

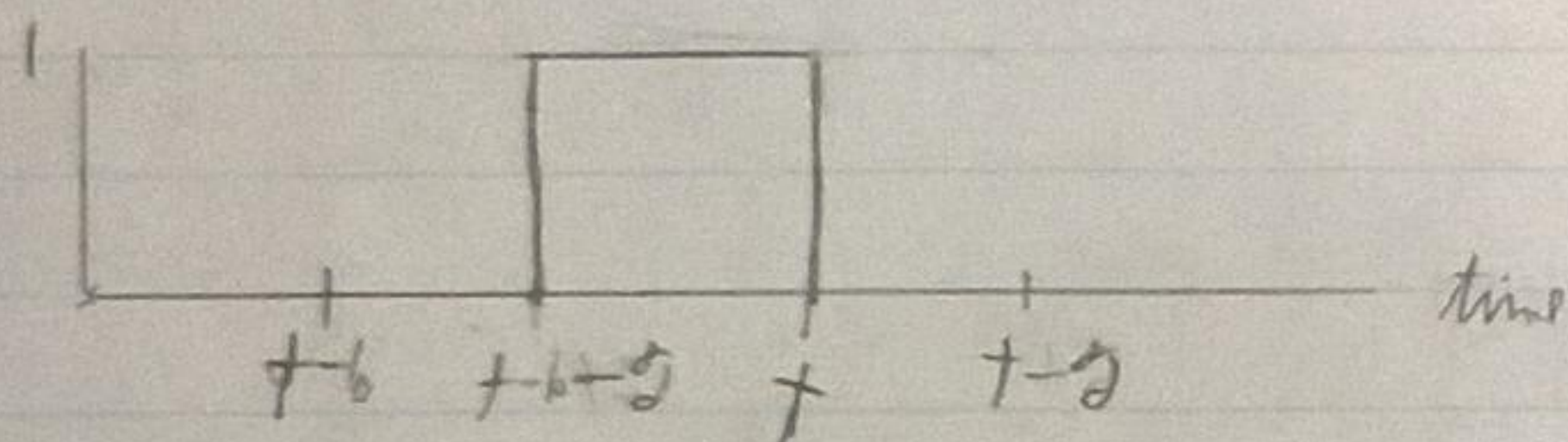
$$R_{xx} = E[x(t)x(t-\tau)] = E\left[\int_{t-b}^t y(t') dt' \int_{t-b-\tau}^{t-b} y(t'') dt''\right]$$

$$= E\left[\int_{t-b}^t \int_{t-b-\tau}^{t-b} y(t') y(t'') dt' dt''\right] = \int_{t-b}^t \int_{t-b-\tau}^{t-b} E[y(t') y(t'')] dt' dt''$$

since $R_{yy}(\tau) = \delta(\tau)$

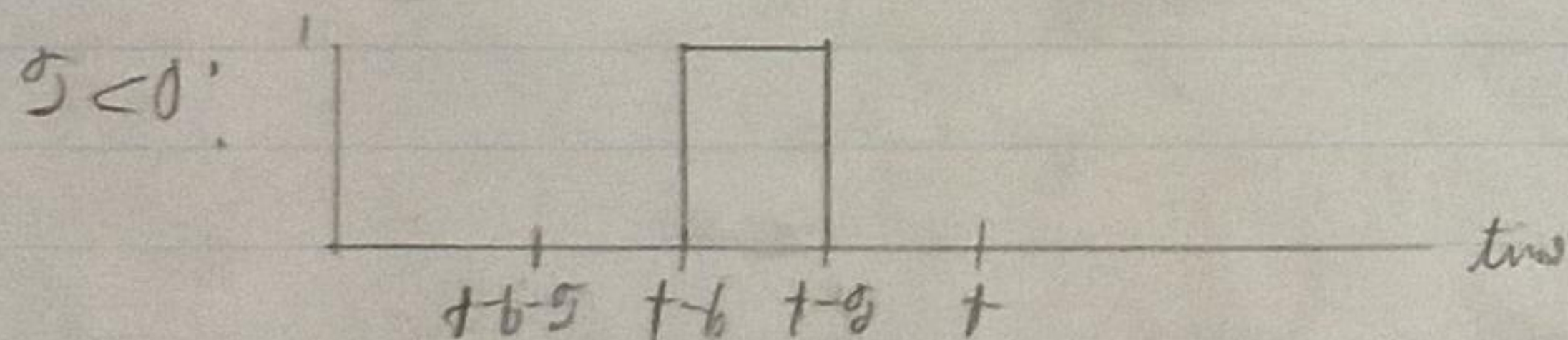
$$R_{xx} = \int_{t-b}^t \int_{t-b-\tau}^{t-b} \delta(t' - t'') dt' dt''$$

This can be seen graphically when $\tau < 0$:



Since the integrand is 1 where t' and t'' overlap, and 0 elsewhere.

So $R_{xx} = t - (t - b - \tau) = b + \tau$ when $\tau < 0$ and $b > |\tau|$



$R_{xx} = t - \tau - (t - b) = b - \tau$ when $\tau > 0$ and $b > \tau$

$\tau = 0$: $R_{xx} = t - (t - b) = b$ when $\tau = 0$

If $b < |\tau|$ $R_{xx} = 0$, since there is no overlap of t' and t'' .

$$R_{xx} = b - |\tau| \quad \text{when } b - |\tau| > 0$$