

## UK SENIOR MATHEMATICAL CHALLENGE

## **Tuesday 8 November 2016**

## Organised by the United Kingdom Mathematics Trust

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## **RULES AND GUIDELINES** (to be read before starting)

- 1. Do not open the question paper until the invigilator tells you to do so.
- 2. Time allowed: **90 minutes**. No answers or personal details may be entered on the Answer Sheet after the 90 minutes are over.
- 3. The use of rough paper is allowed. Calculators, measuring instruments and squared paper are forbidden.
- 4. Candidates must be full-time students at secondary school or FE college, and must be in Year 13 or below (England & Wales); S6 or below (Scotland); Year 14 or below (Northern Ireland).
- 5. **Use B or HB pencil only**. Mark *at most one* of the options A, B, C, D, E on the Answer Sheet for each question. Do not mark more than one option.
- 6. Scoring rules: all candidates start out with 25 marks;

0 marks are awarded for each question left unanswered;

4 marks are awarded for each correct answer;

1 mark is deducted for each incorrect answer.

7. **Guessing**: Remember that there is a penalty for incorrect answers. Note also that later questions are deliberately intended to be harder than earlier questions. You are thus advised to concentrate first on solving as many as possible of the first 15-20 questions. Only then should you try later questions.

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1.	How many times does the digit 9 appear in the answer to $987654321 \times 9$ ?
	A 0 B 1 C 5 D 8 E 9
2.	On a Monday, all prices in Isla's shop are 10% more than normal. On Friday all prices in Isla's shop are 10% less than normal. James bought a book on Monday for £5.50. What would be the price of another copy of this book on Friday?
	A £5.50 B £5.00 C £4.95 D £4.50 E £4.40
3.	The diagram shows a circle with radius 1 that rolls without slipping around the inside of a square with sides of length 5.  The circle rolls once around the square, returning to its starting point.  What distance does the centre of the circle travel?
	A $16-2\pi$ B 12 C $6+\pi$ D $20-2\pi$ E 20
4.	Alex draws a scalene triangle. One of the angles is 80°. Which of the following could be the difference between the other two angles in Alex's triangle?
	A 0° B 60° C 80° D 100° E 120°
5.	All the digits 2, 3, 4, 5 and 6 are placed in the grid, one in each cell, to form two three-digit numbers that are squares.  Which digit is placed in the centre of the grid?  A 2 B 3 C 4 D 5 E 6
6.	
	A $5\frac{1}{4}$ B $5\frac{3}{8}$ C $5\frac{1}{2}$ D $5\frac{5}{8}$ E $5\frac{3}{4}$ B $C$
7.	Which of these has the smallest value?
	A $2016^{-1}$ B $2016^{-1/2}$ C $2016^{0}$ D $2016^{1/2}$ E $2016^{1}$
8.	Points are drawn on the sides of a square, dividing each side into $n$ equal parts (so, in the example shown, $n = 4$ ). The points are joined in the manner indicated, to form several small squares (24 in the example, shown shaded) and some triangles. How many small squares are formed when $n = 7$ ? A 56 B 84 C 140 D 840 E 5040
9.	A square has vertices at $(0, 0)$ , $(1, 0)$ , $(1, 1)$ and $(0, 1)$ . Graphs of the following equations are drawn on the same set of axes as the square.
	$x^{2} + y^{2} = 1$ , $y = x + 1$ , $y = -x^{2} + 1$ , $y = x$ , $y = \frac{1}{x}$

How many of the graphs pass through exactly two of the vertices of the square?

D 4

E 5

C 3

A 1

B 2



