

Regression Vs. ANOVA: Is a main effect really a main effect?

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Outline

- 1 Introduction
 - Defining the problem
 - Content of this talk
- 2 Toy Example
 - Using categorical variables only
 - Using continuous variables
- 3 Real Data Example
 - Methods
 - Results
- 4 Conclusion

Defining the problem

What you might see

We defined a regression model $\text{Score} \sim \text{Condition} * \text{PrePost}$.

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All stats in R have the same syntax

What to expect from this talk?

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What this talk is not about

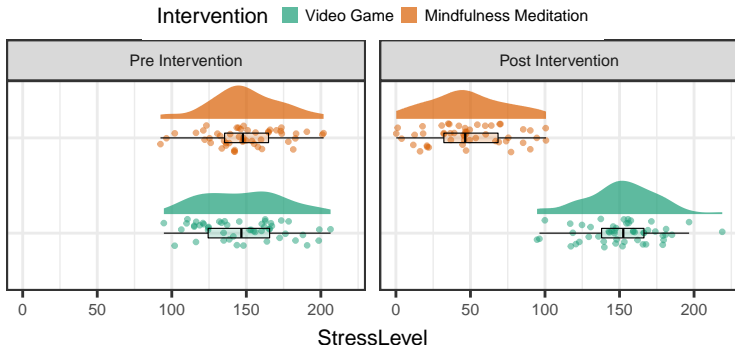
- How to use R
- How to build a good mixed-effects model
- The p -value debate

The simulated data with two categorical variables

Assessing stress levels after and before a 30 minutes intervention, “mindfulness meditation” or “video games”.

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aov(StressLevel ~ Intervention*PrePost)
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Parameter	Sum Square	F value	$Pr(> F)$
Intervention	114381	164.8	$< 2e-16$
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Parameter	Estimate	Std. Error	t value	$Pr(> t)$
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Intervention	1.801	5.195	0.347	0.729
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Graphically understanding the regression results

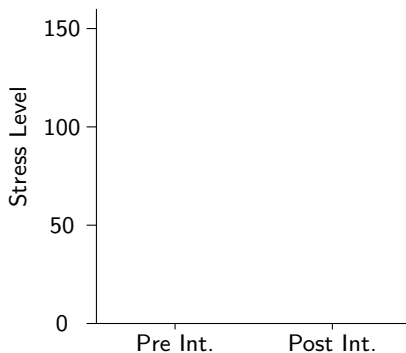
$$\text{Stress} = 147.5 + 2 \times \text{Int} + 3.5 \times \text{PrPo} - 104 \times \text{Int} \times \text{PrPo}$$
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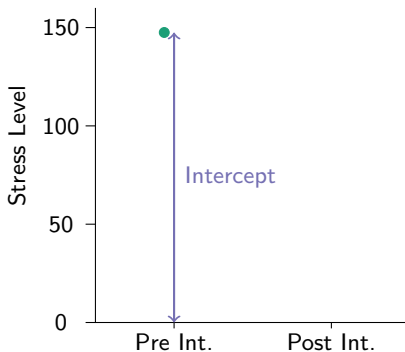


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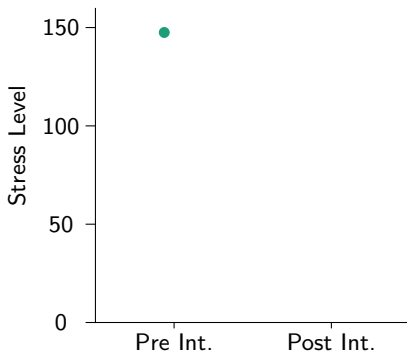


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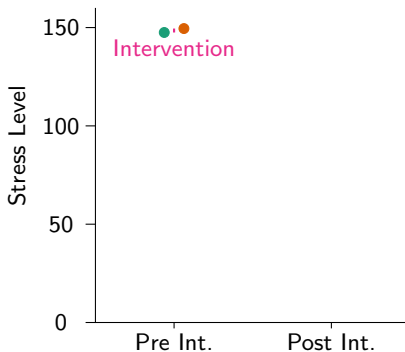


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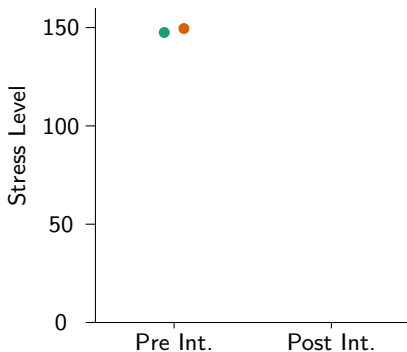


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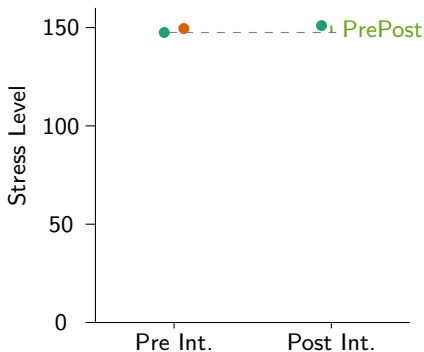


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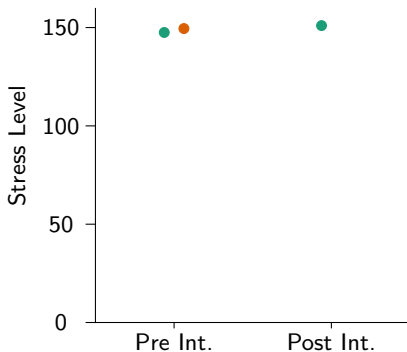


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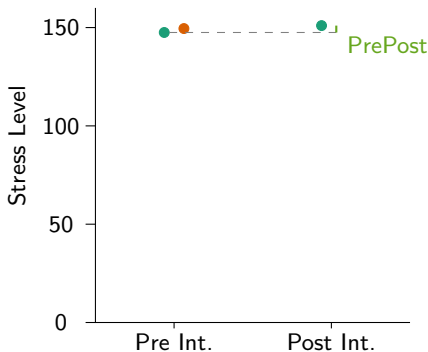


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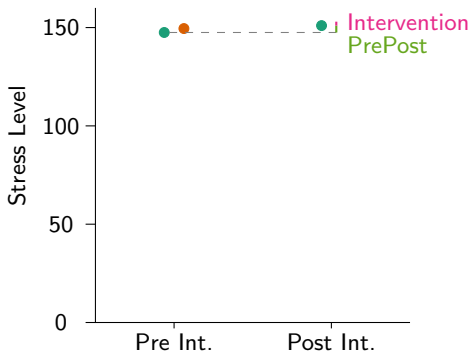


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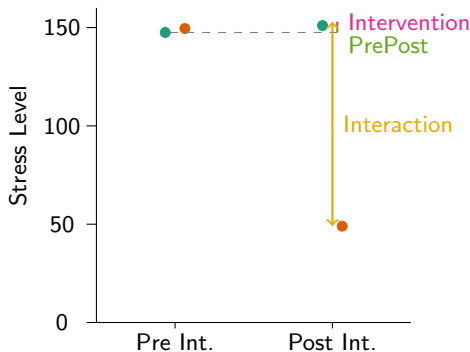


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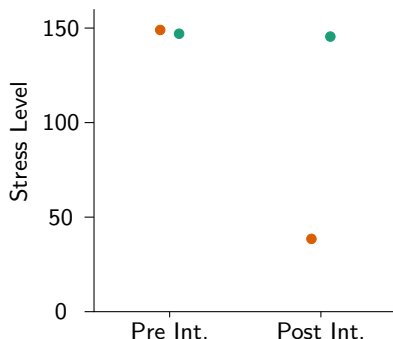
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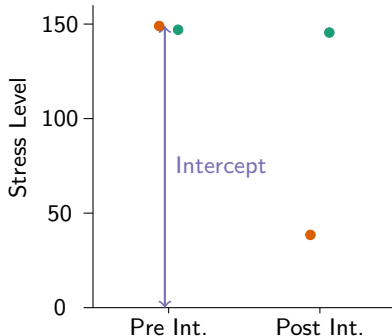
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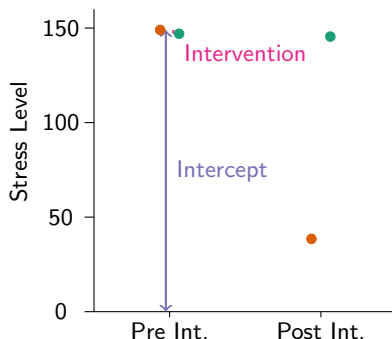
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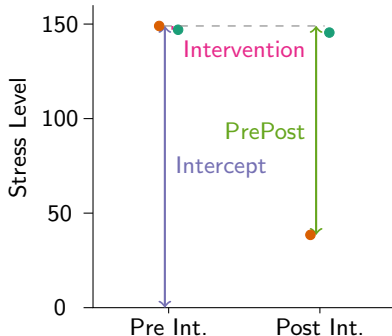
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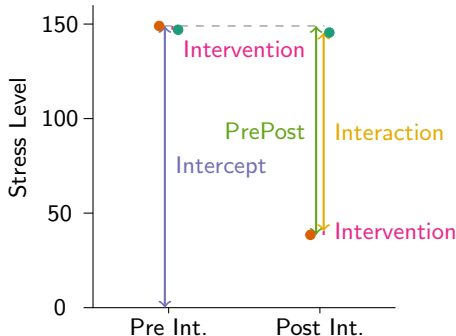
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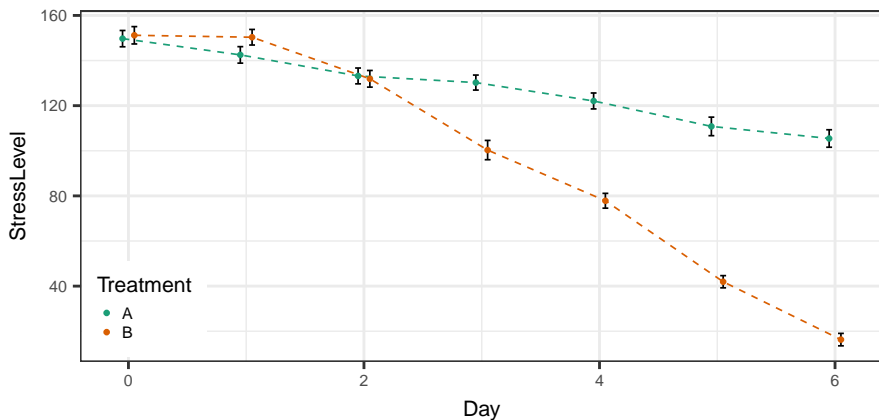


A slightly less meaningful example with a continuous variable

Assessing the difference between treatment A and treatment B in reducing stress levels each day over a week.

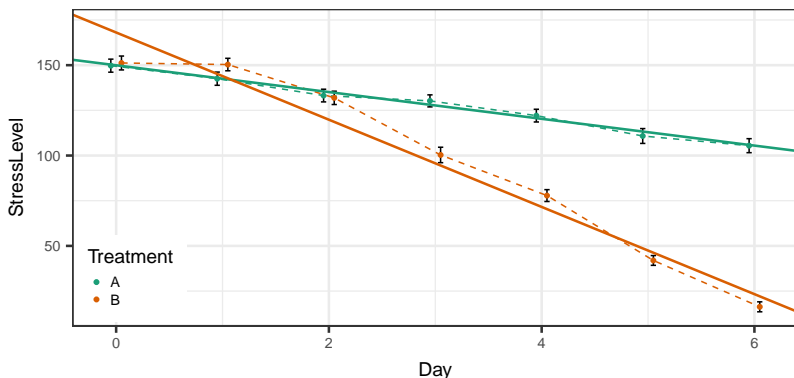
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Regression results

Parameter	Estimate	Std. Error	<i>t</i> value	$Pr(> t)$
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TreatmentB	18.1489	3.5359	5.133	$3.71e-7$
Day	-7.4051	0.6934	-10.679	$< 2e-16$
TreatmentB:Day	-16.7244	0.9807	-17.054	$< 2e-16$



The experiment in a nutshell

Categorisation and labelling in 15-month-old infants.

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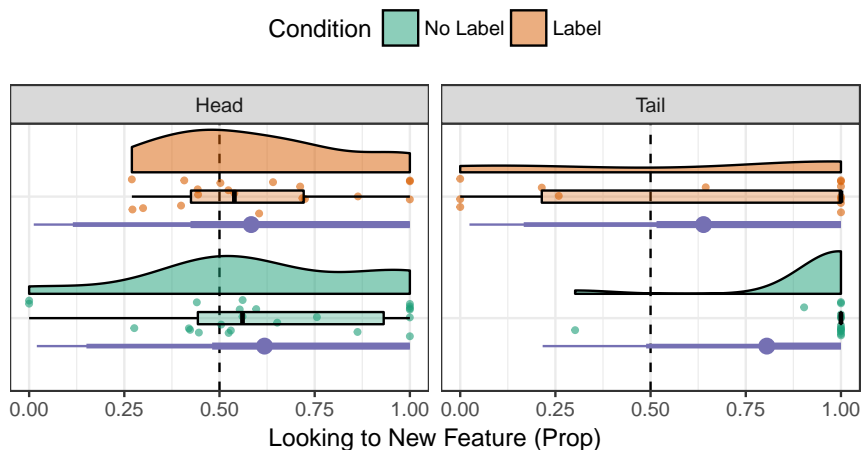
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Label condition: categories defined by the tail.

Novelty Preference Did they encode the tail? The head?

One old animal against one animal with a new head/tail.

Choosing reference levels



What's the take home message?