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Neural Network from scratch in Python

Make your own machine learning library.



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In this post we will go through the mathematics of machine learning and code from scratch, in Python, a small library to build neural networks with a variety of layers (Fully Connected, Convolutional, etc.). You will be able to create networks in a modular fashion.



4K

33

...

will be able to create

```
14     net = Network()
15     net.add(FCLayer(2, 3))
16     net.add(ActivationLayer(tanh, tanh_prime))
17     net.add(FCLayer(3, 1))
18     net.add(ActivationLayer(tanh, tanh_prime))
```

3-layer neural network

I'm assuming you already have *some* knowledge about neural networks. The purpose here is not to explain why we make these models, but to show how to make a proper implementation.

Layer by Layer

We need to keep in mind the big picture here :

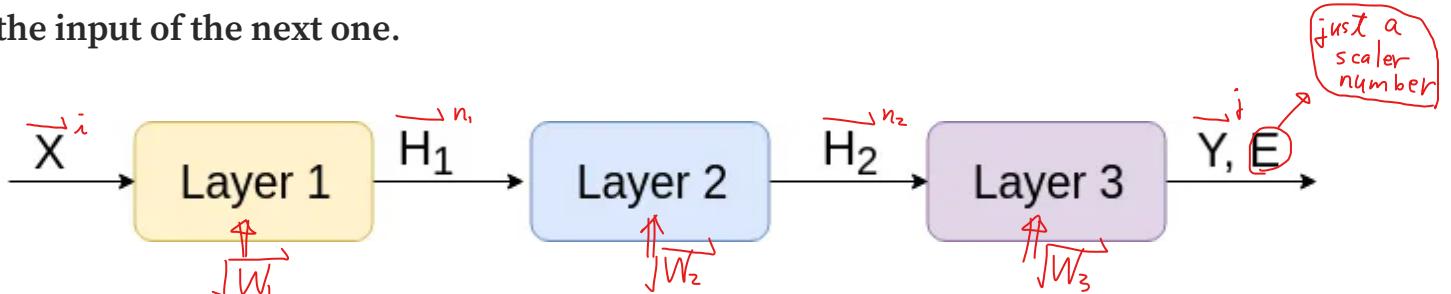
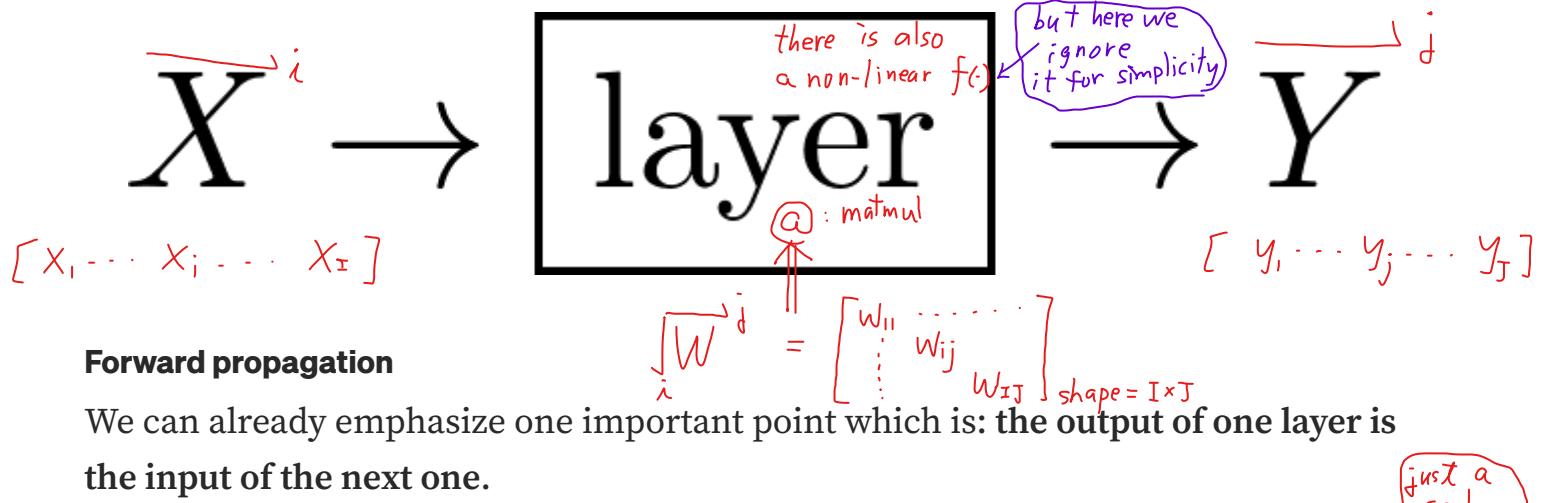
1. We feed **input** data into the neural network.
2. The data flows **from layer to layer** until we have the **output**.
3. Once we have the output, we can calculate the **error** which is a **scalar**.
4. Finally we can adjust a given parameter (weight or bias) by subtracting the **derivative** of the error with respect to the parameter itself.
5. We iterate through that process.

The most important step is the **4th**. We want to be able to have as many layers as we want, and of any type. But if we modify/add/remove one layer from the network, the output of the network is going to change, which is going to change the error, which is going to change the derivative of the error with respect to the parameters. We need to be able to compute the derivatives regardless of the network architecture, regardless of the activation functions, regardless of the loss we use.

In order to achieve that, we must implement each layer separately.

What every layer should implement

Every layer that we might create (fully connected, convolutional, maxpooling, dropout, etc.) have at least 2 things in common: **input** and **output** data.



This is called **forward propagation**. Essentially, we give the input data to the first layer, then the output of every layer becomes the input of the next layer until we reach the end of the network. By comparing the result of the network (Y) with the desired output (let's say Y^*), we can calculate an error E . The goal is to **minimize** that error by changing the parameters in the network. That is backward propagation (backpropagation).

Gradient Descent

This is a quick **reminder**, if you need to learn more about gradient descent there are tons of resources on the internet.

Basically, we want to change some parameter in the network (call it w) so that the total error E **decreases**. There is a clever way to do it (not randomly) which is the following :

$$w_{ij} \leftarrow w_{ij} - \alpha \frac{\partial E}{\partial w_{ij}}$$

Where α is a parameter in the range $[0,1]$ that we set and that is called the **learning rate**. Anyway, the important thing here is $\partial E / \partial w$ (the derivative of E with respect to w). We need to be able to find the value of that expression for any parameter of the network regardless of its architecture.

Backward propagation

Suppose that we give a layer the **derivative of the error with respect to its output** ($\partial E / \partial Y$), then it must be able to provide the **derivative of the error with respect to its input** ($\partial E / \partial X$).

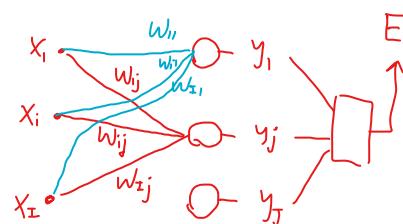


Remember that E is a **scalar** (a number) and x and y are **matrices**.

$$\frac{\partial E}{\partial X} = \left[\frac{\partial E}{\partial x_1} \quad \frac{\partial E}{\partial x_2} \quad \cdots \quad \frac{\partial E}{\partial x_i} \right]$$

$$\frac{\partial E}{\partial Y} = \left[\frac{\partial E}{\partial y_1} \quad \frac{\partial E}{\partial y_2} \quad \cdots \quad \frac{\partial E}{\partial y_j} \right]$$

Let's forget about $\partial E / \partial X$ for now. The trick here, is that if we have access to $\partial E / \partial Y$ we can very easily calculate $\partial E / \partial W$ (if the layer has any trainable parameters) without knowing anything about the network architecture ! We simply use the chain rule :



$$\frac{\partial E}{\partial w_{ij}} = \sum_m \frac{\partial E}{\partial y_j} \frac{\partial y_j}{\partial w_{ij}}$$

$y_j = \text{func}\left(x_1, x_2, \dots, x_i, w_{j1}, w_{j2}, \dots, w_{ij}, w_{j1}, \dots, w_{jj} \right)$
 $y_m \text{ 不 } (m \neq j) \quad w_{ij}$ 沒関連
 也就是說, $\forall m=1\dots J$, 只會留下 $\frac{\partial y_j}{\partial w_{ij}} = x_i$
 $\frac{\partial y_m}{\partial w_{ij}} = 0 \quad (\text{for } m \neq j)$

The unknown is $\partial y_j / \partial w$ which totally depends on how the layer is computing its output. So if every layer have access to $\partial E / \partial Y$, where Y is its own output, then we can update our parameters !

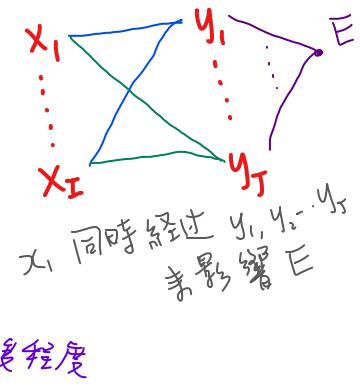
But why $\partial E / \partial X$?

Don't forget, the output of one layer is the input of the next layer. Which means $\partial E / \partial X$ for one layer is $\partial E / \partial Y$ for the previous layer ! That's it ! It's just a clever way to propagate the error ! Again, we can use the chain rule :

$$\begin{aligned} E &= E(y_1, y_2, \dots, y_J) \\ &= E(y_1(x_1, x_2, \dots, x_I), y_2(x_1, x_2, \dots, x_I), \dots) \\ &= E(x_1, x_2, \dots, x_I, y_1, y_2, \dots, y_J) \end{aligned}$$

$$\frac{\partial E}{\partial x_i}$$

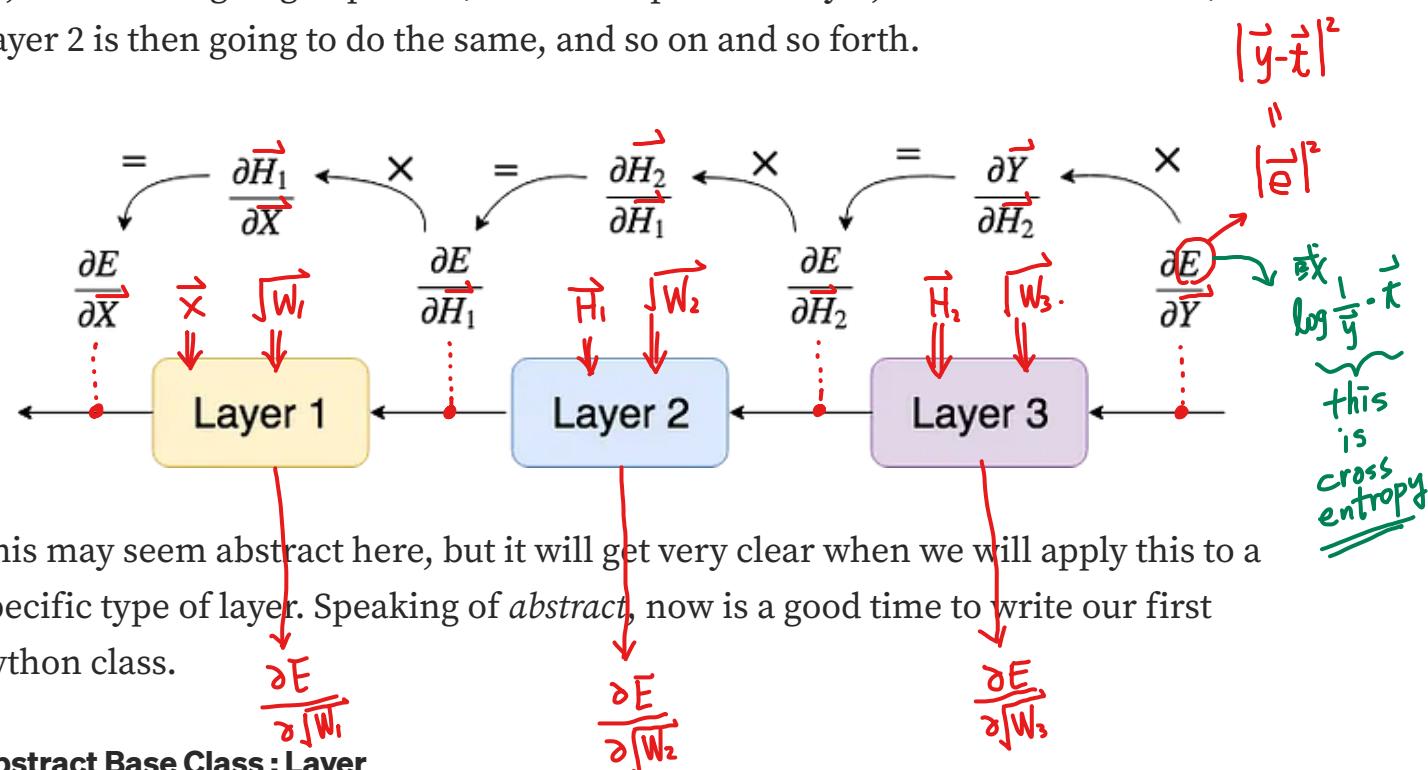
$$\frac{\partial E}{\partial x_i} = \sum_j \frac{\partial E}{\partial y_j} \frac{\partial y_j}{\partial x_i}$$



This is *very* important, it's the *key* to understand backpropagation ! After that, we'll be able to code a Deep Convolutional Neural Network from scratch in no time !

Diagram to understand backpropagation

This is what I described earlier. Layer 3 is going to update its parameters using $\partial E / \partial Y$, and is then going to pass $\partial E / \partial H_2$ to the previous layer, which is its own " $\partial E / \partial Y$ ". Layer 2 is then going to do the same, and so on and so forth.



This may seem abstract here, but it will get very clear when we will apply this to a specific type of layer. Speaking of *abstract*, now is a good time to write our first python class.

Abstract Base Class : Layer

The abstract class *Layer*, which all other layers will inherit from, handles simple properties which are an **input**, an **output**, and both a **forward** and **backward** methods.

```
1 # Base class
2 class Layer:
3     def __init__(self):
4         self.input = None
5         self.output = None
```

```

6
7     # computes the output Y of a layer for a given input X
8     def forward_propagation(self, input):
9         raise NotImplementedError
10
11    # computes dE/dX for a given dE/dY (and update parameters if any)
12    def backward_propagation(self, output_error, learning_rate):
13        raise NotImplementedError

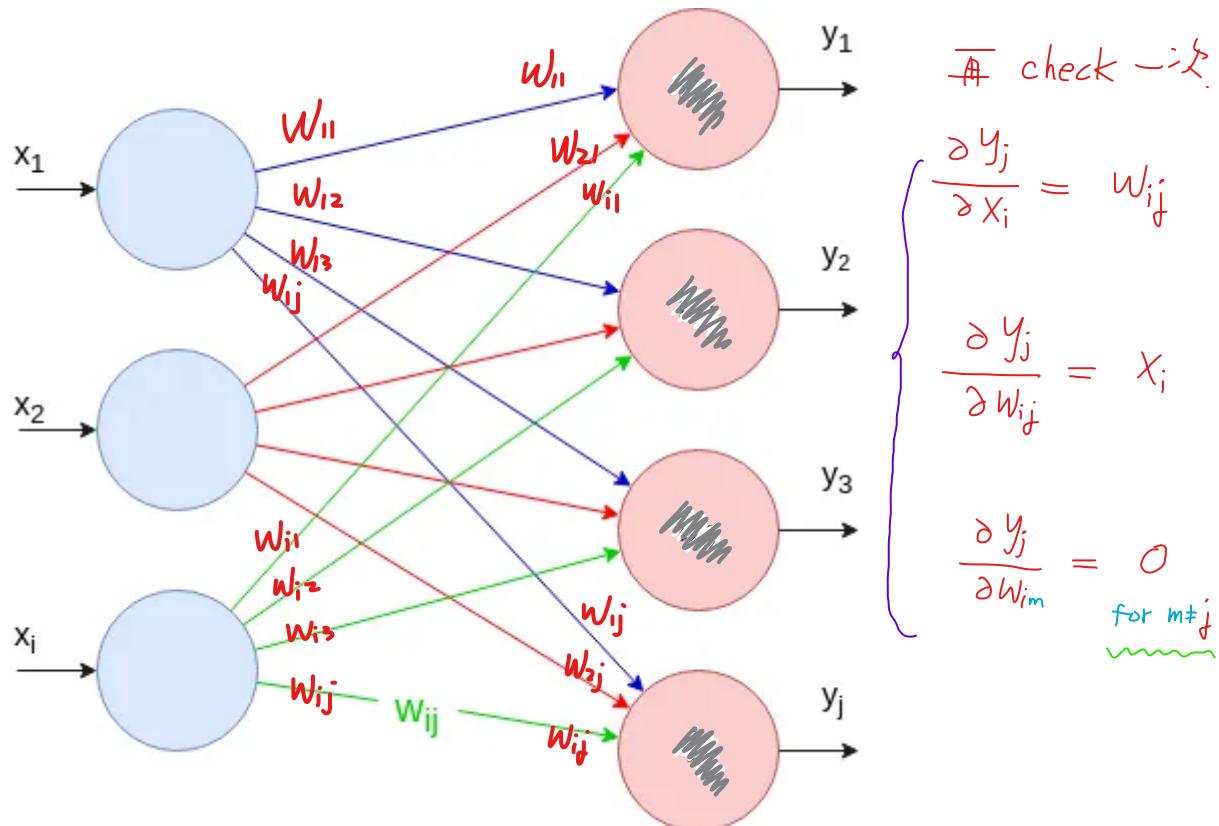
```

medium_nn_py_base_class.py hosted with ❤ by GitHub

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Fully Connected Layer

Now let's define and implement the first type of layer: fully connected layer or FC layer. FC layers are the most basic layers as every input neurons are connected to every output neurons.



Forward Propagation

The value of each output neuron can be calculated as the following :

$$y_j = \text{bias} + \sum_i x_i w_{ij}$$

With matrices, we can compute this formula for every output neuron in one shot using a **dot product**:

$$\vec{X} = [x_1 \dots x_i] \quad \vec{W} = \begin{bmatrix} w_{11} \dots w_{1j} \\ \vdots \quad \ddots \quad \vdots \\ w_{i1} \dots w_{ij} \end{bmatrix} \quad \boxed{B = [b_1 \dots b_j]}$$

$$\vec{Y} = \vec{X} \vec{W} + B$$

We're done with the forward pass. Now let's do the backward pass of the FC layer.

Note that I'm not using any activation function yet, that's because we will implement it in a separate layer!

Backward Propagation

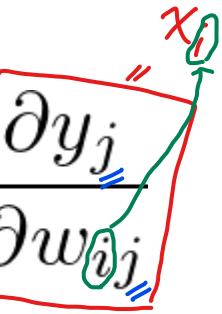
As we said, suppose we have a matrix containing the derivative of the error with respect to **that layer's output** ($\partial E / \partial Y$). We need :

1. The derivative of the error with respect to the parameters ($\partial E / \partial W, \partial E / \partial B$)
2. The derivative of the error with respect to the input ($\partial E / \partial X$)

Let's calculate $\partial E / \partial W$. This matrix should be the same size as W itself: $i \times j$ where i is the number of input neurons and j the number of output neurons. We need **one gradient for every weight**:

$$\frac{\partial E}{\partial \underline{W}_i} = \begin{bmatrix} \frac{\partial E}{\partial w_{11}} & \cdots & \frac{\partial E}{\partial w_{1j}} \\ \vdots & \ddots & \vdots \\ \frac{\partial E}{\partial w_{i1}} & \cdots & \frac{\partial E}{\partial w_{ij}} \end{bmatrix}$$

Using the chain rule stated earlier, we can write :

$$\begin{aligned} \frac{\partial E}{\partial w_{ij}} &= \frac{\partial E}{\partial y_1} \frac{\partial y_1}{\partial w_{ij}} + \dots + \frac{\partial E}{\partial y_j} \frac{\partial y_j}{\partial w_{ij}} \\ &= \frac{\partial E}{\partial y_j} x_i \end{aligned}$$


Therefore,

$$= \chi_i \cdot \frac{\partial E}{\partial y_j}$$

$$\frac{\partial E}{\partial \overbrace{W}^i} = \begin{bmatrix} \frac{\partial E}{\partial y_1} x_1 & \cdots & \frac{\partial E}{\partial y_j} x_1 \\ \vdots & \ddots & \vdots \\ \frac{\partial E}{\partial y_1} x_i & \cdots & \frac{\partial E}{\partial y_j} x_i \end{bmatrix}$$

這個式子是關鍵

$$= \begin{bmatrix} x_1 \\ \vdots \\ x_i \end{bmatrix} \begin{bmatrix} \frac{\partial E}{\partial y_1} & \cdots & \frac{\partial E}{\partial y_j} \end{bmatrix}$$

$$= \boxed{X^t} \boxed{\frac{\partial E}{\partial Y}}$$

That's it we have the first formula to update the weights! Now let's calculate $\partial E / \partial B$.

$$\frac{\partial E}{\partial B} = \left[\frac{\partial E}{\partial b_1} \quad \frac{\partial E}{\partial b_2} \quad \cdots \quad \frac{\partial E}{\partial b_j} \right]$$

Again $\partial E / \partial B$ needs to be of the same size as B itself, one gradient per bias. We can use the chain rule again :

$$\begin{aligned} \frac{\partial E}{\partial b_j} &= \frac{\partial E}{\partial y_1} \frac{\partial y_1}{\partial b_j} + \cdots + \frac{\partial E}{\partial y_j} \frac{\partial y_j}{\partial b_j} \\ &= \frac{\partial E}{\partial y_j} \end{aligned}$$

And conclude that,

$$\begin{aligned}\frac{\partial E}{\partial B} &= \left[\frac{\partial E}{\partial y_1} \quad \frac{\partial E}{\partial y_2} \quad \cdots \quad \frac{\partial E}{\partial y_j} \right] \\ &= \frac{\partial E}{\partial Y}\end{aligned}$$

Now that we have $\partial E / \partial W$ and $\partial E / \partial B$, we are left with $\partial E / \partial X$ which is **very important** as it will “act” as $\partial E / \partial Y$ for the layer before that one.

$$\frac{\partial E}{\partial X} = \left[\frac{\partial E}{\partial x_1} \quad \frac{\partial E}{\partial x_2} \quad \cdots \quad \frac{\partial E}{\partial x_i} \right]$$

Again, using the chain rule,

$$\begin{aligned}\frac{\partial E}{\partial x_i} &= \frac{\partial E}{\partial y_1} \frac{\partial y_1}{\partial x_i} + \cdots + \frac{\partial E}{\partial y_j} \frac{\partial y_j}{\partial x_i} \\ &= \frac{\partial E}{\partial y_1} w_{i1} + \cdots + \frac{\partial E}{\partial y_j} w_{ij}\end{aligned}$$

Finally, we can write the whole matrix :

$$\begin{aligned}\frac{\partial E}{\partial X} &= \left[\left(\frac{\partial E}{\partial y_1} w_{11} + \dots + \frac{\partial E}{\partial y_j} w_{1j} \right) \quad \dots \quad \left(\frac{\partial E}{\partial y_1} w_{i1} + \dots + \frac{\partial E}{\partial y_j} w_{ij} \right) \right] \\ &= \begin{bmatrix} \frac{\partial E}{\partial y_1} & \dots & \frac{\partial E}{\partial y_j} \end{bmatrix} \begin{bmatrix} w_{11} & \dots & w_{i1} \\ \vdots & \ddots & \vdots \\ w_{1j} & \dots & w_{ij} \end{bmatrix} \\ &= \frac{\partial E}{\partial Y} W^t\end{aligned}$$

That's it! We have the three formulas we needed for the FC layer!

精華

$$\left\{ \begin{array}{l} \frac{\partial E}{\partial X} = \frac{\partial E}{\partial Y} W^t \\ \frac{\partial E}{\partial W} = (X^t) \frac{\partial E}{\partial Y} \end{array} \right. \quad \left| \begin{array}{l} \frac{\partial \varepsilon}{\partial x_i} = \sum_j \frac{\partial \varepsilon}{\partial y_j} W_{ji}^t \\ \frac{\partial \varepsilon}{\partial w_{ij}} = x_i \frac{\partial \varepsilon}{\partial y_j} \end{array} \right.$$

Coding the Fully Connected Layer

We can now write some python code to bring this math to life!

```

1  from layer import Layer
2  import numpy as np
3
4  # inherit from base class Layer
5  class FCLayer(Layer):
6      # input_size = number of input neurons
7      # output_size = number of output neurons
8      def __init__(self, input_size, output_size):
9          self.weights = np.random.rand(input_size, output_size) - 0.5
10         self.bias = np.random.rand(1, output_size) - 0.5
11
12     # returns output for a given input
13     def forward_propagation(self, input_data):
14         self.input = input_data
15         self.output = np.dot(self.input, self.weights) + self.bias
16         return self.output
17
18     # computes dE/dW, dE/dB for a given output_error=dE/dY. Returns input_error=dE/dX.
19     def backward_propagation(self, output_error, learning_rate):
20         input_error = np.dot(output_error, self.weights.T)
21         weights_error = np.dot(self.input.T, output_error)
22         # dBias = output_error
23
24         # update parameters
25         self.weights -= learning_rate * weights_error
26         self.bias -= learning_rate * output_error
27         return input_error

```

$X \cdot W + b = Y$

Handwritten notes:

- $\text{Self. input} @ \text{Self. weights} + \text{self. bias}$
- $\text{np. dot}(A, B) = A @ B$

medium_nn_py_fc_layer.py hosted with ❤ by GitHub

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Activation Layer

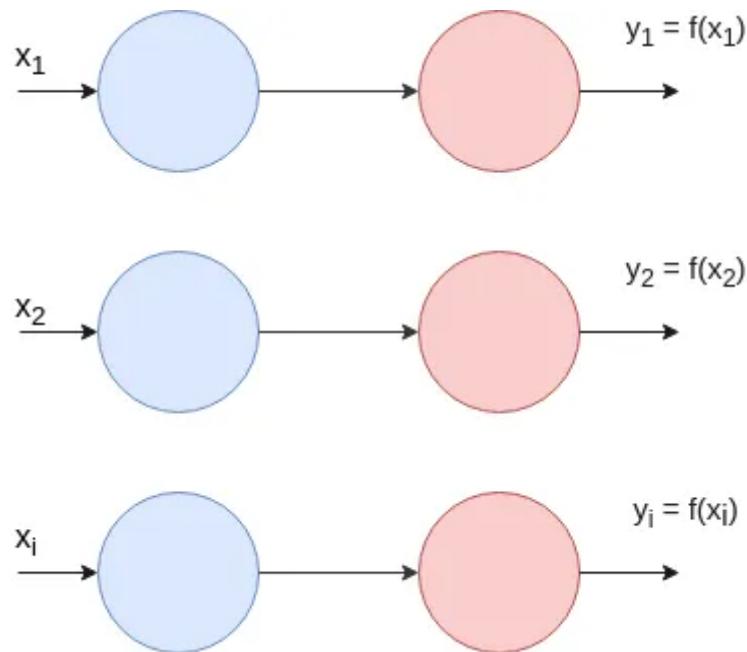
All the calculation we did until now were completely linear. It's hopeless to learn anything with that kind of model. We need to add **non-linearity** to the model by applying non-linear functions to the output of some layers.

Now we need to redo the whole process for this new type of layer!





parameters. We just
e respectively.



Forward Propagation

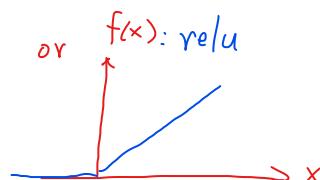
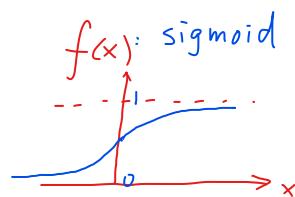
As you will see, it is quite straightforward. For a given input x , the output is simply the activation function applied to every element of x . Which means **input** and **output** have the **same dimensions**.

$$\vec{Y}^i = [f(x_1) \quad \dots \quad f(x_i)] \\ = f(\vec{X})$$

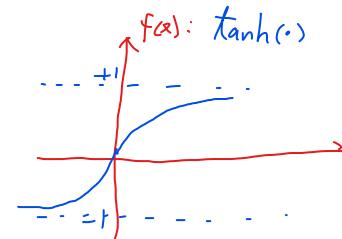
這種 $f(\cdot)$ 不涉及 \vec{X} 和 \vec{Y} 的 ^r_行
_列
是所謂 element-wise 的運算。

Backward Propagation

Given $\partial E / \partial Y$, we want to calculate $\partial E / \partial X$.



$$[y_1 \ y_2 \ \dots \ y_i \ \dots \ y_z] \\ = [f(x_1), f(x_2), \dots, f(x_i), \dots, f(x_z)]$$



$$\begin{aligned}
 \frac{\partial E}{\partial X} &= \left[\frac{\partial E}{\partial x_1} \quad \cdots \quad \frac{\partial E}{\partial x_i} \right] \\
 &= \left[\frac{\partial E}{\partial y_1} \frac{\partial y_1}{\partial x_1} \quad \cdots \quad \frac{\partial E}{\partial y_i} \frac{\partial y_i}{\partial x_i} \right] \\
 &= \left[\frac{\partial E}{\partial y_1} f'(x_1) \quad \cdots \quad \frac{\partial E}{\partial y_i} f'(x_i) \right] \\
 &= \left[\frac{\partial E}{\partial y_1} \quad \cdots \quad \frac{\partial E}{\partial y_i} \right] \odot [f'(x_1) \quad \cdots \quad f'(x_i)] \\
 &= \frac{\partial E}{\partial Y} \odot f'(X)
 \end{aligned}$$

也是向量内积。
元素对元素，不涉及矩阵相乘。结果是1个对1的
相乘。

Be careful, here we are using an **element-wise** multiplication between the two matrices (whereas in the formulas above, it was a dot product).

Coding the Activation Layer

The code for the activation layer is as straightforward.

```

1  from layer import Layer
2
3  # inherit from base class Layer
4  class ActivationLayer(Layer):
5      def __init__(self, activation, activation_prime):
6          self.activation = activation
7          self.activation_prime = activation_prime
8
9      # returns the activated input
10     def forward_propagation(self, input_data):
11         self.input = input_data
12         self.output = self.activation(self.input)
13         return self.output
14
15     # Returns input_error=dE/dX for a given output_error=dE/dY.
16     # learning_rate is not used because there is no "learnable" parameters.
17     def backward_propagation(self, output_error, learning_rate):
18         return self.activation_prime(self.input) * output_error

```

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$$\vec{x} \rightarrow @ \stackrel{f(\cdot)}{\circ} \vec{y}$$

\uparrow
 \sqrt{W}

$$\vec{a} = \vec{x} @ \sqrt{W}$$

$$\vec{y} = f(\vec{a})$$

$$\frac{\partial \vec{y}}{\partial \vec{a}} = f'(\vec{a})$$

$$\frac{\partial \vec{y}}{\partial \vec{x}} = f'(\vec{a}) \cdot \frac{\partial \vec{a}}{\partial \vec{x}}$$

加上一层。
f'(·)
f'(·)
f'(·)
f'(·)

You can also write some activation functions and their derivatives in a separate file.

These will be used later to create an ActivationLayer .

```

1 import numpy as np
2
3 # activation function and its derivative
4 def tanh(x):
5     return np.tanh(x);
6
7 def tanh_prime(x):
8     return 1-np.tanh(x)**2;

```

查一下 Wikipedia, $\tanh(x)$
及其「微分形式」!

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Loss Function

Until now, for a given layer, we supposed that $\partial E / \partial Y$ was given (by the next layer). But what happens to the last layer? How does it get $\partial E / \partial Y$? We simply give it manually, and it depends on how we define the error.

The error of the network, which measures how good or bad the network did for a given input data, is defined by you. There are many ways to define the error, and one of the most known is called MSE — Mean Squared Error. 最常見者中的 - 個.

$$E = \frac{1}{n} \sum_i^n (y_i^* - y_i)^2$$

Where y^* and y denotes desired output and actual output respectively. You can think of the loss as a last layer which takes all the output neurons and squashes them into one single neuron. What we need now, as for every other layer, is to define $\partial E / \partial Y$. Except now, we finally reached E !

$$\begin{aligned}\frac{\partial E}{\partial \vec{Y}} &= \left[\frac{\partial E}{\partial y_1} \quad \cdots \quad \frac{\partial E}{\partial y_i} \right] \\ &= \frac{2}{n} [y_1 - y_1^* \quad \cdots \quad y_i - y_i^*] \\ &= \frac{2}{n} (\vec{Y} - \vec{Y}^*)\end{aligned}$$

These are simply two python functions that you can put in a separate file. They will be used when creating the network.

```

1 import numpy as np
2
3 # loss function and its derivative
4 def mse(y_true, y_pred):
5     return np.mean(np.power(y_true-y_pred, 2));
6
7 def mse_prime(y_true, y_pred):
8     return 2*(y_pred-y_true)/y_true.size;

```

medium_nn_py_loss.py hosted with ❤ by GitHub

$$\mathcal{E} = \frac{1}{n} \sum_{k=1}^n (y_k^* - y_k)^2$$

$$\frac{\partial \mathcal{E}}{\partial \vec{y}} = \frac{1}{n} \cdot 2 \cdot (\vec{y} - \vec{y}^*)$$

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Network Class

Almost done ! We are going to make a `Network` class to create neural networks very easily akin the first picture !

I commented almost every part of the code, it shouldn't be too complicated to understand if you grasped the previous steps. Nevertheless, leave a comment if you have any question, I will gladly answer !


```

49         # backward propagation
50         error = self.loss_prime(y_train[j], output)
51         for layer in reversed(self.layers):
52             error = layer.backward_propagation(error, learning_rate)
53
54         # calculate average error on all samples
55         err /= samples
56         print('epoch %d/%d    error=%f' % (i+1, epochs, err))

```

medium_nn_py_network.py hosted with ❤ by GitHub

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```

1 import numpy as np
2
3 from network import Network
4 from fc_layer import FCLayer
5 from activation_layer import ActivationLayer
6 from activations import tanh, tanh_prime
7 from losses import mse, mse_prime
8
9 # training data
10 x_train = np.array([[[0,0]], [[0,1]], [[1,0]], [[1,1]]])
11 y_train = np.array([[0], [1], [1], [0]])
12
13 # network
14 net = Network()
15 net.add(FCLayer(2, 3))
16 net.add(ActivationLayer(tanh, tanh_prime))
17 net.add(FCLayer(3, 1))
18 net.add(ActivationLayer(tanh, tanh_prime))
19
20 # train
21 net.use(mse, mse_prime)
22 net.fit(x_train, y_train, epochs=1000, learning_rate=0.1)
23
24 # test
25 out = net.predict(x_train)
26 print(out)

```

medium_nn_py_example_xor.py hosted with ❤ by GitHub

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I don't think I need to emphasize many things. Just be careful with the training data, you should always have the **sample dimension first**. For example here, the input shape is (4,1,2).

Result

```
$ python xor.py
epoch 1/1000 error=0.322980
epoch 2/1000 error=0.311174
epoch 3/1000 error=0.307195
...
epoch 998/1000 error=0.000243
epoch 999/1000 error=0.000242
epoch 1000/1000 error=0.000242

[
    array([[ 0.00077435]]),
    array([[ 0.97760742]]),
    array([[ 0.97847793]]),
    array([[-0.00131305]])
]
```

Clearly this is working, great ! We can now solve something more interesting, let's solve MNIST !

Solve MNIST

We didn't implemented the Convolutional Layer but this is not a problem. All we need to do is to reshape our data so that it can fit into a Fully Connected Layer.

MNIST Dataset consists of images of digits from 0 to 9, of shape 28x28x1. The goal is to predict what digit is drawn on a picture.

```
1 import numpy as np
2
3 from network import Network
4 from fc_layer import FCLayer
5 from activation_layer import ActivationLayer
6 from activations import tanh, tanh_prime
7 from losses import mse, mse_prime
8
9 from keras.datasets import mnist
10 from keras.utils import np_utils
11
12 # load MNIST from server
13 (x_train, y_train), (x_test, y_test) = mnist.load_data()
14
15 # training data : 60000 samples
16 # reshape and normalize input data
17 x_train = x_train.reshape(x_train.shape[0], 1, 28*28)
18 x_train = x_train.astype('float32')
19 x_train /= 255
20 # encode output which is a number in range [0,9] into a vector of size 10
21 # e.g. number 3 will become [0, 0, 0, 1, 0, 0, 0, 0, 0, 0]
22 y_train = np_utils.to_categorical(y_train)
23
24 # same for test data : 10000 samples
25 x_test = x_test.reshape(x_test.shape[0], 1, 28*28)
26 x_test = x_test.astype('float32')
27 x_test /= 255
28 y_test = np_utils.to_categorical(y_test)
29
30 # Network
31 net = Network()
32 net.add(FCLayer(28*28, 100))           # input_shape=(1, 28*28) ; output_shape=(1, 100)
33 net.add(ActivationLayer(tanh, tanh_prime))
34 net.add(FCLayer(100, 50))              # input_shape=(1, 100) ; output_shape=(1, 50)
35 net.add(ActivationLayer(tanh, tanh_prime))
36 net.add(FCLayer(50, 10))               # input_shape=(1, 50) ; output_shape=(1, 10)
37 net.add(ActivationLayer(tanh, tanh_prime))
38
39 # train on 1000 samples
40 # as we didn't implemented mini-batch GD, training will be pretty slow if we update at each iteration
41 net.use(mse, mse_prime)
42 net.fit(x_train[0:1000], y_train[0:1000], epochs=35, learning_rate=0.1)
43
44 # test on 3 samples
45 out = net.predict(x_test[0:3])
46 print("\n")
47 print("predicted values : ")
48 print(out, end="\n")
```

```
40     print(out, end=' ')
49     print("true values : ")
50     print(y_test[0:3])
```

medium_nn_py_example_mnist_fc.py hosted with ❤ by GitHub

[view raw](#)

```
epoch 2/30    error=0.093187
epoch 3/30    error=0.073039
...
epoch 28/30   error=0.011636
epoch 29/30   error=0.011306
epoch 30/30   error=0.010901
```

predicted values :

```
[  
    array([[ 0.119,  0.084, -0.081,  0.084, -0.068,  0.011,  0.057,  
0.976, -0.042, -0.0462]]),  
    array([[ 0.071,  0.211,  0.501,  0.058, -0.020,  0.175,  0.057,  
0.037,  0.020,  0.107]]),  
    array([[ 1.197e-01,  8.794e-01, -4.410e-04,  4.407e-02, -4.213e-  
02,  5.300e-02,  5.581e-02,  8.255e-02, -1.182e-01,  9.888e-02]])  
]
```

true values :

```
[[0. 0. 0. 0. 0. 0. 1. 0. 0.]  
 [0. 0. 1. 0. 0. 0. 0. 0. 0.]  
 [0. 1. 0. 0. 0. 0. 0. 0. 0.]]
```

This is working perfectly ! Amazing :)



<https://gph.is/2jzemp3>

GitHub Repository & Google Colab

You can find the whole working code used for this post in the following GitHub repository, and Google Colab file. It also contains the code for other layers like Convolutional or Flatten.

OmarAflak/Medium-Python-Neural-Network

Contribute to OmarAflak/Medium-Python-Neural-Network development by creating an account on GitHub.

[github.com](https://github.com/OmarAflak/Medium-Python-Neural-Network)

Neural Networks from Scratch in Python

Feel free to contact me

colab.research.google.com

I've recently put the content of that article into a beautifully animated video. You can check it out on YouTube.

[Neural Network from Scratch | Mathematics & Pyt...](#)



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Convolutional Neural Network from Scratch | Mathematics & Python Code — The Independent Code

If you liked this post — I'd really appreciate if you hit the clap button it would help me a lot. Peace!

Python

Neural Networks

Mathematics

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