

Parsing with Combinators

Functional Programming (CS-210)

EPFL

Parsing

People write code using **text** (sequences of characters).

```
"""
```

```
(def double(n) = (n + n)  
  double 4)
```

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(def double(n) = (n + n)  
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But writing an interpreters (or compilers) is way easier on **trees**.

```
Defs(  
  List(("double", Fun("n", BinOp(Plus, N("n"), N("n"))))),  
  Call(N("double"), C(4)))
```

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(def double(n) = (n + n)  
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```
Defs(  
  List(("double", Fun("n", BinOp(Plus, N("n"), N("n"))))),  
  Call(N("double"), C(4)))
```

This representation immediately exposes the structure of the code, while the text representation does not.

Parsing

Therefore, in such projects somebody has to write a conversion from text to trees.

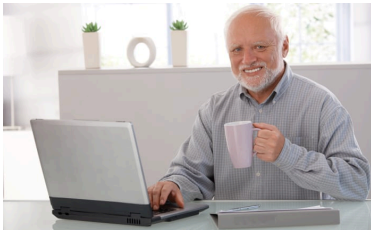
```
def parse(input: List[Char]): Expr
```

Parsing

Therefore, in such projects somebody has to write a conversion from text to trees.

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def parse(input: List[Char]): Expr
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If you take ***Computer Language Processing (CS-320)***, this person will be you!



Parsing

Writing such functions can be very tricky. ***Parser Combinators*** are one way to go about handling this complexity.

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Writing such functions can be very tricky. ***Parser Combinators*** are one way to go about handling this complexity.

Simple idea:

- ▶ Very simple basic parsers
- ▶ Ways to combine parsers into more complex parsers

Parser Combinator Libraries

There exist many parser combinator libraries in Scala:

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What I will present is the ***general idea*** behind many such libraries.

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What I will present is the ***general idea*** behind many such libraries.

The actual implementation may vary but the basic interface will often remain the same.

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case class Parser(parse: List[Char] => (Expr, List[Char]))
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Returning multiple alternatives:

```
case class Parser(parse: List[Char] => LazyList[(Expr, List[Char])])
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Returning multiple alternatives:

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case class Parser(parse: List[Char] => LazyList[(Expr, List[Char])])
```

Abstracting over the type of trees:

```
case class Parser[+A](parse: List[Char] => LazyList[(A, List[Char])])
```

Parser objects

```
// Method of Parser[+A]
def apply(input: List[Char]): Option[A] = {
  this
    .parse(input)
    .filter(_._2.isEmpty)
    .map(_._1)
    .headOption
}
```

Parser objects

```
def parse(input: List[Char]): Tree = {  
  val parser: Parser[Tree] = ???  
  
  parser(input).getOrElse{ throw new ParseError() }  
}
```

Parser objects

```
def parse(input: List[Char]): Tree = {  
    val parser: Parser[Tree] = ??? // How to build this?  
  
    parser(input).getOrElse{ throw new ParseError() }  
}
```

Example: Parser for sums

```
val letter: Parser[Char] = elem(_.isLetter)

val variable: Parser[SumExpr] = letter.map(Var(_))

val digit: Parser[Char] = elem(_.isDigit)

val number: Parser[SumExpr] =
  many(digit)
    .filter(_.length > 0)
    .map(ds => Num(BigInt(ds.mkString(""))))

val atom: Parser[SumExpr] = number | variable

val plus: Parser[Char] = elem('+')

val sum: Parser[SumExpr] =
  (atom ~ many(plus ~> atom)).map {
    case n ~ ns => Sum(n +: ns)
  }
```

Building Parsers



Basic Parsers

Matching a single character:

```
val item: Parser[Char] =  
  Parser(input => input match {  
    case c :: cs => LazyList((c, cs))  
    case _ => LazyList()  
  })
```

Basic Parsers

Returning a value without looking at the input:

```
def success[A](value: A): Parser[A] =  
  Parser(input => LazyList((value, input)))
```

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Returning a value without looking at the input:

```
def success[A](value: A): Parser[A] =  
  Parser(input => LazyList((value, input)))
```

Always failing:

```
val failure: Parser[Nothing] =  
  Parser(input => LazyList())
```

Building Complex Parsers



Building Complex Parsers



Filtering Out Values

Filtering out unwanted values:

```
// Method of Parser[+A]
def filter(predicate: A => Boolean): Parser[A] =
  Parser(input => this.parse(input).filter {
    case (value, _) => predicate(value)
  })
```

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```
// Method of Parser[+A]
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```
def filter(predicate: A => Boolean): Parser[A] =  
  Parser(input => this.parse(input).filter {  
    case (value, _) => predicate(value)  
  })
```

```
def elem(predicate: Char => Boolean): Parser[Char] =  
  item.filter(predicate)
```

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// Method of Parser[+A]
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```
def filter(predicate: A => Boolean): Parser[A] =  
  Parser(input => this.parse(input).filter {  
    case (value, _) => predicate(value)  
  })
```

```
def elem(predicate: Char => Boolean): Parser[Char] =  
  item.filter(predicate)
```

```
def elem(char: Char): Parser[Char] =  
  elem(_ == char)
```


Transforming Values

Modifying the parsed value:

```
// Method of Parser[+A]
def map[B](function: A => B): Parser[B] =
  Parser(input => this.parse(input).map {
    case (value, rest) => (function(value), rest)
  })
```

Example:

```
val variable: Parser[SumExpr] = letter.map(Var(_))
```

Sequencing Parsers

Sequencing parsers:

```
// Method of Parser[+A]
def ~[B](that: Parser[B]): Parser[(A, B)] =
  Parser(input =>
    for {
      (leftValue, leftRest)  <- this.parse(input)
      (rightValue, rightRest) <- that.parse(leftRest)
    } yield ((leftValue, rightValue), rightRest))
```

Sequencing Parsers

Parser combinator libraries generally introduce a bit of sugar...

```
// Method of Parser[+A]  
def ~[B](that: Parser[B]): Parser[A ~ B] =  
    // ^^^^^
```

Instead of pairs, they will use something like:

```
case class ~[+A, +B](_1: A, _2: B)
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    // ^^^^^
```

Instead of pairs, they will use something like:

```
case class ~[+A, +B](_1: A, _2: B)
```

Which is simply to provide better looking pattern matching:

```
val sum: Parser[SumExpr] =
  (atom ~ many(plus ~> atom)).map {
    case n ~ ns => Sum(n +: ns)
  }
```

Sequencing Parsers

Sometimes, we wish to only keep the value from one side of a sequence and ignore the other.

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```
// Methods of Parser[+A]  
def <~(that: Parser[Any]): Parser[A] = (this ~ that).map {  
  case left ~ _ => left  
}
```

Sequencing Parsers

Sometimes, we wish to only keep the value from one side of a sequence and ignore the other.

```
// Methods of Parser[+A]
```

```
def <~(that: Parser[Any]): Parser[A] = (this ~ that).map {  
  case left ~ _ => left  
}
```

```
def ~>[B](that: Parser[B]): Parser[B] = (this ~ that).map {  
  case _ ~ right => right  
}
```

Introducing Alternatives

Specifying alternatives:

```
// Method of Parser[+A]  
def |[B >: A](that: Parser[B]): Parser[B] =  
  Parser(input => this.parse(input) #::: that.parse(input))
```


Introducing Alternatives

Specifying alternatives:

```
// Method of Parser[+A]  
def |[B >: A](that: Parser[B]): Parser[B] =  
  Parser(input => this.parse(input) #::: that.parse(input))
```

Example:

```
val atom: Parser[SumExpr] = number | variable
```

Optional Parsers

Making a parser optional:

```
// Method of Parser[+A]  
def optional: Parser[Option[A]] =  
  this.map(Some(_)) | success(None)
```

Using Recursion

How to parse sums with parentheses?

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Using recursion!

```
lazy val parensSum = elem('(') ~> sum <~ elem('')
```

```
lazy val atom: Parser[SumExpr] = number | variable | parensSum
```

```
val plus: Parser[Char] = elem('+')
```

```
lazy val sum: Parser[SumExpr] = {  
  (atom ~ many(plus ~> atom)).map {  
    case n ~ ns => Sum(n +: ns)  
  }  
}
```

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```
lazy val atom: Parser[SumExpr] = number | variable | parensSum
```

```
val plus: Parser[Char] = elem('+')
```

```
lazy val sum: Parser[SumExpr] = defer { // < Change here!  
  (atom ~ many(plus ~> atom)).map {  
    case n ~ ns => Sum(n +: ns)  
  }  
}
```

Using Recursion

```
def defer[A](parser: => Parser[A]): Parser[A] = {  
  lazy val cached: Parser[A] = parser  
  Parser(cached.parse(_))  
}
```


Repeating Parsers

Repeating a parser:

```
def many[A](parser: Parser[A]): Parser[List[A]] = {  
  lazy val repeated: Parser[List[A]] = defer {  
    (parser ~ repeated).map { case x ~ xs => x :: xs } |  
    success(List())  
  }  
  
  repeated  
}
```

Using Recursion

Some libraries don't have `defer`, and instead pass arguments ***by name*** instead of *by value* for the various combinators.

```
// Methods of Parser[+A]
def ~[B](that: => Parser[B]): Parser[A ~ B] = ...

def |[B >: A](that: => Parser[B]): Parser[B] = ...
```

Handling Spaces

Spaces everywhere!

```
val input =  
    " (3 + 4 ) + x + y  "  
// ^  ^ ^ ^ ^ ^ ^ ^ ^
```

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val input =  
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One solution:

```
val space: Parser[Char] = elem(_ .isWhitespace)
```

Handling Spaces

Spaces everywhere!

```
val input =  
  " (3 + 4 ) + x + y "  
// ^  ^ ^ ^ ^ ^ ^ ^ ^
```

One solution:

```
val space: Parser[Char] = elem(_.isWhitespace)
```

```
def token[A](parser: Parser[A]): Parser[A] = parser <~ many(space)
```

Handling Spaces

Spaces everywhere!

```
val input =  
  " (3 + 4 ) + x + y "  
// ^  ^ ^ ^ ^ ^ ^ ^ ^
```

One solution:

```
val space: Parser[Char] = elem(_.isWhitespace)  
  
def token[A](parser: Parser[A]): Parser[A] = parser <~ many(space)  
  
val variable: Parser[SumExpr] = token(letter.map(Var(_)))
```

Handling Spaces

Spaces everywhere!

```
val input =  
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// ^  ^ ^ ^ ^ ^ ^ ^ ^
```

One solution:

```
val space: Parser[Char] = elem(_.isWhitespace)  
  
def token[A](parser: Parser[A]): Parser[A] = parser <~ many(space)  
  
val variable: Parser[SumExpr] = token(letter.map(Var(_)))  
  
lazy val parser: Parser[SumExpr] = many(space) ~> sum
```

Lexing

Another solution is to write a ***lexer*** to handle spaces, comments and more!

```
def lex(input: List[Char]): List[Token] = ...
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Then, the parser operates on sequences of ***tokens*** instead of Chars.

```
def parse(input: List[Token]): Expr = ...
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Lexing

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Then, the parser operates on sequences of ***tokens*** instead of Chars.

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def parse(input: List[Token]): Expr = ...
```

Some parser combinators libraries support both styles, and even provide ways to write lexers using the similar combinators.

Sequencing Revisited

But wait, there's more!

Sequencing Revisited

Let's go back to sequencing...

```
// Method of Parser[+A]
def ~[B](that: Parser[B]): Parser[(A, B)] =
  Parser(input =>
    for {
      (leftValue, leftRest)  <- this.parse(input)
      (rightValue, rightRest) <- that.parse(leftRest)

    } yield ((leftValue, rightValue), rightRest))
```

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// Method of Parser[+A]
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  Parser(input =>
    for {
      (leftValue, leftRest)  <- this.parse(input)
      (rightValue, rightRest) <- that.parse(leftRest)
                               // ^ leftValue is unused.
    } yield ((leftValue, rightValue), rightRest))
```

Sequencing Revisited

Let's go back to sequencing...

```
// Method of Parser[+A]
def ~[B](that: A => Parser[B]): Parser[B] =
  Parser(input =>
    for {
      (leftValue, leftRest)  <- this.parse(input)
      (rightValue, rightRest) <- that(leftValue).parse(leftRest)
                               // ^ leftValue is passed to that.
    } yield (rightValue, rightRest))
```

Sequencing Revisited

Let's rename ~ to something you already know:

```
// Method of Parser[+A]
def flatMap[B](that: A => Parser[B]): Parser[B] =
  Parser(input =>
    for {
      (leftValue, leftRest)  <- this.parse(input)
      (rightValue, rightRest) <- that(leftValue).parse(leftRest)
                               // ^ leftValue is passed to that.
    } yield (rightValue, rightRest))
```

Parser is a Monad!

```
def unit[A](x: A): Parser[A] = success(x)
```


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def unit[A](x: A): Parser[A] = success(x)
```

Monad laws

Associativity $p.\text{flatMap}(f).\text{flatMap}(g) == p.\text{flatMap}(f(_).\text{flatMap}(g))$

Left unit $\text{unit}(x).\text{flatMap}(f) == f(x)$

Right unit $p.\text{flatMap}(\text{unit}(_)) == p$

For-notation for Parsers

Thanks to `Parser` being a `Monad`, you can write sequences of parsers using for-notation.

```
val ifExpr: Parser[Expr] =  
  for {  
    _ <- keyword("if")  
    c <- expr  
    _ <- keyword("then")  
    t <- expr  
    _ <- keyword("else")  
    e <- expr  
  } yield IfExpr(c, t, e)
```

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  } yield IfExpr(c, t, e)
```

```
val tagged: Parser[XML] =  
  for {  
    o <- openTag  
    c <- contents  
    _ <- closeTag(o.name)  
  } yield Tagged(o, c)
```

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- ▶ That `Parser` is a `Monad`!

Summary

- ▶ Parsing and why it is important.
- ▶ What parser combinators are.
- ▶ How the various combinators can be implemented.
- ▶ Ways to handle lexical analysis.
- ▶ That `Parser` is a `Monad`!

Take a look at the parser for the interpreter language!