Efficient Black-box Checking of Snapshot Isolation in Databases

Kaile Huang, Si Liu, Zhenge Chen, *Hengfeng Wei*, David Basin, Haixiang Li, Anqun Pan

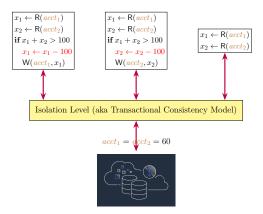
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September 6, 2023



Transaction and Isolation Level

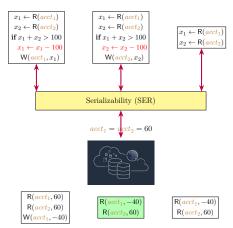
A transaction is a *group* of operations that are executed atomically.



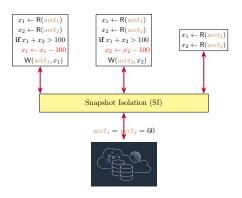
The isolation levels specify how concurrent transactions are isolated from each other.

Serializability (SER)

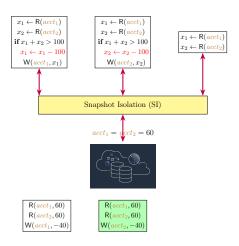
All transactions appear to be executed in some total order.



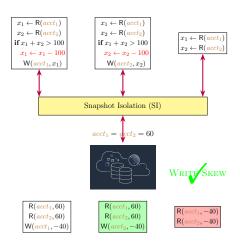
However, implementing serializability is too expensive.



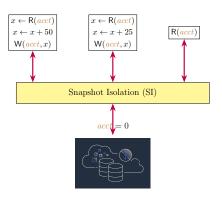
Snapshot Read: Each transaction reads data from a *snapshot* as of the time the transaction started.



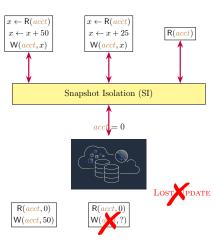
Snapshot Read: Each transaction reads data from a *snapshot* as of the time the transaction started.



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Snapshot Write: Concurrent transactions *cannot* write to the same key. One of them must be aborted.



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Database Systems and Snapshot Isolation

Many database systems implement snapshot isolation.



























Database Systems and Snapshot Isolation

Database systems may fail to provide snapshot isolation correctly.





Elle: Inferring Isolation Anomalies from Experimental Observations Kyle Kingsbury Peter Alvaro

Kyle Kingsbury Jepsen aphyr@jepsen.io Peter Alvaro UC Santa Cruz palvaro@ucsc.edu

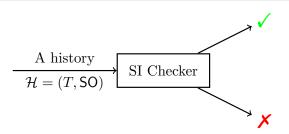




Definition (The SI Checking Problem)

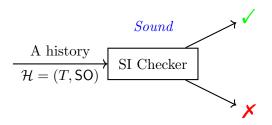
The SI checking problem is the decision problem of determing whether a history $\mathcal{H} = (T, SO)^a$ of a database system satisfies SI?

^aWe take the common "UniqueValue" assumption on histories: for each key, every write to the key assigns a unique value.



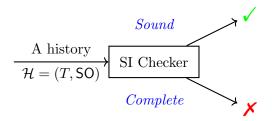
 $SO: session \ order \ among \ the set \ T \ of \ transactions$

Sound: If the checker says X, then the history does not satisfy SI.



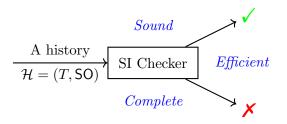
Sound: If the checker says ✓, then the history does not satisfy SI.

Complete: If the checker says ✓, then the history satisfies SI.



Sound: If the checker says \checkmark , then the history does not satisfy SI.

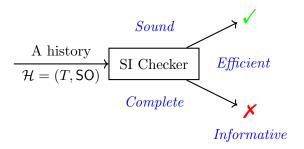
Complete: If the checker says \checkmark , then the history satisfies SI.



Efficient: The checker should *scale* up to large workloads.

Sound: If the checker says \times , then the history does not satisfy SI.

Complete: If the checker says \checkmark , then the history satisfies SI.



Efficient: The checker should scale up to large workloads.

Informative: The checker should provide understandable counterexamples if it finds violations.

dbcop [Biswas and Enea, 2019] checker for SI not practically efficient; not informative, returning only "False" upon violations

Cobra [Tan et al., 2020] state-of-the-art checker for SER The SI checking problem is *harder*.

Elle [Kingsbury and Alvaro, 2020] checker for various isolation levels

Work perfectly on traceable and recoverable histories; but may be incomplete on the key-value datatype

^aCould Elle tell the difference between snapshot isolation and strong-session-snapshot-isolation? https://github.com/jepsen-io/elle/issues/17

^bElle may miss two types of transaction anomalies.

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SI checking based on the Adya-style notions [Adya, 1999] relies on the start/commit timestamps of transactions.

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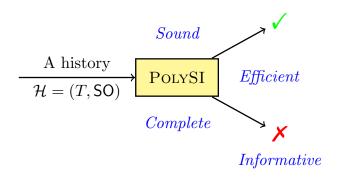
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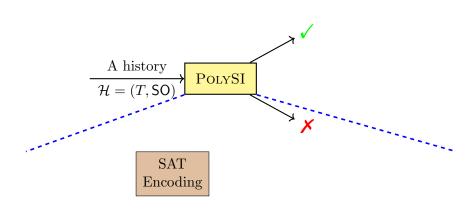
11/42

SI checking based on the [Cerone and Gotsman, 2018] notions may miss SI violations.^a b

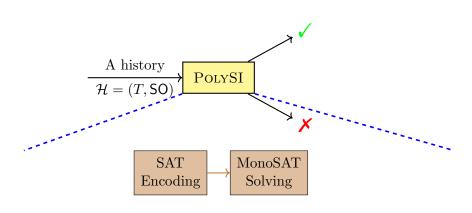
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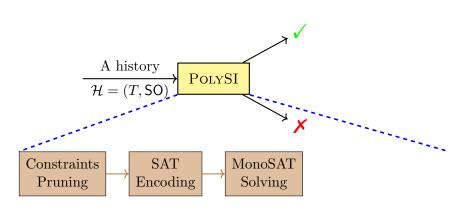




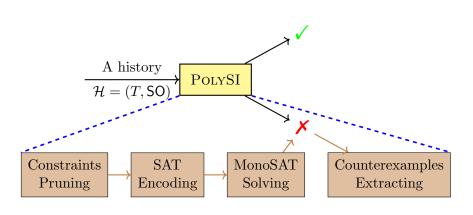
Sound & Complete: a novel polygraph based characterization of SI



Efficient: utilizing MonoSAT solver optimized for graph problems



Efficient: pruning the constraints on polygraph before encoding



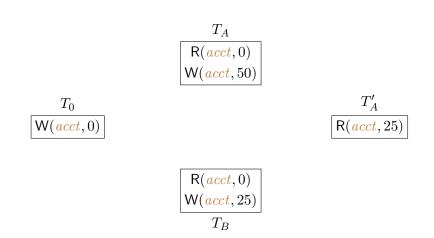
Informative: extract counterexamples from the UNSAT core

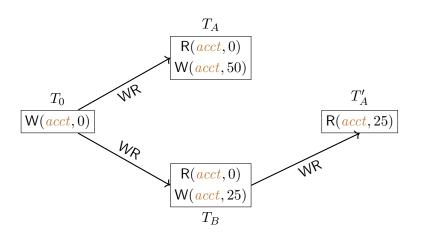
PolySI: Polygraph based Characterization of SI

Before this, we first review the dependency graph based characterization of SI [Cerone and Gotsman, 2018].

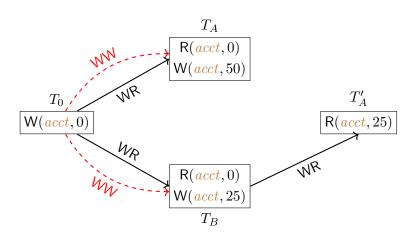
Theorem (Theorem 4.1 of [Cerone and Gotsman, 2018])

Informally, a history satisfies SI if and only if
there exists a dependency graph for it that
contains only cycles (if any) with at least two adjacent RW edges.



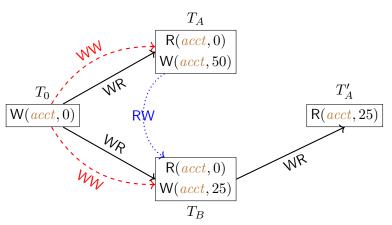


WR: "write-read" dependency capturing the "read-from" relation



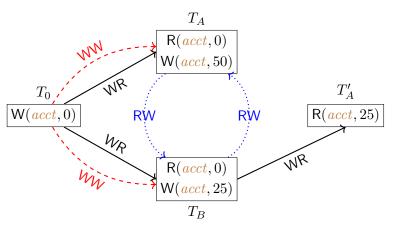
WW: "write-write" dependency capturing the version order on acct

 T_A reads from T_0 which is overwritten by T_B

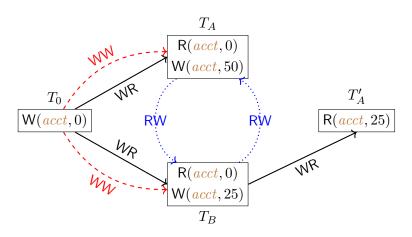


RW: "read-write" dependency

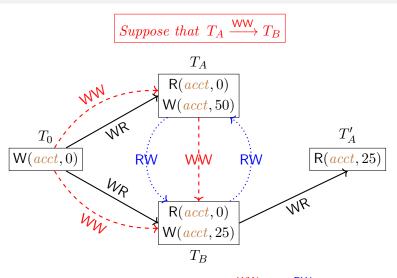
 T_B reads from T_0 which is overwritten by T_A



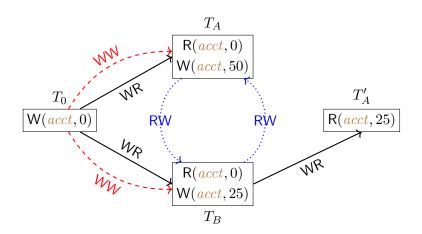
RW: "read-write" dependency

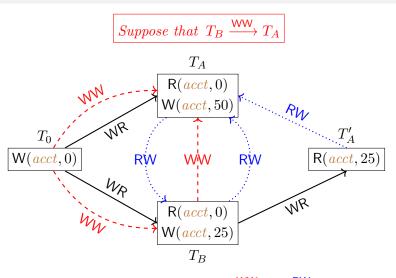


The cycle $T_A \xrightarrow{\mathsf{RW}} T_B \xrightarrow{\mathsf{RW}} T_A$ is allowed by SI.



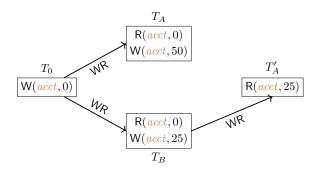
undesired cycle for SI: $T_A \xrightarrow{WW} T_B \xrightarrow{RW} T_A$ 15 / 42





undesired cycle for SI: $T_B \xrightarrow{WW} T_A \xrightarrow{RW} T_B$ 16/42

We have considered both bases $T_A \xrightarrow{\text{WW}} T_B$ and $T_B \xrightarrow{\text{WW}} T_A$, and each case leads to an undesired cycle for SI.

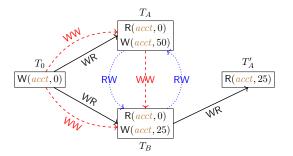


Therefore, this history does not satisfy SI.

Theorem (Equivalence of Theorem 4.1 of [Cerone and Gotsman, 2018]) Informally, a history satisfies SI if and only if there exists a dependency graph \mathcal{G} for it such that the induced graph of \mathcal{G} [((SO_{\mathcal{G}} \cup WR_{\mathcal{G}} \cup WW $_{\mathcal{G}}$); RW $_{\mathcal{G}}$?) is acyclic.

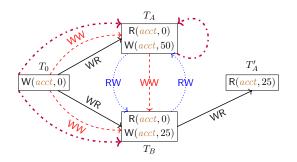
Dependency Graph based Characterization of SI

 $\mathit{induced\ graph}\left\lceil ((\mathsf{SO}_\mathcal{G} \cup \mathsf{WR}_\mathcal{G} \cup \mathsf{WW}_\mathcal{G}) \ ; \ \mathsf{RW}_\mathcal{G}?) \right\rceil \ \mathit{for} \ \mathcal{G}$



Dependency Graph based Characterization of SI

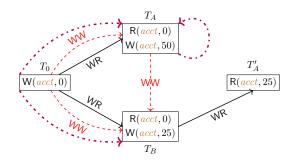
 $\mathit{induced\ graph} \boxed{ ((\mathsf{SO}_\mathcal{G} \cup \mathsf{WR}_\mathcal{G} \cup \mathsf{WW}_\mathcal{G}) \; ; \; \mathsf{RW}_\mathcal{G}?) } \ \mathit{for} \ \mathcal{G}$



first composing (;) the SO/WR/WW edges with the RW edges

Dependency Graph based Characterization of SI

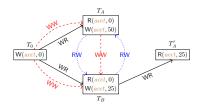
 $\mathit{induced\ graph}\left\lceil ((\mathsf{SO}_\mathcal{G} \cup \mathsf{WR}_\mathcal{G} \cup \mathsf{WW}_\mathcal{G}) \ ; \ \mathsf{RW}_\mathcal{G}?) \right\rceil \ \mathit{for} \ \mathcal{G}$

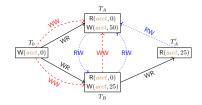


first composing (;) the SO/WR/WW edges with the RW edges then deleting all the RW edges

Polygraph: A Family of Dependency Graphs

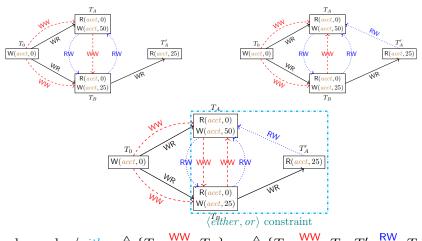
Consider the two cases of WW dependencies between T_A and T_B .





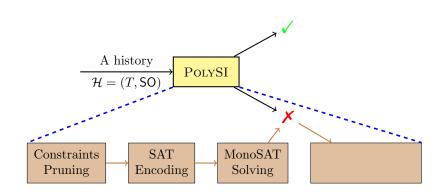
Polygraph: A Family of Dependency Graphs

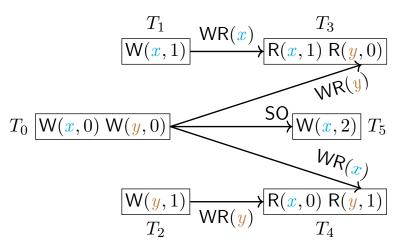
Consider the two cases of WW dependencies between T_A and T_B .



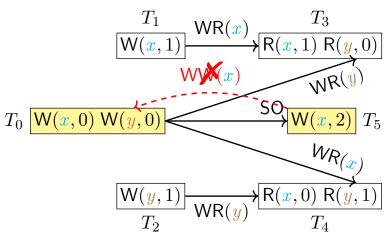
 $\text{polygraph: } \langle either \triangleq \{T_A \xrightarrow{\mathsf{WW}} T_B\}, or \triangleq \{T_B \xrightarrow{\mathsf{WW}} T_A, T_A' \xrightarrow{\mathsf{RW}} T_A\} \rangle$

To explain the whole PolySI procedure with a running example.

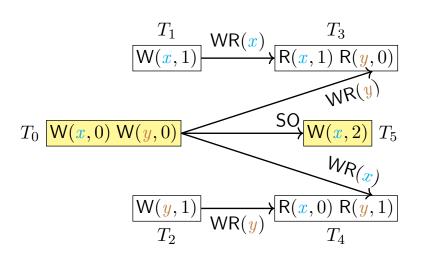


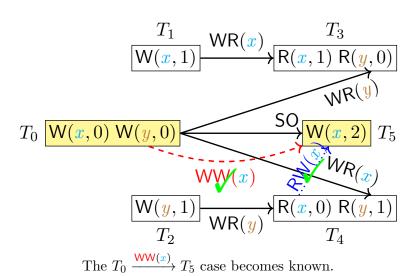


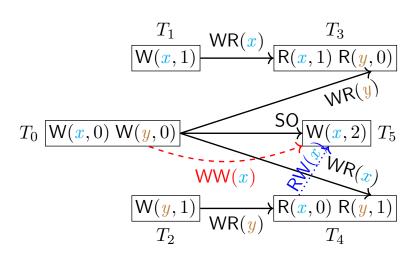
WW between T_0 , T_1 , and T_5 (on x) and between T_0 and T_2 (on y)

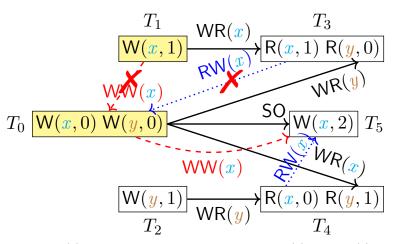


The $T_5 \xrightarrow{\mathsf{WW}(x)} T_0$ case is pruned due to $T_0 \xrightarrow{\mathsf{SO}} T_5 \xrightarrow{\mathsf{WW}(x)} T_0$.

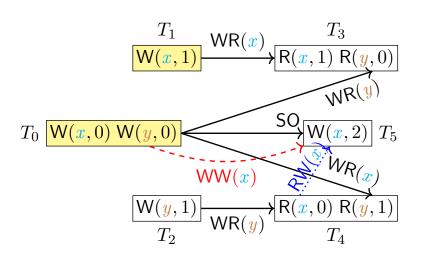


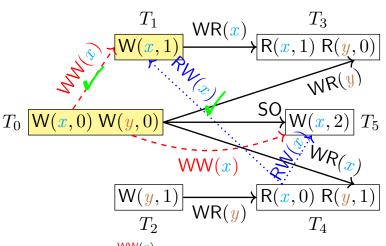




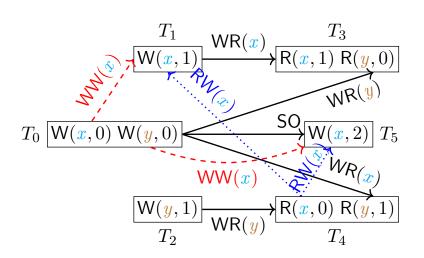


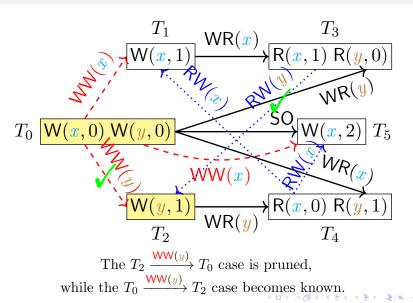
The $T_1 \xrightarrow{\mathsf{WW}(x)} T_0$ case is pruned due to $T_3 \xrightarrow{\mathsf{RW}(x)} T_0 \xrightarrow{\mathsf{WR}(y)} T_3$.

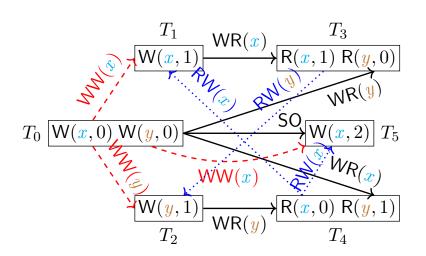


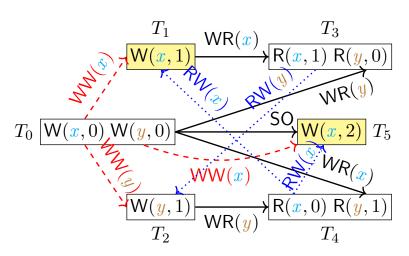


The $T_0 \xrightarrow{\text{WW}(x)} T_1$ case becomes known.









The WW order between T_1 and T_5 is still uncertain after pruning.

 $\begin{array}{c} T_1 \\ \hline W(x,1) \end{array} \xrightarrow{WR(x)} \begin{array}{c} T_3 \\ \hline R(x,1) R(y,0) \end{array}$ $T_0 \left| \mathsf{W}(x,0) \; \mathsf{W}(y,0) \right|$ $|\mathbf{W}(x,2)| T_5$ $\frac{\boxed{\mathsf{R}(x,0)\;\mathsf{R}(y,1)}}{T_4}$ $oxed{ egin{aligned} \mathsf{W}(\pmb{y},1) \ T_2 \end{aligned} }$

$$\langle either = \{T_1 \xrightarrow{\mathsf{WW}(x)} T_5, T_3 \xrightarrow{\mathsf{RW}(x)} T_5\}, or = \{T_5 \xrightarrow{\mathsf{WW}(x)} T_1\} \rangle$$

$$T_1 \qquad \mathsf{WR}(x) \qquad T_3 \qquad \mathsf{R}(x, 1) \; \mathsf{R}(y, 0)$$

$$\mathsf{W}(x, 1) \qquad \mathsf{RW}(x) \qquad \mathsf{RW}(x)$$

$$T_0 \; \mathsf{W}(x, 0) \; \mathsf{W}(y, 0) \qquad \mathsf{W}(x, 2) \; T_5$$

$$\mathsf{W}(y, 1) \qquad \mathsf{R}(x, 0) \; \mathsf{R}(y, 1)$$

$$T_2 \qquad \mathsf{R}(x, 0) \; \mathsf{R}(y, 1)$$

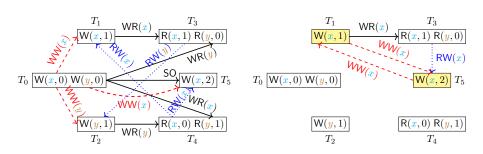


$$\langle either = \{T_1 \xrightarrow{\mathsf{WW}(x)} T_5, T_3 \xrightarrow{\mathsf{RW}(x)} T_5\}, or = \{T_5 \xrightarrow{\mathsf{WW}(x)} T_1\} \rangle$$

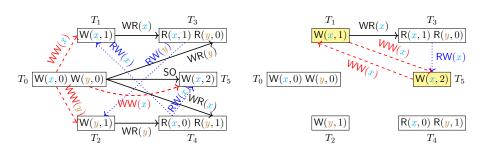
$$T_1 \qquad \mathsf{WR}(x) \qquad T_3 \qquad \mathsf{R}(x, 1) \ \mathsf{R}(x, 1) \ \mathsf{R}(y, 0) \qquad \mathsf{RW}(x) \qquad \mathsf{RW$$

$$\begin{array}{c|c} \hline \mathbb{W}(y,1) & \mathbb{R}(x,0) \ \mathbb{R}(y,1) \\ \hline T_2 & T_4 \\ \hline \underbrace{(\mathsf{BV}_{1,5} \land \mathsf{BV}_{3,5} \land \neg \mathsf{BV}_{5,1})}_{either} \lor \underbrace{(\mathsf{BV}_{5,1} \land \neg \mathsf{BV}_{1,5} \land \neg \mathsf{BV}_{3,5})}_{or} \\ \hline \end{array}$$

 $\mathrm{induced\ graph}\ \mathcal{I}\ \big[\left(\left(\mathsf{SO}_{\mathcal{G}}\cup\mathsf{WR}_{\mathcal{G}}\cup\mathsf{WW}_{\mathcal{G}}\right)\,;\ \mathsf{RW}_{\mathcal{G}}?\right)$



$$\mathrm{induced\ graph}\ \mathcal{I}\ \boxed{((\mathsf{SO}_\mathcal{G} \cup \mathsf{WR}_\mathcal{G} \cup \mathsf{WW}_\mathcal{G})\ ;\ \mathsf{RW}_\mathcal{G}?)}$$



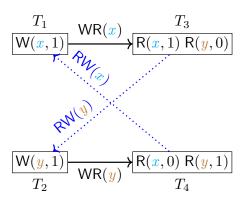
$$T_1 \xrightarrow{\mathsf{WR}} T_3 \xrightarrow{\mathsf{RW}} T_5: \; \mathsf{BV}_{1,5}^{\,\mathcal{I}} = \mathsf{BV}_{1,3} \; \wedge \; \mathsf{BV}_{3,5}$$

The presence of the edge $T_1 \to T_5$ in the induced graph \mathcal{I} depends on that of the edges $T_1 \to T_3$ and $T_3 \to T_5$ in the polygraph.

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Feed the SAT formula into the MonoSAT solver [Bayless et al., 2015] which is optimized for *cycle detection*.





The MonoSAT solver finds an undesired cycle for SI.

Experimental Evaluation

- (1) Effective: Can PolySI find SI violations in databases?
- (2) *Informative*: Can PolySI provide understandable counterexamples for SI violations?
- (3) *Efficient:* How efficient is PolySI?

Workloads

Table: Workload parameters and their default values.^c

Parameter	Default Value	
#sess	20	
#txns/sess	100	
#ops/txn	15	
#keys	10, 000	
%reads	50%	
distribution	zipfian	

^cWe use a database schema of a two-column table storing keys and values= 999

Benchmarks

RuBiS: an eBay-like bidding system

TPC-C: an open standard for OLTP benchmarking

C-Twitter: a Twitter clone

GeneralRH: read-heavy workloads with 95% reads

GeneralRW: medium workloads with 50% reads

GeneralWH: write-heavy workloads with 30% reads

Reproducing Known SI Violations

Database	GitHub Stars	Kind	Release
$\rm Cockroach DB^d$	25.1k	Relational	$v2.1.0^{e}, v2.1.6$
${\it MySQL-Galera}$	381	Relational	v25.3.26
${\bf YugabyteDB}$	6.7k	Multi-model	$v1.1.10.0^{f}$

An extensive collection of 2477 anomalous histories

[Biswas and Enea, 2019; Darnell, Accessed February 14, 2023; Jepsen, Accessed February 14, 2023]

^dRemove SNAPSHOT isolation since (probably) v2.0.4. https://github.com/cockroachdb/cockroach/pull/27040

^eLessons learned from 2+ years of nightly Jepsen tests. https://www.cockroachlabs.com/blog/jepsen-tests-lessons/

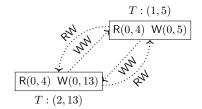
fAcknowledged inserts can be present in reads for tens of seconds, then disappear. https://github.com/YugaByte/yugabyte-db/issues/824

Detecting New SI Violations

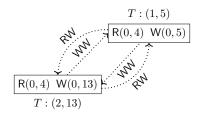
Dgraph: helped the Dgraph team confirm some of their suspicions about their latest release

Database	GitHub Stars	Kind	Release
Dgraph	18.2k	Graph	v21.12.0
MariaDB-Galera	4.4k	Relational	v10.7.3
${\bf YugabyteDB}$	6.7k	Multi-model	v2.11.1.0

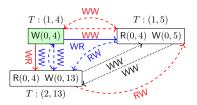
Galera: confirmed the incorrect claim on preventing "lost updates" for transactions issued on different cluster nodes



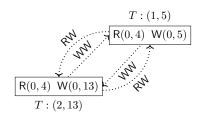
(a) Original output



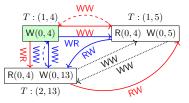
(a) Original output



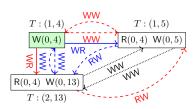
(b) Missing participants



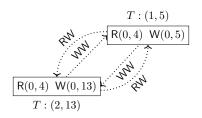
(a) Original output



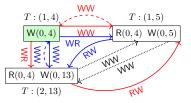
(c) Recovered scenario



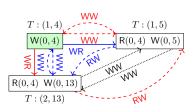
(b) Missing participants



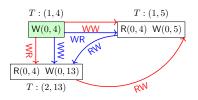
(a) Original output



(c) Recovered scenario



(b) Missing participants



(d) Finalized scenario

Performance Evaluation

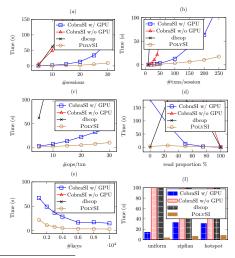
dbcop [Biswas and Enea, 2019]: the state-of-the-art SI checker

CobraSI: reducing SI checking to SER checking [Biswas and Enea, 2019] to leverage Cobra with/without GPU

Cobra [Tan et al., 2020]: the state-of-the-art SER checker using both MonoSAT and GPU

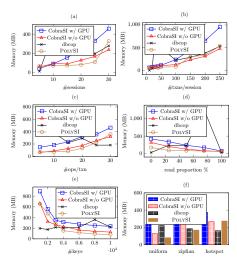
Performance Evaluation: Runtime

PolySI significantly outperforms the competitors.^g



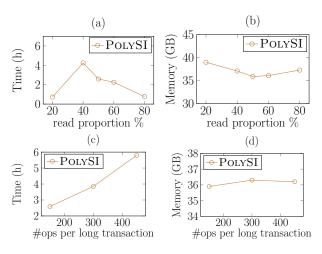
Performance Evaluation: Memory

PolySI consumes less memory.



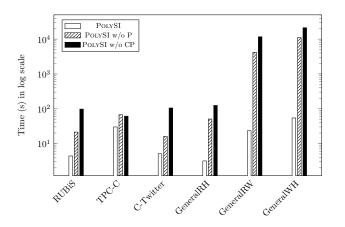
Performance Evaluation: Scalability

several hours and $35 \sim 40 \mathrm{GB}$ memory for checking 1M transactions



Performance Evaluation: Differential Analysis

Pruning (P) is crucial to the efficiency of PolySI.^h



hCompacting (C) encoding has been omitted in this presentation. ■ ▶ ⋑ ♥ ♥ ♥

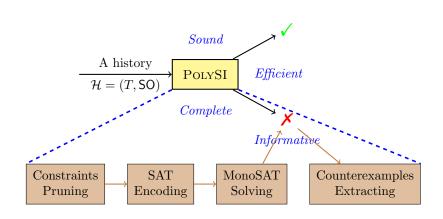
Performance Evaluation: Pruning

PolySI can prune a huge number of constraints before encoding.

Benchmark	#cons.	#cons.	#unk. dep.	#unk. dep.
	before P	after P	before P	after P
TPC-C	386k	0	3628k	0
$\operatorname{GeneralRH}$	4k	29	39k	77
RUBiS	14k	149	171k	839
C-Twitter	59k	277	307k	776
${\it GeneralRW}$	90k	2565	401k	5435
GeneralWH	167k	6962	468k	14376

TPC-C: read-only transactions + RMW transactions

Conclusion



Future Work

PolySI uses MonoSAT as a black-box.

Working on a **theory solver** dedicated to isolation level checking, which is deeply integrated with SAT solvers [He, Sun, and Fan, 2021].



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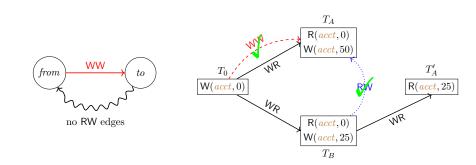
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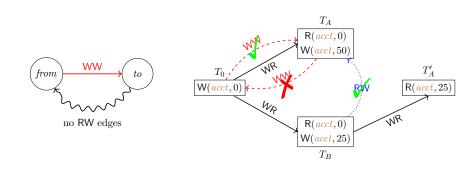


Kingsbury, Kyle and Peter Alvaro (Nov. 2020). "Elle: Inferring Isolation Anomalies from Experimental Observations". In: *Proc. VLDB Endow.* 14.3, pp. 268–280. ISSN: 2150-8097.

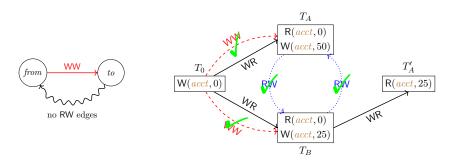


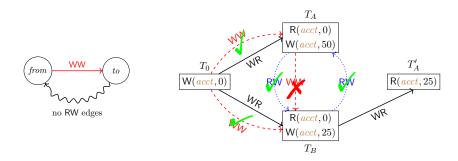
Tan, Cheng, Changgeng Zhao, Shuai Mu, and Michael Walfish (2020). "COBRA: Making Transactional Key-Value Stores Verifiably Serializable". In: OSDI'20. ISBN: 978-1-939133-19-9.



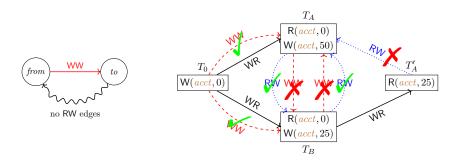


 $T_A \xrightarrow{\mathsf{WW}} T_0$ can be pruned due to the $T_A \xrightarrow{\mathsf{WW}} T_0 \xrightarrow{\mathsf{WR}} T_A$ cycle.



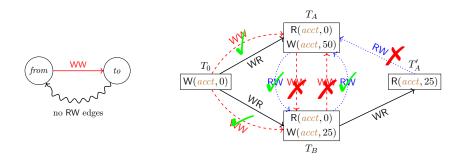


 $T_A \xrightarrow{\mathsf{WW}} T_B$ is pruned due to the $T_A \xrightarrow{\mathsf{WW}} T_B \xrightarrow{\mathsf{RW}} T_A$ cycle.



 $T_A \xrightarrow{\mathsf{WW}} T_B$ is pruned due to the $T_A \xrightarrow{\mathsf{WW}} T_B \xrightarrow{\mathsf{RW}} T_A$ cycle.

 $T_B \xrightarrow{WW} T_A$ is pruned due to the $T_B \xrightarrow{WW} T_A \xrightarrow{RW} T_B$ cycle.

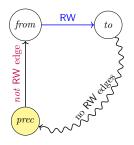


 $T_A \xrightarrow{\mathsf{WW}} T_B$ is pruned due to the $T_A \xrightarrow{\mathsf{WW}} T_B \xrightarrow{\mathsf{RW}} T_A$ cycle.

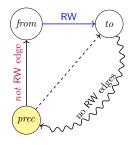
 $T_B \xrightarrow{WW} T_A$ is pruned due to the $T_B \xrightarrow{WW} T_A \xrightarrow{RW} T_B$ cycle.

Therefore, we are sure that the history does *not* satisfy SI.





Check if there is a path from to to any immediate predecessor prec of from that does not contain RW edges.



Check if there is a path from to to any immediate predecessor prec of from that does not contain RW edges.

Dependency Graph based Characterization of SI

```
Theorem (Theorem 4.1 of [Cerone and Gotsman, 2018])

For a history \mathcal{H} = (T, SO),

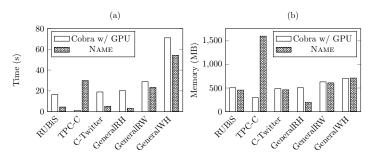
\mathcal{H} \models SI \iff \mathcal{H} \models Int \land

\exists WR, WW, RW. \mathcal{G} = (\mathcal{H}, WR, WW, RW) \land

(((SO_{\mathcal{G}} \cup WR_{\mathcal{G}} \cup WW_{\mathcal{G}}); RW_{\mathcal{G}}?) \text{ is acyclic}).
```

Performance Evaluation: Cobra with GPU

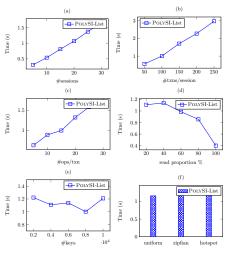
PolySI outperforms Cobra with GPU in 5 of the 6 benchmarks.



Cobra implements a specific optimization for RMW workloads (like TPC-C) before pruning and encoding.

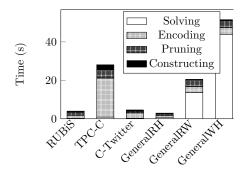
Performance Evaluation: PolySI-List

Integrate list inference of Elle [Kingsbury and Alvaro, 2020] into PolySI



Performance Evaluation: Decomposition

TPC-C incurs more overhead in *encoding* as the number of operations in total is 5x more than the others.



The *solving* time depends on the remaining constraints and unknown dependencies after pruning.