

# ***Principles of Program Analysis***

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# ***Agenda***

- Basics of Analysis
  - Control flow
  - Call graph
  - Data Flow Analysis
  - Symbolic Execution
- Presentation Tips

# ***Program Analysis: Reasoning About Code***

- The process of automatically analyzing the behavior of programs
- Examples?

# ***Major Application Areas***

- Program correctness:
  - code inspection, style checkers, security threats, validation of correctness, robustness
- Program optimization:
  - improving the program's performance while reducing its resource usage
- Program understanding, validation, and repair
  - explaining code, identifying and automatically fixing error

# *Types of Analysis*

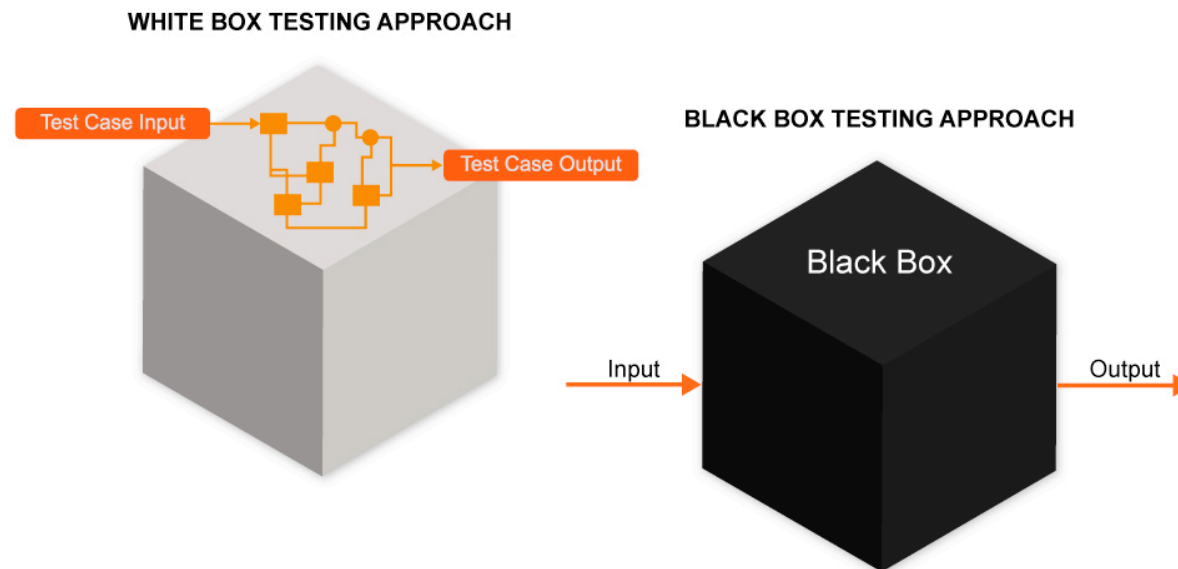
	Static Analysis (without running the code)	Dynamic Analysis (at runtime)
White Box (code internals)	<ul style="list-style-type: none"><li>– Checking that each method has a comment</li><li>– Style checks</li><li>– Symbolic execution</li><li>– Model checking</li></ul>	<ul style="list-style-type: none"><li>– Unit testing</li><li>– Mock testing</li><li>– Debugging</li></ul>
Black Box (input-output)	<ul style="list-style-type: none"><li>– Counting lines of code for a method</li><li>– Checking that each called method is defined</li><li>– Null dereference (security checks)</li><li>– Tracking data flows ...</li></ul>	<ul style="list-style-type: none"><li>– Integration testing</li><li>– User acceptance testing</li><li>– Profiling</li><li>– Monitoring</li></ul>

# *Types of Analysis*

	Static Analysis (without running the code)	Dynamic Analysis (at runtime)
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# ***White-Box Analysis***

Based on internal paths, code structures, and implementation of the software



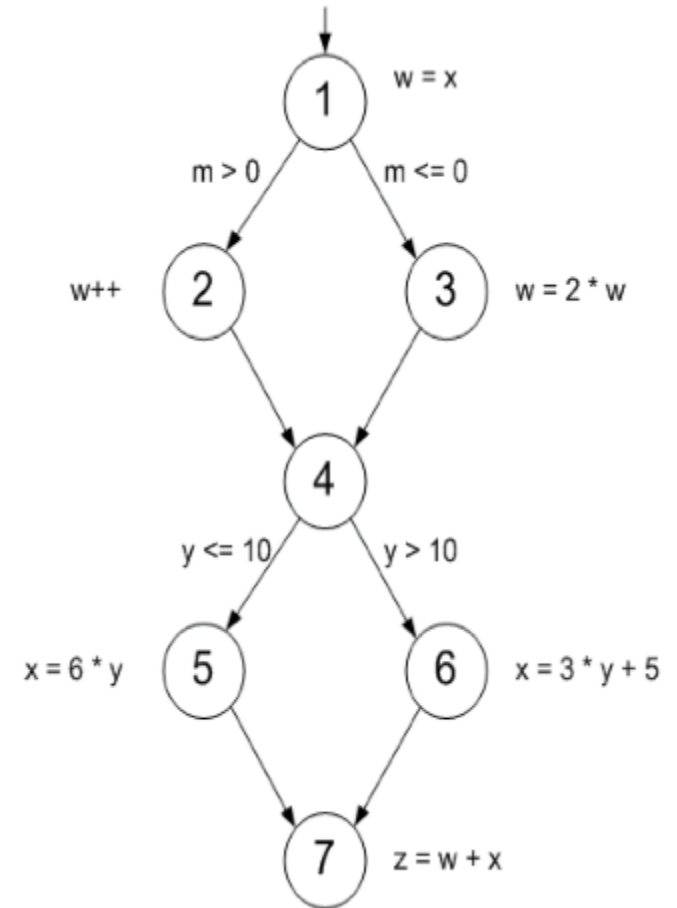
# ***Analysis Primitives***



# Modeling Software

Graphs! E.g.,

- abstract syntax graphs
- control flow graphs
- call graphs
- reachability graphs
- ...

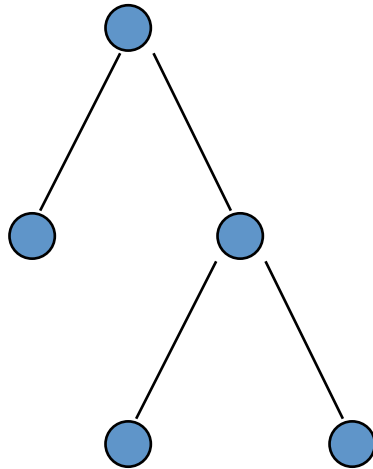


# Graphs

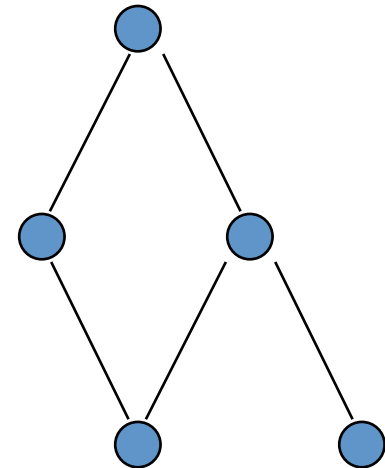
- A **graph**,  $G = (N, E)$ , is an ordered pair consisting of
  - a set of nodes  $N$
  - a set of edges  $E = \{(n_i, n_j)\}$
  - if the pairs in  $E$  are ordered, then  $G$  is called a *directed graph*
  - if not, it is called an *undirected graph*

# Graphs and Trees

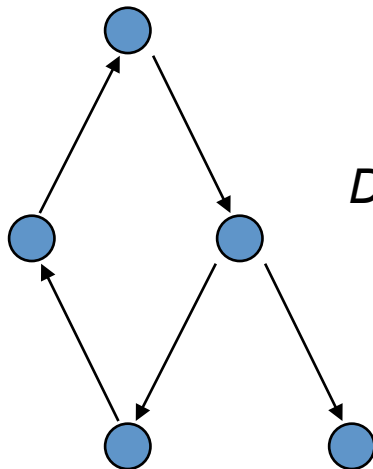
*tree  
(acyclic graph)*



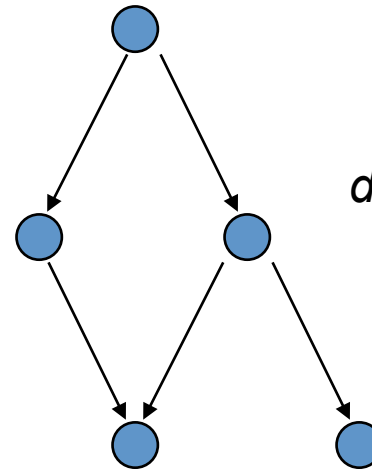
*cyclic undirected  
graph*



*Directed cyclic  
graph*

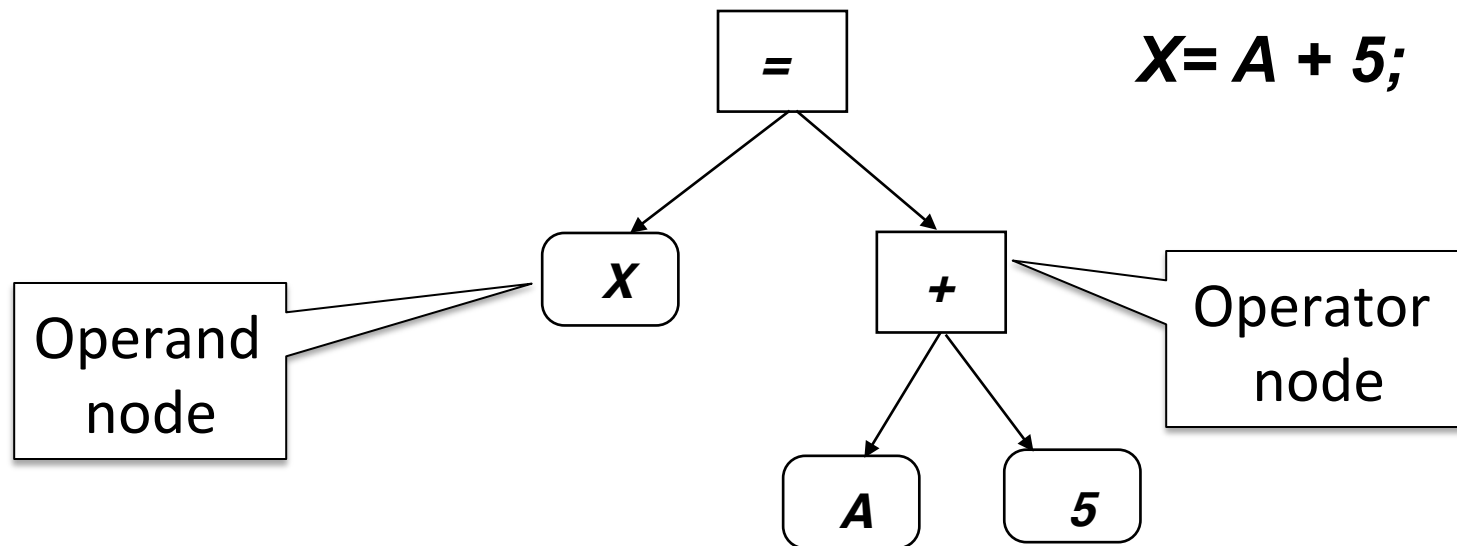


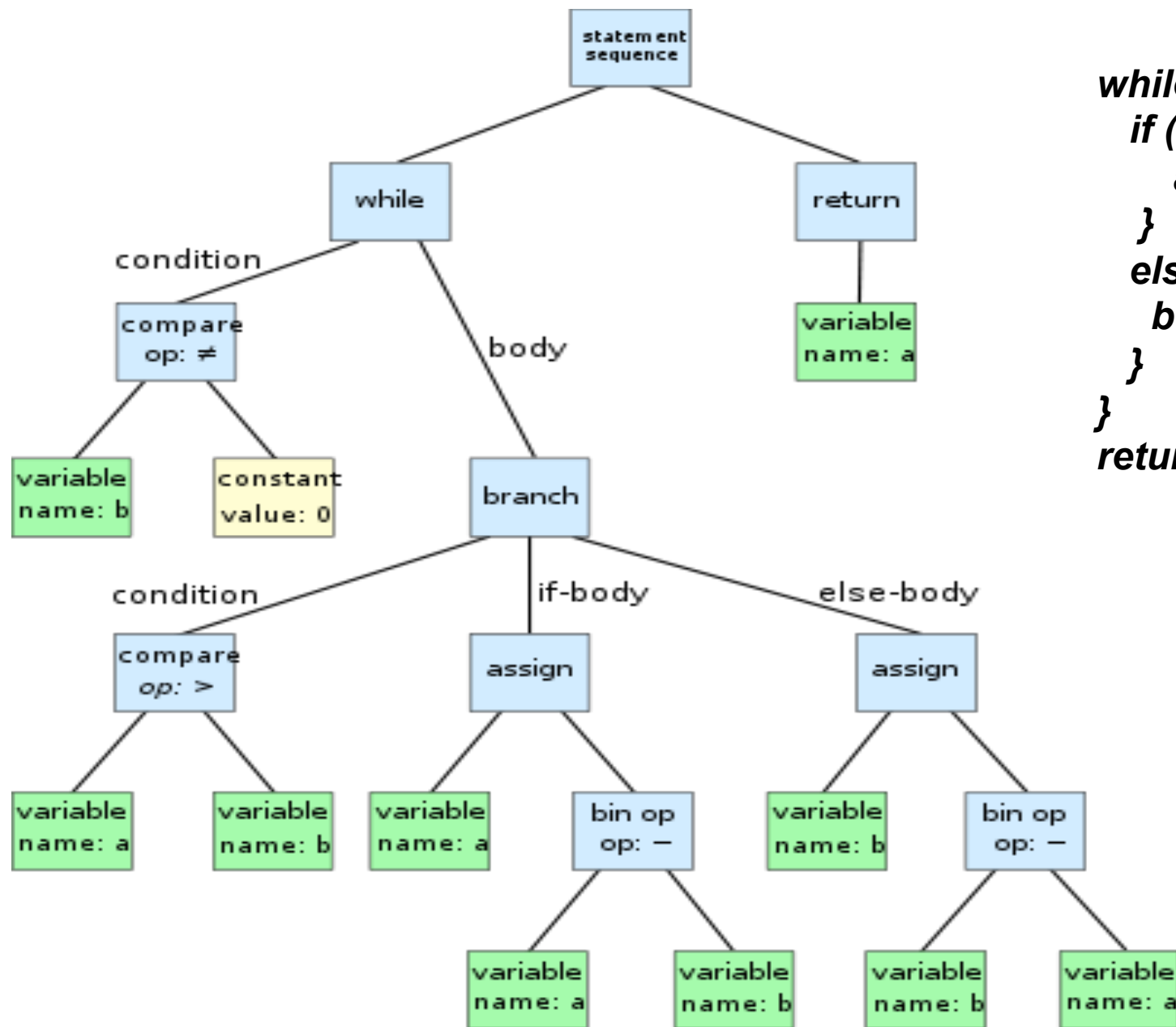
*directed acyclic  
graph (DAG)*



# ***Abstract Syntax Tree (AST)***

- A common form for representing expressions and program statements
- Two kinds of nodes: operator and operands
  - operator applied to N operands
- Each node denotes a construct occurring in the source code





```

while (b!=0) {
    if (a > b) {
        a = a - b;
    }
    else {
        b = b - a;
    }
}
return a;

```

# Control Flow Graph (CFG) – Example

*total, value, count, maximum : int;*

*total := 0;*

*count := 1;*

*read maximum;*

*while (count <= maximum) do*

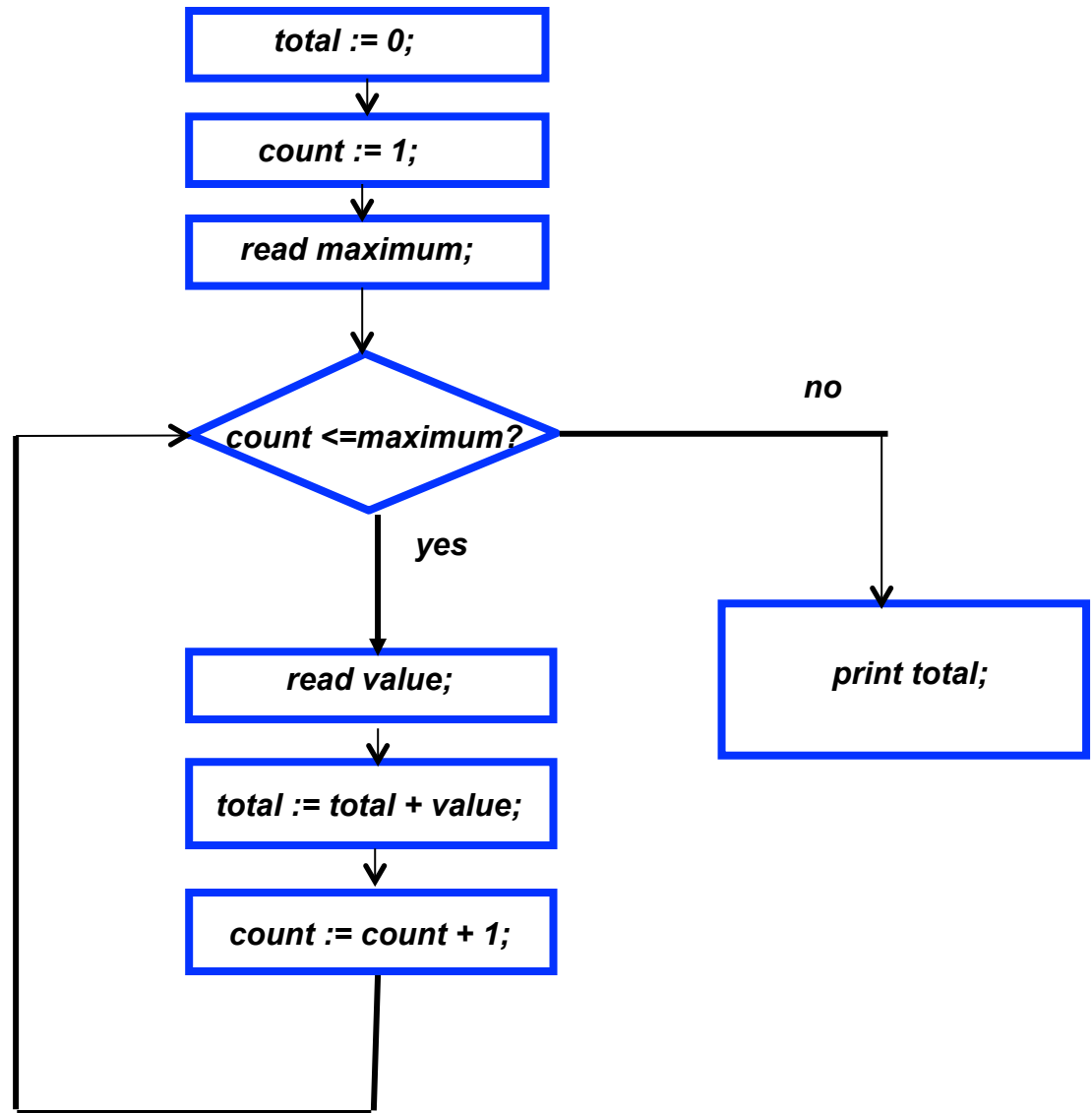
*read value;*

*total := total + value;*

*count := count + 1;*

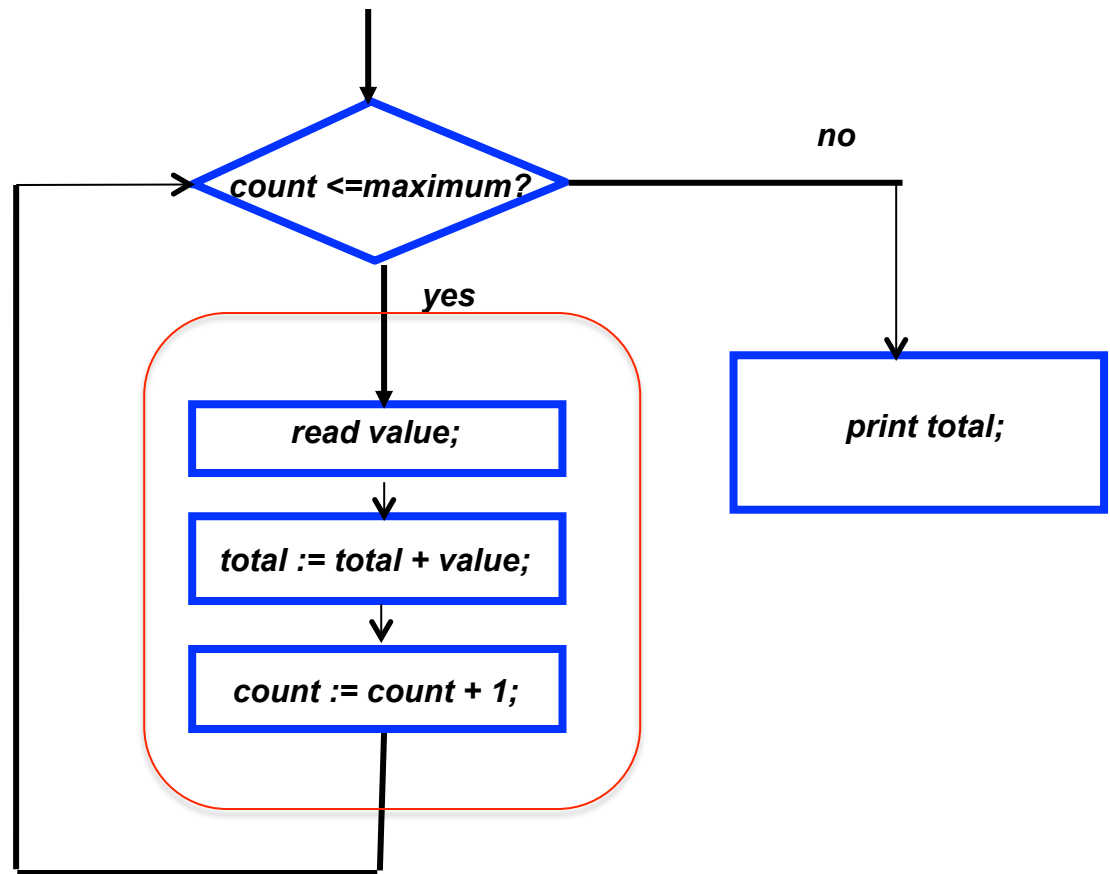
*endwhile;*

*print total;*



# Basic Block

- Maximal program region with a **single entry** and **single exit** point



# Control Flow Graph (CFG) – Example

*total, value, count, maximum : int;*

*total := 0;*

*count := 1;*

*read maximum;*

*while (count <= maximum) do*

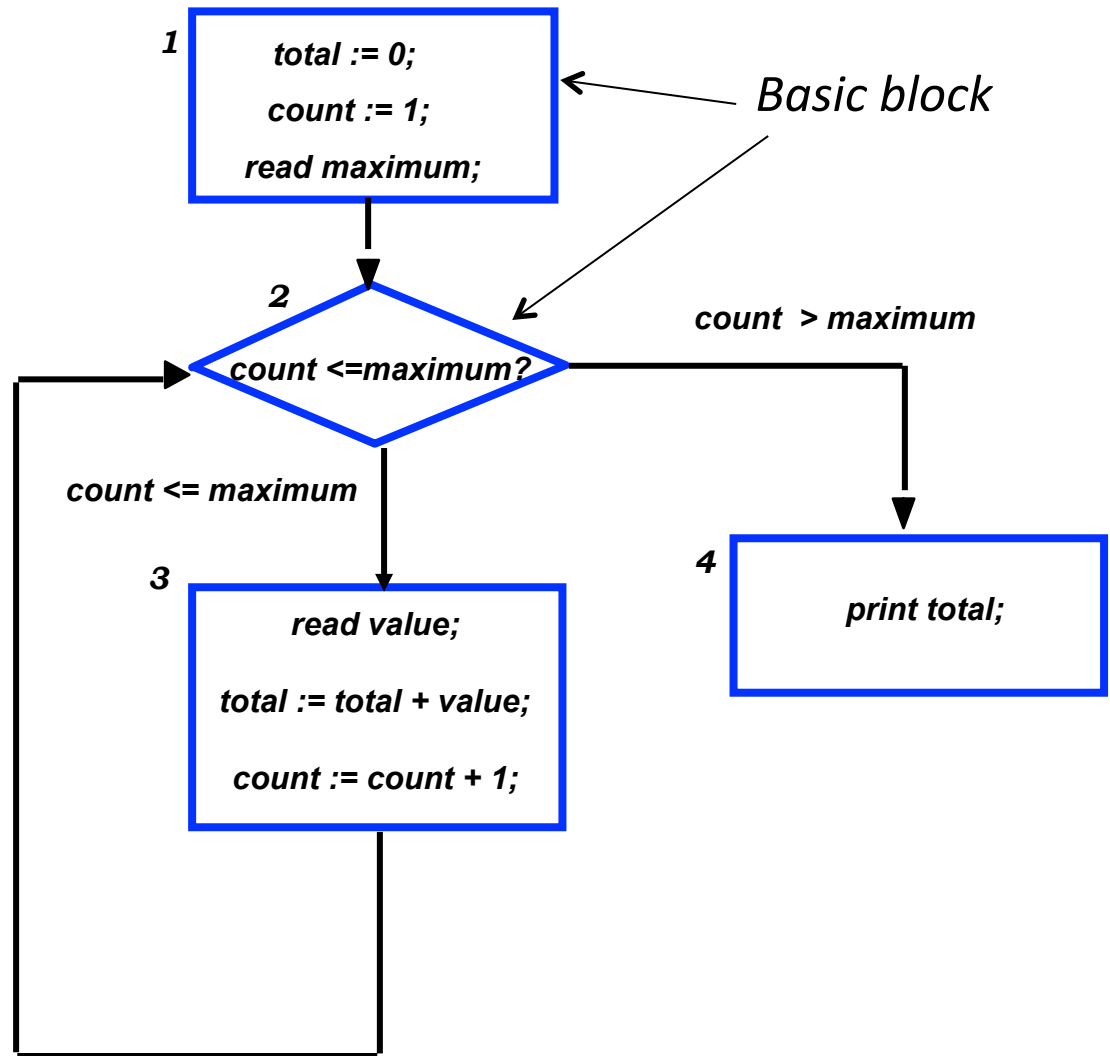
*read value;*

*total := total + value;*

*count := count + 1;*

*endwhile;*

*print total;*



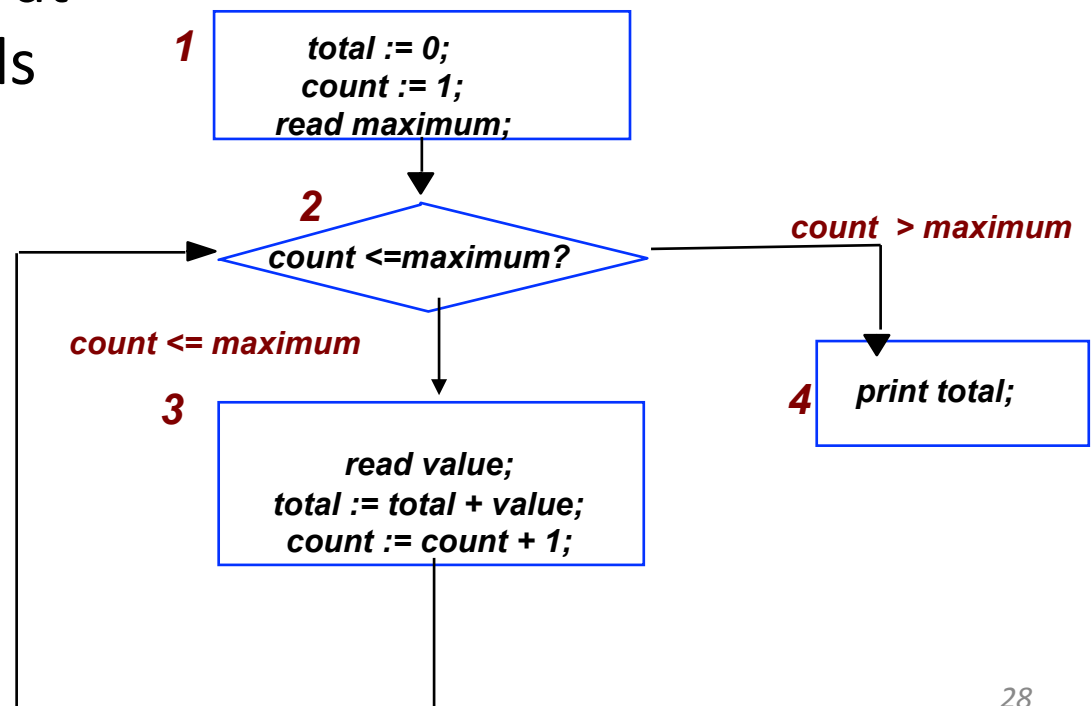


## ***Control Flow Graph (CFG) – Definition***

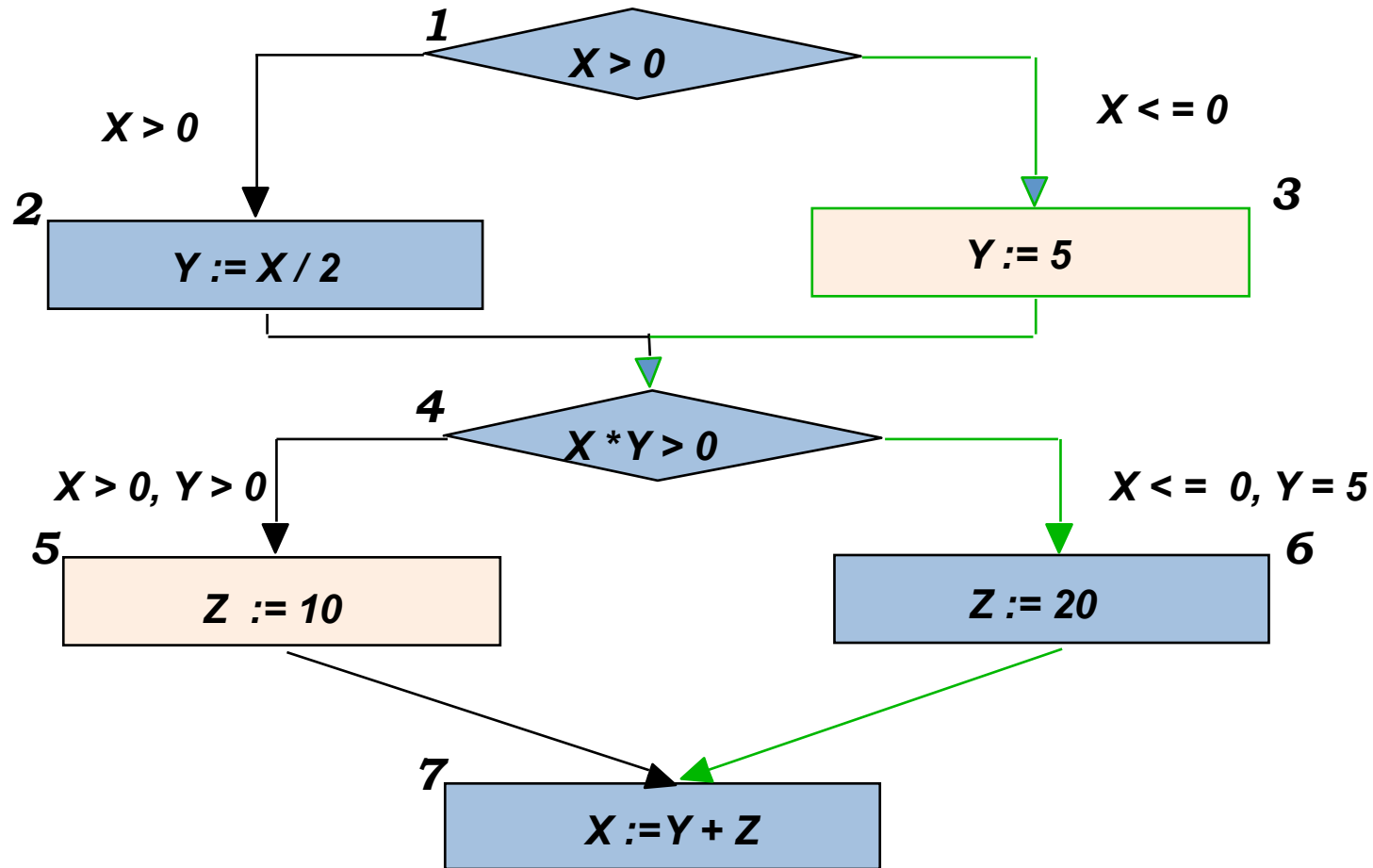
- Nodes  $N$ : statements or (more often) basic blocks
- Directed edges  $E$ : *potential* transfer of control from the end of one region directly to the beginning of another
  - $E = \{ (n_i, n_j) \mid \text{syntactically, the execution of } n_j \text{ follows the execution of } n_i \}$
- Intraprocedural (within a method)

# CFG Paths

- A **subpath** through a control flow graph:  
a sequence of nodes  $n_k, \dots, n_m$ , such that for each  $n_i$ ,  
 $k \leq i < m$ ,  $(n_i, n_{i+1})$  is an edge in the graph,
  - e.g., 2, 3, 2, 3, 2, 4
- a **complete path** starts at the start node and ends at the final node
  - e.g., 1, 2, 3, 2, 4



# Infeasible paths



*CFG overestimates the executable behavior*

# ***Dead and Unreachable Code***

*unreachable code*

X := X + 1;

Goto loop;

Y = Y + 5;

*Never executed*

*dead code*

X = X + 1;

X = 7;

X = X + Y;

*‘Executed’, but  
irrelevant*

## ***CFG - Recap***

- A directed graph where
  - Each node represents a statement or a basic block
  - Edges represent control flow
- Intraprocedural (within a method)
- Over-approximate possible flows

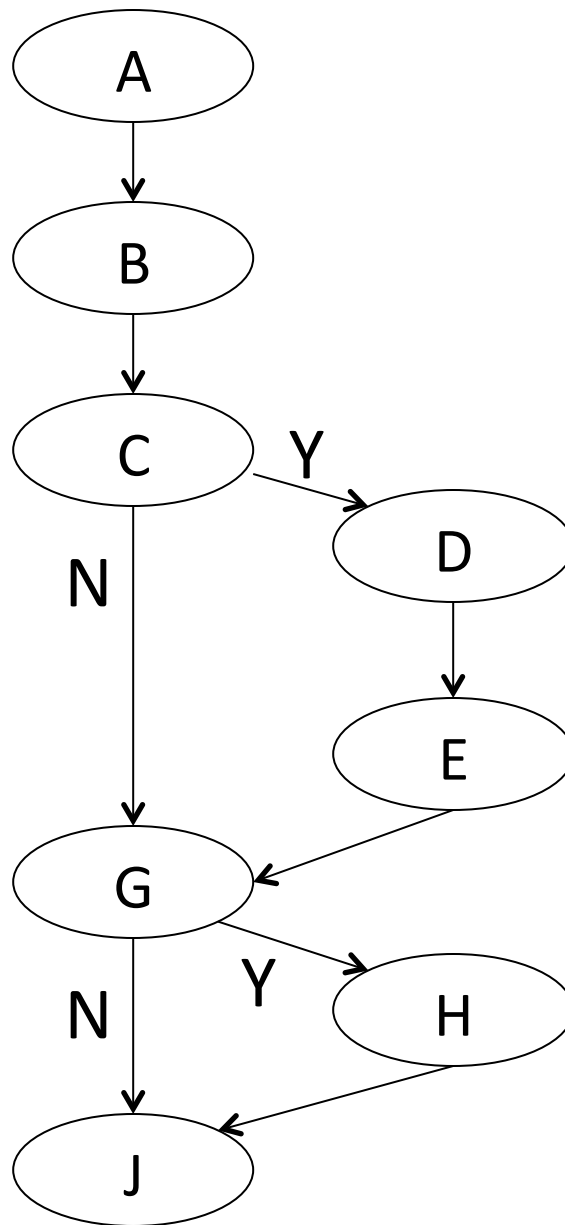
## ***Benefits of CFG***

- Probably the most commonly used representation
- Basis for many types of automated analysis
  - Graphical representations of interesting programs are too complex for direct human understanding
- Basis for various transformations
  - Compiler optimizations
  - S/W analysis

## ***Exercise***

- Draw control flow graph for this method

```
A:  void f(int x) {  
B:      int y = x;  
C:      if (x ≥ 10) {  
D:          x = x - 10;  
E:          y++;  
F:      }  
G:      if (x ≥ 5) {  
H:          x++;  
I:      }  
J:      print(x,y);  
K:  }
```



```

A: void f(int x) {
B:     int y = x;
C:     if (x ≥ 10) {
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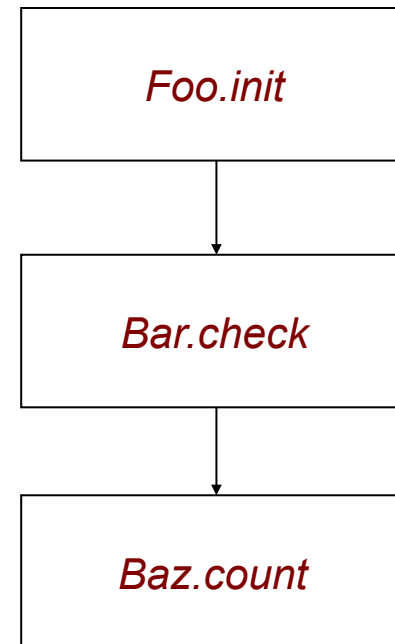


# ***Call Graphs*** ***(Interprocedural CFG)***

- Between functions (not within)
- Nodes represent procedures
  - Java methods
  - C functions
  - ...
- Edges represent **potential** *calls* relation

# Example

```
public class Foo {  
    void init() {  
        new Bar().check();  
    }  
}  
  
public class Bar {  
    void check() {  
        count();  
    }  
}  
  
class Baz {  
    void static count() {  
        //do stuff  
    }  
}
```



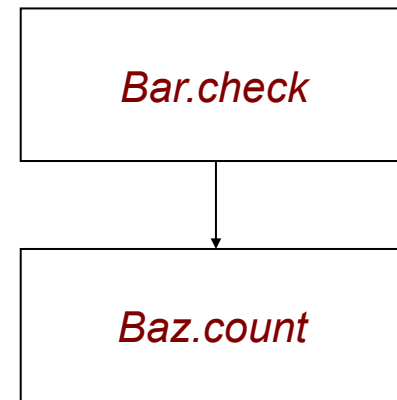
# Example

```
public class Foo {  
    void init() {  
        new Bar().check();  
    }  
}
```

```
public class Bar {  
    void check() {  
        count();  
    }  
}
```

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class Baz {  
    void static count() {  
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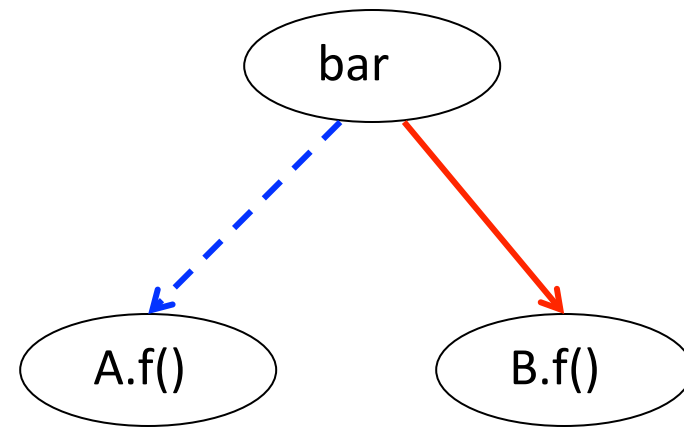
```
public static void main(String args[]) {  
    (new Bar()).check();  
}
```



*Call graph overestimates  
the executable behavior*

# Call Graph With Method Overriding

```
class A {  
    void f();  
}  
class B extends A {  
    void f();  
}  
  
bar() {  
    B b = new B();  
    A a = b;  
    a.f();  
}
```



**Question:** which edges are in the call graph?

**A:** Blue dotted edge

**B:** Red solid edge

**C:** Both

**D:** None

# ***Call Graphs ... Not That Simple***

- Creating the exact (static) call graph is an **undecidable** problem

```
class A {  
    void f();  
}  
class B extends A {  
    void f();  
}  
  
bar(A a) {  
    a.f();  
}
```

## ***(Rice's theorem)***

*“All non-trivial, semantic properties of programs are undecidable”.*

- A *semantic property* is about the program's behavior (for instance, does the program terminate for all inputs)
  - Unlike a syntactic property (for instance, does the program contain an if-then-else statement).
- A property *is non-trivial* if it is neither true nor false for every computable function

# ***Call Graphs ... Not That Simple***

- Creating the exact (static) call graph is an **undecidable** problem
- Computing call graphs requires
  - Point-to analysis (i.e., analysis of types)
  - Exceptions
  - ...
- Multiple existing heuristic algorithms
  - Various degree of precision / scalability

```
class A {  
    void f();  
}  
class B extends A {  
    void f();  
}  
  
bar(A a) {  
    a.f();  
}
```

# ***CFG and Call Graph – Precision***

- Flow Sensitivity
- Context Sensitivity





# Flow Sensitivity

- Flow-sensitive: analysis captures the sequential order of execution of statements
- Flow-insensitive: analysis only concerned with what statements are present in the program, not with the order or the reachability of statements.
- Precise vs. expensive

```
void someMethod(int y)
{
    a();
    b();
}
```

*b() is called after a()*

```
void someMethod(int y)
{
    int x1 = 2 * y;
    int x2 = x1 + 1;
}
```

*x1 is even, x2 is odd*

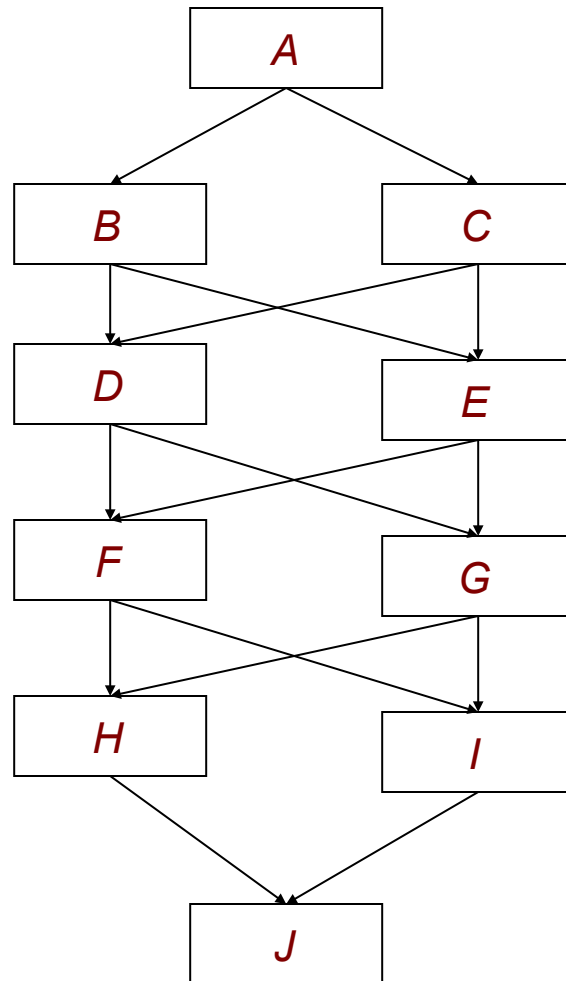
# Context Sensitivity

- For inter-procedural analyses
- Analyze a method separately for different calling contexts
  - call site sensitivity: call from different statements
  - object (a.k.a. allocation site) sensitivity: call for different receivers (objects on which the method is called)
- Precise vs. expensive

```
Class F {  
    int data;  
    void foo();  
}  
F a = new F(1);  
F b = new F(2);  
a.foo();  
b.foo();
```



# Context Sensitive - Expensive



*1 context A*

*2 contexts AB AC*

*4 contexts ABD ABE ACD ACE*

*8 contexts ...*

*16 calling contexts ...*

# ***Static vs. Dynamic CFG / Call Graph***

- Static:
  - Expensive analysis
  - Over-approximate the behaviors (if feasible)
  - Sometimes misses flows
- Dynamic
  - Expensive instrumentation (if feasible)
  - Accurate for the detected flows
  - Clearly under-approximates

# ***Agenda***

- Basics of Analysis
  - Control flow
  - Call graph
  - **Data Flow Analysis**
  - Symbolic Execution
- Presentation Tips

# ***Data Flow Analysis***

- A technique for gathering information about the propagation of data values in the program

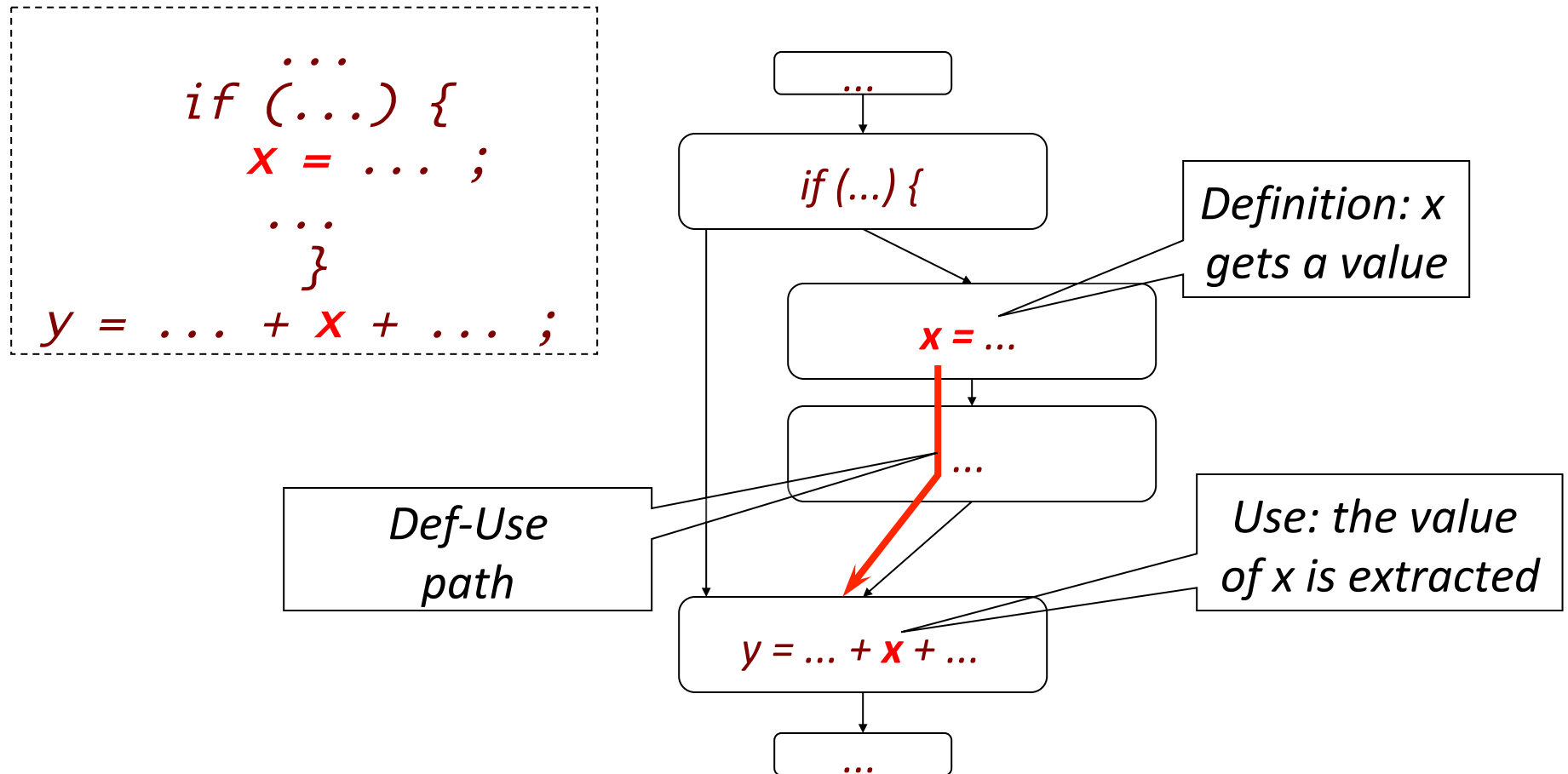
# Variable Definition and Uses (DU)

- Variable **definition**: the variable is assigned a value
  - Variable declaration (often the special value “uninitialized”)
  - Variable initialization
  - Assignment
  - Values received by a parameter, e.g., foo(23);
  - Value increments
- Variable **use**: the variable’s value is actually used
  - Expressions
  - Conditional statements
  - Parameter passing
  - Returns

```
int x
int x = 5
x = 5
foo(int x)
x++
```

```
y = x
if (x > 0)
foo(x)
return x
x++
```

# Def-Use Path



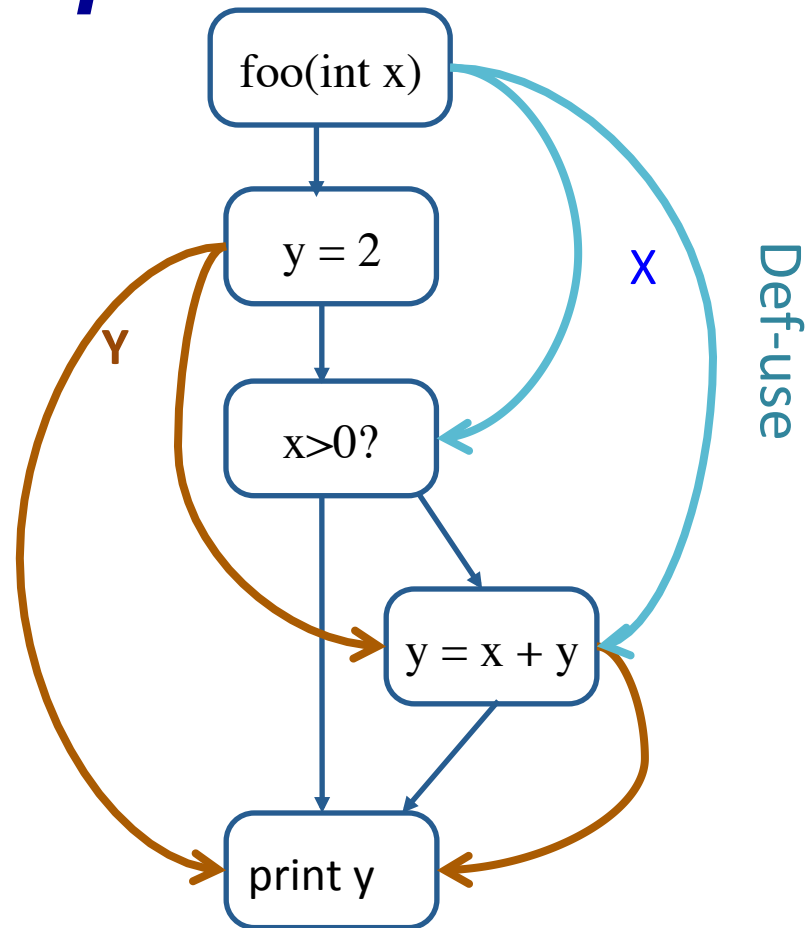


# ***Data Dependence Graph***

- Nodes: program statements
- Edges: def-use (du) pairs, labeled with the variable name

## Example

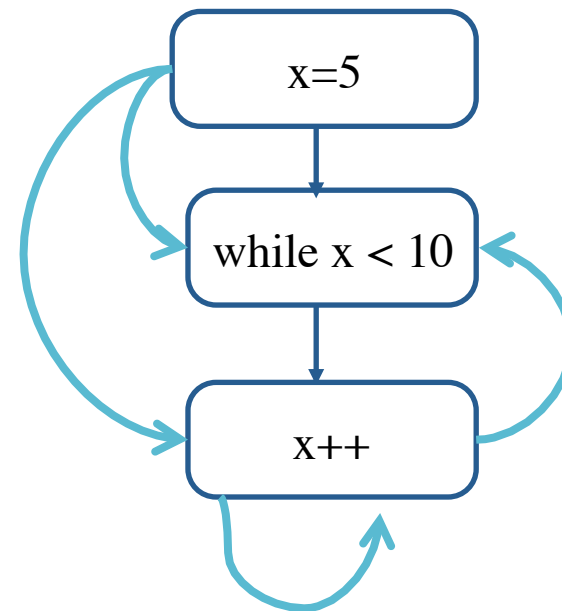
```
foo(int x) {  
    y = 2;  
    if(x > 0)  
        y = x + y;  
    endif;  
    print y;  
}
```



***What can be printed in the last statement?***

# ***What about loops?***

```
x=5;  
while (x< 10)  
{  
    x++;  
}
```



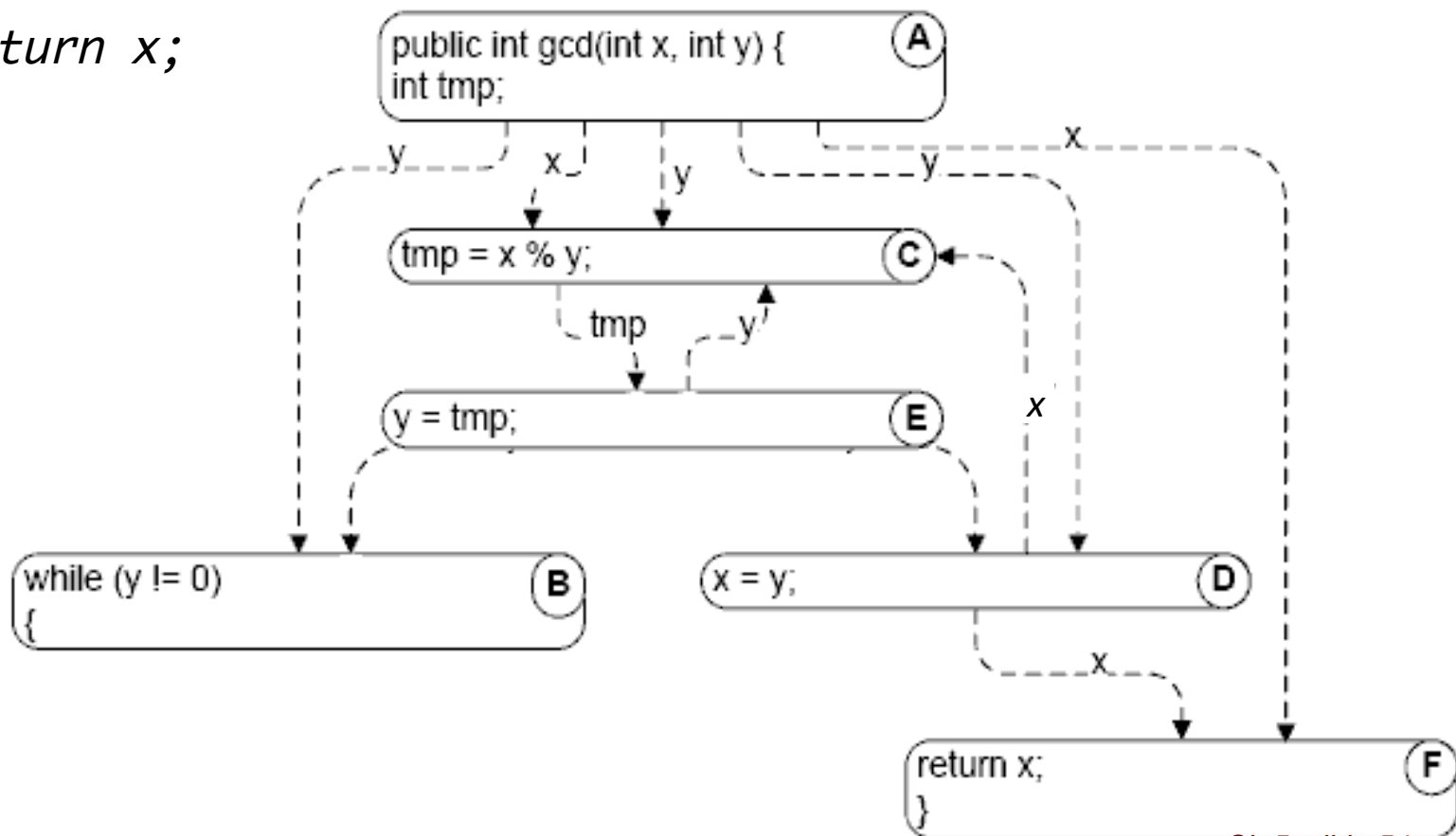
```

A: public int gcd(int x, int y) {
    int tmp;
B: while (y != 0) {
C:     tmp = x % y;
D:     x = y;
E:     y = tmp;

F: }
    return x;
}

```

*Control flow edges are omitted in this example*

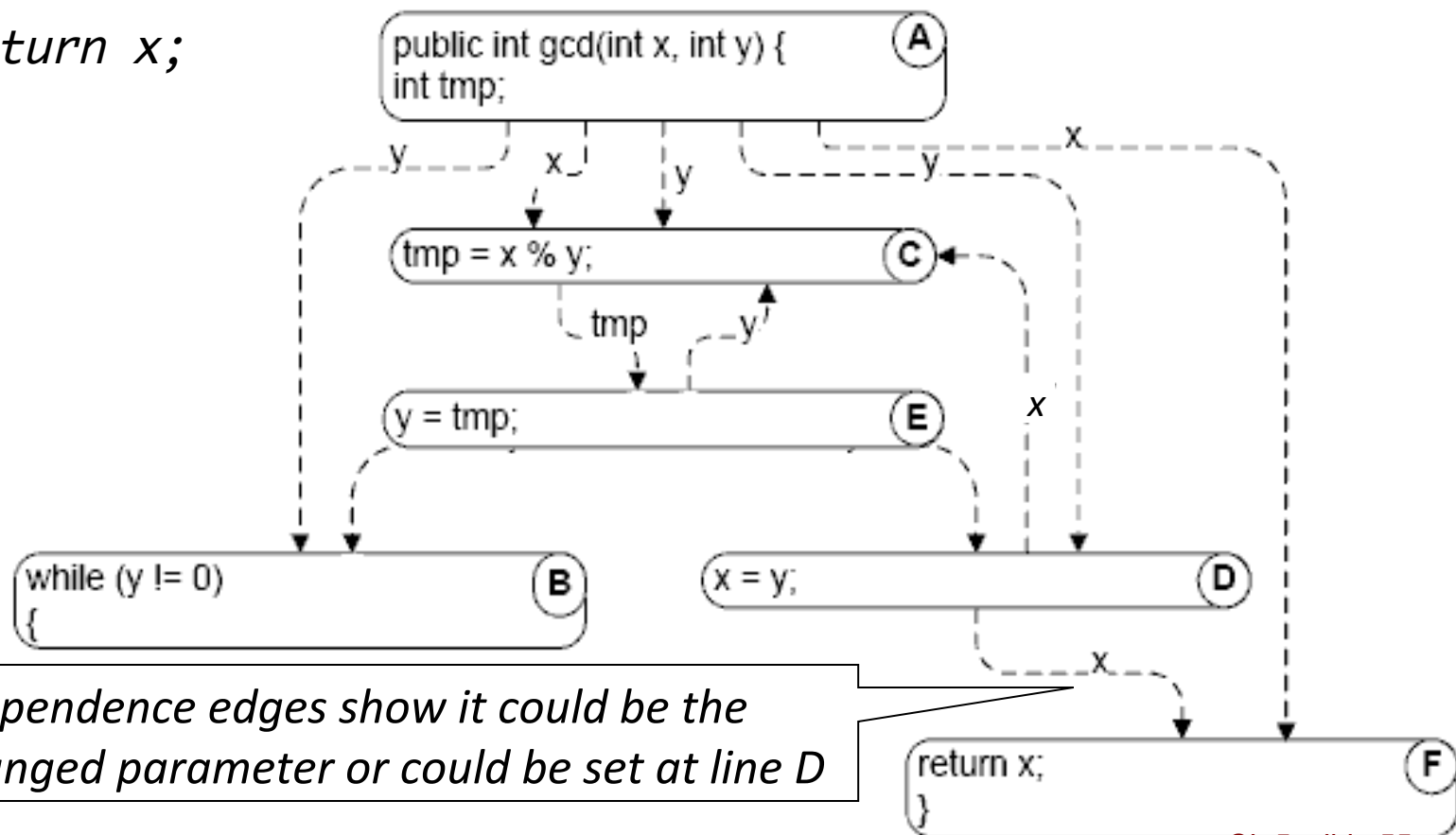


```

A: public int gcd(int x, int y) {
    int tmp;
B: while (y != 0) {
C:     tmp = x % y;
D:     x = y;
E:     y = tmp;
    }
F: return x;
}

```

*“where could the value returned in line F come from?”*



*Dependence edges show it could be the unchanged parameter or could be set at line D*

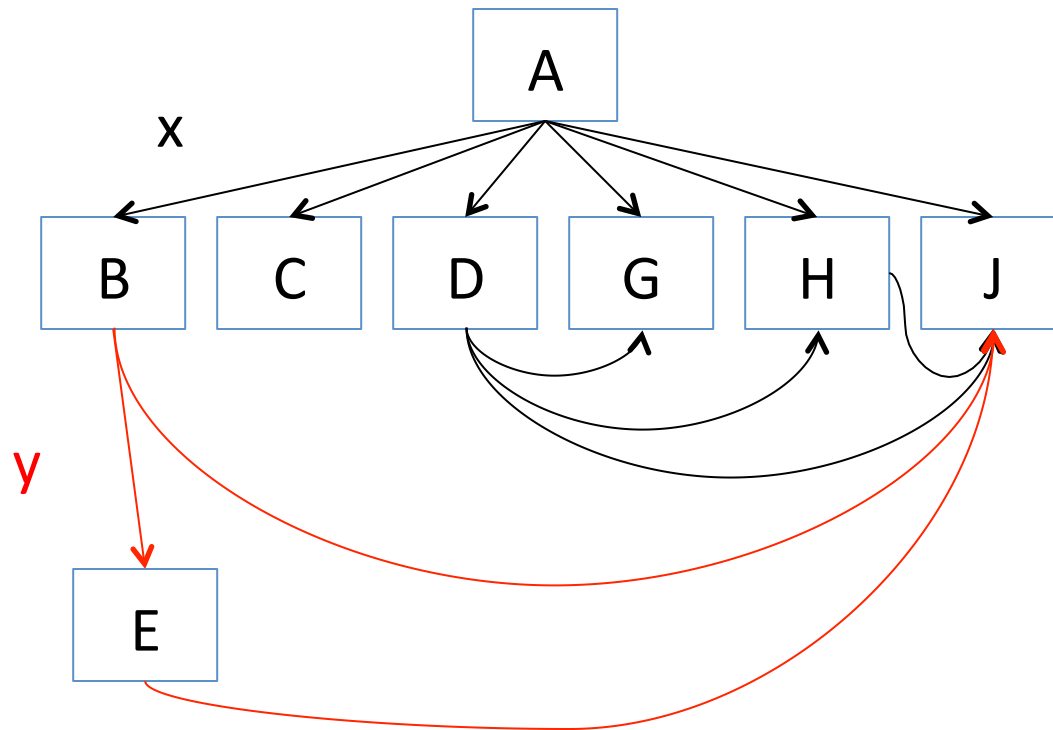
# ***Data Flow Analysis – How Used***

- Compilers and optimization, e.g.,
  - determine if a definition is dead and can be removed
  - determine if a variable always has a constant value
- Security analysis, e.g.,
  - determine if a sensitive value reaches a sensitive sink (taint analysis)
- ...

## ***Exercise***

- Draw data flow graph for this method

```
A: void f(int x) {  
B:     int y = x;  
C:     if (x ≥ 10) {  
D:         x = x - 10;  
E:         y++;  
F:     }  
G:     if (x ≥ 5) {  
H:         x++;  
I:     }  
J:     print(x,y);  
K: }
```



```

A: void f(int x) {
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```



# ***Agenda***

- Basics of Analysis
  - Control flow
  - Call graph
  - Data Flow Analysis
  - **Symbolic Execution**
- Presentation Tips

## ***Motivating Question***

```
1: if( $x > y$ ) {  
2:    $x = x + y$ ;  
3:    $y = x - y$ ;  
4:    $x = x - y$ ;  
5:   if ( $x - y > 0$ )  
6:     assert(false);  
   }
```

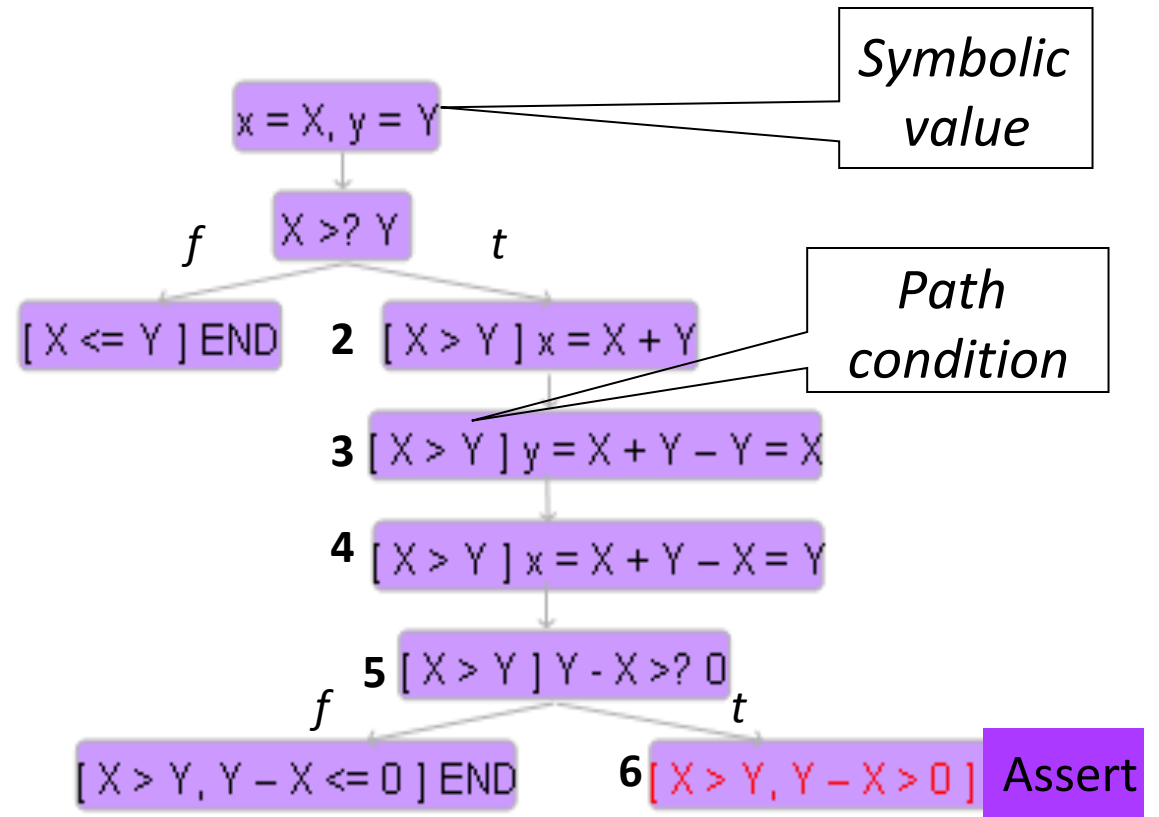
*Is the assert (line 6) reachable?*

# Symbolic Execution by Example

```

1: if(x>y) {
2:   x = x + y;
3:   y = x - y;
4:   x = x - y;
5:   if (x - y > 0)
6:     assert(false);
  }

```

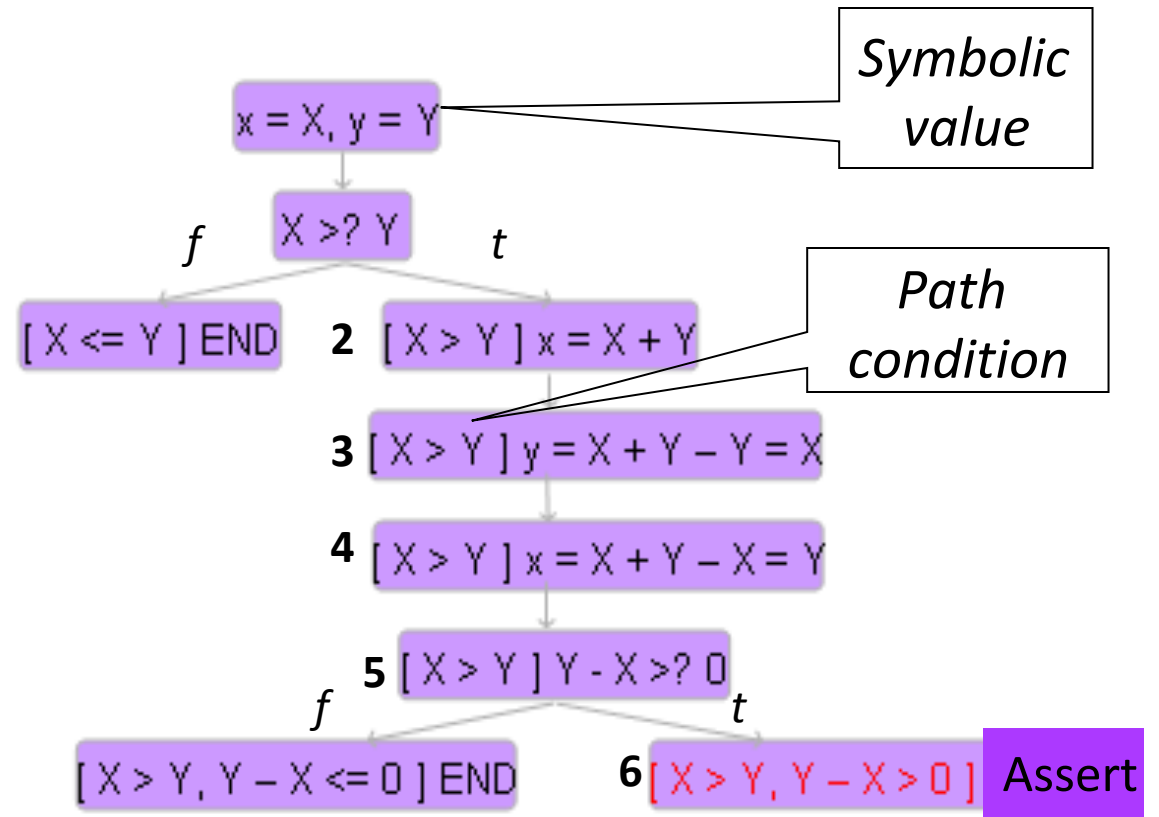


*Is the assert (line 6) reachable?*

2:  $x = X+Y, y=Y$

# Symbolic Execution by Example

```
1: if(x>y) {  
2:   x = x + y;  
3:   y = x - y;  
4:   x = x - y;  
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```

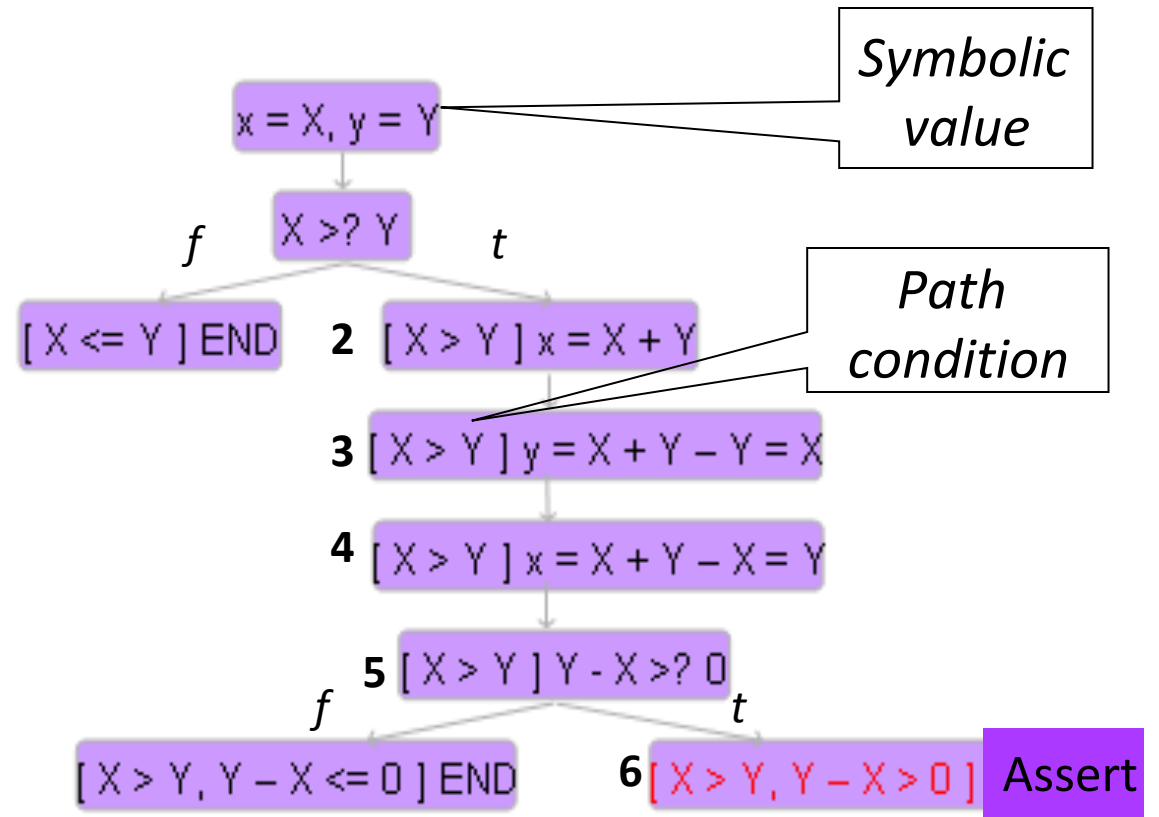


*Is the assert (line 6) reachable?*

3:  $x = X + Y, y = X$

# Symbolic Execution by Example

```
1: if(x>y) {  
2:   x = x + y;  
3:   y = x - y;  
4:   x = x - y;  
5:   if (x - y > 0)  
6:     assert(false);  
}
```

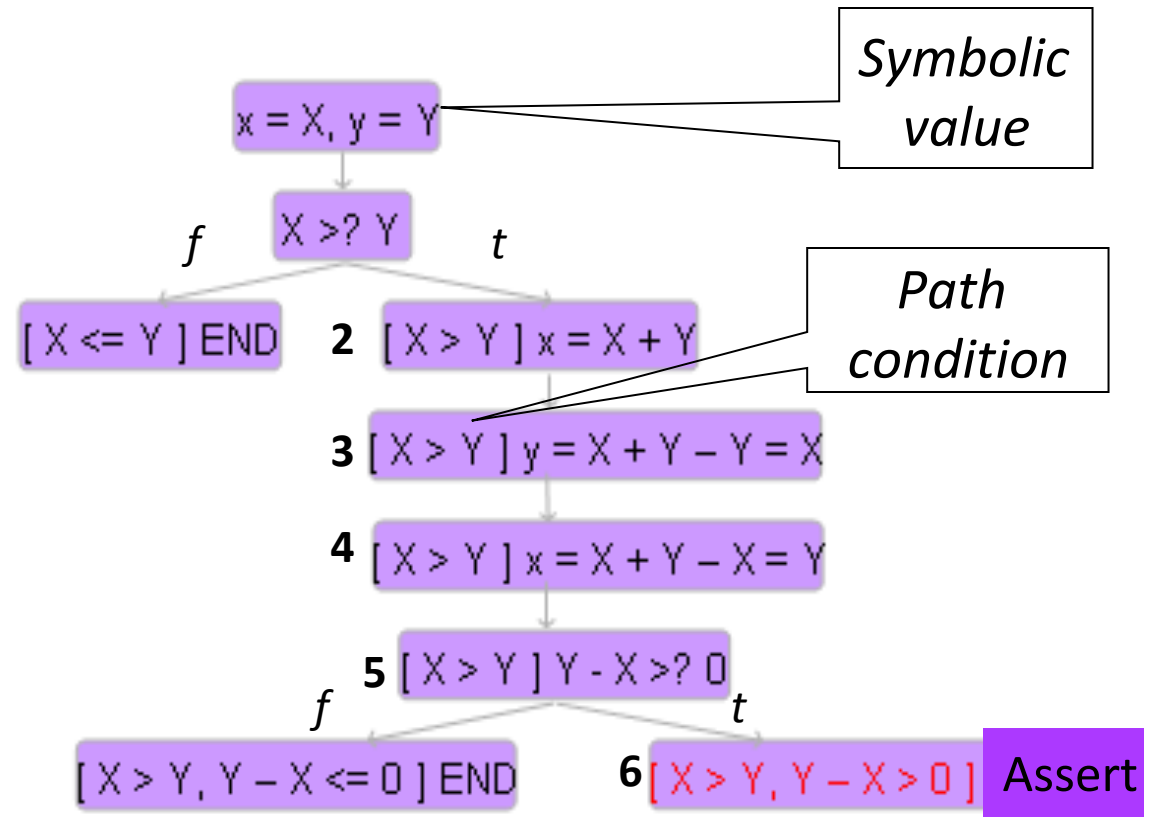


*Is the assert (line 6) reachable?*

4:  $x = Y, y = X$

# Symbolic Execution by Example

```
1: if(x>y) {  
2:   x = x + y;  
3:   y = x - y;  
4:   x = x - y;  
5:   if (x - y > 0)  
6:     assert(false);  
}
```

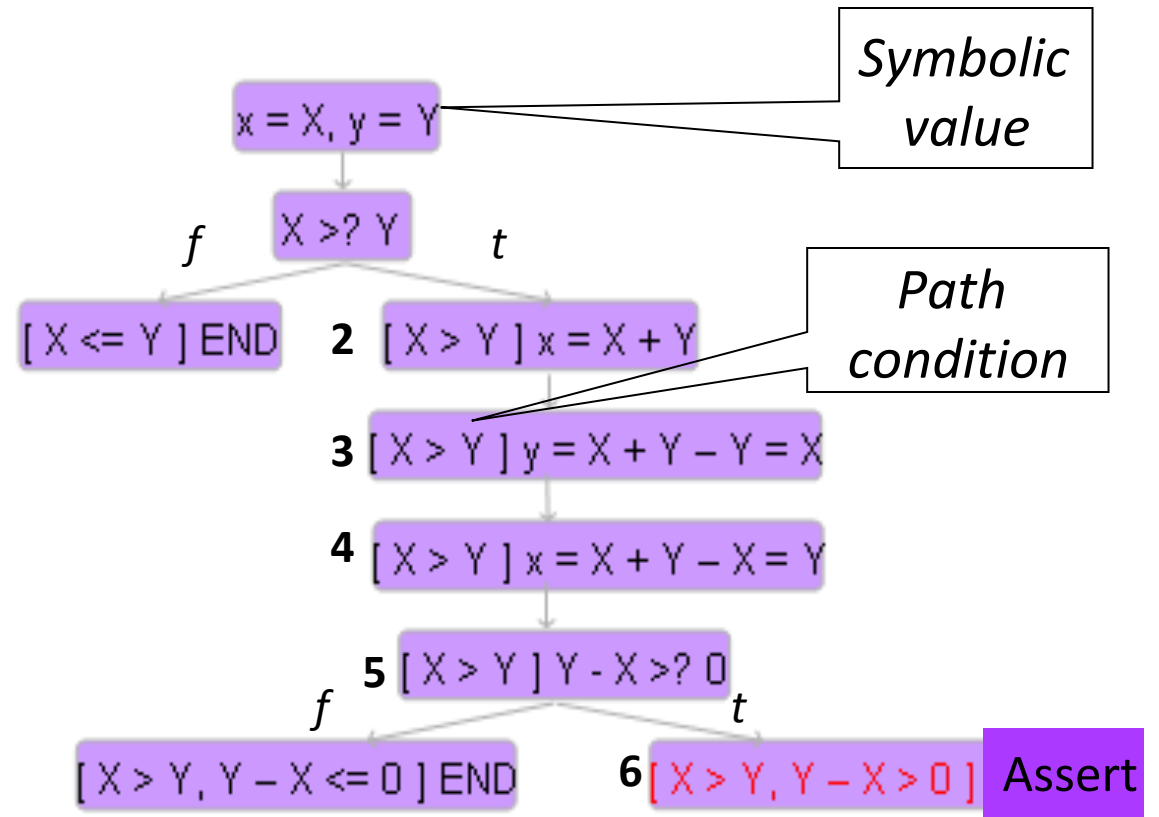


*Is the assert (line 6) reachable?*

5:  $Y - X > 0$ ?

# Symbolic Execution by Example

```
1: if(x>y) {  
2:   x = x + y;  
3:   y = x - y;  
4:   x = x - y;  
5:   if (x - y > 0)  
6:     assert(false);  
}
```

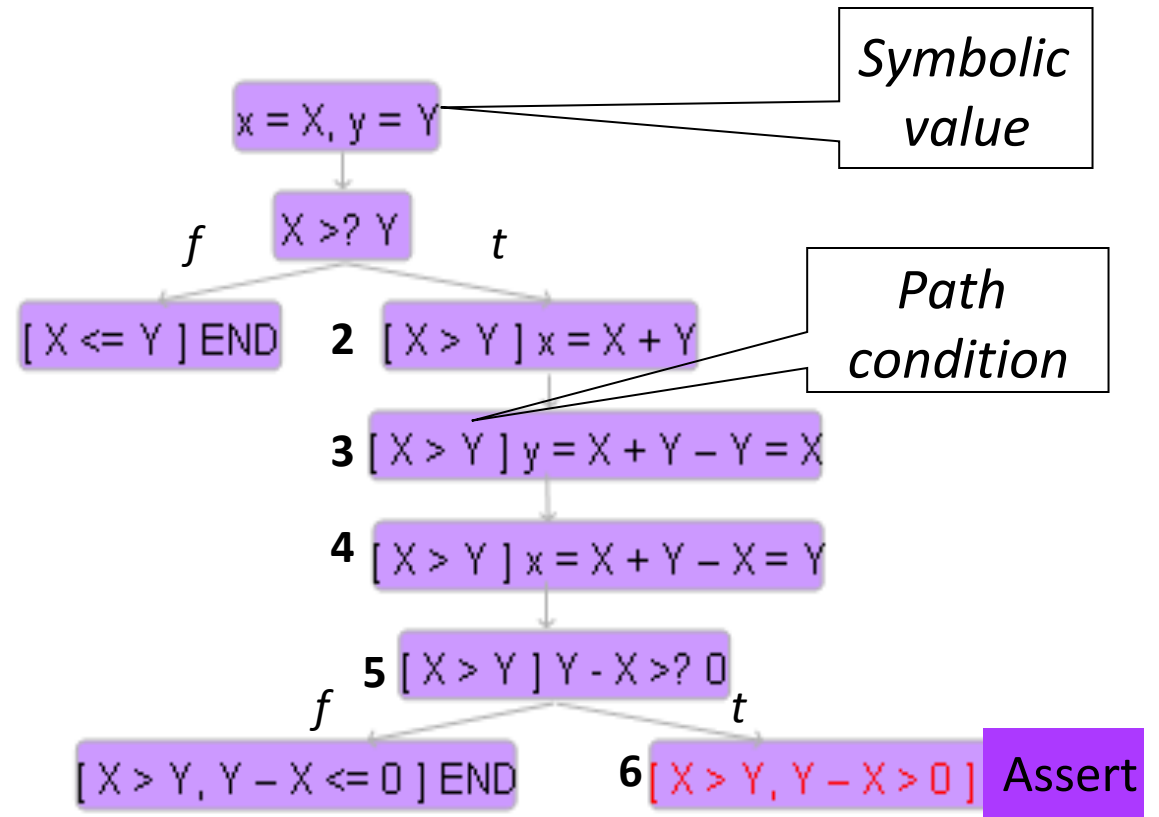


*Is the assert (line 6) reachable?*

Condition for 6:  
 $X > Y \ \& \ Y - X > 0$

# Symbolic Execution by Example

```
1: if(x>y) {  
2:   x = x + y;  
3:   y = x - y;  
4:   x = x - y;  
5:   if (x - y > 0)  
6:     assert(false);  
}
```



*Is the assert (line 6) reachable?*

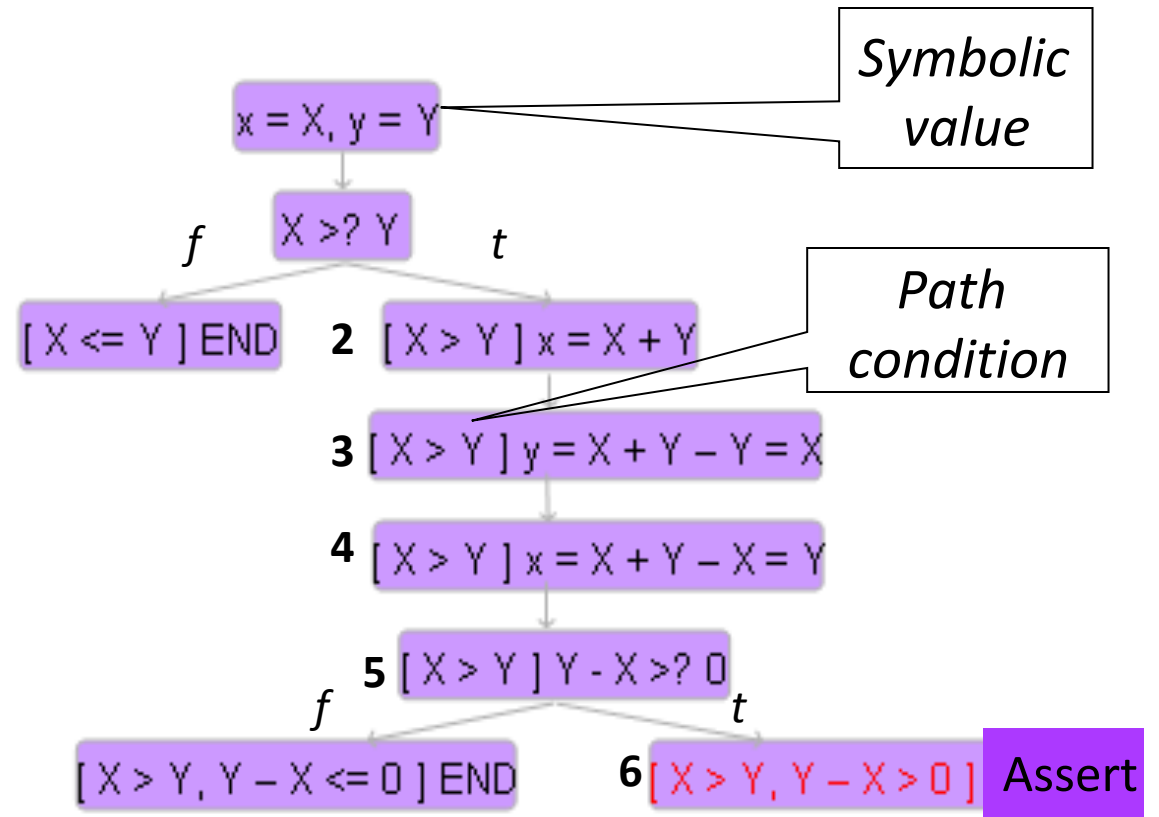
**NO!**



# Symbolic Execution by Example

```

1: if(x>y) {
2:   x = x + y;
3:   y = x - y;
4:   x = x - y;
5:   if (x - y > 0)
6:     assert(false);
}
```



Two equivalence classes

(a)  $X \leq Y$  (b)  $X > Y$

# ***Symbolic Execution***

- Static Analysis
- Tracking **symbolic** rather than **actual** values
- Builds **predicates** that characterize
  - Conditions for executing paths
  - Effects of the execution on **program state**
- Is used to reason about all the **inputs** that take the same path through a program

# ***Symbolic Path Constraints***

- Theorem prover (**constraint solver**) determines if an answer exists and the branch can be taken
  - Popular constraint solvers: Z3, CVC, lp solver
  - Undecidable problem in theory
- Each path in the tree represents an equivalence class of inputs
- When paths terminate, symbolic execution computes concrete values for each path by **solving** the path constraints
  - These values can be thought of as concrete path representatives
  - E.g., test cases that can help developers reproduce bugs

# ***Applications of Symbolic Execution***

- Guiding the test input generation to cover all branches
- Identifying infeasible program paths
- Security testing
- Clone detection (equivalence checking)
- ...

# *Limitations of Symbolic Execution*

- Expensive
  - Executing all feasible program paths is exponential in the number of branches
  - Does not scale to large programs
- Problems with function calls
- Problem with handling loops
  - often *unroll* them up to a certain depth rather than dealing with termination or loop invariants
- Expensive to reason about *expressions*
  - Although modern SMT solvers help!

# ***Difference Between Symbolic Execution and Data Flow Analysis?***

- Different purpose
  - Symbolic execution: reason about path feasibility
  - Data flow analysis: check which definitions are live, which values are constant, etc.
- Different abstraction
  - Symbolic execution: symbolic computational paths
  - Data flow analysis: concrete def-use
- Accuracy
  - Symbolic execution: only feasible paths considered
  - Data flow analysis: all paths considered
- ...

# ***Exercise***

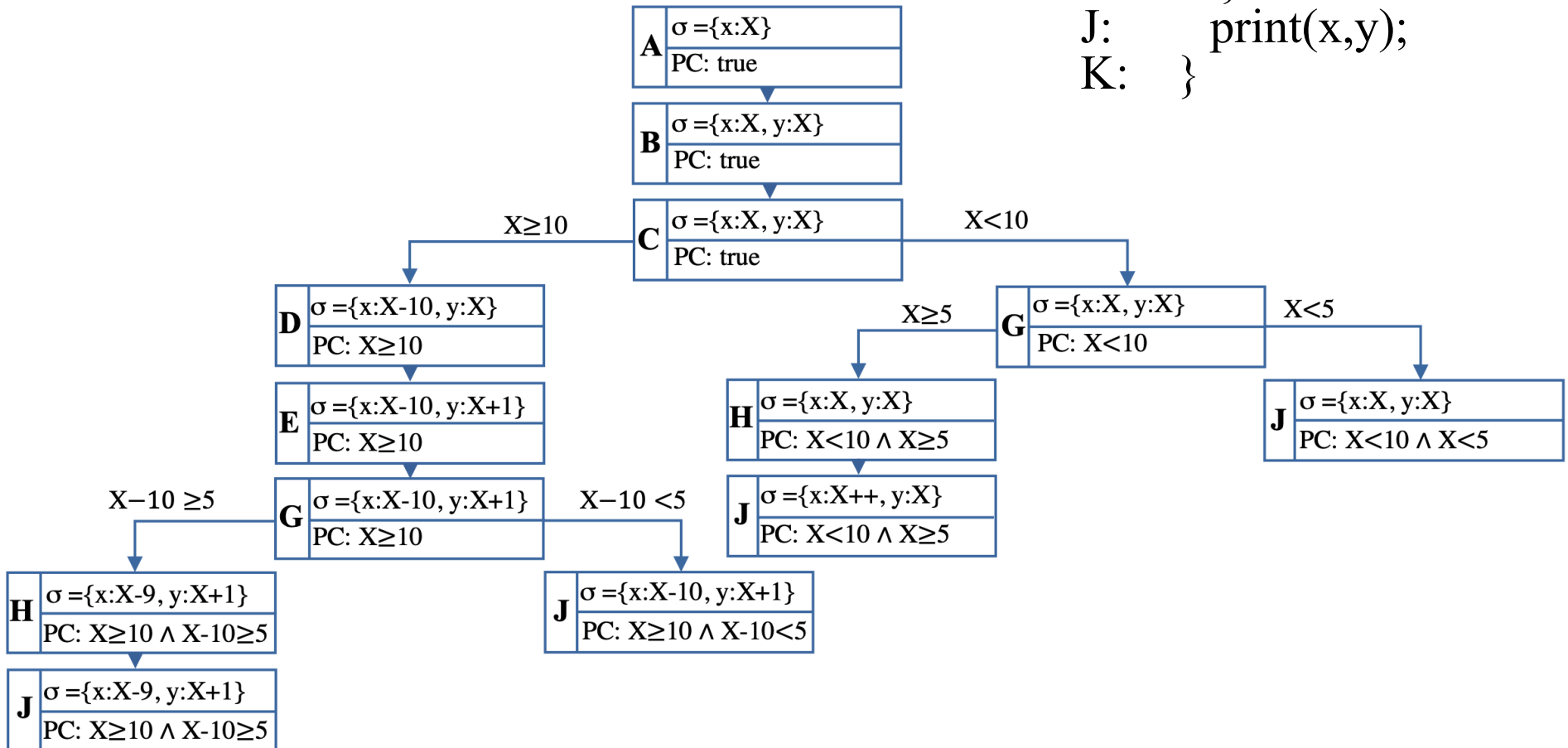
- Execute symbolically

```
A: void f(int x) {  
B:     int y = x;  
C:     if (x ≥ 10) {  
D:         x = x - 10;  
E:         y++;  
F:     }  
G:     if (x ≥ 5) {  
H:         x++;  
I:     }  
J:     print(x,y);  
K: }
```

```

A: void f(int x) {
B:   int y = x;
C:   if (x ≥ 10) {
D:     x = x - 10;
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G:   if (x ≥ 5) {
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J:   print(x,y);
K: }

```





## ***Summary: “Holy-Grail” of Analysis***

- ✓ Useful
- ✓ Accurate
- ✓ Scalable



### Questions:

- What is the right model for the task?
- What is the right analysis for the task?



# ***Summary: Static vs. Dynamic Analysis***

## **Dynamic Analysis**

- Draw inferences from a sample
- Scale well
- Precise for the analyzed samples
- Miss info
- Can require expensive instrumentation

## **Static Analysis**

- Try to be conservative, i.e., never declare a property to be valid if it is not
- Over-estimate actual behavior
- Often sacrifice precision for scalability

***In reality – both have limitations.  
Choose the right tool for the task!***