

# Cross Attention Performs Orthogonal Alignment in Recommendation models

# Contents

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## [1] Motivation

- Cross-Domain Sequential Recommendation (CDSR)

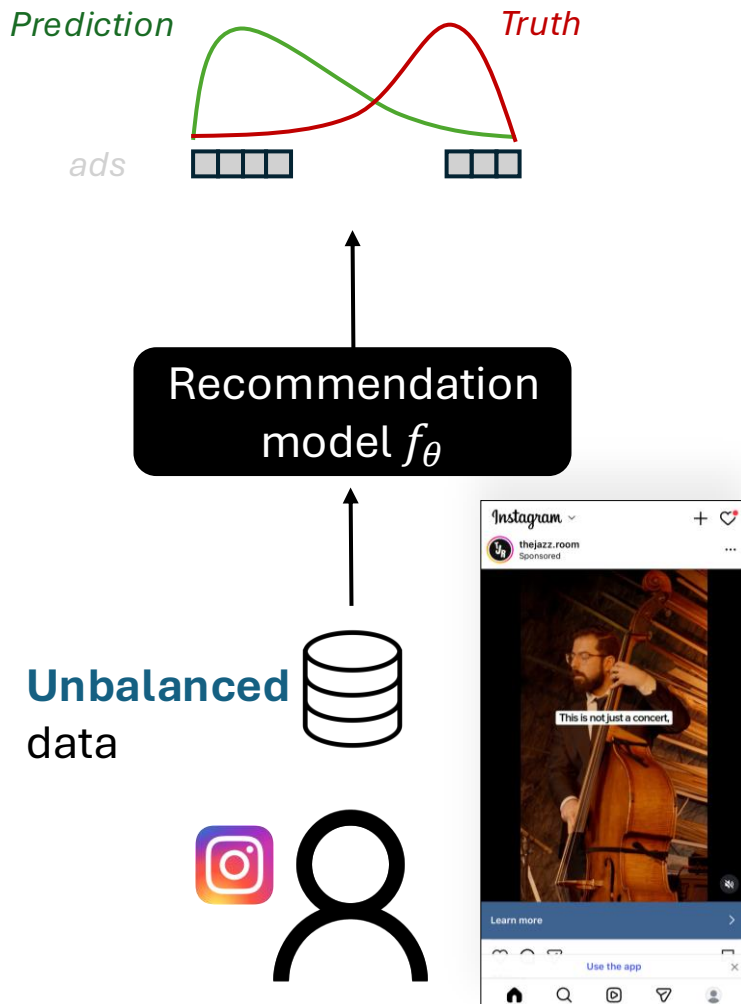
## [2] RQ1: how to improve the performance

- **Gated Cross Attention** at the early stage improve the performance.

## [3] RQ2 (**Main**) : why it improves the performance

- **Orthogonal Alignment** improves the scaling law.

# 1. Motivation



**Problem:** Building **recommendation models** that show advertisement to user.

(If user clicks an ad, that's how company earns money 💰).

**Task:** We train a model:

$$f_{\theta}(\text{user}_i - \text{ads data}) \in [0,1]$$

Which represents the probability that  $\text{user}_i$  clicks on  $\text{ad}_j$

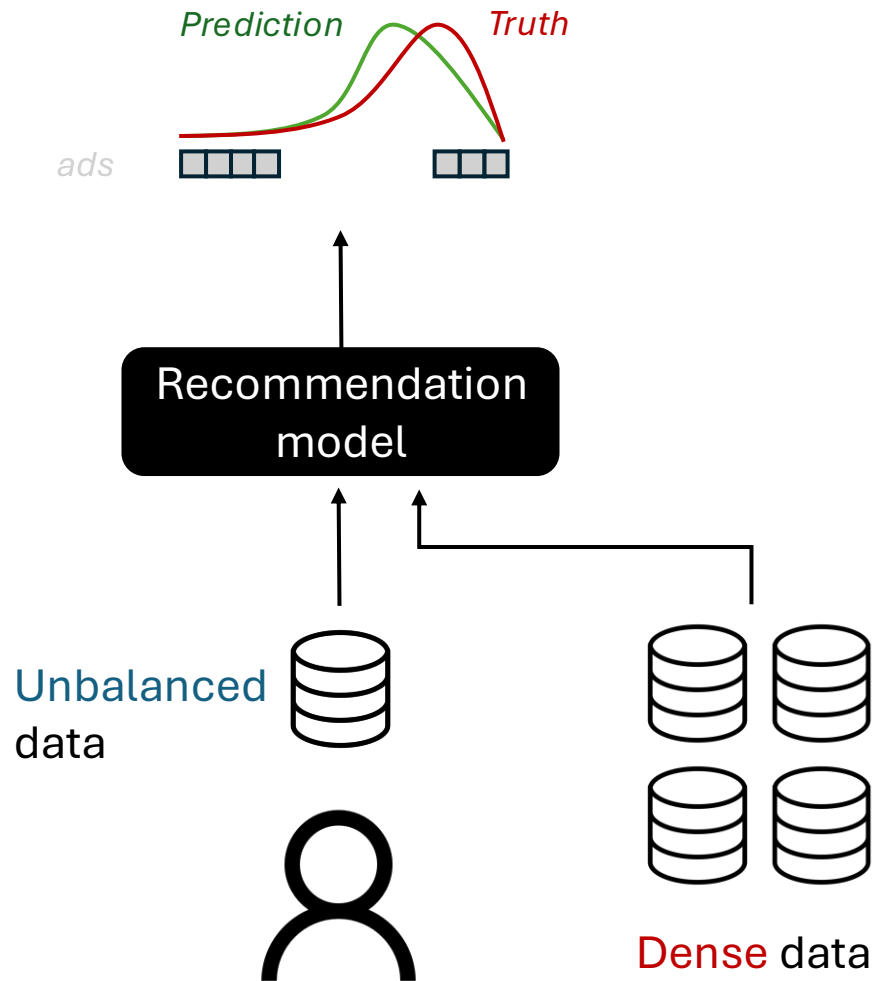
- Times series dataset

$$D = \left\{ \text{user}_i, : \left\{ \text{time}, \text{ad}_j, \{0, 1\} \right\} \right\}_{i \in [I], j \in [J]}$$

**Challenge:** The key challenge was ads-domain data is **Unbalanced**; users rarely click ads.

- Ex:  $\{(14:00, \text{ad-sport}, 0),$   
 $(14:01, \text{ad-movie}, 0),$   
 $(14:02, \text{ad-movie}, 1),$   
 $\dots(14:10, \text{ad-Jazz}, 0)\}$

# 1. Motivation



**Problem:** Building recommendation models that display sponsored posts (ads) to user. *(If user clicks an ad, that's how company earns money 💰).*

**Challenge:** The key challenge was ads-domain data is **Unbalanced**; users rarely click ads.

**Cross-Domain Sequential Recommendation(CDSR)** : Let's use **dense** data from other domain

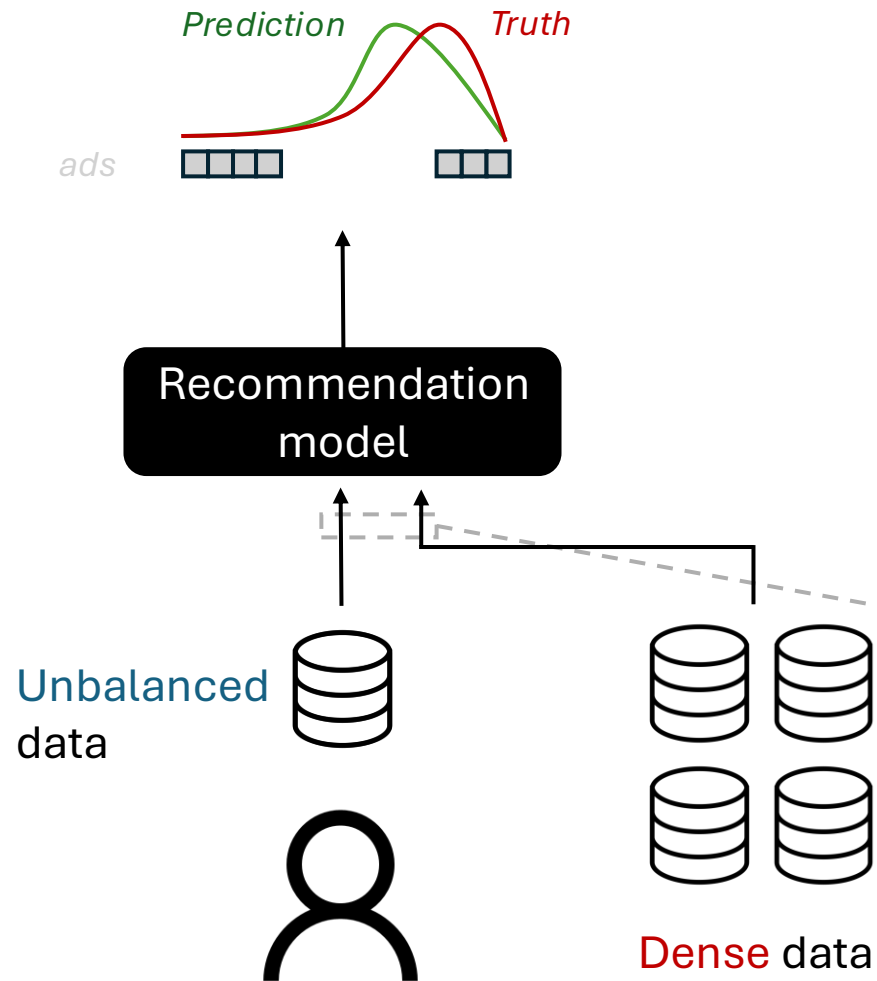
**[Source Domain 1]** Facebook app – post view duration.

- Ex: {(09/06, post-sport, 30s), (09/06, post-movie, 10s), (09/08, post-Jazz, 300s), ... }

**[Source Domain 2]** Instagram app – post likes.

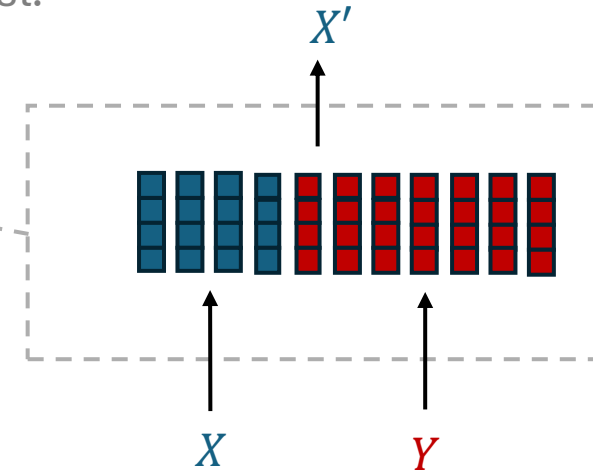
- Ex: {(09/06, post-sport, 1), (09/07, post-Jazz, 1), (09/08, post-Jazz, 1), ... }

## 2. Research Question 1



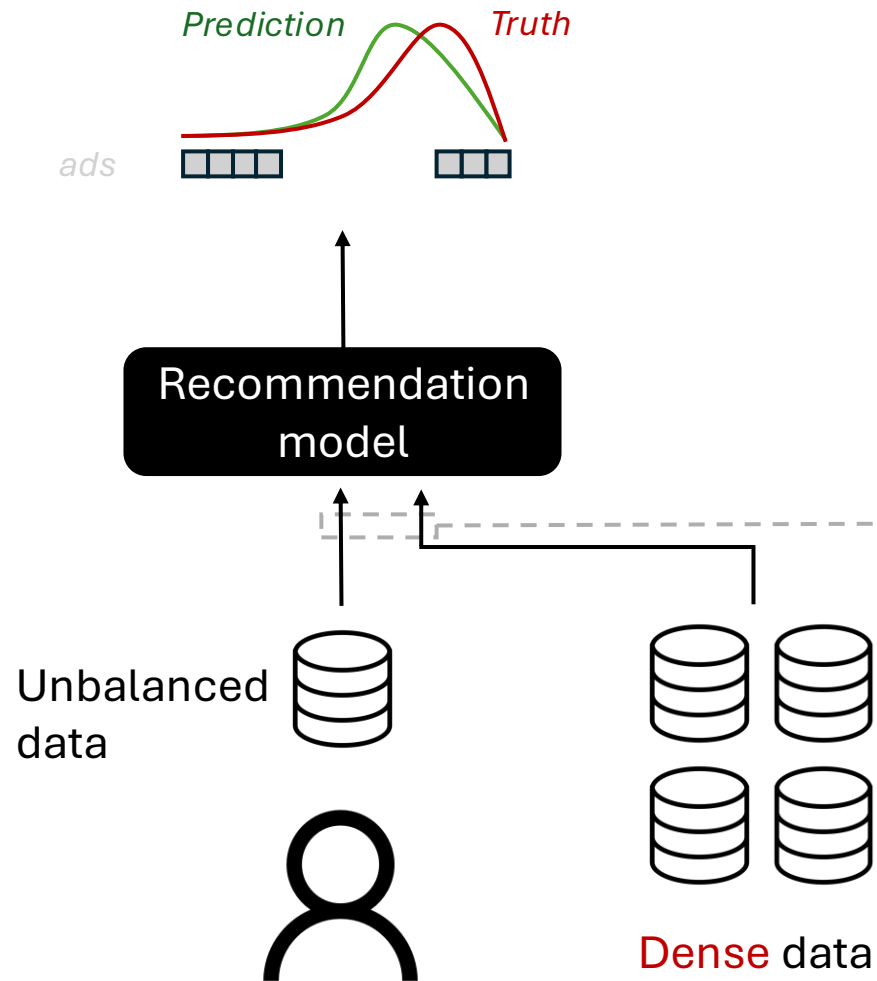
**Research Question1:** How to fuse those different modality data to improve the performance?

- Naive concatenation: Negative Transfer
  - Domain Noise
  - Preference conflicts: *(ex) user like to “view” video game post for a long time, but do not purchase since user just likes to watch streamer’s game broadcast.*



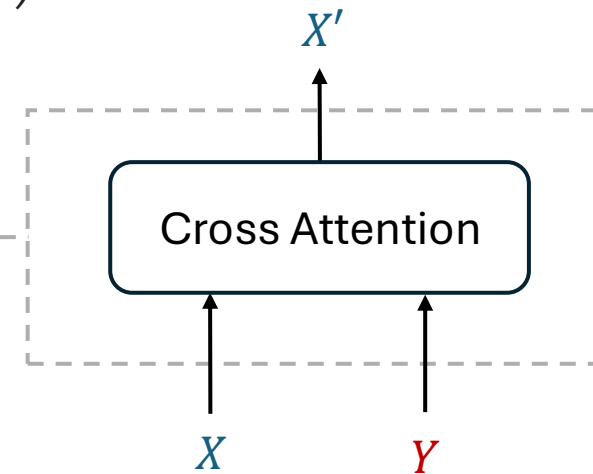
## 2. Research Question 1

### 2.1. observation 1



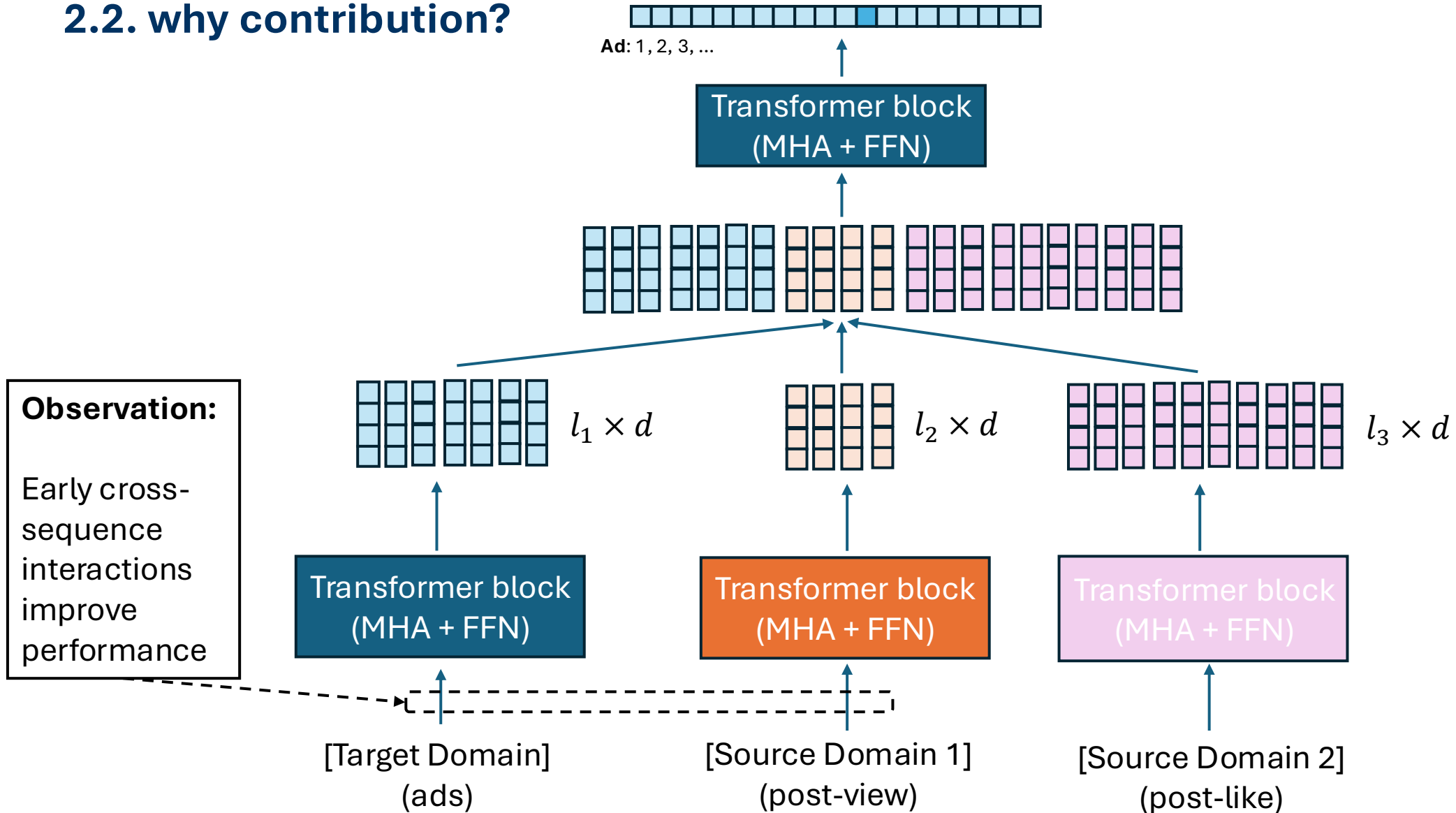
**Research Question1:** How to fuse those different modality data to improve the performance?

**Observation 1:** Using Gated Cross Attention at the Early Stage can improve the performance  
(*First Contribution*)



## 2. Research Question 1

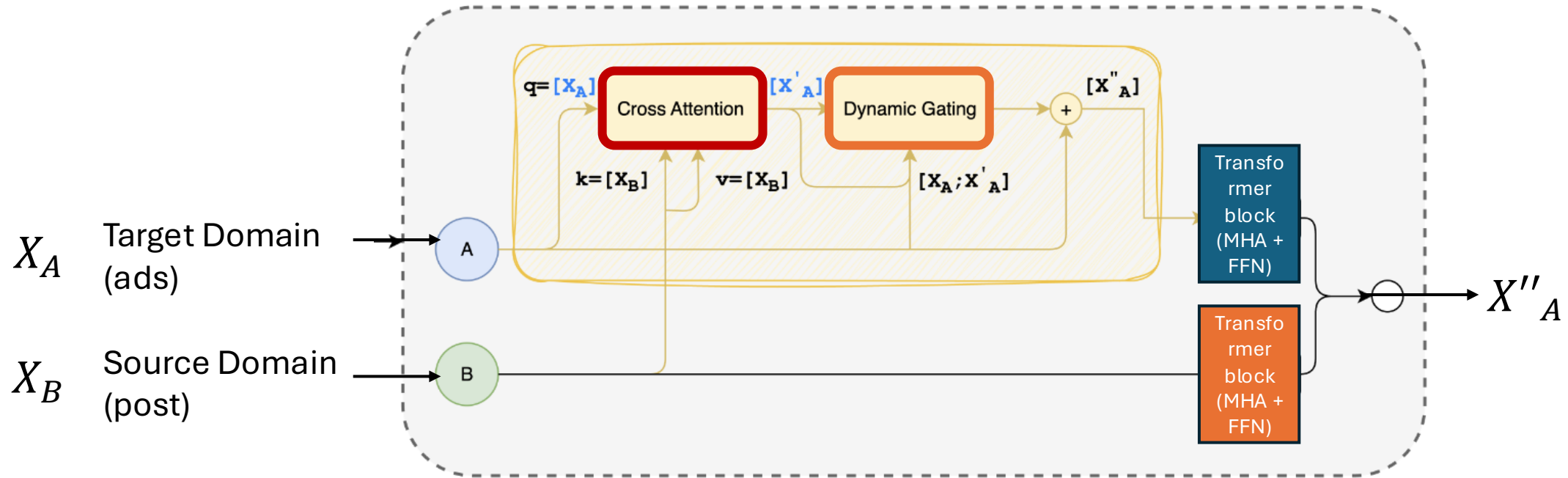
### 2.2. why contribution?



## 2. Research Question 1

### 2.3. Gated Cross Attention module

Gated Cross Attention Module



$$X'_A = \text{CrossAttention}(q=X_A, k=X_B, v=X_B)$$

$$X''_A = X_A + \underbrace{\text{DyanmicGating}([X_A; X'_A])}_{\text{Soft update : Feed Forward Network. Gating depends on input.}} \odot X'_A$$

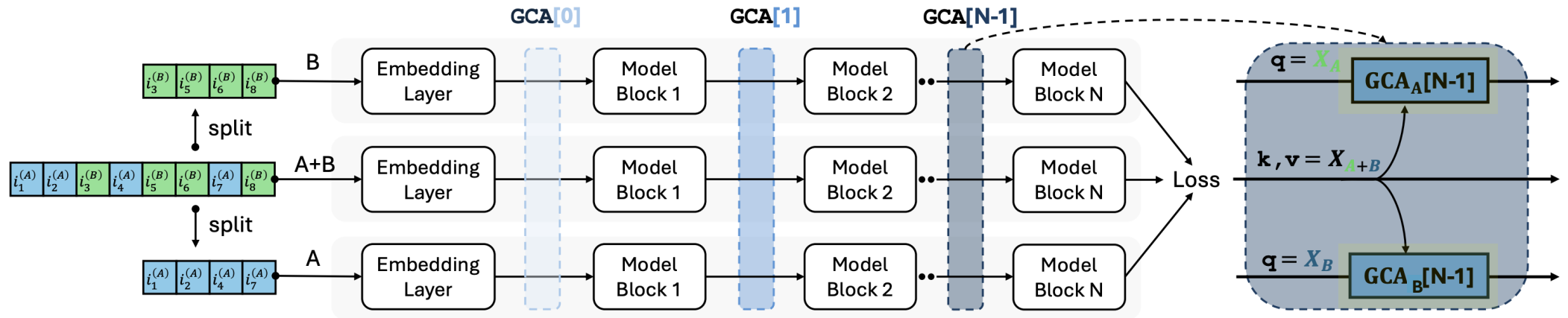
**Soft update** : Feed Forward Network. Gating depends on input.



## 2. Research Question 1

### 2.4. Experiment setting

- Baselines : CDSRNP, ABXI, LLM4CDSR
  - On top of baselines, we use Gated Cross Attention (GCA); that is skip connection:  $X + \alpha X'$ .
- Dataset: Four pairs from Amazon dataset (ex. Beauty-Electronic)



**Figure 3** For each baseline model, we insert GCA modules at multiple vertical positions, denoted as  $\text{GCA}[i]$ , where  $i = 0$  corresponds to the module closest to the raw data and  $i = N$  to the module farthest from the raw data. By design,  $\text{GCA}[0]$  is always placed immediately after the embedding layer, while  $\text{GCA}[1], \text{GCA}[2], \dots$  are positioned within intermediate layers of the backbone. Each  $\text{GCA}[i]$  comprises two parallel gated cross-attention modules, which respectively refine the representations of domains  $A$  and  $B$ .

## 2. Research Question 1

### 2.5. Observation 1

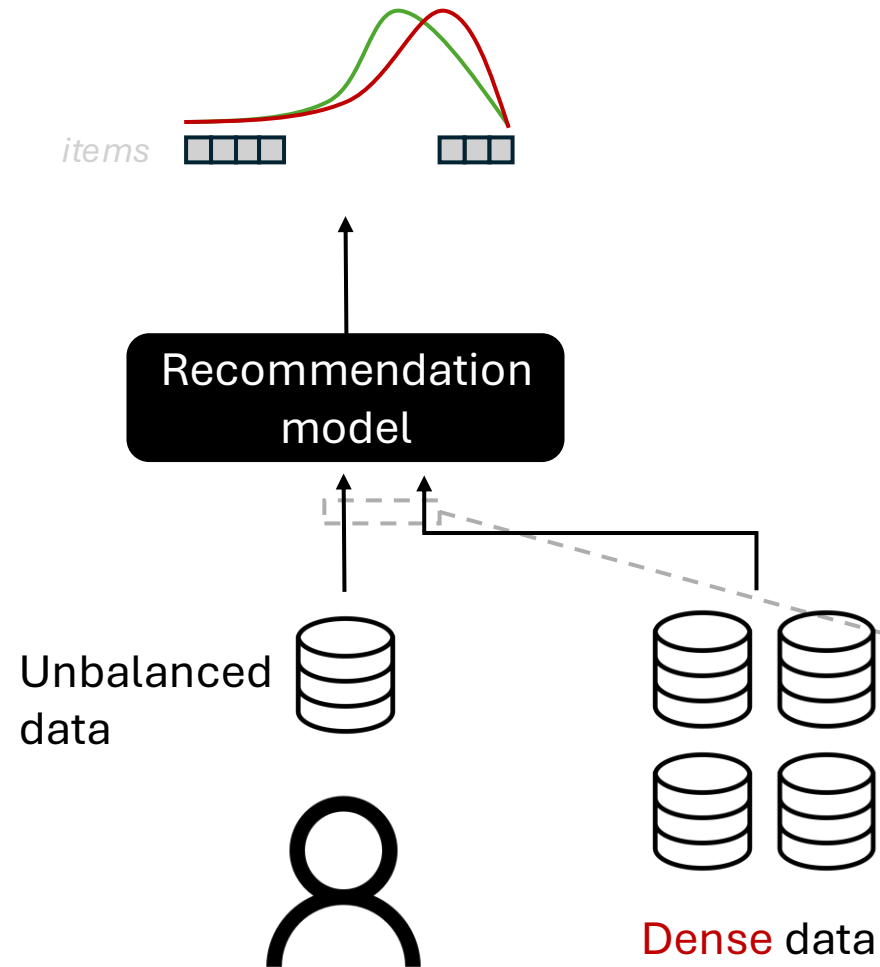
- GCA at the early stage consistently improves performance, but vertical stacking is not scalable.

	Model	Dataset (A-B)	NDCG@1 <sub>A</sub>	NDCG@10 <sub>A</sub>	NDCG@1 <sub>B</sub>	NDCG@10 <sub>B</sub>	AUC <sub>A</sub>	AUC <sub>B</sub>
GCA[0]	LLM4CDSR	Cloth-Sport	0.7157 $\pm$ 0.0025	0.7821 $\pm$ 0.0018	0.5870 $\pm$ 0.0051	0.6493 $\pm$ 0.002	0.9216 $\pm$ 0.0013	0.8621 $\pm$ 0.0054
	+ GCA <sub>early</sub>		0.7283 $\pm$ 0.0027	0.8052 $\pm$ 0.0014	0.5977 $\pm$ 0.0054	0.6560 $\pm$ 0.0046	0.9364 $\pm$ 0.0009	0.8655 $\pm$ 0.0038
	+ GCA <sub>stack</sub>		0.7310 $\pm$ 0.0012	0.8056 $\pm$ 0.0014	0.6112 $\pm$ 0.0032	0.6638 $\pm$ 0.0038	0.9370 $\pm$ 0.0010	0.8664 $\pm$ 0.0030
GCA[0,1] or GCA[0,2],...	LLM4CDSR	Elec-Phone	0.2101 $\pm$ 0.0030	0.3512 $\pm$ 0.0009	0.1419 $\pm$ 0.0008	0.2608 $\pm$ 0.0010	0.7901 $\pm$ 0.0008	0.7197 $\pm$ 0.0011
	+ GCA <sub>early</sub>		0.2378 $\pm$ 0.0011	0.3815 $\pm$ 0.0018	0.1861 $\pm$ 0.0035	0.2845 $\pm$ 0.0027	0.7970 $\pm$ 0.0018	0.7218 $\pm$ 0.0026
	+ GCA <sub>stack</sub>		0.2410 $\pm$ 0.0012	0.3800 $\pm$ 0.0011	0.1994 $\pm$ 0.0054	0.3035 $\pm$ 0.0049	0.7937 $\pm$ 0.0013	0.7252 $\pm$ 0.0026
	ABXI	Beauty-Elec	0.0730 $\pm$ 0.0070	0.1724 $\pm$ 0.0071	0.0548 $\pm$ 0.0038	0.1273 $\pm$ 0.0028	0.7216 $\pm$ 0.0027	0.7123 $\pm$ 0.0009
	+ GCA <sub>early</sub>		0.0727 $\pm$ 0.0060	0.1793 $\pm$ 0.0047	0.0544 $\pm$ 0.0044	0.1244 $\pm$ 0.0025	0.7410 $\pm$ 0.0025	0.7169 $\pm$ 0.0024
	+ GCA <sub>stack</sub>		0.0733 $\pm$ 0.0042	0.1846 $\pm$ 0.0057	0.0566 $\pm$ 0.0052	0.1271 $\pm$ 0.0042	0.7354 $\pm$ 0.0048	0.6973 $\pm$ 0.0051
	ABXI	Food-Kitch	0.0593 $\pm$ 0.0074	0.1541 $\pm$ 0.0130	0.0416 $\pm$ 0.0058	0.1093 $\pm$ 0.0113	0.7205 $\pm$ 0.0015	0.7180 $\pm$ 0.0032
	+ GCA <sub>early</sub>		0.0703 $\pm$ 0.0094	0.1757 $\pm$ 0.0092	0.0548 $\pm$ 0.0053	0.1327 $\pm$ 0.0072	0.7317 $\pm$ 0.0039	0.7150 $\pm$ 0.0031
	+ GCA <sub>stack</sub>		0.0882 $\pm$ 0.0052	0.1853 $\pm$ 0.0013	0.0527 $\pm$ 0.0020	0.1282 $\pm$ 0.0028	0.7148 $\pm$ 0.0026	0.6924 $\pm$ 0.0009
	CDSRNP	Elec-Phone (1M)	0.0499 $\pm$ 0.0087	0.1170 $\pm$ 0.0079	0.0920 $\pm$ 0.0050	0.1935 $\pm$ 0.0021	-	-
	+ GCA <sub>early</sub>		0.0547 $\pm$ 0.0010	0.1209 $\pm$ 0.0092	0.0980 $\pm$ 0.0010	0.1989 $\pm$ 0.0031	-	-
	+ GCA <sub>stack</sub>		0.0531 $\pm$ 0.0078	0.1229 $\pm$ 0.0125	0.0946 $\pm$ 0.0022	0.1942 $\pm$ 0.0012	-	-

**Table 1** NCDG and AUC comparison with the three baselines and adhoc model with GCA. Elec stands for Electronic, and Kitch stands for Kitchen. GCA<sub>early</sub> denotes GCA[0] and GCA<sub>stack</sub> denotes GCA[0,  $i_1, i_2, \dots, i_N$ ] where  $i_n > 1, n \in [N]$

# 3. Research Question 2 (Main)

## 3.1. Research Question 2



**So far:**

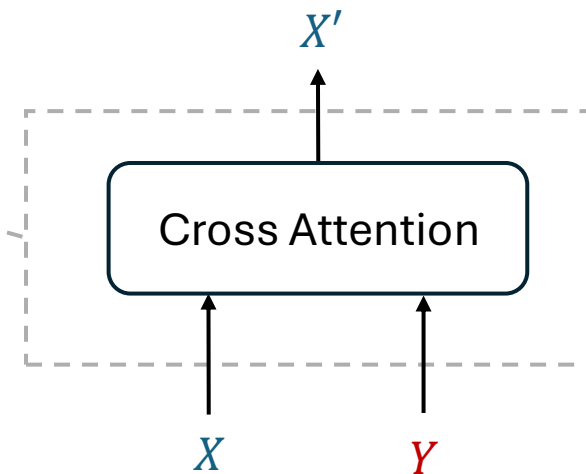
Gated Cross Attention at the early stage can improve performance

**Research Question2:**

Why gated cross attention improve the performance?

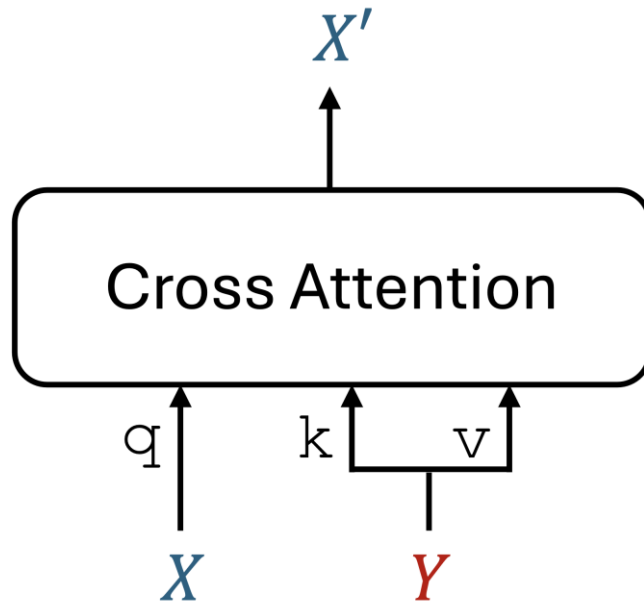
**Observation:**

As training goes by,  $\cos(X, X')$  goes to zero.



### 3. Research Question 2 (Main)

#### 3.2. Previous literature: conventional understanding on cross-attention as residual Alignment



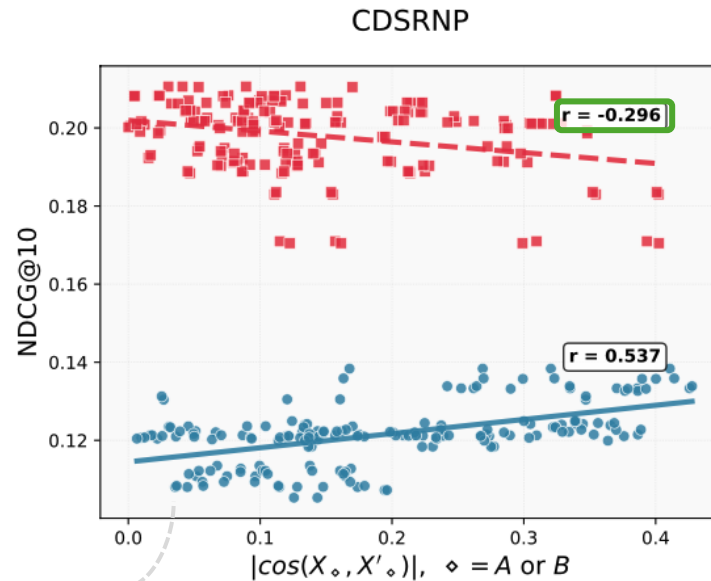
##### *Residual Alignment:*

- $X'$  is generated by removing redundant information from  $X$  and preserving nonredundant information from  $X$  by referring to  $Y$ .
- $X$  : User likes to visit Milan, Italy
- $Y$  : User bought lots of sports players' uniforms
- $X'$  : User may likes to buy AC Millan's uniforms

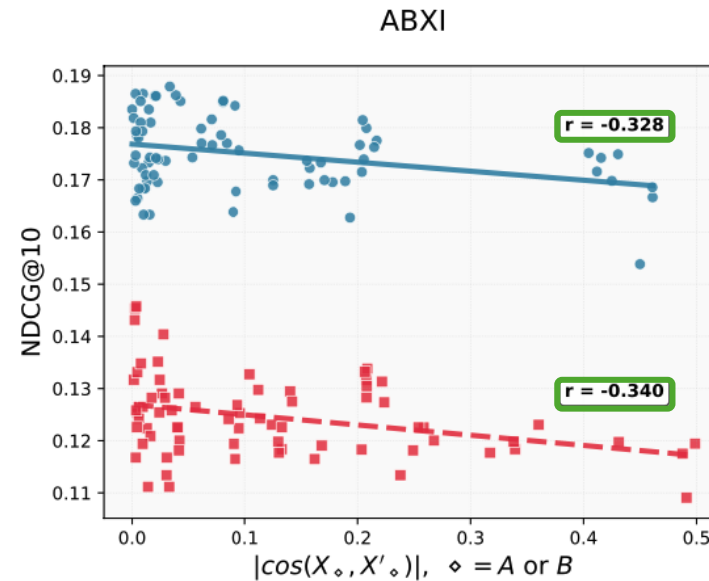
# 3. Research Question 2 (Main)

## 3.3. Observation 2 (Supports main message 1)

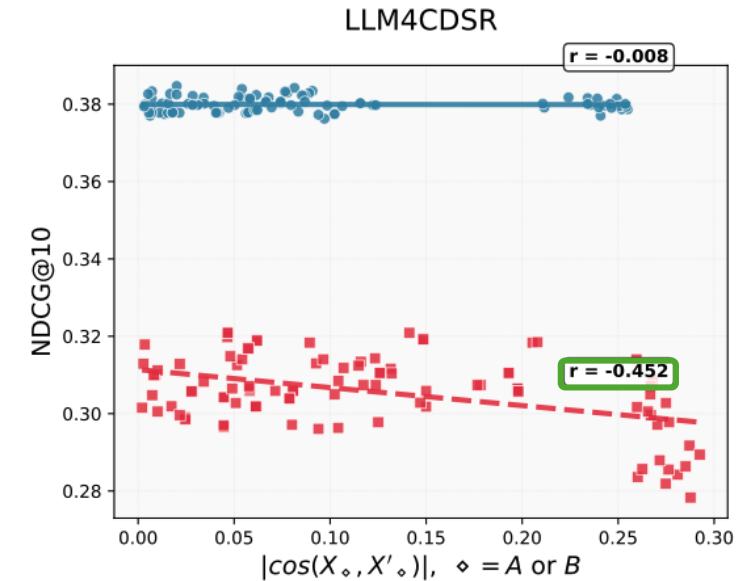
- We observe **negative correlation** between  $\cos(X, X')$  and model performance regardless of dataset and baseline.



(a) CDSRNP



(b) ABXI



(c) LLM4CDSR

Vertical Stacking: {GCA[0], GCA[0,1], GCA[0,2],...}

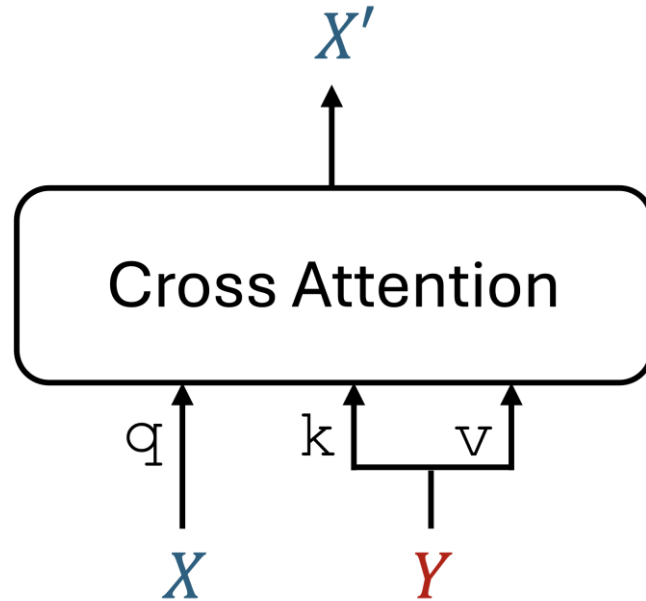
Dataset : {Cloth-sports, Elec-phone, ..}

Hidden dimension: {64, 128, ...}

Num of attention heads: {4, 8, ...}

## 3. Research Question 2 (Main)

### 3.4. Main Message 1



#### Main Message 1

##### ***Orthogonal Alignment:***

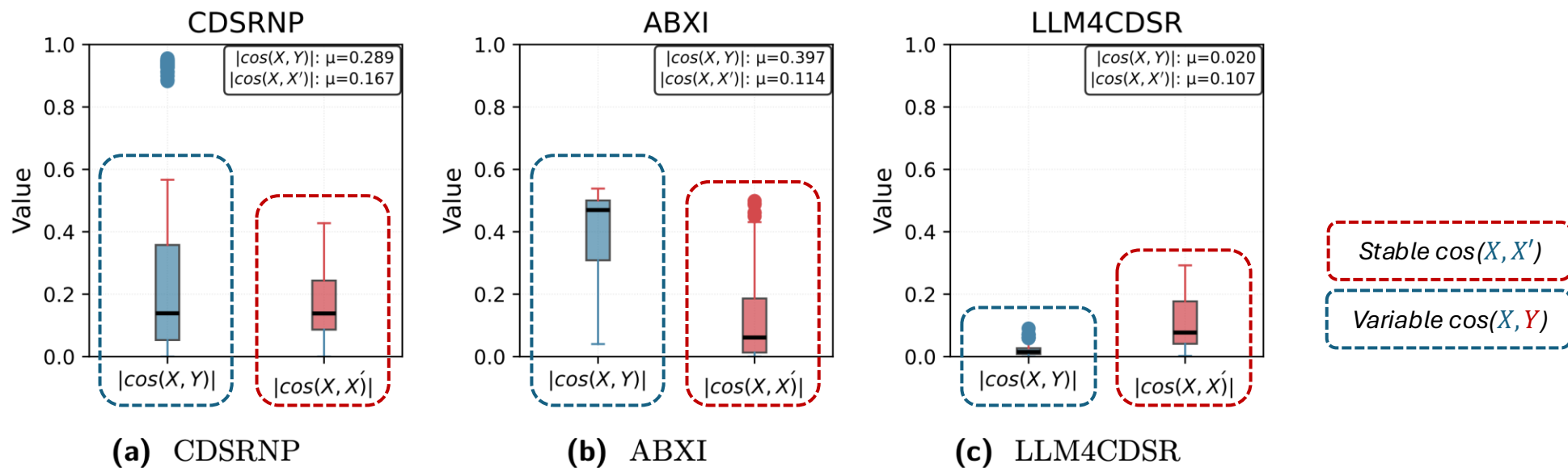
A phenomenon such that as  $X'$  and  $X$  getting orthogonal, then the model performance increases

- $X'$  can be trained to contrain information **irrelevant** to  $X$  by referring to  $Y$ .
  - $X$  : User likes to visit Milan, Italy
  - $Y$  : User bought lots of sports players' uniforms
  - $X'$  : User may likes to visit Manchester, England

## 3. Research Question 2 (Main)

### 3.5. Observation 3 (Supports main message 1)

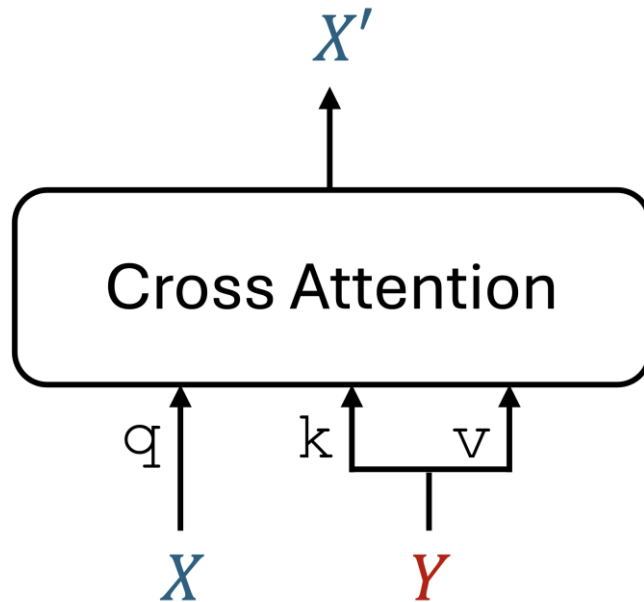
- GCA induces orthogonalization independently of how similar  $X$  and  $Y$  happens to be.



**Figure 8** Boxplots of cosine similarities  $|\cos(X, Y)|$  and  $|\cos(X, X')|$ . While  $|\cos(X, X')|$  remains stable across models (median  $\approx \in [0.1, 0.2]$ ),  $|\cos(X, Y)|$  varies substantially depending on the dataset, highlighting that GCA induces a consistent degree of orthogonalization regardless of underlying  $X$ (query)– $Y$ (key,value) similarity.  $\mu$  represents a median.

## 3. Research Question 2 (Main)

### 3.6. Main Message 2



So far

*Orthogonal Alignment:*

A phenomenon such that as  $X'$  and  $X$  getting orthogonal, then the model performance increases

#### Main Message 2

Orthogonal Alignment ***emerges naturally***, since it improves scaling law

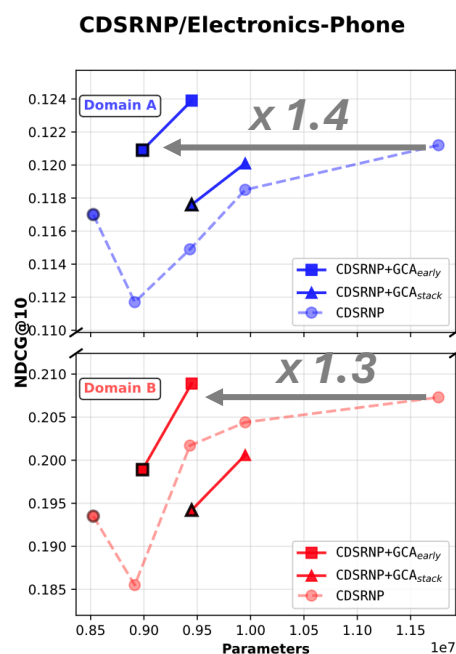
- High level : As an perspective of model, feeding  $X + \alpha X'$  where  $X' \perp X$  is better quality signal than  $X'$  as denoised  $X$ .



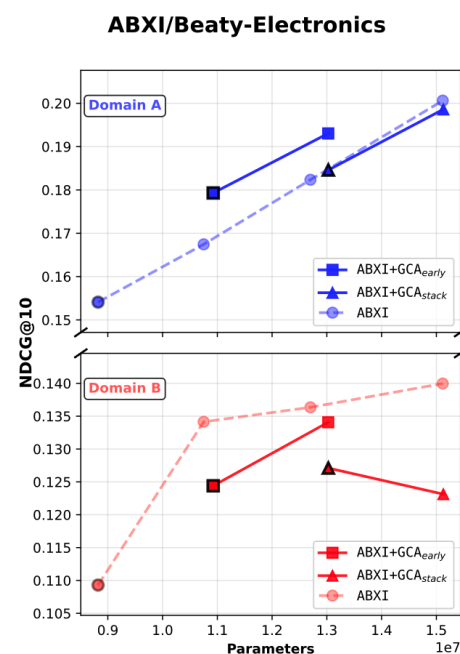
# 3. Research Question 2 (Main)

## 3.7. Observation 4 (Supports main message 2)

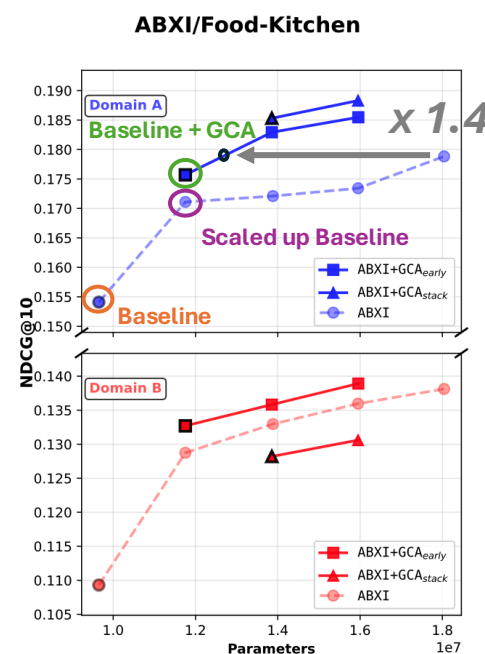
- Ex: Scaled up Baseline (3M) vs. Baseline (2M) + GCA (1M)
- Orthogonal Alignment provides  $\sim x1.4$  parameter efficient scaling up.



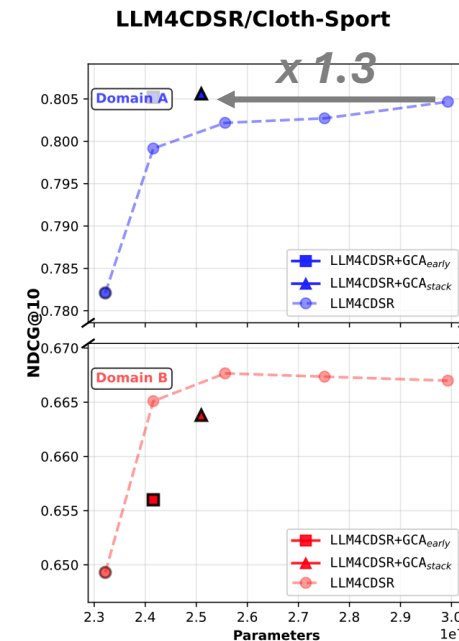
(a) CDSRNP



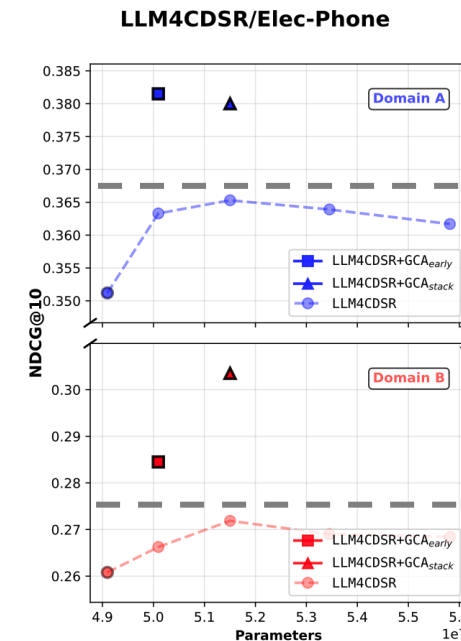
(b) ABXI (Beaty-Elec)



(c) ABXI (Food-Kitch)



(d) LLM4CDSR (Cloth-Sports)



(e) LLM4CDSR (Elec-Phone)

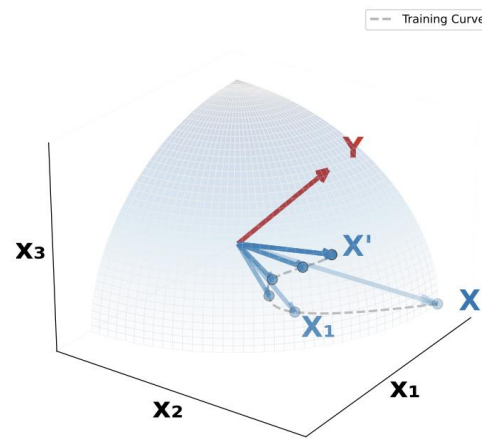
# Summary

**Motivation:** In recommendation models, learning a universal user preference from different modality user behavior data due to some sparse interaction data.

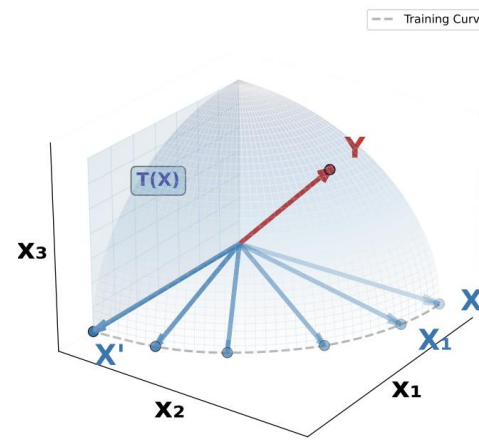
**Research Question:** Cross-attention is widely used mechanism to fuse different modality data, but it's inner mechanism is poorly understood.

## Main Message:

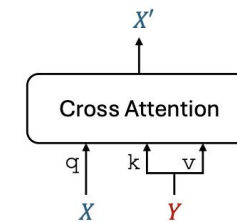
1. Orthogonal Alignment: If input ( $X$ ) and output ( $X'$ ) of cross-attention is getting orthogonal, then performance increases
2. Orthogonal alignment naturally happens since it improves the scaling law.



(a) Residual alignment



(b) Orthogonal alignment



(c) Cross-attention