Program Slicing



What is slicing

Definition: The process that finding all statements in a program that directly or indirectly affect the value of a variable occurrence

```
1 int a = 1;
2 int b = a + 1;
3 assert (a == 2);
4 assert (b == 3);
```

```
1 int a = 1;
2 int b = a + 1;
3 assert (a == 2);
4 assert (b == 3);
```

Input : DCFG, c, v_1 , ..., v_n Output: slice 2 begin > Create working set of pairs of statement instances and used variables $W \leftarrow \{(c, v_1) ... (c, v_n)\}$ while $W \neq \emptyset$ do $(t, v) \leftarrow \text{pick}$ and remove from W slice \leftarrow slice $\cup \{t\}$ $t' \leftarrow$ the instance t is control-dependent on if t' not in slice then ▶ Ensure not processing statements more than once $W \leftarrow W \cup \{(t', v') \mid v' \in use(t')\}\$ 9 \triangleright Add t' to working set with all its used variables $t' \leftarrow$ reaching definition of v at t 10 if t' not in slice then 11 $\mathbf{W} \leftarrow \mathbf{W} \cup \{(t', v') \mid v' \in \mathrm{use}(t)\}$ 12 return slice 13 14 **Procedure** use(t) return all variables used in t

Control Dependencies

```
int m = 1;
2
     int n = 2;
     int p = 4;
3
    int q = m + 2;
5
    if (m == 1) {
6
          p = p - 1;
     assert(p == 4);
```

If	A can alter the program's control and it determines whether B executes
Then	B is control-dependent on A

> 6 is control-dependent on 5

Example statements: <u>if</u> and <u>while</u>

Control-flow Dependencies

```
int m = 1;
     int n = 2;
3
     int p = 4;
    int q = m + 2;
5
    if (m == 1) {
6
          p = p - 1;
     assert(p == 4);
```

If	B is executed immediately after A in the same execution thread
Then	B is control-flow-dependent on A

- 2 is control-flow-dependent on 1
- 3 is control-flow-dependent on 2
- 4 is control-flow-dependent on 3
- **>**

Data-flow Dependencies

```
int m = 1;
     int n = 2;
3
     int p = 4;
    int q = m + 2;
5
     if (m == 1) {
6
           p = p - 1;
     assert(p == 4);
```

If	a). B is control-flow-dependent on A b). v used in B is defined in A and no other statement redefines v between A and B
Then	B is data-flow-dependent on A i.e. dynamic reaching definition of v in B is A

- 4 is data-flow-dependent on 1
 - Dynamic reaching definition of m in 4 is 1
- ➤ 5 is data-flow-dependent on 1
 - Dynamic reaching definition of m in 5 is 1
- ➤ 6 is data-flow-dependent on 3
 - Dynamic reaching definition of p in 6 is 3

Statement & Statement instance

$$S_i = Statement$$

The statement in line i

$$t_{i}^{j}$$
 = Statement instance

jth execution of statement si

```
1 int a = 1;
2 while (a >= 0) {
3 a = a - 1;
4 }
```

$$s_1, s_2, s_3$$

 $t_1^1, t_2^1, t_3^1, t_2^2, t_3^2, t_2^3$

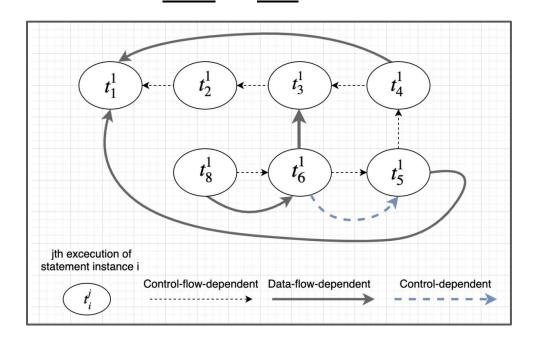
Graphs: DCFG and DDG

DCFG - Dynamic Control-Flow Graph Control-flow Construct Nodes: statement instances dependencies **Edges**: control-flow-dependencies Control **DDG** - Dynamic Dependence Graph dependencies Construct Nodes: statement instances **Edges**: control dependencies or data-flow Data-flow dependencies dependencies

Graph: CDDG

```
int m = 1;
     int n = 2;
3
    int p = 4;
    int q = m + 2;
    if (m == 1) {
6
          p = p - 1;
     assert(p == 4);
```

CDDG - Combined Dynamic Dependence GraphCombination of <u>CDFG</u> and <u>DDG</u>



Input: (c, v)

```
int m = 1;
     int n = 2;
3
     int p = 4;
    int q = m + 2;
    if (m == 1) {
          p = p - 1;
     assert(p == 4);
```

Slicing Criterion - (c, v)

A statement instance and all variables of interest **used** in this statement instance

Examples:
$$(t_4^1, m), (t_5^1, m), (t_6^1, p), (t_8^1, p)$$

```
Input: DCFG, c, v_1, ..., v_n
  Output: slice
2 begin
      ▶ Create
                         int m = 1;
        variable
                         int n = 2;
      3
      while W \neq
                        int p = 4;
           (t, v)
           slice ·
                        int q = m + 2;
           t' \leftarrow
           if t'
                        if (m == 1) {
                                                   nore than once
                         p = p - 1;
9
10
                         assert(p == 4);
11
12
      return slice
13
14 Procedure use(t)
      return all variables used in t
```

instances and used

$$c = t_8^1$$
$$v_1 = p$$

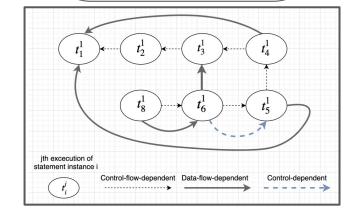
all its used variables

```
1 Input: DCFG, c, v_1, ..., v_n
    Output: slice
 2 begin
         > Create working set of pairs of statement instances and used
           variables
         W \leftarrow \{(c, v_1) ... (c, v_n)\}
 3
         while W \neq \emptyset do
                 v) \leftarrow pick and remove from W
 5
                ce \leftarrow slice \cup \{t\}
                 \leftarrow the instance t is control-dependent on
                 t' not in slice then
                   ▶ Ensure not processing statements more than once
                   W \leftarrow W \cup \{(t', v') \mid v' \in use(t')\}
 9
                            \triangleright Add t' to working set with all its used variables
                 \leftarrow reaching definition of v at t
 10
                 t' not in slice then
 11
                   W \leftarrow W \cup \{(t', v') \mid v' \in use(t)\}
 12
                 slice
         retu
 13
14 Procedu
                use(t)
                 all variables used in t
         retu
```

$$W \leftarrow \{(t_8^1, p)\}$$

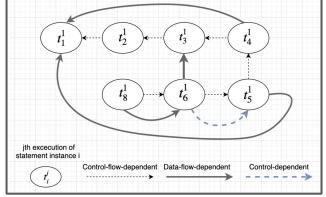
$$slice \leftarrow \{\}$$

```
int m = 1;
     int n = 2;
3
     int p = 4;
     int q = m + 2;
     if (m == 1) {
6
          p = p - 1;
     assert(p == 4);
```



```
1 Input: DCFG, c, v_1, ..., v_n
    Output: slice
 2 begin
         > Create working set of pairs of statement instances and used
            variables
         W \leftarrow \{(c, v_1) ... (c, v_n)\}\
 3
         while W \neq \emptyset do
              (t, v) \leftarrow \text{pick} and remove from W
 5
              slice \leftarrow slice \cup \{t\}
              t' \leftarrow the instance is control-dependent on
              if t' not in slice to
                    ▶ Ensure not cessing statements more than once
                    W \leftarrow W \cup \{(t', | v' \in use(t'))\}
                             \triangleright Add t' to vorking set with all its used variables
               t' \leftarrow reaching definition of at t
10
               if t' not in slice then
11
                   \mathbf{W} \leftarrow \mathbf{W} \cup \{(t', v') \mid v' \in \mathbf{e}(t)\}
12
            turn slice
13
                                                                                 t \leftarrow t_{g}^{1}, v \leftarrow p
14 Pro
            \mathbf{ure} \ \mathsf{use}(t)
            turn all variables used in t
                                                             slice \leftarrow \{t_8^1\}
       W \leftarrow \{\}
```

```
int m = 1;
     int n = 2;
3
     int p = 4;
     int q = m + 2;
     if (m == 1) {
6
          p = p - 1;
     assert(p == 4);
```

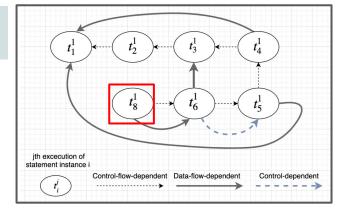


 $W \leftarrow \{\}$

```
1 Input: DCFG, c, v_1, ..., v_n
   Output: slice
 2 begin
        ▶ Create working set of pairs of statement instances and used
           variables
                                                    t' is empty (intra-method slicing)
        W \leftarrow \{(c, v_1) \dots (c, v_n)\}\
 3
                                                    Note: t' is the method containing t
        while W \neq \emptyset do
             (t, v) \leftarrow \text{pick} and remove from W in inter-method slicing
             slice \leftarrow slice \cup \{t\}
             t' \leftarrow the instance t is control-dependent on
 7
             if t' not in slice then
                  ▶ Ensure not processing statements more than once
                  W \leftarrow W \cup \{(t', v') \mid v' \in use(t')\}
 9
                           \triangleright Add t' to working set with all its used variables
             t' \leftarrow reaching definition of v at t
10
             if t' not in slice then
11
                  W \leftarrow W \cup \{(t', v') \mid v' \in use(t)\}
12
        return slice
13
                                                                          t \leftarrow t_{g}^{1}, v \leftarrow p
14 Procedure use(t)
        return all variables used in t
```

$$slice \leftarrow \{t_8^1\}$$

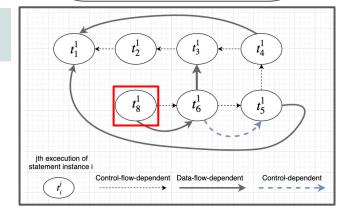
```
int m = 1;
     int n = 2;
3
     int p = 4;
     int q = m + 2;
     if (m == 1) {
          p = p - 1;
6
     assert(p == 4);
```



```
1 Input: DCFG, c, v_1, ..., v_n
    Output: slice
 2 begin
         ▶ Create working set of pairs of statement instances and used
           variables
         W \leftarrow \{(c, v_1) ... (c, v_n)\}\
 3
         while W \neq \emptyset do
              (t, v) \leftarrow \text{pick} and remove from W
 5
               slice \leftarrow slice \cup \{t\}
 6
              t' \leftarrow the instance t is control-dependent on
 7
              if t' not in slice then
                    ▶ Ensure not processing statements more than once
                    W \leftarrow W \cup \{(t', v') \mid v' \in use(t')\}
 9
                             \triangleright Add t' to working set with all its used variables
              t' \leftarrow reaching definition of v at t
10
              if t' not in slice then
                                                                   t' \leftarrow t_6^1
11
                   W \leftarrow W \cup \{(t', v') \mid v' \in use(t)\}
12
         return slice
13
                                                                               t \leftarrow t_{g}^{1}, v \leftarrow p
14 Procedure use(t)
         return all variables used in t
```

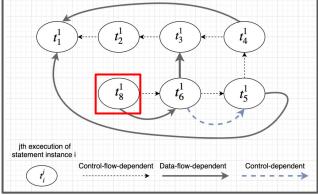
$$W \leftarrow \{\}$$
 $slice \leftarrow \{t_8^1\}$

```
int m = 1;
     int n = 2;
3
     int p = 4;
     int q = m + 2;
     if (m == 1) {
          p = p - 1;
6
     assert(p == 4);
```



```
1 Input: DCFG, c, v_1, ..., v_n
    Output: slice
 2 begin
         > Create working set of pairs of statement instances and used
           variables
         W \leftarrow \{(c, v_1) ... (c, v_n)\}\
 3
         while W \neq \emptyset do
              (t, v) \leftarrow \text{pick} and remove from W
              slice \leftarrow slice \cup \{t\}
              t' \leftarrow the instance t is control-dependent on
 7
              if t' not in slice then
                   ▶ Ensure not processing statements more than once
                    W \leftarrow W \cup \{(t', v') \mid v' \in use(t')\}
 9
                             \triangleright Add t' to working set with all its used variables
              t' \leftarrow reaching definition of v at t
10
                                                                 t' \leftarrow t_6^1
              if t' not in slice then
11
                    W \leftarrow W \cup \{(t', v') \mid v' \in use(t)\}
12
         return slice
13
                                                                               t \leftarrow t_{g}^{1}, v \leftarrow p
14 Procedure use(t)
         return all variables used in t
                                                         slice \leftarrow \{t_8^1\}
      W \leftarrow \{\}
```

```
int m = 1;
     int n = 2;
3
     int p = 4;
     int q = m + 2;
     if (m == 1) {
          p = p - 1;
6
     assert(p == 4);
```

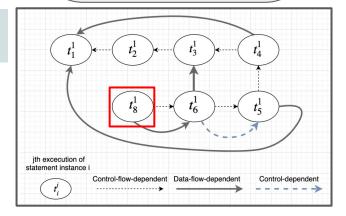


 $W \leftarrow \{(t_6^1, p)\}$

```
1 Input: DCFG, c, v_1, ..., v_n
    Output: slice
 2 begin
         ▶ Create working set of pairs of statement instances and used
           variables
         W \leftarrow \{(c, v_1) ... (c, v_n)\}\
 3
         while W \neq \emptyset do
              (t, v) \leftarrow \text{pick} and remove from W
              slice \leftarrow slice \cup \{t\}
              t' \leftarrow the instance t is control-dependent on
 7
              if t' not in slice then
                   ▶ Ensure not processing statements more than once
                    W \leftarrow W \cup \{(t', v') \mid v' \in use(t')\}
 9
                             \triangleright Add t' to working set with all its used variables
              t' \leftarrow reaching definition of v at t
10
              if t' not in slice then
11
                    W \leftarrow W \cup \{(t', v') \mid v' \in use(t)\}
12
         return slic
13
                                                                               t \leftarrow t_{g}^{1}, v \leftarrow p
14 Procedure use
                        riables used in t
         return all
```

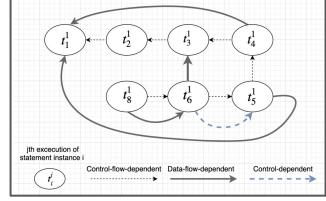
 $slice \leftarrow \{t_8^1\}$

```
int m = 1;
     int n = 2;
3
     int p = 4;
     int q = m + 2;
     if (m == 1) {
6
          p = p - 1;
     assert(p == 4);
```



```
1 Input : DCFG, c, v_1, ..., v_n
    Output: slice
 2 begin
         > Create working set of pairs of statement instances and used
           variables
         W \leftarrow \{(c, v_1) ... (c, v_n)\}\
 3
         while W \neq \emptyset do
              (t, v) \leftarrow \text{pick} and remove from W
 5
              slice \leftarrow slice \cup \{t\}
              t' \leftarrow the instance t is control-dependent on
              if t' not in slice en
                    ▶ Ensure no rocessing statements more than once
                    W \leftarrow W \cup \{(t \quad ') \mid v' \in use(t')\}
                             \triangleright Add t working set with all its used variables
              t' \leftarrow reaching definition v at t
10
              if t' not in slice then
11
                   W \leftarrow W \cup \{(t', v') \mid v \quad use(t)\}
12
            turn slice
13
                                                                              t \leftarrow t_6^1, v \leftarrow p
14 Pro
            \mathbf{ure} \ \mathsf{use}(t)
            turn all variables used in t
                                                             slice \leftarrow \{t_8^1, t_6^1\}
        W \leftarrow \{\}
```

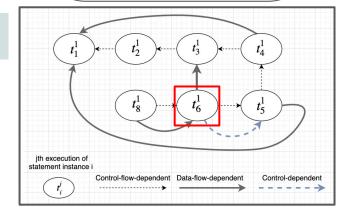
```
int m = 1;
     int n = 2;
3
     int p = 4;
     int q = m + 2;
     if (m == 1) {
6
          p = p - 1;
     assert(p == 4);
```



```
1 Input: DCFG, c, v_1, ..., v_n
    Output: slice
 2 begin
         ▶ Create working set of pairs of statement instances and used
            variables
         W \leftarrow \{(c, v_1) ... (c, v_n)\}\
 3
         while W \neq \emptyset do
                                                                            t' \leftarrow t_5^1
               (t, v) \leftarrow \text{pick} and remove from W
 5
              slice \leftarrow slice \cup \{t\}
 6
               t' \leftarrow the instance t is control-dependent on
 7
               if t' not in slice then
 8
                    ▶ Ensure not processing statements more than once
                    W \leftarrow W \cup \{(t', v') \mid v' \in use(t')\}
 9
                             \triangleright Add t' to working set with all its used variables
               t' \leftarrow reaching definition of v at t
 10
               if t' not in slice then
11
                   W \leftarrow W \cup \{(t', v') \mid v' \in use(t)\}
 12
         return slice
 13
                                                                              t \leftarrow t_6^1, v \leftarrow p
14 Procedure use(t)
         return all variables used in t
```

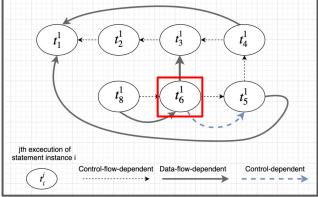
$$W \leftarrow \{\} \qquad \qquad slice \leftarrow \{t_8^1, t_6^1\}$$

```
int m = 1;
     int n = 2;
3
     int p = 4;
     int q = m + 2;
     if (m == 1) {
6
          p = p - 1;
     assert(p == 4);
```



```
1 Input: DCFG, c, v_1, ..., v_n
    Output: slice
 2 begin
         > Create working set of pairs of statement instances and used
            variables
         W \leftarrow \{(c, v_1) ... (c, v_n)\}\
 3
         while W \neq \emptyset do
                                                                        t' \leftarrow t_5^1
               (t, v) \leftarrow \text{pick} and remove from W
 5
               slice \leftarrow slice \cup \{t\}
 6
               t' \leftarrow the instance t is control-dependent on
 7
               if t' not in slice then
 8
                    ▶ Ensure not processing statements more than once
                    W \leftarrow W \cup \{(t', v') \mid v' \in use(t')\}
 9
                             \triangleright Add t' to working set with all its used variables
               t' \leftarrow reaching definition of
10
               if t' not in slice then
11
                    \mathbf{W} \leftarrow \mathbf{W} \cup \{(t', v') \mid v' \in \mathbf{U}(t)\}\
12
         return slice
13
                                                                                t \leftarrow t_6^1, v \leftarrow p
14 Procedure use(t)
         return all variables used in t
                                                              slice \leftarrow \{t_8^1, t_6^1\}
     W \leftarrow \{\}
```

```
int m = 1;
     int n = 2;
3
     int p = 4;
     int q = m + 2;
     if (m == 1) {
          p = p - 1;
     assert(p == 4);
```

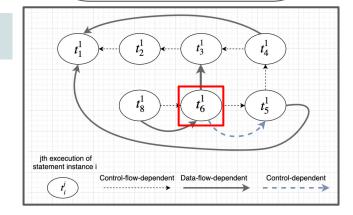


```
1 Input: DCFG, c, v_1, ..., v_n
    Output: slice
 2 begin
          > Create working set of pairs of statement instances and used
            variables
          W \leftarrow \{(c, v_1) ... (c, v_n)\}\
 3
         while W \neq \emptyset do
               (t, v) \leftarrow \text{pick} and remove from W
 5
               slice \leftarrow slice \cup \{t\}
 6
               t' \leftarrow the instance t is control-dependent on
 7
               if t' not in slice then
 8
                    ▶ Ensure not processing statements more than once
                    W \leftarrow W \cup \{(t', v') \mid v' \in use(t')\}
 9
                              \triangleright Add t' to working set with all its used variables
               t' \leftarrow reaching definition of v at t
 10
                      t in slice then
 11
                        \leftarrow \mathbf{W} \cup \{(t', v') \mid v' \in \mathbf{use}(t)\}
 12
          return sl
 13
                                                                                t \leftarrow t_6^1, v \leftarrow p
14 Procedure us
                       ariables used in t
         return al
```

$$W \leftarrow \{(t_5^1, m)\}$$

$$slice \leftarrow \{t_8^1, t_6^1\}$$

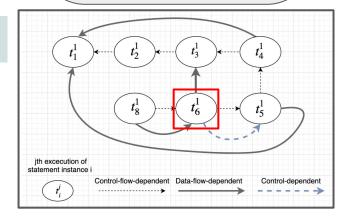
```
int m = 1;
     int n = 2;
3
     int p = 4;
     int q = m + 2;
     if (m == 1) {
6
          p = p - 1;
     assert(p == 4);
```



```
1 Input: DCFG, c, v_1, ..., v_n
    Output: slice
 2 begin
         > Create working set of pairs of statement instances and used
           variables
         W \leftarrow \{(c, v_1) ... (c, v_n)\}\
 3
         while W \neq \emptyset do
              (t, v) \leftarrow \text{pick} and remove from W
              slice \leftarrow slice \cup \{t\}
              t' \leftarrow the instance t is control-dependent on
 7
              if t' not in slice then
                   ▶ Ensure not processing statements more than once
                    W \leftarrow W \cup \{(t', v') \mid v' \in use(t')\}
 9
                             \triangleright Add t' to working set with all its used variables
              t' \leftarrow reaching definition of v at t
10
              if t' not in slice then
11
                    W \leftarrow W \cup \{(t', v') \mid v' \in use(t)\}
12
         return slice
13
                                                                              t \leftarrow t_6^1, v \leftarrow p
14 Procedure us
                      ariables used in t
         return al
```

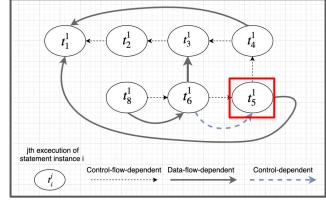
$$W \leftarrow \{(t_5^1, m), (t_3^1, p)\}$$
 $slice \leftarrow \{t_8^1, t_6^1\}$

```
int m = 1;
     int n = 2;
3
     int p = 4;
     int q = m + 2;
     if (m == 1) {
6
          p = p - 1;
     assert(p == 4);
```



```
1 Input: DCFG, c, v_1, ..., v_n
    Output: slice
 2 begin
         > Create working set of pairs of statement instances and used
            variables
         W \leftarrow \{(c, v_1) ... (c, v_n)\}\
 3
         while W \neq \emptyset do
              (t, v) \leftarrow \text{pick} and remove from W
 5
              slice \leftarrow slice \cup \{t\}
              t' \leftarrow the instance t is control-dependent on
              if t' not in slice en
                    ▶ Ensure no rocessing statements more than once
                    W \leftarrow W \cup \{(t \quad ') \mid v' \in use(t')\}
                              \triangleright Add t working set with all its used variables
               t' \leftarrow \text{reaching definition} \quad v \text{ at } t
10
               if t' not in slice then
11
                    W \leftarrow W \cup \{(t', v') \mid v \quad use(t)\}
12
            turn slice
13
                                                                                 t \leftarrow t_{5}^{1}, v \leftarrow m
14 Pro
            \mathbf{ure} \ \mathsf{use}(t)
            turn all variables used in t
                                                             slice \leftarrow \{t_8^1, t_6^1, t_5^1\}
    W \leftarrow \{(t_3^1, p)\}
```

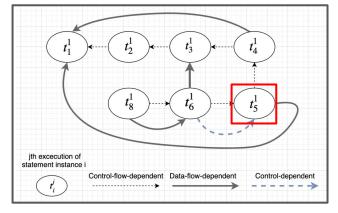
```
int m = 1;
     int n = 2;
3
     int p = 4;
     int q = m + 2;
    if (m == 1) {
          p = p - 1;
     assert(p == 4);
```



```
1 Input: DCFG, c, v_1, ..., v_n
   Output: slice
 2 begin
        > Create working set of pairs of statement instances and used
           variables
                                                    t' is empty (intra-method slicing)
        W \leftarrow \{(c, v_1) \dots (c, v_n)\}
 3
                                                    Note: t' is the method containing
        while W \neq \emptyset do
             (t, v) \leftarrow \text{pick} and remove from W t in inter-method slicing
             slice \leftarrow slice \cup \{t\}
             t' \leftarrow the instance t is control-dependent on
 7
             if t' not in slice then
                  ▶ Ensure not processing statements more than once
                  W \leftarrow W \cup \{(t', v') \mid v' \in use(t')\}
 9
                           \triangleright Add t' to working set with all its used variables
             t' \leftarrow reaching definition of v at t
10
             if t' not in slice then
11
                  W \leftarrow W \cup \{(t', v') \mid v' \in use(t)\}
12
        return slice
13
                                                                          t \leftarrow t_{5}^{1}, v \leftarrow m
14 Procedure use(t)
        return all variables used in t
```

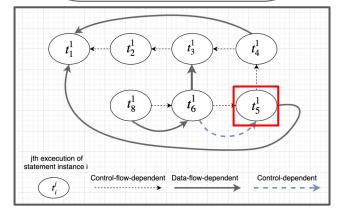
```
W \leftarrow \{(t_3^1, p)\} slice \leftarrow \{t_8^1, t_6^1, t_5^1\}
```

```
int m = 1;
     int n = 2;
3
     int p = 4;
     int q = m + 2;
     if (m == 1) {
          p = p - 1;
     assert(p == 4);
```



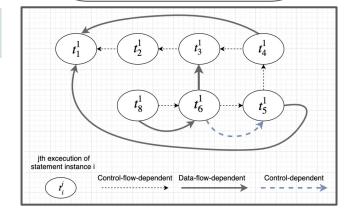
```
1 Input: DCFG, c, v_1, ..., v_n
    Output: slice
 2 begin
         > Create working set of pairs of statement instances and used
           variables
         W \leftarrow \{(c, v_1) ... (c, v_n)\}\
 3
         while W \neq \emptyset do
              (t, v) \leftarrow \text{pick} and remove from W
              slice \leftarrow slice \cup \{t\}
              t' \leftarrow the instance t is control-dependent on
 7
              if t' not in slice then
                   ▶ Ensure not processing statements more than once
                   W \leftarrow W \cup \{(t', v') \mid v' \in use(t')\}
 9
                            \triangleright Add t' to working set with all its used variables
              t' \leftarrow reaching definition of v at t
10
              if t' not in slice then
11
                   W \leftarrow W \cup \{(t', v') \mid v' \in use(t)\}
12
         return sl
13
                                                                             t \leftarrow t_{5}^{1}, v \leftarrow m
14 Procedure us
                      ariables used in t
         return al
     W \leftarrow \{(t_3^1, p), (t_1^1, m)\} slice \leftarrow \{t_8^1, t_6^1, t_5^1\}
```

```
int m = 1;
     int n = 2;
3
     int p = 4;
     int q = m + 2;
    if (m == 1) {
          p = p - 1;
     assert(p == 4);
```



```
1 Input: DCFG, c, v_1, ..., v_n
    Output: slice
 2 begin
         > Create working set of pairs of statement instances and used
           variables
         W \leftarrow \{(c, v_1) ... (c, v_n)\}\
 3
         while W \neq \emptyset do
              (t, v) \leftarrow \text{pick} and remove from W
              slice \leftarrow slice \cup \{t\}
              t' \leftarrow the instance t is control-dependent on
              if t' not in slice en
                    ▶ Ensure no rocessing statements more than once
                    W \leftarrow W \cup \{(t \quad ') \mid v' \in use(t')\}
                             \triangleright Add t working set with all its used variables
              t' \leftarrow reaching definition v at t
10
              if t' not in slice then
11
                   W \leftarrow W \cup \{(t', v') \mid v \quad use(t)\}
12
            turn slice
13
                                                                               t \leftarrow t_3^1, v \leftarrow p
14 Pro
            \mathbf{ure} \ \mathsf{use}(t)
            turn all variables used in t
15
     W \leftarrow \{(t_1^1, m)\}
                                                       slice \leftarrow \{t_8^1, t_6^1, t_5^1, t_3^1\}
```

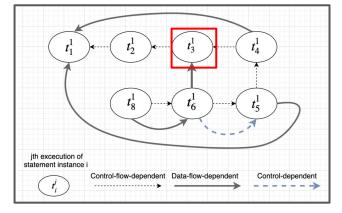
```
int m = 1;
int n = 2;
int p = 4;
int q = m + 2;
if (m == 1) {
     p = p - 1;
assert(p == 4);
```



```
1 Input: DCFG, c, v_1, ..., v_n
   Output: slice
 2 begin
        > Create working set of pairs of statement instances and used
          variables
                                                   t' is empty (intra-method slicing)
        W \leftarrow \{(c, v_1) \dots (c, v_n)\}\
 3
                                                   Note: t' is the method containing
        while W \neq \emptyset do
             (t, v) \leftarrow \text{pick} and remove from W t in inter-method slicing
             slice \leftarrow slice \cup \{t\}
             t' \leftarrow the instance t is control-dependent on
 7
             if t' not in slice then
                  ▶ Ensure not processing statements more than once
                  W \leftarrow W \cup \{(t', v') \mid v' \in use(t')\}
 9
                          \triangleright Add t' to working set with all its used variables
             t' \leftarrow reaching definition of v at t
                                                     t' is empty in this case
10
             if t' not in slice then
11
                  W \leftarrow W \cup \{(t', v') \mid v' \in use(t)\}
12
        return slice
13
                                                                        t \leftarrow t_3^1, v \leftarrow p
14 Procedure use(t)
        return all variables used in t
```

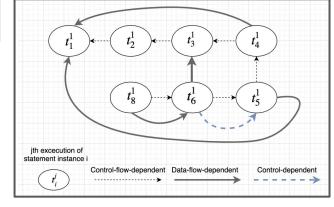
```
W \leftarrow \{(t_1^1, m)\} slice \leftarrow \{t_8^1, t_6^1, t_5^1, t_3^1\}
```

```
int m = 1;
int n = 2;
int p = 4;
int q = m + 2;
if (m == 1) {
     p = p - 1;
assert(p == 4);
```



```
1 Input: DCFG, c, v_1, ..., v_n
    Output: slice
 2 begin
         > Create working set of pairs of statement instances and used
            variables
         W \leftarrow \{(c, v_1) ... (c, v_n)\}\
 3
         while W \neq \emptyset do
              (t, v) \leftarrow \text{pick} and remove from W
 5
              slice \leftarrow slice \cup \{t\}
              t' \leftarrow the instance t is control-dependent on
              if t' not in slice en
                    ▶ Ensure no rocessing statements more than once
                    W \leftarrow W \cup \{(t \quad ') \mid v' \in use(t')\}
                             \triangleright Add t working set with all its used variables
               t' \leftarrow \text{reaching definition} \quad v \text{ at } t
10
               if t' not in slice then
11
                   W \leftarrow W \cup \{(t', v') \mid v \quad use(t)\}
12
            turn slice
13
                                                                               t \leftarrow t_1^1, v \leftarrow m
14 Pro
            \mathbf{ure} \ \mathsf{use}(t)
            turn all variables used in t
15
                                         slice \leftarrow \{t_8^1, t_6^1, t_5^1, t_3^1, t_1^1\}
      W \leftarrow \{\}
```

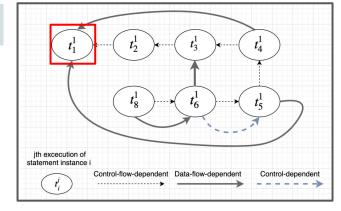
```
int m = 1;
int n = 2;
int p = 4;
int q = m + 2;
if (m == 1) {
     p = p - 1;
assert(p == 4);
```



```
1 Input: DCFG, c, v_1, ..., v_n
   Output: slice
 2 begin
        ▶ Create working set of pairs of statement instances and used
          variables
                                                   t' is empty (intra-method slicing)
        W \leftarrow \{(c, v_1) \dots (c, v_n)\}\
 3
                                                   Note: t' is the method containing
        while W \neq \emptyset do
             (t, v) \leftarrow \text{pick} and remove from W t in inter-method slicing
             slice \leftarrow slice \cup \{t\}
             t' \leftarrow the instance t is control-dependent on
 7
             if t' not in slice then
                  ▶ Ensure not processing statements more than once
                  W \leftarrow W \cup \{(t', v') \mid v' \in use(t')\}
 9
                          \triangleright Add t' to working set with all its used variables
             t' \leftarrow reaching definition of v at t
                                                     t' is empty in this case
10
             if t' not in slice then
11
                 W \leftarrow W \cup \{(t', v') \mid v' \in use(t)\}
12
        return slice
13
                                                                       t \leftarrow t_1^1, v \leftarrow m
14 Procedure use(t)
        return all variables used in t
```

```
W \leftarrow \{\} \qquad slice \leftarrow \{t_8^1, \ t_6^1, \ t_5^1, \ t_3^1, \ t_1^1\}
```

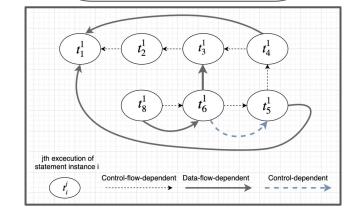
```
int m = 1;
int n = 2;
int p = 4;
int q = m + 2;
if (m == 1) {
     p = p - 1;
assert(p == 4);
```



```
1 Input: DCFG, c, v_1, ..., v_n
    Output: slice
 2 begin
         > Create working set of pairs of statement instances and used
           variables
         W \leftarrow \{(c, v_1) ... (c, v_n)\}\
 3
         while W \neq \emptyset do
              (t, v) \leftarrow \text{pick} and remove from W
 5
              slice \leftarrow slice \cup \{t\}
 6
              t' \leftarrow the instance t is control-dependent on
 7
              if t' not in slice then
                   ▶ Ensure not processing statements more than once
                   W \leftarrow W \cup \{(t', v') \mid v' \in use(t')\}
 9
                            \triangleright Add t' to working set with all its used variables
              t' \leftarrow reaching definition of v at t
10
              if t' not in slice then
11
                   W \leftarrow W \cup \{(t', v') \mid v' \in use(t)\}
12
         return slice
13
14 Procedure use(t)
         return all variables used in t
```

```
W \leftarrow \{\}  slice \leftarrow \{t_8^1, t_6^1, t_5^1, t_3^1, t_1^1\}
```

```
int m = 1;
int n = 2;
int p = 4;
int q = m + 2;
if (m == 1) {
     p = p - 1;
assert(p == 4);
```



References

H. Agrawal and J. R. Horgan, "Dynamic Program Slicing," ACM SIGPLAN Notices, vol. 25, no. 6, pp. 246–256, 1990.

Khaled Ahmed, Mieszko Lis, and Julia Rubin. MANDOLINE: Dynamic Slicing of Android Applications with Trace-Based Alias Analysis. IEEE International Conference on Software Testing, Verification and Validation (ICST), Distinguished Paper Award, 2021 (28% acceptance rate).

Khaled Ahmed, Mieszko Lis, and Julia Rubin. Slicer4J: A Dynamic Slicer for Java. ACM Joint European Software Engineering Conference and Symposium on the Foundations of Software Engineering (ESEC/FSE), tools track, 2021.