## Efficient Black-box Checking of Snapshot Isolation in Databases

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August 24, 2023

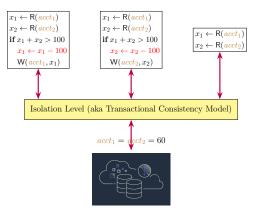




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#### Transaction and Isolation Level

A transaction is a *group* of operations that are executed atomically.



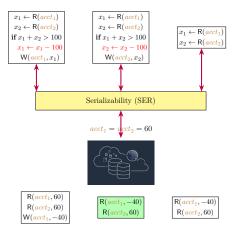
The isolation levels specify how they are isolated from each other.

PolySI: SI Checking

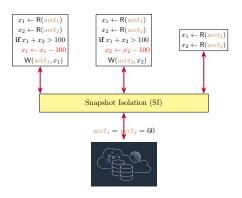
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## Serializability (SER)

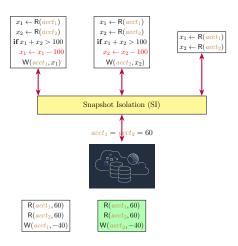
All transactions appear to be executed in some total order.



Implementing serializability is too expensive.

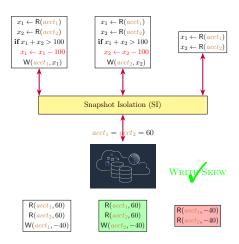


Snapshot Read: Each transaction reads data from a *snapshot* as of the time the transaction started.

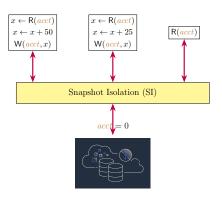


Snapshot Read: Each transaction reads data from a *snapshot* as of the time the transaction started.

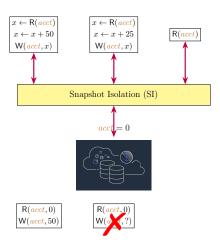
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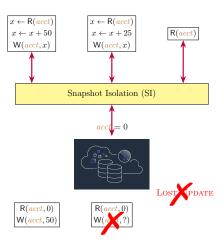
Snapshot Read: Each transaction reads data from a *snapshot* as of the time the transaction started.



Snapshot Write: Concurrent transactions *cannot* write to the same key. One of them must be aborted.



Snapshot Write: Concurrent transactions *cannot* write to the same key. One of them must be aborted.



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## Database systems and Snapshot Isolation

Many database systems implement snapshot isolation.





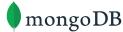






















## Database Systems and Snapshot Isolation

Database systems may fail to provide snapshot isolation correctly.





# Elle: Inferring Isolation Anomalies from Experimental Observations Kyle Kingsbury Peter Alvaro

Kyle Kingsbury Jepsen aphyr@jepsen.io

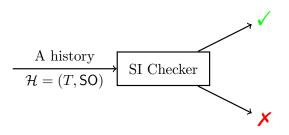
UC Santa Cruz palvaro@ucsc.edu



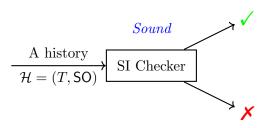


#### Definition (The SI Checking Problem)

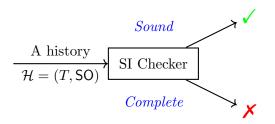
The SI checking problem is the decision problem of determing whether a history  $\mathcal{H} = (T, SO)$  of a database system satisfies SI?



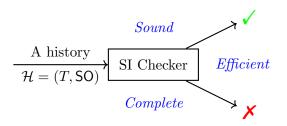
 $\mathsf{SO}: session\ order\ \mathrm{among}\ \mathrm{the\ set}\ T\ \mathrm{of\ transactions}$ 



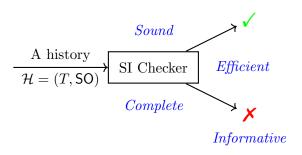
Sound: If the checker says  $\times$ , then the history does not satisfy SI.



Complete: If the checker says  $\checkmark$ , then the history satisfies SI.



*Efficient:* The checker should *scale* up to large workloads.



*Informative:* The checker should provide understandable counterexamples if it finds violations.

dbcop [Biswas and Enea, 2019] checker for SI

not practically efficient;

not informative, returning only "False" upon violations

Cobra [Tan et al., 2020] state-of-the-art checker for SER The SI checking problem is *harder*.

Elle [Kingsbury and Alvaro, 2020] checker for various isolation levels

Work perfectly on traceable and recoverable histories; but may be incomplete on the key-value datatype

<sup>&</sup>lt;sup>a</sup>Could Elle tell the difference between snapshot isolation and strong-session-snapshot-isolation? https://github.com/jepsen-io/elle/issues/17

<sup>&</sup>lt;sup>b</sup>Elle may miss two types of transaction anomalies.

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SI checking based on the Adya-style notions [Adya, 1999] relies on the start/commit timestamps of transactions.

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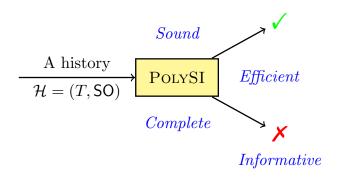
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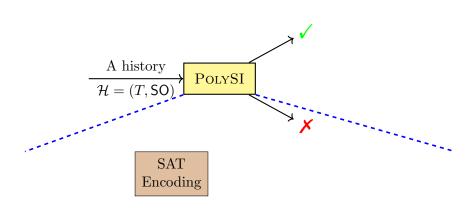
SI checking based on the Adya-style notions [Adya, 1999] relies on the start/commit timestamps of transactions.

SI checking based on the [Cerone and Gotsman, 2018] notions may miss SI violations.<sup>a</sup> b

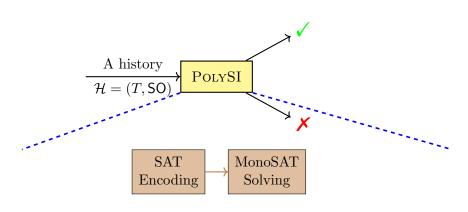
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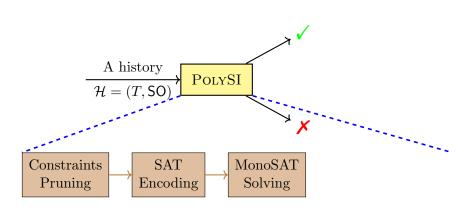




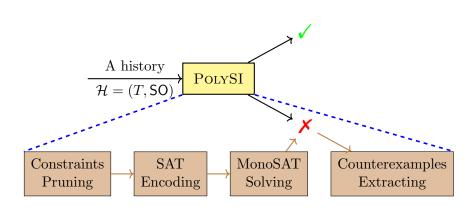
Sound & Complete: a novel polygraph based characterization of SI



Efficient: utilizing MonoSAT solver optimized for graph problems



Efficient: domain-specific pruning before encoding



Informative: extract counterexamples from the UNSAT core

## PolySI: Polygraph based Characterization of SI

Before this, we first review the *dependency graph* based characterization of SI [Cerone and Gotsman, 2018].

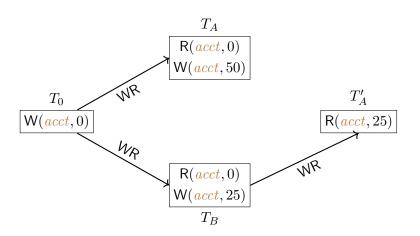
Theorem (Theorem 4.1 of [Cerone and Gotsman, 2018])
Informally, a history satisfies SI if and only if
there exists a dependency graph for it that
contains only cycles (if any) with at least two adjacent RW edges.



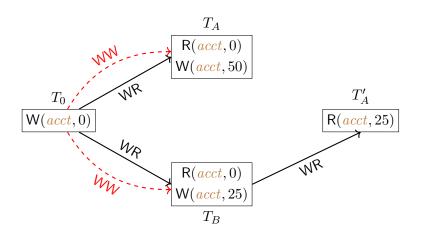
$$T_0$$
 $W(acct, 0)$ 

$$\frac{T_A''}{\mathsf{R}(\boldsymbol{\mathit{acct}},25)}$$

$$egin{array}{c} \mathsf{R}(m{acct},0) \ \mathsf{W}(m{acct},25) \ \hline T_B \end{array}$$



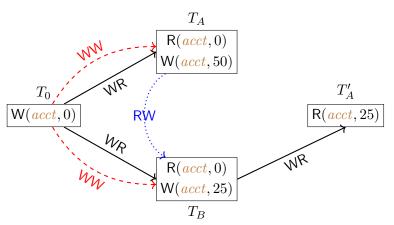
WR: "write-read" dependency capturing the "read-from" relation



WW: "write-write" dependency capturing the version order on acct

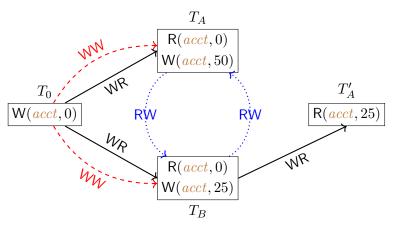
15/42

 $T_A$  reads from  $T_0$  which is overwritten by  $T_B$ 

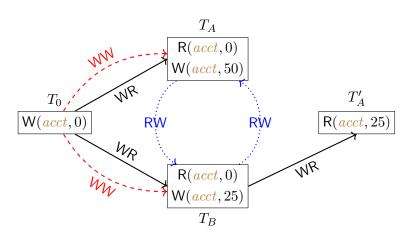


RW: "read-write" dependency

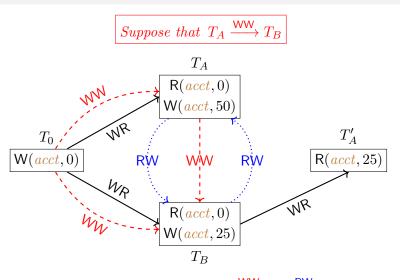
 $T_B$  reads from  $T_0$  which is overwritten by  $T_A$ 



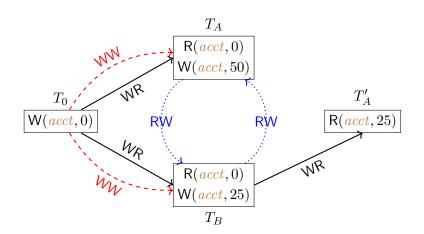
RW: "read-write" dependency

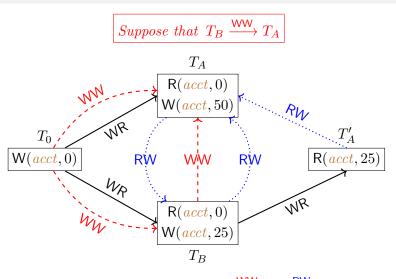


The cycle  $T_A \xrightarrow{\mathsf{RW}} T_B \xrightarrow{\mathsf{RW}} T_A$  is allowed by SI.



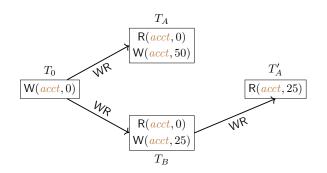
undesired cycle for SI:  $T_A \xrightarrow{WW} T_B \xrightarrow{RW} T_A$ 





undesired cycle for SI:  $T_B \xrightarrow{WW} T_A \xrightarrow{RW} T_B$ 

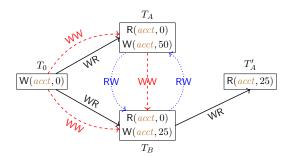
We have considered both bases  $T_A \xrightarrow{\text{WW}} T_B$  and  $T_B \xrightarrow{\text{WW}} T_A$ , and each case leads to an undesired cycle for SI.



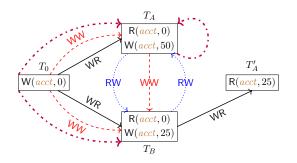
Therefore, this history does not satisfy SI.

Theorem (Equivalence of Theorem 4.1 of [Cerone and Gotsman, 2018]) Informally, a history satisfies SI if and only if there exists a dependency graph  $\mathcal{G}$  for it such that the induced graph  $((SO_{\mathcal{G}} \cup WR_{\mathcal{G}} \cup WW_{\mathcal{G}}); RW_{\mathcal{G}}?)$  is acyclic.

 $\mathit{induced\ graph} \ \overline{ \left( \left( \mathsf{SO}_{\mathcal{G}} \cup \mathsf{WR}_{\mathcal{G}} \cup \mathsf{WW}_{\mathcal{G}} \right) \; ; \; \mathsf{RW}_{\mathcal{G}} ? \right) } \ \mathit{for} \ \mathcal{G}$ 

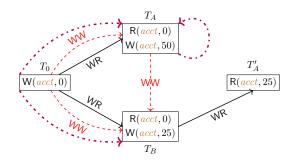


 $\mathit{induced\ graph}\left\lceil ((\mathsf{SO}_\mathcal{G} \cup \mathsf{WR}_\mathcal{G} \cup \mathsf{WW}_\mathcal{G}) \ ; \ \mathsf{RW}_\mathcal{G}?) \right\rceil \ \mathit{for} \ \mathcal{G}$ 



first composing (;) SO/WR/WW edges with RW edges

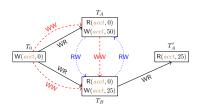
 $\mathit{induced\ graph}\left\lceil ((\mathsf{SO}_\mathcal{G} \cup \mathsf{WR}_\mathcal{G} \cup \mathsf{WW}_\mathcal{G}) \ ; \ \mathsf{RW}_\mathcal{G}?) \right\rceil \ \mathit{for} \ \mathcal{G}$ 

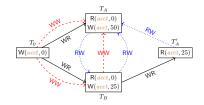


first composing ( ; )  $\mathsf{SO/WR/WW}$  edges with  $\mathsf{RW}$  edges then deleting the  $\mathsf{RW}$  edges

### Polygraph based Characterization of SI

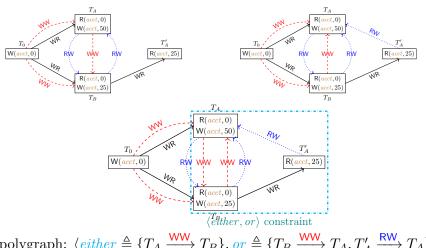
Consider the two cases of WW dependencies between  $T_A$  and  $T_B$ .





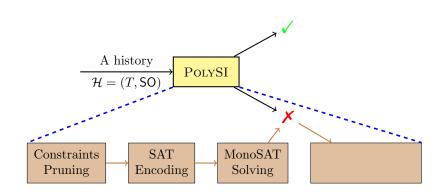
### Polygraph based Characterization of SI

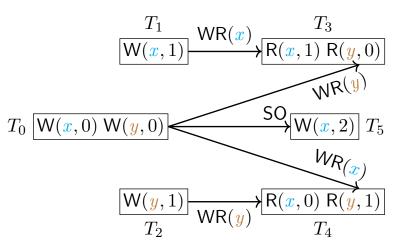
Consider the two cases of WW dependencies between  $T_A$  and  $T_B$ .



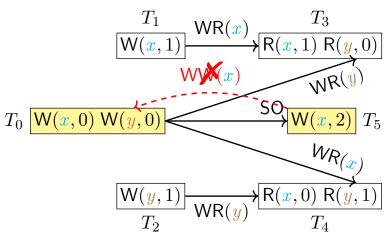
polygraph:  $\langle either \triangleq \{T_A \xrightarrow{\mathsf{WW}} T_B\}, or \triangleq \{T_B \xrightarrow{\mathsf{WW}} T_A, T_A' \xrightarrow{\mathsf{RW}} T_A\} \rangle$ 

To explain the whole PolySI procedure with a running example.

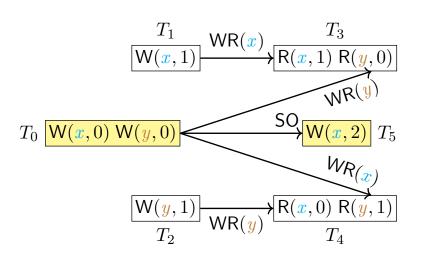


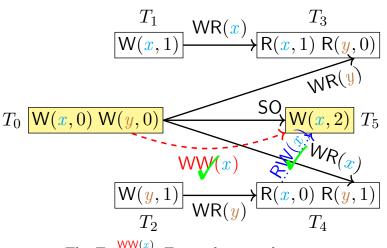


WW between  $T_0$ ,  $T_1$ , and  $T_5$  (on x) and between  $T_0$  and  $T_2$  (on y)

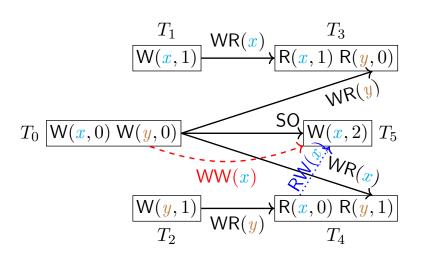


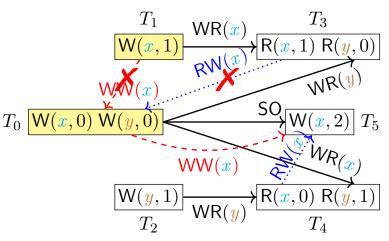
The  $T_5 \xrightarrow{\mathsf{WW}(x)} T_0$  case is pruned due to  $T_0 \xrightarrow{\mathsf{SO}} T_5 \xrightarrow{\mathsf{WW}(x)} T_0$ .





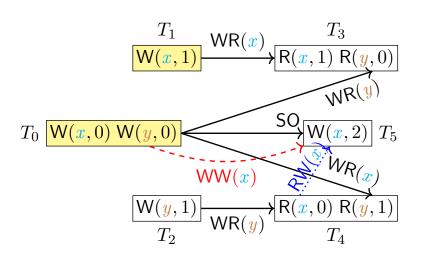
The  $T_0 \xrightarrow{\text{WW}(x)} T_5$  case becomes known.

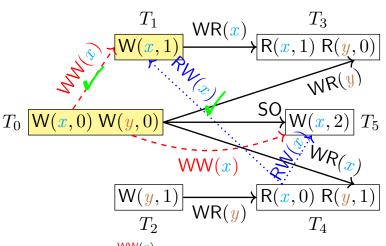




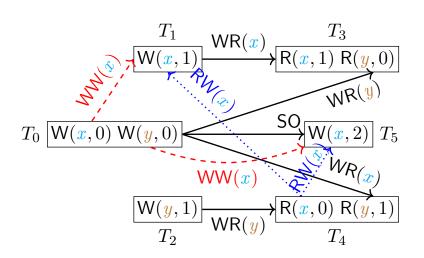
The  $T_1 \xrightarrow{\mathsf{WW}(x)} T_0$  case is pruned due to  $T_3 \xrightarrow{\mathsf{RW}(x)} T_0 \xrightarrow{\mathsf{WR}(y)} T_3$ .

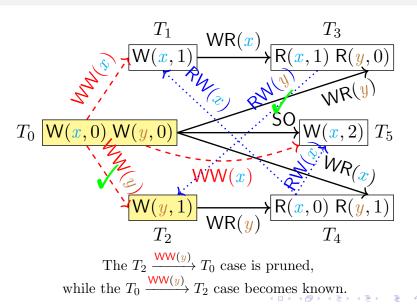
August 24, 2023

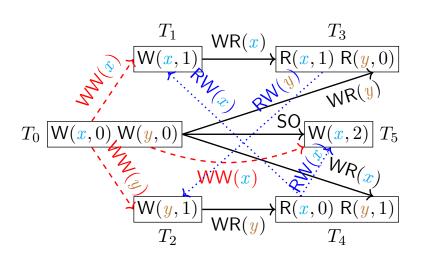


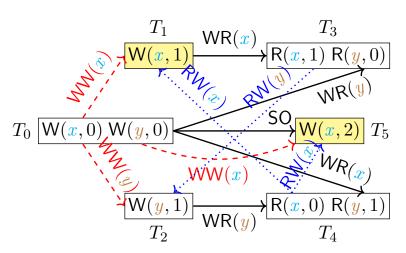


The  $T_0 \xrightarrow{\text{WW}(x)} T_1$  case becomes known.









The WW order between  $T_1$  and  $T_5$  is still uncertain after pruning.

 $\begin{array}{c} T_1 \\ \hline W(x,1) \end{array} \xrightarrow{WR(x)} \begin{array}{c} T_3 \\ \hline R(x,1) R(y,0) \end{array}$  $T_0 \left| \mathsf{W}(x,0) \; \mathsf{W}(y,0) \right|$  $|\mathbf{W}(x,2)| T_5$  $oxed{ egin{aligned} {\sf W}({\it y},1) \ T_2 \end{aligned} }$  $\frac{\left|\mathsf{R}(x,0)\;\mathsf{R}(y,1)\right|}{T_4}$ 

$$\langle either = \{T_1 \xrightarrow{\mathsf{WW}(x)} T_5, T_3 \xrightarrow{\mathsf{RW}(x)} T_5\}, or = \{T_5 \xrightarrow{\mathsf{WW}(x)} T_1\} \rangle$$

$$T_1 \qquad \mathsf{WR}(x) \qquad \mathsf{R}(x, 1) \; \mathsf{R}(y, 0)$$

$$\mathsf{W}(x, 1) \qquad \mathsf{RW}(x) \qquad \mathsf{RW}(x)$$

$$T_0 \; \mathsf{W}(x, 0) \; \mathsf{W}(y, 0) \qquad \mathsf{W}(x, 2) \; T_5$$

$$\mathsf{W}(y, 1) \qquad \mathsf{R}(x, 0) \; \mathsf{R}(y, 1)$$

$$T_2 \qquad \mathsf{R}(x, 0) \; \mathsf{R}(y, 1)$$

$$\langle either = \{T_1 \xrightarrow{\mathsf{WW}(x)} T_5, T_3 \xrightarrow{\mathsf{RW}(x)} T_5\}, or = \{T_5 \xrightarrow{\mathsf{WW}(x)} T_1\} \rangle$$

$$T_1 \qquad \mathsf{WR}(x) \qquad \mathsf{R}(x, 1) \; \mathsf{R}(y, 0)$$

$$T_0 \; \mathsf{W}(x, 0) \; \mathsf{W}(y, 0) \qquad \mathsf{W}(x, 2) \; \mathsf{T}_5$$

$$\mathsf{W}(x, 1) \qquad \mathsf{R}(x, 1) \; \mathsf{R}(y, 0)$$

$$\mathsf{W}(x, 2) \; \mathsf{T}_5$$

$$\mathsf{W}(x, 2) \; \mathsf{T}_5$$

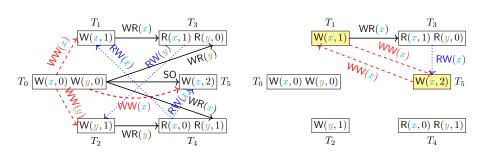
$$\mathsf{W}(x, 3) \; \mathsf{W}(x, 2) \; \mathsf{T}_5$$

$$\mathsf{W}(x, 3) \; \mathsf{W}(x, 3)$$

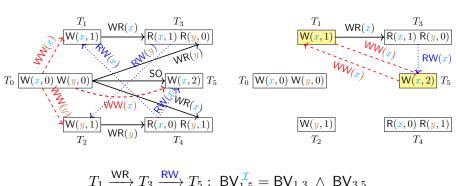
$$\mathsf{W}(x, 3) \; \mathsf{W}(x, 3)$$

$$\mathsf{W}(x, 3) \; \mathsf{W}(x, 3) \; \mathsf$$

 $\mathrm{induced\ graph}\ \mathcal{I}\ \left(\left(\mathsf{SO}_{\mathcal{G}}\cup\mathsf{WR}_{\mathcal{G}}\cup\mathsf{WW}_{\mathcal{G}}\right)\ ;\ \mathsf{RW}_{\mathcal{G}}?\right)$ 



induced graph  $\mathcal{I} \mid ((SO_{\mathcal{G}} \cup WR_{\mathcal{G}} \cup WW_{\mathcal{G}}); RW_{\mathcal{G}}?) \mid$ 

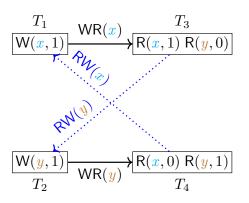


$$T_1 \xrightarrow{\mathsf{WR}} T_3 \xrightarrow{\mathsf{RW}} T_5: \; \mathsf{BV}_{1,5}^{\, \mathcal{I}} = \mathsf{BV}_{1,3} \; \wedge \; \mathsf{BV}_{3,5}$$

$$T_1 \xrightarrow{\mathsf{WR}} T_3 \xrightarrow{\mathsf{RW}} T_2 : \mathsf{BV}_{1,2}^{\mathcal{I}} = \mathsf{BV}_{1,3} \wedge \mathsf{BV}_{3,2}$$

Feed the SAT formula into the MonoSAT solver [Bayless et al., 2015] which is optimized for *cycle detection* 





The MonoSAT solver finds an undesired cycle for SI.

# Experimental Evaluation

- (1) *Effective:* Can PolySI find SI violations in production databases?
- (2) *Informative:* Can PolySI provide understandable counterexamples for SI violations?
- (3) *Efficient*: How efficient is PolySI?

#### Workloads

Table: Workload parameters and their default values.<sup>c</sup>

Parameter	Default Value
#sess	20
#txns/sess	100
#ops/txn	15
#keys	10, 000
%reads	50%
distribution	zipfian

<sup>&</sup>lt;sup>c</sup>We use a database schema of a two-column table storing keys and values.

#### Benchmarks

RuBiS: an eBay-like bidding system

TPC-C: an open standard for OLTP benchmarking

C-Twitter: a Twitter clone

GeneralRH: read-heavy workloads with 95% reads

GeneralRW: medium workloads with 50% reads

GeneralWH: write-heavy workloads with 30% reads

#### Reproducing Known SI Violations

Database	GitHub Stars	Kind	Release
$\rm Cockroach DB^d$	25.1k	Relational	v2.1.0 <sup>e</sup> , v2.1.6
${\it MySQL-Galera}$	381	Relational	v25.3.26
YugabyteDB	6.7k	Multi-model	$v1.1.10.0^{f}$

#### An extensive collection of 2477 anomalous histories

[Biswas and Enea, 2019; Darnell, Accessed February 14, 2023; Jepsen, Accessed February 14, 2023]

<sup>&</sup>lt;sup>d</sup>Remove SNAPSHOT isolation since (probably) v2.0.4. https://github.com/cockroachdb/cockroach/pull/27040

<sup>&</sup>lt;sup>e</sup>Lessons learned from 2+ years of nightly Jepsen tests. https://www.cockroachlabs.com/blog/jepsen-tests-lessons/

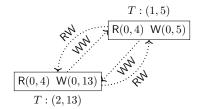
fAcknowledged inserts can be present in reads for tens of seconds, then disappear. https://github.com/YugaByte/yugabyte-db/issues/824

### Detecting New SI Violations

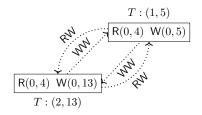
Dgraph: helped the Dgraph team confirm some of their suspicions about their latest release

Database	GitHub Stars	Kind	Release
Dgraph	18.2k	Graph	v21.12.0
MariaDB-Galera	4.4k	Relational	v10.7.3
${\bf YugabyteDB}$	6.7k	Multi-model	v2.11.1.0

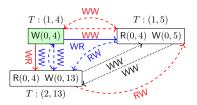
Galera: confirmed the incorrect claim on preventing "lost updates" for transactions issued on different cluster nodes



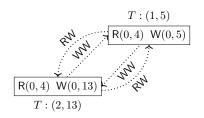
(a) Original output



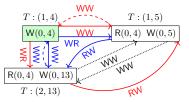
(a) Original output



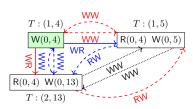
(b) Missing participants



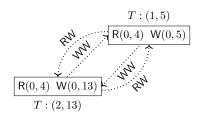
(a) Original output



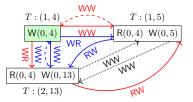
(c) Recovered scenario



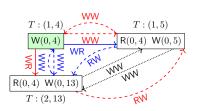
(b) Missing participants



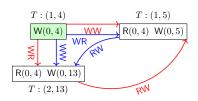
(a) Original output



(c) Recovered scenario



(b) Missing participants



(d) Finalized scenario

#### Performance Evaluation

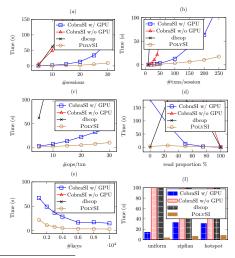
dbcop [Biswas and Enea, 2019]: the state-of-the-art SI checker

CobraSI: reducing SI checking to SER checking [Biswas and Enea, 2019] to leverage Cobra with/without GPU

Cobra [Tan et al., 2020]: the state-of-the-art SER checker using both MonoSAT and GPU

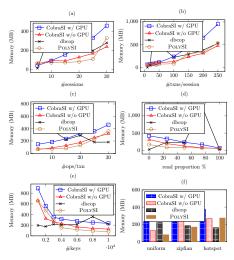
#### Performance Evaluation: Runtime

#### PolySI significantly outperforms the competitors.<sup>g</sup>



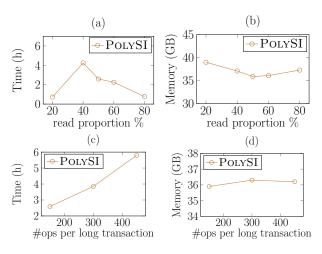
#### Performance Evaluation: Memory

#### PolySI consumes less memory.



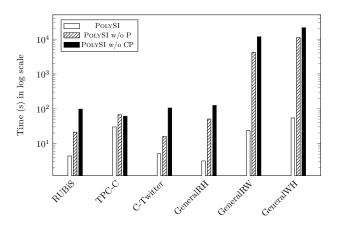
#### Performance Evaluation: Scalability

several hours and  $35 \sim 40 \mathrm{GB}$  memory for checking 1M transactions



#### Performance Evaluation: Differential Analysis

Pruning (P) is crucial to the efficiency of PolySI.<sup>h</sup>



<sup>&</sup>lt;sup>h</sup>Compacting (C) encoding has been omitted in this presentation.

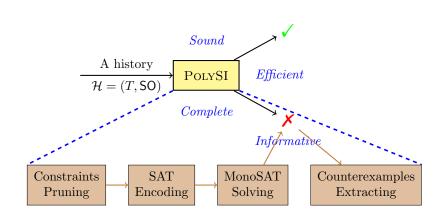
### Performance Evaluation: Pruning

PolySI can prune a huge number of constraints before encoding.

Benchmark	#cons.	#cons.	#unk. dep.	#unk. dep.
	before P	after P	before P	after P
TPC-C	386k	0	3628k	0
$\operatorname{GeneralRH}$	4k	29	39k	77
RUBiS	14k	149	171k	839
C-Twitter	59k	277	307k	776
${\it GeneralRW}$	90k	2565	401k	5435
GeneralWH	167k	6962	468k	14376

TPC-C: read-only transactions + RMW transactions

#### Conclusion



#### Future Work

PolySI uses MonoSAT as a black-box.

Working on a theory solver dedicated to isolation level checking, which is deeply integrated with SAT solvers [He, Sun, and Fan, 2021].



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Adya, Atul (1999). "Weak Consistency: A Generalized Theory and Optimistic Implementations for Distributed Transactions". PhD thesis. USA.



Bayless, Sam, Noah Bayless, Holger H. Hoos, and Alan J. Hu (2015). "SAT modulo Monotonic Theories". In: *Proceedings of the Twenty-Ninth AAAI Conference on Artificial Intelligence*. AAAI'15. AAAI Press, pp. 3702–3709. ISBN: 0262511290.



Biswas, Ranadeep and Constantin Enea (Oct. 2019). "On the Complexity of Checking Transactional Consistency". In: *Proc. ACM Program. Lang.* 3.OOPSLA. DOI: 10.1145/3360591. URL: https://doi.org/10.1145/3360591.



Cerone, Andrea and Alexey Gotsman (Jan. 2018). "Analysing Snapshot Isolation". In: J.~ACM~65.2.~ISSN:~0004-5411.~DOI:~10.1145/3152396.~URL:~https://doi.org/10.1145/3152396.



Darnell, Ben (Accessed February 14, 2023). Lessons Learned from 2+ Years of Nightly Jepsen Tests.

https://www.cockroachlabs.com/blog/jepsen-tests-lessons/.



He, Fei, Zhihang Sun, and Hongyu Fan (2021). "Satisfiability modulo Ordering Consistency Theory for Multi-Threaded Program Verification". In: Proceedings of the 42nd ACM SIGPLAN International Conference on Programming Language Design and Implementation. PLDI 2021. Virtual, Canada: Association for Computing Machinery, pp. 1264–1279. ISBN: 9781450383912. DOI: 10.1145/3453483.3454108. URL: https://doi.org/10.1145/3453483.3454108.



Jepsen (Accessed February 14, 2023). *Issue #824*. https://github.com/YugaByte/yugabyte-db/issues/824.



Kingsbury, Kyle and Peter Alvaro (Nov. 2020). "Elle: Inferring Isolation Anomalies from Experimental Observations". In: *Proc. VLDB Endow.* 14.3, pp. 268–280. ISSN: 2150-8097.



Tan, Cheng, Changgeng Zhao, Shuai Mu, and Michael Walfish (2020). "COBRA: Making Transactional Key-Value Stores Verifiably Serializable". In: *OSDI'20*. ISBN: 978-1-939133-19-9.