

**Cross Attention Performs Orthogonal
Alignment in Recommendation models**

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[1] Motivation

- Cross-Domain Sequential Recommendation (CDSR)

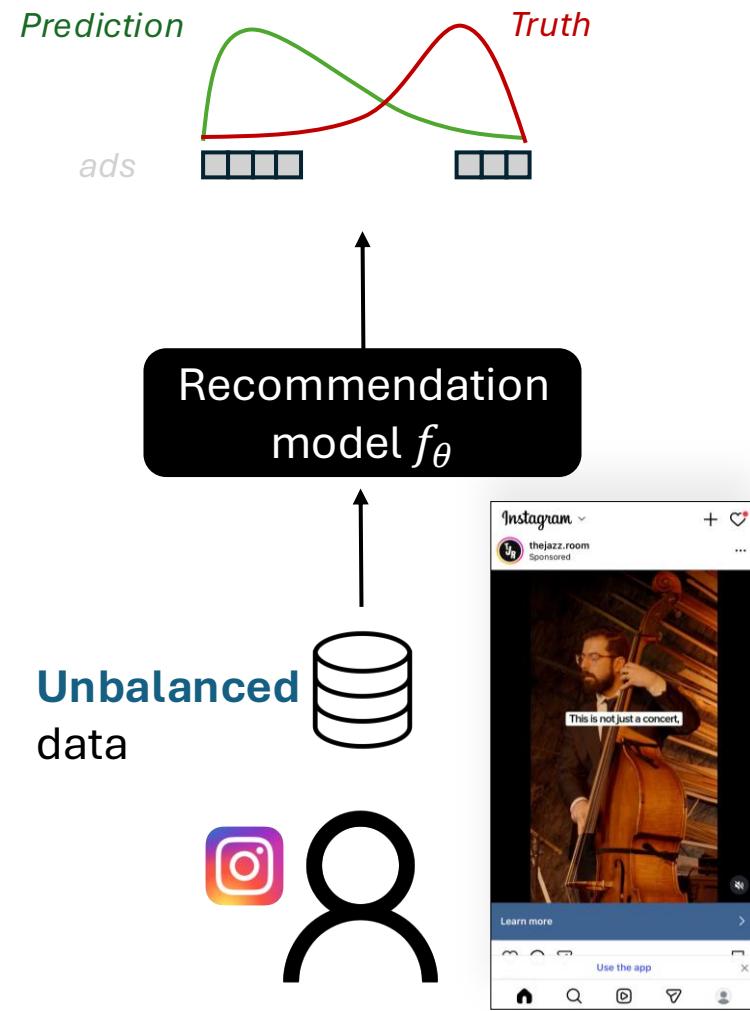
[2] RQ1: how to improve the performance

- **Gated Cross Attention** at the early stage improve the performance.

[3] RQ2 (**Main**) : why it improves the performance

- **Orthogonal Alignment** improves the scaling law.

1. Motivation



Problem: Building **recommendation models** that show advertisement to user.

(If user clicks an ad, that's how company earns money).

Task: We train a model:

$$f_{\theta}(user_i - ads \text{ data}) \in [0,1]$$

Which represents the probability that $user_i$ clicks on ad_j

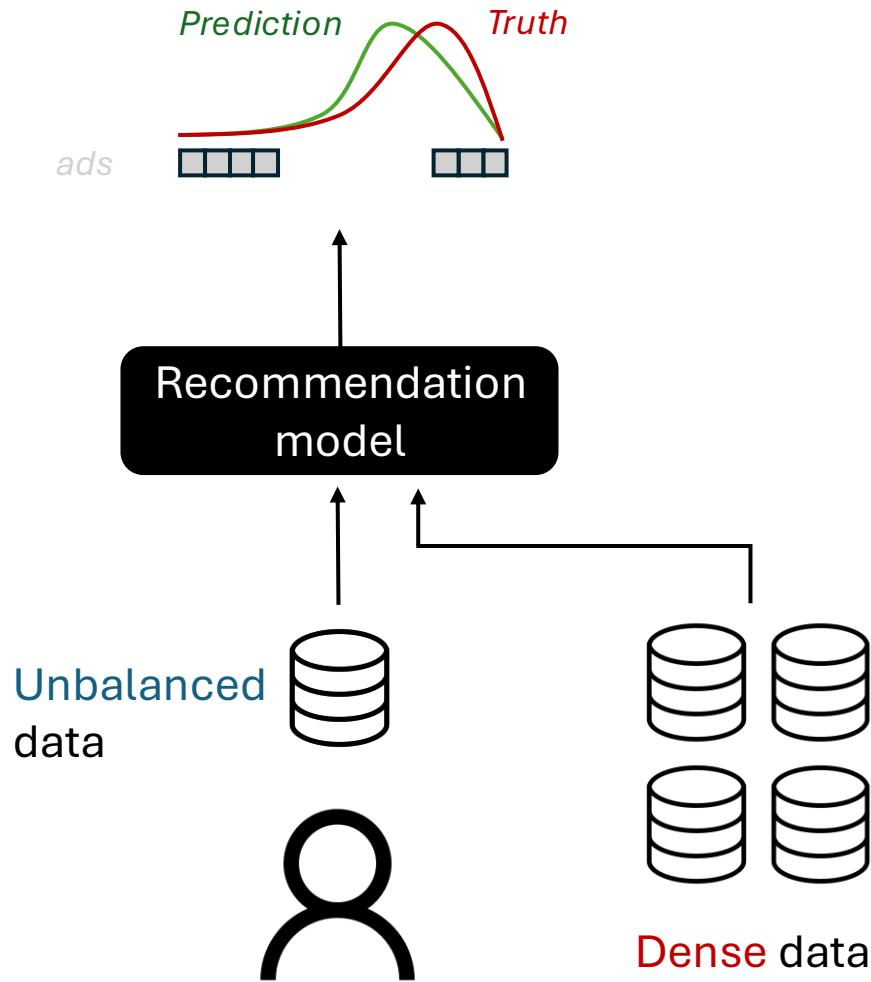
- Times series dataset

$$\mathcal{D} = \left\{ user_i, : \left\{ time, ad_j, \{0, 1\} \right\} \right\}_{i \in [I], j \in [J]}$$

Challenge: The key challenge was ads-domain data is **Unbalanced**; users rarely click ads.

- Ex: {(14:00, ad-sport, 0),
(14:01 ,ad-movie, 0),
(14:02 ,ad-movie, 1),
...(14:10, ad-Jazz, 0)}

1. Motivation



Problem: Building recommendation models that display sponsored posts (ads) to user. (*If user clicks an ad, that's how company earns money*).

Challenge: The key challenge was ads-domain data is **Unbalanced**; users rarely click ads.

Cross-Domain Sequential Recommendation(CDSR) : Let's use **dense** data from other domain

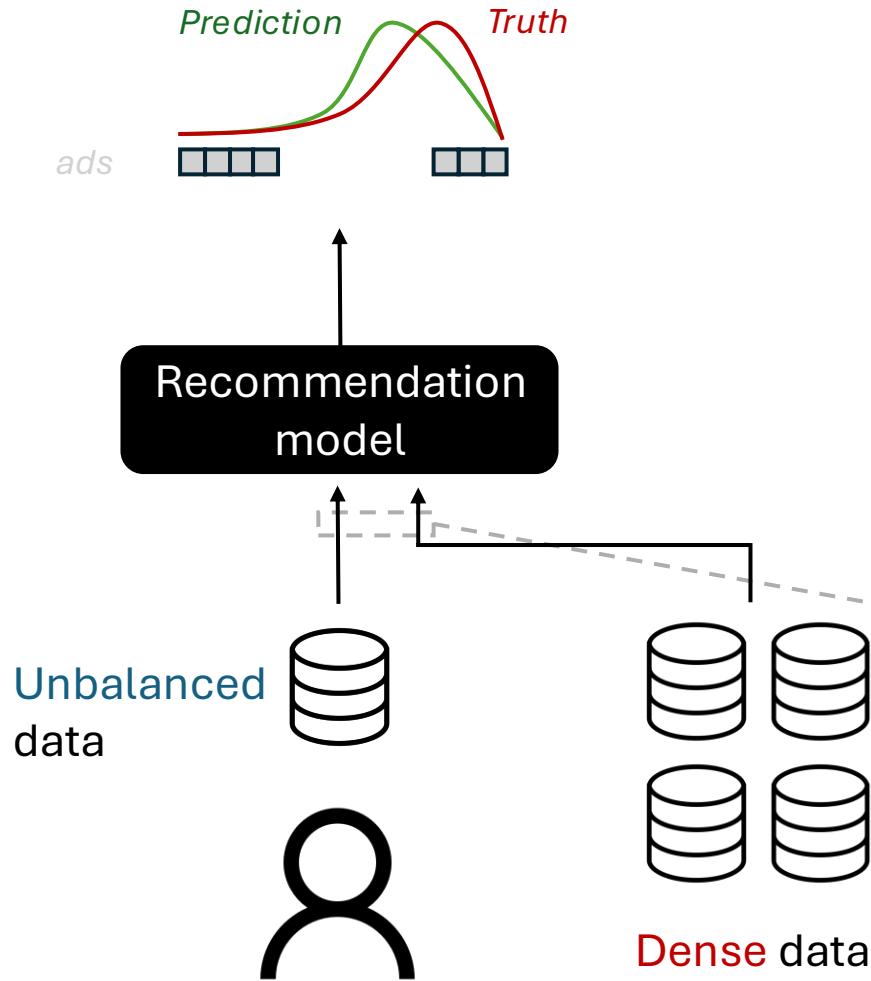
[Source Domain 1] Facebook app – post view duration.

- Ex: {(09/06, post-sport, 30s), (09/06, post-movie, 10s), (09/08, post-Jazz, 300s), ... }

[Source Domain 2] Instagram app – post likes.

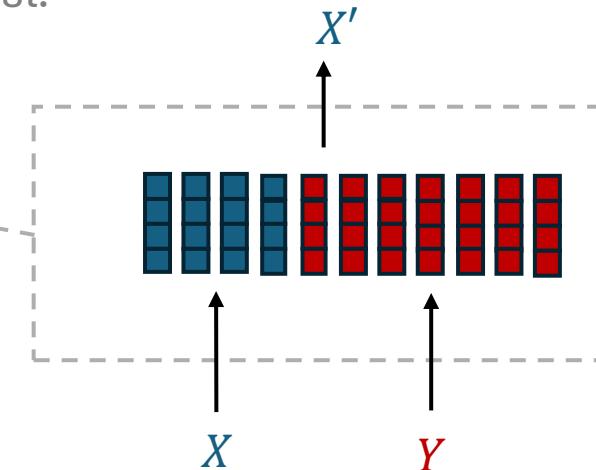
- Ex: {(09/06, post-sport, 1), (09/07, post-Jazz, 1), (09/08, post-Jazz, 1), ... }

2. Research Question 1



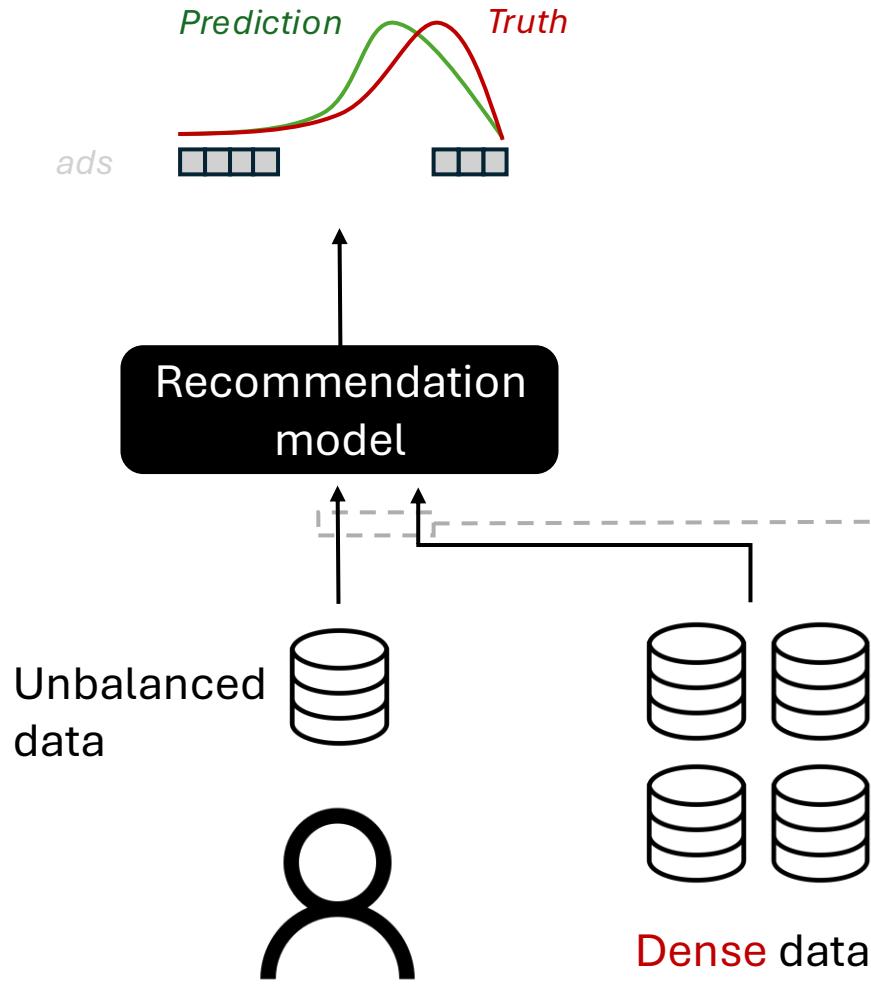
Research Question 1: How to fuse those different modality data to improve the performance?

- Naive concatenation: Negative Transfer
 - Domain Noise
 - Preference conflicts: (ex) user like to “view” video game post for a long time, but do not purchase since user just likes to watch streamer’s game broadcast.



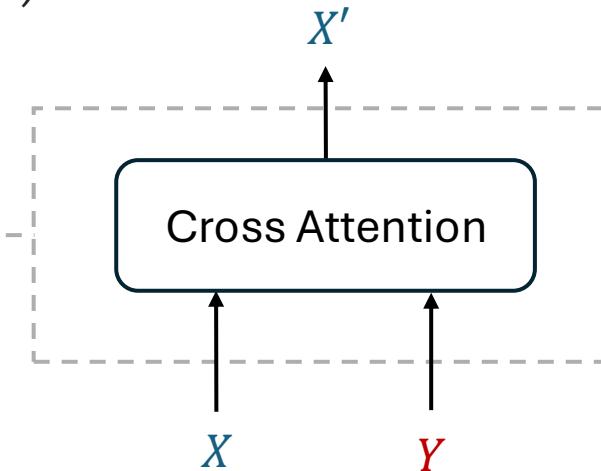
2. Research Question 1

2.1. observation 1



Research Question 1: How to fuse those different modality data to improve the performance?

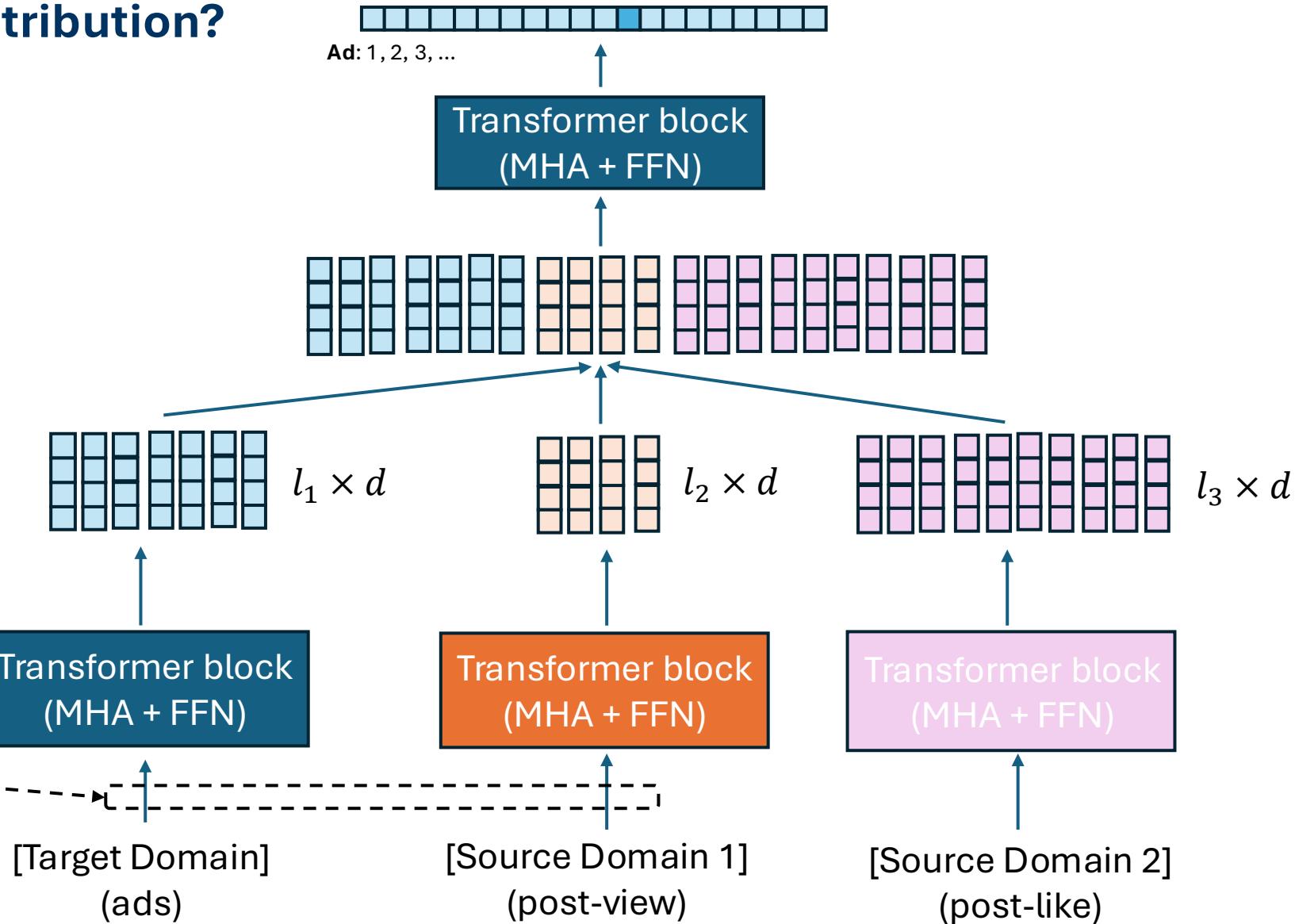
Observation 1: Using Gated Cross Attention at the Early Stage can improve the performance
(*First Contribution*)



2. Research Question 1

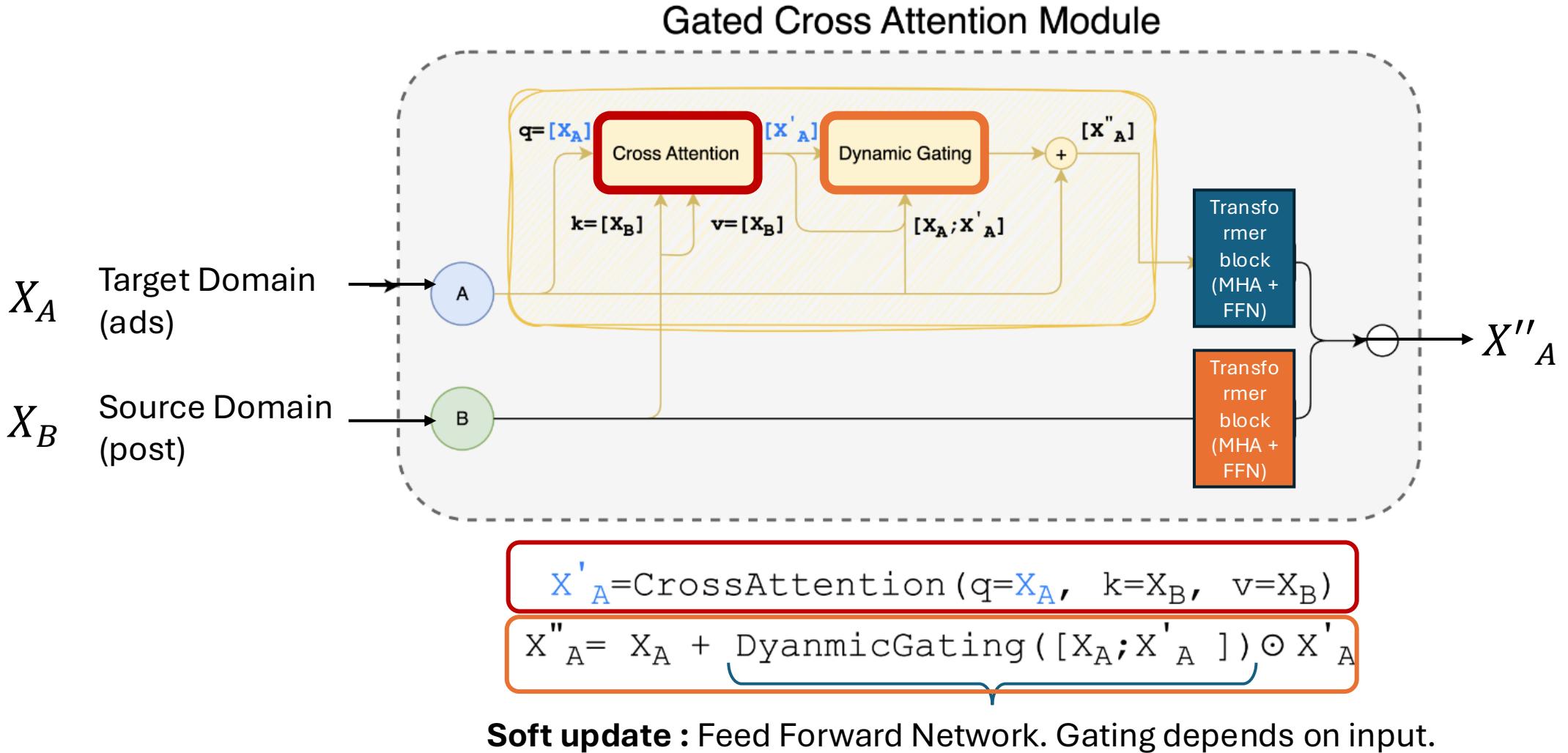
2.2. why contribution?

Observation:
Early cross-sequence interactions improve performance



2. Research Question 1

2.3. Gated Cross Attention module



2. Research Question 1

2.4. Experiment setting

- Baselines : CDSRNP, ABXI, LLM4CDSR
 - On top of baselines, we use Gated Cross Attention (GCA); that is skip connection: $X + \alpha X'$.
- Dataset: Four pairs from Amazon dataset (ex. Beauty-Electronic)

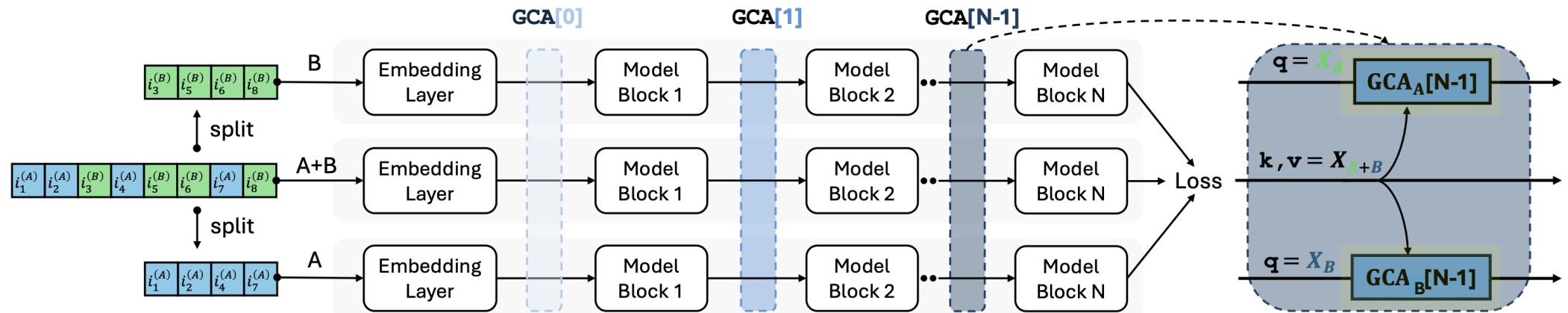


Figure 3 For each baseline model, we insert GCA modules at multiple vertical positions, denoted as $\text{GCA}[i]$, where $i = 0$ corresponds to the module closest to the raw data and $i = N$ to the module farthest from the raw data. By design, $\text{GCA}[0]$ is always placed immediately after the embedding layer, while $\text{GCA}[1], \text{GCA}[2], \dots$ are positioned within intermediate layers of the backbone. Each $\text{GCA}[i]$ comprises two parallel gated cross-attention modules, which respectively refine the representations of domains A and B .

2. Research Question 1

2.5. Observation 1

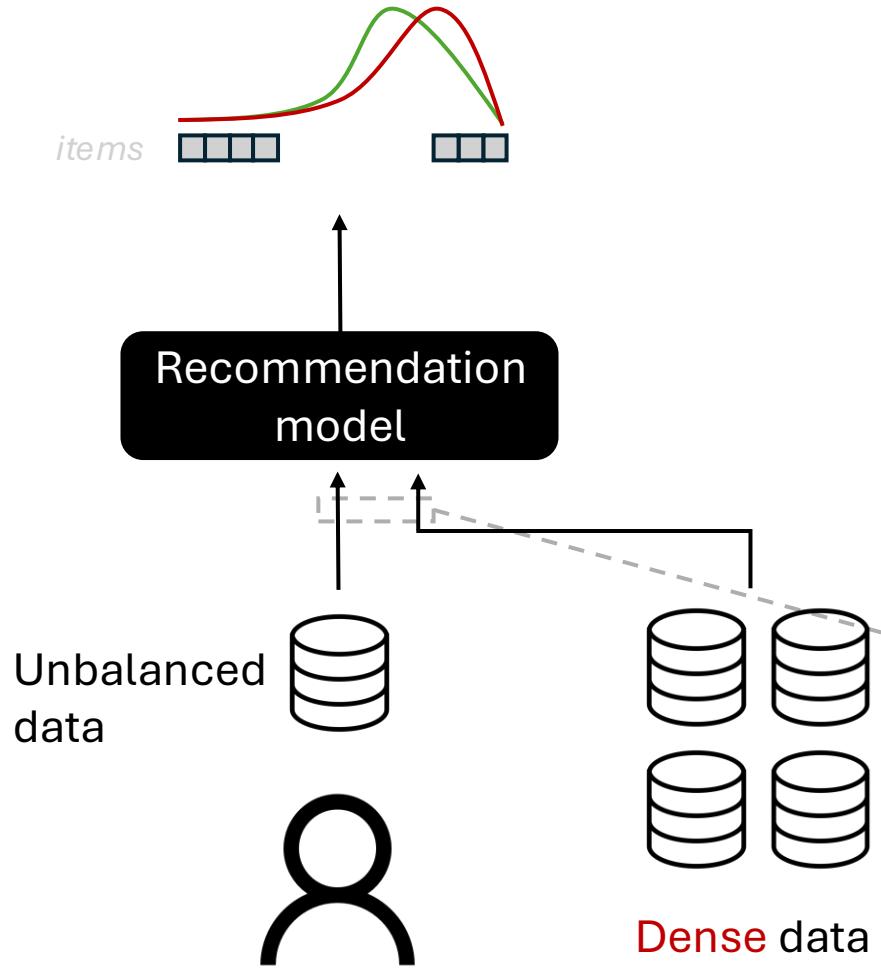
- GCA at the early stage consistently improves performance, but vertical stacking is not scalable.

Model	Dataset (A-B)	NDCG@1 _A	NDCG@10 _A	NDCG@1 _B	NDCG@10 _B	AUC _A	AUC _B
GCA [0]	LLM4CDSR	0.7157 \pm 0.0025	0.7821 \pm 0.0018	0.5870 \pm 0.0051	0.6493 \pm 0.002	0.9216 \pm 0.0013	0.8621 \pm 0.0054
	+ GCA _{early}	0.7283 \pm 0.0027	0.8052 \pm 0.0014	0.5977 \pm 0.0054	0.6560 \pm 0.0046	0.9364 \pm 0.0009	0.8655 \pm 0.0038
	+ GCA _{stack}	0.7310 \pm 0.0012	0.8056 \pm 0.0014	0.6112 \pm 0.0032	0.6638 \pm 0.0038	0.9370 \pm 0.0010	0.8664 \pm 0.0030
GCA [0,1] or GCA [0,2], ...	LLM4CDSR	0.2101 \pm 0.0030	0.3512 \pm 0.0009	0.1419 \pm 0.0008	0.2608 \pm 0.0010	0.7901 \pm 0.0008	0.7197 \pm 0.0011
	+ GCA _{early}	0.2378 \pm 0.0011	0.3815 \pm 0.0018	0.1861 \pm 0.0035	0.2845 \pm 0.0027	0.7970 \pm 0.0018	0.7218 \pm 0.0026
	+ GCA _{stack}	0.2410 \pm 0.0012	0.3800 \pm 0.0011	0.1994 \pm 0.0054	0.3035 \pm 0.0049	0.7937 \pm 0.0013	0.7252 \pm 0.0026
ABXI	Beauty-Elec	0.0730 \pm 0.0070	0.1724 \pm 0.0071	0.0548 \pm 0.0038	0.1273 \pm 0.0028	0.7216 \pm 0.0027	0.7123 \pm 0.0009
	+ GCA _{early}	0.0727 \pm 0.0060	0.1793 \pm 0.0047	0.0544 \pm 0.0044	0.1244 \pm 0.0025	0.7410 \pm 0.0025	0.7169 \pm 0.0024
	+ GCA _{stack}	0.0733 \pm 0.0042	0.1846 \pm 0.0057	0.0566 \pm 0.0052	0.1271 \pm 0.0042	0.7354 \pm 0.0048	0.6973 \pm 0.0051
ABXI	Food-Kitch	0.0593 \pm 0.0074	0.1541 \pm 0.0130	0.0416 \pm 0.0058	0.1093 \pm 0.0113	0.7205 \pm 0.0015	0.7180 \pm 0.0032
	+ GCA _{early}	0.0703 \pm 0.0094	0.1757 \pm 0.0092	0.0548 \pm 0.0053	0.1327 \pm 0.0072	0.7317 \pm 0.0039	0.7150 \pm 0.0031
	+ GCA _{stack}	0.0882 \pm 0.0052	0.1853 \pm 0.0013	0.0527 \pm 0.0020	0.1282 \pm 0.0028	0.7148 \pm 0.0026	0.6924 \pm 0.0009
CDSRNP	Elec-Phone (1M)	0.0499 \pm 0.0087	0.1170 \pm 0.0079	0.0920 \pm 0.0050	0.1935 \pm 0.0021	-	-
	+ GCA _{early}	0.0547 \pm 0.0010	0.1209 \pm 0.0092	0.0980 \pm 0.0010	0.1989 \pm 0.0031	-	-
	+ GCA _{stack}	0.0531 \pm 0.0078	0.1229 \pm 0.0125	0.0946 \pm 0.0022	0.1942 \pm 0.0012	-	-

Table 1 NCDG and AUC comparison with the three baselines and adhoc model with GCA. Elec stands for Electronic, and Kitch stands for Kitchen. GCA_{early} denotes GCA[0] and GCA_{stack} denotes GCA[0, i_1, i_2, \dots, i_N] where $i_n > 1, n \in [N]$

3. Research Question 2 (Main)

3.1. Research Question 2



So far:

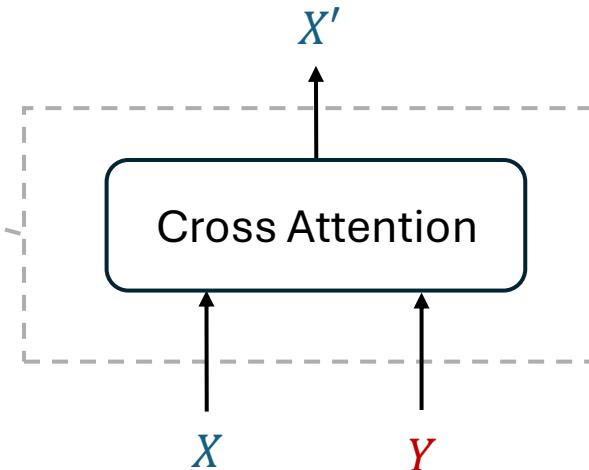
Gated Cross Attention at the early stage can improve performance

Research Question 2:

Why gated cross attention improve the performance?

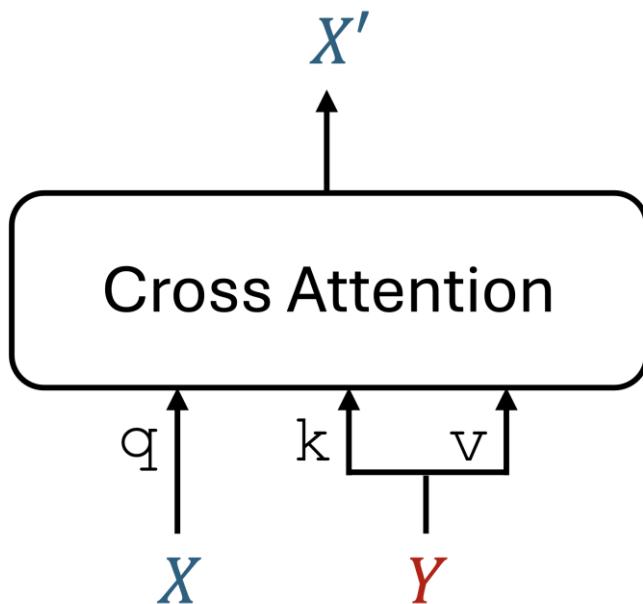
Observation:

As training goes by, $\cos(X, X')$ goes to zero.



3. Research Question 2 (Main)

3.2. Previous literature: conventional understanding on cross-attention as residual Alignment



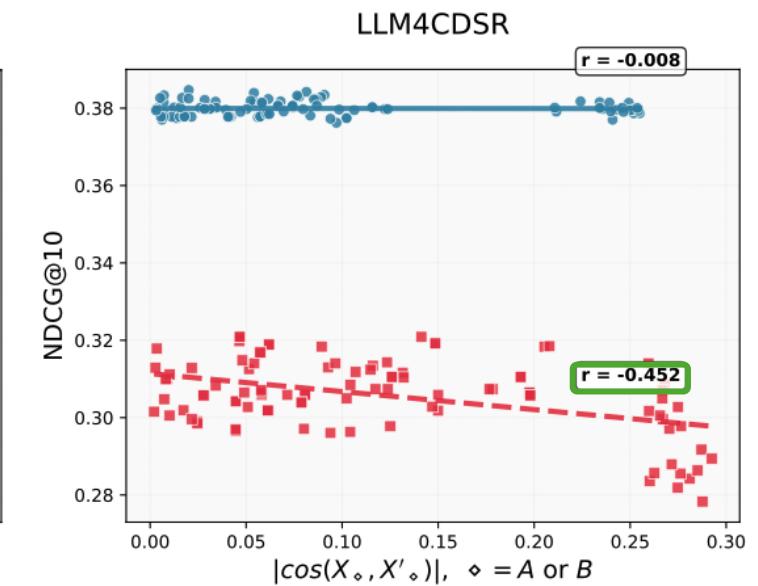
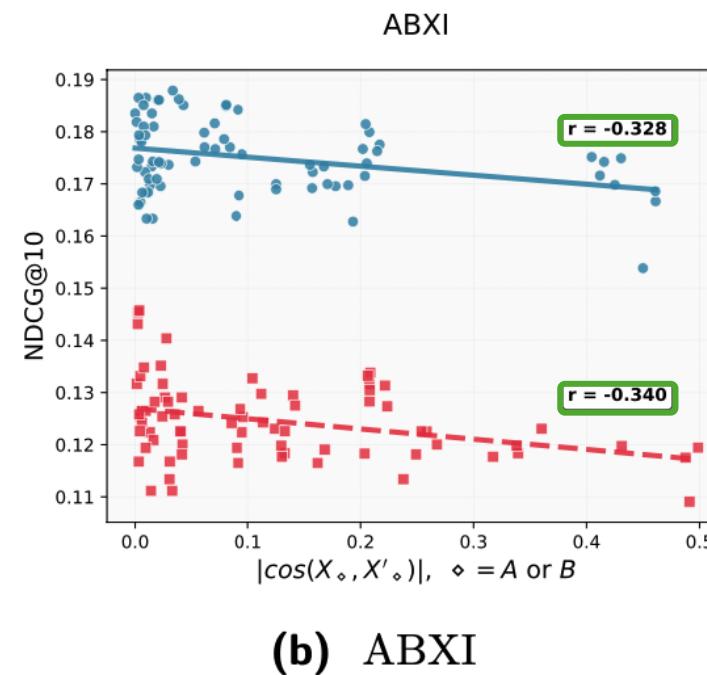
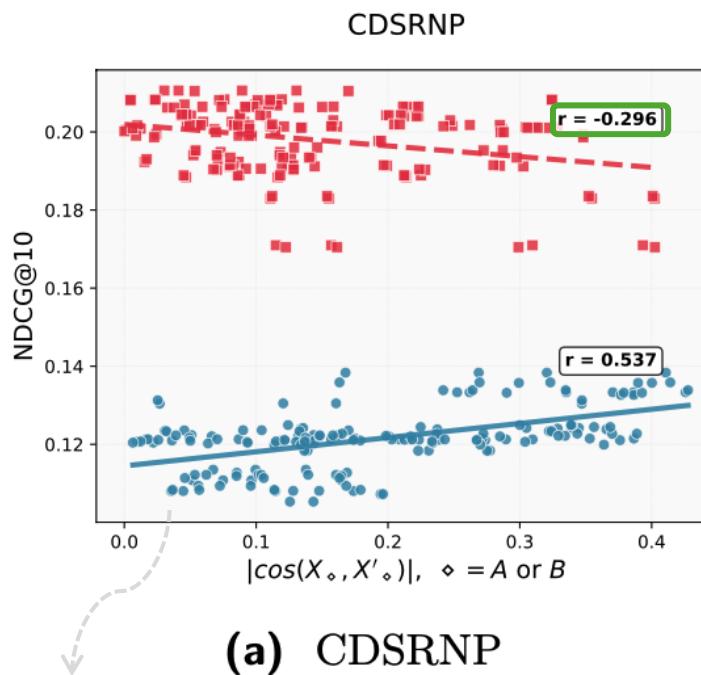
Residual Alignment:

- X' is generated by removing redundant information from X and preserving nonredundant information from X by referring to Y .
 - X : User likes to visit Milan, Italy
 - Y : User bought lots of sports players' uniforms
 - X' : User may likes to buy AC Millan's uniforms

3. Research Question 2 (Main)

3.3. Observation 2 (Supports main message 1)

- We observe **negative correlation** between $\cos(X, X')$ and model performance regardless of dataset and baseline.



Vertical Stacking: {GCA[0], GCA[0,1], GCA[0,2],...}

Dataset : {Cloth-sports, Elec-phone, ...}

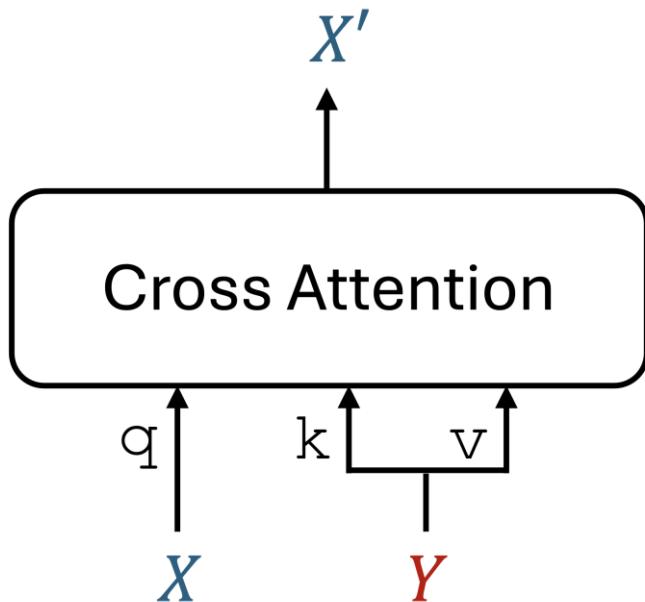
Hidden dimension: {64, 128, ...}

Num of attention heads: {4, 8, ...}

3. Research Question 2 (Main)

3.4. Main Message 1

Main Message 1



Orthogonal Alignment:

A phenomenon such that as X' and X getting orthogonal, then the model performance increases

- X' can be trained to contain information **irrelevant** to X by referring to Y .
 - X : User likes to visit Milan, Italy
 - Y : User bought lots of sports players' uniforms
 - X' : User may likes to visit Manchester, England

3. Research Question 2 (Main)

3.5. Observation 3 (Supports main message 1)

- GCA induces orthogonalization independently of how similar X and Y happens to be.

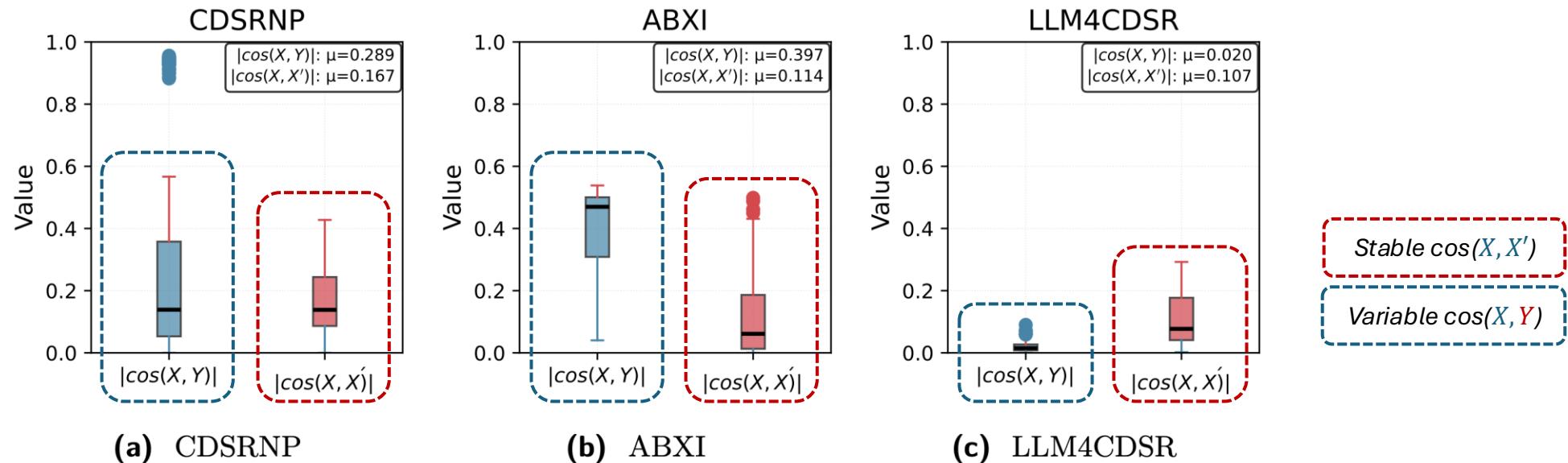


Figure 8 Boxplots of cosine similarities $|\cos(X, Y)|$ and $|\cos(X, X')|$. While $|\cos(X, X')|$ remains stable across models (median $\approx [0.1, 0.2]$), $|\cos(X, Y)|$ varies substantially depending on the dataset, highlighting that GCA induces a consistent degree of orthogonalization regardless of underlying X (query)– Y (key,value) similarity. μ represents a median.

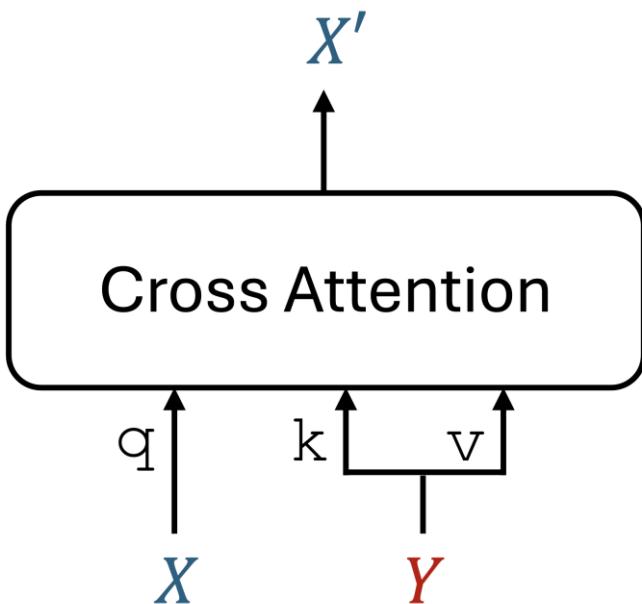
3. Research Question 2 (Main)

3.6. Main Message 2

So far

Orthogonal Alignment:

A phenomenon such that as X' and X getting orthogonal, then the model performance increases



Main Message 2

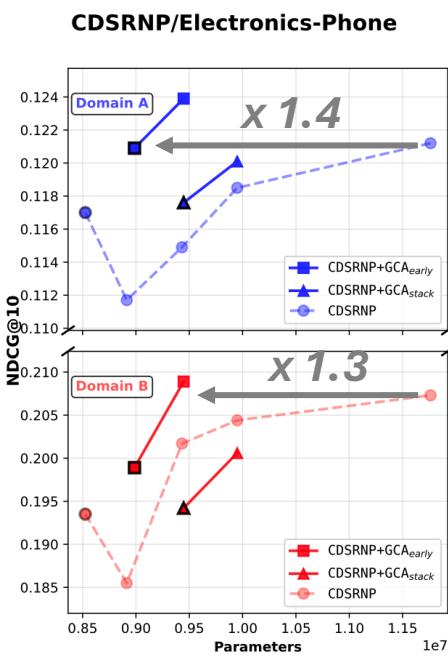
Orthogonal Alignment **emerges naturally**, since it improves scaling law

- High level : As an perspective of model, feeding $X + \alpha X'$ where $X' \perp X$ is better quality signal than X' as denoised X .

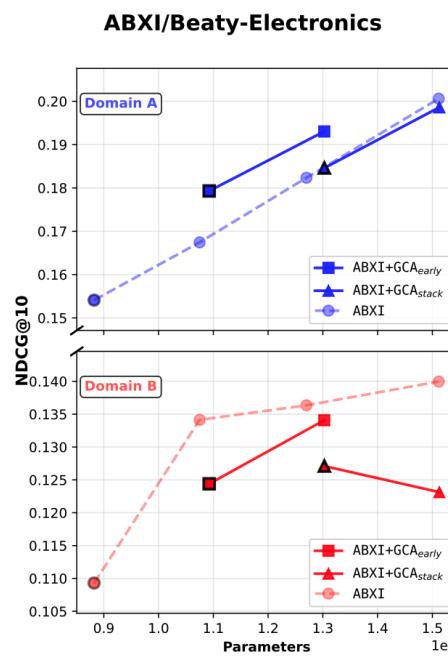
3. Research Question 2 (Main)

3.7. Observation 4 (Supports main message 2)

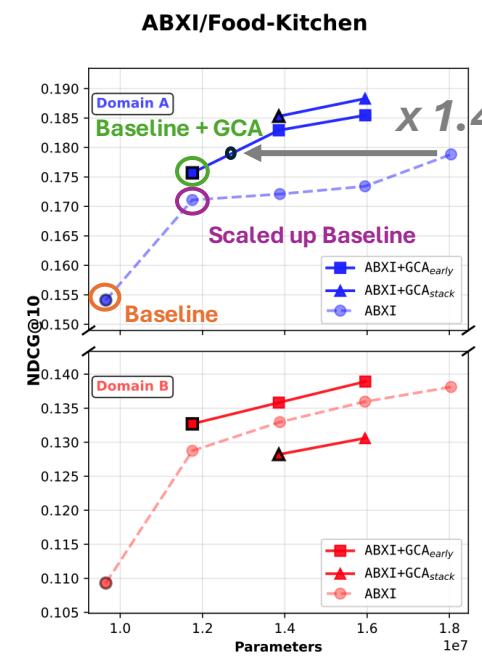
- Ex: Scaled up Baseline (3M) vs. Baseline (2M) + GCA (1M)
- Orthogonal Alignment provides $\sim x1.4$ parameter efficient scaling up.



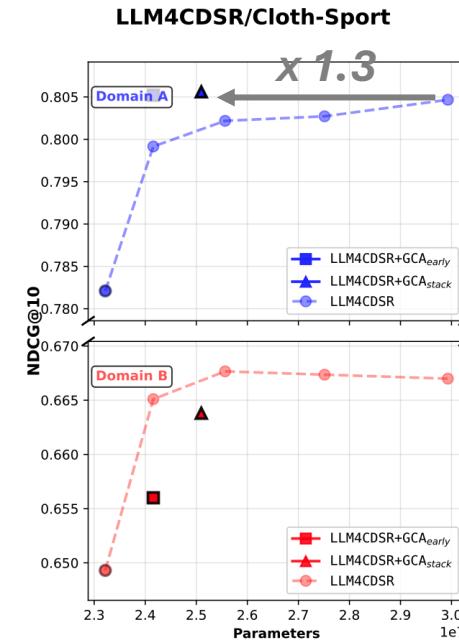
(a) CDSRNP



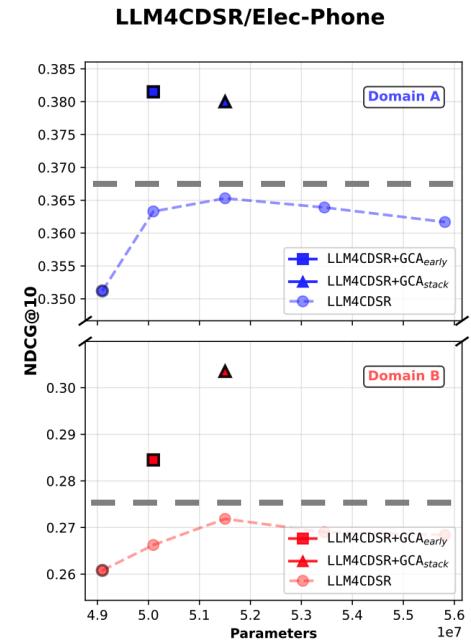
(b) ABXI (Beauty-Elec)



(c) ABXI (Food-Kitch)



(d) LLM4CDSR (Cloth-Sports)



(e) LLM4CDSR (Elec-Phone)

Summary

Motivation: In recommendation models, learning a universal user preference from different modality user behavior data due to some sparse interaction data.

Research Question: Cross-attention is widely used mechanism to fuse different modality data, but it's inner mechanism is poorly understood.

Main Message:

1. Orthogonal Alignment: If input (X) and output (X') of cross-attention is getting orthogonal, then performance increases
2. Orthogonal alignment naturally happens since it improves the scaling law.

