#### Introduction to AFM Line Scan Simulator

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## 1 Marcus Theory

Marcus theory models the rate of thermally assisted adiabatic electron transfers. The rate equation for an electron tunneling from an initial site to a final site is given by:

$$\nu_{if} = \frac{|t_{if}|^2}{\hbar} \sqrt{\frac{\pi}{\lambda k_B T}} \exp\left(-\frac{(\Delta G_{if} + \lambda)^2}{4\lambda k_B T}\right) \tag{1}$$

Where  $t_{if}$  is the tunneling term (overlap of wavefunctions);  $\lambda$  is the self-trapping energy;  $\Delta G_{if}$  is the Coulombic energy difference between the configurations before and after electron exchange.

### 2 AFM Line Scan Simulation

#### 2.1 Implementation

A tool for simulating AFM line scans has been implemented. The simulator takes the position of dangling bonds, scan type (read or write) and other parameters to produce simulated line scan plots.

The simulation engine consists of two classes:

- AFMLine: This is the class that users interact with. It contains the user configuration for the AFM tip and dangling bonds, and facilitates the line scan simulation. To approximate an AFM's behavior, a measurement is made at each DB location to see whether it contains an electron. Plots are also generated by this class.
- Marcus Model: This class is called by *AFMLine* to generate the timing for electron tunneling events. Marcus theory is used to determine electron hopping rates between two sites, which is used to generate randomized timings for electron tunneling events from an exponential distribution. This class is also responsible for keeping track of electron count and position.

Currently, two items are still pending proper implementation: 1. the current model of the AFM tip is a result of trial-and-error parameterization, Lucian's model should be able to fill this gap; 2. the electron population count is determined by hand, an automated implementation is needed.

#### 2.2 Usage

Example simulation setup options can be found at afm-sim/src/python/demo.py, executing it yields a line scan plot. The contents of demo.py have also been included below for your convenience:

```
#!/usr/bin/env python

from afm import AFMLine

# set the corrdinates of the dangling bonds in lattice units
# #X = [1, 12, 15, 22, 25] # 1-2-2
```

```
7 X = [1, 8, 10, 15, 17, 24] # 1-2-2-1
afm = AFMLine(X)
                             # create AFM handler for the given DB arrangement
# set the scan type
afm.setScanType(0)
                             # read-read, set by default
                              # write(right)-read(left) with a strength of 10meV
#afm.setScanType(1, .01)
#afm.setScanType(-1, .01)
                              # write(left)-read(right) with a strength of 10meV
17 # set the bias
18 #afm.setBias(.00012)
                              # 120 ueV/angstrom bias gradient
_{20} # run the AFM and produce the AFM image, image will be saved to tempfig.pdf
21 # Nel: number of electrons in the system, half filled by default
             number of line scans, 2 per sweep with read-read else 1
22 # nscans:
             number of lattice sites included on the [left, right] edge of the scan
23 # pad:
           tip speed in angstroms/second
24 # srate:
afm.run(Nel=3, nscans=200, pad=[3,3], srate=82)
```

If you wish to alter the behavior of the simulation beyond what's shown above, you may tweak the 'magic numbers' in afm-sim/src/python/marcus.py within the section # somewhat magic numbers.