Efficient Black-box Checking of Snapshot Isolation in Databases

(Conference VLDB'2024)

Hengfeng Wei

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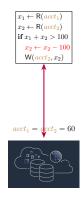
August 21, 2023





Transaction and Isolation Level

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$$\begin{aligned} x_1 \leftarrow \mathsf{R}(acct_1) \\ x_2 \leftarrow \mathsf{R}(acct_2) \\ \text{if } x_1 + x_2 > 100 \\ x_1 \leftarrow x_1 - 100 \\ \mathsf{W}(acct_1, x_1) \end{aligned}$$

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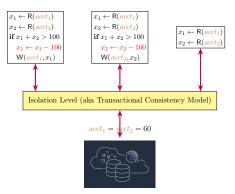
$$x_1 \leftarrow \mathsf{R}(\underbrace{acct_1}) \\ x_2 \leftarrow \mathsf{R}(\underbrace{acct_2})$$

$${\it acct}_1 = {\it acct}_2 = 60$$

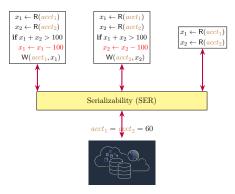


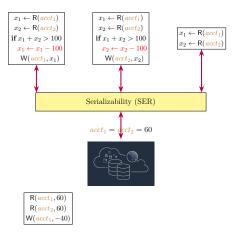
Transaction and Isolation Level

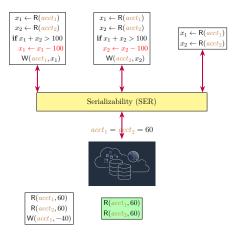
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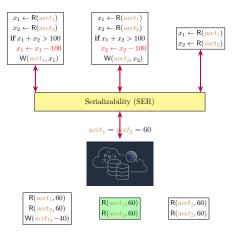


The isolation levels specify how they are isolated from each other.

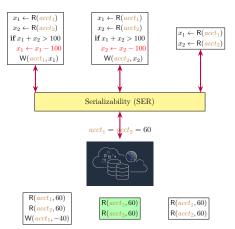




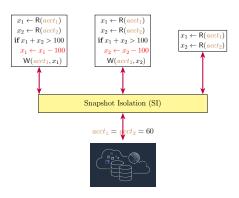


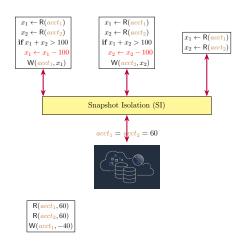


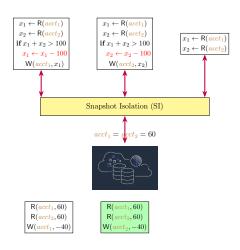
All transactions appear to execute in some total order.

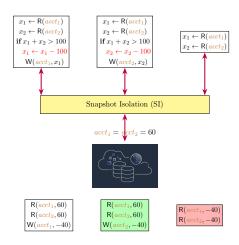


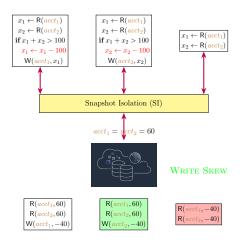
too expensive, especially for distributed transactions

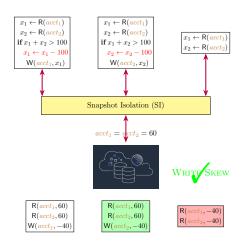


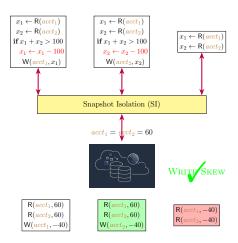




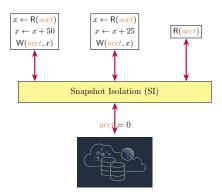


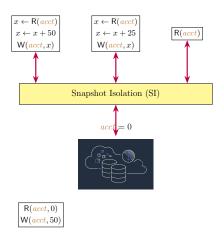


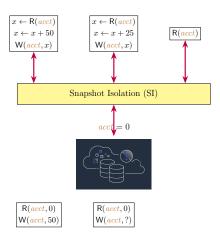


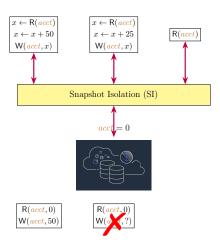


Snapshot Read: Each transaction reads data from a *snapshot* of committed data valid as of the (logical) time the transaction started.

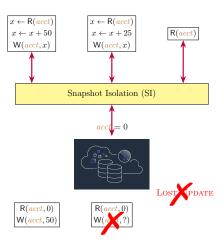




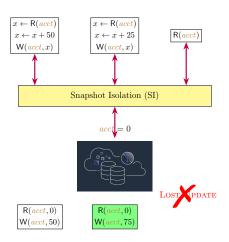




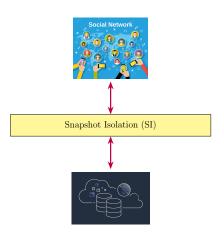
Snapshot Write: Concurrent transactions cannot write to the same key. One of them must be aborted.

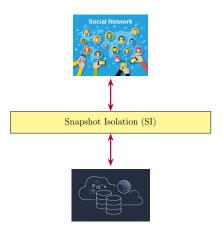


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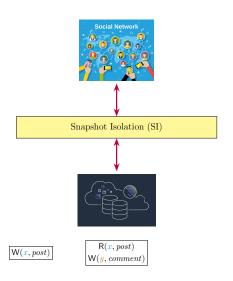


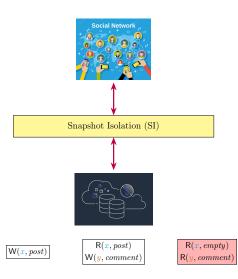
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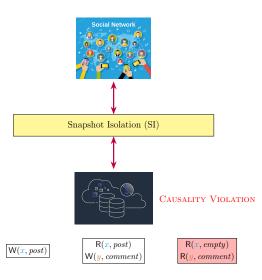


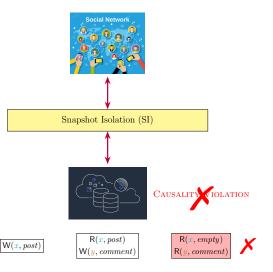












Databases and Snapshot Isolation

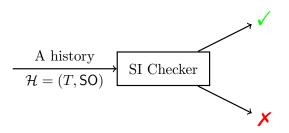
 ${\rm database\ logos}$ Many databases claim to support SI.

Databases and Snapshot Isolation

+papers
Databases may fail to provide SI as they claim.

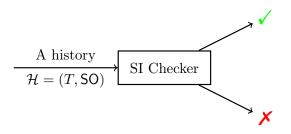
Definition (The SI Checking Problem)

The SI checking problem is the decision problem of determing whether a given history $\mathcal{H} = (T, SO)$ satisfies SI?



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 $\mathsf{SO}: session\ order\ \mathrm{among}\ \mathrm{the\ set}\ T\ \mathrm{of\ transactions}$

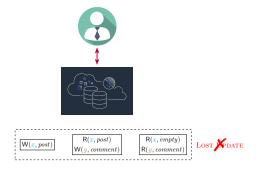
Black-box checking: do not rely on database internals



The histories are collected from database logs.



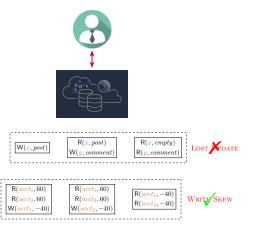
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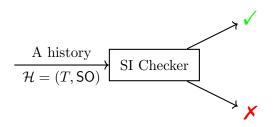
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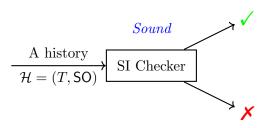


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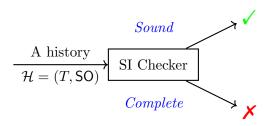


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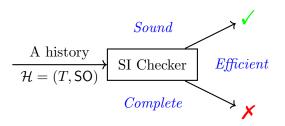




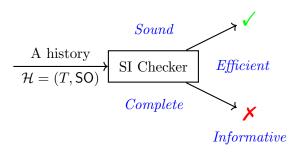
Sound: If the checker says \times , then the history does not satisfy SI.



Complete: If the checker says \checkmark , then the history satisfies SI.

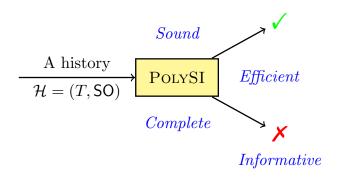


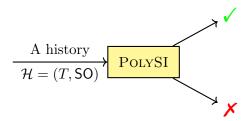
Efficient: The checker should *scale* up to large workloads.

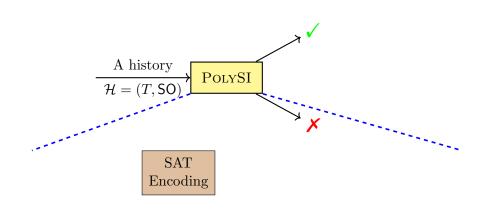


Informative: The checker should provide understandable counterexamples if it says \times .

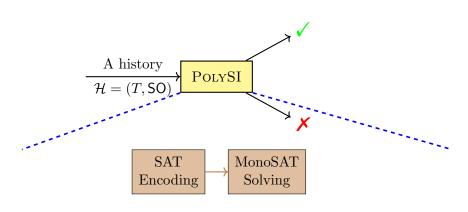
related-work



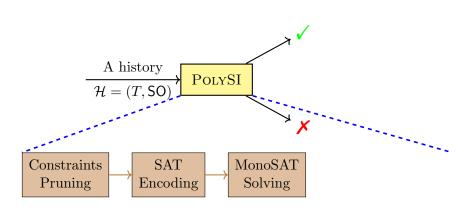




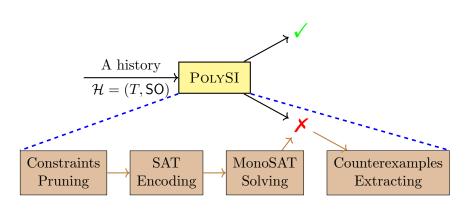
Sound & Complete: polygraph-based characterization of SI



Efficient: utilizing MonoSAT solver optimized for graph problems



Efficient: domain-specific pruning before encoding



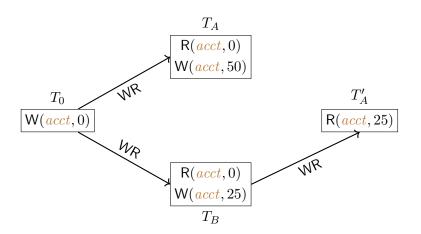
Informative: extract counterexamples from the unsatisifiable core



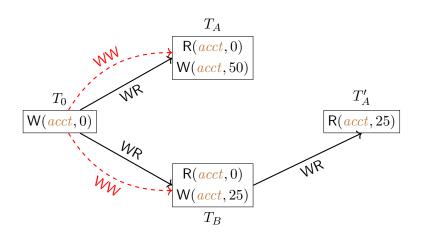
$$\frac{T_0}{\mathsf{W}({\color{red}acct},0)}$$

$$\frac{T_A'}{\mathsf{R}({\color{red}acct},25)}$$

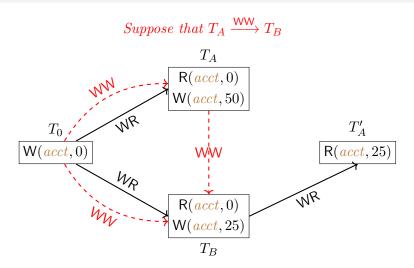
$$R({\it acct},0) \ W({\it acct},25) \ T_B$$



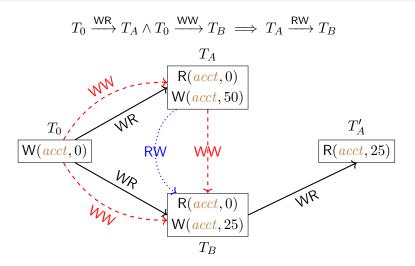
WR: "write-read" dependency capturing the "read-from" relation



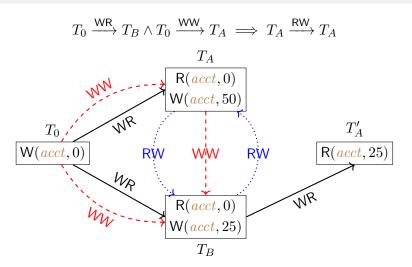
WW: "write-write" dependency capturing the version order



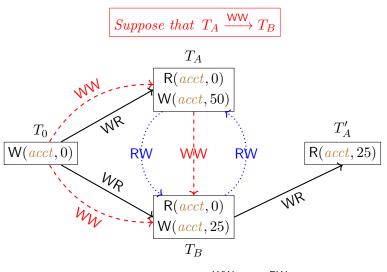
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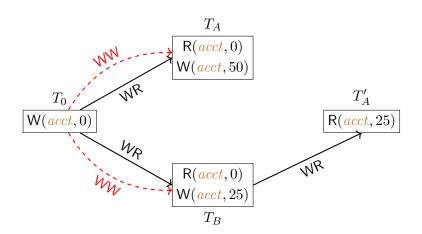
RW: "read-write" dependency capturing the overwritten relation

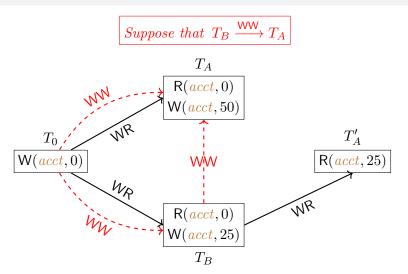


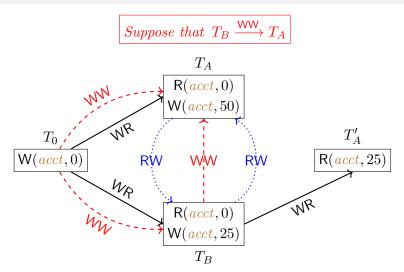
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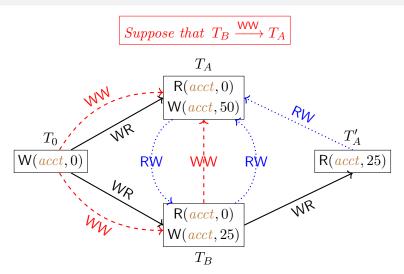


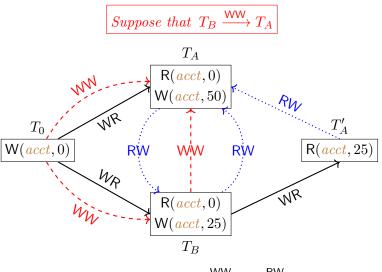
undesired cycle: $T_A \xrightarrow{WW} T_B \xrightarrow{RW} T_A$



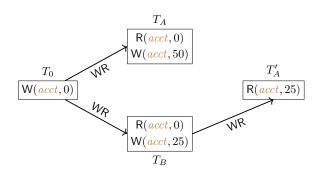








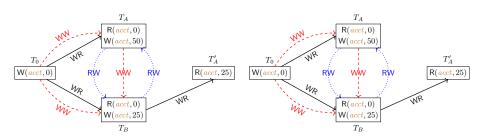
We have considered both bases $T_A \xrightarrow{\mathsf{WW}} T_B$ and $T_B \xrightarrow{\mathsf{WW}} T_A$.



Either case leads to an undesired cycle.

Therefore, it does not satisfy SI.

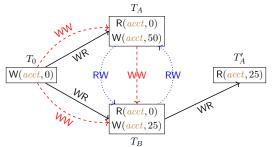
Theorem (Theorem 4.1 of [AnalysingSI:JACM2018])
Informally, a history satisfies SI if only if
there exists a dependency graph for it that contains
only cycles (if any) with at least two adjacent RW edges.



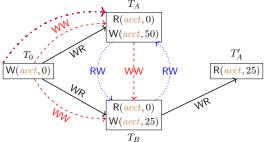
Every possible dependency graph contains an undesired



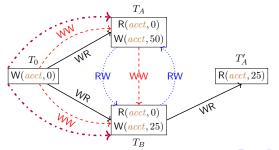
For a history
$$\mathcal{H} = (T, \mathsf{SO})$$
,
$$\mathcal{H} \models \mathsf{SI} \iff \mathcal{H} \models \mathsf{Int} \land$$
$$\exists \mathsf{WR}, \mathsf{WW}, \mathsf{RW}. \ \mathcal{G} = (\mathcal{H}, \mathsf{WR}, \mathsf{WW}, \mathsf{RW}) \land$$
$$(((\mathsf{SO}_{\mathcal{G}} \cup \mathsf{WR}_{\mathcal{G}} \cup \mathsf{WW}_{\mathcal{G}}) \ ; \ \mathsf{RW}_{\mathcal{G}}?) \ is \ acyclic).$$



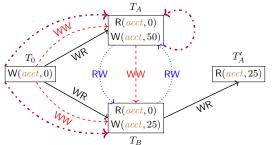
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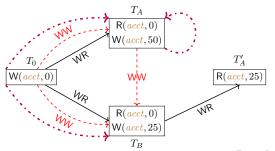
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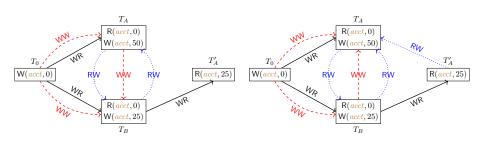
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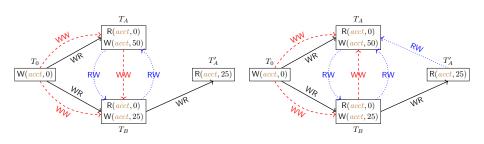
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\mathcal{Q} : How to capture and resolve all possible WW dependencies?



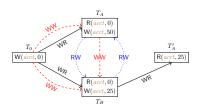
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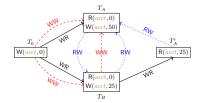


 \mathcal{A} : encode them into SAT formulas based on (generalized) polygraphs and solve them using SAT solvers.

Polygraphs: A Family of Dependency Graphs

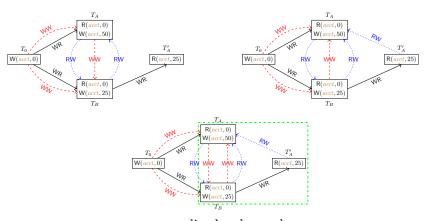
Consider the two cases of WW dependencies between T_A and T_B .





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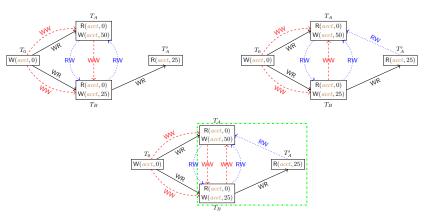
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generalized polygraph:

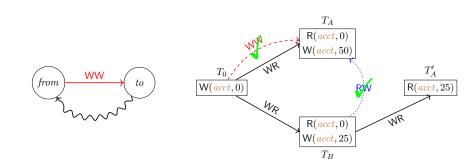
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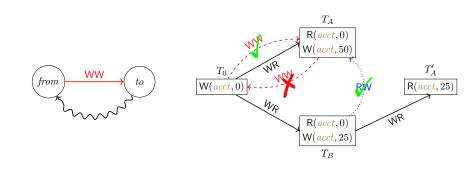
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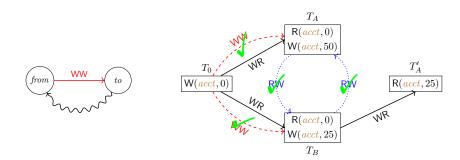
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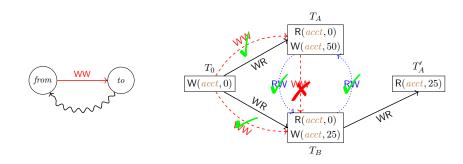




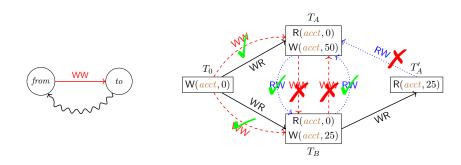


 $T_A \xrightarrow{\mathsf{WW}} T_0$ can be pruned due to the $T_A \xrightarrow{\mathsf{WW}} T_0 \xrightarrow{\mathsf{WR}} T_A$ cycle.

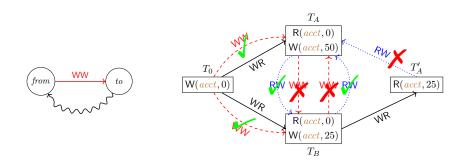




 $T_A \xrightarrow{WW} T_B$ is pruned due to the $T_A \xrightarrow{WW} T_B \xrightarrow{RW} T_A$ cycle.



 $T_A \xrightarrow{\mathsf{WW}} T_B$ is pruned due to the $T_A \xrightarrow{\mathsf{WW}} T_B \xrightarrow{\mathsf{RW}} T_A$ cycle. $T_B \xrightarrow{\mathsf{WW}} T_A$ is pruned due to the $T_B \xrightarrow{\mathsf{WW}} T_A \xrightarrow{\mathsf{RW}} T_B$ cycle.

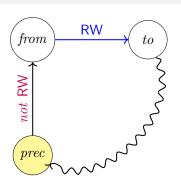


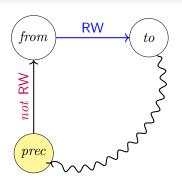
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Therefore, we are sure that the history does *not* satisfy SI.

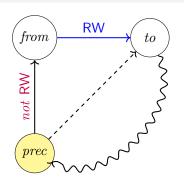








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$$T_0 \left[\mathsf{W}(x,0) \; \mathsf{W}(y,0) \right]$$



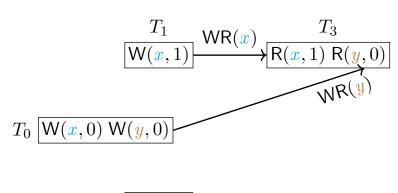
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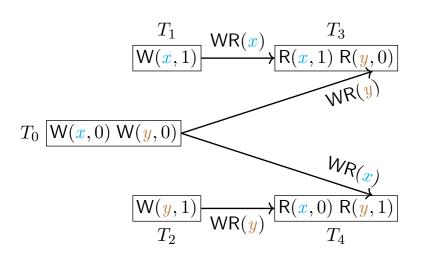
$$egin{aligned} T_1 \ \hline old (x,1) \end{bmatrix}$$

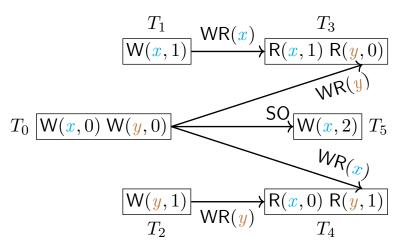
$$T_0 \left[\mathsf{W}(x,0) \; \mathsf{W}(y,0) \right]$$

$$\frac{ \left[\mathsf{W}({\color{red} {\color{red} {y}}},1) \right] }{T_2}$$

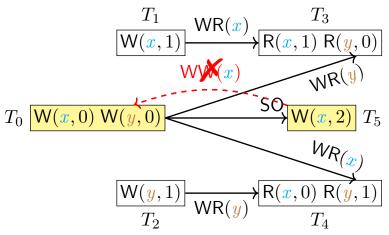




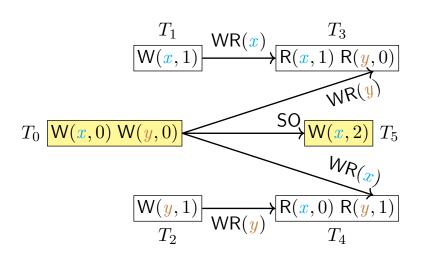


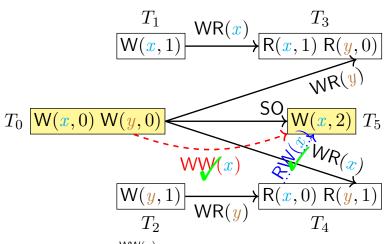


order between T_0 , T_1 , and T_5 (on x) and between T_0 and T_2 (on y)

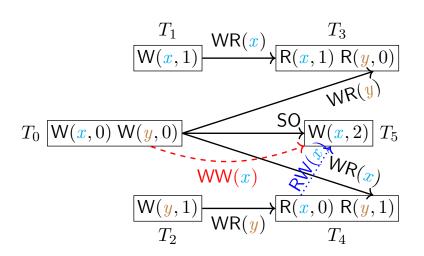


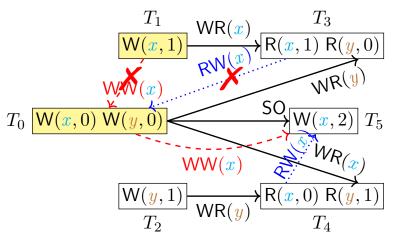
The $T_5 \xrightarrow{\mathsf{WW}(x)} T_0$ case is pruned due to $T_0 \xrightarrow{\mathsf{SO}} T_5 \xrightarrow{\mathsf{WW}(x)} T_0$.



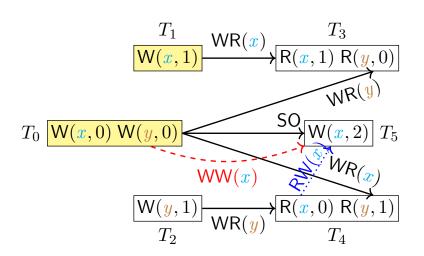


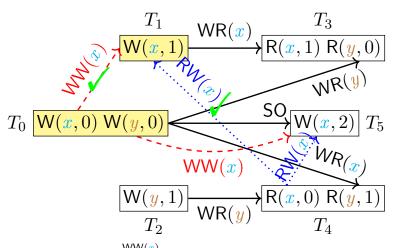
The $T_0 \xrightarrow{\text{WW}(x)} T_5$ case becomes known.



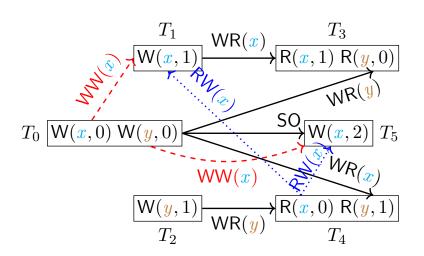


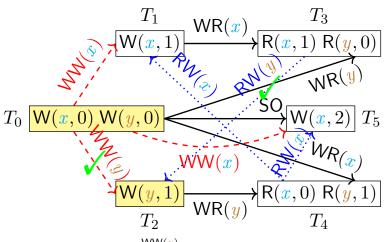
The $T_1 \xrightarrow{\mathsf{WW}(x)} T_0$ case is pruned due to $T_3 \xrightarrow{\mathsf{RW}(x)} T_0 \xrightarrow{\mathsf{WR}(y)} T_3$.



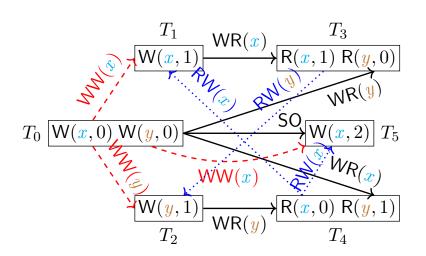


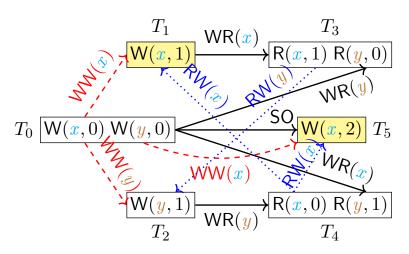
The $T_0 \xrightarrow{\mathsf{WW}(x)} T_1$ case becomes known.





The $T_2 \xrightarrow{\mathsf{WW}(y)} T_0$ case is pruned, while the $T_0 \xrightarrow{\mathsf{WW}(y)} T_2$ case becomes known.





The order between T_1 and T_5 is still uncertain after pruning.

〈 , , *)*

$$\begin{array}{c|c} T_1 & \mathsf{WR}(x) & T_3 \\ \hline \mathsf{W}(x,1) & \mathsf{R}(x,1) & \mathsf{R}(y,0) \end{array}$$

$$T_0 \left[\mathsf{W}(\boldsymbol{x},0) \; \mathsf{W}(\boldsymbol{y},0) \right]$$

$$W(x,2)$$
 T_5

$$\begin{array}{c} \left[\mathsf{R}(\boldsymbol{x},0) \; \mathsf{R}(\boldsymbol{y},1) \right] \\
T_4 \end{array}$$

$$\langle either = \{T_1 \xrightarrow{\mathsf{WW}(x)} T_5, T_3 \xrightarrow{\mathsf{RW}(x)} T_5\}, \qquad \rangle$$

$$T_1 \qquad \mathsf{WR}(x) \qquad T_3 \qquad \mathsf{R}(x, 1) \; \mathsf{R}(y, 0)$$

$$T_0 \qquad \mathsf{W}(x, 0) \; \mathsf{W}(y, 0) \qquad \mathsf{W}(x, 2) \; T_5$$

$$\mathsf{W}(y, 1) \qquad \mathsf{R}(x, 0) \; \mathsf{R}(y, 1)$$

$$T_2 \qquad \mathsf{R}(x, 0) \; \mathsf{R}(y, 1)$$

$$T_4$$

$$\langle either = \{T_1 \xrightarrow{\mathsf{WW}(x)} T_5, T_3 \xrightarrow{\mathsf{RW}(x)} T_5\}, or = \{T_5 \xrightarrow{\mathsf{WW}(x)} T_1\} \rangle$$

$$T_1 \xrightarrow{\mathsf{WR}(x)} R(x, 1) R(y, 0)$$

$$T_0 \xrightarrow{\mathsf{W}(x, 0)} W(y, 0) \xrightarrow{\mathsf{WW}(x)} R(x, 1) R(y, 0)$$

$$T_0 \xrightarrow{\mathsf{W}(x, 0)} W(y, 0) \xrightarrow{\mathsf{W}(x, 0)} R(y, 1)$$

$$T_2 \xrightarrow{\mathsf{R}(x, 0)} R(y, 1)$$

$$T_4$$

$$\langle either = \{T_1 \xrightarrow{\mathsf{WW}(x)} T_5, T_3 \xrightarrow{\mathsf{RW}(x)} T_5\}, or = \{T_5 \xrightarrow{\mathsf{WW}(x)} T_1\} \rangle$$

$$T_1 \xrightarrow{\mathsf{WR}(x)} T_3 \xrightarrow{\mathsf{RW}(x, 1)} \mathsf{R}(x, 1) \mathsf{R}(y, 0)$$

$$T_0 \xrightarrow{\mathsf{W}(x, 0)} \mathsf{W}(y, 0) \xrightarrow{\mathsf{W}(x, 2)} T_5$$

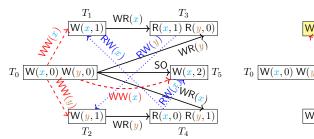
$$\mathsf{W}(x, 0) \xrightarrow{\mathsf{W}(x, 0)} \mathsf{W}(y, 0) \xrightarrow{\mathsf{W}(x, 2)} T_5$$

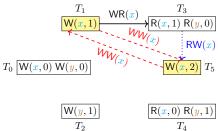
$$\mathsf{W}(x, 0) \xrightarrow{\mathsf{W}(x, 0)} \mathsf{R}(y, 1) \xrightarrow{\mathsf{T}_4} \mathsf{R}(x, 0) \xrightarrow{\mathsf{R}(x, 0)} \mathsf{R}(y, 1)$$

$$T_2 \xrightarrow{\mathsf{T}_4} \mathsf{R}(x, 0) \xrightarrow{\mathsf{R}(x, 0)} \mathsf{R}(y, 0)$$

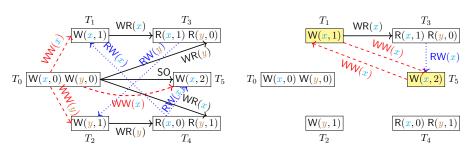
$$\mathsf{R}(x, 0) \xrightarrow{\mathsf{R}(x, 0)} \mathsf{R}(y, 0)$$

$$\mathsf{R}(x, 0) \xrightarrow{\mathsf{R}(x, 0)} \mathsf{R}(y, 0)$$

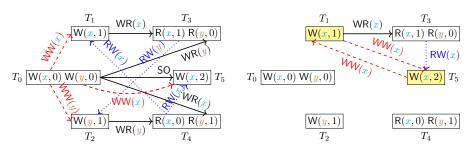




 $\label{eq:continuity} \boxed{ ((\mathsf{SO}_\mathcal{G} \cup \mathsf{WR}_\mathcal{G} \cup \mathsf{WW}_\mathcal{G}) \; ; \; \mathsf{RW}_\mathcal{G}?) } \; \; \mathit{is acyclic}.$

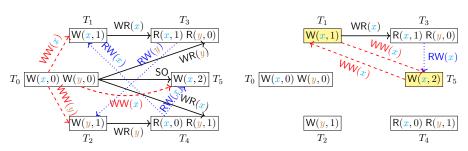


 $((SO_{\mathcal{G}} \cup WR_{\mathcal{G}} \cup WW_{\mathcal{G}}) \; ; \; RW_{\mathcal{G}}?) \quad \textit{is acyclic}.$



We need to encode the "composition (;)" of dependency edges.

 $((\mathsf{SO}_\mathcal{G} \cup \mathsf{WR}_\mathcal{G} \cup \mathsf{WW}_\mathcal{G}) \; ; \; \mathsf{RW}_\mathcal{G}?) \quad \textit{is acyclic}.$

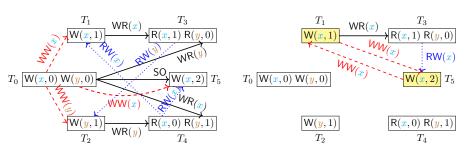


We need to encode the "composition (;)" of dependency edges.

$$T_1 \xrightarrow{\mathsf{WR}} T_3 \xrightarrow{\mathsf{RW}} T_2 : \mathsf{BV}_{1,2}^{I} = \mathsf{BV}_{1,3} \wedge \mathsf{BV}_{3,2} \quad (I \text{ for the induced graph})$$

→□ → ←団 → ← 重 → ← 重 → りへで

 $((SO_{\mathcal{G}} \cup WR_{\mathcal{G}} \cup WW_{\mathcal{G}}) ; RW_{\mathcal{G}}?)$ is acyclic.



We need to encode the "composition (;)" of dependency edges.

$$T_1 \xrightarrow{\mathsf{WR}} T_3 \xrightarrow{\mathsf{RW}} T_2 : \mathsf{BV}_{1,2}^{I} = \mathsf{BV}_{1,3} \land \mathsf{BV}_{3,2} \quad (I \text{ for the induced graph})$$
 $T_1 \xrightarrow{\mathsf{WR}} T_3 \xrightarrow{\mathsf{RW}} T_5 : \mathsf{BV}_{1,5}^{I} = \mathsf{BV}_{1,3} \land \mathsf{BV}_{3,5} \quad (I \text{ for the induced graph})$

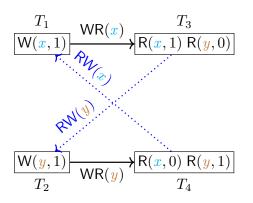
PolySI: An Illustrating Example of "Long Fork"

Feed the SAT formula into the MonoSAT solver [MonoSAT:AAAI2015] optimized for cycle detection



Assert that the induced graph I is acyclic.

PolySI: An Illustrating Example of "Long Fork"



The undesired cycle for "long fork" found by MonoSAT.

Experimental Evaluation

- (1) Effective: Can PolySI find SI violations in production databases?
- (2) *Informative:* Can PolySI provide understandable counterexamples for SI violations?
- (3) *Efficient:* How efficient is PolySI? Is it scalable?

https://github.com/hengxin/PolySI-PVLDB2023-Artifacts

Workloads

Table: Workload parameters and their default values.

Parameter	Default Value
#sess	20
#txns/sess	100
#ops/txn	15
#keys	10, 000
%reads	50%
distribution	zipfian

Benchmarks

RuBis: an eBay-like bidding system

TPC-C: an open standard for OLTP benchmarking

C-Twitter: a Twitter clone

GeneralRH: read-heavy workloads with 95% reads

GeneralRW: medium workloads with 50% reads

GeneralWH: write-heavy workloads with 30% reads

Use a simple database schema of a *two-column table* storing keys and values.

Finding SI Violations

Table: Reproducing known SI violations.

Database	GitHub Stars	Kind	Release
CockroachDB	25.1k	Relational	v2.1.0, v2.1.6
${\it MySQL-Galera}$	381	Relational	v25.3.26
${\bf YugabyteDB}$	6.7k	Multi-model	v1.1.10.0

An extensive collection of 2477 anomalous histories [Complexity:OOPSLA2019; CockroachDB-bug; YugabyteDB-bug]

Finding SI Violations

Dgraph: helped the Dgraph team confirm some of their suspicions about their latest release

Table: Detecting new violations.

Database	GitHub Stars	Kind	Release
Dgraph	18.2k	Graph	v21.12.0
MariaDB-Galera	4.4k	Relational	v10.7.3
YugabyteDB	6.7k	Multi-model	v2.11.1.0

Galera: confirmed the incorrect claim on preventing "lost updates" for transactions issued on different cluster nodes

Understanding Violations

Performance Evaluation

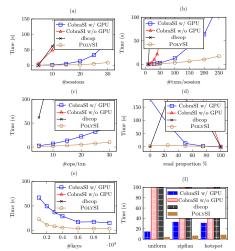
dbcop [Complexity:OOPSLA2019]: the state-of-the-art SI checker without using SAT solvers

Cobra [Cobra:OSDI2020]: the state-of-the-art SER checker using both MonoSAT and GPU; as a baseline

CobraSI: reducing SI checking to SER checking
[Complexity:OOPSLA2019] to leverage Cobra
with/without GPU

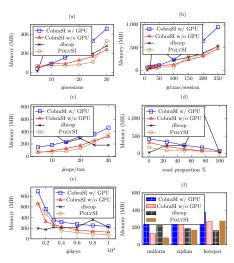
Performance Evaluation: Runtime

PolySI significantly outperforms the competitors.



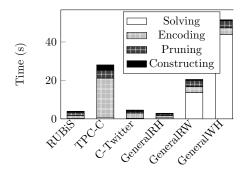
Performance Evaluation: Memory

PolySI consumes less memory.



Performance Evaluation: Decomposition

TPC-C incurs more overhead in *encoding* as the number of operations in total is 5x more than the others.



The solving time depends on the remaining constraints and unknown dependencies *after pruning*.

Performance Evaluation: Pruning

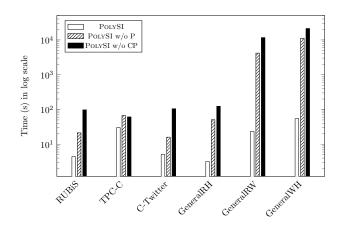
PolySI can effectively prune a huge number of constraints.

Benchmark	#cons.	#cons.	#unk. dep.	#unk. dep.
	before P	after P	before P	after P
TPC-C	386k	0	3628k	0
$\operatorname{GeneralRH}$	4k	29	39k	77
RUBiS	14k	149	171k	839
C-Twitter	59k	277	307k	776
${\it GeneralRW}$	90k	2565	401k	5435
GeneralWH	167k	6962	468k	14376

TPC-C: read-only transactions + RMW transactions

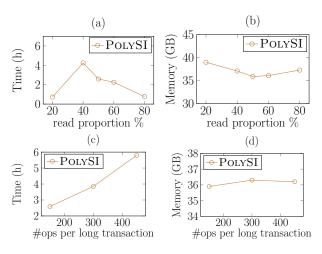
Performance Evaluation: Differential Analysis

Pruning is crucial to the efficiency of PolySI.

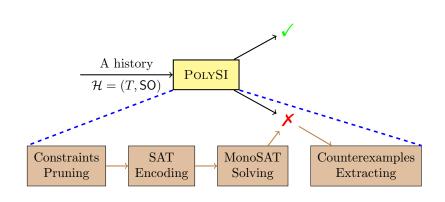


Performance Evaluation: Scalability

several hours and $35 \sim 40 \mathrm{GB}$ memory for checking 1M transactions



Conclusion





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