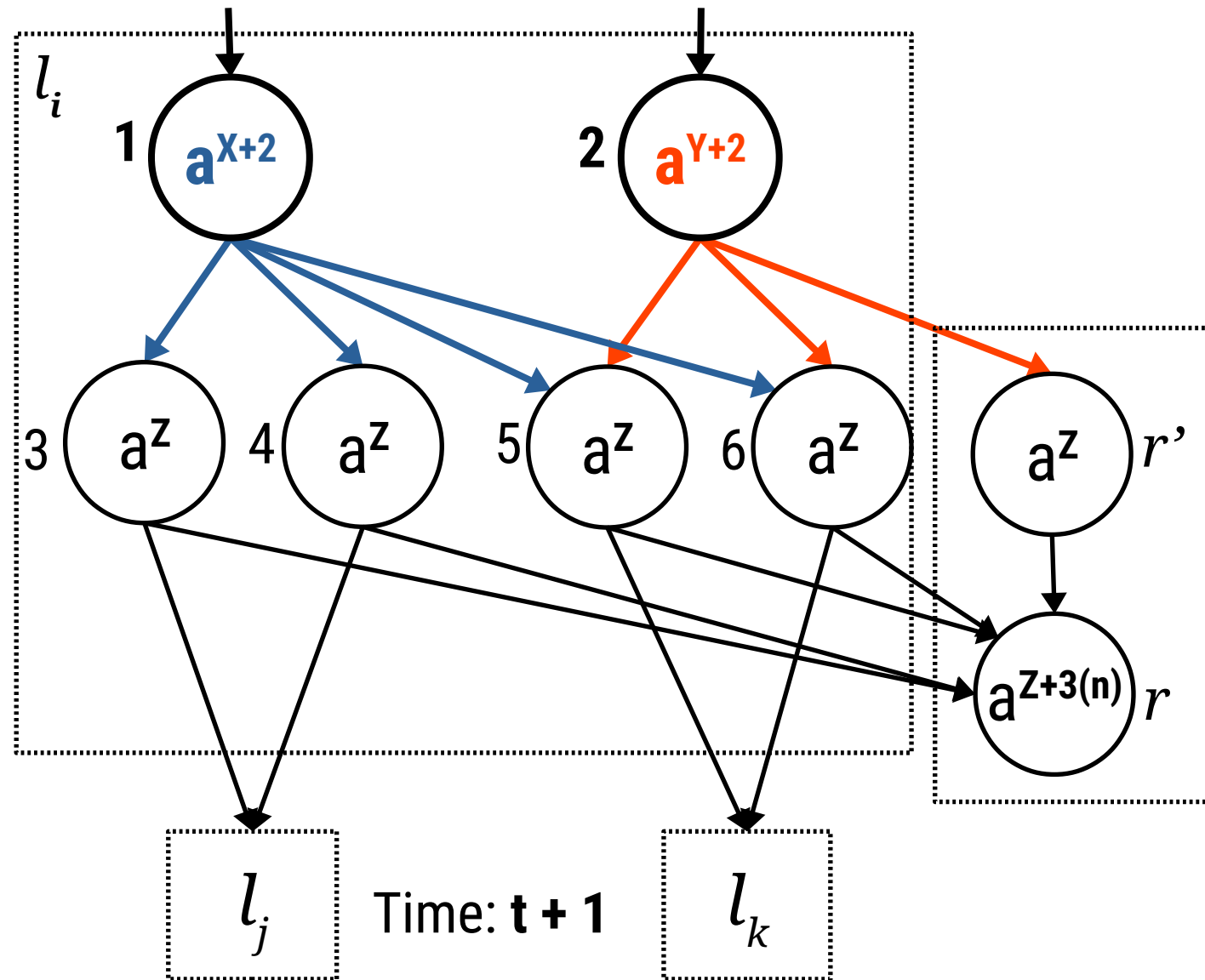
Rule 7: $a^{z+1} (a^3)^+ / a^4 \rightarrow \lambda$

Rule 8: $a^{z+2} (a^3)^+ / a^3 \rightarrow a$

Case 1: Rule 1 is activated.

ADD Module

l_i	ADD(r)	l_j	l_k
-------	------------	-------	-------



Rule 0: $a^{x+1} / a^1 \rightarrow \lambda$

Rule 1: $a^{x+2} / a^2 \rightarrow \lambda$

Rule 2: $a^{x+2} / a^2 \rightarrow a$

Rule 3: $a^{y+1} / a^1 \rightarrow \lambda$

Rule 4: $a^{y+2} / a^2 \rightarrow a$

Rule 5: $a^{z+1} / a^1 \rightarrow a$

Rule 6: $a^{z+2} / a^2 \rightarrow \lambda$

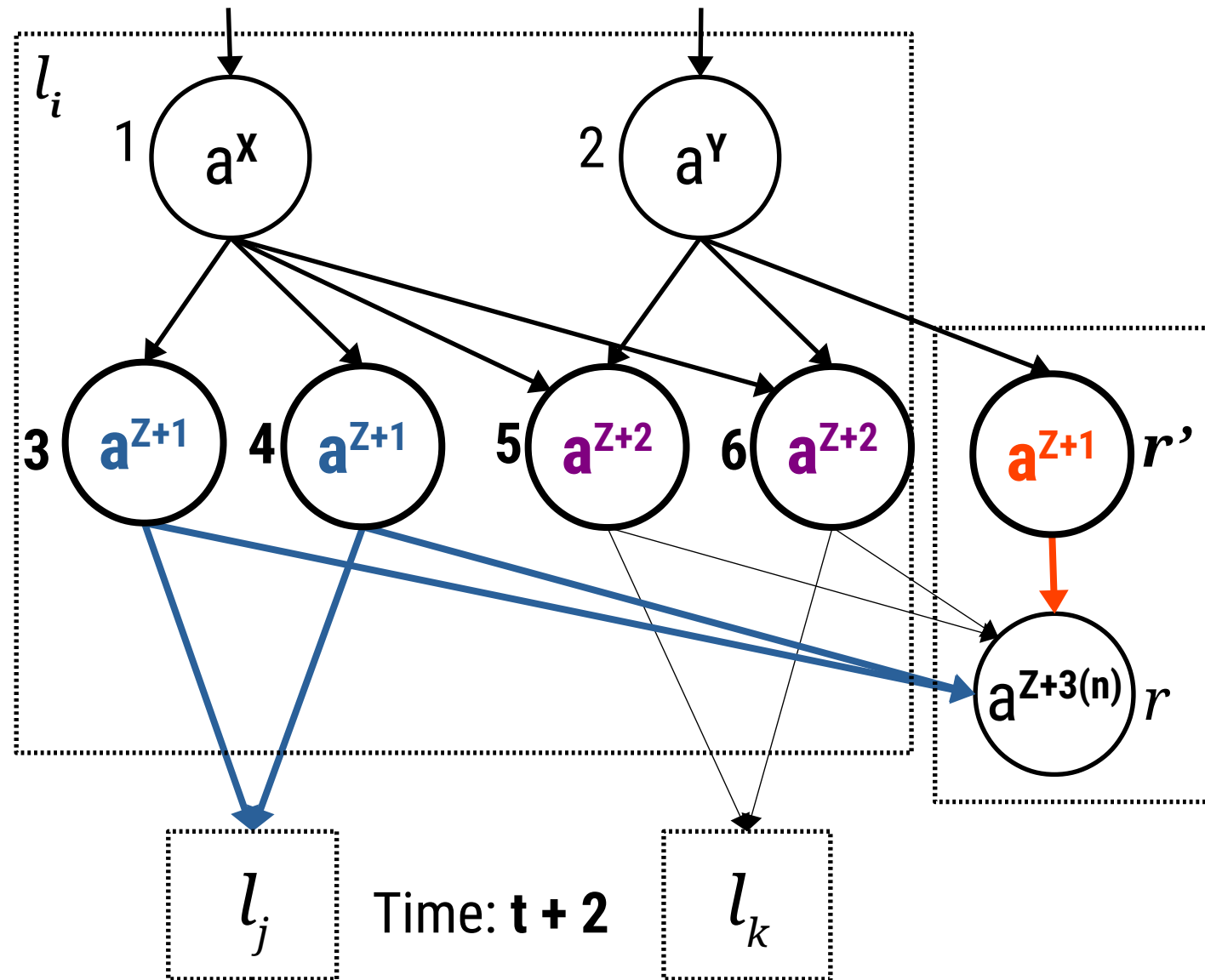
Rule 7: $a^{z+1} (a^3)^+ / a^4 \rightarrow \lambda$

Rule 8: $a^{z+2} (a^3)^+ / a^3 \rightarrow a$

Case 2: Rule 2 is activated.

ADD Module

l_i	ADD(r)	l_j	l_k
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Rule 0: $a^{x+1} / a^1 \rightarrow \lambda$

Rule 1: $a^{x+2} / a^2 \rightarrow \lambda$

Rule 2: $a^{x+2} / a^2 \rightarrow a$

Rule 3: $a^{y+1} / a^1 \rightarrow \lambda$

Rule 4: $a^{y+2} / a^2 \rightarrow a$

Rule 5: $a^{z+1} / a^1 \rightarrow a$

Rule 5: $a^{z+1} / a^1 \rightarrow a$

Rule 6: $a^{z+2} / a^2 \rightarrow \lambda$

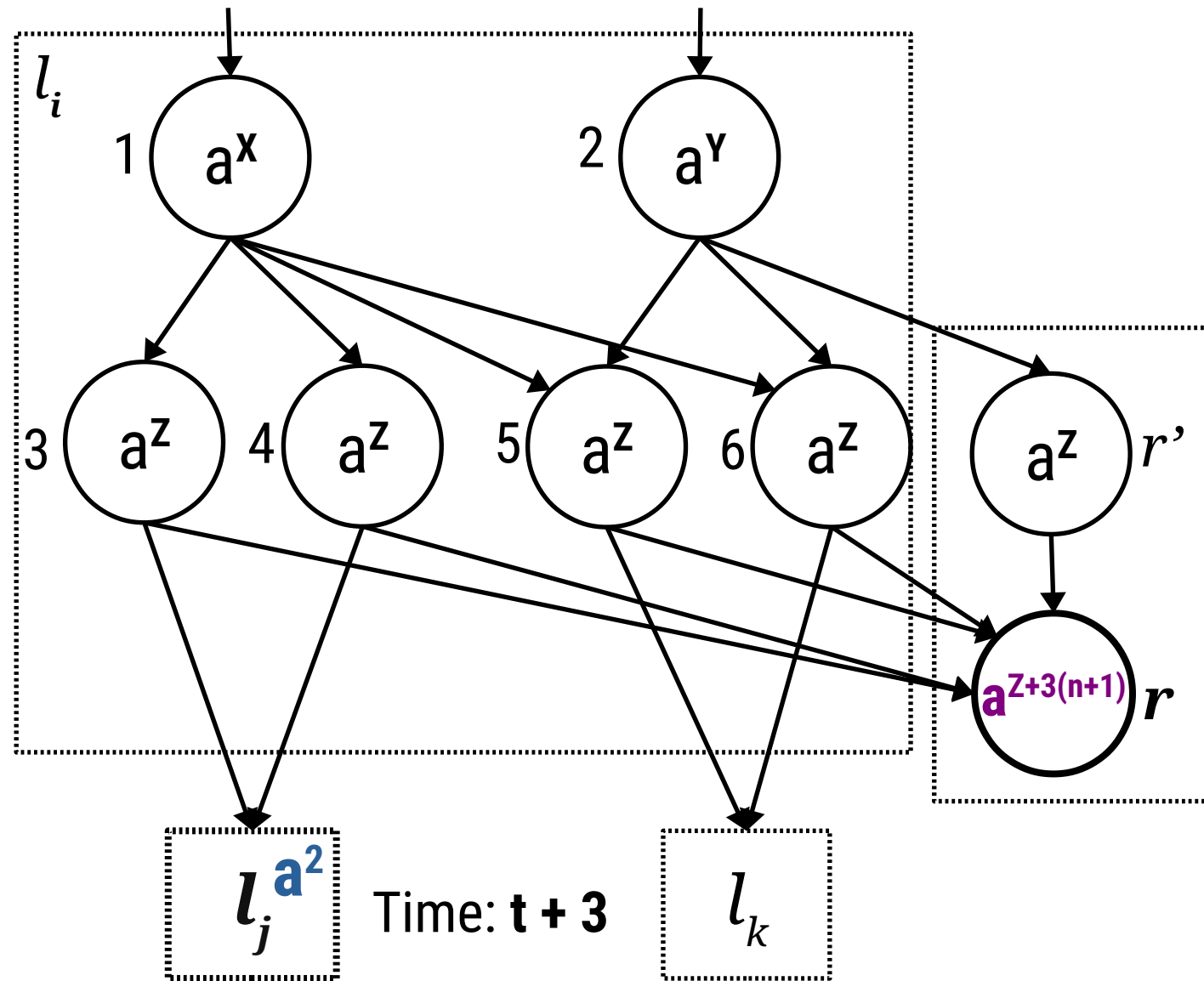
Rule 7: $a^{z+1} (a^3)^+ / a^4 \rightarrow \lambda$

Rule 8: $a^{z+2} (a^3)^+ / a^3 \rightarrow a$

Case 2: Rule 2 is activated.

ADD Module

l_i	ADD(r)	l_j	l_k
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Rule 0: $a^{x+1} / a^1 \rightarrow \lambda$

Rule 1: $a^{x+2} / a^2 \rightarrow \lambda$

Rule 2: $a^{x+2} / a^2 \rightarrow a$

Rule 3: $a^{y+1} / a^1 \rightarrow \lambda$

Rule 4: $a^{y+2} / a^2 \rightarrow a$

Rule 5: $a^{z+1} / a^1 \rightarrow a$

Rule 6: $a^{z+2} / a^2 \rightarrow \lambda$

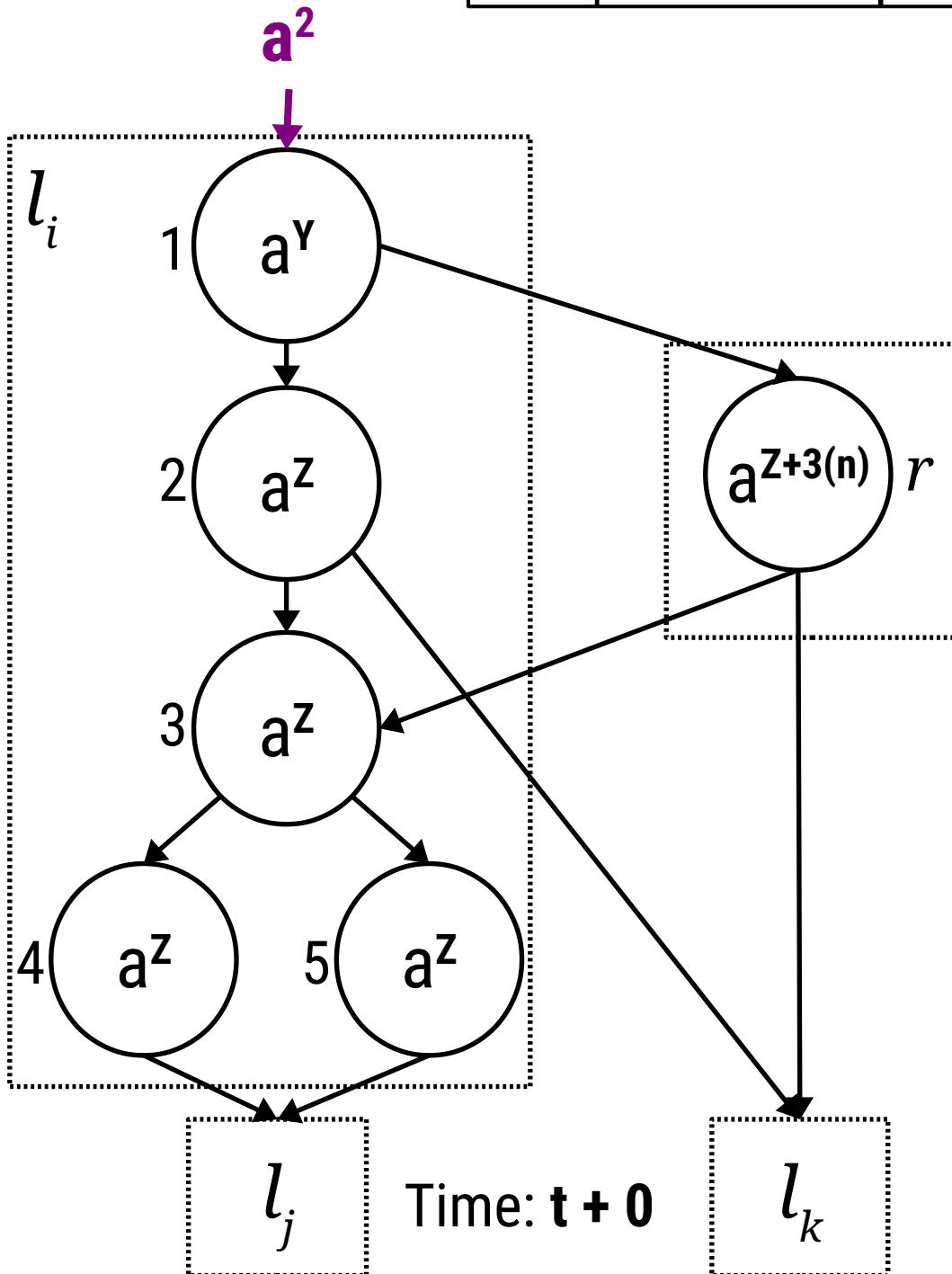
Rule 7: $a^{z+1} (a^3)^+ / a^4 \rightarrow \lambda$

Rule 8: $a^{z+2} (a^3)^+ / a^3 \rightarrow a$

Case 2: Rule 2 is activated.

SUB Module

l_i	SUB(r)	l_j	l_k
-------	----------------------------	-------	-------



Rule 0: $a^{x+1} / a^1 \rightarrow \lambda$

Rule 1: $a^{x+2} / a^2 \rightarrow \lambda$

Rule 2: $a^{x+2} / a^2 \rightarrow a$

Rule 3: $a^{y+1} / a^1 \rightarrow \lambda$

Rule 4: $a^{y+2} / a^2 \rightarrow a$

Rule 5: $a^{z+1} / a^1 \rightarrow a$

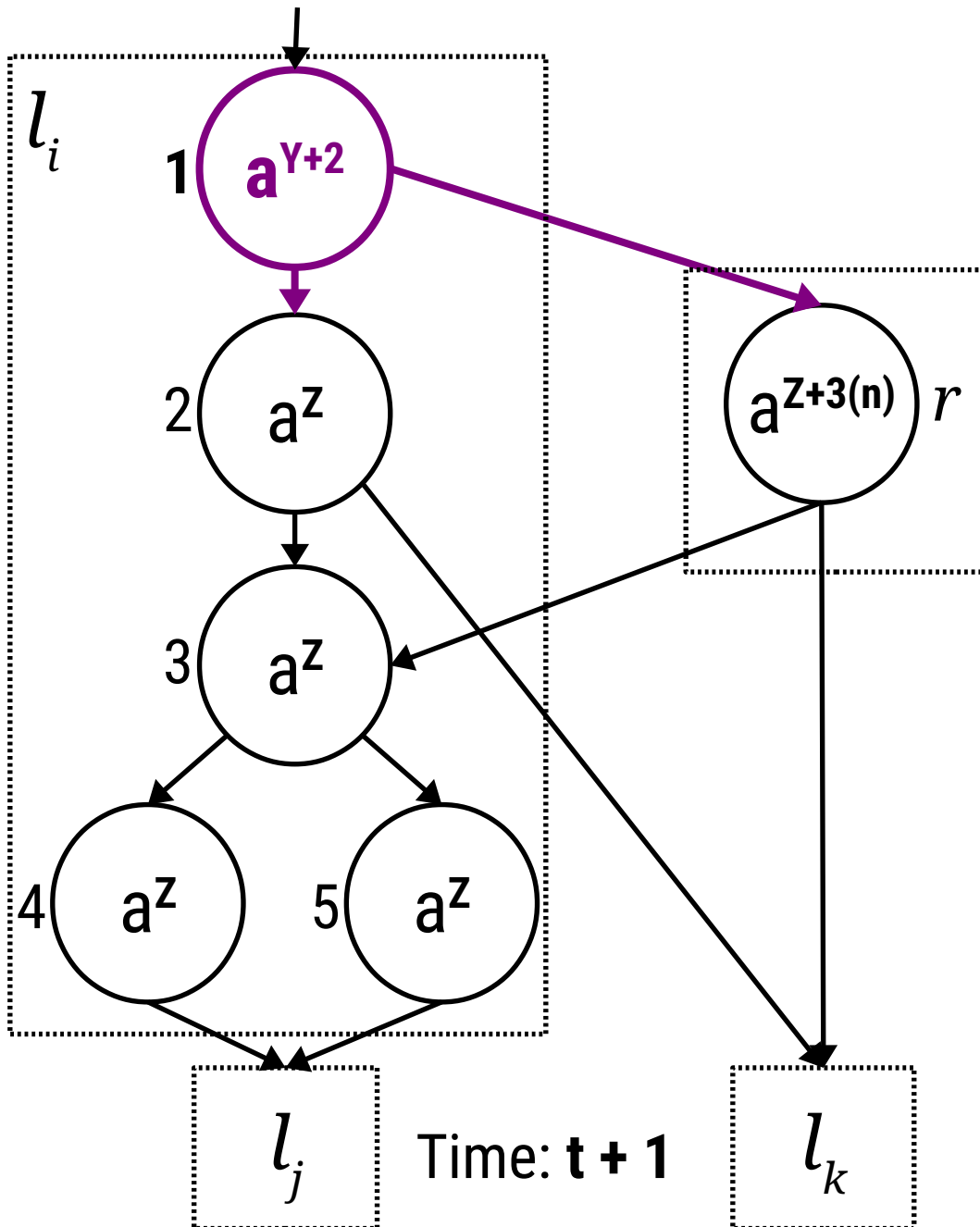
Rule 6: $a^{z+2} / a^2 \rightarrow \lambda$

Rule 7: $a^{z+1} (a^3)^+ / a^4 \rightarrow \lambda$

Rule 8: $a^{z+2} (a^3)^+ / a^3 \rightarrow a$

SUB Module

l_i	SUB(r)	l_j	l_k
-------	----------------------------	-------	-------



Rule 0: $a^{X+1} / a^1 \rightarrow \lambda$

Rule 1: $a^{X+2} / a^2 \rightarrow \lambda$

Rule 2: $a^{X+2} / a^2 \rightarrow a$

Rule 3: $a^{Y+1} / a^1 \rightarrow \lambda$

Rule 4: $a^{Y+2} / a^2 \rightarrow a$

Rule 5: $a^{Z+1} / a^1 \rightarrow a$

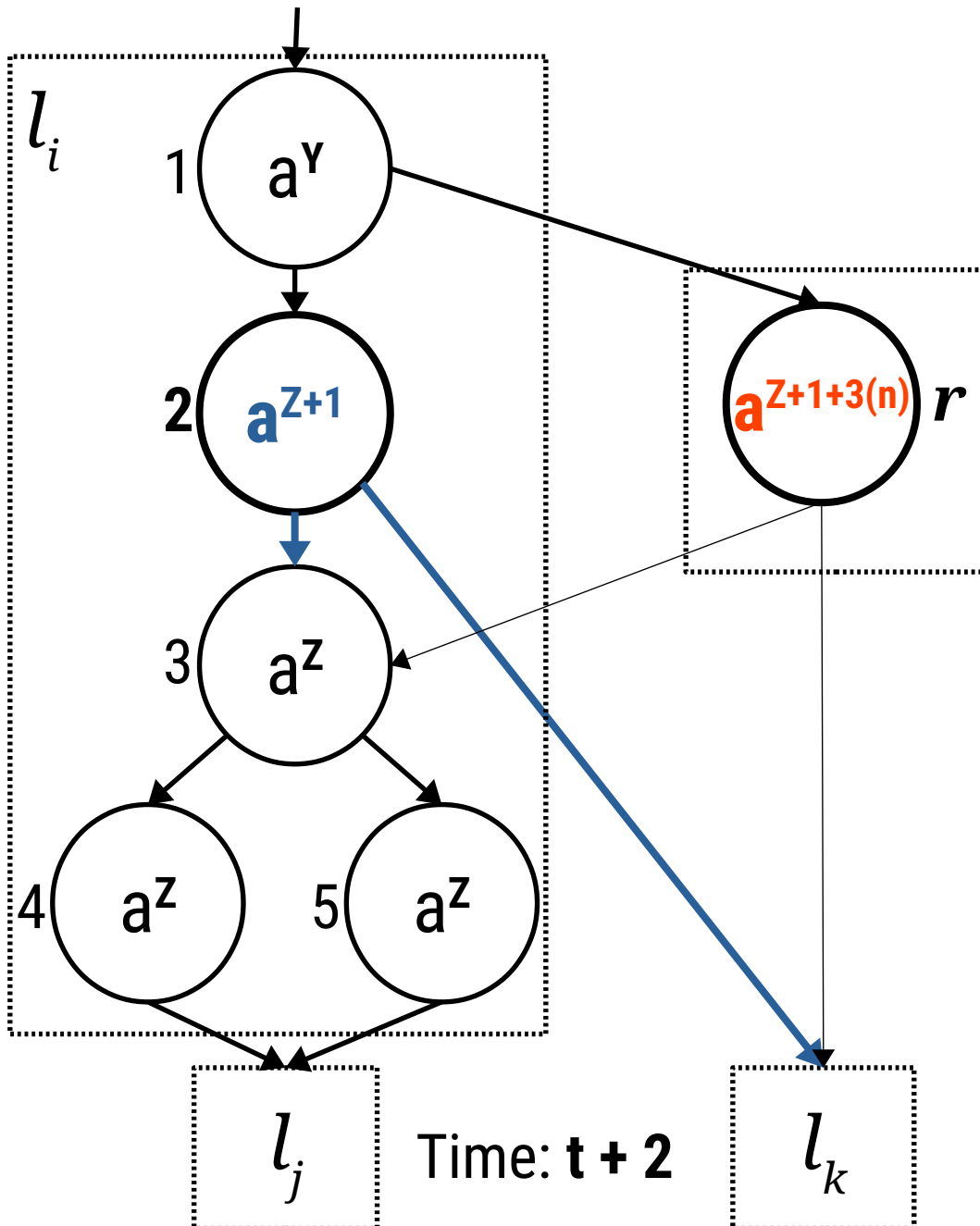
Rule 6: $a^{Z+2} / a^2 \rightarrow \lambda$

Rule 7: $a^{Z+1} (a^3)^+ / a^4 \rightarrow \lambda$

Rule 8: $a^{Z+2} (a^3)^+ / a^3 \rightarrow a$

SUB Module

l_i	SUB(r)	l_j	l_k
-------	----------------------------	-------	-------



Rule 0: $a^{x+1} / a^1 \rightarrow \lambda$

Rule 1: $a^{x+2} / a^2 \rightarrow \lambda$

Rule 2: $a^{x+2} / a^2 \rightarrow a$

Rule 3: $a^{y+1} / a^1 \rightarrow \lambda$

Rule 4: $a^{y+2} / a^2 \rightarrow a$

Rule 5: $a^{z+1} / a^1 \rightarrow a$

Rule 6: $a^{z+2} / a^2 \rightarrow \lambda$

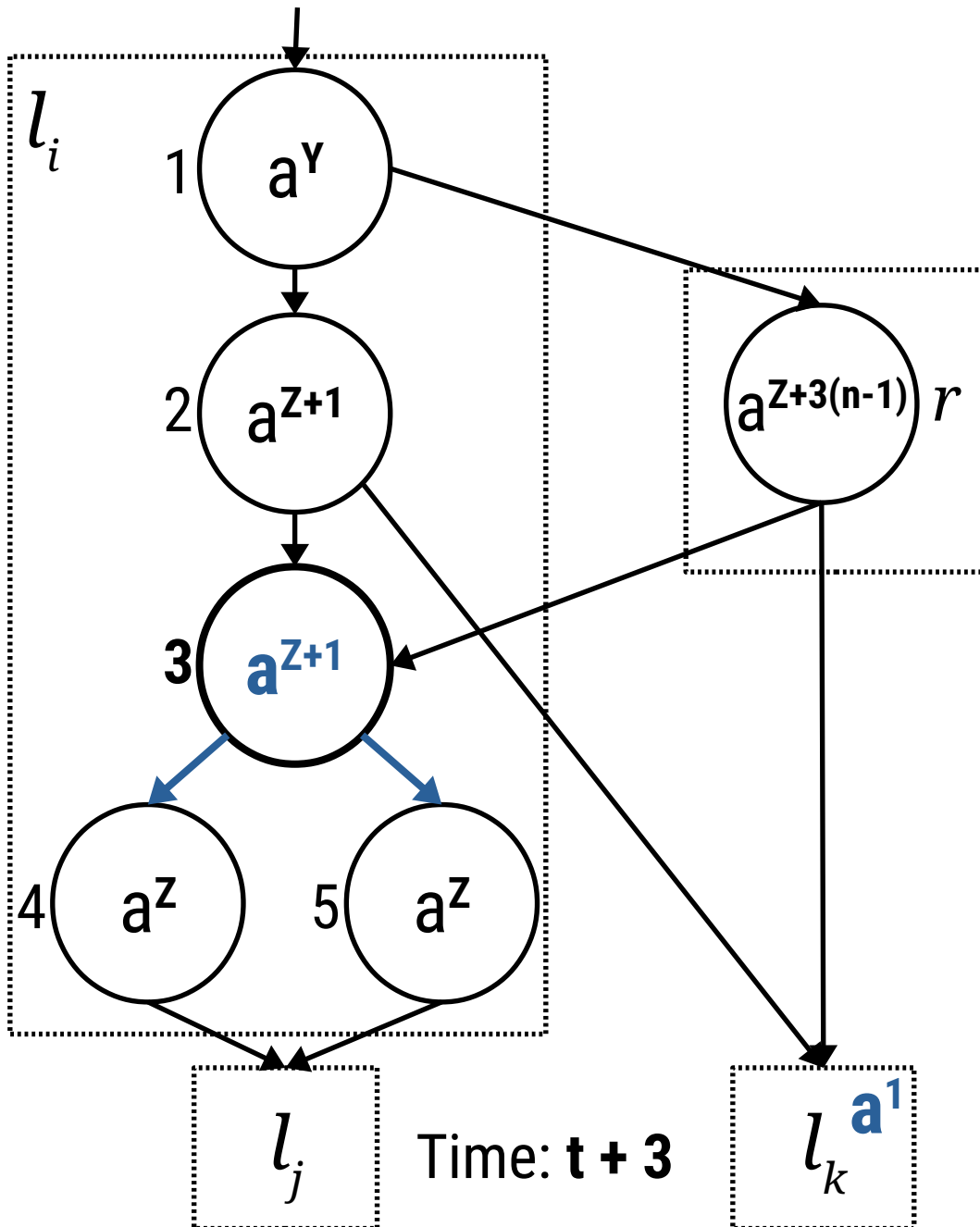
Rule 7: $a^{z+1} (a^3)^+ / a^4 \rightarrow \lambda$

Rule 8: $a^{z+2} (a^3)^+ / a^3 \rightarrow a$

Case 1: $n > 0$

SUB Module

l_i	SUB(r)	l_j	l_k
-------	----------------------------	-------	-------



Rule 0: $a^{x+1} / a^1 \rightarrow \lambda$

Rule 1: $a^{x+2} / a^2 \rightarrow \lambda$

Rule 2: $a^{x+2} / a^2 \rightarrow a$

Rule 3: $a^{y+1} / a^1 \rightarrow \lambda$

Rule 4: $a^{y+2} / a^2 \rightarrow a$

Rule 5: $a^{z+1} / a^1 \rightarrow a$

Rule 6: $a^{z+2} / a^2 \rightarrow \lambda$

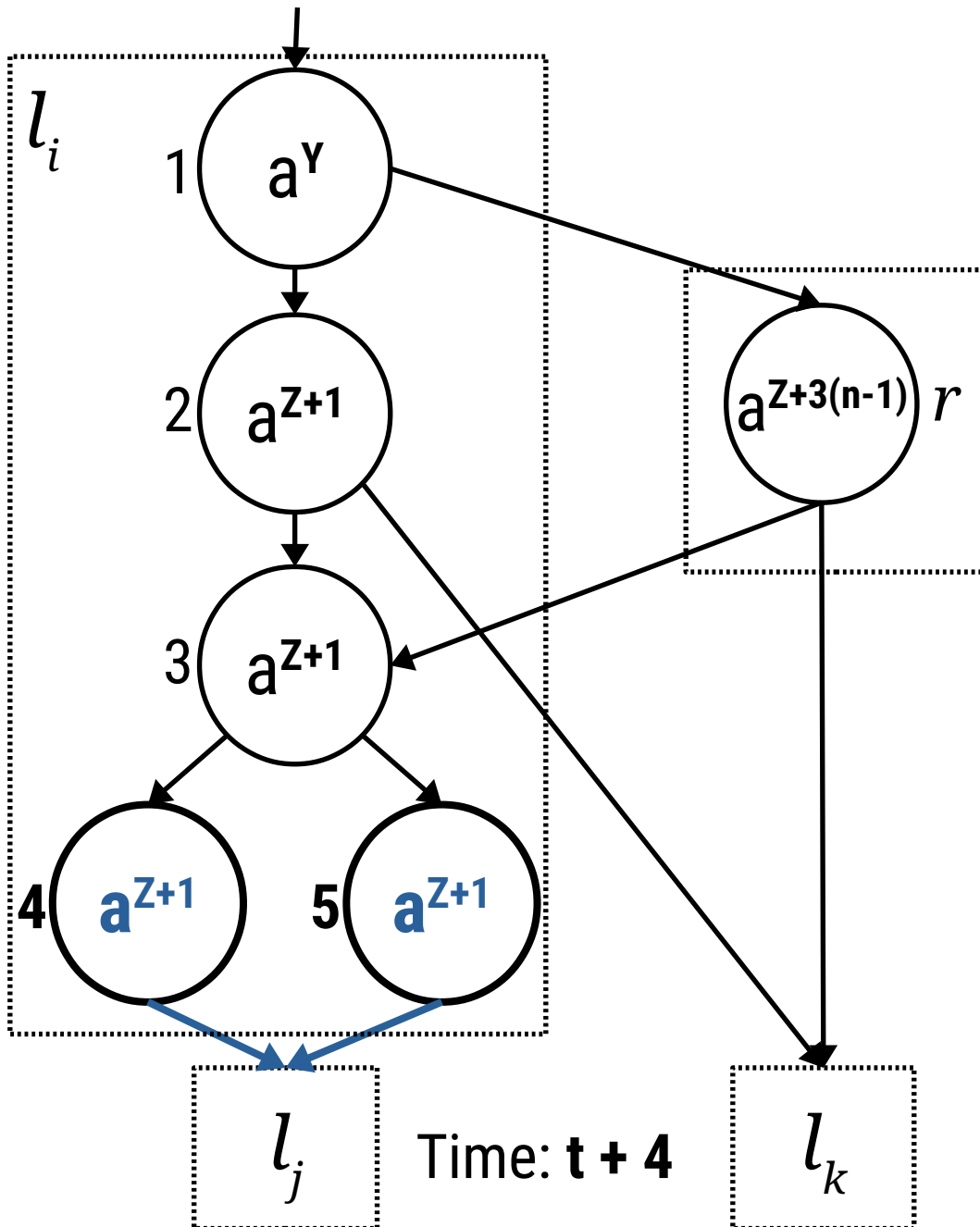
Rule 7: $a^{z+1} (a^3)^+ / a^4 \rightarrow \lambda$

Rule 8: $a^{z+2} (a^3)^+ / a^3 \rightarrow a$

Case 1: $n > 0$

SUB Module

l_i	SUB(r)	l_j	l_k
-------	----------------------------	-------	-------



Rule 0: $a^{x+1} / a^1 \rightarrow \lambda$

Rule 1: $a^{x+2} / a^2 \rightarrow \lambda$

Rule 2: $a^{x+2} / a^2 \rightarrow a$

Rule 3: $a^{y+1} / a^1 \rightarrow \lambda$

Rule 4: $a^{y+2} / a^2 \rightarrow a$

Rule 5: $a^{z+1} / a^1 \rightarrow a$

Rule 6: $a^{z+2} / a^2 \rightarrow \lambda$

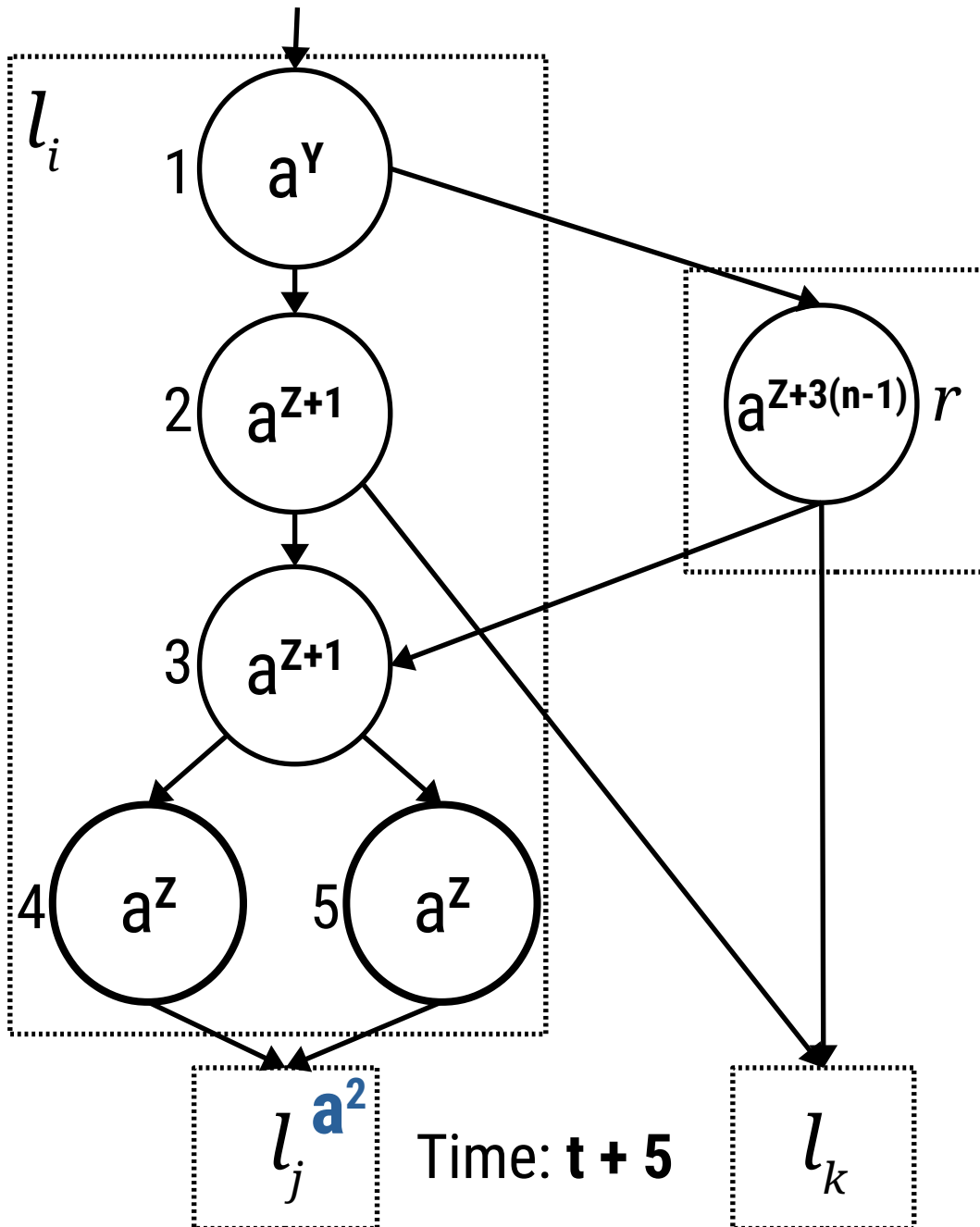
Rule 7: $a^{z+1} (a^3)^+ / a^4 \rightarrow \lambda$

Rule 8: $a^{z+2} (a^3)^+ / a^3 \rightarrow a$

Case 1: $n > 0$

SUB Module

l_i	SUB(r)	l_j	l_k
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Rule 0: $a^{x+1} / a^1 \rightarrow \lambda$

Rule 1: $a^{x+2} / a^2 \rightarrow \lambda$

Rule 2: $a^{x+2} / a^2 \rightarrow a$

Rule 3: $a^{y+1} / a^1 \rightarrow \lambda$

Rule 4: $a^{y+2} / a^2 \rightarrow a$

Rule 5: $a^{z+1} / a^1 \rightarrow a$

Rule 6: $a^{z+2} / a^2 \rightarrow \lambda$

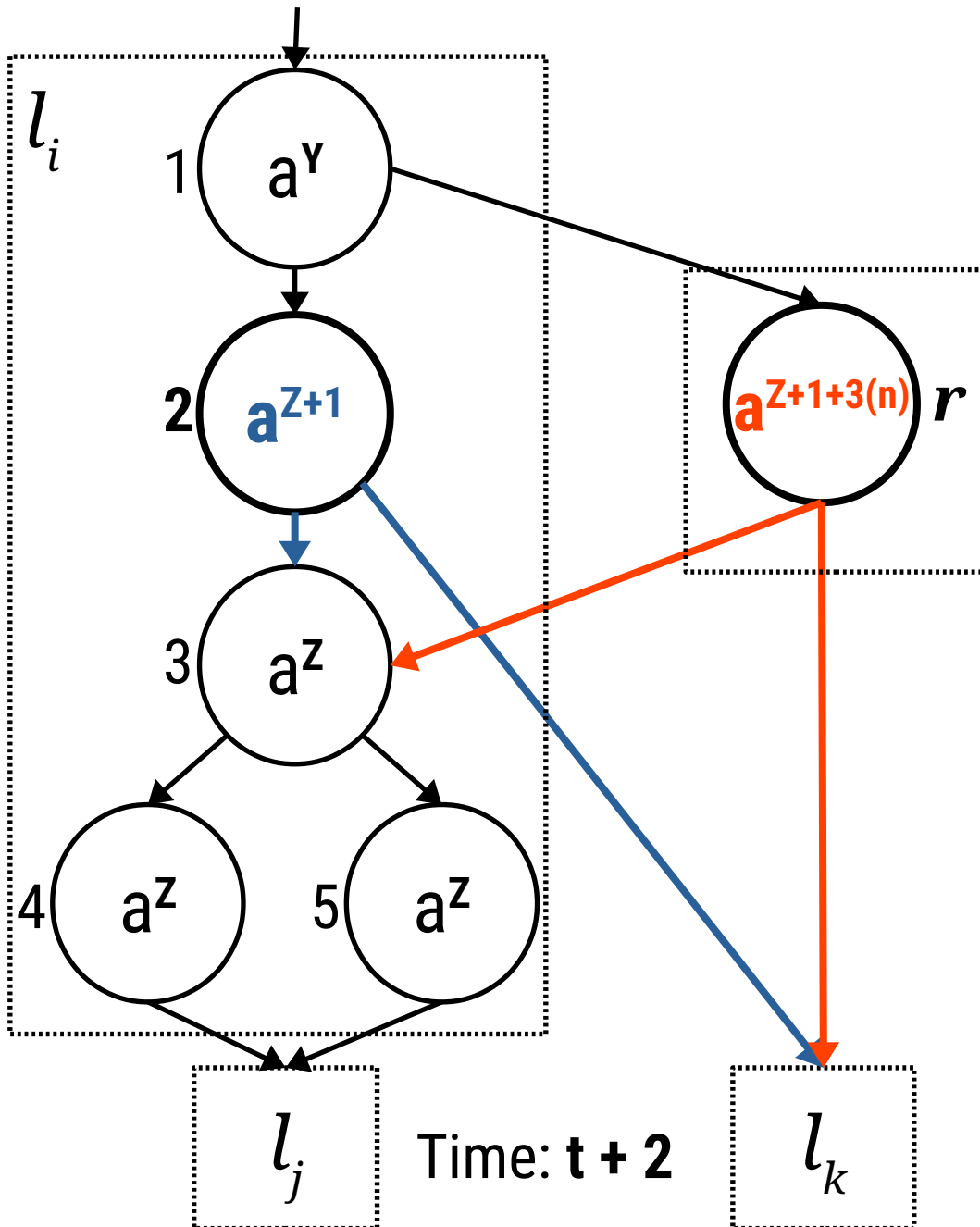
Rule 7: $a^{z+1} (a^3)^+ / a^4 \rightarrow \lambda$

Rule 8: $a^{z+2} (a^3)^+ / a^3 \rightarrow a$

Case 1: $n > 0$

SUB Module

l_i	SUB(r)	l_j	l_k
-------	----------------------------	-------	-------



Rule 0: $a^{x+1} / a^1 \rightarrow \lambda$

Rule 1: $a^{x+2} / a^2 \rightarrow \lambda$

Rule 2: $a^{x+2} / a^2 \rightarrow a$

Rule 3: $a^{y+1} / a^1 \rightarrow \lambda$

Rule 4: $a^{y+2} / a^2 \rightarrow a$

Rule 5: $a^{z+1} / a^1 \rightarrow a$ (Blue label)

Rule 5: $a^{z+1} / a^1 \rightarrow a$ (Red label)

Rule 6: $a^{z+2} / a^2 \rightarrow \lambda$

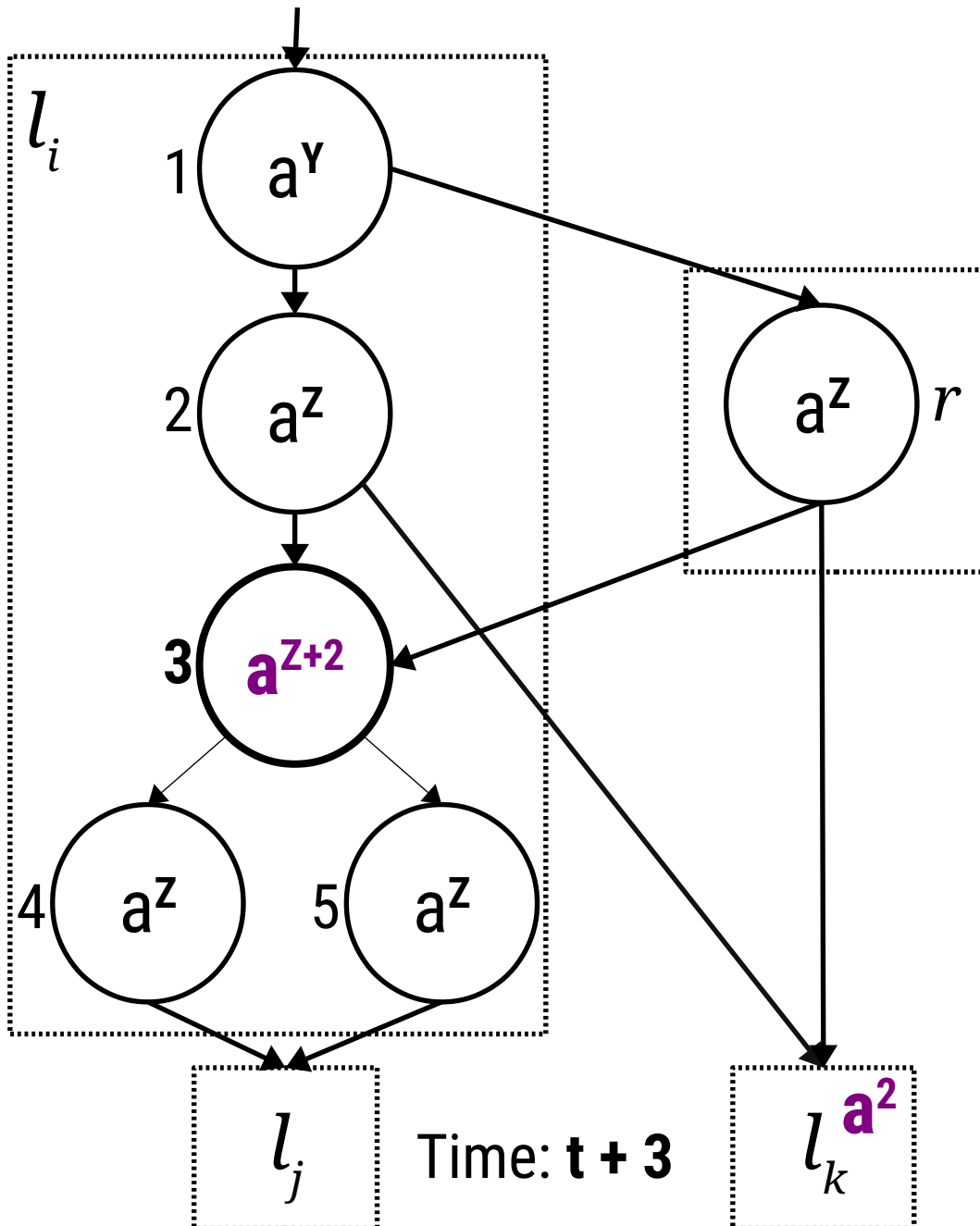
Rule 7: $a^{z+1} (a^3)^+ / a^4 \rightarrow \lambda$

Rule 8: $a^{z+2} (a^3)^+ / a^3 \rightarrow a$

Case 2: $n = 0$

SUB Module

l_i	SUB(r)	l_j	l_k
-------	----------------------------	-------	-------



Rule 0: $a^{x+1} / a^1 \rightarrow \lambda$

Rule 1: $a^{x+2} / a^2 \rightarrow \lambda$

Rule 2: $a^{x+2} / a^2 \rightarrow a$

Rule 3: $a^{y+1} / a^1 \rightarrow \lambda$

Rule 4: $a^{y+2} / a^2 \rightarrow a$

Rule 5: $a^{z+1} / a^1 \rightarrow a$

Rule 6: $a^{z+2} / a^2 \rightarrow \lambda$

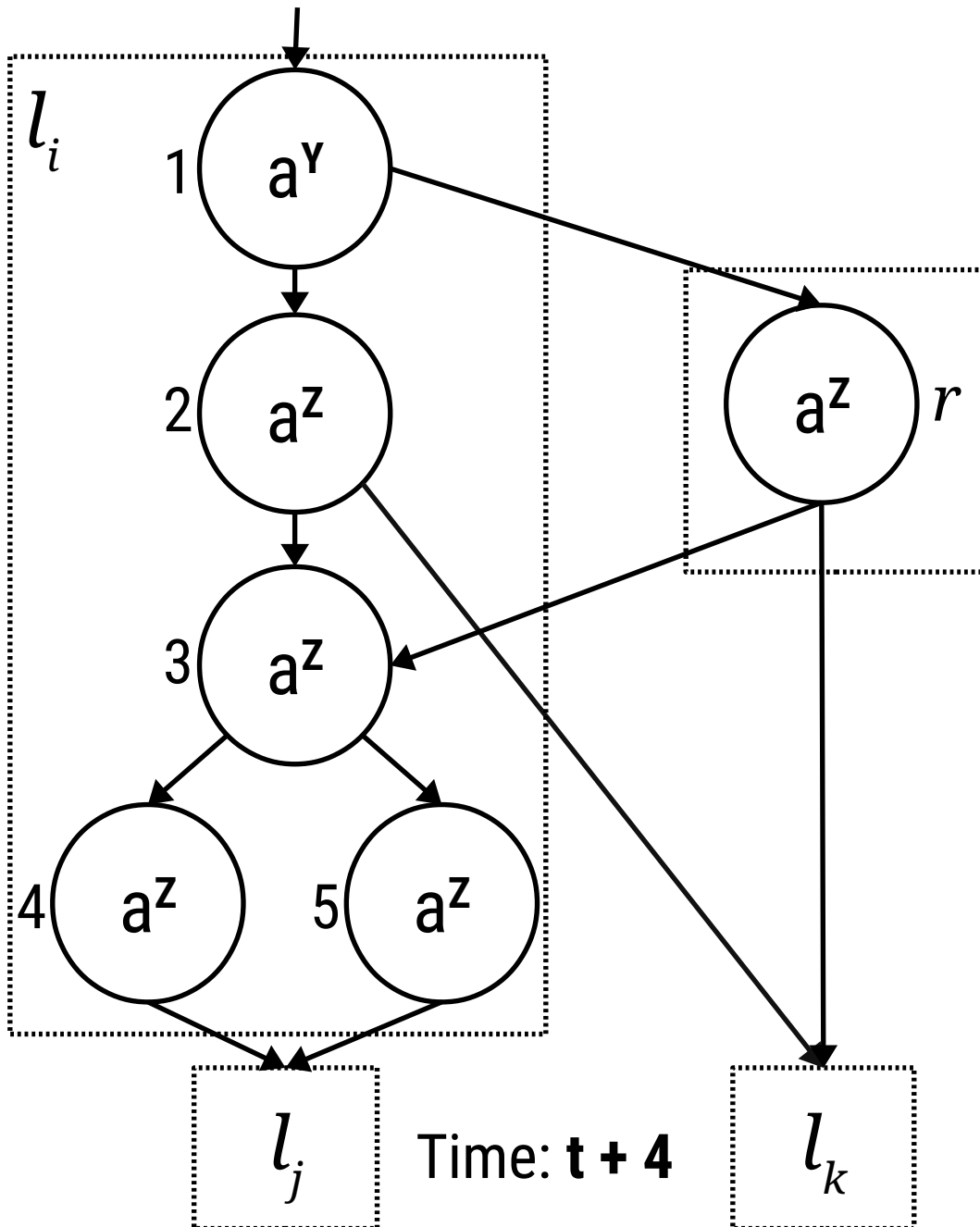
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SUB Module

l_i	SUB(r)	l_j	l_k
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Rule 1: $a^{x+2} / a^2 \rightarrow \lambda$

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Rule 3: $a^{y+1} / a^1 \rightarrow \lambda$

Rule 4: $a^{y+2} / a^2 \rightarrow a$

Rule 5: $a^{z+1} / a^1 \rightarrow a$

Rule 6: $a^{z+2} / a^2 \rightarrow \lambda$

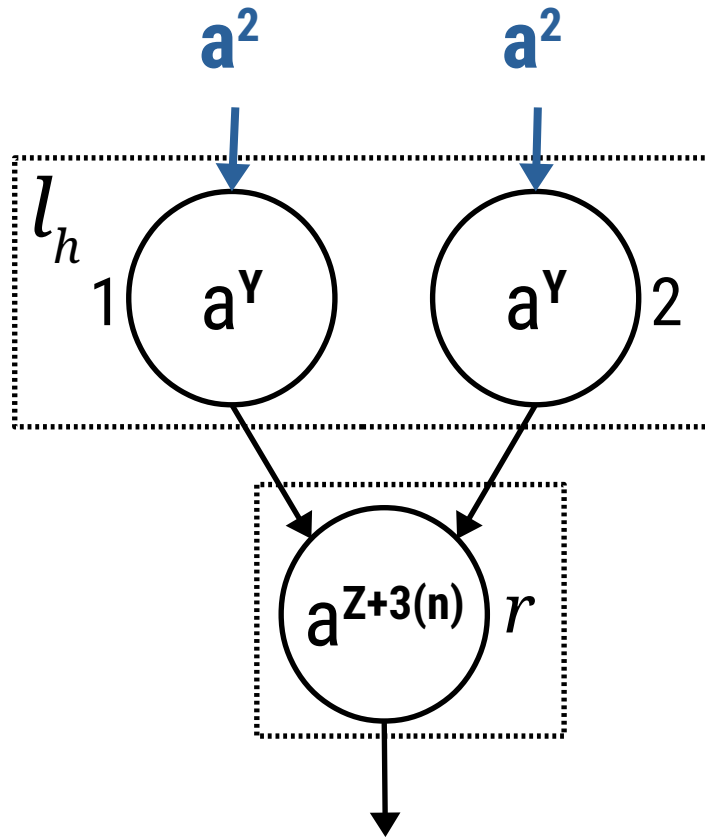
Rule 7: $a^{z+1} (a^3)^+ / a^4 \rightarrow \lambda$

Rule 8: $a^{z+2} (a^3)^+ / a^3 \rightarrow a$

Case 2: $n = 0$

HALT Module

l_h	HALT
-------	------



Time: $t + 0$

Rule 0: $a^{x+1} / a^1 \rightarrow \lambda$

Rule 1: $a^{x+2} / a^2 \rightarrow \lambda$

Rule 2: $a^{x+2} / a^2 \rightarrow a$

Rule 3: $a^{y+1} / a^1 \rightarrow \lambda$

Rule 4: $a^{y+2} / a^2 \rightarrow a$

Rule 5: $a^{z+1} / a^1 \rightarrow a$

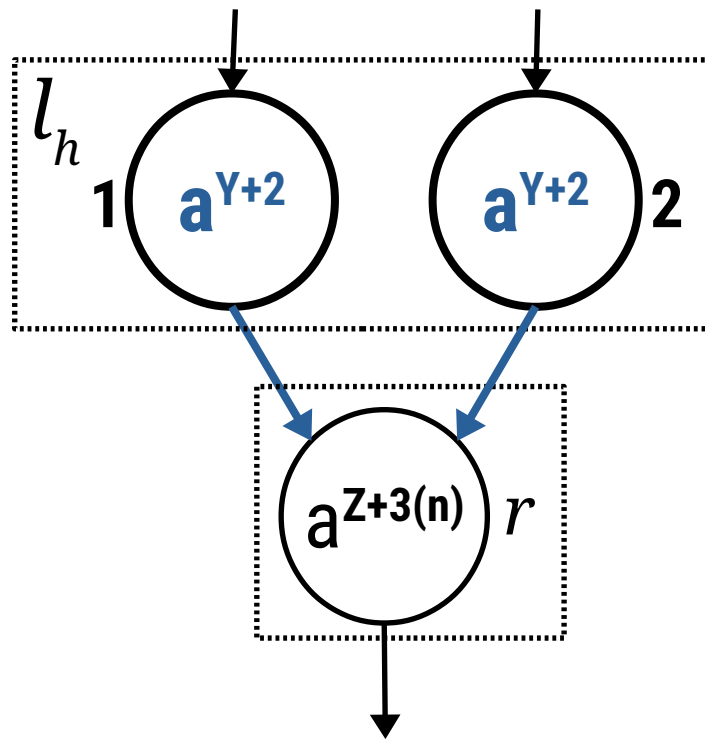
Rule 6: $a^{z+2} / a^2 \rightarrow \lambda$

Rule 7: $a^{z+1} (a^3)^+ / a^4 \rightarrow \lambda$

Rule 8: $a^{z+2} (a^3)^+ / a^3 \rightarrow a$

HALT Module

l_h	HALT
-------	------



Time: $t + 1$

Rule 0: $a^{X+1} / a^1 \rightarrow \lambda$

Rule 1: $a^{X+2} / a^2 \rightarrow \lambda$

Rule 2: $a^{X+2} / a^2 \rightarrow a$

Rule 3: $a^{Y+1} / a^1 \rightarrow \lambda$

Rule 4: $a^{Y+2} / a^2 \rightarrow a$

Rule 5: $a^{Z+1} / a^1 \rightarrow a$

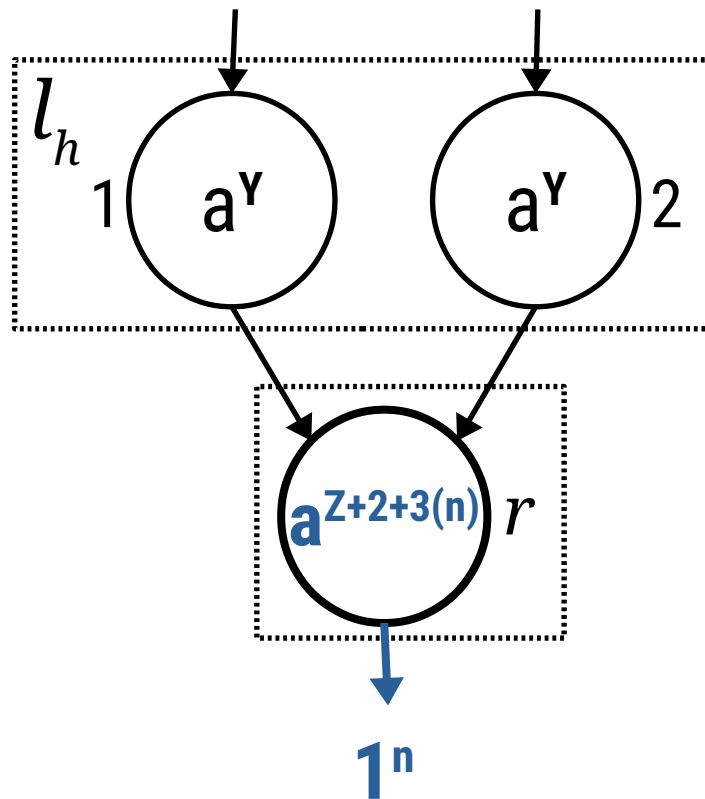
Rule 6: $a^{Z+2} / a^2 \rightarrow \lambda$

Rule 7: $a^{Z+1} (a^3)^+ / a^4 \rightarrow \lambda$

Rule 8: $a^{Z+2} (a^3)^+ / a^3 \rightarrow a$

HALT Module

l_h	HALT
-------	------



Time: $t + 2$

to

Time: $t + n + 1$

Rule 0: $a^{x+1} / a^1 \rightarrow \lambda$

Rule 1: $a^{x+2} / a^2 \rightarrow \lambda$

Rule 2: $a^{x+2} / a^2 \rightarrow a$

Rule 3: $a^{y+1} / a^1 \rightarrow \lambda$

Rule 4: $a^{y+2} / a^2 \rightarrow a$

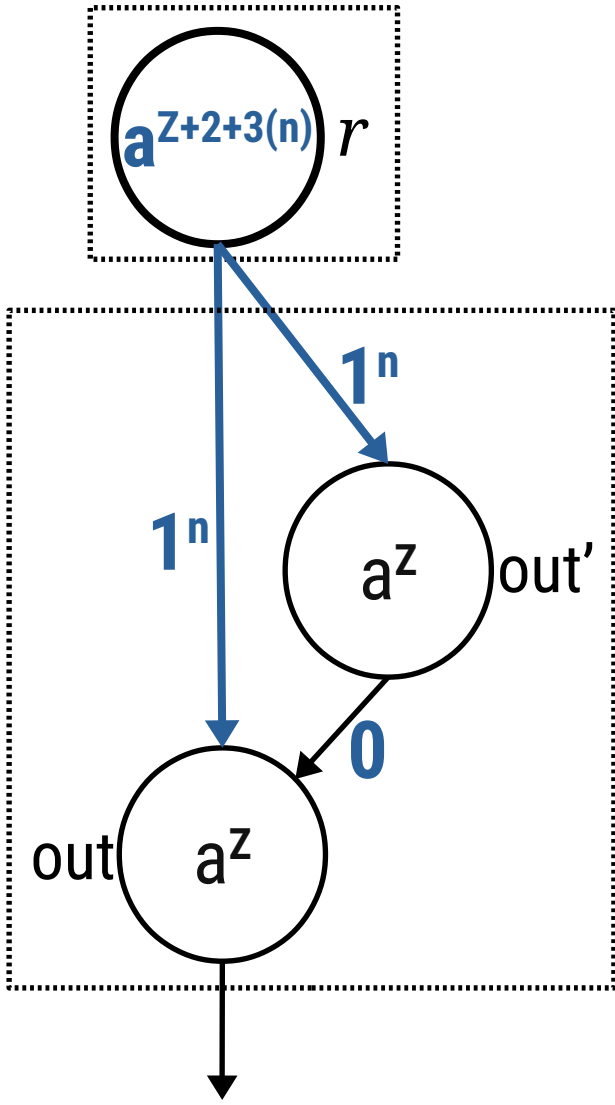
Rule 5: $a^{z+1} / a^1 \rightarrow a$

Rule 6: $a^{z+2} / a^2 \rightarrow \lambda$

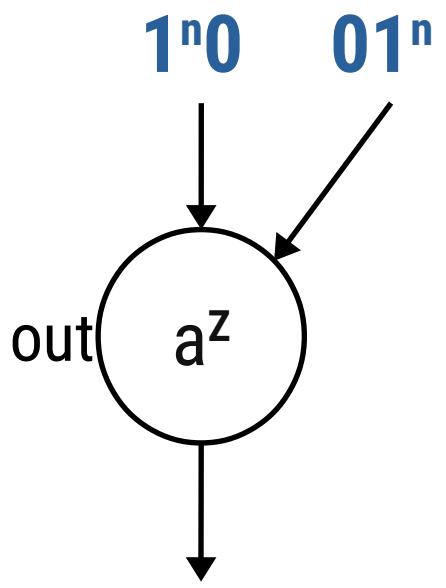
Rule 7: $a^{z+1} (a^3)^+ / a^4 \rightarrow \lambda$

Rule 8: $a^{z+2} (a^3)^+ / a^3 \rightarrow a$

OUTPUT Module



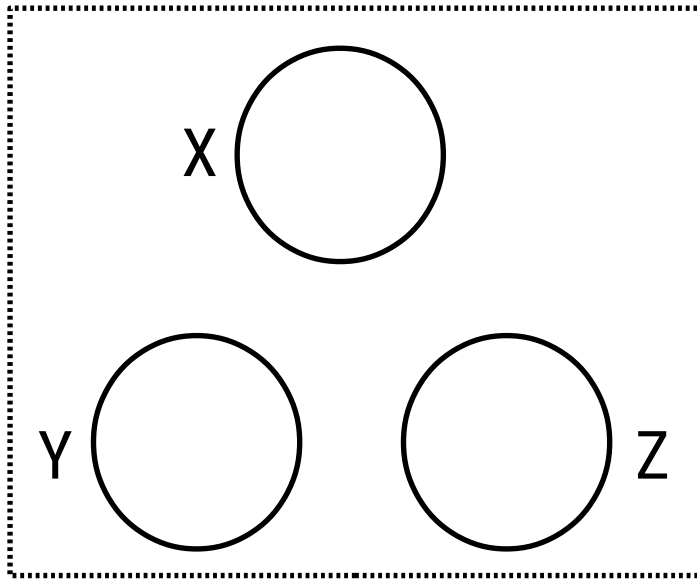
r	1^n	0	
out'	0	1^n	
out	1	2^{n-1}	1
out	1	0^{n-1}	1



- Rule 0: $a^{x+1} / a^1 \rightarrow \lambda$
Rule 1: $a^{x+2} / a^2 \rightarrow \lambda$
Rule 2: $a^{x+2} / a^2 \rightarrow a$
- Rule 3: $a^{y+1} / a^1 \rightarrow \lambda$
Rule 4: $a^{y+2} / a^2 \rightarrow a$
- Rule 5:** $a^{z+1} / a^1 \rightarrow a$
Rule 6: $a^{z+2} / a^2 \rightarrow \lambda$
Rule 7: $a^{z+1} (a^3)^+ / a^4 \rightarrow \lambda$
Rule 8: $a^{z+2} (a^3)^+ / a^3 \rightarrow a$

Discussion: On why plasticity rules are only used as forgetting rules.

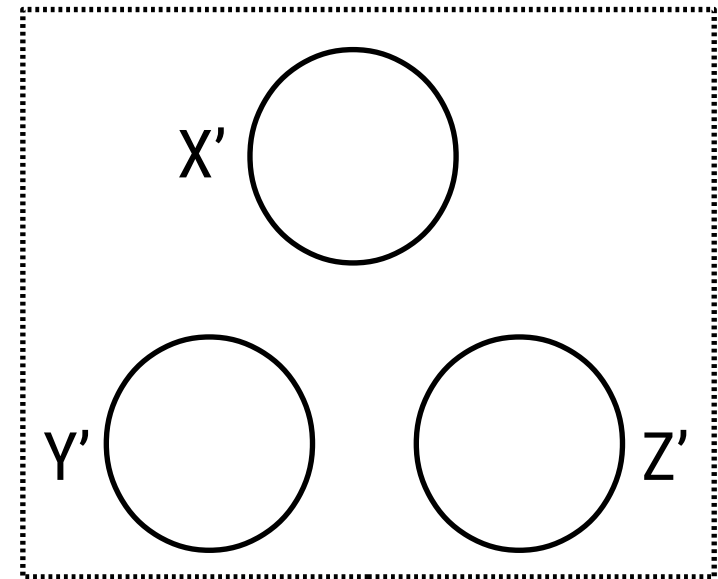
Module A



In neuron X:

Rule 1: $E / a^c \rightarrow +2(\{Y, Z\})$

Module A'

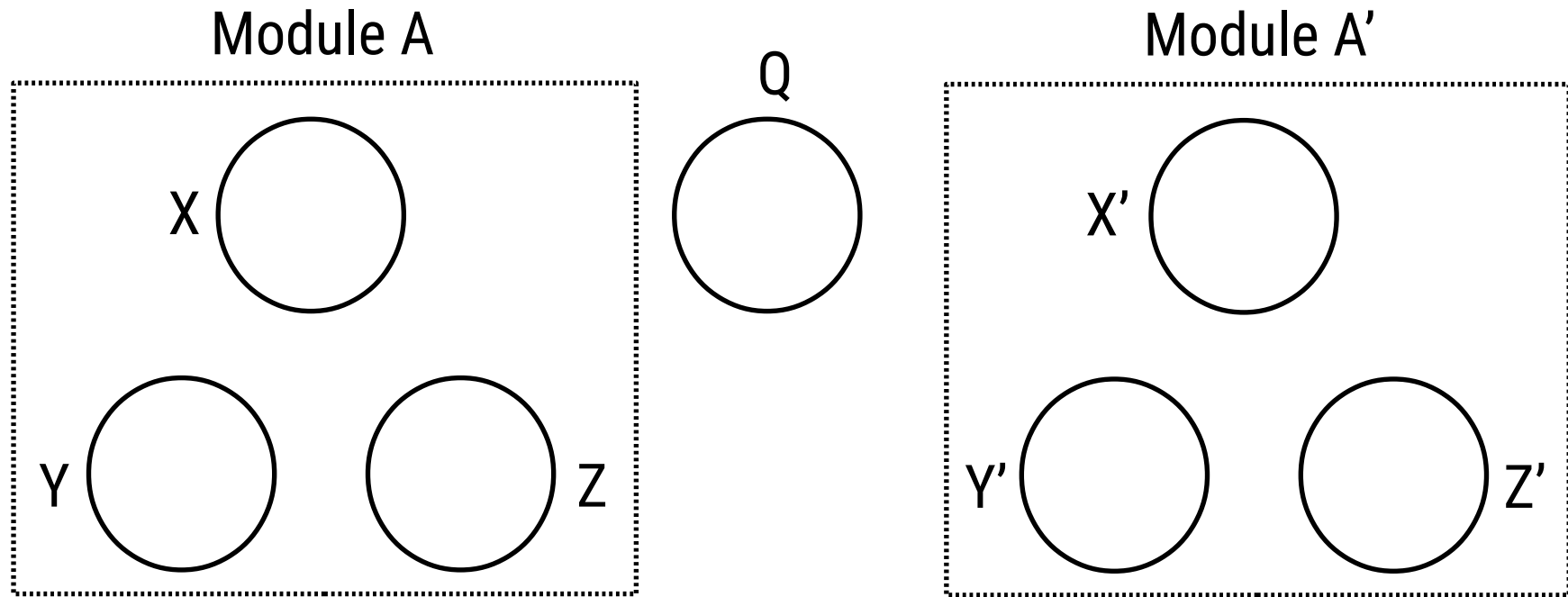


In neuron X':

Rule 1': $E / a^c \rightarrow +2(\{Y', Z'\})$

Neuron X' can not reuse Rule 1 of neuron X.
Neuron X can not reuse Rule 1' of neuron X'.

Discussion: On why plasticity rules are only used as forgetting rules.



In neuron X:

Rule 1: $E / a^c \rightarrow -1(\{Q\})$

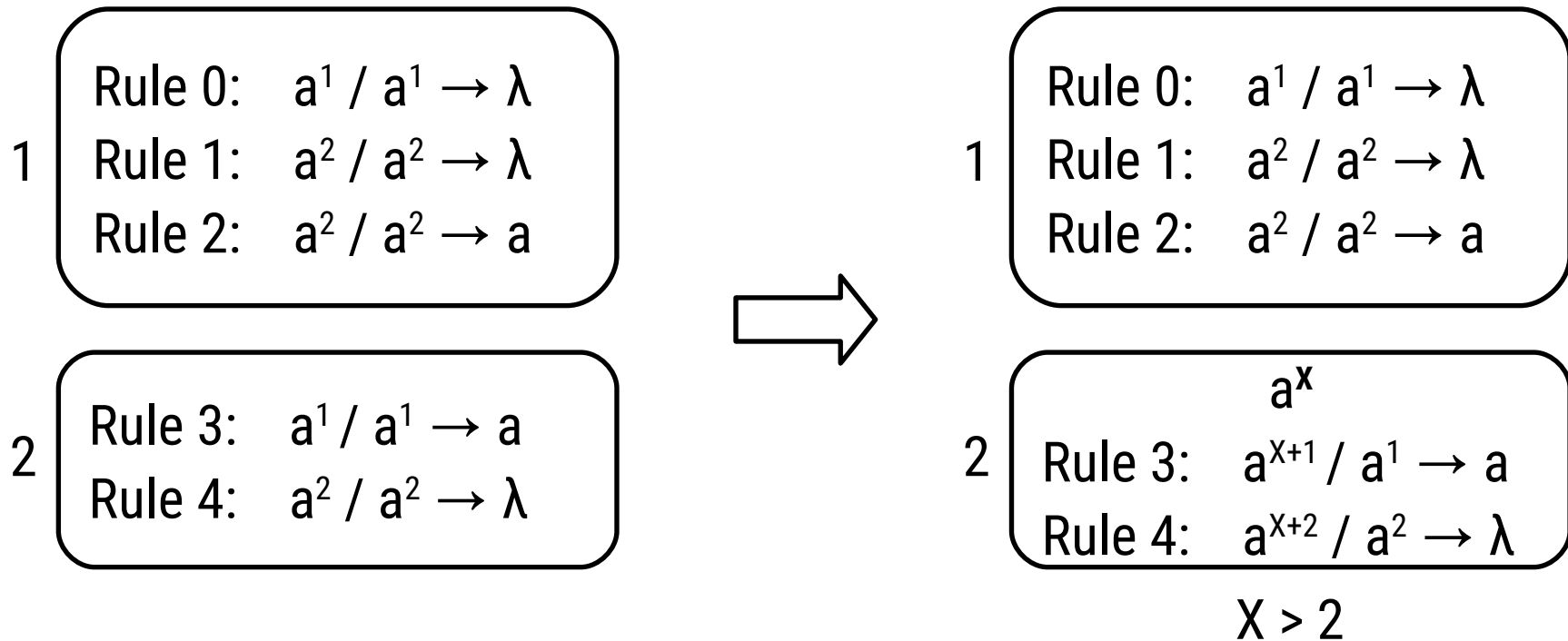
Rule 1: $E / a^c \rightarrow \lambda$

In neuron X':

Rule 1': $E / a^c \rightarrow -1(\{Q\})$

Rule 1': $E / a^c \rightarrow \lambda$

Discussion: On “translating” rules



You can easily create a common set of rules by “translating” different rule sets then combining them and adding the appropriate initial spike counts to the neurons.

Discussion: On “translating” rules

Rule 0: $a^{X+1} / a^1 \rightarrow \lambda$

Rule 1: $a^{X+2} / a^2 \rightarrow \lambda$

Rule 2: $a^{X+2} / a^2 \rightarrow a$

Rule 3: $a^{Y+1} / a^1 \rightarrow \lambda$

Rule 4: $a^{Y+2} / a^2 \rightarrow a$

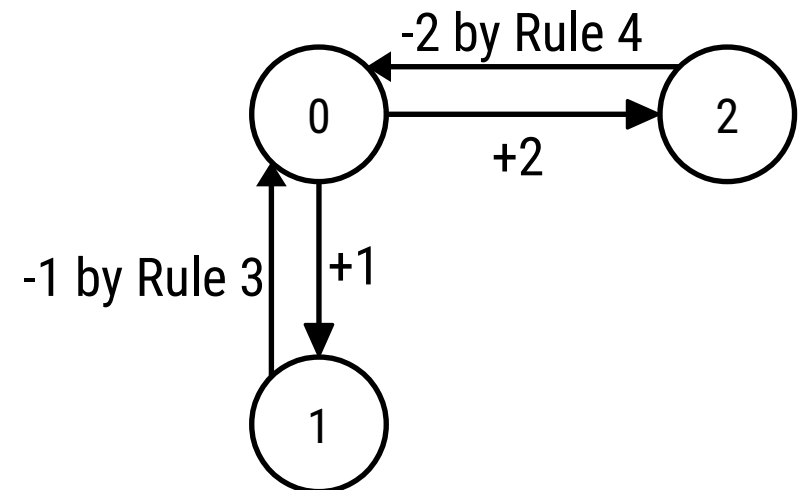
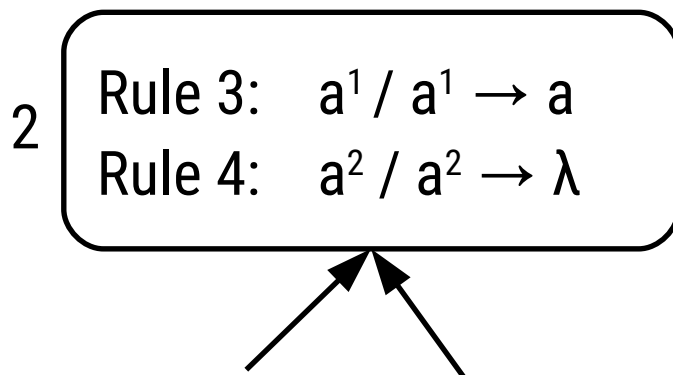
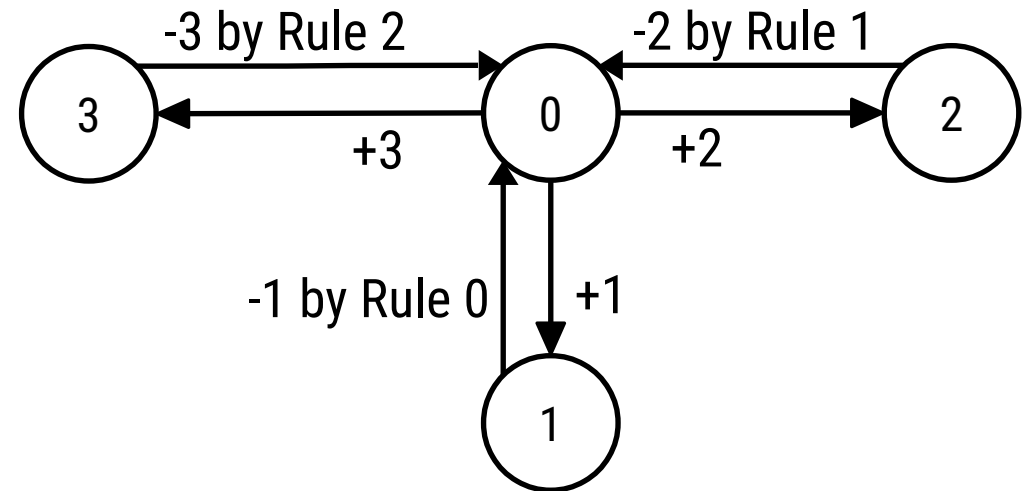
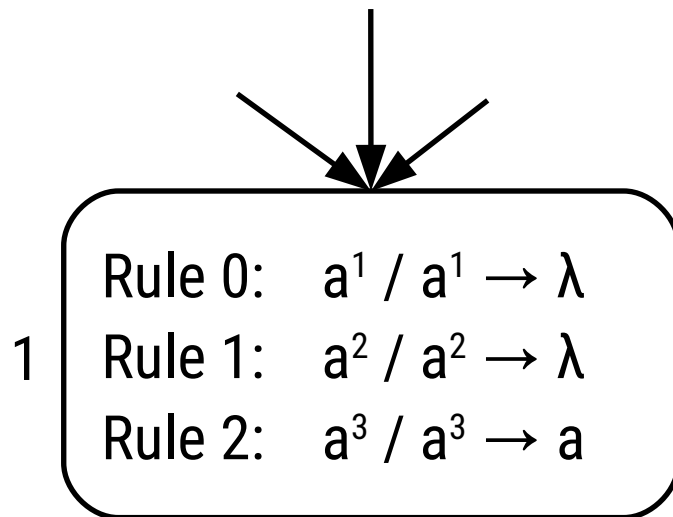
Rule 5: $a^{Z+1} / a^1 \rightarrow a$

Rule 6: $a^{Z+2} / a^2 \rightarrow \lambda$

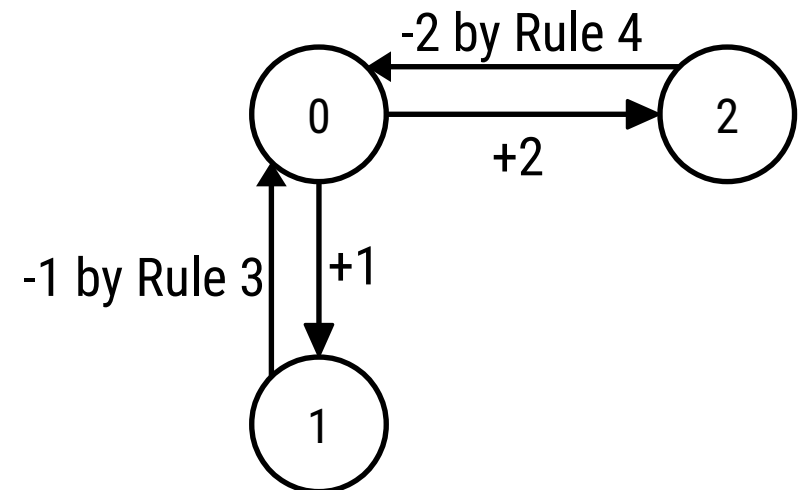
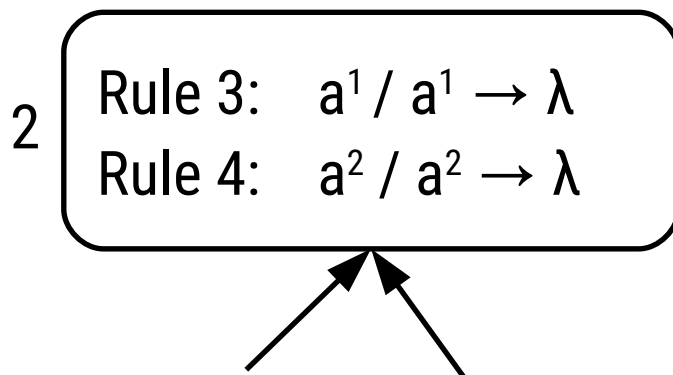
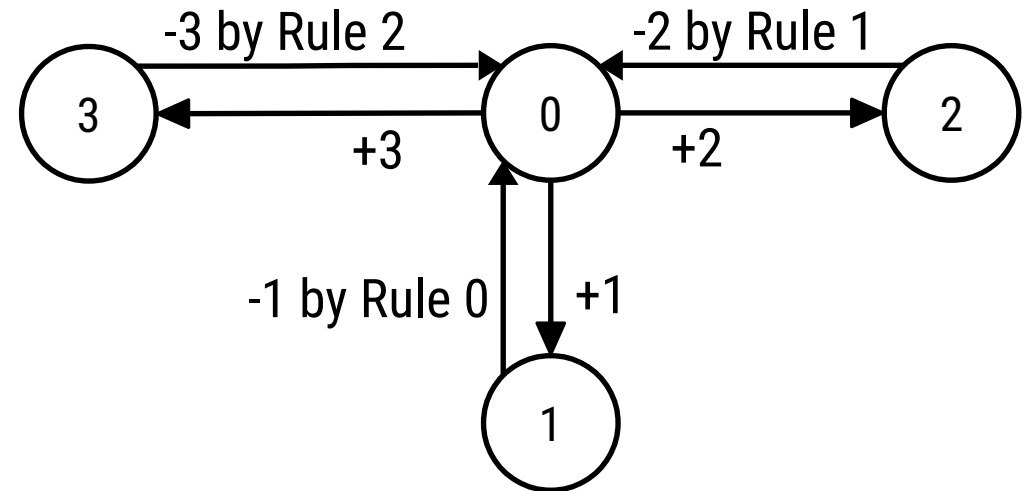
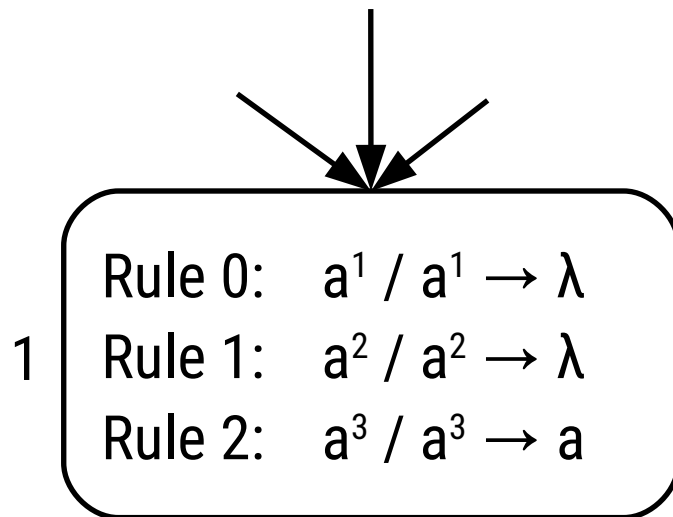
Rule 7: $a^{Z+1} (a^3)^+ / a^4 \rightarrow \lambda$

Rule 8: $a^{Z+2} (a^3)^+ / a^3 \rightarrow a$

Discussion: On combining rules



Discussion: On combining rules



End of Presentation. Thank you!

Acknowledgements

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