

数据库系统事务一致性验证问题研究

(工业软件产教联合主题交流会)

魏恒峰

hfwei@nju.edu.cn

2024 年 11 月 10 日



(使用**形式化方法理论与技术**) 解决**分布式系统**中的**数据一致性**问题



数据副本 带来了 **数据一致性**问题



PostgreSQL



yugabyteDB



ORACLE®



TiDB



mongoDB®



Dgraph



TDSQL



fauna

正确吗?

IT'S NOT
A BUG
IT'S AN UNDOCUMENTED
FEATURE





- ▶ **数据库系统**实现正确了吗?
- ▶ **客户端程序**编写正确了吗?

► 数据库系统实现正确了吗?



数据库系统通过 事务 与 隔离级别 来保证 数据一致性



Microsoft®
SQL Server™



PostgreSQL



yugabyteDB



SQLite

ORACLE®



MEM
GRAPH



TiDB



mongoDB®



Dgraph



TDSQL



fauna

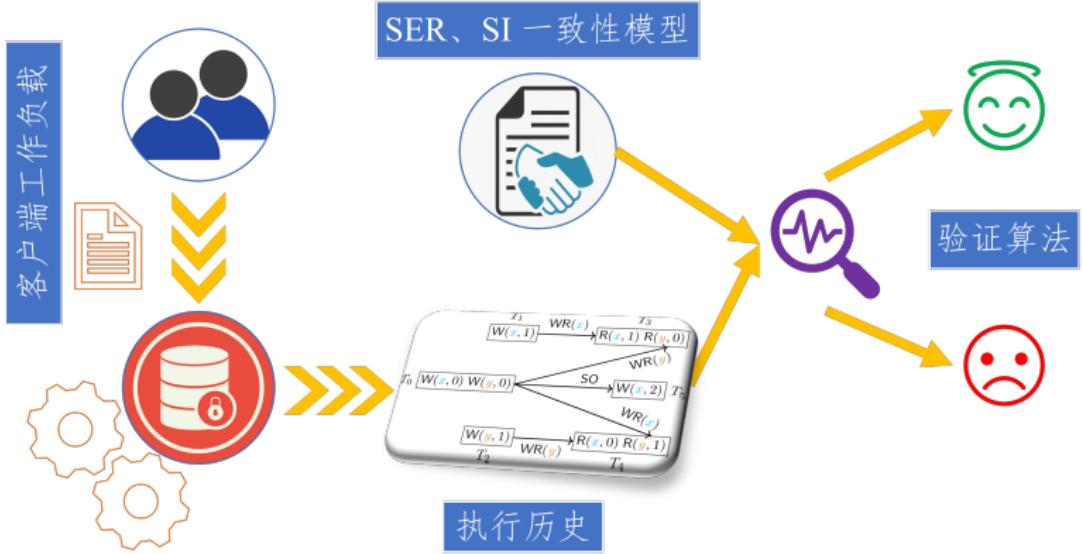
Elle: Inferring Isolation Anomalies from Experimental Observations

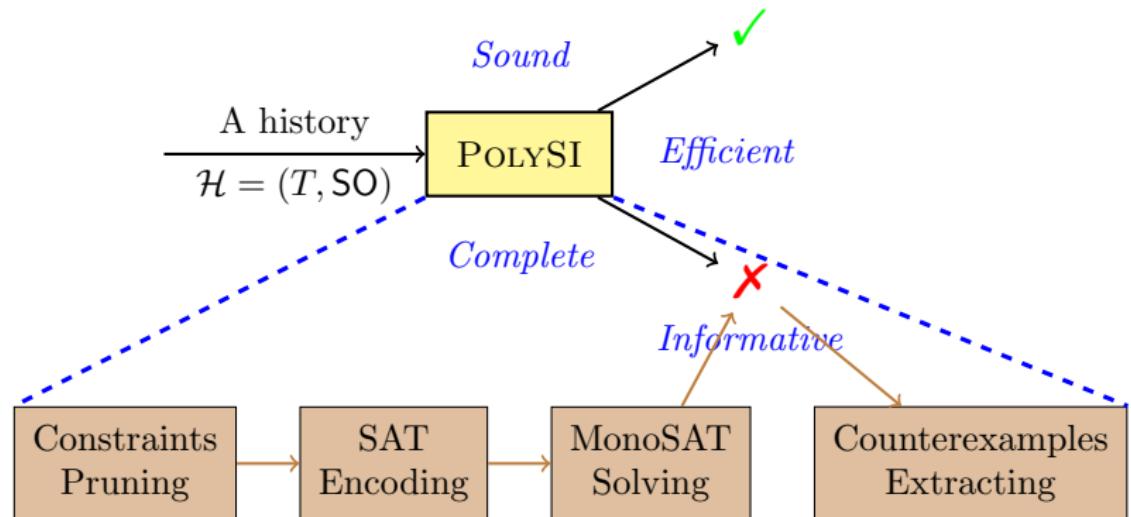
Kyle Kingsbury
Jepsen
aphyr@jepsen.io

Peter Alvaro
UC Santa Cruz
palvaro@ucsc.edu

FaunaDB 2.5.4
Kyle Kingsbury
2019-03-05

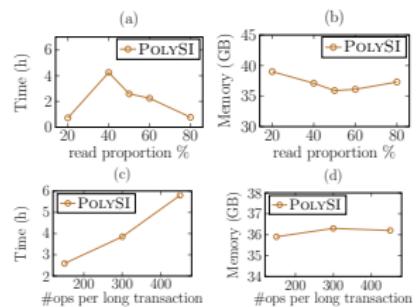
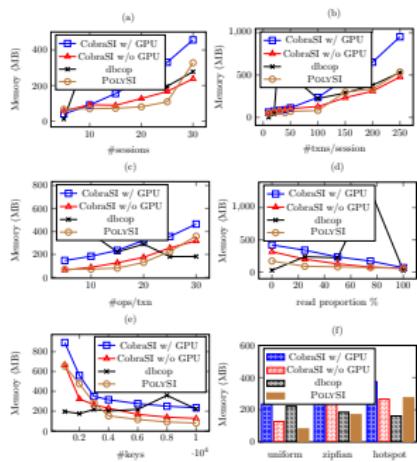
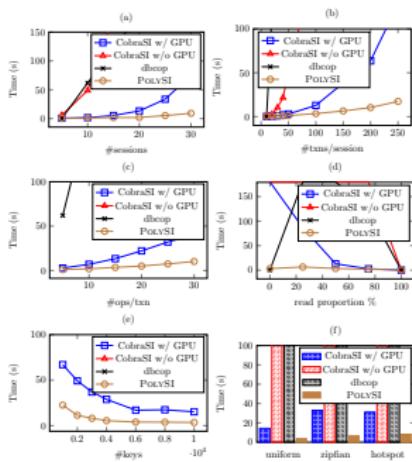
Dgraph 1.1.1
Kyle Kingsbury
2020-04-30





[PolySI@VLDB'2023]

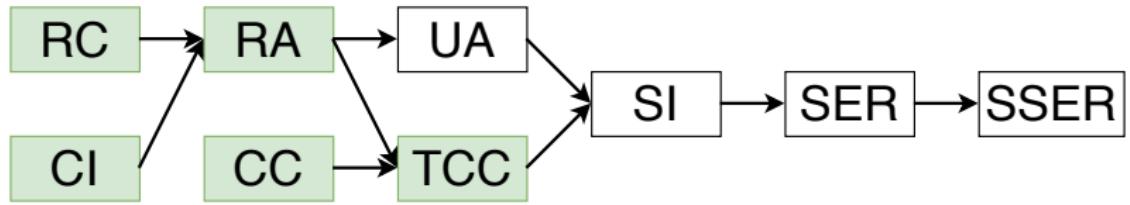




可扩展性

时间

内存



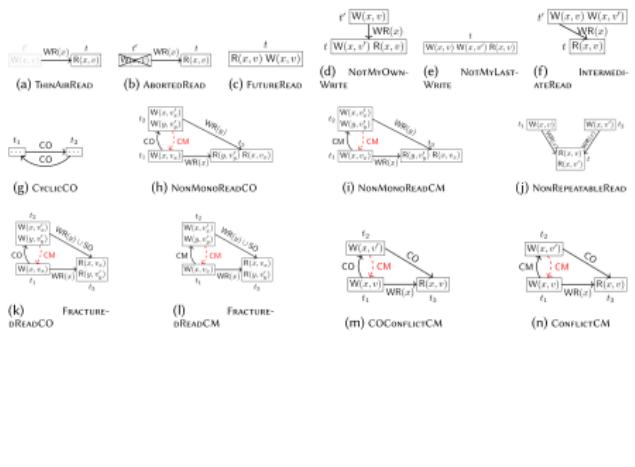
[Plume@OOPSLA'2024]

Table 1. The description and formalization of 14 TAPs (also visualized in Figure 3).

TAP	Description	TAP	Description
(a)	A transaction reads a value out of thin air. $\exists r \in R(T). \forall w \in W(T \cup T_{\otimes}). \neg(w \xrightarrow{\text{wr}} r).$	(b)	A transaction reads a value written by an aborted transaction. $\exists r \in R(T). \exists w \in W(T_{\otimes}). w \xrightarrow{\text{wr}} r.$
(c)	A transaction reads from a future write within the same transaction. $\exists t \in T. \exists w \in W(t). \exists r \in R(t).$ $(w \xrightarrow{\text{wr}} r \wedge r \xrightarrow{\text{po}_t} w).$	(d)	Transaction t reads key x from transaction $t' \neq t$, but t has written to x before this read. $\exists x \in K. \exists t, t' \neq t \in W_x(t). \exists r \in R_x(t). \exists w \in W_x(t).$ $\exists w' \in W_x(t'). (w' \xrightarrow{\text{wr}(x)} r \wedge w \xrightarrow{\text{po}_t} r).$
(e)	Transaction t reads key x from a write w in itself, but w is not the last write on x in t before this read. $\exists x \in K. \exists t \in T. \exists w, w' \neq w \in W_x(t). \exists r \in R_x(t).$ $(w \xrightarrow{\text{po}_t} w' \xrightarrow{\text{po}_t} r \wedge w \xrightarrow{\text{wr}(x)} r)$	(f)	Transaction t reads key x from a write w in transaction $t' \neq t$ which writes x more than once, but w is not the last write on x in t' . $\exists x \in K. \exists t \in RT_x. \exists t' \neq t \in WT_x. \exists r \in R_x(t).$ $\exists w, w' \neq w \in W_x(t'). (w \xrightarrow{\text{wr}(x)} r \wedge w \xrightarrow{\text{po}_{t'}} w').$
(g)	The relation SO \cup WR is cyclic. $(SO \cup WR)^+ \cap I_T \neq \emptyset.$	(h)	Transaction t_3 reads y from t_2 and then reads $x \neq y$ from t_1 . CO Transaction t_2 also writes to x but $t_1 \xrightarrow{\text{co}} t_2$. $\exists x, y \neq x \in K. \exists t_1, t_2 \neq t_3 \in WT_x. \exists t_3 \in (RT_x \cap RT_y) \setminus \{t_1, t_2\}.$ $\exists w_x \in W_x(t_1). \exists w_y \in W_y(t_2). \exists r_x \in R_x(t_3). \exists r_y \in R_y(t_3).$ $(w_x \xrightarrow{\text{wr}(x)} r_x \wedge w_y \xrightarrow{\text{wr}(y)} r_y \wedge r_y \xrightarrow{\text{po}_{t_3}} r_x \wedge t_1 \xrightarrow{\text{co}} t_2).$
(i)	Transaction t_3 reads y from t_2 and then reads $x \neq y$ from t_1 . CM Transaction t_2 also writes to x but $t_1 \xrightarrow{\text{cm}} t_2$. This is a general case of (h). $\exists x, y \neq x \in K. \exists t_1, t_2 \neq t_3 \in WT_x. \exists t_3 \in (RT_x \cap RT_y) \setminus \{t_1, t_2\}.$ $\exists w_x \in W_x(t_1). \exists w_y \in W_y(t_2). \exists r_x \in R_x(t_3). \exists r_y \in R_y(t_3).$ $(w_x \xrightarrow{\text{wr}(x)} r_x \wedge w_y \xrightarrow{\text{wr}(y)} r_y \wedge r_y \xrightarrow{\text{po}_{t_3}} r_x \wedge t_1 \xrightarrow{\text{cm}} t_2).$	(j)	A transaction reads from a key from other transactions more than once, but with different values. $\exists x \in K. \exists v, v' \neq v \in V. \exists t \in RT_x. \exists t_1 \neq t, t_2 \neq t \in WT_x.$ $\exists r_1 \triangleq R(x, v), r_2 \triangleq R(x, v') \in R_x(t).$ $\exists w_1 \in W_x(t_1). \exists w_2 \in W_x(t_2).$ $(t_1 \neq t_2 \wedge w_1 \xrightarrow{\text{wr}(x)} r_1 \wedge w_2 \xrightarrow{\text{wr}(x)} r_2).$
(k)	Transaction t_3 reads x from t_1 and $y \neq x$ from t_2 . CO Transaction t_2 also writes to x but $t_1 \xrightarrow{\text{co}} t_2$. $\exists x, y \neq x \in K. \exists t_1, t_2 \neq t_3 \in WT_x. \exists t_3 \in (RT_x \cap RT_y) \setminus \{t_1, t_2\}.$	(l)	Transaction t_3 reads x from t_1 and $y \neq x$ from t_2 . CM Transaction t_2 also writes to x but $t_1 \xrightarrow{\text{cm}} t_2$. This is a general case of (i) and (k). $\exists x, y \neq x \in K. \exists t_1, t_2 \neq t_3 \in WT_x. \exists t_3 \in (RT_x \cap RT_y) \setminus \{t_1, t_2\}.$

Table 1. The description and formalization of 14 TAPs (also visualized in Figure 3).

TAP	Description	TAP	Description
(a)	A transaction reads a value out of thin air. $\exists r \in R(T), \forall w \in W(T \cup T_0), \neg(w \xrightarrow{w} r).$	(b)	A transaction reads a value written by an aborted transaction. $\exists r \in R(T), \exists w \in W(T_0), w \xrightarrow{w} r.$
(c)	A transaction reads from a future write within the same transaction. $\exists t \in T, \exists w \in W(t), \exists r \in R(t), (w \xrightarrow{w} r \wedge r \xrightarrow{p_{t,w}} w).$	(d)	Transaction t reads key x from transaction $t' \neq t$, but t has written to x before this read. $\exists t \in K, \exists t', t \neq t' \in W_t(t), \exists r \in R_x(t), \exists w \in W_x(t), \exists w' \in W_{t'}(t'), (w \xrightarrow{w} r \wedge r \wedge w \xrightarrow{p_{t,w}} r).$
(e)	Transaction t reads key x from a write w in itself, but w is not the last write on x in t before this read. $\exists t \in K, \exists t, \exists w \in W_t(t), \exists r \in R_x(t), (w \xrightarrow{p_w} w' \xrightarrow{p_w} r \wedge r \wedge w \xrightarrow{w(x)} r).$	(f)	Transaction t reads key x from a write w in transaction t' $\neq t$ which writes x more than once, but t is the last write on x in t' . $\exists t \in K, \exists t, \exists t' \neq t \in W_{t'}(t'), \exists r \in R_x(t), \exists w \in W_x(t), \exists w' \in W_{t'}(t'), (w \xrightarrow{w(x)} r \wedge r \wedge w \xrightarrow{p_{t,w}} w').$
(g)	The relation $SO \cup WR$ is cyclic. $(SO \cup WR)^* \cap I_T \neq \emptyset.$	(h)	Transaction t reads y from t_1 and then reads $x \neq y$ from t_1 . Transaction t_1 also writes to x but $t_1 \xrightarrow{CM} t_2$. This is a general case of (b). $\exists x, y \neq x \in K, \exists t_1, t_2 \neq t_1 \in WT_y, \exists y \in (RT_x \cap RT_y) \setminus \{t_1, t_2\}, \exists w_x \in W_x(t_1), \exists w_y \in W_y(t_2), \exists r_x \in R_x(t_1), \exists r_y \in R_y(t_2), (w_x \xrightarrow{w(x)} r_x \wedge w_y \xrightarrow{w(y)} r_y \wedge r_x \xrightarrow{p_{t,y}} r_x \wedge t_1 \xrightarrow{CM} t_2).$
(i)	Transaction t_1 reads y from t_1 and then reads $x \neq y$ from t_1 . Transaction t_1 also writes to x but $t_1 \xrightarrow{CM} t_2$. This is a general case of (b). $\exists x, y \neq x \in K, \exists t_1, t_2 \neq t_1 \in WT_y, \exists y \in (RT_x \cap RT_y) \setminus \{t_1, t_2\}, \exists w_x \in W_x(t_1), \exists w_y \in W_y(t_2), \exists r_x \in R_x(t_1), \exists r_y \in R_y(t_2), (w_x \xrightarrow{w(x)} r_x \wedge w_y \xrightarrow{w(y)} r_y \wedge r_x \xrightarrow{p_{t,y}} r_x \wedge t_1 \xrightarrow{CM} t_2).$	(j)	Transaction t_1 reads x from t_1 and $y \neq x$ from t_2 . Transaction t_1 also writes to x but $t_1 \xrightarrow{CO} t_2$. This is a general case of (i) and (k). $\exists x, y \neq x \in K, \exists t_1, t_2 \neq t_1 \in WT_x, \exists y \in (RT_x \cap RT_y) \setminus \{t_1, t_2\}, \exists w_x \in W_x(t_1), \exists w_y \in W_y(t_2), \exists r_x \in R_x(t_1), \exists r_y \in R_y(t_2), (w_x \xrightarrow{w(x)} r_x \wedge w_y \xrightarrow{w(y)} r_y \wedge r_x \xrightarrow{CO} t_2).$
(m)	Transaction t_1 reads x from t_1 . There is a transaction t_2 that also writes to x such that $t_1 \xrightarrow{CO} t_2 \xrightarrow{CO} t_1$. $\exists t \in K, \exists t_1, t_2 \neq t_1 \in WT_x, \exists y \in RT_x \setminus \{t_1, t_2\}, (t_1 \xrightarrow{WR(x)} r_1 \wedge t_1 \xrightarrow{CM} t_2 \xrightarrow{CO} t_1).$	(n)	Transaction t_1 reads x from t_1 . There is a transaction t_2 that also writes to x such that $t_1 \xrightarrow{CM} t_2 \xrightarrow{CO} t_1$. This is a general case of (l) and (m). $\exists x \in K, \exists t_1, t_2 \neq t_1 \in WT_x, \exists y \in RT_x \setminus \{t_1, t_2\}, (t_1 \xrightarrow{WR(x)} r_1 \wedge t_1 \xrightarrow{CM} t_2 \xrightarrow{CO} t_1).$

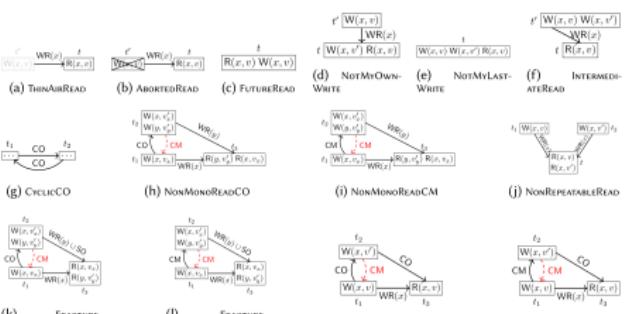


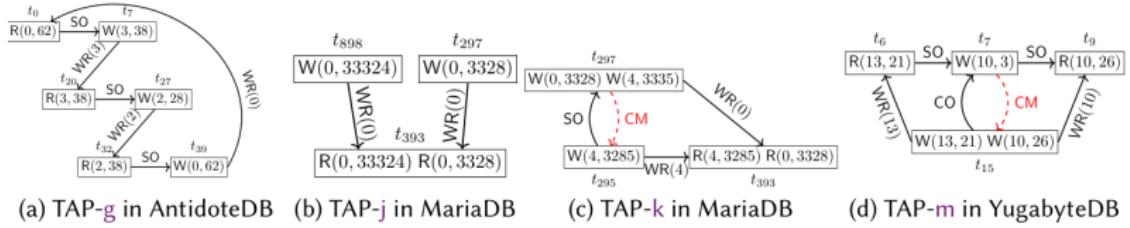
如何利用 数据异常全面、准确地定义这些事务隔离级别

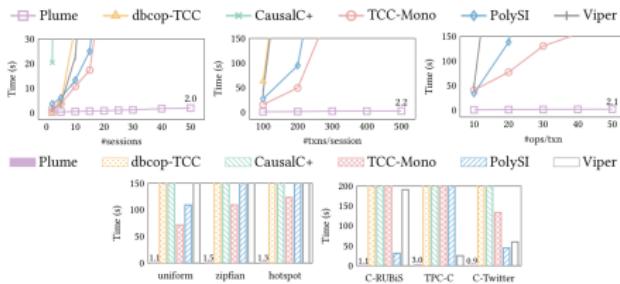
Isolation Level	Prohibited TAPs
Transactional Causal Consistency	All 14 TAPs
Read Atomicity	TAP-a to TAP-l (12 TAPs)
Read Committed	TAP-a to TAP-i (9 TAPs)
Cut Isolation	TAP-j

Table 1. The description and formalization of 14 TAPs (also visualized in Figure 3).

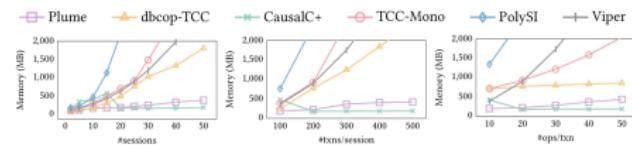
TAP	Description	TAP	Description
(a)	A transaction reads a value out of thin air. $\exists r \in R(T), \forall w \in W(T) \setminus T_0, \neg(w \xrightarrow{w} r).$	(b)	A transaction reads a value written by an aborted transaction. $\exists r \in R(T), \exists v \in W(T_0), w \xrightarrow{w} r.$
(c)	A transaction reads from a future write within the same transaction. $\exists t \in T, \exists w \in W(t), \exists r \in R(t), (w \xrightarrow{w} r \wedge r \xrightarrow{p_{t,w}} w).$	(d)	Transaction t reads key x from transaction $t' \neq t$, but it has written to x before this read. $\exists x \in K, \exists t, t' \neq t \in W_t(t), \exists r \in R_t(t), \exists w \in W_t(t), (w \xrightarrow{w} W_t(t'), w \xrightarrow{w(x)} r \wedge r \xrightarrow{p_{t,w}} w).$
(e)	Transaction t reads key x from a write w itself, but w is not the last write on x in t before this read. $\exists x \in K, \exists t \in T, \exists w, w' \in W_t(t), \exists r \in R_t(t), (w \xrightarrow{p_{t,w}} w' \xrightarrow{p_{t,w'}} w \wedge w \xrightarrow{w(x)} r)$	(f)	Transaction t reads key x from a write w in transaction $t' \neq t$ which writes x more than once, but w is not the last write on x in t' . $\exists x \in K, \exists t, \exists t' \neq t \in W_T, \exists r \in R_{t'}(t), \exists w, w' \in W_{t'}(t'), (w \xrightarrow{w(x)} r \wedge r \xrightarrow{p_{t,w}} w')$
(g)	The relation SO \sqcap WR is cyclic. (SO \sqcap WR) $t \sqsubset t$.	(h)	Transaction t_1 reads from t_2 and then reads $x \neq y$ from t_2 . Transaction t_1 also writes to x but $t_1 \xrightarrow{CO} t_2$. $\exists x, y \in K, \exists t_1, t_2 \neq t_1 \in W_{T_1}, \exists r_1 \in (R_{T_1} \cap RT_{T_2}) \setminus \{t_1, t_2\}, \exists w_x \in W_{t_1}(t_1), \exists w_y \in W_{t_2}(t_2), \exists r_x \in R_{t_1}(t_1), \exists r_y \in R_{t_2}(t_2), (w_x \xrightarrow{w(x)} r_1 \wedge w_y \xrightarrow{w(y)} r_2 \wedge r_2 \xrightarrow{p_{t_2,w}} r_x \wedge t_1 \xrightarrow{CO} t_2)$
(i)	Transaction t_1 reads y from t_2 and then reads $x \neq y$ from t_1 . Transaction t_2 also writes to x but $t_2 \xrightarrow{CM} t_1$. This is a general case of (h). $\exists x, y \in K, \exists t_1, t_2 \neq t_1 \in W_{T_1}, \exists r_1 \in (R_{T_1} \cap RT_{T_2}) \setminus \{t_1, t_2\}, \exists w_x \in W_{t_1}(t_1), \exists w_y \in W_{t_2}(t_2), \exists r_y \in R_{t_2}(t_2), (w_y \xrightarrow{w(y)} r_2 \wedge w_x \xrightarrow{w(x)} r_1 \wedge r_2 \xrightarrow{p_{t_1,w}} r_x \wedge t_2 \xrightarrow{CM} t_1)$	(j)	Transaction t_1 reads from t_2 and then reads $x \neq y$ from t_2 . Transaction t_2 also writes to x but $t_2 \xrightarrow{CM} t_1$. $\exists x, y \in K, \exists t_1, t_2 \neq t_1 \in W_{T_1}, \exists r_1 \in (R_{T_1} \cap RT_{T_2}) \setminus \{t_1, t_2\}, \exists w_x \in W_{t_1}(t_1), \exists w_y \in W_{t_2}(t_2), \exists r_y \in R_{t_2}(t_2), (w_x \xrightarrow{w(x)} r_1 \wedge w_y \xrightarrow{w(y)} r_2 \wedge r_2 \xrightarrow{p_{t_1,w}} r_x \wedge t_1 \xrightarrow{CM} t_2)$
(k)	Transaction t_1 reads from t_2 and $y \neq x$ from t_2 . Transaction t_2 also writes to x but $t_2 \xrightarrow{CO} t_1$. $\exists x, y \in K, \exists t_1, t_2 \neq t_1 \in W_{T_1}, \exists r_1 \in (R_{T_1} \cap RT_{T_2}) \setminus \{t_1, t_2\}, \exists w_x \in W_{t_1}(t_1), \exists w_y \in W_{t_2}(t_2), \exists r_x \in R_{t_2}(t_2), (w_x \xrightarrow{w(x)} r_1 \wedge w_y \xrightarrow{w(y)} r_2 \wedge r_2 \xrightarrow{p_{t_2,w}} r_x \wedge t_2 \xrightarrow{CO} t_1)$	(l)	Transaction t_1 reads from t_2 and $y \neq x$ from t_2 . Transaction t_2 also writes to x but $t_2 \xrightarrow{CM} t_1$. This is a general case of (i) and (k). $\exists x, y \in K, \exists t_1, t_2 \neq t_1 \in W_{T_1}, \exists r_1 \in (R_{T_1} \cap RT_{T_2}) \setminus \{t_1, t_2\}, \exists w_x \in W_{t_1}(t_1), \exists w_y \in W_{t_2}(t_2), \exists r_y \in R_{t_2}(t_2), (w_x \xrightarrow{w(x)} r_1 \wedge w_y \xrightarrow{w(y)} r_2 \wedge r_2 \xrightarrow{p_{t_1,w}} r_x \wedge t_2 \xrightarrow{CM} t_1)$
(m)	Transaction t_1 reads from t_2 . There is a transaction t_3 that also writes to x such that $t_1 \xrightarrow{CO} t_2 \xrightarrow{CO} t_3$. $\exists x \in K, \exists t_1, t_2, t_3 \in W_{T_1}, \exists r_1 \in RT_{T_1} \setminus \{t_1, t_2\}, (t_1 \xrightarrow{WR(x)} r_1 \wedge t_1 \xrightarrow{CO} t_2 \xrightarrow{CO} t_3)$	(n)	Transaction t_1 reads from t_2 . There is a transaction t_2 that also writes to x such that $t_1 \xrightarrow{CO} t_2 \xrightarrow{CO} t_1$. This is a general case of (l) and (m). $\exists x \in K, \exists t_1, t_2 \in W_{T_1}, \exists r_1 \in RT_{T_1} \setminus \{t_1, t_2\}, (t_1 \xrightarrow{WR(x)} r_1 \wedge t_1 \xrightarrow{CO} t_2 \xrightarrow{CO} t_1)$



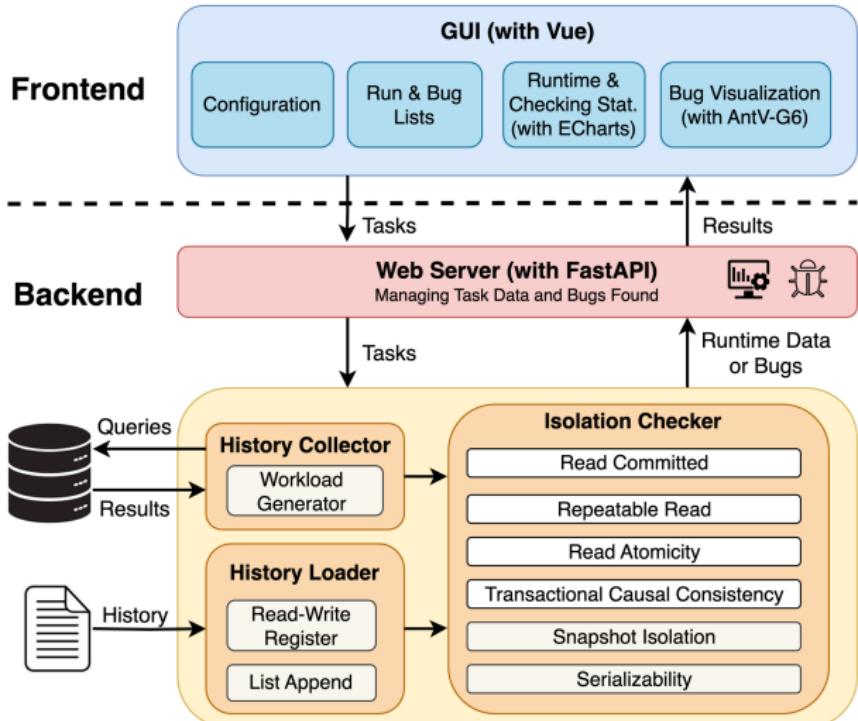




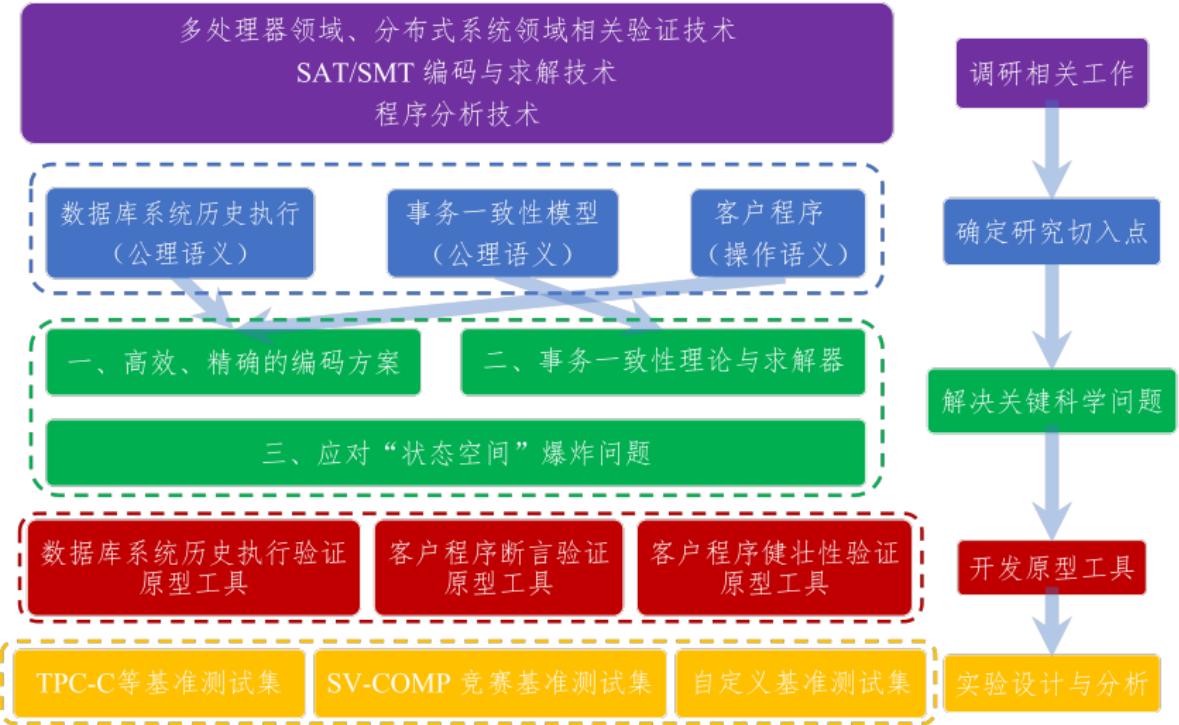
时间



内存



[IsoVista@VLDB'2024 (Demo)]



混合 (Mixing) 隔离级别





Hengfeng Wei (hfwei@nju.edu.cn)