Analysis for Melin et al: 'Allometric relationships shape foreleg evolution of long-legged oil bees (Melittidae: Rediviva)'

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1 Introduction

This document is an appendix to the paper 'Allometric relationships shape foreleg evolution of long-legged oil bees (Melittidae: Rediviva)' by Annalie Melin, Res Altwegg, John C. Manning and Jonathan F. Colville, detailing the statistical analyses presented there. The data are published on UCT's data portal (DOI: 10.25375/uct.13297640).

This study examines narrow-sense allometry of foreleg length in a group of oil-collecting bee species from South Africa. Narrow-sense allometry is defined as

$$Y = a \times X^b \tag{1}$$

where Y is foreleg length, and X is a linear measure of body size (inter-tegula distance) in our case. The allometric parameters a and b determine the shape of the allometric relationship.

On the log scale, the allometric power law becomes linear, $ln(Y) = ln(a) + b \times ln(X)$, and we can estimate the parameters ln(a) and b using linear regression techniques, where ln(a) is estimated by the intercept and b is estimated by the slope.

Different types of allometry are recognised. For us here, two are important: 1) *static allometry* is the allometric relationship measured within species across individuals at the same developmental state (adults in our case), and 2) *evolutionary allometry* is the allometric relationship measured across species.

2 Data preparation

We'll need the following R packages:

```
library(ape)
library(phylolm)
library(geiger)
library(nlme)
library(RColorBrewer)
```

The data set consists of data on 869 individual bees belonging to 25 species in the genus *Rediviva*. Each row corresponds to an individual bee and the next two columns give total leg length and a linear measure of body size (inter-tegula distance). The column 'spur_length' contains the average spur length of the flowers of the plant species this particular bee species is known to visit For two species, *R.neliana* and *R.pallidula*, we have enough data to be able to distinguish between populations. The columns 'Taxa' and 'population_spur_length' identify the population an individual bee came from, for these two species, and the spur length of the flowers that they visit in these particular locations.

```
beemorph <- read.csv("Rediviva_allom_dataset.csv")
summary(beemorph)</pre>
```

```
##
        Taxa
                          leg_length
                                                             spur_length
                                             body_size
                                : 5.515
                                                                   : 0.000
##
    Length:869
                                                 :1.822
                        Min.
                                                            Min.
##
    Class : character
                        1st Qu.: 7.907
                                           1st Qu.:2.704
                                                            1st Qu.: 4.075
                        Median : 9.383
                                                            Median : 7.295
##
    Mode : character
                                          Median :2.907
##
                        Mean
                                :10.371
                                          Mean
                                                  :2.898
                                                            Mean
                                                                   : 7.368
##
                                                            3rd Qu.: 9.929
                        3rd Qu.:12.038
                                           3rd Qu.:3.128
                                :22.665
                                                  :4.378
##
                        Max.
                                          Max.
                                                            Max.
                                                                   :19.429
##
##
    population_code
                        population_spur_length
##
    Length:869
                        Min.
                                : 5.320
                        1st Qu.: 7.070
##
    Class : character
##
                        Median: 8.810
    Mode :character
##
                        Mean
                                : 8.684
##
                        3rd Qu.:10.550
##
                        Max.
                                :13.880
##
                        NA's
                                :668
```

Create some variables that make life easier later:

```
beemorph$log.leg <- log(beemorph$leg_length)
beemorph$log.body <- log(beemorph$body_size)
beemorph$Taxa <- as.factor(beemorph$Taxa)
beemorph$SPECIES.no <- as.numeric(beemorph$Taxa)</pre>
```

So we have measurements of leg length and body size for a number of individuals for each of 25 species of the genus *Rediviva* and want to estimate the parameters of the static allometric relationship and the evolutionary allometric relationship. The former is the ordinary linear regression line of log(leg length) on log(body size) within species and the latter is the same relationship between species.

3 Estimating the parameters of the static allometric relationships for each species

In a first step, we examine the static allometry for each species, using maximum likelihood methods:

```
m1 <- lm(log.leg ~ Taxa * log.body, data=beemorph)</pre>
anova(m1)
## Analysis of Variance Table
##
## Response: log.leg
##
                 Df Sum Sq Mean Sq
                                     F value
                 24 72.102 3.0043 924.1195 < 2.2e-16 ***
## Taxa
## log.body
                  1 3.671 3.6708 1129.1422 < 2.2e-16 ***
## Taxa:log.body 24 0.474 0.0198
                                      6.0809 < 2.2e-16 ***
## Residuals
                819
                     2.663
                            0.0033
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

The ANOVA table above shows that there is variation among taxa in both the allometric intercept and the allometric slope even though the Mean Squares for the former was much larger than for the latter. The model explained 96.6% of the variation in leg length.

We slightly re-parameterise Model m1 above to estimate the parameters of the static allometry for each species directly and collect the parameter estimates with confidence intervals, from Model m2:

```
m2 <- lm(log.leg ~ -1 + Taxa + Taxa:log.body, data=beemorph)
nspecies <- length(unique(beemorph$Taxa)) # the number of species we have
a <- exp(m2$coefficients[1:nspecies])
b <- m2$coefficients[(nspecies+1):(nspecies*2)]
allometries <- data.frame(cbind(a, b))
allometries$lcl.a <- exp(confint(m2)[1:nspecies,1])
allometries$ucl.a <- exp(confint(m2)[1:nspecies,2])
allometries$lcl.b <- confint(m2)[(nspecies +1):(nspecies*2),1]
allometries$ucl.b <- confint(m2)[(nspecies +1):(nspecies*2),2]
allometries$loga <- m2$coefficients[1:nspecies]
allometries$loga.se <- sqrt(diag(vcov(m2)))[1:nspecies*2)]</pre>
```

The models above fitted separate allometric curves to each species, i.e. $ln(leg) = ln(a) + b \times ln(body)$. The slopes estimate b for each species and exponentiating the intercepts estimates a for each species. Table S1 below gives the parameter estimates with confidence intervals and Figure S1 plots the fitted relationships.

The variance in slopes among species was 0.0755 which is smaller than the mean of the squared standard error of the species-specific slope estimates, 0.1084, suggesting that the variation in slopes is largely due to sampling variance.

Table S1: Summary of morphological data and allometric parameters for 25 species of *Rediviva* bees. N: sample size (number of individuals); LegLength: mean total length of foreleg length [mm]; LL.SD: standard deviation of leg length; BodySize: inter-tegula distance as a measure of body size; BS.SD: standard deviation of body size; a and b: parameters a of the allometric relationships; lcl.a, ucl.a: lower and upper 95% confidence limits of parameter a; lcl.b, ucl.b: lower and upper 95% confidence limits of parameter b.

	N	LegLength	LL.SD	BodySize	BS.SD	a	b	lcl.a	ucl.a	lcl.b	ucl.b
Rediviva albifasciata	29	5.86	0.17	2.51	0.15	4.60	0.26	3.31	6.38	-0.09	0.62
Rediviva alonsoae	11	8.10	0.38	3.33	0.16	4.93	0.41	2.06	11.77	-0.31	1.14
Rediviva aurata	30	9.07	0.51	2.75	0.14	4.08	0.79	2.71	6.15	0.38	1.19
Rediviva autumnalis	19	13.92	0.43	3.17	0.14	10.34	0.26	5.32	20.11	-0.32	0.83
Rediviva brunnea	15	11.78	0.54	3.18	0.11	9.27	0.21	3.52	24.39	-0.63	1.04
Rediviva colorata	39	10.49	0.65	3.00	0.24	9.29	0.11	7.06	12.25	-0.14	0.36
Rediviva emdeorum	45	20.14	1.39	3.36	0.16	8.76	0.69	5.61	13.70	0.32	1.05
Rediviva gigas	8	10.82	0.47	4.20	0.10	3.43	0.80	0.29	40.23	-0.92	2.52
Rediviva intermedia	19	9.10	0.28	3.26	0.16	5.16	0.48	2.75	9.69	-0.05	1.01
Rediviva intermixta	18	8.05	0.27	2.96	0.17	5.58	0.34	3.33	9.36	-0.14	0.81
Rediviva longimanus	39	17.43	0.91	3.19	0.19	8.91	0.58	6.29	12.63	0.28	0.88
Rediviva macgregori	35	12.86	0.64	3.19	0.16	7.05	0.52	4.58	10.84	0.15	0.89
Rediviva micheneri	41	13.79	0.63	2.84	0.15	7.05	0.64	5.02	9.90	0.32	0.97
Rediviva neliana	147	8.79	1.74	2.46	0.37	3.35	1.06	3.16	3.55	1.00	1.13
Rediviva nitida	31	9.29	0.76	3.02	0.19	3.56	0.87	2.51	5.04	0.55	1.18
Rediviva pallidula	64	10.20	0.53	2.94	0.17	6.54	0.41	5.05	8.48	0.17	0.65
Rediviva parva	50	7.43	0.52	2.85	0.18	3.26	0.78	2.50	4.27	0.53	1.04
Rediviva peringueyi	19	9.74	0.39	3.09	0.17	6.90	0.31	4.01	11.86	-0.17	0.79
Rediviva rhodosoma	24	12.44	0.47	3.08	0.17	6.34	0.60	3.90	10.30	0.17	1.03
Rediviva ruficornis	30	9.54	0.36	2.78	0.09	5.95	0.46	3.18	11.15	-0.15	1.07
Rediviva rufipes	49	7.47	0.32	2.93	0.14	5.33	0.31	3.68	7.73	-0.03	0.66
Rediviva rufocincta	66	8.05	0.52	2.75	0.14	3.56	0.80	2.66	4.77	0.52	1.09
Rediviva saetigera	23	7.09	0.27	2.94	0.13	4.37	0.45	2.40	7.94	-0.11	1.00
Rediviva transkeiana	7	10.01	0.06	2.74	0.10	9.20	0.08	2.78	30.43	-1.10	1.27
Rediviva whiteheadi	11	10.88	0.22	3.15	0.09	11.48	-0.05	2.60	50.67	-1.34	1.25

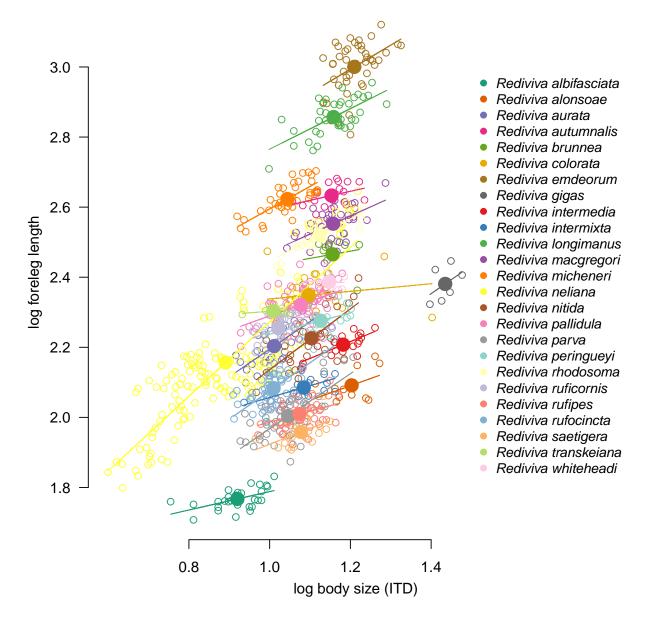


Figure S1: Allometric relationship of leg length against body size in *Rediviva* species. The solid circles indicate the species means.

4 Comparing the static and evolutionary allometric relationships

In a next step, we want to estimate the evolutionary allometric relationship and compare it to the static allometric relationship. We also want to estimate the variance among species in the coefficients of their static allometric relationship. We use random effects to estimate these variances.

We use multi-level models (also known as contextual models (Heisler and Damuth 1987; Egset et al. 2011)), to separately estimate the within-species and between-species slope, following van de Pol and Wright (2009):

$$l_{ij} = \beta_0 + \beta_w (b_{ij} - b_{,j}) + \beta_b b_{,j} + \epsilon_{ij} \tag{2}$$

where l_{ij} is the logarithm of the leg length measurement of the i^{th} individual of species j, b_{ij} is the logarithm of the body size of that individual, $b_{.j}$ is the logarithm of the mean body size across all individuals of species j, β_0 is the intercept, β_w is the within-species effect, i.e. the static allometric slope, β_b is the between-species effect, i.e. the evolutionary allometric slope, and ϵ_{ij} are the residuals. The residuals are assumed to follow a normal distribution with a mean of zero and variances to be estimated.

The model in equation 2 assumes a common intercept and static allometric slope across all species. In the next model, we allow the intercept to vary among species by adding species random effects, μ_{0j} . These random effects are assumed to follow a normal distribution with a mean of zero and variances to be estimated.

$$l_{ij} = \beta_0 + \beta_w (b_{ij} - b_{.j}) + \beta_b b_{.j} + \mu_{0j} + \epsilon_{ij}$$
(3)

Next, we allow the static allometric slopes to vary among species by adding a random slope to Model 3:

$$l_{ij} = (\beta_0 + \mu_{0j}) + (\beta_w + \mu_{wj})(b_{ij} - b_{.j}) + \beta_b b_{.j} + \epsilon_{ij}$$
(4)

The code chunk below calculates $b_{.j}$ and $b_{ij} - b_{.j}$:

```
# calculate mean body size per species:
mean.body <- aggregate(beemorph$log.body, by = list(beemorph$Taxa), FUN=mean)
colnames(mean.body) <- c("Taxa", "mean.body")

# add mean body size back onto data frame:
beemorph <- merge(beemorph, mean.body, by.x = "Taxa", by.y = "Taxa", all.x=T)
# difference in body size within species:
beemorph$diff.body <- beemorph$log.body - beemorph$mean.body</pre>
```

The evolutionary allometry describes how a trait scales with body size across species. From Figure S1 it is clear that *R. gigas* is an outlier in that respect. This species has the largest body size in this data set but has average leg length. As it also is ecologically quite different from the other species, we exclude it from the main analysis but for completeness report results also with this species included.

```
beemorph.r <- beemorph[beemorph$Taxa !="Rediviva gigas",]
beemorph.r$Taxa <- factor(beemorph.r$Taxa)
beemorph.r$SPECIES.no <- as.numeric(beemorph.r$Taxa)</pre>
```

We are now ready to fit the models:

```
m3 <- lm(log.leg ~ diff.body + mean.body, data=beemorph.r) # static allometry same across species summary(m3)
```

```
##
## Call:
## lm(formula = log.leg ~ diff.body + mean.body, data = beemorph.r)
##
```

```
## Residuals:
##
       Min
                     Median
                 10
                                   30
## -0.54867 -0.19005 -0.00064 0.14524 0.53487
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.37723
                          0.08918 4.230 2.59e-05 ***
                          0.10571 8.031 3.18e-15 ***
## diff.body
               0.84896
## mean.body
               1.81666
                          0.08437 21.533 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2385 on 858 degrees of freedom
## Multiple R-squared: 0.381, Adjusted R-squared: 0.3796
## F-statistic: 264.1 on 2 and 858 DF, p-value: < 2.2e-16
m4 <- lme(log.leg ~ diff.body + mean.body, random =~1 Taxa, data=beemorph.r) # random intercept
summary(m4)
## Linear mixed-effects model fit by REML
## Data: beemorph.r
         AIC
                   BIC logLik
##
##
    -2205.44 -2181.667 1107.72
##
## Random effects:
## Formula: ~1 | Taxa
          (Intercept)
                        Residual
## StdDev: 0.2451031 0.06115609
##
## Fixed effects: log.leg ~ diff.body + mean.body
##
                  Value Std.Error DF
                                       t-value p-value
## (Intercept) 0.1780596 0.6772183 836 0.262928 0.7927
## diff.body 0.8489607 0.0271087 836 31.316885 0.0000
## mean.body
              1.9577526 0.6214584 22 3.150255 0.0046
## Correlation:
            (Intr) dff.bd
## diff.body 0.000
## mean.body -0.997 0.000
##
## Standardized Within-Group Residuals:
           Min
                         Q1
                                     Med
## -5.281023741 -0.546657864 -0.007954349 0.532025096 3.694688325
## Number of Observations: 861
## Number of Groups: 24
m5 <- lme(log.leg ~ diff.body + mean.body, random =~diff.body | Taxa, data=beemorph.r)
   # random intercept and slope
summary(m5)
## Linear mixed-effects model fit by REML
## Data: beemorph.r
##
          AIC
                          logLik
                    BIC
    -2302.875 -2269.593 1158.438
##
```

```
## Random effects:
   Formula: ~diff.body | Taxa
   Structure: General positive-definite, Log-Cholesky parametrization
##
               {\tt StdDev}
                          Corr
## (Intercept) 0.24610390 (Intr)
               0.22844234 0.385
## diff.body
## Residual
               0.05691609
##
## Fixed effects: log.leg ~ diff.body + mean.body
##
                    Value Std.Error DF
                                          t-value p-value
  (Intercept) -0.1713919 0.6488697 836 -0.264139 0.7917
## diff.body
                0.5399429 0.0637053 836
                                         8.475640
                                                   0.0000
## mean.body
                2.2792734 0.5952827 22 3.828893 0.0009
##
   Correlation:
##
             (Intr) dff.bd
## diff.body 0.069
  mean.body -0.997 -0.047
##
##
## Standardized Within-Group Residuals:
##
                        Q1
                                                 Q3
## -3.51719191 -0.52455906 -0.01995853 0.56459790 3.59964321
##
## Number of Observations: 861
## Number of Groups: 24
```

The residual standard error decreases markedly, from 0.238 in Model m3 to 0.061 in Model m4, when we included random intercepts. Including random slopes reduced the residual standard error to 0.057 in Model m5. This is a relatively small reduction, which agrees with our earlier result that the variation in slopes among species is likely largely due to sampling variance. AIC favoured Model m5 over Model m4, however (-2302.88 compared to -2205.44).

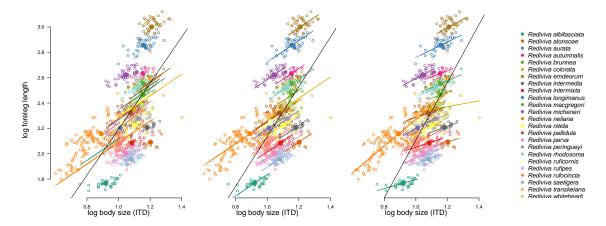


Figure S2: Allometric relationship of leg length against body size in *Rediviva* species. The black line shows the fitted evolutionary allometric relationship.

Does the evolutionary allometric slope (β_b in Equations 2 - 4; mean.body in the R output above) differ from isometry? The estimates are 1.8 (Model m3), 1.958 (Model m4) and 2.279 (Model m5). Do these estimates of β_b differ from 1? We can easily test this for the estimates of β_b from Models m3 to m5 against the null hypothesis $H_0: \beta_b = 1$.

```
# m3
(tstat.m3 <-(coefficients(m3)[3]-1)/sqrt(vcov(m3)[3,3])) # t statistic</pre>
## mean.body
    9.679821
pt(tstat.m3,df=summary(m3)$df[2], lower.tail = F)*2 # p value (2-sided alternative)
##
      mean.body
## 4.204085e-21
# m4
(tstat.m4 <-(summary(m4)$tTable[3,1]-1)/summary(m4)$tTable[3,2]) # t statistic
## [1] 1.541137
pt(tstat.m4,df=summary(m4)$tTable[3,3], lower.tail = F)*2 # p value (2-sided alternative)
## [1] 0.1375452
(tstat.m5 <-(summary(m5)$tTable[3,1]-1)/summary(m5)$tTable[3,2]) # t statistic</pre>
## [1] 2.149018
pt(tstat.m5,df=summary(m5)$tTable[3,3], lower.tail = F)*2 # p value (2-sided alternative)
```

According to Models m3 and m5, the evolutionary allometric slope is significantly different from 1. In Model m4, β_b was estimated with a large standard error, leading to a relatively high P value and weak evidence against H_0 . We note that Model m5 was best supported by the data and therefore conclude that -on balance - the data support the notion that the evolutionary allometric slope is larger than 1.

[1] 0.04289424

What proportion of the between species variation in foreleg length is explained by the variation in mean body size between species? I.e. does the evolutionary allometric relationship examined above explain a large proportion of the variation in mean leg length? If it does, this would suggest that body size constrained the evolution of leg length. To examine this question, we re-fitted the model with random intercept (Equation 3) without entering mean body size as predictor.

$$l_{ij} = \beta_0 + \beta_w(b_{ij} - b_{.j}) + \mu_{Tj} + \epsilon_{ij}$$
 (5)

In this model, the variance of the random effects $\mu_{Tj} - \sigma_{Tj}^2$ – estimates the total among-species variance in foreleg length whereas the variance of the random effects μ_{0j} (in Equation 3) – σ_{0j}^2 – estimates the among-species variance after accounting for mean body size. Comparing σ_{Tj}^2 to σ_{0j}^2 , we can then estimate the proportion of among-species variance in foreleg length that is explained by species-specific body size:

$$\frac{\sigma_{Tj}^2 - \sigma_{0j}^2}{\sigma_{Tj}^2}$$

m4.T <- lme(log.leg ~ diff.body, random =~1|Taxa, data=beemorph.r) # random intercept

The variance of the random intercepts increased from 0.06 in Model m4 to 0.083 in Model m4.T and mean body size therefore explained 28% of the variance in the foreleg length among species.

4.1 Variation in allometric parameters when R. neliana is excluded

R. neliana had the steepest static allometric relationship of all species and we are going to examine this species in more detail later. Here, we quickly want to check how much the estimated variation in static allometric slopes changes if we exclude this species.

Re-running the analyses in the previous section without R. neliana, we obtained qualitatively similar results. The residual standard error decreases markedly, from 0.225 in Model m3 to 0.045 in Model m4, when we included random intercepts. Including random slopes reduced the residual standard error to 0.044 in Model m5 (Figure S3). The variance in slopes among species was 0.0638 which is smaller than the mean of the squared standard error of the species-specific slope estimates, 0.1129, suggesting that the variation in slopes is largely due to sampling variance.

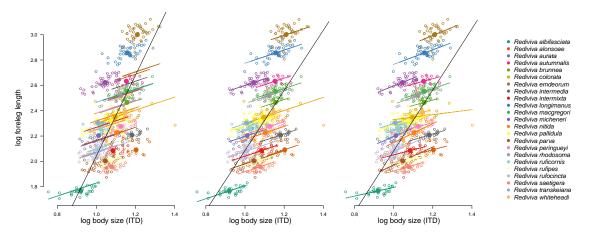


Figure S3: Allometric relationship of leg length against body size in *Rediviva* species, excluding *R. neliana*. The black line shows the fitted evolutionary allometric relationship.

5 Testing whether static and evolutionary allometric slopes differ

We reparameterised the multi-level model in Equations 2 to 4 to allow us to directly test whether the evolutionary allometric slope differs from the (mean) static allometric slope (Pol and Wright 2009):

$$l_{ij} = \beta_0 + \beta_w b_{ij} + (\beta_b - \beta_w) b_{,i} + \epsilon_{ij} \tag{6}$$

$$l_{ij} = \beta_0 + \beta_w b_{ij} + (\beta_b - \beta_w) b_{.j} + \mu_{0j} + \epsilon_{ij}$$
(7)

$$l_{ij} = (\beta_0 + \mu_{0j}) + (\beta_w + \mu_{wj})b_{ij} + (\beta_b - \beta_w)b_{,j} + \epsilon_{ij}$$
(8)

The models are very similar to the ones in Equations 2 to 4 except that we include the individual body size measures instead of the difference to the species mean. This way, the coefficient for species-specific mean body size estimates the difference between the evolutionary and static allometric slopes (see van de Pol and Wright (2009) for details).

```
m6 <- lm(log.leg ~ log.body + mean.body, data=beemorph.r) # static allometry same across species

m7 <- lme(log.leg ~ log.body + mean.body, random =~1|Taxa, data=beemorph.r) # random intercept

m8 <- lme(log.leg ~ log.body + mean.body, random =~diff.body|Taxa, data=beemorph.r)

# random intercept and slope
```

Note that Models m6 to m8 are just reparameterisations of models m3 to m5 and thus identical to those in terms of their fit to the data. The estimated difference between the evolutionary and static allometric slopes $(\text{delta} = \beta_b - \beta_w)$ with confidence intervals are shown in Table S2

Table S2: Difference (delta) between the evolutionary and static allometric slopes estimated by three different models across *Rediviva* species. lcl and ucl are the lower and upper limits of the 95% confidence interval.

Model	delta	lcl	ucl
m6	0.97	0.70	1.23
m7	1.11	-0.18	2.40
m8	1.74	0.49	2.99

The coefficient estimating the difference between the evolutionary and static allometric slopes is positive, indicating that the evolutionary allometric slope is steeper than the static allometric slope. The estimates broadly agree across models but Model m7 yielded a wide confidence interval that included 0.

6 Do these results change when we include R. gigas?

R. gigas was a clear outlier in the general relationship between body size and leg length across species and we therefore excluded R. gigas above. Here, we repeat the analysis with R. gigas included.

We refit Models m3 to m5 to test whether the evolutionary allometric slope differs from isometry. The estimated evolutionary slopes, i.e. β_b , are now 1.617 (se = 0.08, t = 7.666, P = 0 testing $H_0: \beta_b = 1$) for Model m3, 1.216 (se = 0.494, t = 0.436, P = 0.667 testing $H_0: \beta_b = 1$) for Model m4 and 1.322 (se = 0.49, t = 0.656, P = 0.518 testing $H_0: \beta_b = 1$) for Model m5. Only Model m3, which was poorly supported by the data, suggests some evidence against H_0 and therefore conclude that -on balance - when including R. gigas, we have no clear evidence that the evolutionary allometric slope differs from 1.

We re-fitted models m6 to m8 including R. gigas and Table S3 below gives the estimated difference between the evolutionary and static allometric slopes (delta = $\beta_b - \beta_w$) with confidence intervals.

Table S3: Difference (delta) between the evolutionary and static allometric slopes estimated by three different models across *Rediviva* species including *R. gigas*. lcl and ucl are the lower and upper limits of the 95% confidence interval.

Model	delta	lcl	ucl
m6	0.77	0.50	1.03
m7	0.37	-0.66	1.39
m8	0.78	-0.25	1.81

Including R. gigas, the analysis still suggested that the evolutionary allometric slope is steeper than the static allometric slope but the difference was smaller and the confidence interval overlapped zero for Models m7 and m8. In conclusion, including the outlier species R. gigas affects the results presented earlier, albeit not the general pattern. Figure S4 below shows, however, that the fitted evolutionary allometric line is a poor description of the general relationship between log body size and log leg length across species.

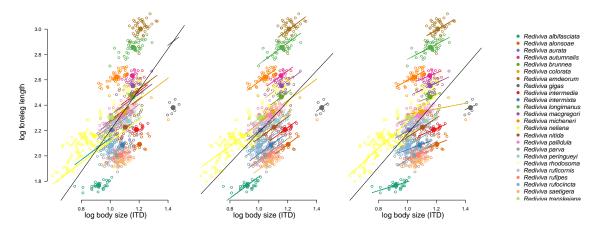


Figure S4: Allometric relationship of leg length against body size in Rediviva species, including R. gigas. The black line shows the fitted evolutionary allometric relationship.

7 Does accounting for phylogeny affect our results?

Our analyses above assumed independent residuals but clearly, the species are phylogenetically related and this relatedness could cause non-independence in the data. Our maximum likelihood estimates of the parameters of the static allometric relationships in Table S1 should not be affected because we estimated separate parameters for each species. However, our estimate of the evolutionary allometric parameters could be affected. In this section, we therefore re-run some key models while accounting for phylogenetic non-independence. We do not have complete phylogenetic information for all species examined so far, so this re-analysis is based on a reduced set of species, which is the main reason why we did not include phylogeny throughout.

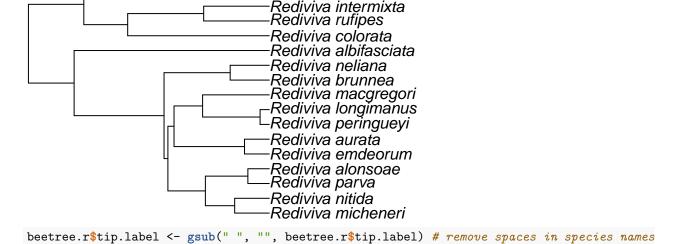
A phylogeny published by Kahnt et al (2017) included most of the species in our sample. The code chunk below reads the tree and renames the tips so that the species names match those in the data frame. We drop R. qiqas from the phylogenetic tree:

```
beetree <- read.tree("Rediviva simplified treeUSE.nex")
beetree$tip.label <- gsub("Rediviva_", "Rediviva ", beetree$tip.label)

beetree.r <- drop.tip(beetree, c("Rediviva gigas")) ## drop R. gigas

plot(beetree.r)</pre>
```

Rediviva intermedia Rediviva saetigera



There are seven species in our morphological data set that don't appear in the phylogeny and we remove all observations of these species:

Our data set contains multiple individuals per species and we therefore need to add tips to the phylogenetic tree:

```
beemorph.phy$species <- gsub(" ", "", beemorph.phy$Taxa)
rownames(beemorph.phy) <- gsub(" ", "", pasteO(beemorph.phy$species, 1:NROW(beemorph.phy)))
species <- unique(beemorph.phy$species)</pre>
```

```
## because there are multiple rows per species:
nice.tree.multi <- beetree.r</pre>
for (g in 1:NROW(species)){
  if(!is.null(nice.tree.multi$edge.length)){
    flat.tree <- read.tree(text =
      paste0("(", paste(rownames(beemorph.phy))[grep(species[g],rownames(beemorph.phy))],
                         collapse = ":0.02, "), ":0.02);"))
  } else {
    flat.tree <- read.tree(text =</pre>
      c("(", paste(rownames(beemorph.phy)[grep(species[g], rownames(beemorph.phy))],
                   collapse = ", "), ");"))
  }
  nice.tree.multi <- bind.tree(nice.tree.multi, flat.tree,</pre>
                      where = which(nice.tree.multi$tip.label == species[g]),
                     position = 0, interactive = FALSE)
 }
```

Next, we use phylogenetic generalized least squares models. We first add phylogenetic model structures to the errors using model m3, which is the simplest multi-level model without random effects:

```
m3.bm <- phylolm(log.leg ~ diff.body + mean.body, phy = nice.tree.multi, model = "BM",
                 data = beemorph.phy)
summary(m3.bm)
##
## Call:
## phylolm(formula = log.leg ~ diff.body + mean.body, data = beemorph.phy,
      phy = nice.tree.multi, model = "BM")
##
      AIC logLik
##
## -1506.4
           757.2
##
## Raw residuals:
       Min
                 1Q
                     Median
                                           Max
## -0.42575 -0.07941 0.17859 0.45240 0.65894
##
## Mean tip height: 28.94673
## Parameter estimate(s) using ML:
## sigma2: 0.2111338
##
## Coefficients:
                           StdErr t.value p.value
               Estimate
## (Intercept) -0.122356 3.513058 -0.0348 0.9722
## diff.body
               0.885533 0.030477 29.0559 <2e-16 ***
## mean.body
               2.128502 3.084062 0.6902 0.4903
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## R-squared: 0.5701
                       Adjusted R-squared: 0.5687
m3.OUr <- phylolm(log.leg ~ diff.body + mean.body, phy = nice.tree.multi, model = "OUrandomRoot",
                 data = beemorph.phy)
summary(m3.0Ur)
```

```
##
## Call:
## phylolm(formula = log.leg ~ diff.body + mean.body, data = beemorph.phy,
      phy = nice.tree.multi, model = "OUrandomRoot")
      AIC logLik
##
## -1550.6
           780.3
##
## Raw residuals:
##
       Min
                 1Q
                     Median
                                   30
## -0.48847 -0.17793 0.09323 0.34111 0.59753
##
## Mean tip height: 28.94673
## Parameter estimate(s) using ML:
## alpha: 1.48124
## sigma2: 0.2230513
##
## Coefficients:
                         StdErr t.value
              Estimate
                                         p.value
## (Intercept) 0.174178 0.811901 0.2145 0.830202
## diff.body 0.885533 0.030867 28.6888 < 2.2e-16 ***
## mean.body
             1.934129 0.742226 2.6058 0.009379 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.5657
                       Adjusted R-squared: 0.5644
## Note: p-values and R-squared are conditional on alpha=1.48124.
m3.OUf <- phylolm(log.leg ~ diff.body + mean.body, phy = nice.tree.multi, model = "OUfixedRoot",
                 data = beemorph.phy)
summary(m3.OUf)
##
## Call:
## phylolm(formula = log.leg ~ diff.body + mean.body, data = beemorph.phy,
      phy = nice.tree.multi, model = "OUfixedRoot")
##
##
##
      AIC logLik
## -1550.6
           780.3
##
## Raw residuals:
       Min
                 1Q
                     Median
                                   3Q
                                           Max
## -0.48847 -0.17793 0.09323 0.34111 0.59753
##
## Mean tip height: 28.94673
## Parameter estimate(s) using ML:
## alpha: 1.48124
## sigma2: 0.2230513
##
## Coefficients:
##
              Estimate
                         StdErr t.value
                                          p.value
## (Intercept) 0.174178 0.811902 0.2145 0.830202
## diff.body 0.885533 0.030867 28.6888 < 2.2e-16 ***
## mean.body 1.934129 0.742226 2.6058 0.009379 **
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
                        Adjusted R-squared: 0.5644
## R-squared: 0.5657
##
## Note: p-values and R-squared are conditional on alpha=1.48124.
m3.lambda <- phylolm(log.leg ~ diff.body + mean.body, phy = nice.tree.multi, model = "lambda",
                     data = beemorph.phy)
summary(m3.lambda)
##
  phylolm(formula = log.leg ~ diff.body + mean.body, data = beemorph.phy,
       phy = nice.tree.multi, model = "lambda")
##
##
##
       AIC
           logLik
##
  -1535.6
            772.8
##
## Raw residuals:
##
       Min
                  1Q
                                    3Q
                                            Max
                      Median
##
  -0.42575 -0.07952 0.17842 0.45212
                                       0.65895
##
## Mean tip height: 28.94673
## Parameter estimate(s) using ML:
## lambda : 0.9894676
## sigma2: 0.0133414
##
## Coefficients:
##
                Estimate
                            StdErr t.value
                                             p.value
## (Intercept) -0.121285
                         0.879727 -0.1379 0.890389
## diff.body
                0.885533
                         0.030867 28.6885 < 2.2e-16 ***
## mean.body
                2.127609
                         0.772462 2.7543 0.006049 **
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## R-squared: 0.566 Adjusted R-squared: 0.5646
##
## Note: p-values and R-squared are conditional on lambda=0.9894676.
```

AIC suggests that the best model structure is the one assuming an Ornstein-Uhlenbeck process (Models m3.0Ur and m3.0Uf). However, all models return a similar estimate for the evolutionary allometric slope (β_b in Equation 2 and mean.body in the output above ranged from 1.934 to 2.129), which is also comparable to the slope that was estimated by the model without phylogenetic structure (m3: 1.817) in an earlier section.

We saw earlier, however, that Model m3 was not a good description of our data. We next add a phylogenetic correlation structure to Models m4 and m5. These models include random effects and are more complex statistical models. We only managed to get the models assuming a Brownian Motion process to converge.

```
-5817.773 -5795.489 2913.886
##
##
## Random effects:
## Formula: ~1 | Taxa
          (Intercept)
                        Residual
## StdDev:
           0.2837536 0.07824462
## Correlation Structure: corBrownian
## Formula: ~1 | Taxa
## Parameter estimate(s):
## numeric(0)
## Fixed effects: log.leg ~ diff.body + mean.body
                  Value Std.Error DF
                                       t-value p-value
## (Intercept) 0.1728923 0.8626126 622 0.200429 0.8412
## diff.body
              0.6746445 0.0287997 622 23.425432 0.0000
## mean.body
              1.9366506 0.7884406 15 2.456305 0.0267
## Correlation:
##
            (Intr) dff.bd
## diff.body 0.000
## mean.body -0.997 0.000
## Standardized Within-Group Residuals:
##
                       Q1
          Min
                                  Med
                                               QЗ
                                                          Max
## -3.44538322 -0.43478179 -0.04354433 0.44087324 3.42865107
##
## Number of Observations: 640
## Number of Groups: 17
m5.bm <- lme(log.leg ~ diff.body + mean.body, random =~diff.body Taxa, data=beemorph.phy,
            correlation = corBrownian(1, nice.tree.multi))
summary(m5.bm)
## Linear mixed-effects model fit by REML
## Data: beemorph.phy
##
          AIC
                    BIC
                          logLik
##
    -5960.922 -5929.725 2987.461
##
## Random effects:
## Formula: ~diff.body | Taxa
## Structure: General positive-definite, Log-Cholesky parametrization
              StdDev
                         Corr
## (Intercept) 0.28478004 (Intr)
## diff.body 0.25217861 0.531
## Residual
              0.06872903
##
## Correlation Structure: corBrownian
## Formula: ~1 | Taxa
## Parameter estimate(s):
## numeric(0)
## Fixed effects: log.leg ~ diff.body + mean.body
                   Value Std.Error DF
                                         t-value p-value
## (Intercept) -0.3468319 0.7848926 622 -0.441885 0.6587
## diff.body
               0.5376452 0.0804316 622 6.684499
## mean.body
               2.4142344 0.7169023 15 3.367592 0.0042
## Correlation:
```

```
## (Intr) dff.bd
## diff.body 0.121
## mean.body -0.996 -0.086
##
## Standardized Within-Group Residuals:
## Min Q1 Med Q3 Max
## -2.90794724 -0.48515084 -0.04479196 0.47746928 2.97036221
##
## Number of Observations: 640
## Number of Groups: 17
```

Again, the estimated evolutionary allometric slopes were similar to the ones obtained earlier from the models assuming no phylogenetic dependence structure: 1.937 in Model m4.bm compared to 1.958 in Model m4 and 2.414 in Model m5.bm compared to 2.279 in Model m5. We conclude that our earlier results were not sensitive to violation of the assumption that the errors were phylogenetically independent.

8 Estimating the parameters of the static allometric relationships for each population in $R.\ neliana$

We saw earlier that R. neliana had a steeper allometric slope than the other species. Is it possible that our R. neliana sample is made up of individuals that belong to several isolated populations on independent evolutionary tracks? In this section, we examine variation within and between populations of R. neliana. For this section, we refer to the within-population allometric relationship as the static allometric relationship and to the between-population allometric relationship as the evolutionary allometric relationship.

We first select the R. neliana individuals from the full data set and tabulate them by population:

```
beemorph.n <- beemorph[beemorph$Taxa =="Rediviva neliana", c(2,3,5:8)]
beemorph.n$population_code <- factor(beemorph.n$population_code)
beemorph.n$pop.no <- as.numeric(beemorph.n$population_code)
table(beemorph.n$population_code)</pre>
```

```
##
## R. neliana_1 R. neliana_11 R. neliana_18 R. neliana_2 R. neliana_21
## 20 15 15 15 15 15
## R. neliana_22 R. neliana_3 R. neliana_4 R. neliana_6 R. neliana_8
## 7 15 15 15 15
```

Following identical procedures as above, we first estimate the static allometric relationship for each population separately:

```
m1.n <- lm(log.leg ~ population_code * log.body, data=beemorph.n)
anova(m1.n)</pre>
```

```
## Analysis of Variance Table
##
## Response: log.leg
                            Df Sum Sq Mean Sq F value
##
                                                          Pr(>F)
## population_code
                             9 3.9149 0.43499 471.6891 < 2.2e-16 ***
## log.body
                             1 0.8239 0.82385 893.3554 < 2.2e-16 ***
## population_code:log.body
                             9 0.0239 0.00266
                                                2.8845 0.003913 **
                            127 0.1171 0.00092
## Residuals
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

The ANOVA table above shows that there is variation among populations in both the allometric intercept

and the allometric slope even though the Mean Squares for the former was much larger than for the latter. The model explained 97.6% of the variation in leg length. Table S4 shows the maximum likelihood estimates for the parameters a and b (Equation 1) of the population-specific allometric relationships.

The variance in slopes among populations was 0.0478 which is not much larger than the mean of the squared standard error of the population-specific slope estimates 0.0234 suggesting that the variation in slopes is largely due to sampling variance.

Table S4: Summary of morphological data and allometric parameters for 10 populations of *R. neliana* bees. N: sample size (number of individuals per population); LegLength: mean total length of foreleg length [mm]; LL.SD: standard deviation of leg length; BodySize: inter-tegula distance as a measure of body size; BS.SD: standard deviation of body size; a and b are the parameters of the allometric relationships; lcl.a, ucl.a: lower and upper 95% confidence limits of parameter a; lcl.b, ucl.b: lower and upper 95% confidence limits of parameter b.

	N	LegLength	LL.SD	BodySize	BS.SD	a	b	lcl.a	ucl.a	lcl.b	ucl.b
R. neliana_1	20	8.54	0.42	2.69	0.15	4.74	0.60	3.72	6.04	0.35	0.84
R. neliana_11	15	8.47	0.66	2.21	0.19	4.51	0.79	3.86	5.27	0.60	0.99
R. neliana_18	15	9.17	0.97	2.52	0.28	3.98	0.90	3.46	4.58	0.75	1.05
R. neliana_2	15	7.48	1.09	2.35	0.34	3.25	0.98	2.96	3.56	0.87	1.09
R. neliana_21	15	13.00	0.50	3.20	0.14	6.94	0.54	4.61	10.46	0.19	0.89
R. neliana_22	7	10.15	0.29	2.48	0.11	6.59	0.48	3.96	10.97	-0.08	1.04
R. neliana_3	15	7.56	0.84	2.34	0.34	4.02	0.74	3.67	4.40	0.64	0.85
R. neliana_4	15	7.27	0.30	2.12	0.10	4.26	0.71	3.30	5.50	0.37	1.05
R. neliana_6	15	8.10	0.22	2.35	0.08	6.37	0.28	4.36	9.30	-0.16	0.73
R. neliana_8	15	9.01	0.99	2.31	0.27	4.23	0.90	3.75	4.78	0.76	1.05

We fit the models described in equations 2 to 4 to the R. neliana data:

```
m3.n <- lm(log.leg ~ diff.body + mean.body, data=beemorph.n) # static allometry same across species summary(m3.n)
```

```
##
## Call:
## lm(formula = log.leg ~ diff.body + mean.body, data = beemorph.n)
##
## Residuals:
##
         Min
                    1Q
                          Median
                                         3Q
                                                  Max
##
   -0.199955 -0.076061
                       0.003661 0.082739
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
                1.07708
                           0.06135
                                    17.555
                                              <2e-16 ***
## (Intercept)
## diff.body
                0.82854
                           0.08584
                                      9.652
                                              <2e-16 ***
                                    17.738
## mean.body
                1.21159
                           0.06831
                                              <2e-16 ***
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
## Residual standard error: 0.09404 on 144 degrees of freedom
## Multiple R-squared: 0.739, Adjusted R-squared: 0.7354
## F-statistic: 203.9 on 2 and 144 DF, p-value: < 2.2e-16
m4.n <- lme(log.leg ~ diff.body + mean.body, random =~1|population_code, data=beemorph.n)
   # random intercept
summary(m4.n)
```

```
## Linear mixed-effects model fit by REML
## Data: beemorph.n
##
          AIC
                    BIC
                          logLik
    -525.8002 -510.9511 267.9001
##
## Random effects:
## Formula: ~1 | population_code
          (Intercept)
                       Residual
## StdDev: 0.09881118 0.03220614
##
## Fixed effects: log.leg ~ diff.body + mean.body
                  Value Std.Error DF
                                         t-value p-value
## (Intercept) 1.0483477 0.25280300 136 4.146896 0.0001
## diff.body 0.8285352 0.02939846 136 28.182945 0.0000
## mean.body
             1.2570502 0.28226277 8 4.453475 0.0021
## Correlation:
##
            (Intr) dff.bd
## diff.body 0.000
## mean.body -0.992 0.000
## Standardized Within-Group Residuals:
                       Q1
## -2.22130307 -0.67146969 -0.06919938 0.67961895 2.49822234
## Number of Observations: 147
## Number of Groups: 10
m5.n <- lme(log.leg ~ diff.body + mean.body, random =~diff.body population_code, data=beemorph.n)
   # random intercept and slope
summary(m5.n)
## Linear mixed-effects model fit by REML
## Data: beemorph.n
          AIC
                   BIC
                         logLik
    -528.1827 -507.394 271.0913
##
##
## Random effects:
## Formula: ~diff.body | population_code
## Structure: General positive-definite, Log-Cholesky parametrization
              StdDev
                         Corr
## (Intercept) 0.09885416 (Intr)
## diff.body 0.13291295 0.011
## Residual
              0.03049193
## Fixed effects: log.leg ~ diff.body + mean.body
                  Value Std.Error DF t-value p-value
## (Intercept) 1.0462855 0.25281557 136 4.138533 0.0001
## diff.body 0.7690741 0.05632445 136 13.654356 0.0000
## mean.body
              1.2593852 0.28227695
                                   8 4.461524 0.0021
## Correlation:
            (Intr) dff.bd
## diff.body 0.002
## mean.body -0.992 -0.001
##
## Standardized Within-Group Residuals:
```

```
## Min Q1 Med Q3 Max
## -2.0080129 -0.6828817 0.1063575 0.6916677 2.2161583
##
## Number of Observations: 147
## Number of Groups: 10
```

The residual standard error decreased markedly, from 0.094 in Model m3.n to 0.032 in Model m4.n, when we included random intercepts. Including random slopes reduced the residual standard error to 0.03 in Model m5.n. This is a relatively small reduction, which agrees with our earlier result that the variation in slopes among species is likely largely due to sampling variance. AIC favoured Model m5 over Model m4, however (-528.18 compared to -525.8).

Using the fitted Models m3.n to m5.n, we test whether the evolutionary allometric slope differs from isometry. The estimated evolutionary slopes, i.e. β_b , are 1.212 (se = 0.068, t = 3.098, P = 0.002 testing $H_0: \beta_b = 1$) for Model m3.n, 1.257 (se = 0.282, t = 0.911, P = 0.389 testing $H_0: \beta_b = 1$) for Model m4.n and 1.259 (se = 0.282, t = 0.919, P = 0.385 testing $H_0: \beta_b = 1$) for Model m5.n. Only Model m5.n, which was poorly supported by the data, suggests some evidence against H_0 and we therefore conclude that we have no strong evidence that the evolutionary allometric slope among populations of R. neliana differs from 1.

We next examined \mathbb{R}^2 for the evolutionary allometric relationship as we did in the between-species comparison earlier.

```
m4.T.n <- lme(log.leg ~ diff.body, random =~1|population_code, data=beemorph.n) # random intercept
```

The variance of the random intercepts increased from 0.01 in Model m4.n to 0.03 in Model m4.T.n and mean body size therefore explained 67.8% of the variance in the foreleg length among species.

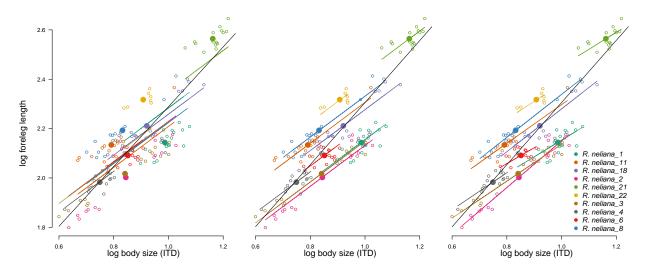


Figure S5: Allometric relationship of leg length against body size in *R. neliana* populations The black line shows the fitted evolutionary allometric relationship.

As we saw when comparing evolutionary and static allometry across species, the allometric slope is steeper among populations than within. Is this difference statistically supported?

The coefficient estimating the difference between the evolutionary and static allometric slopes was positive (Table S5), indicating that the evolutionary allometric slope is steeper than the static allometric slope but the difference is much smaller than in the comparison across species and Models m7 and m8 both yielded a confidence interval that included 0.

In summary, when examining within- and among-population allometric relationships in R. neliana, we found qualitatively similar patterns as we did when examining within- and among-species allometric relationship

across the *Rediviva* genus but these patterns were weaker and not always statistically supported.

Table S5: Difference (delta) between the evolutionary and static allometric slopes estimated by three different models across R. neliana populations. lcl and ucl are the lower and upper limits of the 95% confidence interval.

$\overline{\text{Model}}$	delta	lcl	ucl
$\overline{\mathrm{m}6}$	0.38	0.17	0.60
m7	0.43	-0.23	1.08
m8	0.49	-0.17	1.15

9 Is variation in allometric relationships explained by spur length of the host flowers?

For all species except R. neliana, the allometric exponent (slope) was estimated to be smaller than one. And when we considered within-population allometry for R. neliana, this was also true for all populations of that species. An allometric exponent < 1 implies that small individuals have relatively long legs for their size and large individuals have relatively short legs for their size. What are the selective forces acting on this relationship and what could explain the variation among species – and in the case of R. neliana, variation among population – in these allometric parameters?

These bees collect oil from flowers using their forelegs, so spur length of the flowers from which these bees collect the oil is a candidate environmental driver likely to act as selective force. We generated a list of oil host plants for each *Rediviva* species, combined this with spur length data and calculated a mean spur length across all host plants per bee species.

Figure S6 shows leg length as a function of spur length (using a weighted mean across all plant species each bee species is known to visit). *R. gigas* is included in this plot. Leg length tracks spur length with most species having legs that are longer than the spur length of the flowers they visit.

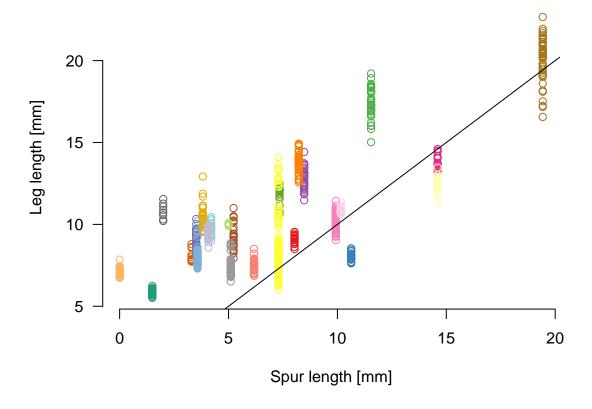


Figure S6: Leg length of *Rediviva* individuals of different species against mean spur length of their host plant flowers. The solid black line is the 1:1 relationship. Colours indicate different species using the same colour scheme as in Figure S1.)

We slightly re-parameterise the model described in Equation 3 by subtracting the overall mean log body size $(\beta_{..})$ from the species-specific mean log body size $(\beta_{.j})$ so that the intercept estimates the log leg length for a bee of average log body size.

$$l_{ij} = (\beta_0 + \mu_{0j}) + \beta_w(b_{ij} - b_{.j}) + \beta_b(b_{.j} - b_{..}) + \epsilon_{ij}$$
(9)

We then add log spur length, s, as an explanatory variable to this model:

$$l_{ij} = (\beta_0 + \mu_{rj}) + \beta_w (b_{ij} - b_{.j}) + \beta_b (b_{.j} - b_{..}) + \beta_s s + \epsilon_{ij}$$
(10)

Spur length varies among species and the random effects μ_{rj} in Equation 10 therefore estimate the remaining variation among species in the allometric intercept after accounting for variation in spur length.

We estimate the proportion of variance of the allometric intercept that is explained by spur length as:

$$\frac{\sigma_{0j}^2 - \sigma_{rj}^2}{\sigma_{rj}^2}$$

where σ_{0j}^2 is the estimated variance of the random effects μ_{0j} and σ_{rj}^2 is the estimated variance of the random effects μ_{rj} . We excluded R. gigas from this analysis because this species was an outlier with a large influence on the estimated evolutionary allometric relationship.

```
m9 <- lme(log.leg ~ diff.body + I(mean.body-mean(log.body)), random =~1|Taxa, data=beemorph.r) # random
summary(m9)
## Linear mixed-effects model fit by REML
   Data: beemorph.r
##
          AIC
                    BIC logLik
##
     -2205.44 -2181.667 1107.72
##
## Random effects:
   Formula: ~1 | Taxa
           (Intercept)
                         Residual
##
             0.2451031 0.06115609
## StdDev:
## Fixed effects: log.leg ~ diff.body + I(mean.body - mean(log.body))
                                     Value Std.Error DF t-value p-value
## (Intercept)
                                 2.2388955 0.0543921 836 41.16216 0.0000
## diff.body
                                 0.8489607 0.0271087 836 31.31688 0.0000
## I(mean.body - mean(log.body)) 1.9577526 0.6214584 22 3.15026 0.0046
   Correlation:
##
                                 (Intr) dff.bd
## diff.body
## I(mean.body - mean(log.body)) -0.389
## Standardized Within-Group Residuals:
##
           Min
                          Q1
                                      Med
                                                    Q3
                                                                 Max
## -5.281023741 -0.546657864 -0.007954349 0.532025096 3.694688325
##
## Number of Observations: 861
## Number of Groups: 24
m10 <- lme(log.leg ~ diff.body + I(mean.body-mean(log.body)) + log(spur_length+0.5),
           random =~1 | Taxa, data=beemorph.r) # adding spur length
summary (m10)
## Linear mixed-effects model fit by REML
   Data: beemorph.r
##
           AIC
                     BIC
                           logLik
     -2210.385 -2181.864 1111.192
##
##
## Random effects:
   Formula: ~1 | Taxa
##
           (Intercept)
                         Residual
## StdDev: 0.1960997 0.06115595
## Fixed effects: log.leg ~ diff.body + I(mean.body - mean(log.body)) + log(spur_length +
                                                                                                0.5)
                                     Value Std.Error DF
                                                           t-value p-value
## (Intercept)
                                 1.8703386 0.1099693 836 17.007819
                                                                     0.0000
## diff.body
                                 0.8489607 0.0271087 836 31.316955
                                                                     0.0000
## I(mean.body - mean(log.body)) 1.1922890 0.5400352 21
                                                          2.207799
                                                                     0.0385
## log(spur_length + 0.5)
                                 0.2134248 0.0584735 21 3.649937
## Correlation:
```

```
##
                                  (Intr) dff.bd I(.-m(
                                   0.000
## diff.body
  I(mean.body - mean(log.body))
                                   0.215
                                          0.000
   log(spur_length + 0.5)
                                          0.000 -0.389
                                  -0.918
##
##
  Standardized Within-Group Residuals:
##
           Min
                         01
                                    Med
                                                  Q3
                                                             Max
   -5.27703519 -0.54397154 -0.01176452 0.53283239
##
                                                      3.69351607
##
## Number of Observations: 861
## Number of Groups: 24
```

There was strong evidence that leg length was positively related to spur length Figure S7 and variance of the random intercepts decreased from 0.06 in Model m9 to 0.038 in Model m10. Spur length therefore explained 36% of the variance in the intercept among species.

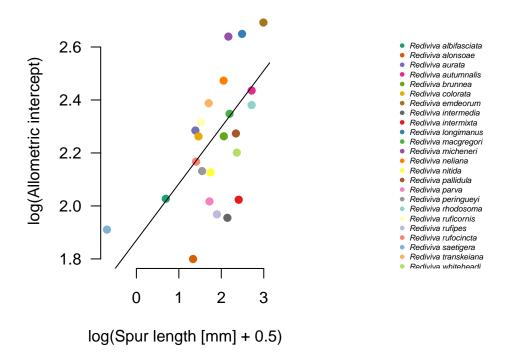


Figure S7: Relationship of allometric intercept to spur length of the host plants for *Rediviva* bee species. The allometric intercept shown are the Best Linear Unbiased Predictors for the species-specific intercepts estimated by model m9. The regression line shows the fitted relationship from model m10.

So far, we analysed narrow-sense allometry as a power law (Equation 1) and we used log-transformed values for body size, leg length and spur length. An argument could be made that selection on leg length through variation in spur length follows arithmetic relationships instead: 1 mm change in spur length should trigger a 1 mm response in leg length. We therefore re-fitted Model m10 on the arithmetic scale:

$$l_{ij}^{a} = (\beta_0 + \mu_{rj}) + \beta_w (b_{ij}^{a} - b_{.j}^{a}) + \beta_b (b_{.j}^{a} - b_{..}^{a}) + \beta_s s^{a} + \epsilon_{ij}$$
(11)

The superscripts ^a indicate that these variables were on the arithmetic scale, rather than the logarithmic scale used so far.

```
# calculate mean body size per species on arithmetic scale:
mean.body.a <- aggregate(beemorph.r$body_size, by = list(beemorph.r$Taxa), FUN=mean)</pre>
colnames(mean.body.a) <- c("Taxa", "mean.body.a")</pre>
# add mean body size back onto data frame:
beemorph.r <- merge(beemorph.r, mean.body.a, by.x = "Taxa", by.y = "Taxa", all.x=T)
# difference in body size within species:
beemorph.r$diff.body.a <- beemorph.r$body_size - beemorph.r$mean.body.a
m11 <- lme(leg_length ~ diff.body.a + I(mean.body.a-mean(body_size)) + spur_length,
           random =~1 | Taxa, data=beemorph.r) # adding spur length
summary(m11)
## Linear mixed-effects model fit by REML
   Data: beemorph.r
##
          AIC
                   BIC
                          logLik
     1880.656 1909.176 -934.3279
##
##
## Random effects:
##
   Formula: ~1 | Taxa
           (Intercept) Residual
##
              2.025004 0.6631789
## StdDev:
##
## Fixed effects: leg_length ~ diff.body.a + I(mean.body.a - mean(body_size)) +
                                                                                      spur_length
                                       Value Std.Error DF
                                                              t-value p-value
                                    6.508818 0.8215969 836 7.922155 0.0000
## (Intercept)
## diff.body.a
                                    3.015978 0.1081592 836 27.884618
                                                                       0.0000
## I(mean.body.a - mean(body_size)) 2.724555 2.0723341 21 1.314728 0.2028
## spur_length
                                    0.508026 0.1074654 21 4.727347
                                                                       0.0001
  Correlation:
##
                                     (Intr) dff.b. I(..-m
## diff.body.a
                                     0.000
## I(mean.body.a - mean(body_size)) 0.252 0.000
## spur_length
                                    -0.840 0.000 -0.507
##
## Standardized Within-Group Residuals:
##
            Min
                          Q1
                                      Med
                                                     0.3
                                                                 Max
## -5.824013443 -0.557119795 -0.003935144 0.503045983 3.814275300
##
## Number of Observations: 861
## Number of Groups: 24
# testing whether the effect of spur length is different from 1
tstat.m11 <-(summary(m11)$tTable[4,1]-1)/summary(m11)$tTable[4,2] # t statistic
p.spur <- pt(tstat.m11,df=summary(m11)$tTable[4,3], lower.tail = T)*2 # p value (2-sided alternative)
```

In this analysis, the coefficient for spur length is easier to interpret: it estimates the change in leg length in millimeters, for every millimeter change in spur length. If leg length tracked spur length perfectly, we would expect this coefficient to be close to 1. However, the estimated effect was 0.51, which is considerably less than 1 (t = -4.58, $P = 1.6 \times 10^{-4}$, Figure S8).

Comparing the variance of the random intercepts in Model m11 to an equivalent model without spur length,

we find that spur length explained 49.4% of the variance in the intercept among species when analysing allometry on the arithmetic scale.

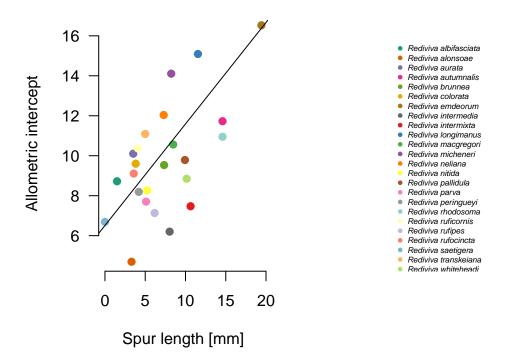


Figure S8: Relationship of allometric intercept (i.e. estimated species-specific leg length from Model m11) to spur length of the host plants for Rediviva bee species, fitted on the aritmetic scale.

10 Is allometric variation among R. neliana populations explained by spur length of the host flowers?

We next apply the analyses of the section above to *R. neliana* and examine whether variation in the allometric parameters among populations is related to spur length of the population-specific host plants.

Figure S9 shows leg length as a function of spur length. Leg length tracks spur length reasonably well across populations.

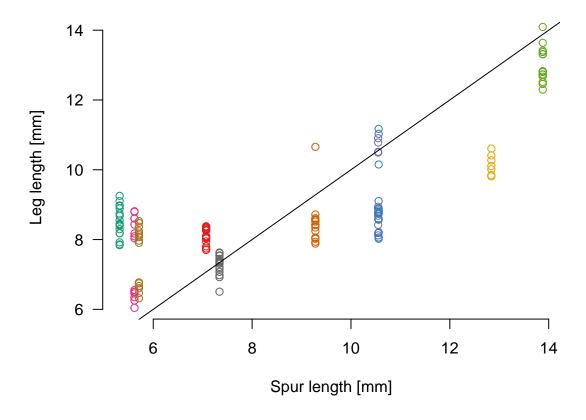


Figure S9: Leg length of *R. neliana* individuals from different populations against spur length of their host plant flowers. The solid black line is the 1:1 relationship. Colours indicate different populations using the same colour scheme as in Figure S5.)

```
## Linear mixed-effects model fit by REML
##
   Data: beemorph.n
##
           AIC
                     BIC
                           logLik
##
     -525.8002 -510.9511 267.9001
##
##
   Random effects:
##
   Formula: ~1 | population_code
##
           (Intercept)
                         Residual
## StdDev: 0.09881118 0.03220614
##
## Fixed effects: log.leg ~ diff.body + I(mean.body - mean(log.body))
##
                                     Value Std.Error DF t-value p-value
## (Intercept)
                                 2.1683868 0.03137374 136 69.11472 0.0000
## diff.body
                                 0.8285352 0.02939846 136 28.18295
## I(mean.body - mean(log.body)) 1.2570502 0.28226277
                                                         8 4.45348
                                                                    0.0021
## Correlation:
```

```
##
                                 (Intr) dff.bd
## diff.body
                                 0.000
## I(mean.body - mean(log.body)) 0.021 0.000
## Standardized Within-Group Residuals:
##
                        Q1
                                   Med
                                                 Q3
                                                            Max
  -2.22130307 -0.67146969 -0.06919938 0.67961895
##
## Number of Observations: 147
## Number of Groups: 10
m10.n <- lme(log.leg ~ diff.body + I(mean.body-mean(log.body)) + log(population_spur_length+0.5),
           random =~1|population_code, data=beemorph.n) # adding spur length
summary(m10.n)
## Linear mixed-effects model fit by REML
   Data: beemorph.n
##
           AIC
                     BIC
                           logLik
     -541.5314 -523.7543 276.7657
##
##
## Random effects:
   Formula: ~1 | population_code
##
           (Intercept)
                         Residual
## StdDev: 0.02348257 0.03219929
## Fixed effects: log.leg ~ diff.body + I(mean.body - mean(log.body)) + log(population_spur_length +
##
                                          Value Std.Error DF t-value p-value
## (Intercept)
                                     1.5161072 0.06041296 136 25.09573
## diff.body
                                     0.8285352 0.02939221 136 28.18894
                                                                              0
## I(mean.body - mean(log.body))
                                     0.9190710 0.07718875
                                                             7 11.90680
                                                                              0
## log(population_spur_length + 0.5) 0.2985221 0.02748450
                                                             7 10.86147
                                                                              0
  Correlation:
##
                                      (Intr) dff.bd I(.-m(
## diff.body
                                      0.000
## I(mean.body - mean(log.body))
                                      0.396 0.000
## log(population_spur_length + 0.5) -0.991 0.000 -0.397
##
## Standardized Within-Group Residuals:
##
                                   Med
                        Q1
                                                 QЗ
                                                            Max
## -2.16171198 -0.63306065 -0.04199296 0.66023437
                                                     2.54849768
##
## Number of Observations: 147
## Number of Groups: 10
```

The variance of the random intercepts decreased from 0.01 in Model m9 to 0.001 in Model m10 and spur length therefore explained 94.4% of the variance in the intercept among species. The relationship between intercepts and spur length was strongly positive (Figure S10).

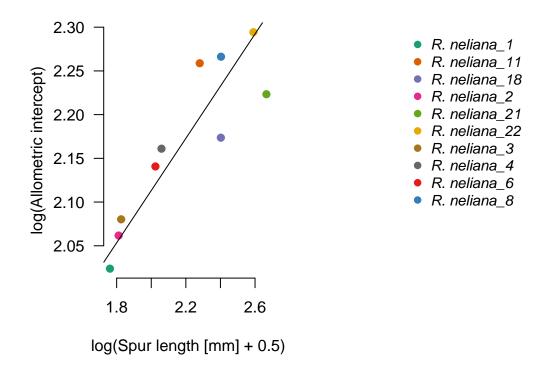


Figure S10: Relationship of allometric intercept to spur length of the host plants for *Rediviva neliana* populations. The allometric intercept shown are the Best Linear Unbiased Predictors for the population-specific intercepts estimated by model m9. The regression line shows the fitted relationship from model m10.

```
# calculate mean body size per population on arithmetic scale:
mean.body.a <- aggregate(exp(beemorph.n$log.body), by = list(beemorph.n$population_code), FUN=mean)
colnames(mean.body.a) <- c("Taxa", "mean.body.a")</pre>
# add mean body size back onto data frame:
beemorph.n <- merge(beemorph.n, mean.body.a, by.x = "population_code", by.y = "Taxa", all.x=T)
# difference in body size within species:
beemorph.n$diff.body.a <- exp(beemorph.n$log.body) - beemorph.n$mean.body.a
m11.n <- lme(exp(log.leg) ~ diff.body.a + I(mean.body.a-mean(body_size)) + population_spur_length,
           random =~1 population_code, data=beemorph.n) # adding spur length
summary(m11.n)
## Linear mixed-effects model fit by REML
##
   Data: beemorph.n
##
          AIC
                   BIC
                          logLik
##
     96.24288 114.0199 -42.12144
##
  Random effects:
##
##
   Formula: ~1 | population_code
##
           (Intercept) Residual
## StdDev:
             0.2013907 0.2918618
```

```
##
## Fixed effects: exp(log.leg) ~ diff.body.a + I(mean.body.a - mean(body_size)) +
                                                                                        population_spur_
##
                                       Value Std.Error DF t-value p-value
## (Intercept)
                                    6.179117 0.24712044 136 25.00448
## diff.body.a
                                    2.889377 0.11122753 136 25.97717
                                                                            0
## I(mean.body.a - mean(body_size)) 3.271283 0.26950322
                                                                            0
                                                          7 12.13820
## population spur length
                                    0.308210 0.02703073
                                                          7 11.40223
                                                                            0
   Correlation:
##
                                    (Intr) dff.b. I(..-m
## diff.body.a
                                     0.000
## I(mean.body.a - mean(body_size))
                                     0.480 0.000
## population_spur_length
                                    -0.961 0.000 -0.495
##
## Standardized Within-Group Residuals:
##
                                                           Max
                        Q1
                                   Med
                                                Q3
## -2.28662680 -0.57060922 -0.03948262 0.56448828
##
## Number of Observations: 147
## Number of Groups: 10
# testing whether the effect of spur length is different from 1
tstat.m11 <-(summary(m11.n)$tTable[4,1]-1)/summary(m11.n)$tTable[4,2] # t statistic
p.spur <- pt(tstat.m11,df=summary(m11.n)$tTable[4,3], lower.tail = T)*2 # p value (2-sided alternative)
```

As for the between-species comparison, we re-fitted the multi-level model (Equation 11) to leg length and body length on the arithmetic scale. If leg length tracked spur length perfectly, we would expect this coefficient to be close to 1 on this scale. However, the estimated effect was 0.31, which is considerably less than 1 (t = -25.59, P = 0, Figure S11).

Comparing the variance of the random intercepts in Model m11 to an equivalent model without spur length, we find that spur length explained 94.9% of the variance in the intercept among populations when analysing allometry on the arithmetic scale.

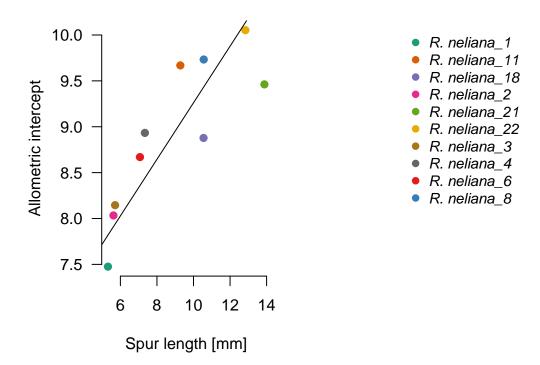


Figure S11: Relationship of allometric intercept (i.e. estimated population-specific leg length from Model m11) to spur length of the host plants for *Rediviva neliana* populations, fitted on the aritmetic scale.

References

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Heisler, I. L., and J. Damuth. 1987. A Method for Analyzing Selection in Hierarchically Structured Populations. American Naturalist 130:582–602.

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