## 1

## SEQUENCE AND SERIES

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Q: Find the sum to n terms of  $3 \times 8 + 6 \times 11 + 9 \times 14 + ...$  Solution:

Variable	Description	Value
x(n)	<i>n</i> <sup>th</sup> term of sequence	(3n+3)(3n+8)u(n)
TABLE 0		
INPUT PARAMETERS		

Sum of n terms of AP is given by

$$x(n) = (3n+3)(3n+8)u(n)$$
 (1)

$$y(n) = x(n) * u(n)$$
(2)

$$u(n) \stackrel{\mathcal{Z}}{\longleftrightarrow} \frac{1}{(1-z^{-1})} \quad |z| > 1 \tag{3}$$

$$nu(n) \stackrel{\mathcal{Z}}{\longleftrightarrow} \frac{z^{-1}}{(1-z^{-1})^2} \quad |z| > 1 \tag{4}$$

$$n^2 u(n) \stackrel{\mathcal{Z}}{\longleftrightarrow} \frac{z^{-1}(1+z^{-1})}{(1-z^{-1})^3} \quad |z| > 1$$
 (5)

$$n^{3}u(n) \leftrightarrow \frac{z^{-1}\left(1 + 4z^{-1} + z^{-2}\right)}{\left(1 - z^{-1}\right)^{4}} \quad |z| > 1$$
 (6)

$$\implies X(z) = 9z^{-1} \frac{\left(1 + z^{-1}\right)}{\left(1 - z^{-1}\right)^3} + \frac{33\left(z^{-1}\right)}{\left(1 - z^{-1}\right)^2} + \frac{24}{\left(1 - z^{-1}\right)} |z| > 1 \tag{7}$$

$$Y(z) = X(z)U(z)$$
(8)

$$\implies Y(z) = 9z^{-1} \frac{\left(1 + z^{-1}\right)}{\left(1 - z^{-1}\right)^4} + \frac{33\left(z^{-1}\right)}{\left(1 - z^{-1}\right)^3} + \frac{24}{\left(1 - z^{-1}\right)^2} |z| > 1$$
(9)

Now from (3), (4), (5), (6), (9) By using inverse Z-transform pairs,

$$y(n) = \left(\frac{9n(n+1)(2n+1)}{6} + \frac{33n(n+1)}{2} + 24(n+1)\right)u(n)$$
 (10)

... Sum of *n* terms of the series whose  $n^{th}$  term is given by (3n + 3)(3n + 8)u(n) is  $(\frac{9n(n+1)(2n+1)}{6} + \frac{33n(n+1)}{2} + 24(n+1))u(n)$ 

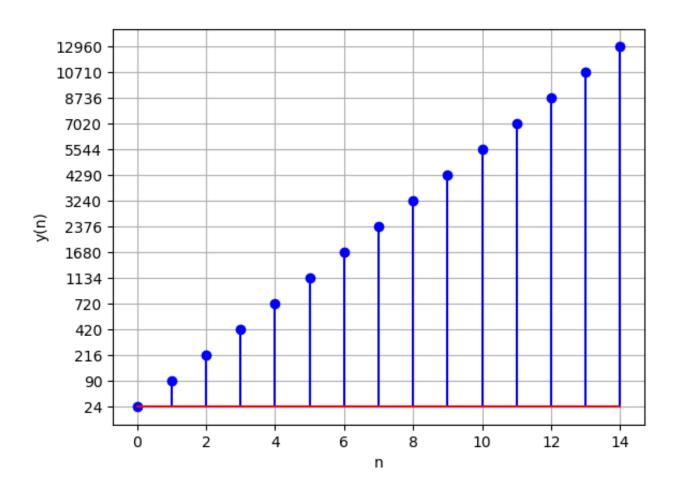


Fig. 0. Theory vs Simulation