Static Program Analysis

Pointer Analysis Foundations (I)

Nanjing University

Tian Tan

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Contents

- 1. Pointer Analysis: Rules
- 2. How to Implement Pointer Analysis
- 3. Pointer Analysis: Algorithms
- 4. Pointer Analysis with Method Calls

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Pointer-Affecting Statements

New
$$x = \text{new } T()$$

Assign $x = y$

Store $x \cdot f = y$

First focus on these statements (suppose the program has just one method)

Load $y = x \cdot f$

Call $r = x \cdot k(a, ...)$

Will come back to this in pointer analysis with method calls

Domain and Notations

Variables: $x, y \in V$

Fields: $f, g \in F$

Objects: $o_i, o_j \in O$

Instance fields: $o_{i,f}, o_{j,g} \in O \times F$

Pointers: Pointer = $V \cup (O \times F)$

Points-to relations: pt: Pointer $\rightarrow \mathcal{P}(0)$

- $\mathcal{P}(0)$ denotes the powerset of O
- pt(p) denotes the points-to set of p

Rules

Kind	Statement	Rule
New	i: x = new T()	$\overline{o_i \in pt(x)}$
Assign	x = y	$\frac{o_i \in pt(y)}{o_i \in pt(x)}$
Store	x.f = y	$\frac{o_i \in pt(x), \ o_j \in pt(y)}{o_j \in pt(o_i.f)}$
Load	y = x.f	$\frac{o_i \in pt(x), \ o_j \in pt(o_i.f)}{o_j \in pt(y)}$

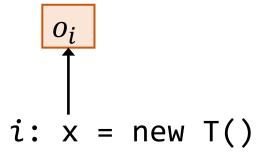
Rules

Kind	Statement	Rule	
New	i: x = new T()	$\overline{o_i \in pt(x)} \leftarrow \text{unconditional}$	
Assign	x = y	$\frac{o_i \in pt(y)}{o_i \in pt(x)} \leftarrow \text{premises}$	
Store	x.f = y	$\frac{o_i \in pt(x), \ o_j \in pt(y)}{o_j \in pt(o_i, f)}$	
Load	y = x.f	$\frac{o_i \in pt(x), \ o_j \in pt(o_i.f)}{o_j \in pt(y)}$	

Rule: New

$$\overline{o_i \in pt(x)}$$

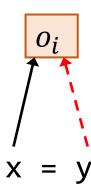
---- Conclusion



Rule: Assign

$$\frac{o_i \in pt(y)}{o_i \in pt(x)}$$

- ---→ Premises
- ---- Conclusion

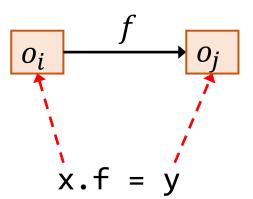


Rule: Store

$$\frac{o_i \in pt(x), \ o_j \in pt(y)}{o_j \in pt(o_i, f)}$$



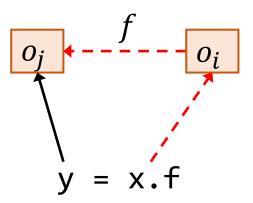
---- Conclusion



Rule: Load

$$\frac{o_i \in pt(x), \ o_j \in pt(o_i.f)}{o_j \in pt(y)}$$

- ---→ Premises
- --- Conclusion



Rules

---→ Premises

→ Conclusion

Kind	Rule	Illustration
New	$\overline{o_i \in pt(x)}$	i: x = new T()
Assign	$\frac{o_i \in pt(y)}{o_i \in pt(x)}$	x = y
Store	$\frac{o_i \in pt(x), \ o_j \in pt(y)}{o_j \in pt(o_i, f)}$	f o_i f o_j f o_j
Load	$\frac{o_i \in pt(x), \ o_j \in pt(o_i, f)}{o_j \in pt(y)}$	$ \begin{array}{c} o_j \\ y = x.f \end{array} $

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Our Pointer Analysis Algorithms

A complete whole-program pointer analysis

Carefully designed for understandability

Easy to follow and implement

• Essentially, pointer analysis is to **propagate** pointsto information among pointers (variables & fields)

Kind	Statement	Rule
New	i: x = new T()	$\overline{o_i \in pt(x)}$
Assign	x = y	$\frac{o_i \in pt(\mathbf{y})}{o_i \in pt(\mathbf{x})} $
Store	x.f = y	$\frac{o_i \in pt(x), \ o_j \in pt(y)}{o_j \in pt(o_i, f)}$
Load	y = x.f	$o_i \in pt(x), \ o_j \in pt(o_i, f)$ $o_j \in pt(y)$

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Store	x.f = y	$\frac{o_i \in pt(x), \ o_j \in pt(y)}{o_j \in pt(o_i, f)}$
Load	y = x.f	$\frac{o_i \in pt(x), \ o_j \in pt(\mathbf{o_i}, \mathbf{f})}{o_j \in pt(\mathbf{y})}$

Pointer analysis as solving a system of inclusion constraints for pointers

Referred as Andersen-style analysis*

^{*} Lars Ole Andersen, 1994. "Program Analysis and Specialization for the C Programming Language". Ph.D. Thesis. University of Copenhagen.

• Essentially, pointer analysis is to **propagate** pointsto information among pointers (variables & fields)

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New	i: x = new T()	$\overline{o_i \in pt(x)}$
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Store	x.f = y	$\frac{o_i \in pt(x), \ o_j \in pt(\mathbf{y})}{o_j \in pt(\mathbf{o_i}.\mathbf{f})}$
Load	y = x.f	$\frac{o_i \in pt(x), \ o_j \in pt(\mathbf{o_i}.\mathbf{f})}{o_j \in pt(\mathbf{y})}$

Key to implementation: when pt(x) is **changed**, **propagate** the **changed part** to the **related pointers** of x

 Essentially, pointer analysis is to propagate pointsto information among pointers (variables & fields)

Kind	Statement	Rule
New	i: x = new T()	$\overline{o_i \in pt(x)}$
Assign	x = y	$\frac{o_i \in pt(\mathbf{y})}{o_i \in pt(\mathbf{x})} $
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Load	y = x.f	$\frac{o_i \in pt(x), \ o_j \in pt(\mathbf{o_i}, \mathbf{f})}{o_j \in pt(\mathbf{y})}$



Solution

- We use a **graph** to connect related pointers
- When pt(x) changes, propagate the changed part to x's successors

Key to implementation: when pt(x) is **changed**, **propagate** the changed part to the related pointers of x

Pointer Flow Graph (PFG)

Pointer flow graph of a program is a *directed graph* that expresses how objects flow among the pointers in the program.

Pointer Flow Graph (PFG)

Pointer flow graph of a program is a *directed graph* that expresses how objects flow among the pointers in the program.

- Nodes: Pointer = $V \cup (O \times F)$ A node n represents a variable or a field of an abstract object
- Edges: Pointer × Pointer
 An edge x → y means that the objects pointed by pointer x may flow to (and also be pointed to by) pointer y

Pointer Flow Graph: Edges

 PFG edges are added according to the statements of the program and the corresponding rules

Kind	Statement	Rule
New	i: x = new T()	$\overline{o_i \in pt(x)}$
Assign	x = y	$\frac{o_i \in pt(\mathbf{y})}{o_i \in pt(\mathbf{x})}$
Store	x.f = y	$\frac{o_i \in pt(x), \ o_j \in pt(y)}{o_j \in pt(o_i, f)}$
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Pointer Flow Graph: Edges

 PFG edges are added according to the statements of the program and the corresponding rules

Kind	Statement	Rule	PFG Edge
New	i: x = new T()	$\overline{o_i \in pt(x)}$	N/A
Assign	x = y	$\frac{o_i \in pt(\mathbf{y})}{o_i \in pt(\mathbf{x})}$	$x \leftarrow y$
Store	x.f = y	$\frac{o_i \in pt(x), \ o_j \in pt(y)}{o_j \in pt(o_i, f)}$	$o_i.f \leftarrow y$
Load	y = x.f	$o_i \in pt(x), \ o_j \in pt(o_i, f)$ $o_j \in pt(y)$	$y \leftarrow o_i.f$

Program

$$(o_i \in pt(c), o_i \in pt(d))$$

$$a = b;$$

c.f = a;
$$②$$

$$d = c;$$
 (3)

$$c.f = d;$$
 (4)

Pointer flow graph

> Variable node





Program

$$(o_i \in pt(c), o_i \in pt(d))$$

\rightarrow a = b;



c.f = a;
$$②$$

$$d = c;$$
 ③



$$c.f = d;$$
 (4)

Pointer flow graph

➤ Variable node





Program

$$(o_i \in pt(c), o_i \in pt(d))$$

$$\rightarrow$$
 a = b; (1)

c.f = a;
$$②$$

$$d = c;$$

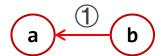
$$c.f = d;$$
 (4)

Pointer flow graph

Variable node







Program

$$(o_i \in pt(c), o_i \in pt(d))$$

$$a = b;$$







$$d = c$$
:



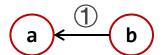
$$c.f = d;$$
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Pointer flow graph

> Variable node







Program

$$(o_i \in pt(c), o_i \in pt(d))$$

$$a = b;$$

(1)

$$d = c;$$

3

$$c.f = d;$$

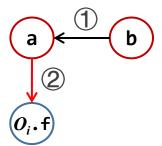
$$e = d.f;$$
 ⑤

Pointer flow graph

Variable node







Program

$$(o_i \in pt(c), o_i \in pt(d))$$

$$a = b;$$

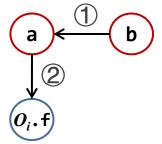
c.f = a;
$$②$$

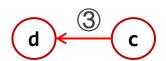
$$\rightarrow$$
 d = c; $\widehat{3}$

$$c.f = d;$$
 (4)

- Variable node
- v
- ➤ Instance field node







Program

$$(o_i \in pt(c), o_i \in pt(d))$$

$$a = b;$$

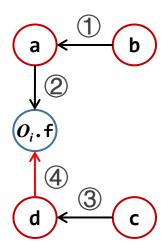
$$d = c;$$
 3

$$\rightarrow$$
 c.f = d; \bigcirc

$$e = d.f;$$
 (5)

- > Variable node
- v
- ➤ Instance field node





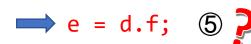
Program

$$(o_i \in pt(c), o_i \in pt(d))$$

$$a = b;$$

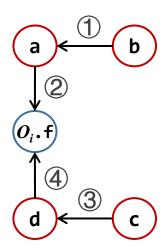
$$d = c;$$

$$c.f = d;$$
 4



- > Variable node
- v
- ➤ Instance field node





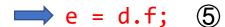
Program

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$$a = b;$$

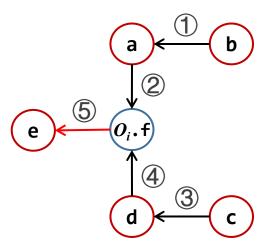
$$d = c;$$

$$c.f = d;$$
 (4)



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Program

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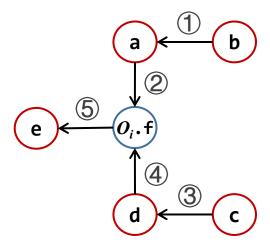
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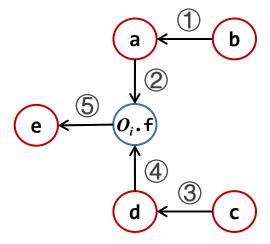
$$c.f = d;$$
 (4)

$$e = d.f; (5)$$

Pointer flow graph

- > Variable node
- v
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With PFG, pointer analysis can be solved by computing *transitive closure* of the PFG

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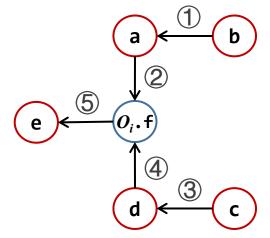
$$c.f = d;$$
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Pointer flow graph

- > Variable node
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With PFG, pointer analysis can be solved by computing *transitive closure* of the PFG

E.g, **e** is reachable from **b** on the PFG, which means that the objects pointed by **b** may flow to and also be pointed by **e**

Program

$$(o_i \in pt(c), o_i \in pt(d))$$

$$\rightarrow$$
 j: b = new T();

$$a = b$$
;

$$d = c;$$

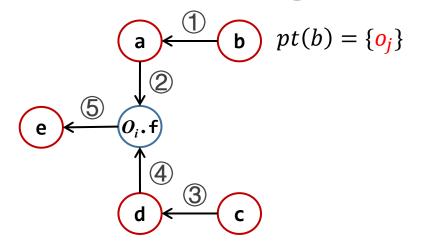
c.f = d;
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Pointer flow graph

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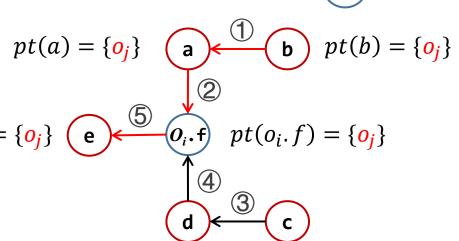
$$c.f = d;$$
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$$e = d.f;$$
 (5)

Pointer flow graph

- Variable node
- v
- > Instance field node

$$(o_i,f)$$



With PFG, pointer analysis can be solved by computing *transitive closure* of the PFG

E.g, **e** is reachable from **b** on the PFG, which means that the objects pointed by **b** may flow to and also be pointed by **e**

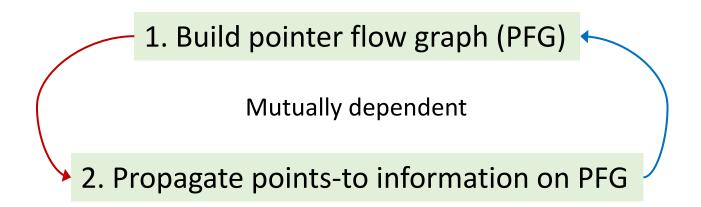
1. Build pointer flow graph (PFG)

2. Propagate points-to information on PFG

1. Build pointer flow graph (PFG)

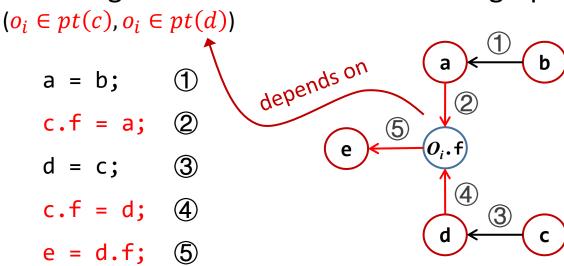
Mutually dependent

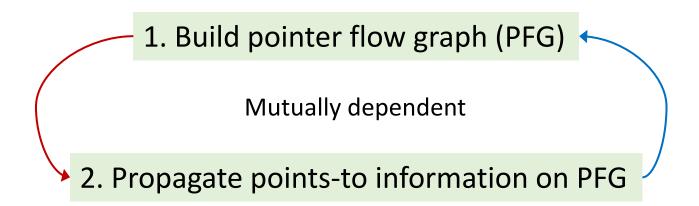
2. Propagate points-to information on PFG



Program

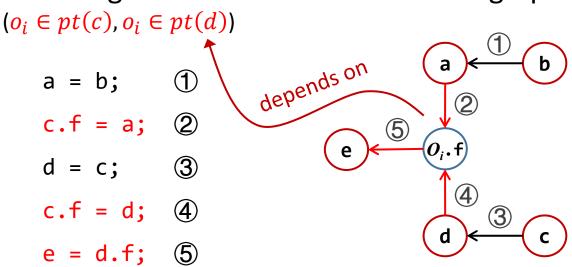
Pointer flow graph





Program

Pointer flow graph



PFG is dynamically updated during pointer analysis

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Pointer Analysis: Algorithms

```
Solve(S)
  WL = [], PFG = {}
  foreach i: x = new T() \in S do
     add \langle x, \{o_i\} \rangle to WL
  foreach x = y \in S do
     AddEdge(y, x)
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
          foreach x.f = y \in S do
             AddEdge(y, o_i, f)
           foreach y = x.f \in S do
             AddEdge(o_i, f, y)
```

```
AddEdge(s, t)

if s \to t \notin PFG then

add s \to t to PFG

if pt(s) is not empty then

add \langle t, pt(s) \rangle to WL
```

```
Propagate(n, pts)

if pts is not empty then

pt(n) \cup = pts

foreach n \rightarrow s \in PFG do

add \langle s, pts \rangle to WL
```

```
Set of statements of the input program

WL Work list

PFG Pointer flow graph
```

Pointer Analysis: Algorithms

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Solve(S)
  WL = [], PFG = \{\}
  foreach i: x = \text{new } T() \in S \text{ do}
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  foreach x = y \in S do
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  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
           for each x.f = y \in S do
              AddEdge(y, o_i, f)
           foreach y = x.f \in S do
              AddEdge(o_i, f, y)
```

```
AddEdge(s, t)
   if s \rightarrow t \notin PFG then
      add s \rightarrow t to PFG
      if pt(s) is not empty then
         add \langle t, pt(s) \rangle to WL
Propagate(n, pts)
   if pts is not empty then
     pt(n) \cup = pts
      foreach n \rightarrow s \in PFG do
         add \langle s, pts \rangle to WL
         Set of statements of
         the input program
  WL
         Work list
 PFG
         Pointer flow graph
```

Pointer Analysis: Algorithms

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Solve(S)
    WL = [], PFG = \{\}
    foreach i: x = new T() \in S do
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    foreach x = y \in S do
       AddEdge(y, x)
\rightarrow while WL is not empty do
       remove \langle n, pts \rangle from WL
       \Delta = pts - pt(n)
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         foreach o_i \in \Delta do
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               AddEdge(y, o_i, f)
            foreach y = x.f \in S do
               AddEdge(o_i, f, y)
```

```
AddEdge(s, t)

if s \rightarrow t \notin PFG then

add s \rightarrow t to PFG

if pt(s) is not empty then

add \langle t, pt(s) \rangle to WL

Propagate(n, pts)

if pts is not empty then

pt(n) \cup = pts
```

foreach $n \rightarrow s \in PFG$ **do**

add $\langle s, pts \rangle$ to WL

```
Set of statements of the input program

WL Work list

PFG Pointer flow graph
```

Worklist (WL)

- Worklist contains the points-to information to be processed
 - $WL \subseteq \langle Pointer, \mathcal{P}(0) \rangle^*$
- Each worklist entry $\langle n, pts \rangle$ is a pair of pointer n and points-to set pts, which means that pts should be propagated to pt(n)
 - E.g., $[\langle x, \{o_i\} \rangle, \langle y, \{o_j, o_k\} \rangle, \langle o_j, f, \{o_l\} \rangle \dots]$

Main Algorithm

```
Solve(S)
  WL = [], PFG = \{\}
  foreach i: x = new T() \in S do
     add \langle x, \{o_i\} \rangle to WL
  foreach x = y \in S do
     AddEdge(y, x)
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
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          foreach y = x.f \in S do
             AddEdge(o_i, f, y)
```

```
Solve(S)

WL = [], PFG = \{\}

foreach i: x = new T() \in S do

Add \langle x, \{o_i\} \rangle to WL

foreach x = y \in S do

AddEdge(y, x)

while WL is not empty do

remove \langle n, pts \rangle from WL

\Delta = pts - pt(n)

Propagate(n, \Delta)
```

Initialize the analysis

Kind	Statement	Rule	PFG Edge
New	i: x = new T()	$\overline{o_i \in pt(x)}$	N/A
Assign	x = y	$\frac{o_i \in pt(\mathbf{y})}{o_i \in pt(\mathbf{x})}$	$x \leftarrow y$

```
Solve(S)
WL = [], PFG = \{\}
foreach i: x = new T() \in S do
add \langle x, \{o_i\} \rangle \text{ to } WL
foreach x = y \in S do
AddEdge(y, x)
while WL is not empty do
remove \langle n, pts \rangle \text{ from } WL
\Delta = pts - pt(n)
Propagate(n, \Delta)
```

Initialize the analysis

Add assign edges to PFG

Kind	Statement	Rule	PFG Edge
New	i: x = new T()	$\overline{o_i \in pt(x)}$	N/A
Assign	x = y	$\frac{o_i \in pt(\mathbf{y})}{o_i \in pt(\mathbf{x})}$	$x \leftarrow y$

```
Solve(S)
WL = [], PFG = \{\}
foreach i: x = \text{new } T() \in S \text{ do}
\text{add } \langle x, \{o_i\} \rangle \text{ to } WL
foreach x = y \in S \text{ do}
\text{AddEdge}(y, x)
```

while WL is not empty **do** remove $\langle n, pts \rangle$ from WL $\Delta = pts - pt(n)$ Propagate (n, Δ)

```
AddEdge(s, t)

if s \rightarrow t \notin PFG then

add s \rightarrow t to PFG

if pt(s) is not empty then

add \langle t, pt(s) \rangle to WL
```

Do nothing if $s \rightarrow t$ is already in PFG

Kind	Statement	Rule	PFG Edge
New	i: x = new T()	$\overline{o_i \in pt(x)}$	N/A
Assign	x = y	$\frac{o_i \in pt(\mathbf{y})}{o_i \in pt(\mathbf{x})}$	$x \leftarrow y$

```
Solve(S)

WL = [], PFG = \{\}

foreach i: x = \text{new T()} \in S \text{ do}

\text{add } \langle x, \{o_i\} \rangle \text{ to } WL

foreach x = y \in S \text{ do}

AddEdge(y, x)
```

```
AddEdge(s, t)

if s \rightarrow t \notin PFG then

add s \rightarrow t to PFG

if pt(s) is not empty then

add \langle t, pt(s) \rangle to WL
```

- ① Do nothing if $s \rightarrow t$ is already in PFG
- 2 Add PFG edge

Kind	Statement	Rule	PFG Edge
New	i: x = new T()	$\overline{o_i \in pt(x)}$	N/A
Assign	x = y	$\frac{o_i \in pt(\mathbf{y})}{o_i \in pt(\mathbf{x})}$	$x \leftarrow y$

```
Solve(S)

WL = [], PFG = \{\}

foreach i: x = new T() \in S do

add \langle x, \{o_i\} \rangle to WL

foreach x = y \in S do

AddEdge(y, x)
```

```
AddEdge(s, t)

if s \to t \notin PFG then

add s \to t to PFG

if pt(s) is not empty then

add \langle t, pt(s) \rangle to WL
```

- ① Do nothing if $s \rightarrow t$ is already in PFG
- 2 Add PFG edge
- **3 Ensure** every object pointed by s is also pointed by t

Kind	Statement	Rule	PFG Edge
New	i: x = new T()	$\overline{o_i \in pt(x)}$	N/A
Assign	x = y	$\frac{o_i \in pt(\mathbf{y})}{o_i \in pt(\mathbf{x})}$	$x \leftarrow y$

```
Solve(S)

WL = [], PFG = \{\}

foreach i: x = new T() \in S do

add \langle x, \{o_i\} \rangle to WL

foreach x = y \in S do

AddEdge(y, x)

while WL is not empty do

remove \langle n, pts \rangle from WL

\Delta = pts - pt(n)

Propagate(n, \Delta)
```

Process the entries in WL

Kind	Statement	Rule	PFG Edge
New	i: x = new T()	$\overline{o_i \in pt(x)}$	N/A
Assign	x = y	$\frac{o_i \in pt(\mathbf{y})}{o_i \in pt(\mathbf{x})}$	$x \leftarrow y$

```
Solve(S)

WL = [], PFG = \{\}

foreach i: x = new T() \in S do

Add \langle x, \{o_i\} \rangle to WL

foreach x = y \in S do

AddEdge(y, x)

while WL is not empty do

Color Peropeople (n, pts) from WL

Color Peropeople (n, \Delta)
```

remove
$$\langle x, \{o_1, o_3\} \rangle$$
 from WL
 $pt(x) = \{o_1, o_2\}$
 $\Delta = pts - pt(x)$
 $= \{o_1, o_3\} - \{o_1, o_2\}$
 $= \{o_3\}$

Propagate $(x, \{o_3\})$

Process the entries in WL

Kind	Statement	Rule	PFG Edge
New	i: x = new T()	$\overline{o_i \in pt(x)}$	N/A
Assign	x = y	$\frac{o_i \in pt(\mathbf{y})}{o_i \in pt(\mathbf{x})}$	$x \leftarrow y$

```
Solve(S)
WL = [], PFG = \{\}
foreach i: x = \text{new } T() \in S \text{ do}
\text{add } \langle x, \{o_i\} \rangle \text{ to } WL
foreach x = y \in S \text{ do}
\text{AddEdge}(y, x)
```

```
Propagate(n, pts)

if pts is not empty then

pt(n) \cup = pts

foreach n \rightarrow s \in PFG do

add \langle s, pts \rangle to WL
```

Do nothing if *pts* is empty

1.1	opagare(n, \(\Delta\)		
Kind	Statement	Rule	PFG Edge
New	i: x = new T()	$\overline{o_i \in pt(x)}$	N/A
Assign	x = y	$\frac{o_i \in pt(\mathbf{y})}{o_i \in pt(\mathbf{x})}$	$x \leftarrow y$

```
Solve(S)

WL = [], PFG = \{\}

foreach i: x = new T() \in S do

add \langle x, \{o_i\} \rangle to WL

foreach x = y \in S do

AddEdge(y, x)
```

```
Propagate(n, pts)

if pts is not empty then

pt(n) \cup = pts
foreach \ n \rightarrow s \in PFG \ do
add \ \langle s, pts \rangle \text{ to } WL
```

- ① Do nothing if pts is empty
- $\widehat{2}$ Propagate pts to points-to set of n

Kind	Statement	Rule	PFG Edge
New	i: x = new T()	$\overline{o_i \in pt(x)}$	N/A
Assign	x = y	$\frac{o_i \in pt(\mathbf{y})}{o_i \in pt(\mathbf{x})}$	$x \leftarrow y$

```
Solve(S)

WL = [], PFG = \{\}

foreach i: x = new T() \in S do

add \langle x, \{o_i\} \rangle to WL

foreach x = y \in S do

AddEdge(y, x)
```

```
Propagate(n, pts)

if pts is not empty then

pt(n) \cup = pts
foreach \ n \rightarrow s \in PFG \ do
add \ \langle s, pts \rangle \text{ to } WL
```

- ① Do nothing if pts is empty
- ② Propagate pts to points-to set of n

Kind	Statement	Rule	PFG Edge
New	i: x = new T()	$\overline{o_i \in pt(x)}$	N/A
Assign	x = y	$\frac{o_i \in pt(\mathbf{y})}{o_i \in pt(\mathbf{x})}$	$x \leftarrow y$

```
Solve(S)
...

while WL is not empty do
remove \langle n, pts \rangle from WL
\Delta = pts - pt(n)
Propagate(n, \Delta)
...
```

Why?

- Differential propagation is employed to avoid propagation and processing of redundant points-to information
- Insight: existing points-to information in pt(n) have already been propagated to n's successors, and **no need** to be propagated again

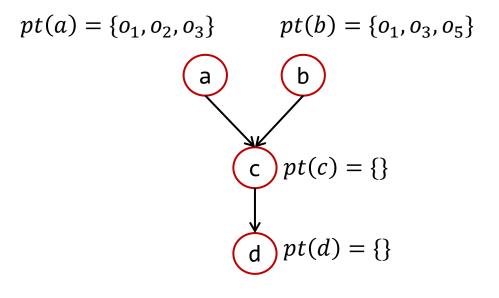
```
Solve(S)
...

while WL is not empty do
remove \langle n, pts \rangle from WL
\Delta = pts - pt(n)
Propagate(n, \Delta)
...
```

- Differential propagation is employed to avoid propagation and processing of redundant points-to information
- Insight: existing points-to information in pt(n) have already been propagated to n's successors, and no need to be propagated again

```
Solve(S)
...

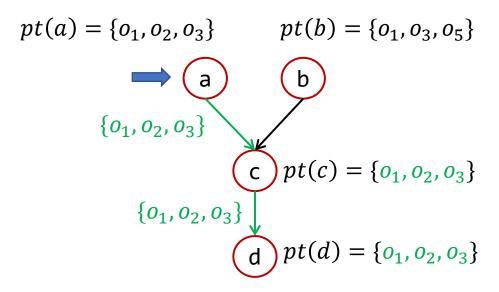
while WL is not empty do
remove \langle n, pts \rangle from WL
\Delta = pts - pt(n)
Propagate(n, \Delta)
...
```



- Differential propagation is employed to avoid propagation and processing of redundant points-to information
- Insight: existing points-to information in pt(n) have already been propagated to n's successors, and no need to be propagated again

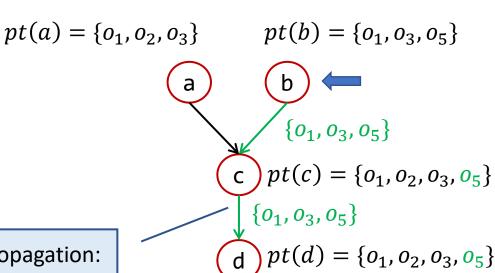
```
Solve(S)
...

while WL is not empty do
remove \langle n, pts \rangle from WL
\Delta = pts - pt(n)
Propagate(n, \Delta)
...
```



- **Differential propagation** is employed to avoid propagation and processing of redundant points-to information
- **Insight**: existing points-to information in pt(n) have already been propagated to n's successors, and **no need** to be propagated again

```
Solve(S)
   while WL is not empty do
      remove \langle n, pts \rangle from WL
      \Delta = pts - pt(n)
      Propagate(n, \Delta)
```



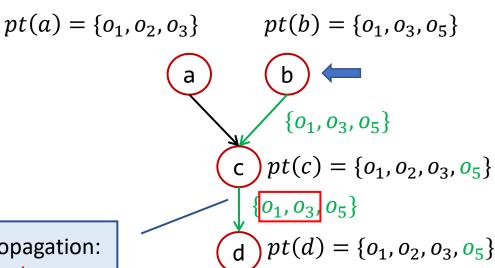
Direct propagation:

PFG

- Differential propagation is employed to avoid propagation and processing of redundant points-to information
- Insight: existing points-to information in pt(n) have already been propagated to n's successors, and no need to be propagated again

```
Solve(S)
...

while WL is not empty do
remove \langle n, pts \rangle from WL
\Delta = pts - pt(n)
Propagate(n, \Delta)
...
```



Direct propagation: redundant

- Differential propagation is employed to avoid propagation and processing of redundant points-to information
- Insight: existing points-to information in pt(n) have already been propagated to n's successors, and **no need** to be propagated again

```
Solve(S)
...

while WL is not empty do

remove \langle n, pts \rangle from WL
\Delta = pts - pt(n)
Propagate(n, \Delta)
...
```

$$pt(a) = \{o_1, o_2, o_3\} \qquad pt(b) = \{o_1, o_3, o_5\}$$

$$\{o_1, o_3, o_5\}$$

$$c \qquad pt(c) = \{o_1, o_2, o_3, o_5\}$$

In practice, Δ is usually small compared with the original set, so propagating only the new points-to information (Δ) improves efficiency

Differential propagation:

$$\Delta = pts - pt(c)$$
= $\{o_1, o_3, o_5\} - \{o_1, o_2, o_3\}$
= $\{o_5\}$

d
$$pt(d) = \{o_1, o_2, o_3, o_5\}$$

PFG 63

- *Differential propagation* is employed to avoid propagation and processing of redundant points-to information
- Insight: existing points-to information in pt(n) have already been propagated to n's successors, and **no need** to be propagated again

```
Solve(S)
...

while WL is not empty do

remove \langle n, pts \rangle from WL
\Delta = pts - pt(n)
Propagate(n, \Delta)
...
```

$$pt(a) = \{o_1, o_2, o_3\} \qquad pt(b) = \{o_1, o_3, o_5\}$$

$$\{o_1, o_3, o_5\}$$

$$c \qquad pt(c) = \{o_1, o_2, o_3, o_5\}$$

Besides, Δ is also important for efficiency when handling stores, loads, and method calls, as explained later

Differential propagation: $\Delta = pts - pt(c)$

$$= \{o_1, o_3, o_5\} - \{o_1, o_2, o_3\}$$
$$= \{o_5\}$$

PFG

64

```
Solve(S)

WL = [], PFG = \{\}

foreach i: x = new T() \in S do

add \langle x, \{o_i\} \rangle to WL

foreach x = y \in S do

AddEdge(y, x)

while WL is not empty do

remove \langle n, pts \rangle from WL

\Delta = pts - pt(n)

Propagate(n, \Delta)
```

Kind	Statement	Rule	PFG Edge
New	i: x = new T()	$\overline{o_i \in pt(x)}$	N/A
Assign	x = y	$\frac{o_i \in pt(\mathbf{y})}{o_i \in pt(\mathbf{x})}$	$x \leftarrow y$

Handling of Store and Load

```
Solve(S)

...

while WL is not empty do

remove \langle n, pts \rangle from WL

\Delta = pts - pt(n)

Propagate(n, \Delta)

if n represents a variable x then

foreach o_i \in \Delta do

foreach x \cdot f = y \in S do

AddEdge(y, o_i, f)

foreach y = x \cdot f \in S do

AddEdge(o_i, f, y)
```

Kind	Statement	Rule	PFG Edge
Store	x.f = y	$\frac{o_i \in pt(\boldsymbol{x}), \ o_j \in pt(\boldsymbol{y})}{o_j \in pt(\boldsymbol{o_i}, \boldsymbol{f})}$	$o_i.f \leftarrow y$
Load	y = x.f	$\frac{o_i \in pt(\boldsymbol{x}), \ o_j \in pt(\boldsymbol{o_i}, \boldsymbol{f})}{o_j \in pt(\boldsymbol{y})}$	$y \leftarrow o_i.f$

Handling of Store and Load

```
Solve(S)

...

while WL is not empty do

remove \langle n, pts \rangle from WL

\Delta = pts - pt(n)
Propagate(n, \Delta)
```

```
if n represents a variable x then foreach o_i \in \Delta do foreach x \cdot f = y \in S do AddEdge(y, o_i, f) foreach y = x \cdot f \in S do AddEdge(o_i, f, y)
```

```
AddEdge(s, t)

if s \rightarrow t \notin PFG then

add s \rightarrow t to PFG

if pt(s) is not empty then

add \langle t, pt(s) \rangle to WL
```

New points-to information may introduce new PFG edges

Kind	Statement	Rule	PFG Edge
Store	x.f = y	$\frac{o_i \in pt(\boldsymbol{x}), \ o_j \in pt(\boldsymbol{y})}{o_j \in pt(\boldsymbol{o_i}, \boldsymbol{f})}$	$o_i.f \leftarrow y$
Load	y = x.f	$\frac{o_i \in pt(\mathbf{x}), \ o_j \in pt(\mathbf{o_i}, \mathbf{f})}{o_j \in pt(\mathbf{y})}$	$y \leftarrow o_i.f$

Algorithms: Review

```
Solve(S)
  WL = [], PFG = \{\}
  foreach i: x = new T() \in S do
     add \langle x, \{o_i\} \rangle to WL
  foreach x = y \in S do
     AddEdge(y, x)
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
          for each x.f = y \in S do
             AddEdge(y, o_i, f)
           foreach y = x.f \in S do
             AddEdge(o_i, f, y)
```

```
AddEdge(s, t)

if s \rightarrow t \notin PFG then

add s \rightarrow t to PFG

if pt(s) is not empty then

add \langle t, pt(s) \rangle to WL

Propagate(n, pts)

if pts is not empty then

pt(n) \cup = pts
```

foreach $n \rightarrow s \in PFG$ **do**

add $\langle s, pts \rangle$ to WL

```
Set of statements of the input program

WL Work list

PFG Pointer flow graph
```

```
S:
Solve(S)
\rightarrow WL = [], PFG = \{\}
  foreach i: x = \text{new } T() \in S \text{ do}
      add \langle x, \{o_i\} \rangle to WL
                                                WL: []
  foreach x = y \in S do
     AddEdge(y, x)
   while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
      if n represents a variable x then
                                               PFG:
        foreach o_i \in \Delta do
           for each x.f = y \in S do
              AddEdge(y, o_i, f)
           foreach y = x.f \in S do
              AddEdge(o_i, f, y)
```

1 b = new C(); 2 a = b;3 c = new C();4 c.f = a;5 d = c;6 c.f = d;7 e = d.f;

```
Solve(S)
  WL = [], PFG = \{\}
\Rightarrow foreach i: x = \text{new } T() \in S \text{ do}
     add \langle x, \{o_i\} \rangle to WL
  foreach x = y \in S do
     AddEdge(y, x)
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
           for each x.f = y \in S do
              AddEdge(y, o_i, f)
           foreach y = x.f \in S do
              AddEdge(o_i, f, y)
```

```
1 b = new C();

2 a = b;

3 c = new C();

4 c.f = a;

5 d = c;

6 c.f = d;

7 e = d.f;
```

WL: $[\langle b, \{o_1\} \rangle, \langle c, \{o_3\} \rangle]$

PFG:

```
Solve(S)
  WL = [], PFG = \{\}
  foreach i: x = new T() \in S do
     add \langle x, \{o_i\} \rangle to WL
 foreach x = y \in S do
     AddEdge(y, x)
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
          for each x.f = y \in S do
             AddEdge(y, o_i, f)
          foreach y = x.f \in S do
             AddEdge(o_i, f, y)
```

```
1 b = new C();

2 a = b;

3 c = new C();

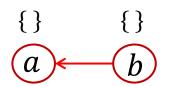
4 c.f = a;

5 d = c;

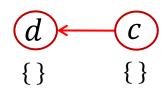
6 c.f = d;

7 e = d.f;
```

WL: $[\langle b, \{o_1\}\rangle, \langle c, \{o_3\}\rangle]$



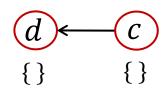
PFG:



```
Solve(S)
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
          foreach x.f = y \in S do
             AddEdge(y, o_i, f)
           foreach y = x.f \in S do
             AddEdge(o_i, f, y)
```

```
1 b = new C();
                 2 a = b;
                 3 c = new C();
 S:
                 4 c.f = a;
                 5 d = c;
                 6 c.f = d;
                 7 e = d.f;
WL: [\langle c, \{o_3\} \rangle]
Processing: \langle b, \{o_1\} \rangle
```

PFG:

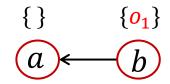


```
Solve(S)
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
           foreach x.f = y \in S do
             AddEdge(y, o_i, f)
           foreach y = x.f \in S do
             AddEdge(o_i, f, y)
```

```
1 b = new C();
            2 a = b;
            3 c = new C();
S:
           4 c.f = a;
           5 d = c;
           6 c.f = d;
            7 e = d.f;
```

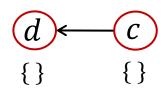
 $WL: [\langle c, \{o_3\} \rangle]$

Processing: $\langle b, \{o_1\} \rangle$



PFG:

Propagate(n, pts)if pts is not empty then $pt(n) \cup = pts$ foreach $n \rightarrow s \in PFG$ do add $\langle s, pts \rangle$ to WL



```
Solve(S)
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
           foreach x.f = y \in S do
             AddEdge(y, o_i, f)
           foreach y = x.f \in S do
             AddEdge(o_i, f, y)
```

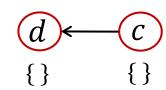
```
1 b = new C();
                      2 a = b;
                      3 c = new C();
  S:
                     4 c.f = a;
                      5 d = c;
                      6 c.f = d;
                      7 e = d.f;
WL: \left[\langle c, \{o_3\} \rangle, \langle a, \{o_1\} \rangle\right]
Processing: \langle b, \{o_1\} \rangle
                                       {0<sub>1</sub>}
```

PFG:

Propagate(n, pts)

if pts is not empty then $pt(n) \cup = pts$ foreach $n \rightarrow s \in PFG$ do

add $\langle s, pts \rangle$ to WLTian T



```
Solve(S)
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
          foreach x.f = y \in S do
             AddEdge(y, o_i, f)
           foreach y = x.f \in S do
             AddEdge(o_i, f, y)
```

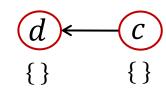
```
1 b = new C();
                   2 a = b;
                   3 c = new C();
 S:
                  4 c.f = a;
                  5 d = c;
                  6 \text{ c.f} = d;
                   7 e = d.f;
WL: [\langle a, \{o_1\}\rangle]
Processing: \langle c, \{o_3\} \rangle
                                  \{o_1\}
```

PFG:

Propagate(n, pts)

if pts is not empty then $pt(n) \cup = pts$ foreach $n \rightarrow s \in PFG$ do

add $\langle s, pts \rangle$ to WLTian Tan G



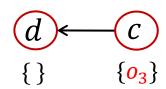
```
Solve(S)
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
           foreach x.f = y \in S do
             AddEdge(y, o_i, f)
           foreach y = x.f \in S do
             AddEdge(o_i, f, y)
```

```
1 b = new C();
                   2 a = b;
                   3 c = new C();
 S:
                  4 c.f = a;
                  5 d = c;
                  6 \text{ c.f} = d;
                   7 e = d.f;
WL: [\langle a, \{o_1\}\rangle]
Processing: \langle c, \{o_3\} \rangle
                                  \{o_1\}
```

PFG:

Propagate(n, pts)

if pts is not empty then $pt(n) \bigcup = pts$ foreach $n \to s \in PFG$ do
add $\langle s, pts \rangle$ to WLTian Tar



```
Solve(S)
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
           foreach x.f = y \in S do
             AddEdge(y, o_i, f)
           foreach y = x.f \in S do
             AddEdge(o_i, f, y)
```

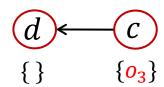
```
1 b = new C();
                     2 a = b;
                     3 c = new C();
  S:
                    4 c.f = a;
                     5 d = c;
                    6 \text{ c.f} = d;
                     7 e = d.f;
WL: [\langle a, \{o_1\} \rangle, \langle d, \{o_3\} \rangle]
Processing: \langle c, \{o_3\} \rangle
                                     \{o_1\}
```

PFG:

Propagate(n, pts)

if pts is not empty then $pt(n) \cup = pts$ foreach $n \rightarrow s \in PFG$ do

add $\langle s, pts \rangle$ to WL



```
Solve(S)
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
           for each x.f = y \in S do
             AddEdge(y, o_i, f)
           foreach y = x.f \in S do
             AddEdge(o_i, f, y)
```

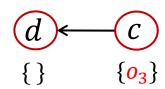
```
1 b = new C();
                    2 a = b;
                    3 c = new C();
  S:
                    4 c.f = a;
                    5 d = c;
                    6 \text{ c.f} = d;
                    7 e = d.f;
WL: [\langle a, \{o_1\} \rangle, \langle d, \{o_3\} \rangle]
Processing: \langle c, \{o_3\} \rangle
                                    \{o_1\}
What next?
```

PFG:

Propagate(n, pts)

if pts is not empty then $pt(n) \cup = pts$ foreach $n \rightarrow s \in PFG$ do

add $\langle s, pts \rangle$ to WL Tian Tan @ Nanjing University



```
Solve(S)
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
           foreach x.f = y \in S do
             AddEdge(y, o_i, f)
           foreach y = x.f \in S do
             AddEdge(o_i, f, y)
```

```
AddEdge(s, t)

if s \to t \notin PFG then

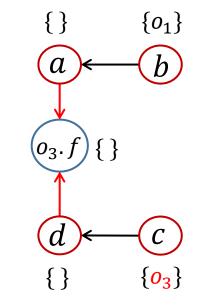
\Rightarrow add s \to t to PFG

if pt(s) is not empty then

add \langle t, pt(s) \rangle to WL Tian Tan @ Nanjing University
```

WL: $[\langle a, \{o_1\} \rangle, \langle d, \{o_3\} \rangle]$

Processing: $\langle c, \{o_3\} \rangle$



```
Solve(S)
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
           foreach x.f = y \in S do
             AddEdge(y, o_i, f)
           foreach y = x.f \in S do
             AddEdge(o_i, f, y)
```

```
Propagate(n, pts)

if pts is not empty then

pt(n) \cup = pts

foreach n \to s \in PFG do

add \langle s, pts \rangle to WL Tian Tan @ Nanjing University
```

```
1 b = new C();

2 a = b;

3 c = new C();

4 c.f = a;

5 d = c;

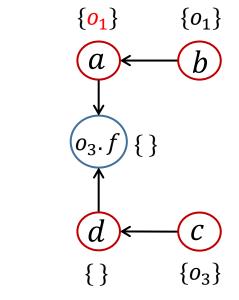
6 c.f = d;

7 e = d.f;
```

WL: $[\langle d, \{o_3\}\rangle]$

PFG:

Processing: $\langle a, \{o_1\} \rangle$



```
Solve(S)
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
           foreach x.f = y \in S do
             AddEdge(y, o_i, f)
           foreach y = x.f \in S do
             AddEdge(o_i, f, y)
```

```
Propagate(n, pts)

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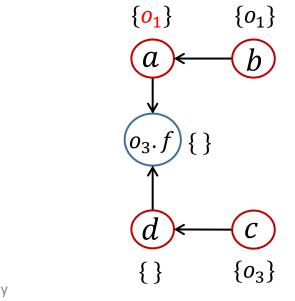
5 d = c;

6 c.f = d;

7 e = d.f;
```

WL: $[\langle d, \{o_3\} \rangle, \langle o_3, f, \{o_1\} \rangle]$

Processing: $\langle a, \{o_1\} \rangle$



```
Solve(S)
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
     if n represents a variable x then
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             AddEdge(y, o_i, f)
           foreach y = x.f \in S do
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```

```
Propagate(n, pts)

if pts is not empty then

pt(n) \bigcup = pts

foreach n \to s \in PFG do

add \langle s, pts \rangle to WL Tian Tan @ Nanjing University
```

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4 c.f = a;

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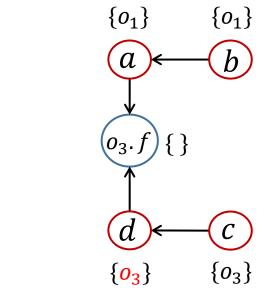
6 c.f = d;

7 e = d.f;
```

WL: $[\langle o_3.f, \{o_1\}\rangle]$

PFG:

Processing: $\langle d, \{o_3\} \rangle$



```
Solve(S)
  while WL is not empty do
     remove \langle n, pts \rangle from WL
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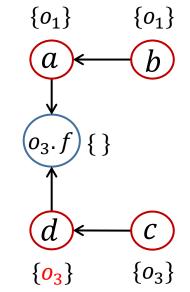
6 c.f = d;

7 e = d.f;
```

WL: $[\langle o_3, f, \{o_1\} \rangle]$

Processing: $\langle d, \{o_3\} \rangle$

What next?



```
Solve(S)
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
           foreach x.f = y \in S do
             AddEdge(y, o_i, f)
           foreach y = x.f \in S do
             AddEdge(o_i, f, y)
```

```
Propagate(n, pts)

if pts is not empty then

pt(n) \bigcup = pts
foreach n \to s \in PFG do

add \langle s, pts \rangle to WL Tian Tan @ Nanjing University
```

```
1 b = new C();

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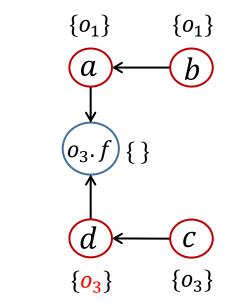
5 d = c;

6 c.f = d;

7 e = d.f;
```

WL: $[\langle o_3, f, \{o_1\} \rangle, \langle o_3, f, \{o_3\} \rangle]$

Processing: $\langle d, \{o_3\} \rangle$



```
Solve(S)
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
           foreach x.f = y \in S do
             AddEdge(y, o_i, f)
           foreach y = x.f \in S do
             AddEdge(o_i, f, y)
```

```
Propagate(n, pts)

if pts is not empty then

pt(n) \cup = pts
foreach n \to s \in PFG do

add \langle s, pts \rangle to WL Tian Tan @ Nanjing University
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```
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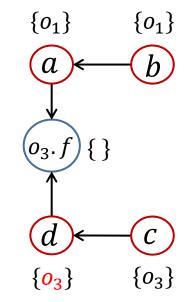
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7 e = d.f;
```

WL: $[\langle o_3, f, \{o_1\} \rangle, \langle o_3, f, \{o_3\} \rangle]$

Processing: $\langle d, \{o_3\} \rangle$

What next?



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     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
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        foreach o_i \in \Delta do
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           foreach y = x.f \in S do
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```

```
AddEdge(s, t)

if s \to t \notin PFG then

add s \to t to PFG

if pt(s) is not empty then

add \langle t, pt(s) \rangle to WL Tian Tan @ Nanjing University
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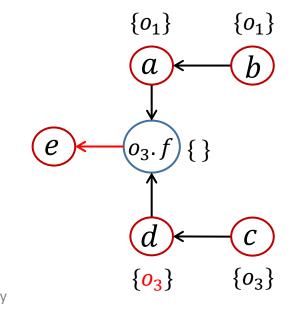
5 d = c;

6 c.f = d;

7 e = d.f;
```

WL: $[\langle o_3, f, \{o_1\} \rangle, \langle o_3, f, \{o_3\} \rangle]$

Processing: $\langle d, \{o_3\} \rangle$



```
Solve(S)
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
           foreach x.f = y \in S do
             AddEdge(y, o_i, f)
           foreach y = x.f \in S do
             AddEdge(o_i, f, y)
```

```
Propagate(n, pts)

if pts is not empty then

pt(n) \cup = pts

foreach n \to s \in PFG do

add \langle s, pts \rangle to WL Tian Tan @ Nanjing University
```

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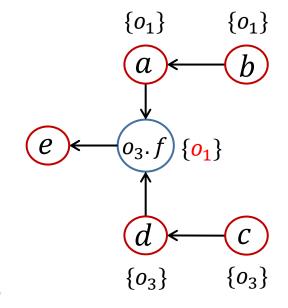
5 d = c;

6 c.f = d;

7 e = d.f;
```

WL: $[\langle o_3, f, \{o_3\} \rangle, \langle e, \{o_1\} \rangle]$

Processing: $\langle o_3, f, \{o_1\} \rangle$



```
Solve(S)
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
           foreach x.f = y \in S do
             AddEdge(y, o_i, f)
           foreach y = x.f \in S do
             AddEdge(o_i, f, y)
```

```
Propagate(n, pts)

if pts is not empty then

pt(n) \cup = pts

foreach n \rightarrow s \in PFG do

add \langle s, pts \rangle to WL Tian Tan @ Nanjing University
```

```
1 b = new C();

2 a = b;

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5 d = c;

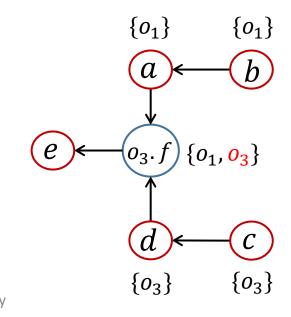
6 c.f = d;

7 e = d.f;
```

WL: $[\langle e, \{o_1\}\rangle, \langle e, \{o_3\}\rangle]$

PFG:

Processing: $\langle o_3, f, \{o_3\} \rangle$



```
Solve(S)
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
           foreach x.f = y \in S do
             AddEdge(y, o_i, f)
           foreach y = x.f \in S do
             AddEdge(o_i, f, y)
```

```
Propagate(n, pts)

if pts is not empty then

pt(n) \cup = pts

foreach n \rightarrow s \in PFG do

add \langle s, pts \rangle to WL Tian Tan @ Nanjing University
```

```
1 b = new C();

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4 c.f = a;

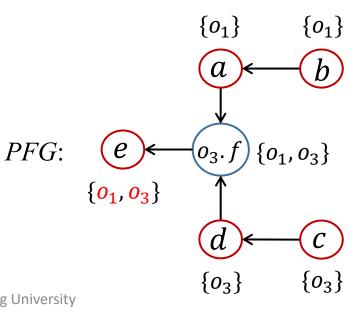
5 d = c;

6 c.f = d;

7 e = d.f;
```

WL: []

Processing: $\langle e, \{o_1\} \rangle, \langle e, \{o_3\} \rangle$



```
Solve(S)
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
           foreach x.f = y \in S do
             AddEdge(y, o_i, f)
           foreach y = x.f \in S do
             AddEdge(o_i, f, y)
```

```
Propagate(n, pts)

if pts is not empty then

pt(n) \cup = pts

foreach n \rightarrow s \in PFG do

add \langle s, pts \rangle to WL Tian Tan @ Nanjing University
```

```
1 b = new C();

2 a = b;

3 c = new C();

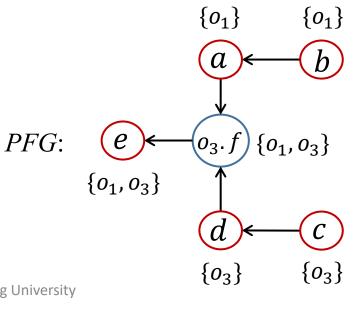
4 c.f = a;

5 d = c;

6 c.f = d;

7 e = d.f;
```

WL: []



Algorithms: Review

```
Solve(S)
  WL = [], PFG = {}
  foreach i: x = new T() \in S do
     add \langle x, \{o_i\} \rangle to WL
  foreach x = y \in S do
     AddEdge(y, x)
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
          for each x.f = y \in S do
             AddEdge(y, o_i, f)
          foreach y = x.f \in S do
             AddEdge(o_i, f, y)
```

```
AddEdge(s, t)
   if s \rightarrow t \notin PFG then
      add s \rightarrow t to PFG
      if pt(s) is not empty then
         add \langle t, pt(s) \rangle to WL
Propagate(n, pts)
   if pts is not empty then
      pt(n) \cup = pts
      foreach n \rightarrow s \in PFG do
         add \langle s, pts \rangle to WL
          Set of statements of
         the input program
  WL
         Work list
```

Pointer flow graph

PFG

The X You Need To Understand in This Lecture

- Understand pointer analysis rules
- Understand pointer flow graph
- Understand pointer analysis algorithms

注意注意! 划重点了!



Static Program Analysis

Pointer Analysis Foundations (II)

Nanjing University

Tian Tan

2020

Contents

- 1. Pointer Analysis: Rules
- 2. How to Implement Pointer Analysis
- 3. Pointer Analysis: Algorithms
- 4. Pointer Analysis with Method Calls

Pointer Analysis in the Presence of Method Invocations

Inter-procedural pointer analysis requires call graph

Pointer Analysis in the Presence of Method Invocations

Inter-procedural pointer analysis requires call graph

CHA: resolve call targets based on declared type of a

- Call graph construction
 - >CHA: imprecise, introduce spurious call graph edges and points-to relations

Pointer Analysis in the Presence of Method Invocations

Inter-procedural pointer analysis requires call graph

CHA: resolve call targets based on declared type of a

Pointer analysis: resolve call targets based on pt(a)

- Call graph construction
 - ➤ CHA: imprecise, introduce spurious call graph edges and points-to relations
 - ▶ Pointer analysis: more precise than CHA, both for call graph and points-to relations
 a.k.a on-the-fly call graph construction

Kind	Statement	Rule
Call	l: r = x.k(a1,,an)	$o_{i} \in pt(x), \ m = \underset{o_{u} \in pt(aj), 1 \leq j \leq n}{\text{Dispatch}(o_{i}, k)}$ $o_{u} \in pt(aj), 1 \leq j \leq n$ $o_{v} \in pt(m_{ret})$ $o_{i} \in pt(m_{this})$ $o_{u} \in pt(m_{pj}), 1 \leq j \leq n$ $o_{v} \in pt(r)$

Kind	Statement	Rule
Call	l: r = x.k(a1,,an)	$o_{i} \in pt(\mathbf{x}), \ m = \underset{o_{u} \in pt(aj), 1 \leq j \leq n}{Dispatch(o_{i}, k)}$ $o_{u} \in pt(aj), 1 \leq j \leq n$ $o_{v} \in pt(m_{ret})$ $o_{i} \in pt(m_{this})$ $o_{u} \in pt(m_{pj}), 1 \leq j \leq n$ $o_{v} \in pt(r)$

• Dispatch (o_i, k) : resolves the virtual dispatch of k on o_i to a target method (based on type of o_i)

Kind	Statement	Rule
Call	l: r = x.k(a1,,an)	$o_{i} \in pt(\mathbf{x}), \ m = \text{Dispatch}(o_{i}, \mathbf{k})$ $o_{u} \in pt(aj), 1 \leq j \leq n$ $o_{v} \in pt(m_{ret})$ $o_{i} \in pt(\mathbf{m}_{this})$ $o_{u} \in pt(m_{pj}), 1 \leq j \leq n$ $o_{v} \in pt(r)$

- Dispatch (o_i, k) : resolves the virtual dispatch of k on o_i to a target method (based on type of o_i)
- m_{this} : this variable of m

Kind	Statement	Rule
Call	l: r = x.k(a1,,an)	$o_{i} \in pt(\mathbf{x}), \ m = \text{Dispatch}(o_{i}, \mathbf{k})$ $o_{u} \in pt(aj), 1 \leq j \leq n$ $o_{v} \in pt(m_{ret})$ $o_{i} \in pt(\mathbf{m}_{this})$ $o_{u} \in pt(m_{pj}), 1 \leq j \leq n$ $o_{v} \in pt(r)$

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- Dispatch (o_i, k) : resolves the virtual dispatch of k on o_i to a target method (based on type of o_i)
- m_{this} : this variable of m
- m_{pj} : the *j*-th parameter of m

Kind	Statement	Rule	PFG Edge
Call	l: r = x.k(a1,,an)	$o_{i} \in pt(x), \ m = \text{Dispatch}(o_{i}, k)$ $o_{u} \in pt(aj), 1 \leq j \leq n$ $o_{v} \in pt(m_{ret})$ $o_{i} \in pt(m_{this})$ $o_{u} \in pt(m_{pj}), 1 \leq j \leq n$ $o_{v} \in pt(r)$	$a1 \rightarrow m_{p1}$ $an \rightarrow m_{pn}$

- Dispatch (o_i, k) : resolves the virtual dispatch of k on o_i to a target method (based on type of o_i)
- m_{this} : this variable of m
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Kind	Statement	Rule	PFG Edge
Call	l: r = x.k(a1,,an)	$o_{i} \in pt(x), \ m = \underset{o_{u} \in pt(aj), 1 \leq j \leq n}{Dispatch(o_{i}, k)}$ $o_{u} \in pt(aj), 1 \leq j \leq n$ $o_{v} \in pt(m_{ret})$ $o_{i} \in pt(m_{this})$ $o_{u} \in pt(m_{pj}), 1 \leq j \leq n$ $o_{v} \in pt(r)$	$a1 \to m_{p1}$ $an \to m_{pn}$

- Dispatch (o_i, k) : resolves the virtual dispatch of k on o_i to a target method (based on type of o_i)
- m_{this} : this variable of m
- m_{pj} : the *j*-th parameter of m
- m_{ret} : the variable that holds the return value of m

Kind	Statement	Rule	PFG Edge
Call	l: r = x.k(a1,,an)	$o_{i} \in pt(x), \ m = \text{Dispatch}(o_{i}, k)$ $o_{u} \in pt(aj), 1 \leq j \leq n$ $o_{v} \in pt(m_{ret})$ $o_{i} \in pt(m_{this})$ $o_{u} \in pt(m_{pj}), 1 \leq j \leq n$ $o_{v} \in pt(r)$	$a1 \rightarrow m_{p1}$ $an \rightarrow m_{pn}$ $r \leftarrow m_{ret}$

- $Dispatch(o_i, k)$: resolves the virtual dispatch of k on o_i to a target method (based on type of o_i)
- m_{this} : this variable of m
- m_{pj} : the *j*-th parameter of m
- m_{ret} : the variable that holds the return value of m

```
C x = new T();
r = x.foo(a1, a2);
  B foo(A p1, A p2) {
  '≯this...
    return ret;
                     105
```

Why not add PFG edge $x \rightarrow m_{this}$

_	
this	
I.N.I.S	

Kind	Statement	Rule	PFG Edge
Call	l: r = x.k(a1,,an)	$o_{i} \in pt(x), \ m = \underset{o_{u} \in pt(aj), 1 \leq j \leq n}{Dispatch(o_{i}, k)}$ $o_{u} \in pt(aj), 1 \leq j \leq n$ $o_{v} \in pt(m_{ret})$ $o_{i} \in pt(m_{this})$ $o_{u} \in pt(m_{pj}), 1 \leq j \leq n$ $o_{v} \in pt(r)$	$a1 \rightarrow m_{p1}$ $$ $an \rightarrow m_{pn}$ $r \leftarrow m_{ret}$

- Dispatch (o_i, k) : resolves the virtual dispatch of k on o_i to a target method (based on type of o_i)
- m_{this} : this variable of m
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- m_{ret} : the variable that holds the return value of m

```
C x = new T();
```

```
r = x.foo(a1, a2);

class T ... { ...

B foo(A p1, A p2) {

this...

return ret;
}}
```

Why not add PFG edge $x \rightarrow m_{this}$



Kind	Statement	Rule	PFG Edge
Call	l: r = x.k(a1,,an)	$o_{i} \in pt(x), \ m = \underset{o_{u} \in pt(aj), 1 \leq j \leq n}{Dispatch(o_{i}, k)}$ $o_{u} \in pt(aj), 1 \leq j \leq n$ $o_{v} \in pt(m_{ret})$ $o_{i} \in pt(m_{this})$ $o_{u} \in pt(m_{pj}), 1 \leq j \leq n$ $o_{v} \in pt(r)$	$a1 \rightarrow m_{p1}$ $$ $an \rightarrow m_{pn}$ $r \leftarrow m_{ret}$

```
{ new A,
pt(x) = \text{new B},
          new C }
x.foo();
```

```
class A {
 T foo() {
    this...
  }}
```

```
class B extends A {
 T foo() {
    this...?
```

```
class C extends A {
 T foo() {
    this...
  }}
```

Why not add PFG edge $x \rightarrow m_{this}$



Kind	Statement	Rule	PFG Edge
Call	l: r = x.k(a1,,an)	$o_{i} \in pt(x), \ m = \underset{o_{u} \in pt(aj), 1 \leq j \leq n}{Dispatch(o_{i}, k)}$ $o_{u} \in pt(aj), 1 \leq j \leq n$ $o_{v} \in pt(m_{ret})$ $o_{i} \in pt(m_{this})$ $o_{u} \in pt(m_{pj}), 1 \leq j \leq n$ $o_{v} \in pt(r)$	$a1 \rightarrow m_{p1}$ $$ $an \rightarrow m_{pn}$ $r \leftarrow m_{ret}$

```
{ new A,
pt(x) = \text{new B},
          new C }
x.foo();
```

```
class A {
  T foo() {
    this... ?
  }}
```

```
class B extends A {
 T foo() {
    this...
  }}
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class C extends A {
  T foo() {
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Why not add PFG edge $x \rightarrow m_{this}$



Kind	Statement	Rule	PFG Edge
Call	l: r = x.k(a1,,an)	$o_{i} \in pt(x), \ m = \underset{o_{u} \in pt(aj), 1 \leq j \leq n}{Dispatch(o_{i}, k)}$ $o_{u} \in pt(aj), 1 \leq j \leq n$ $o_{v} \in pt(m_{ret})$ $o_{i} \in pt(m_{this})$ $o_{u} \in pt(m_{pj}), 1 \leq j \leq n$ $o_{v} \in pt(r)$	$a1 \rightarrow m_{p1}$ $$ $an \rightarrow m_{pn}$ $r \leftarrow m_{ret}$
ativa malatia ati ala avulal avalu. Classo		$\theta_v \in p\iota(r)$	

Receiver object should only flow to this variable of the corresponding target method

PFG edge $x \rightarrow m_{this}$ would introduce **spurious** points-to relations for **this** variables

```
pt(x) = { new A,
new B,
new C }
```

```
class A {
   T foo() {
     this...
   }}
```

```
class B extends A {
  T foo() {
    this...
  }}
```

```
class C extends A {
  T foo() {
    this...
}}
```

Why not add PFG edge $x \rightarrow m_{this}$



Call L:	r = x.k(a1,,an)	$o_{i} \in pt(x), \ m = \underset{o_{u} \in pt(aj), 1 \leq j \leq n}{Dispatch(o_{i}, k)}$ $o_{u} \in pt(aj), 1 \leq j \leq n$ $o_{v} \in pt(m_{ret})$ $o_{i} \in pt(m_{this})$ $o_{u} \in pt(m_{pj}), 1 \leq j \leq n$ $o_{v} \in pt(r)$	$a1 \rightarrow m_{p1}$ $$ $an \rightarrow m_{pn}$ $r \leftarrow m_{ret}$

Receiver object should only flow to this variable of the corresponding target method

PFG edge $x \rightarrow m_{this}$ would introduce **spurious** points-to relations for **this** variables

```
pt(x) = \begin{array}{l} \text{ new A,} \\ \text{new B,} \\ \text{new C } \} \end{array} \times .foo(); \qquad \qquad \text{With } x \to m_{this}
```

```
class A {
  T foo() {
    this...
}}
```

```
class B extends A {
  T foo() {
    this...
  }}
```

```
class C extends A {
  T foo() {
    this...
  }}
```

Why not add PFG edge $x \rightarrow m_{this}$



Kind	Statement	Rule	PFG Edge
Call	l: r = x.k(a1,,an)	$o_{i} \in pt(x), \ m = \underset{o_{u} \in pt(aj), 1 \leq j \leq n}{Dispatch(o_{i}, k)}$ $o_{u} \in pt(aj), 1 \leq j \leq n$ $o_{v} \in pt(m_{ret})$ $o_{i} \in pt(m_{this})$ $o_{u} \in pt(m_{pj}), 1 \leq j \leq n$ $o_{v} \in pt(r)$	$a1 \rightarrow m_{p1}$ $$ $an \rightarrow m_{pn}$ $r \leftarrow m_{ret}$
	ant alancida andre flace	$0_v \in p\iota(I)$	

Receiver object should only flow to this variable of the corresponding target method

PFG edge $x \rightarrow m_{this}$ would introduce **spurious** points-to relations for **this** variables

 $pt(x) = new B, \\ new C$

x.foo();

....

With $x \rightarrow m_{this}$



```
class A {
    {new A,
    new B,
    new C }
}
```

```
class B extends A {
  T foo() { new A,
    new B,
    new C }
```

```
class C extends A {
  T foo()
  this...
}

mew B,
new C}
```

Why not add PFG edge $x \rightarrow m_{this}$



Kind	Statement	Rule	PFG Edge
Call	l: r = x.k(a1,,an)	$o_{i} \in pt(x), \ m = \underset{o_{u} \in pt(aj), 1 \leq j \leq n}{Dispatch(o_{i}, k)}$ $o_{u} \in pt(aj), 1 \leq j \leq n$ $o_{v} \in pt(m_{ret})$ $o_{i} \in pt(m_{this})$ $o_{u} \in pt(m_{pj}), 1 \leq j \leq n$ $o_{v} \in pt(r)$	$a1 \rightarrow m_{p1}$ $an \rightarrow m_{pn}$ $r \leftarrow m_{ret}$
ativa a latinati ala avalal avalvi flavo		$o_v \in \rho\iota(r)$	

Receiver object should only flow to this variable of the corresponding target method

PFG edge $x \rightarrow m_{this}$ would introduce **spurious** points-to relations for **this** variables

 $pt(x) = \begin{cases} \text{new A,} \\ \text{new B,} \\ \text{new C} \end{cases}$

Without $x \rightarrow m_{this}$



x.foo();

class A {
 T foo() {
 new A}
 this...
}

```
class B extends A {
  T foo() {
    this... { new B }
  }
}
```

Interprocedural Pointer Analysis

Run together with call graph construction

```
void foo(A a) {
     ...
     b = a.bar();
     ...
}
```

Pointer analysis

Mutually dependent

Call graph construction

Interprocedural Pointer Analysis

Run together with call graph construction

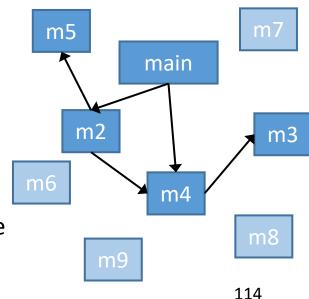
```
void foo(A a) {
     ...
     b = a.bar();
     ...
}
```

Pointer analysis

Mutually dependent

Call graph construction

- Call graph forms a "reachable world"
 - Entry methods (e.g., the main method) are reachable from the beginning
 - The other reachable methods are gradually discovered during analysis
 - Only reachable methods and statements are analyzed



Algorithms

```
Solve(m^{entry})
  WL=[],PFG={},S={},RM={},CG={}
  AddReachable(m^{entry})
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
     if n represents a variable x then
       foreach o_i \in \Delta do
          for each x.f = y \in S do
             AddEdge(y, o_i, f)
          foreach y = x.f \in S do
             AddEdge(o_i, f, y)
          ProcessCall(x, o_i)
```

```
S Set of reachable statements S_m Set of statements in method m RM Set of reachable methods CG Call graph edges
```

```
AddReachable(m)

if m \notin RM then

add m to RM

S \cup = S_m

foreach i: \times = \text{new T}() \in S_m do

add \langle x, \{o_i\} \rangle to WL

foreach \times = y \in S_m do

AddEdge(y, x)
```

```
ProcessCall(x, o_i)

foreach L: r = x.k(a1,...,an) \in S do

m = Dispatch(o_i, k)

add \langle m_{this}, \{o_i\} \rangle to WL

if L \to m \notin CG then

add L \to m to CG

AddReachable(m)

foreach parameter p_i of m do

AddEdge(a_i, p_i)

AddEdge(m_{ret}, r)
```

AddReachable(m)

- Expand the "reachable world", called
 - > at the beginning for entry methods
 - when new call graph edge is discovered

```
AddReachable(m)

if m \notin RM then

add m to RM

S \cup = S_m

foreach i: x = \text{new T}() \in S_m do

add \langle x, \{o_i\} \rangle to WL

foreach x = y \in S_m do

AddEdge(y, x)
```

S Set of reachable statements S_m Set of statements in method m RM Set of reachable methods

AddReachable(m)

- Expand the "reachable world", called
 - > at the beginning for entry methods
 - when new call graph edge is discovered

```
AddReachable(m)

if m \notin RM then

add m to RM

S \cup = S_m

foreach i : x = \text{new } T() \in S_m do

add \langle x, \{o_i\} \rangle to WL

foreach x = y \in S_m do

AddEdge(y, x)
```

S Set of reachable statements S_m Set of statements in method m

RM Set of reachable methods

AddReachable(m)

- Expand the "reachable world", called
 - > at the beginning for entry methods
 - when new call graph edge is discovered

```
AddEdge(s, t)
   if s \rightarrow t \notin PFG then
      add s \rightarrow t to PFG
      if pt(s) is not empty then
          add \langle t, pt(s) \rangle to WL
```

(Same as before)

```
AddReachable(m)
  if m \notin RM then
     add m to RM
                                 Add new reachable method and statements
     S \cup = S_m
     foreach i: x = \text{new } T() \in S_m \text{ do}
        add \langle x, \{o_i\} \rangle to WL
     foreach x = y \in S_m do
        AddEdge(y, x)
```

Update worklist and PFG for new discovered statements

Set of reachable statements Set of statements in method *m* S_m RMSet of reachable methods

Algorithms

```
Solve(m^{entry})
  WL=[],PFG={},S={},RM={},CG={}
  AddReachable(m^{entry})
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
     if n represents a variable x then
       foreach o_i \in \Delta do
          for each x.f = y \in S do
             AddEdge(y, o_i, f)
          foreach y = x.f \in S do
             AddEdge(o_i, f, y)
          ProcessCall(x, o_i)
```

```
S Set of reachable statements S_m Set of statements in method m RM Set of reachable methods CG Call graph edges
```

```
AddReachable(m)

if m \notin RM then

add m to RM

S \cup = S_m

foreach i: \times = \text{new } T() \in S_m do

add \langle x, \{o_i\} \rangle to WL

foreach \times = y \in S_m do

AddEdge(y, x)
```

```
ProcessCall(x, o_i)

foreach L: r = x.k(a1,...,an) \in S do

m = Dispatch(o_i, k)

add \langle m_{this}, \{o_i\} \rangle to WL

if L \to m \notin CG then

add L \to m to CG

AddReachable(m)

foreach parameter p_i of m do

AddEdge(a_i, p_i)

AddEdge(m_{ret}, r)
```

```
ProcessCall(x, o_i)

foreach L: r = x.k(a1,...,an) \in S do

m = Dispatch(o_i, k)

add \langle m_{this}, \{o_i\} \rangle to WL

if L \to m \notin CG then

add L \to m to CG

AddReachable(m)

foreach parameter p_i of m do

AddEdge(a_i, p_i)

AddEdge(m_{ret}, r)
```

Kind	Statement	Rule	PFG Edge
Call	l: r = x.k(a1,,an)	$\begin{aligned} o_i &\in pt(x), \ m = \underset{o_u \in pt(aj), 1 \leq j \leq n}{Dispatch}(o_i, k) \\ o_u &\in pt(aj), 1 \leq j \leq n \\ \hline o_v &\in pt(m_{ret}) \\ o_i &\in pt(m_{this}) \\ o_u &\in pt(m_{pj}), 1 \leq j \leq n \\ o_v &\in pt(r) \end{aligned}$	$a1 \rightarrow m_{p1}$ $an \rightarrow m_{pn}$ $r \leftarrow m_{ret}$

```
ProcessCall(x, o_i)

foreach L: r = x.k(a1,...,an) \in S do

m = Dispatch(o_i, k)

add \langle m_{this}, \{o_i\} \rangle to WL

Pass receiver object to this variable if L \to m \notin CG then

add L \to m to CG

AddReachable(m)

foreach parameter p_i of m do

AddEdge(a_i, p_i)

AddEdge(m_{ret}, r)
```

Kind	Statement	Rule	PFG Edge
Call	l: r = x.k(a1,,an)	$o_{i} \in pt(x), \ m = \underset{o_{u} \in pt(aj), 1 \leq j \leq n}{ o_{u} \in pt(aj), 1 \leq j \leq n}$ $\underbrace{o_{v} \in pt(m_{ret})}_{o_{i} \in pt(m_{this})}$ $o_{u} \in pt(m_{pj}), 1 \leq j \leq n$ $o_{v} \in pt(r)$	$a1 \rightarrow m_{p1}$ $$ $an \rightarrow m_{pn}$ $r \leftarrow m_{ret}$

```
ProcessCall(x, o_i)

foreach l: r = x.k(a1,...,an) \in S do

m = Dispatch(o_i, k)

add (m_{this}, \{o_i\}) to WL

if l \to m \notin CG then

add l \to m to l \to m
```

Kind	Statement	Rule	PFG Edge
Call	l: r = x.k(a1,,an)	$\begin{aligned} o_i &\in pt(x), \ m = \underset{o_u \in pt(aj), 1 \leq j \leq n}{Dispatch(o_i, k)} \\ o_u &\in pt(aj), 1 \leq j \leq n \\ \hline o_v &\in pt(m_{ret}) \\ o_i &\in pt(m_{this}) \\ o_u &\in pt(m_{pj}), 1 \leq j \leq n \\ o_v &\in pt(r) \end{aligned}$	$a1 \rightarrow m_{p1}$ $$ $an \rightarrow m_{pn}$ $r \leftarrow m_{ret}$

```
ProcessCall(x, o_i)

foreach L: r = x.k(a1,...,an) \in S do

m = Dispatch(o_i, k)

add \langle m_{this}, \{o_i\} \rangle to WL

Pass receiver object to this variable if L \to m \notin CG then

add L \to m to CG

AddReachable(m)

foreach parameter p_i of m do

AddEdge(a_i, p_i)

AddEdge(m_{ret}, r)

Pass return values
```

Kind	Statement	Rule	PFG Edge
Call	l: r = x.k(a1,,an)	$o_{i} \in pt(x), \ m = \underset{o_{u} \in pt(aj), 1 \leq j \leq n}{ o_{u} \in pt(aj), 1 \leq j \leq n}$ $\underbrace{o_{v} \in pt(m_{ret})}_{o_{i} \in pt(m_{this})}$ $o_{u} \in pt(m_{pj}), 1 \leq j \leq n$ $o_{v} \in pt(r)$	$a1 \rightarrow m_{p1}$ $an \rightarrow m_{pn}$ $r \leftarrow m_{ret}$

Algorithms Output: Ca

```
Points-to Relations (pt) Call Graph (CG)
```

```
Solve(m^{entry})
  WL=[],PFG=\{\},S=\{\},RM=\{\},CG=\{\}\}
  AddReachable(m^{entry})
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
          for each x.f = y \in S do
             AddEdge(y, o_i, f)
          foreach y = x.f \in S do
             AddEdge(o_i, f, y)
          ProcessCall(x, o_i)
```

```
S Set of reachable statements S_m Set of statements in method m RM Set of reachable methods CG Call graph edges
```

```
AddReachable(m)

if m \notin RM then

add m to RM

S \cup = S_m

foreach i: \times = \text{new } T() \in S_m do

add \langle x, \{o_i\} \rangle to WL

foreach \times = y \in S_m do

AddEdge(y, x)
```

```
ProcessCall(x, o_i)

foreach L: r = x.k(a1,...,an) \in S do

m = Dispatch(o_i, k)

add \langle m_{this}, \{o_i\} \rangle to WL

if L \to m \notin CG then

add L \to m to CG

AddReachable(m)

foreach parameter p_i of m do

AddEdge(a_i, p_i)

AddEdge(m_{ret}, r)
```

```
Solve(m^{entry})
  WL=[],PFG={},S={},RM={},CG={}
  AddReachable(m^{entry})
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
     if n represents a variable x then
       foreach o_i \in \Delta do
          foreach x.f = y \in S do
            AddEdge(v, o_i, f)
          foreach y = x.f \in S do
            AddEdge(o_i, f, y)
          ProcessCall(x, o_i)
```

```
class A {
    static void main() {
A a = new A();
A b = new B();
     A c = b.foo(a);
7 A foo(A x) { ... }
  class B extends A {
10 A foo(A y) \{
11 A r = new A();
12 return r;
13 }
14 }
```

```
Solve(m^{entry})
→ WL=[],PFG={},S={},RM={},CG={}
  AddReachable(m^{entry})
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
     if n represents a variable x then
       foreach o_i \in \Delta do
          foreach x.f = y \in S do
            AddEdge(v, o_i, f)
          foreach y = x.f \in S do
            AddEdge(o_i, f, y)
          ProcessCall(x, o_i)
```

```
WL: []
```

```
RM: { }
```

CG: {}

```
class A {
    static void main() {
      A = new A();
A b = new B();
     A c = b.foo(a);
7 A foo(A x) { ... }
  class B extends A {
10 A foo(A y) \{
11 A r = new A();
12 return r;
13 }
14 }
```

```
Solve(m^{entry})
  WL=[],PFG={},S={},RM={},CG={}
\rightarrow AddReachable(m^{entry})
  AddReachable(m)
     if m \notin RM then
        add m to RM
        S \cup = S_m
        foreach i: x = \text{new } T() \in S_m \text{ do}
           add \langle x, \{o_i\} \rangle to WL
        foreach x = y \in S_m do
           AddEdge(y, x)
```

```
WL: [] RM: {}

CG: {}
```

```
class A {
     static void main() {
      A a = new A();
      A b = new B();
5
      A c = b.foo(a);
6
   A foo(A x) { ... }
8
  class B extends A {
10 A foo(A y) \{
11 A r = new A();
12 return r;
13 }
14 }
```

```
Solve(m^{entry})
  WL=[],PFG={},S={},RM={},CG={}
  AddReachable(m^{entry})
  AddReachable(m)
     if m \notin RM then
     \Rightarrow add m to RM
        S \cup = S_m
        foreach i: x = \text{new } T() \in S_m \text{ do}
           add \langle x, \{o_i\} \rangle to WL
        foreach x = y \in S_m do
           AddEdge(y, x)
```

```
class A {
     static void main() {
      A = new A();
      A b = new B();
5
      A c = b.foo(a);
6
   A foo(A x) \{ \dots \}
8
   class B extends A {
10 A foo(A y) \{
11 A r = new A();
12 return r;
13 }
14 }
```

```
WL: []

RM: { A.main() }

CG: { }
```

```
Solve(m^{entry})
  WL=[],PFG={},S={},RM={},CG={}
  AddReachable(m^{entry})
  AddReachable(m)
     if m \notin RM then
        add m to RM
        S \cup = S_m
        foreach i: x = \text{new } T() \in S_m \text{ do}
     \longrightarrow add \langle x, \{o_i\} \rangle to WL
        foreach x = y \in S_m do
           AddEdge(y, x)
```

```
WL: [\langle a, \{o_3\} \rangle, \langle b, \{o_4\} \rangle]   RM: \{ A.main() \}
```

CG: {}

```
Solve(m^{entry})
  WL=[],PFG={},S={},RM={},CG={}
  AddReachable(m^{entry})
  while WL is not empty do
 \implies remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
          foreach x.f = y \in S do
             AddEdge(v, o_i, f)
          foreach y = x.f \in S do
             AddEdge(o_i, f, y)
          ProcessCall(x, o_i)
```

```
WL: [\langle b, \{o_4\} \rangle]
```

RM: { A.main() }

```
Processing: \langle a, \{o_3\} \rangle
```

```
CG: { }
```

```
class A {
    static void main() {
      A = new A();
      A b = new B();
      A c = b.foo(a);
7 A foo(A x) { ... }
  class B extends A {
10 A foo(A y) \{
11 A r = new A();
12 return r;
13 }
14 }
```

```
Solve(m^{entry})
  WL=[],PFG={},S={},RM={},CG={}
  AddReachable(m^{entry})
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
  \Rightarrow Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
          foreach x.f = y \in S do
             AddEdge(y, o_i, f)
          foreach y = x.f \in S do
             AddEdge(o_i, f, y)
          ProcessCall(x, o_i)
```

```
WL: [\langle b, \{o_4\} \rangle]
```

RM: { A.main() }

```
Processing: \langle a, \{o_3\} \rangle
```

```
CG: { }
```

```
class A {
    static void main() {
      A = new A();
      A b = new B();
      A c = b.foo(a);
7 A foo(A x) { ... }
  class B extends A {
10 A foo(A y) \{
      A r = new A();
12 return r;
13 }
14 }
```

```
\{o_3\}
```

```
Solve(m^{entry})
  WL=[],PFG={},S={},RM={},CG={}
  AddReachable(m^{entry})
  while WL is not empty do
 \implies remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
     Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
          foreach x.f = y \in S do
             AddEdge(v, o_i, f)
          foreach y = x.f \in S do
             AddEdge(o_i, f, y)
          ProcessCall(x, o_i)
```

```
WL: []
```

RM: { A.main() }

```
Processing: \langle b, \{o_4\} \rangle
```

```
CG: { }
```

```
class A {
    static void main() {
      A = new A();
      A b = new B();
      A c = b.foo(a);
7 A foo(A x) { ... }
  class B extends A {
10 A foo(A y) \{
11 A r = new A();
12 return r;
13 }
14 }
```

```
\{o_3\}
```

```
Solve(m^{entry})
  WL=[],PFG={},S={},RM={},CG={}
  AddReachable(m^{entry})
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
  \rightarrow Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
          foreach x.f = y \in S do
             AddEdge(v, o_i, f)
          foreach y = x.f \in S do
             AddEdge(o_i, f, y)
          ProcessCall(x, o_i)
```

```
WL: []
```

RM: { A.main() }

```
Processing: \langle b, \{o_4\} \rangle
```

```
CG: { }
```

```
class A {
     static void main() {
       A = new A();
       A b = new B();
       A c = b.foo(a);
7 A foo(A x) { ... }
   class B extends A {
10 A foo(A y) \{
       A r = new A();
        return r;
13 }
14 }
              {o<sub>3</sub>}
      \{\mathbf{0_4}\}
```

```
b) (a)
```

```
Solve(m^{entry})
  WL=[],PFG={},S={},RM={},CG={}
  AddReachable(m^{entry})
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
  \Rightarrow Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
          foreach x.f = y \in S do
             AddEdge(v, o_i, f)
          foreach y = x.f \in S do
             AddEdge(o_i, f, y)
          ProcessCall(x, o_i)
```

What next?

```
class A {
     static void main() {
      A = new A();
      A b = new B();
      A c = b.foo(a);
7 A foo(A x) { ... }
   class B extends A {
10
  A foo(A y) \{
      A r = new A();
12 return r;
13
14 }
      \{o_4\}
             \{o_3\}
```

```
WL: []
```

RM: { A.main() }

```
Processing: \langle b, \{o_4\} \rangle
```

```
CG: {}
```

```
ProcessCall(x, o_i)
  foreach l: r = x.k(a1,...,an) \in S do
     m = Dispatch(o_i, k)
     add \langle m_{this}, \{o_i\} \rangle to WL
     if l \to m \notin CG then
        add L \rightarrow m to CG
        AddReachable(m)
        foreach parameter p_i of m do
           AddEdge(a_i, p_i)
        AddEdge(m_{ret}, r)
        \Rightarrow ProcessCall(x, o_i)
```

WL: []

Processing: $\langle b, \{o_4\} \rangle$

```
RM: { A.main() }
```

```
CG: {}
```

```
class A {
     static void main() {
       A = new A();
A b = new B();
5 \longrightarrow A c = b.foo(a);
7 A foo(A x) { ... }
   class B extends A {
10 A foo(A y) \{
       A r = new A();
       return r;
13 }
14 }
      \{o_4\}
             \{o_3\}
```

```
ProcessCall(x, o_i)
  foreach l: r = x.k(a1,...,an) \in S do
  \rightarrow m = Dispatch(o_i, k) m = ?
     add \langle m_{this}, \{o_i\} \rangle to WL
     if l \rightarrow m \notin CG then
        add L \rightarrow m to CG
        AddReachable(m)
        foreach parameter p_i of m do
          AddEdge(a_i, p_i)
        AddEdge(m_{ret}, r)
          ProcessCall(x, o_i)
```

```
WL: []
                                     RM: { A.main() }
                                     CG: {}
Processing:
    \langle b, \{o_4\} \rangle
```

```
class A {
     static void main() {
       A = new A();
A b = new B();
5 \longrightarrow A c = b.foo(a);
7 A foo(A x) { ... }
   class B extends A {
10 A foo(A y) \{
      A r = new A();
12 return r;
13 }
14 }
      \{o_4\}
             \{o_3\}
```

```
ProcessCall(x, o_i)
foreach l: r = x.k(a1,...,an) \in S do

m = Dispatch(o_i, k)
m = B.foo(A)

add \langle m_{this}, \{o_i\} \rangle to WL

if l \to m \notin CG then

add l \to m to l \to m
foreach parameter l \to m
AddEdgel \to m
```

ProcessCall (x, o_i)

```
WL: []

RM: {A.main()}

Processing: CG: {}

\langle b, \{o_4\} \rangle
```

```
class A {
     static void main() {
       A = new A();
A b = new B();
5 \longrightarrow A c = b.foo(a);
7 A foo(A x) { ... }
   class B extends A {
10 A foo(A y) \{
      A r = new A();
12
       return r;
13 }
14 }
      \{o_4\}
             \{o_3\}
```

```
ProcessCall(x, o_i)
  foreach l: r = x.k(a1,...,an) \in S do
     m = Dispatch(o_i, k)
   \Rightarrow add \langle m_{this}, \{o_i\} \rangle to WL
     if l \to m \notin CG then
        add L \rightarrow m to CG
        AddReachable(m)
        foreach parameter p_i of m do
           AddEdge(a_i, p_i)
        AddEdge(m_{ret}, r)
          ProcessCall(x, o_i)
```

```
WL: [\langle B. foo/this, \{o_4\} \rangle]
                                        RM: { A.main() }
```

```
Processing:
      \langle b, \{o_4\} \rangle
```

```
CG: {}
```

```
class A {
     static void main() {
       A = new A();
A b = new B();
5 \longrightarrow A c = b.foo(a);
7 A foo(A x) { ... }
   class B extends A {
10 A foo(A y) \{
       A r = new A();
12
       return r;
13
14 }
      \{o_4\}
             \{o_3\}
```

```
ProcessCall(x, o_i)
  foreach l: r = x.k(a1,...,an) \in S do
     m = Dispatch(o_i, k)
     add \langle m_{this}, \{o_i\} \rangle to WL
     if L \to m \notin CG then
    \Longrightarrow add L \to m to CG
       AddReachable(m)
        foreach parameter p_i of m do
          AddEdge(a_i, p_i)
        AddEdge(m_{ret}, r)
          ProcessCall(x, o_i)
```

WL: $[\langle B. foo/this, \{o_4\} \rangle]$ *RM*: { A.main() }

Processing: $\langle b, \{o_4\} \rangle$

```
CG: \{5 \rightarrow B.foo(A)\}
```

```
class A {
     static void main() {
       A = new A();
A b = new B();
5 \longrightarrow A c = b.foo(a);
7 A foo(A x) { ... }
   class B extends A {
10 A foo(A y) \{
       A r = new A();
12
       return r;
13
14 }
      \{o_4\}
             \{o_3\}
```

```
ProcessCall(x, o_i)
  foreach l: r = x.k(a1,...,an) \in S do
     m = Dispatch(o_i, k)
     add \langle m_{this}, \{o_i\} \rangle to WL
     if L \to m \notin CG then
   \Longrightarrow add L \to m to CG
       AddReachable(m)
        foreach parameter p_i of m do
          AddEdge(a_i, p_i)
        AddEdge(m_{ret}, r)
```

```
WL: [\langle B. foo/this, \{o_4\} \rangle]
```

```
RM: { A.main() }
```

```
Processing:
      \langle b, \{o_4\} \rangle
```

```
CG: \{ 5 \rightarrow B.foo(A) \}
                                      PFG:
 CHA: \{5 \rightarrow B.foo(A), \underline{5 \rightarrow A.foo(A)}\}
                                     Spurious call edge
     Tian Tan @ Nanjing University
```

```
class A {
     static void main() {
A a = new A();
A b = new B();
5 \longrightarrow A c = b.foo(a);
7 A foo(A x) { ... }
   class B extends A {
10 A foo(A y) \{
11 A r = new A();
12 return r;
13 }
14 }
      \{o_4\}
            \{o_3\}
```

```
ProcessCall(x, o_i)
  foreach l: r = x.k(a1,...,an) \in S do
     m = Dispatch(o_i, k)
     add \langle m_{this}, \{o_i\} \rangle to WL
     if l \to m \notin CG then
        add L \rightarrow m to CG
   \implies AddReachable(m)
        foreach parameter p_i of m do
          AddEdge(a_i, p_i)
        AddEdge(m_{ret}, r)
                                          What change?
```

ProcessCall (x, o_i)

WL: $[\langle B. foo/this, \{o_4\} \rangle]$

Processing: $\langle b, \{o_4\} \rangle$

```
RM: { A.main() }
```

```
CG: \{5 \rightarrow B.foo(A)\}
```

```
class A {
     static void main() {
       A = new A();
      A b = new B();
  \rightarrow A c = b.foo(a);
   A foo(A x) { ... }
   class B extends A {
10
    A foo(A y) {
11
       A r = new A();
12
       return r;
13
14 }
      \{o_4\}
              \{o_3\}
```

```
ProcessCall(x, o_i)

foreach l: r = x.k(a1,...,an) \in S do

m = Dispatch(o_i, k)

add \langle m_{this}, \{o_i\} \rangle to WL

if l \to m \notin CG then

add l \to m to l \to m

foreach parameter l \to m do

AddEdgel \to m do

AddEdgel \to m do

AddEdgel \to m
```

ProcessCall (x, o_i)

WL: $[\langle B. foo/this, \{o_4\} \rangle]$

RM: { A.main() }

Processing: $\langle b, \{o_4\} \rangle$

 $CG: \{ 5 \rightarrow B.foo(A) \}$

```
class A {
     static void main() {
       A = new A();
A b = new B();
5 \longrightarrow A c = b.foo(a);
  A foo(A x) { ... }
   class B extends A {
10
    A foo(A y) {
       A r = new A();
11
12
       return r;
13
14 }
```

```
AddReachable(m)

if m \notin RM then

add m to RM

S \cup = S_m

foreach i: \times = \text{new } T() \in S_m do

add \langle x, \{o_i\} \rangle to WL

foreach \times = y \in S_m do

AddEdge(y, x)
```

 $\langle b, \{o_4\} \rangle$

```
ProcessCall(x, o_i)
  foreach l: r = x.k(a1,...,an) \in S do
     m = Dispatch(o_i, k)
     add \langle m_{this}, \{o_i\} \rangle to WL
     if l \rightarrow m \notin CG then
        add L \rightarrow m to CG
    \implies AddReachable(m)
        foreach parameter p_i of m do
           AddEdge(a_i, p_i)
        AddEdge(m_{ret}, r)
          ProcessCall(x, o_i)
```

```
WL: [\langle B. foo/this, \{o_4\} \rangle] RM: \{A.main(), B.foo(Processing: CG: \{5 \rightarrow B.foo(A)\}
```

```
class A {
         static void main() {
           A = new A();
    A b = new B();
    5 \longrightarrow A c = b.foo(a);
       A foo(A x) { ... }
       class B extends A {
    10
        A foo(A y) {
    11
           A r = new A();
    12
            return r;
    13
    14 }
AddReachable(m)
  \triangleright add m to RM
    S \cup = S_m
```

```
if m \notin RM then

add m to RM
S \cup = S_m
RM: \{ A.main(), B.foo(A) \}  for each i : x = new T() \in S_m  do
add \langle x, \{o_i\} \rangle  to WL
for each x = y \in S_m  do
AddEdge(y, x)
```

```
ProcessCall(x, o_i)
  foreach l: r = x.k(a1,...,an) \in S do
     m = Dispatch(o_i, k)
     add \langle m_{this}, \{o_i\} \rangle to WL
     if l \rightarrow m \notin CG then
        add L \rightarrow m to CG
    \longrightarrow AddReachable(m)
        foreach parameter p_i of m do
           AddEdge(a_i, p_i)
        AddEdge(m_{ret}, r)
```

ProcessCall (x, o_i)

```
WL: [\langle B. foo/this, \{o_4\} \rangle,
             \langle r, \{o_{11}\}\rangle
```

Processing:

 $\langle b, \{o_4\} \rangle$

```
class A {
     static void main() {
       A = new A();
A b = new B();
5 \longrightarrow A c = b.foo(a);
7 A foo(A x) { ... }
   class B extends A {
10
    A foo(A y) {
11
       A r = new A();
12
       return r;
13
14 }
```

```
AddReachable(m)
                                    if m \notin RM then
                                       add m to RM
                                       S \cup = S_m
RM: { A.main(), B.foo(A) } foreach i: x = \text{new } T() \in S_m \text{ do}
                                   \longrightarrow add \langle x, \{o_i\} \rangle to WL
                                       foreach x = y \in S_m do
CG: \{ 5 \rightarrow B.foo(A) \}
                                         AddEdge(y, x)
```

```
ProcessCall(x, o_i)
  foreach l: r = x.k(a1,...,an) \in S do
     m = Dispatch(o_i, k)
     add \langle m_{this}, \{o_i\} \rangle to WL
     if l \to m \notin CG then
        add L \rightarrow m to CG
        AddReachable(m)
        foreach parameter p_i of m do
    \longrightarrow AddEdge(a_i, p_i)
        AddEdge(m_{ret}, r)
```

ProcessCall (x, o_i)

```
WL: [\langle B. foo/this, \{o_4\} \rangle,
              \langle r, \{o_{11}\}\rangle, \langle y, \{o_3\}\rangle
```

Processing: $\langle b, \{o_4\} \rangle$

```
RM: { A.main(), B.foo(A) }
```

```
CG: \{ 5 \rightarrow B.foo(A) \}
                                   PFG:
```

```
class A {
     static void main() {
       A = new A();
A b = new B();
5 \longrightarrow A c = b.foo(a);
7 A foo(A x) { ... }
   class B extends A {
10 A foo(A y) \{
       A r = new A();
       return r;
13
14 }
      \{o_4\}
             \{o_3\}
                      {}
```

```
ProcessCall(x, o_i)
  foreach l: r = x.k(a1,...,an) \in S do
     m = Dispatch(o_i, k)
     add \langle m_{this}, \{o_i\} \rangle to WL
     if l \to m \notin CG then
        add L \rightarrow m to CG
        AddReachable(m)
        foreach parameter p_i of m do
           AddEdge(a_i, p_i)
      \rightarrow AddEdge(m_{ret}, r)
          ProcessCall(x, o_i)
```

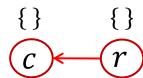
```
class A {
     static void main() {
       A = new A();
      A b = new B();
  \rightarrow A c = b.foo(a);
  A foo(A x) { ... }
   class B extends A {
10 A foo(A y) \{
       A r = new A();
       return r;
13
14 }
      \{o_4\}
             \{o_3\}
```

```
WL: [\langle B. foo/this, \{o_4\} \rangle,
              \langle r, \{o_{11}\}\rangle, \langle y, \{o_3\}\rangle]
```

RM: { A.main(), B.foo(A) }

Processing: $\langle b, \{o_4\} \rangle$

 $CG: \{ 5 \rightarrow B.foo(A) \}$



```
Solve(m^{entry})
  WL=[],PFG={},S={},RM={},CG={}
  AddReachable(m^{entry})
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
  \Rightarrow Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
          foreach x.f = y \in S do
             AddEdge(v, o_i, f)
          foreach y = x.f \in S do
             AddEdge(o_i, f, y)
          ProcessCall(x, o_i)
```

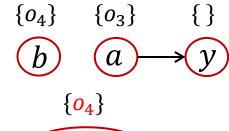
```
WL: [\langle r, \{o_{11}\}\rangle, \langle y, \{o_3\}\rangle]
```

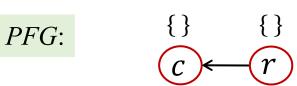
```
Processing:
   \langle B. foo/this, \{o_4\} \rangle
```

```
RM: { A.main(), B.foo(A) }
```

```
CG: \{ 5 \rightarrow B.foo(A) \}
```

```
class A {
     static void main() {
       A = new A();
       A b = new B();
       A c = b.foo(a);
   A foo(A x) { ... }
   class B extends A {
10
     A foo(A y) \{
       A r = new A();
       return r;
13
14 }
```





B.foo/this

```
Solve(m^{entry})
  WL=[],PFG={},S={},RM={},CG={}
  AddReachable(m^{entry})
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)

ightharpoonup Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
          foreach x.f = y \in S do
             AddEdge(y, o_i, f)
          foreach y = x.f \in S do
             AddEdge(o_i, f, y)
          ProcessCall(x, o_i)
```

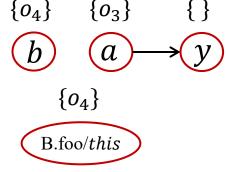
```
WL: [\langle y, \{o_3\}\rangle, \langle c, \{o_{11}\}\rangle]
```

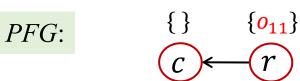
```
Processing: \langle r, \{o_{11}\} \rangle
```

```
RM: { A.main(), B.foo(A) }
```

```
CG: \{5 \rightarrow B.foo(A)\}
```

```
class A {
     static void main() {
       A = new A();
       A b = new B();
       A c = b.foo(a);
   A foo(A x) { ... }
   class B extends A {
10
     A foo(A y) \{
       A r = new A();
       return r;
13
14 }
      \{o_4\}
             \{o_3\}
```





```
Solve(m^{entry})
  WL=[],PFG={},S={},RM={},CG={}
  AddReachable(m^{entry})
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
  \Rightarrow Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
          foreach x.f = y \in S do
             AddEdge(v, o_i, f)
          foreach y = x.f \in S do
             AddEdge(o_i, f, y)
          ProcessCall(x, o_i)
```

```
AddEdge(y, o_i. f)

foreach y = x. f \in S do

AddEdge(o_i. f, y)

ProcessCall(x, o_i)

**Processing:

(y, {o_3})

**CG: {5 \rightarrow B.foo(A)}

**CG: {5 \rightarrow B.foo(A)}
```

```
class A {
      static void main() {
        A = new A();
        A b = new B();
        A c = b.foo(a);
   A foo(A x) { ... }
   class B extends A {
10
     A foo(A y) \{
        A r = new A();
        return r;
13
14 }
       \{o_4\}
               \{o_3\}
                         {0<sub>3</sub>}
            {o_4}
          B.foo/this
                         \{o_{11}\}
PFG:
```

```
Solve(m^{entry})
  WL=[],PFG={},S={},RM={},CG={}
  AddReachable(m^{entry})
  while WL is not empty do
     remove \langle n, pts \rangle from WL
     \Delta = pts - pt(n)
  \Rightarrow Propagate(n, \Delta)
     if n represents a variable x then
        foreach o_i \in \Delta do
          foreach x.f = y \in S do
             AddEdge(v, o_i, f)
          foreach y = x.f \in S do
             AddEdge(o_i, f, y)
          ProcessCall(x, o_i)
```

```
class A {
      static void main() {
        A = new A();
        A b = new B();
        A c = b.foo(a);
   A foo(A x) { ... }
   class B extends A {
10
   A foo(A y) \{
        A r = new A();
        return r;
13
14 }
       \{o_4\}
               \{o_3\}
                         \{o_3\}
            \{o_4\}
          B.foo/this
               {0<sub>11</sub>}
                         \{o_{11}\}
PFG:
```

RM: { A.main(), B.foo(A) }

Processing: $\langle c, \{o_{11}\} \rangle$ $CG: \{ 5 \rightarrow B.foo(A) \}$

```
Solve(m^{entry})
  WL=[],PFG={},S={},RM={},CG={}
  AddReachable(m^{entry})
  while WL is not empty do
    remove \langle n, pts \rangle from WL
    \Delta = pts - pt(n)
    Propagate(n, \Delta)
    if n represents a variable x then
       foreach o_i \in \Delta do
          foreach x.f = y \in S do
            AddEdge(v, o_i, f)
          foreach y = x.f \in S do Algorithm finishes
            AddEdge(o_i, f, y)
          ProcessCall(x, o_i)
```

WL: []

Processing:

RM: { A.main(), B.foo(A) }

B.foo/this $\{o_{11}\}$ PFG:

 $\{o_4\}$

class A {

10

13

14 }

static void main() {

A = new A();A b = new B();

A c = b.foo(a);

A foo(A x) { ... }

class B extends A {

A r = new A();

A foo(A y) $\{$

return r;

 $\{o_4\}$ $\{o_3\}$

 $\{o_3\}$

The X You Need To Understand in This Lecture

- Understand pointer analysis rule for method call
- Understand inter-procedural pointer analysis algorithm
- Understand on-the-fly call graph construction

注意注意! 划重点了!



软件分析

南京大学 计算机科学与技术系 程序设计语言与 谭添