

The SiPM Physics and Technology

- a Review -

G.Collazuol

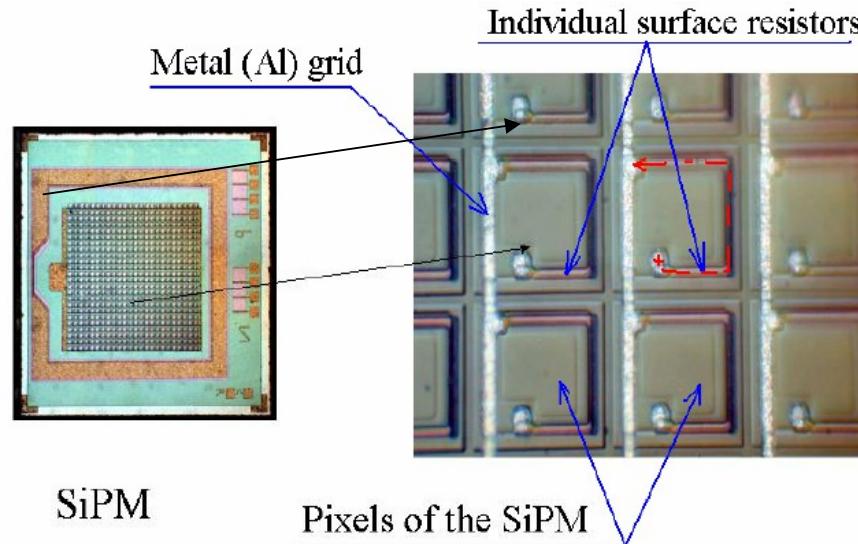
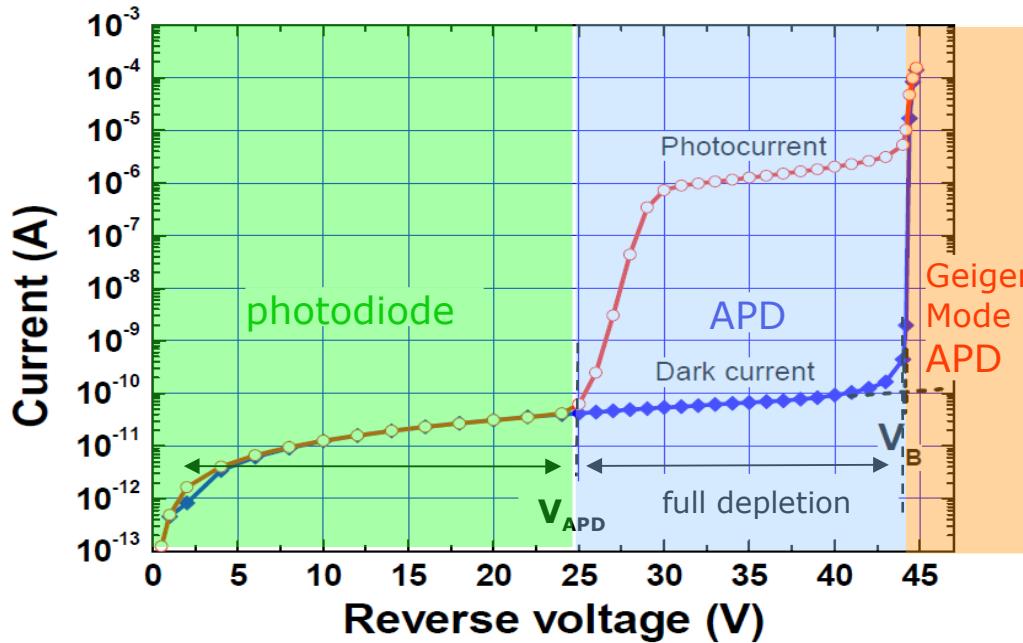
Department of Physics and Astronomy, University of Padova and INFN

Overview

- Introduction
 - Key physics and technology features
 - I-V characteristics
 - Device response
 - Noises
 - Photo-detection efficiency
 - Timing properties
 - Summary and Future

The silicon PM: array of GM-APD

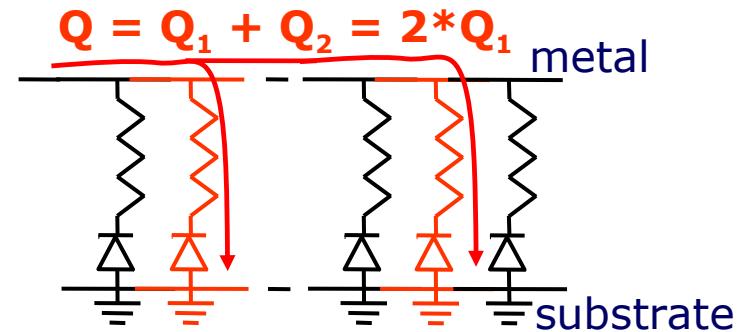
Single GM-APD gives no information on light intensity → **MATRIX** structure first proposed in the late '80-ies by [Golovin and Sadygov](#)



A SiPM is segmented in tiny GM-APD cells and connected in parallel through a **decoupling resistor**, which is also used for **quenching** avalanches in the cells

Each element is independent and gives the same signal when fired by a photon

In principle output charge is proportional to the number of incident photons



Σ digital signals → analog signal !!!

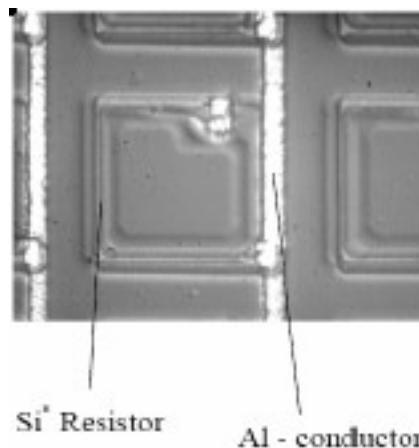
A bit of history

Pioneering work since late 80-ies
at Russian institutes

Investigations of various multi-layer silicon structures with local micro-plasma suppression effect to develop low-cost GM-APD arrays

Early devices ageing quickly, unstable, noisy

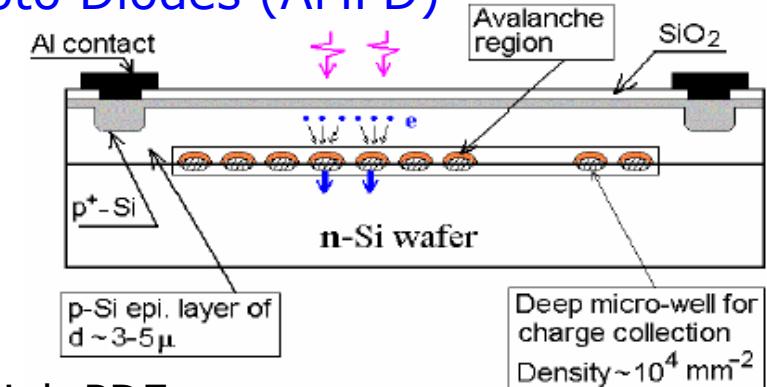
Dolgoshin - MePhi/Pulsar (Moscow)
Poly-silicon resistor



- Low fill-factor
- Simple fabrication technology

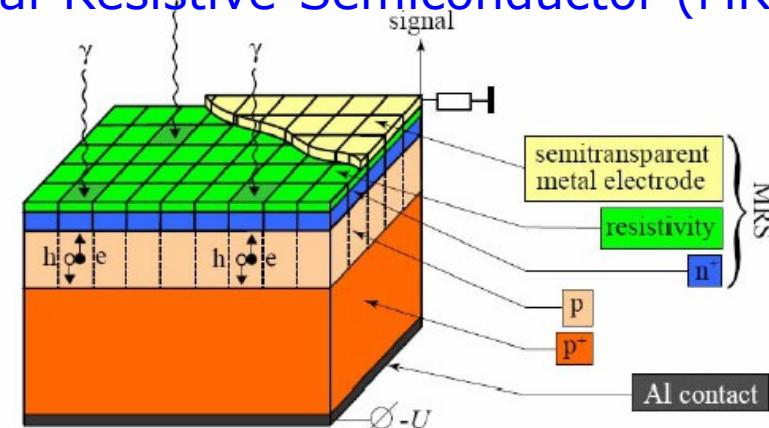
e.g., Dolgoshein, NIMA 563 (2006)

Sadygov – JINR/Micron (Dubna)
Avalanche Micro-channel/pixel
Photo Diodes (AMPD)



- high PDE
- very high density of micro-cells
eg Sadygov, NIMA 567 (2006)

Golovin - Obninsk/CPTA (Moscow)
Metal-Resistive-Semiconductor (MRS)



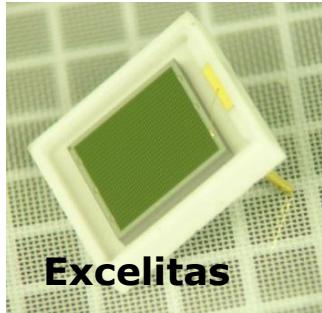
- High fill factor
- Good pixel to pixel uniformity

e.g., Golovin
NIMA 539 (2005)

Today

Many institutes/companies are involved in SiPM development/production:

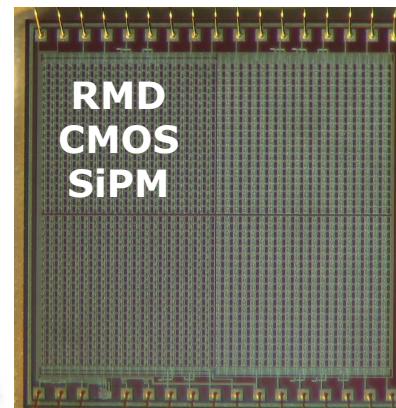
- **CPTA**, Moscow, Russia
- **MePhi/Pulsar** Enterprise, Moscow, Russia
- **Zecotek**, Vancouver, Canada
- **Hamamatsu HPK**, Hamamatsu, Japan
- **FBK-AdvanSiD**, Trento, Italy
- **ST Microelectronics**, Catania, Italy
- **Amplification Technologies** Orlando, USA
- **SensL**, Cork, Ireland
- **MPI-HLL**, Munich, Germany
- **RMD**, Boston, USA
- **Philips**, Aachen, Germany
- **Excelitas** tech. (formerly Perkin-Elmer)
- **KETEK**, Munich, Germany
- **National Nano Fab Center**, Korea
- **Novel Device Laboratory (NDL)**, Beijing, China
- **E2V**
- **CSEM**



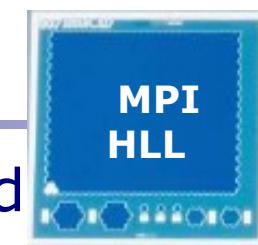
**Amplification
Technologies
(DAPD)**



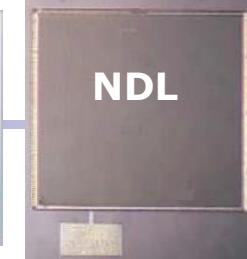
Excelitas



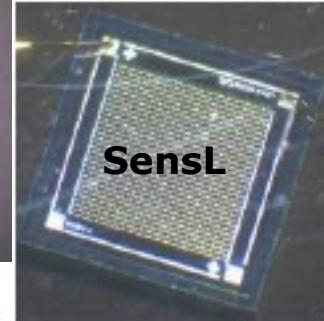
**RMD
CMOS
SiPM**



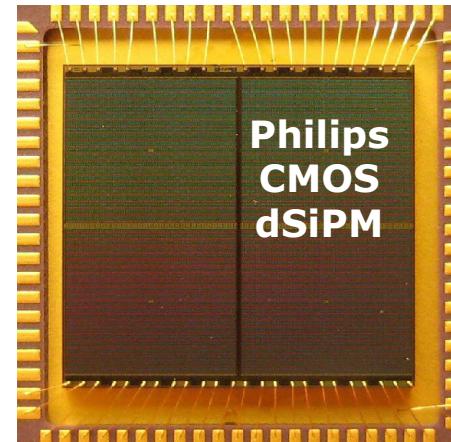
**MPI
HLL**



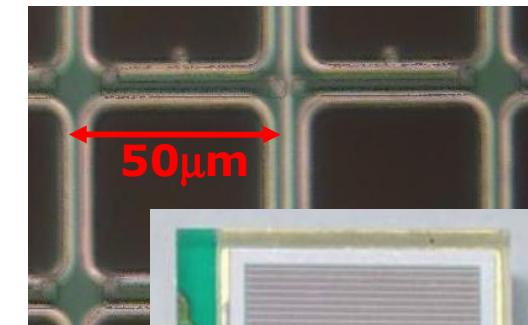
NDL



SensL



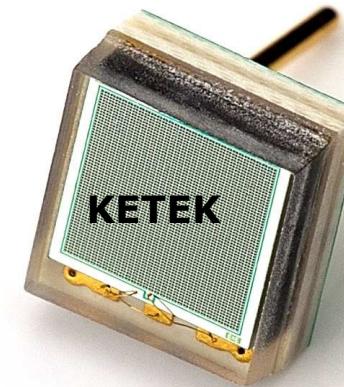
**Philips
CMOS
dSiPM**



HAMAMATSU



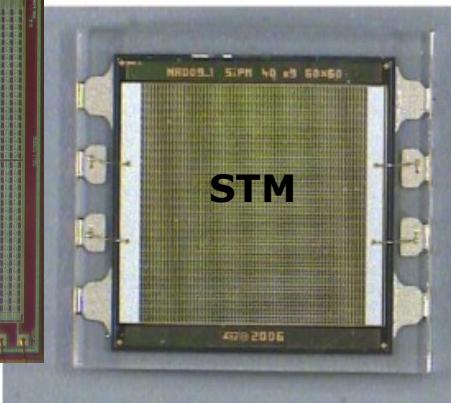
**NanoFab
Korea**



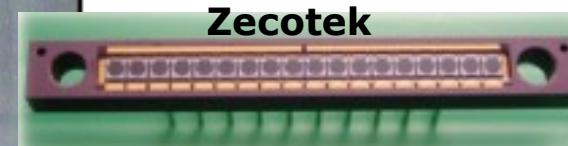
KETEK

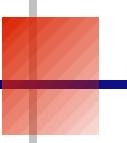


Zecotek



STM





Physics & Technology

Key features

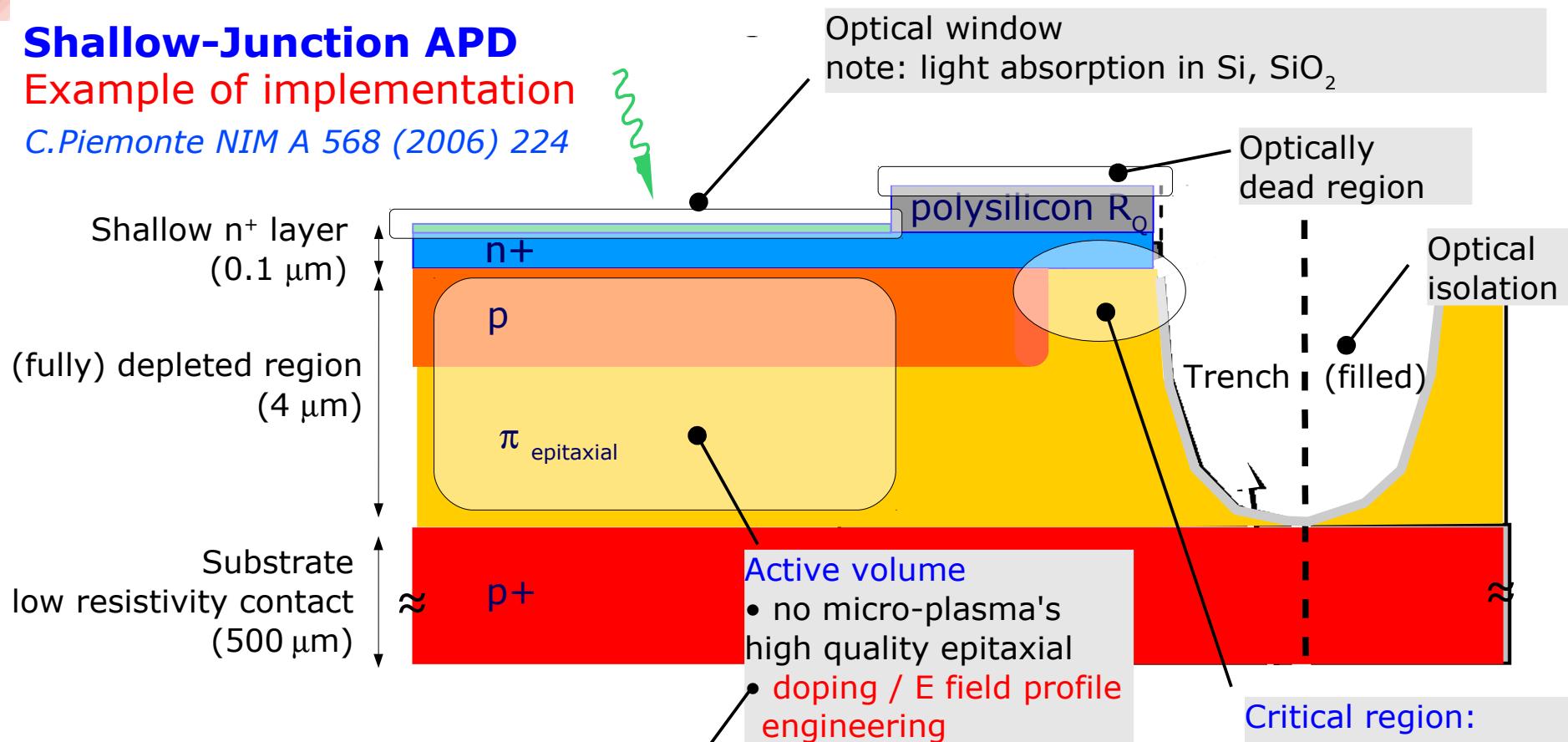
- Closeup of a cell – Custom vs CMOS
- Guard Ring and Optical isolation
- Operation principles of GM-APD and quenching modes

Close up of a cell – custom process

Shallow-Junction APD

Example of implementation

C.Piemonte NIM A 568 (2006) 224



- n⁺ on p abrupt junction structure
- Anti-reflective coating (ARC)
- **Very thin (100nm) n⁺ layer:** "low" doping
→ minimize Auger and SHR recombination
- **Thin high-field region:** "high" doping p layer
→ limited by tunneling breakdown
→ fixes V_{BD} junction well below V_{BD} at edge
- R_Q by poly-silicon
- Trenches for optical insulation (cross-talk)
- Fill factor: 20% - 80%

Optimization for blue light (420nm)

Critical region:

- Leakage current
- Surface charges
- **Guard Ring** for
 - preventing early edge-breakdown
 - isolating cells
 - tuning E field shape

→ impact on Fill Factor

CMOS vs Custom processes

"Standard" CMOS processes

- shallow implant depths
- high doping concentrations
- shallow trench isolation (STI)
- deep well implants (flash extension)
- no extra gettering and high T annealing
- non optimized optical stacks
- design rule restrictions

high E field
(low V_{bd})

tunneling
lattice stress
(defects/traps)

high DCR

limited PDE
(often p-on-n)

limited timing performances
(long diffusion tails)

Recent progresses in CMOS APDs due to:

- 1) **high voltage (flash) extension** often available in **standard** processes
 - deep wells (needed for the high voltages used in flash memories)
- 2) **Additional processes** (custom) available:
 - buried implants
 - deep trench isolation
 - optical stack optimization

Key elements for CMOS SiPMs

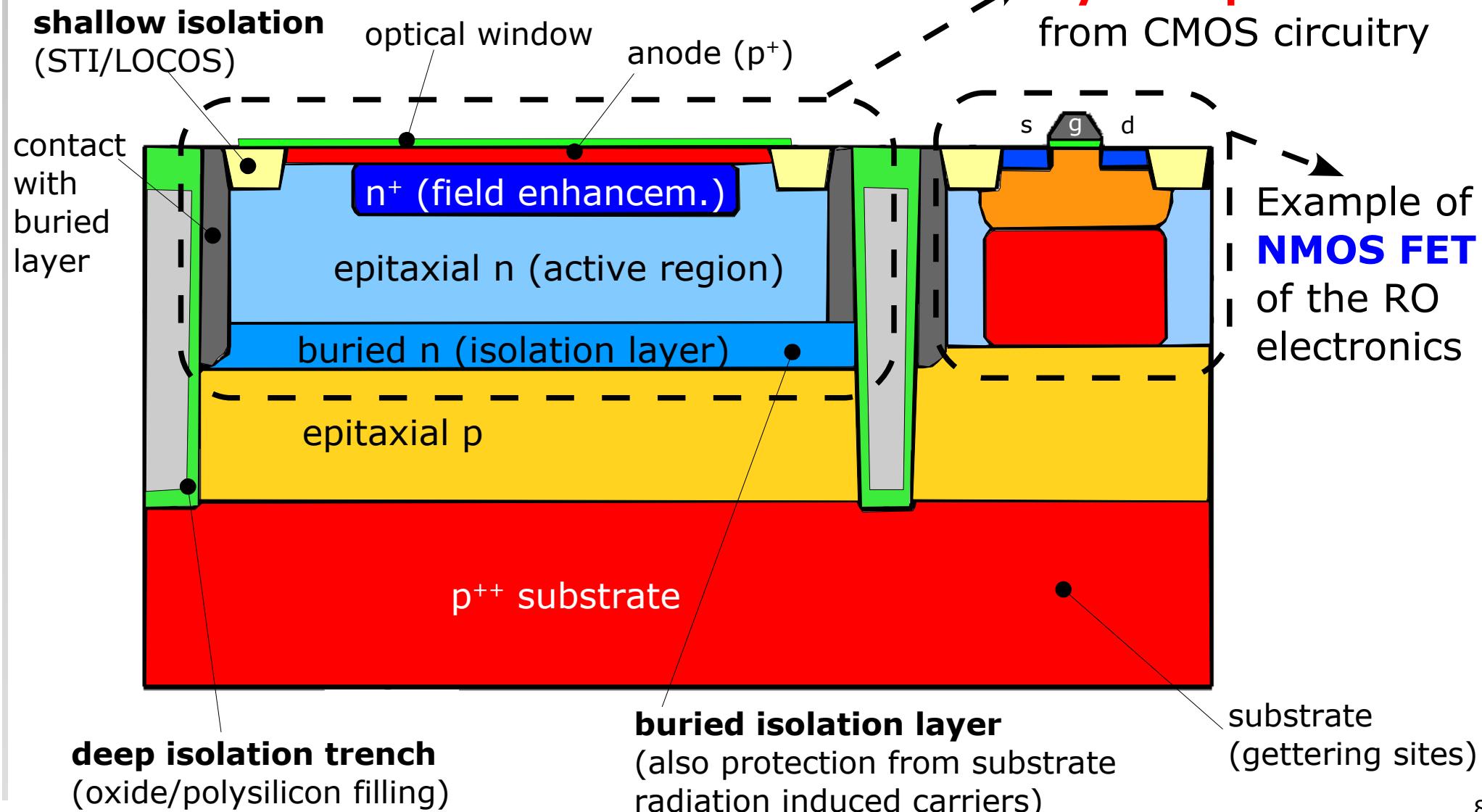
- **APD cell isolation** from CMOS circuitry
- **guard ring** (again)

Close up of a CMOS cell

APD integration into CMOS

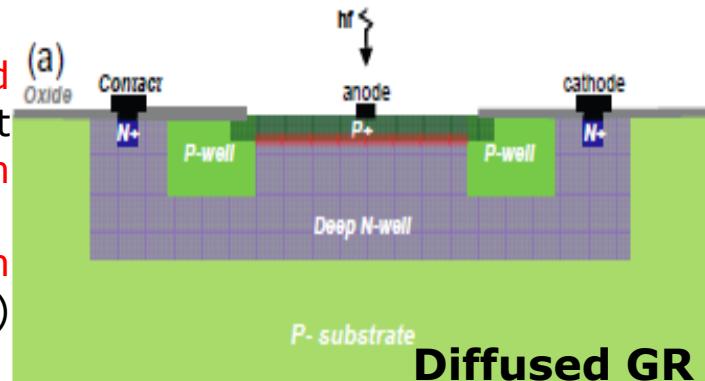
Example of implementation T.Frach in US patent 2010/0127314

- Note • extended CMOS processes exploited
• careful design of cell isolation and guard ring



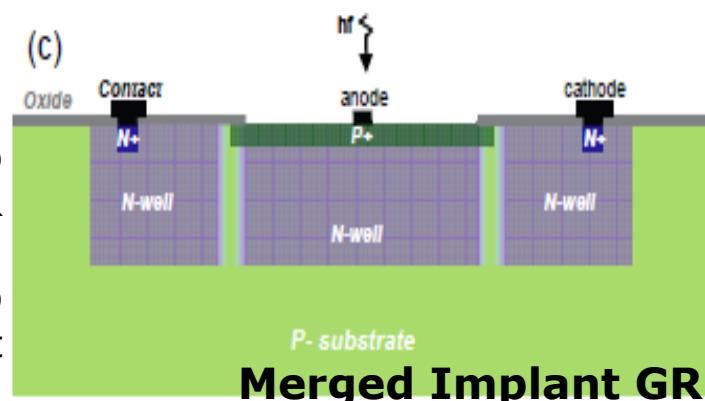
The Guard Ring structure

- high E field structure, not uniform

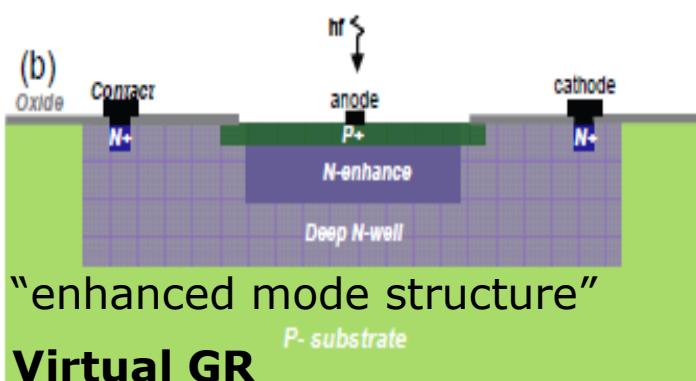


- neutral region (timing tails)

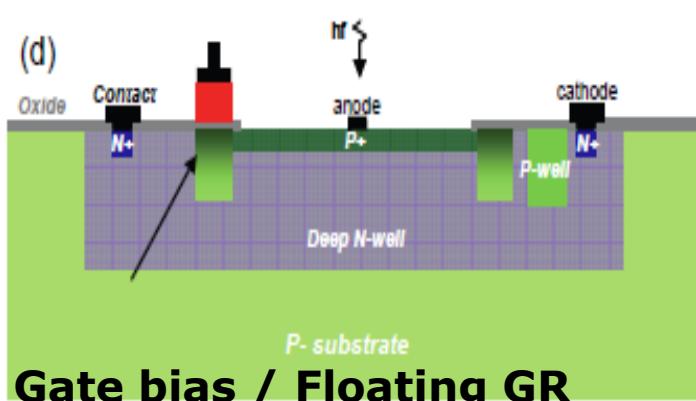
- limited fill factor



- alternative to Diffused GR
- difficult to implement

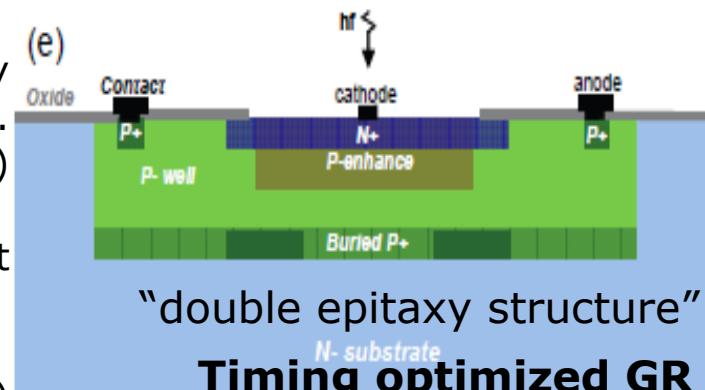


- well tuned high E field structure
- no additional neutral regions
- fill factor less limited

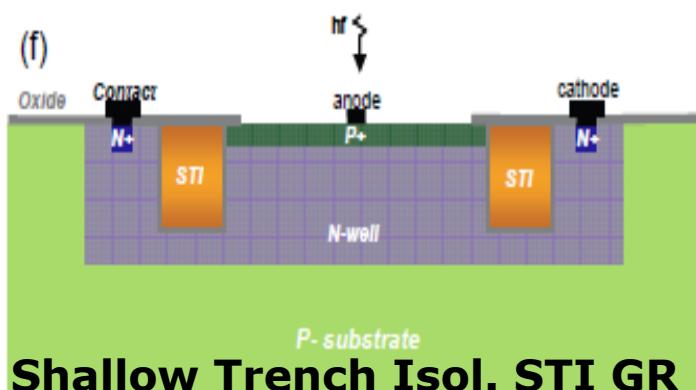


- less commonly exploited
- careful modeling required

- developed by S.Cova and coll. (fully custom)



- state of the art SPAD timing and PDE (red enhanced)



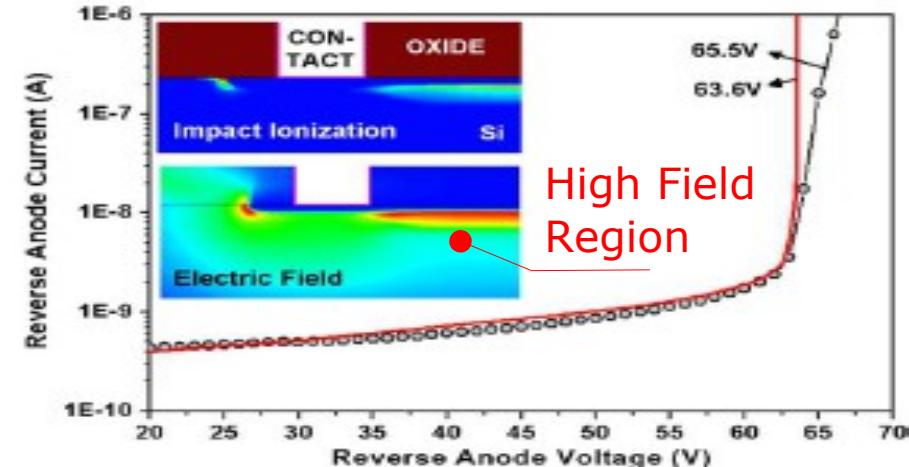
- physically blocks and confines the high E field in active region
- might cause high DCR due to
 - tunneling
 - etching induced defects/traps

from "Avalanches in Photodiodes" G.F.Dalla Betta Ed., InTech Pub. (2011)

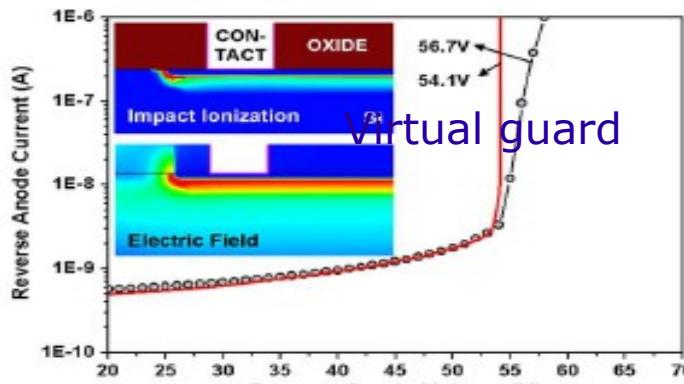
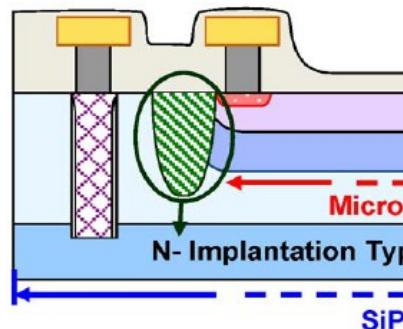
Guard Ring structures in SiPM

Sul et al, IEEE EDL 31 2010 "G.R. Structures for SiPM"

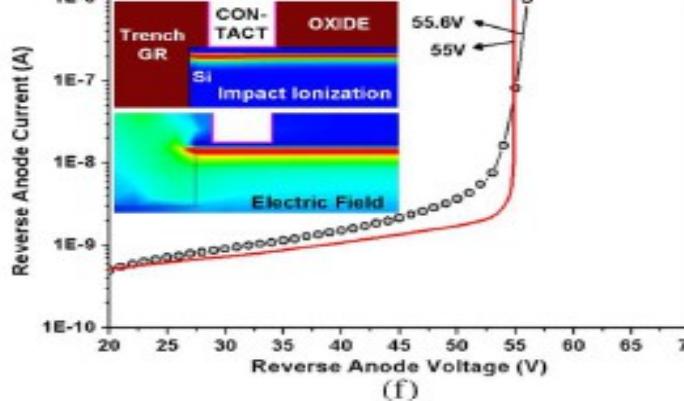
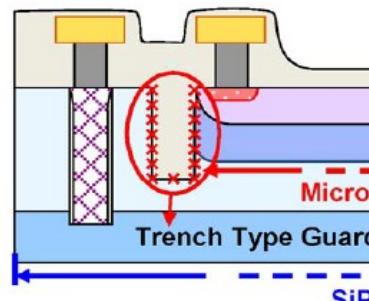
Virtual guard ring
most often used



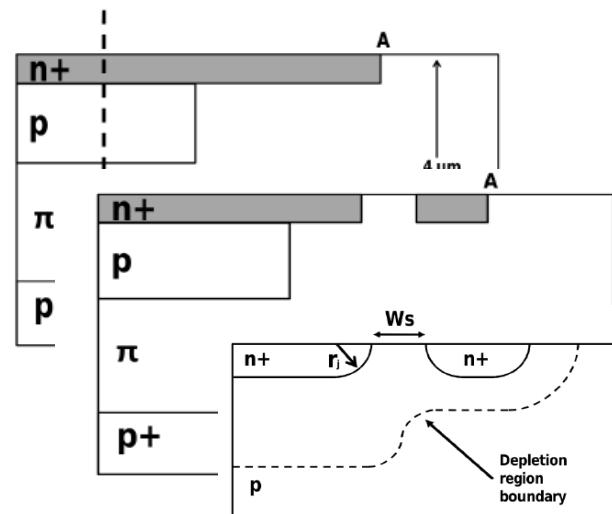
Implant / Gate bias



Trench type



Maresca et al. Proc. of SPIE Vol. 8072
"Floating field ring ...
to enhance fill factor of SiPM"



Operation principle of a GM-APD

Avalanche processes in semiconductors

are studied in detail since the '60 for modeling micro-plasma instabilities

McIntyre JAP 32 (1961), Hitz JAP 35 (1964)
and Ruegg IEEE TED 14 (1967)

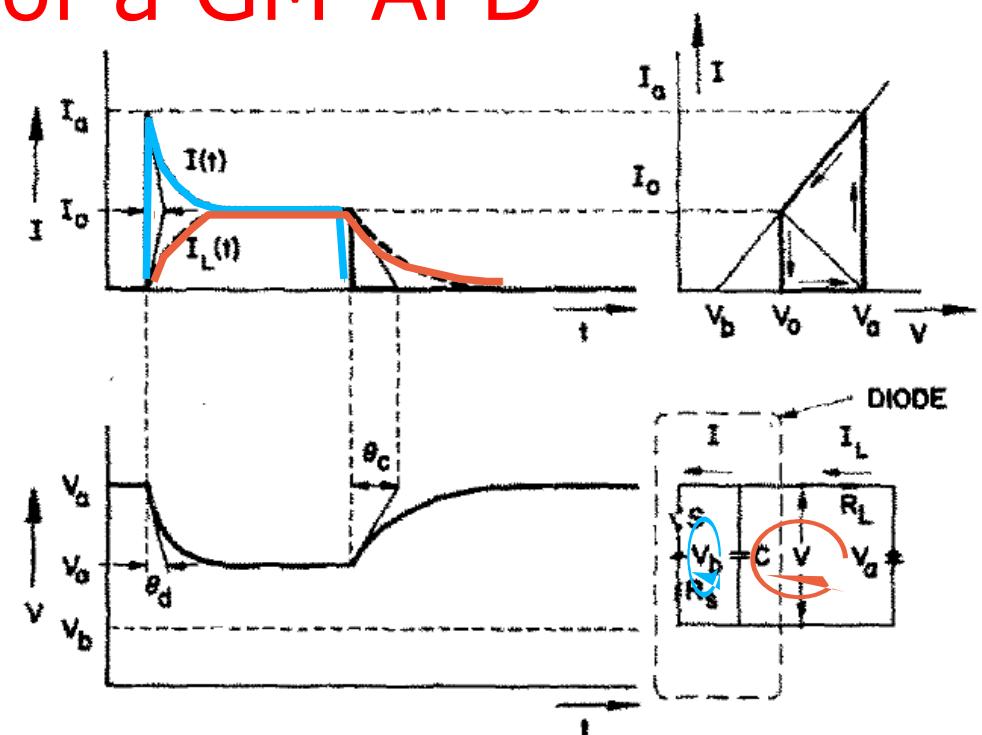
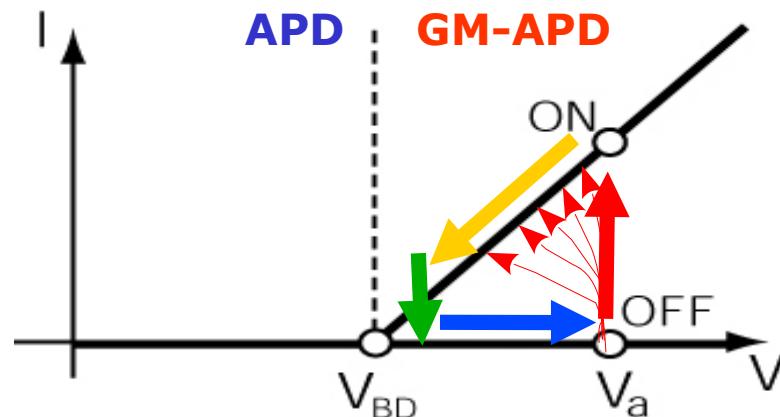


FIG. 3. Shape of current pulse for $\theta_d \ll r_1(I_0)$.

OFF condition: avalanche quenched, switch open, capacitance charged until no current flowing from V_{bd} to V_{BIAS} with time constant $R_q \times C_d = \tau_{quenching}$ (\rightarrow recovery time)

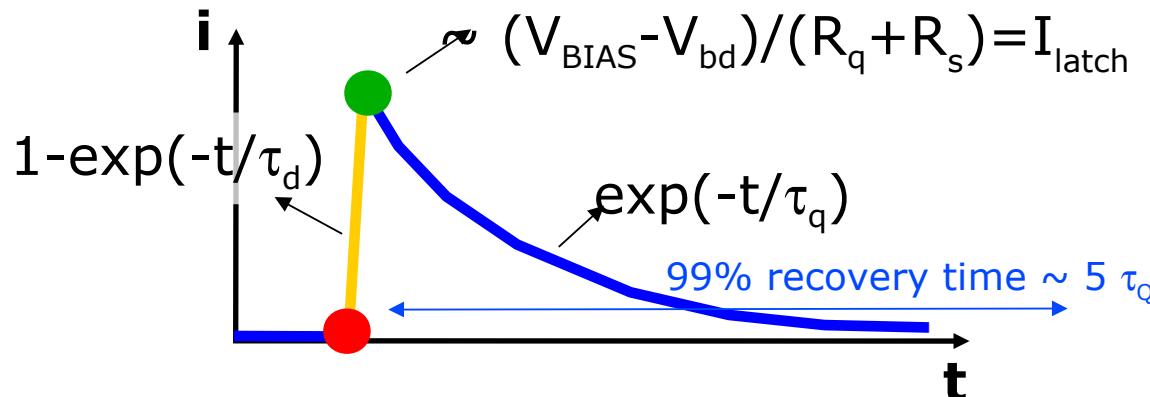
P_{01} = turn-on probability
probability that a carrier traversing the high-field region triggers the avalanche

P_{10} = turn-off probability
probability that the number of carriers traversing the high-field region fluctuates to 0

ON condition: avalanche triggered, switch closed
 C_d discharges to V_{bd} with a time constant $R_d \times C_d = \tau_{discharge}$,
at the same time the external current asymptotic grows to $(V_{bias} - V_{bd}) / (R_q + R_d)$

Passive Quenching

If R_Q is high enough the internal current is so low that statistical fluctuations may quench the avalanche



The leading edge of the signal is much faster than trailing edge:

1. $\tau_d = R_s C_d \ll R_q C_d = \tau_q$
2. turn-off mean time is very short
(if R_q is sufficiently high, $I_{latch} \sim 20\mu A$)

The charge collected per event is the **area under the exponential** which is determined by circuital elements and bias.

→ It is possible to **define a GAIN** (discharge of a capacitor)

$$G = \frac{I_{max} \cdot \tau_q}{q_e} = \frac{(V_{bias} - V_{bd}) \cdot \tau_q}{(R_q + R_s) \cdot q_e} = \frac{(V_{bias} - V_{bd}) \cdot C_d}{q_e}$$

→ Gain **fluctuations** in GM-APD are **smaller than in APD** essentially because electrons and holes give the same signal

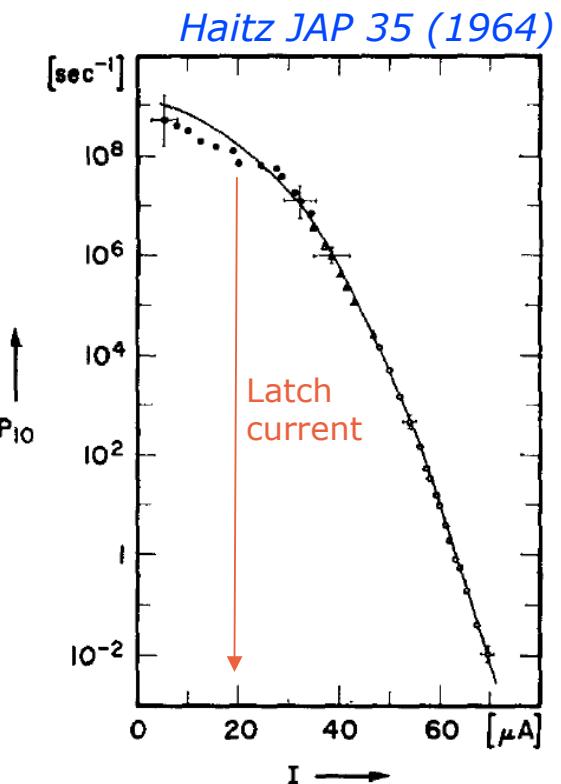
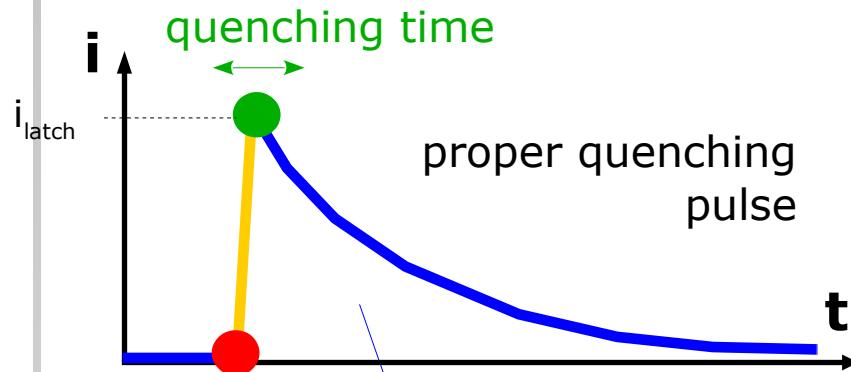


FIG. 2. Turnoff probability per second as function of pulse current.

Passive Quenching Regime

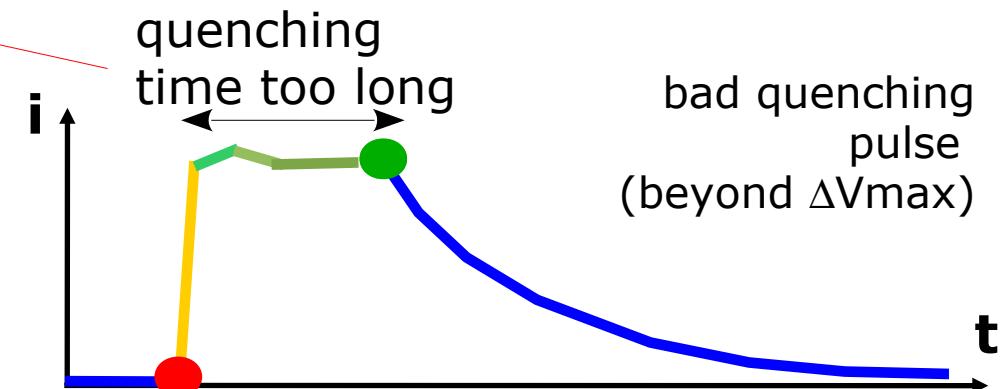
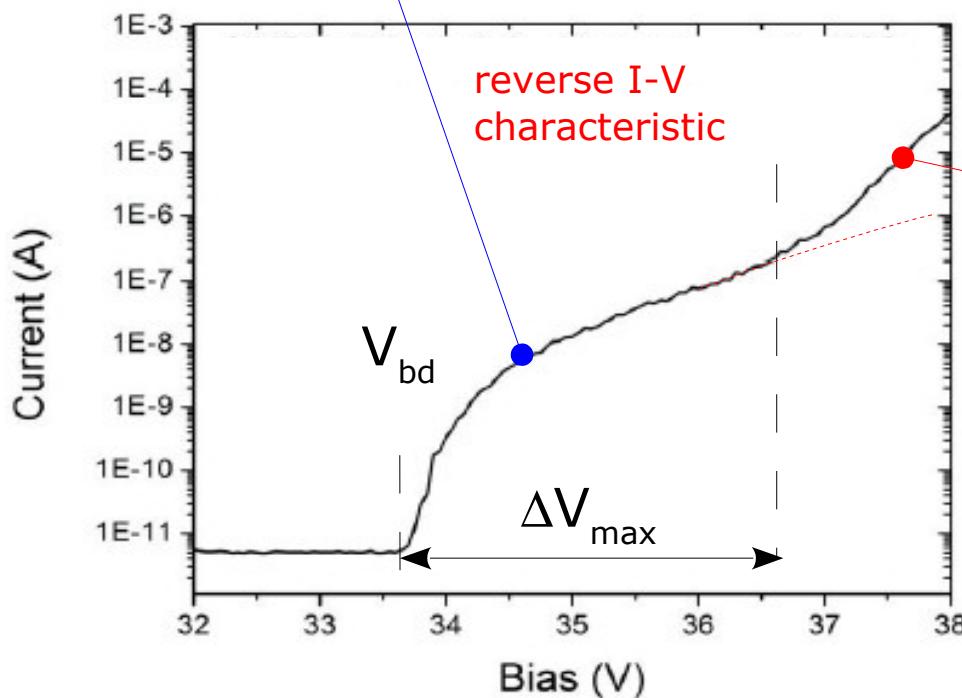
Proper value of quenching resistance R_q is crucial to let the internal current decrease to a level such that **statistical fluctuations may quench the avalanche**
→ sub-ns quenching time → crucial to have **well defined gain**



Given R_q the proper quenching regime is for ΔV in the range:

$$0 < \Delta V < R_q I_{latch}$$

where as a rule of thumb
 $I_{latch} \sim 20\mu A \rightarrow \Delta V_{max} \sim \text{a few Volts (typically)}$



bad quenching pulse
(beyond ΔV_{max})

Operative ΔV Range – $I_{\text{dark}}/\text{DCR}$

Operative ΔV limited by:

- 1) $I_{\text{latch}} \sim 20 \mu\text{A} \rightarrow \Delta V < I_{\text{latch}} R_q$ (non-quenching regime)
- 2) Dark Count Rate (DCR) acceptable level \leftarrow PDE vs $\Delta V \leftarrow$ E field shape
- 3) $V_{\text{bd}}^{\text{edge}}$ edge breakdown (usually some 10V above V_{bd})

A practical method for estimating the operative range (limited by effect 1) is to measure the ratio R_I of the measured dark current I_D to the dark current I'_D calculated from the measured dark rate and pixel count spectra:

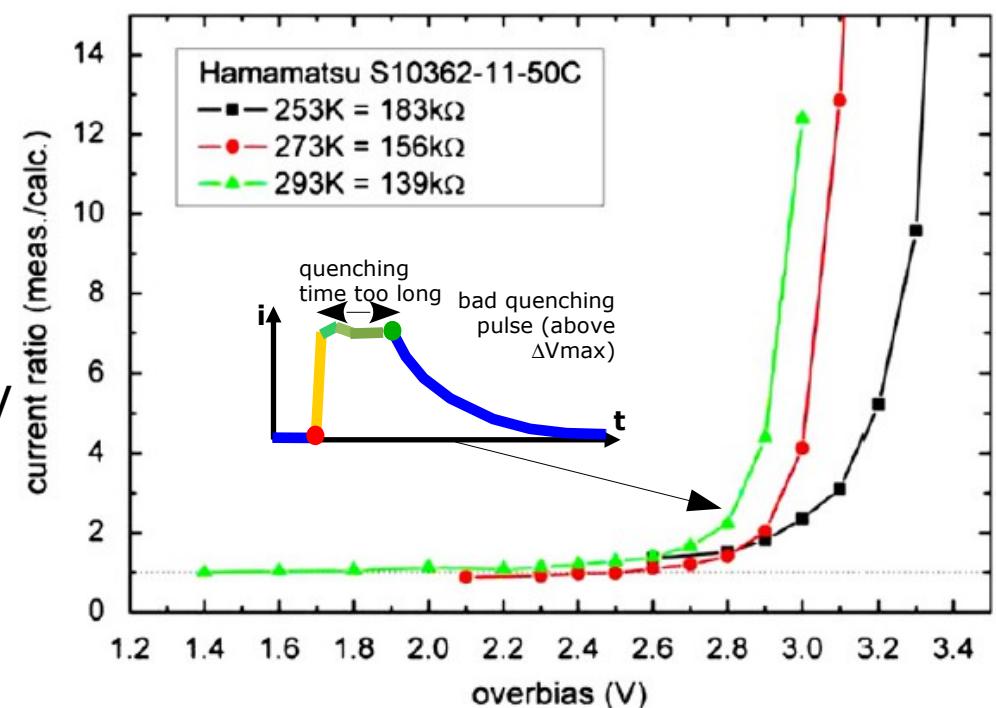
after Jendrysik et al NIM A 2011
doi:10.1016/j.nima.2011.10.007

$$R_I = \frac{I_D}{I'_D} = \frac{I_D}{DCR \cdot \bar{N} \cdot G \cdot q_e}$$

where \bar{N} is the average N of fired cells

Non-quenching regime for values of ΔV when R_I deviates significantly from 1

Jendrysik et al suggest
 $R_I=2$ as reasonable threshold



Passive Quenching (Resistive)

1) common solution: poly-silicon

2) alternative: metal thin film

→ higher fill factor

→ milder T dependence

3) alternative principle: bulk integrate resistor

→ flat optical window → simpler ARC

→ fully active entrance window

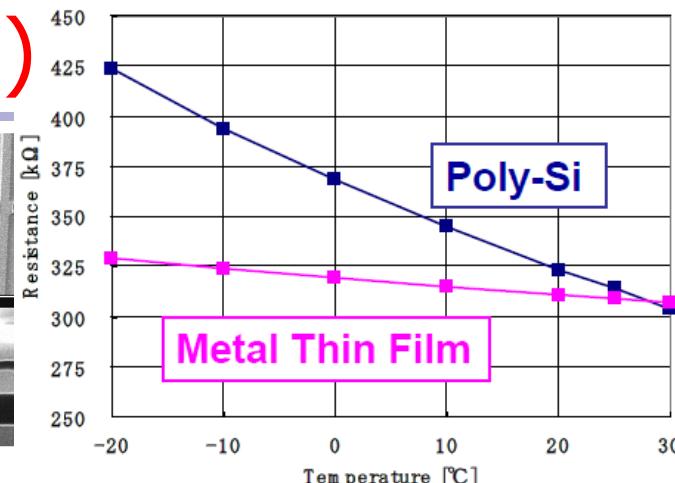
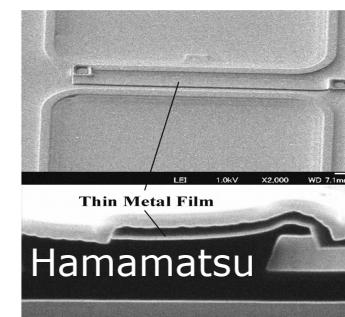
→ high fill factor (constraints only from guard ring and X-talk)

→ diffusion barrier against minorities

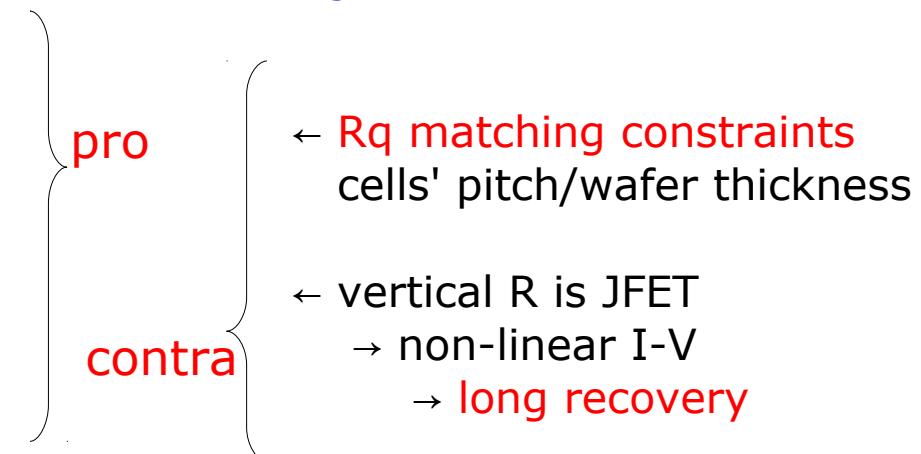
→ less X-talk

→ positive T coeff. ($R \sim T^{+2.4}$)

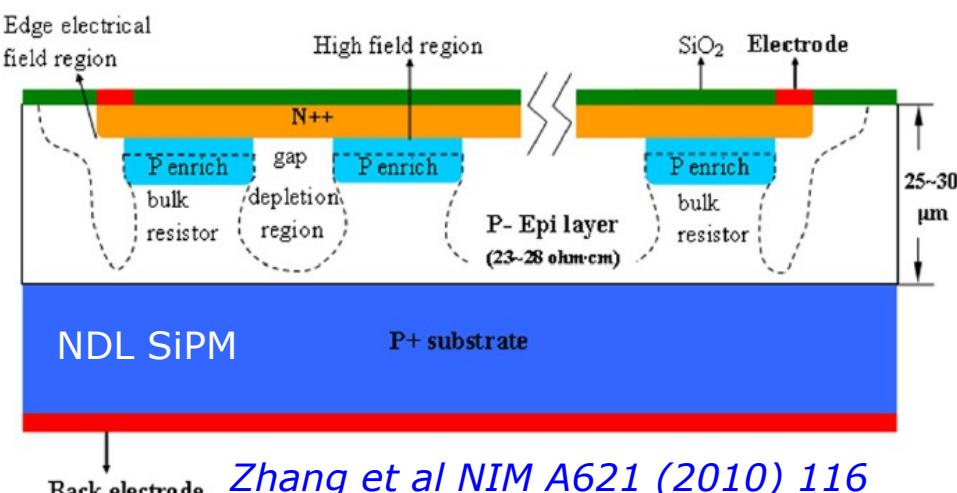
→ production process simplified → cost



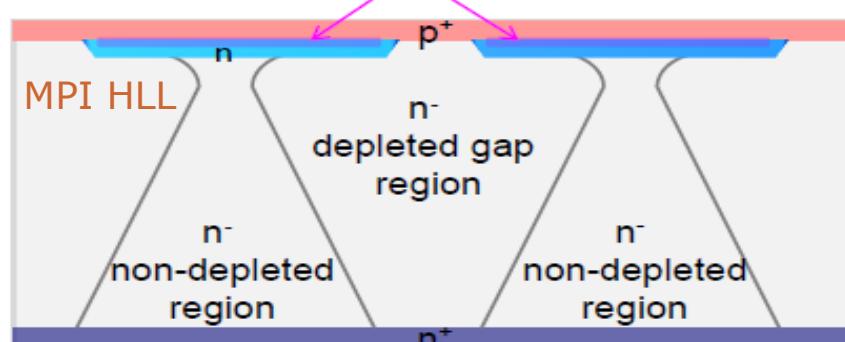
Nagano IEEE NSS-MIC 2011



principle proved



Zhang et al NIM A621 (2010) 116



Ninkovic et al NIM A610 (2009) 142
and NIM A628 (2011) 407

Richter et al US patent № 2011/0095388

Passive Quenching (Capacitive)

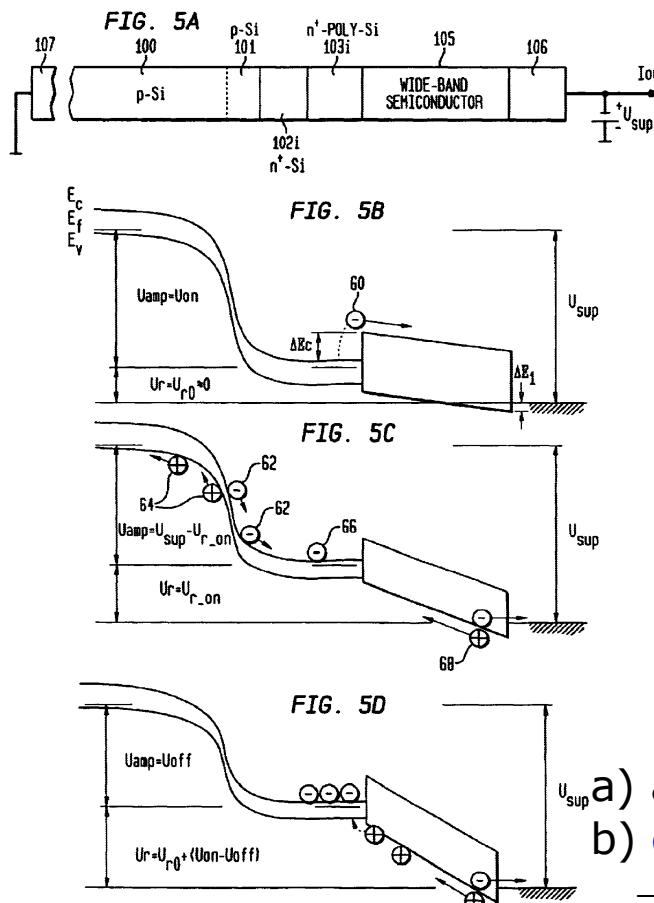
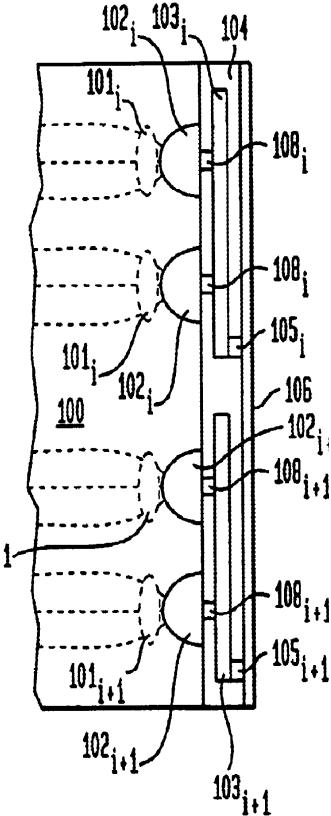
Quenching feedback due to charge accumulated by means by semiconductor barriers

Amplification Technologies

Shushakov et al US Patents

Nº 2004/6885827 and Nº 2011/7899339

FIG. 3

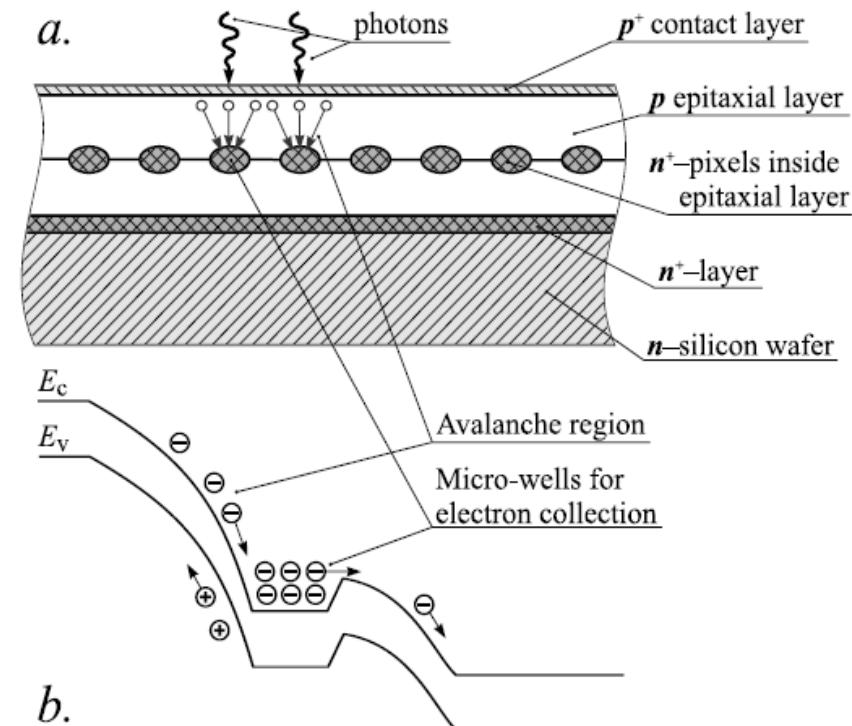


Note: induced signal is fast (ns)
but recovery quite slow (ms)
(non exponential)

Zecotek

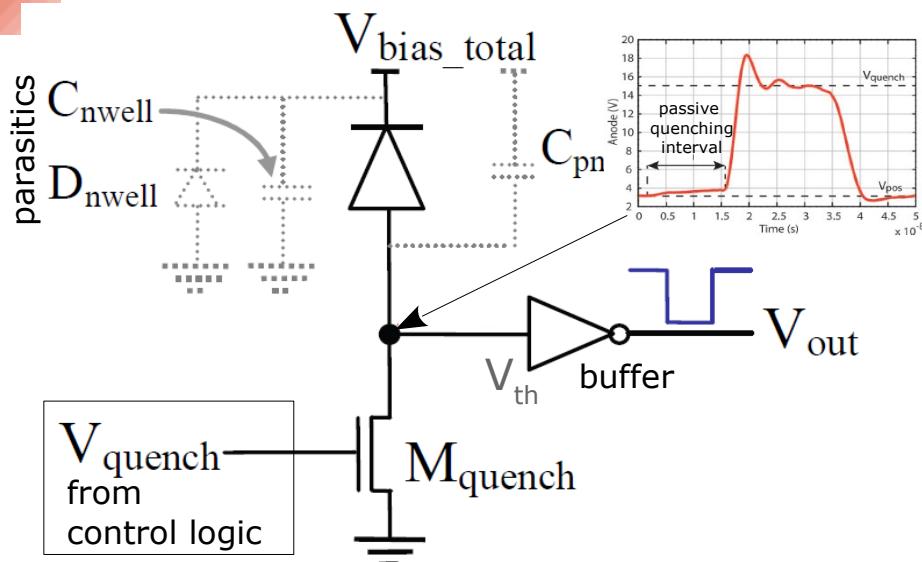
Sadygov et al arXiv 1001.3050

Sadygov RU Patents Nº 1996/2102820
and Nº 2006/2316848

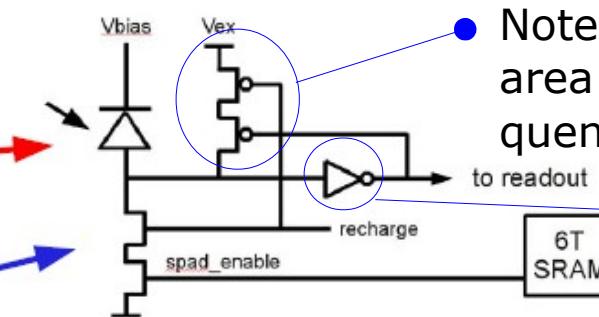
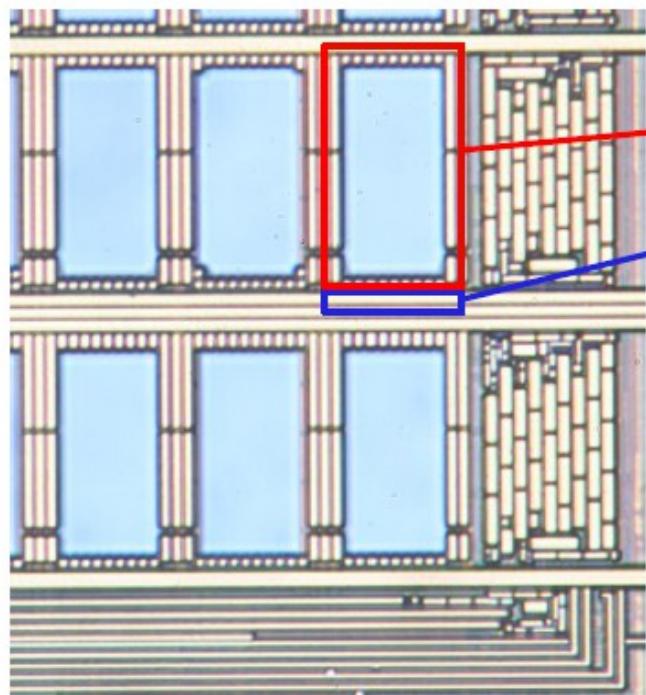


- avalanche at internal high field regions
- charges accumulated in isolated potential wells
→ E field reduced (locally) → avalanche quenched
→ Fast signal induced (capacitive) outside
- potential wells discharge slowly by tunneling
(discharge must be delayed for good quenching)
→ high E field recovered

Active Quenching



(in addition n-well regions (cathode) can be shared among many cells)



- Cell electronics area: $120\mu\text{m}^2$
- 25 transistors including 6T SRAM
- $\sim 6\%$ of total cell area
- Modified 0.18 μm 5M CMOS
- Foundry: NXP Nijmegen

dSiPM cell electronics

- Cell area $\sim 30 \times 50\mu\text{m}^2$
- Fill Factor $\sim 50\%$

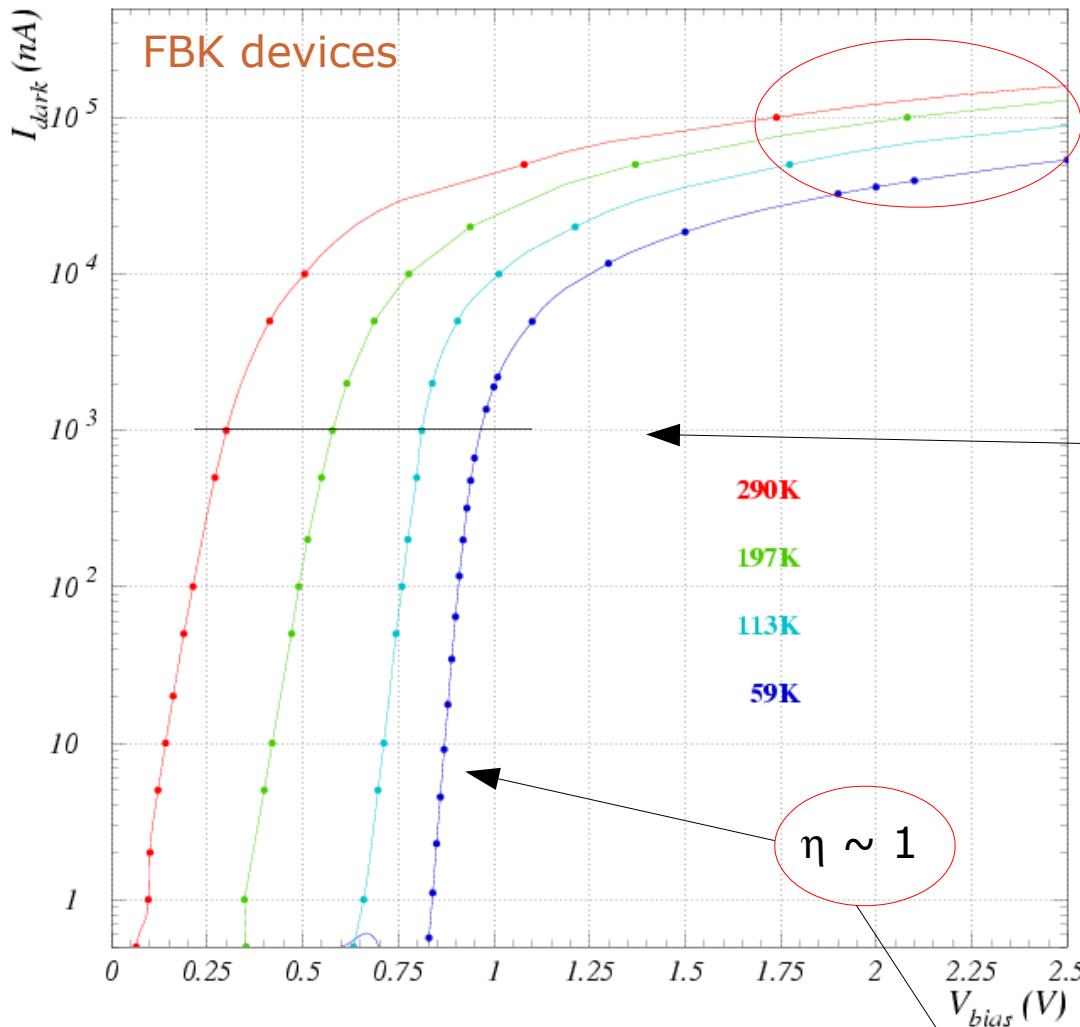
T.Frach at LIGHT 2011

I-V characteristics

- Information from Forward current →
 - R_q
 - junction Temperature
 - ...

- Information from Reverse current →
 - breakdown V_{bd}
 - T coefficient
 - ...

I-V characterization: forward bias



② **Voltage drop (V_d) decreases linearly with T decreasing (e.g. at 1 μ A)**

① **Forward current**

$$I_{forward} \sim C(\eta) A(T) \left[\exp\left(\frac{q V_d}{\eta k T}\right) - 1 \right]$$

Shockley et al. Proc. IRE 45 (1957)

η ideality factor
Diffusion current dominating: $\eta \rightarrow 1$
Recombination current dominating: $\eta \rightarrow 2$

③ **Ohmic behavior at high current**

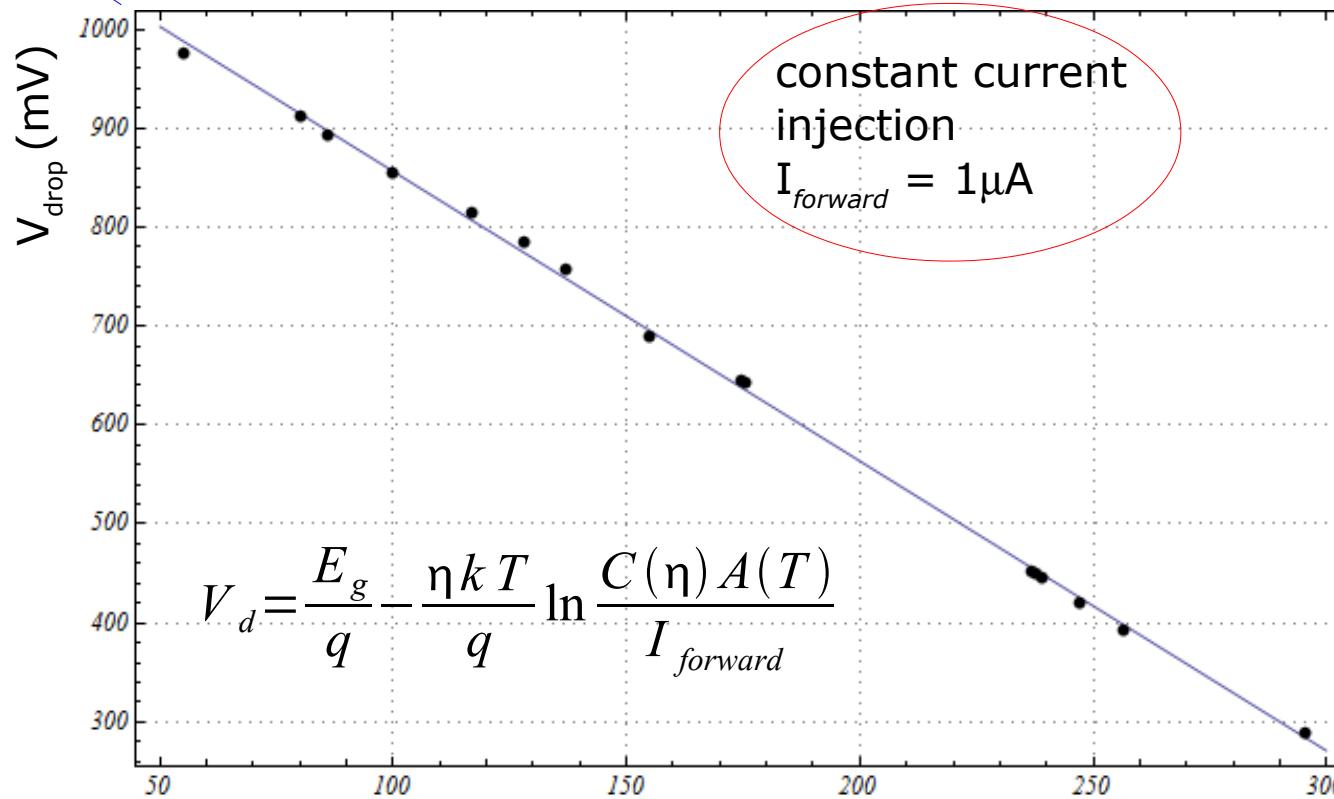
Linear fit $\rightarrow R_{series} \sim R_q / N_{cells}$

Forward I-V → Junction Temperature probe

Voltage drop at fixed forward current → precise **measurement of junction T...**

for $T \rightarrow 0$ ideally $V_d \rightarrow E_g$
(freeze-out effects apart)

... otherwise not trivially measured !

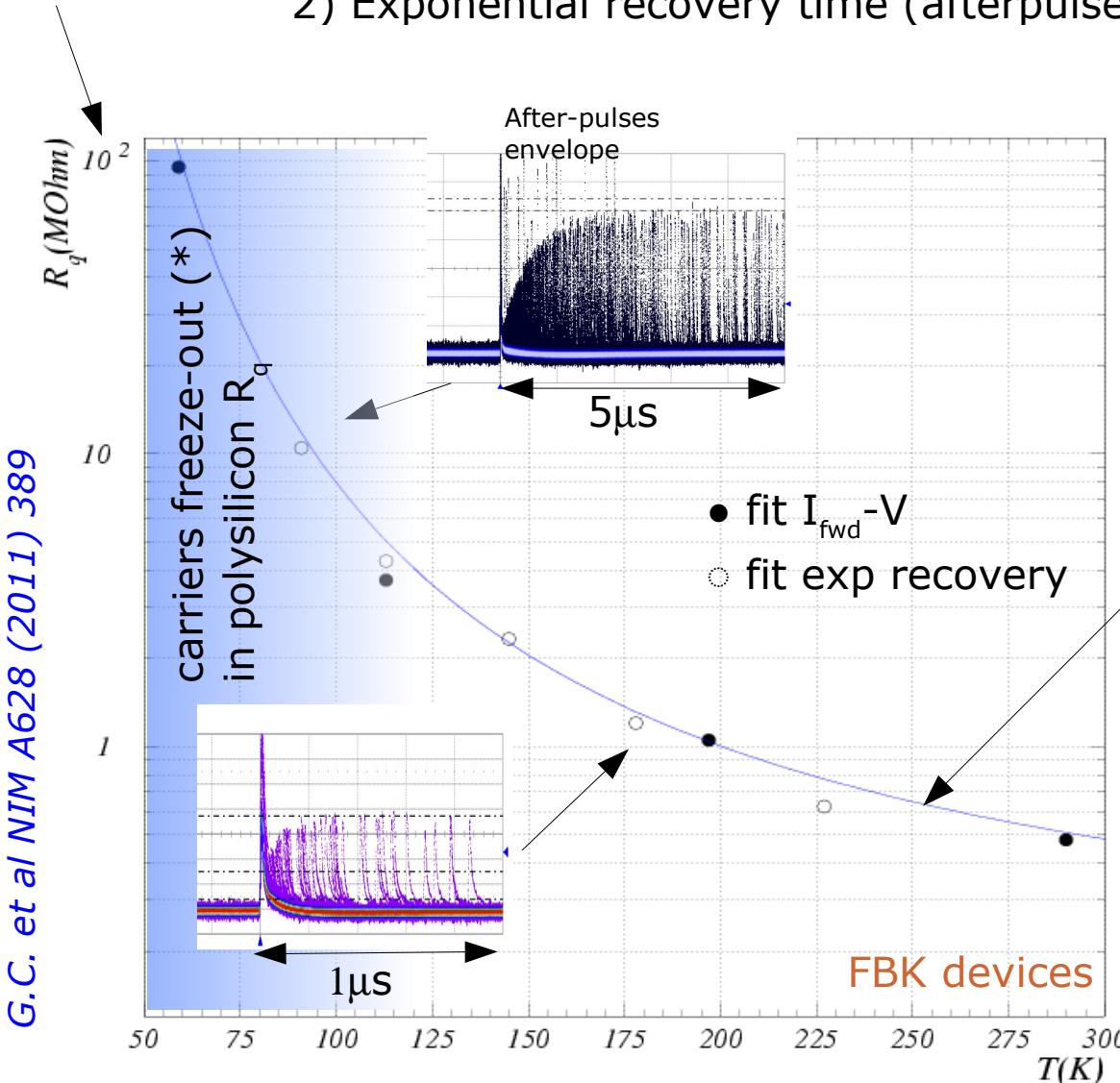


- (almost) linear dependence with slope $dV_{drop}/dT|_{1\mu\text{A}} \sim -3\text{mV/K}^T$ (K)
(we don't see freeze-out effects down to 50K)
- direct and precise **calibration/probe** of junction(s) Temperature

Forward I-V → Series Resistance (vs T)

Two ways for measuring series resistance (R_s)

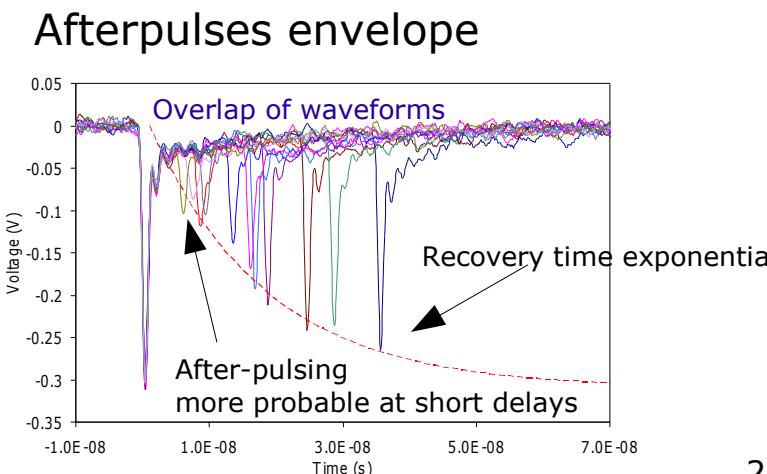
- 1) Fit at high V of forward characteristic
- 2) Exponential recovery time (afterpulses envelope)



Measurements (1) and (2) consistent
→ **dominant effect from quenching resistor R_q**
(→ series R bulk gives smaller contribution)

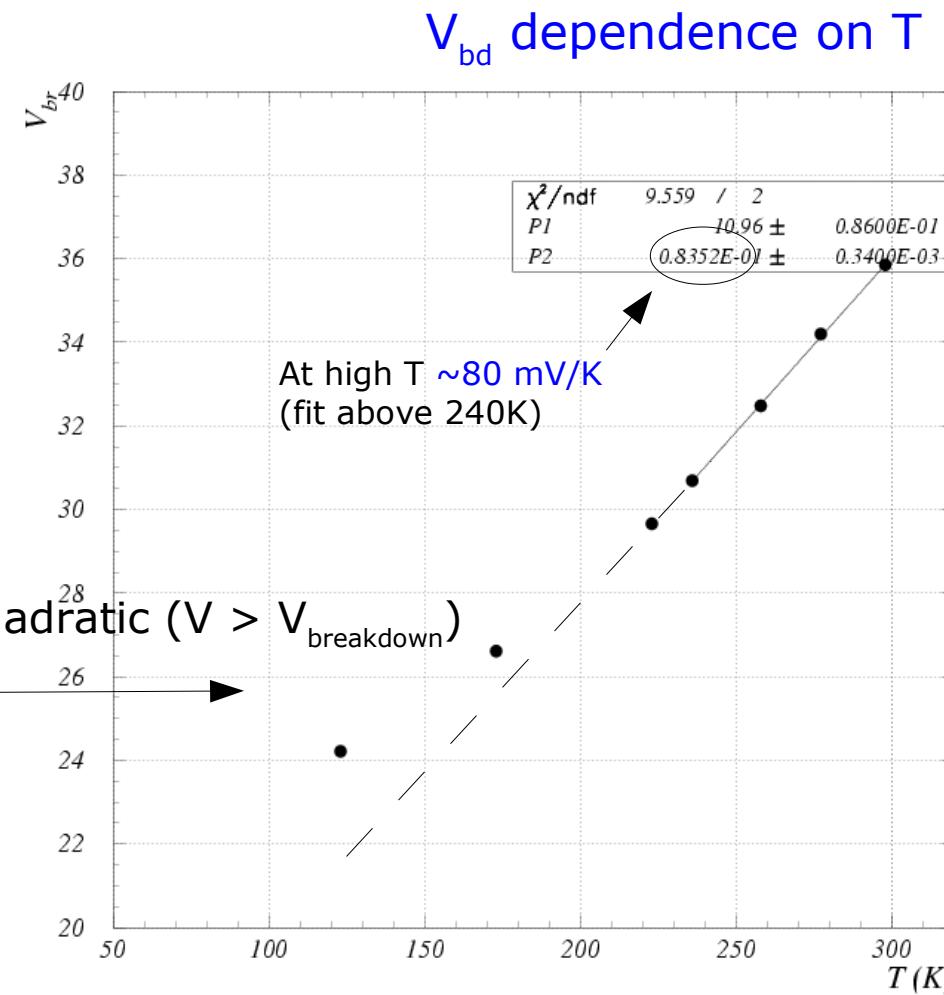
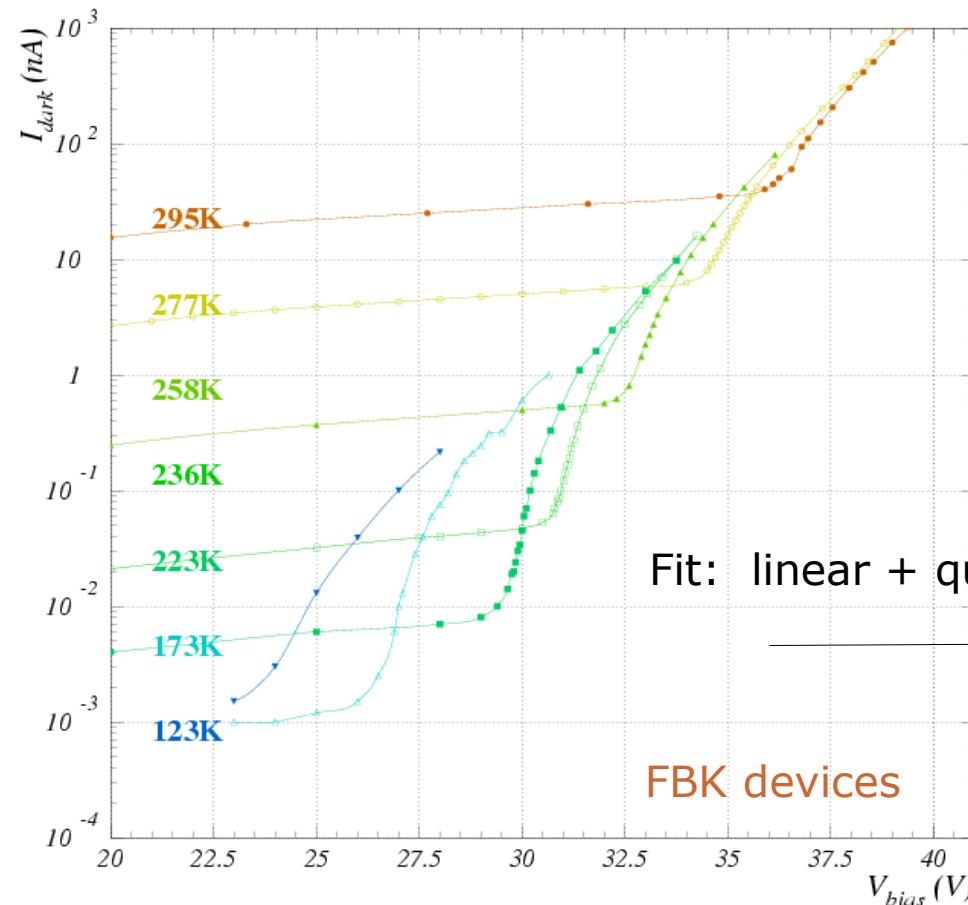
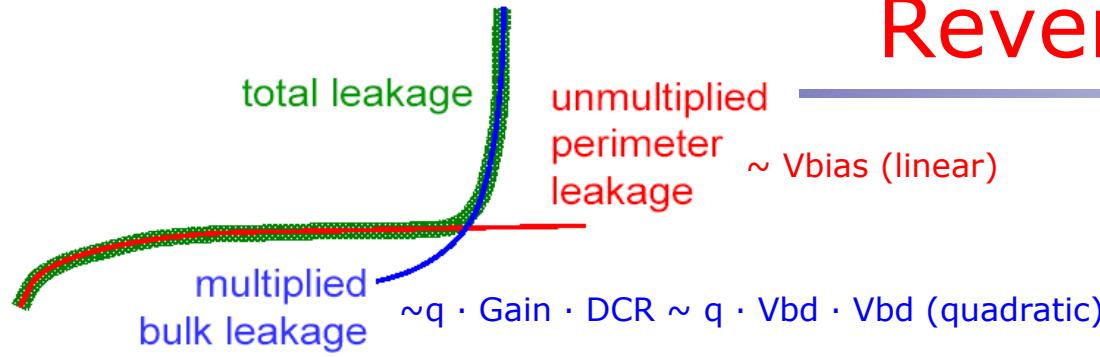
Empirical fit:

$$R_q(T) \sim 0.13(1 + 300/T e^{300/T}) M\Omega$$



Note: SiPM for low T applications must have appropriate quenching R (not quenching at room T !)

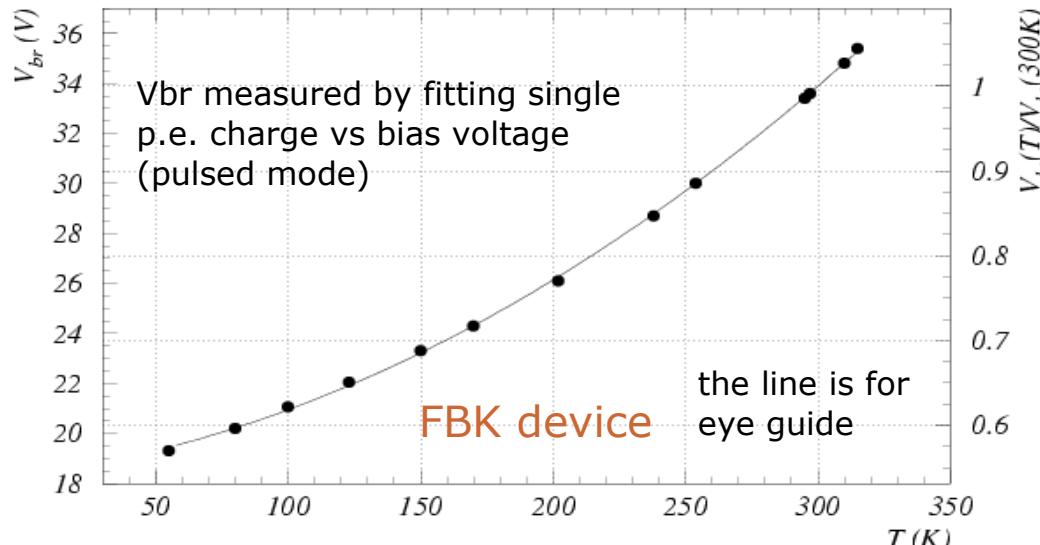
Reverse I-V



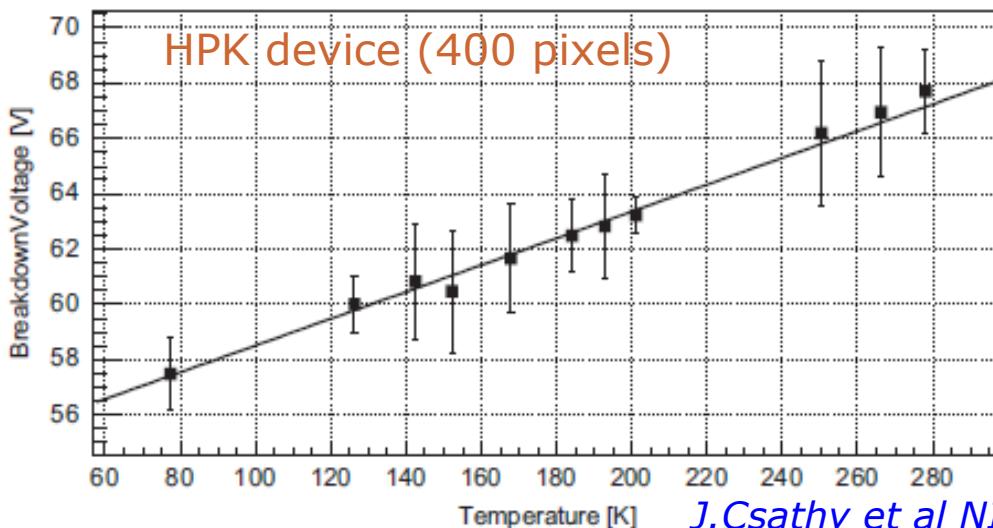
Breakdown voltage decreases at low T due to larger carriers mobility
 \rightarrow larger ionization rate (electric E field fixed)

V_{bd} vs T → T coefficient (ΔV stability)

Breakdown Voltage



G.C. et al NIM A628 (2011) 389



J.Csathy et al NIM A 654 (2011) 225

Temperature coefficient

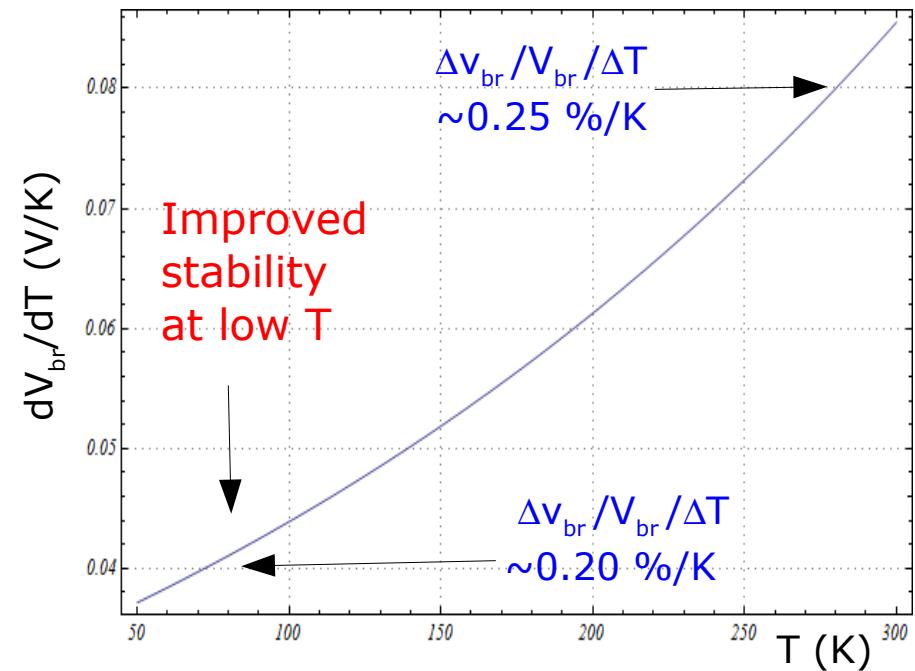
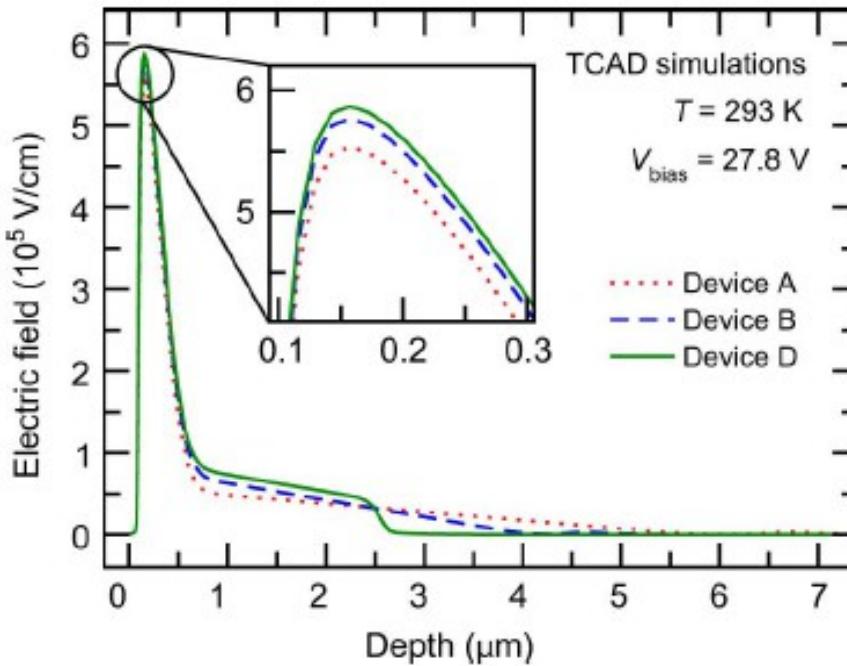


Fig. 6. Breakdown voltage as a function of temperature of the MPPC with 400 pixels.

Depletion layer $\rightarrow V_{bd}$ dependence on T



Narrow depletion layer (high background doping^(*) or thin epitaxial layer)

\rightarrow minimize V_{bd} dependence on T

$$\rightarrow \text{gain stability } \frac{\delta V_{bd}/V_{bd}}{\delta T} = \frac{\delta G/G}{\delta T}$$

(^{*}) resulting in epitaxial layer not fully depleted at V_{bd}

Trade off:

- \rightarrow PDE (thickness)
- \rightarrow minimum gain (capacity) against after-pulses and cross-talk

Serra et. al. (FBK) IEEE TNS 58 (2011) 1233
"Experimental and TCAD Study of Breakdown Voltage Temperature Behavior in n+/p SiPMs"

Note: precise agreement simulation/data is not trivial at all. Definition of ionization coefficients is device dependent...

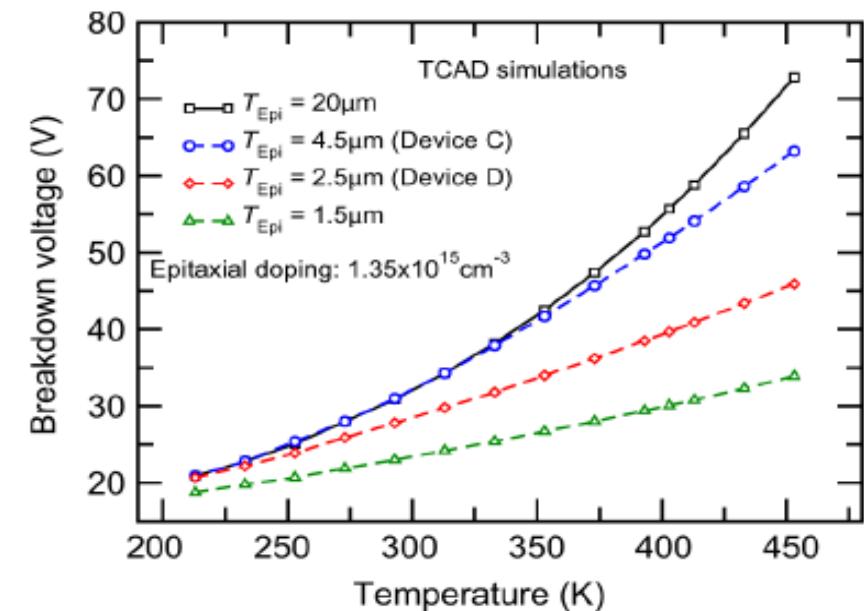
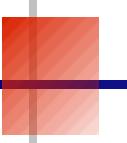


Fig. 9. TCAD simulated V_{BD} in the GM-APDs of this work (see Table I) in an extended temperature range. Two additional epitaxial layer thickness are considered ($20\mu\text{m}$, $1.5\mu\text{m}$) to emphasize the impact of the depletion layer width on the V_{BD} vs. temperature characteristic.



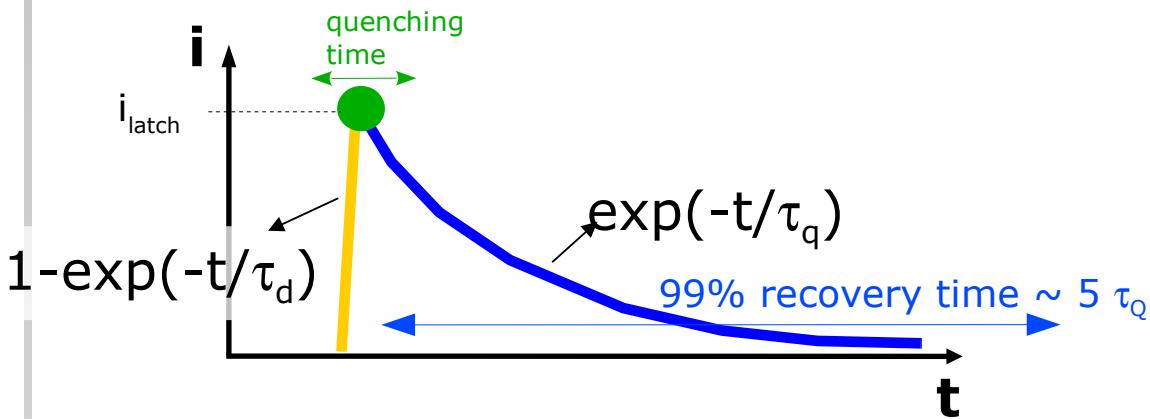
Pulse shape, Gain and Response

- Detailed electrical model
- Pulse shape
- Gain and Gain fluctuation
- Response non-linearity

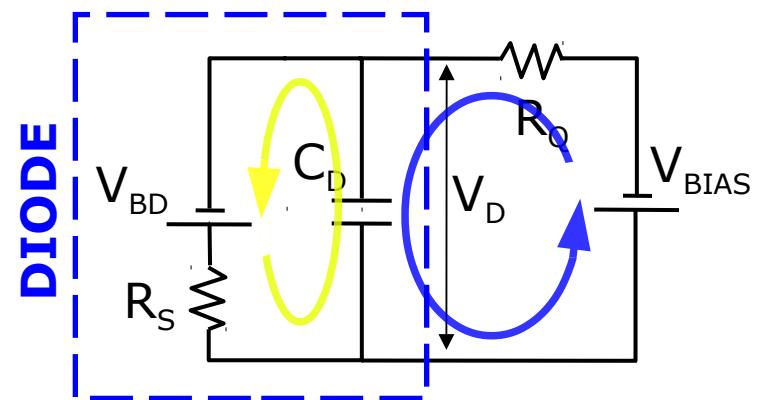
(mostly for passive mode)

Basic electrical model

Fast Capacitor (cell) discharge and slow recharge (roughly speaking)



currents **internal / external**



Rise time

$$\tau_d = R_d C_d \quad \Leftarrow \quad \tau_q = R_q C_d$$

Recovery time:

T dependence due to R_q
 C_d is independent of T

Rise time: T dependent (to lesser extent) due to R_d

Gain $\sim C \Delta V \rightarrow$ independent of T

at fixed Over-Voltage ($\Delta V = V_{bias} - V_{bd}$)

SiPM equivalent circuit (detailed model)

Single cell model $\rightarrow (R_d \parallel C_d) + (R_q \parallel C_q)$

SiPM + load $\rightarrow (\parallel Z_{cell}) \parallel C_{grid} + Z_{load}$

Signal = **slow** pulse ($\tau_{d(rise)}, \tau_{slow(fall)}$) +
+ **fast** pulse ($\tau_{d(rise)}, \tau_{fast(fall)}$)

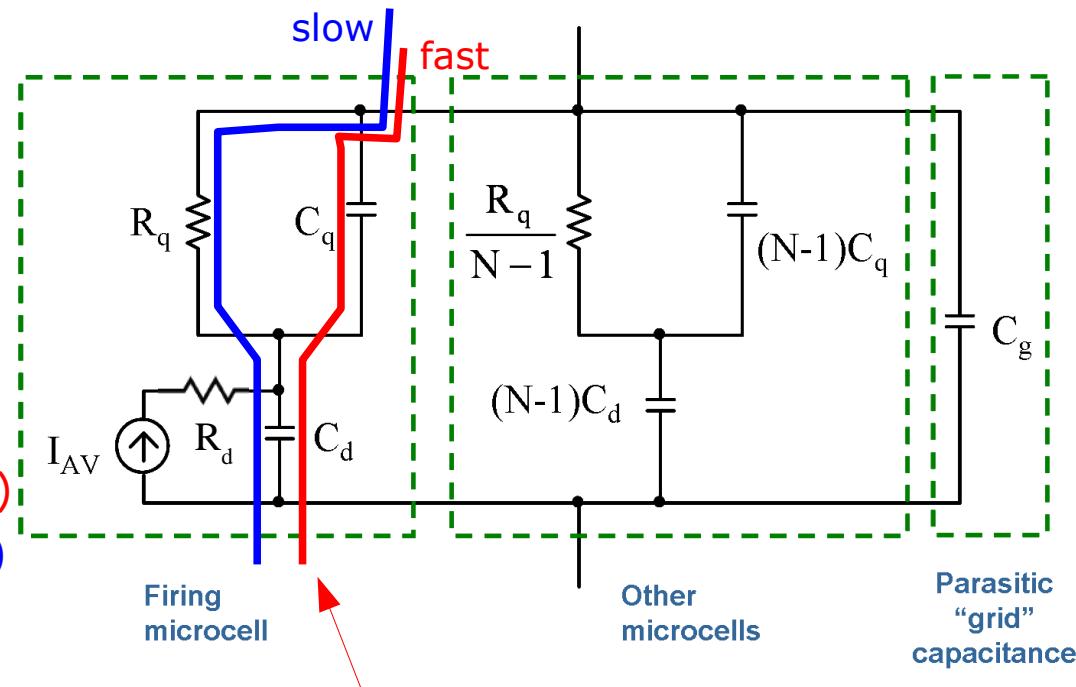
- $\bullet \tau_{d(rise)} \sim R_d(C_q + C_d)$

- $\bullet \tau_{fast(fall)} = R_{load} C_{tot}$ (fast; parasitic spike)

- $\bullet \tau_{slow(fall)} = R_q(C_q + C_d)$ (slow; cell recovery)

F.Corsi, et al. NIM A572 (2007) 416

S.Seifert et al. IEEE TNS 56 (2009) 3726



C_q → fast current supply path in the beginning of avalanche

Pulse shape

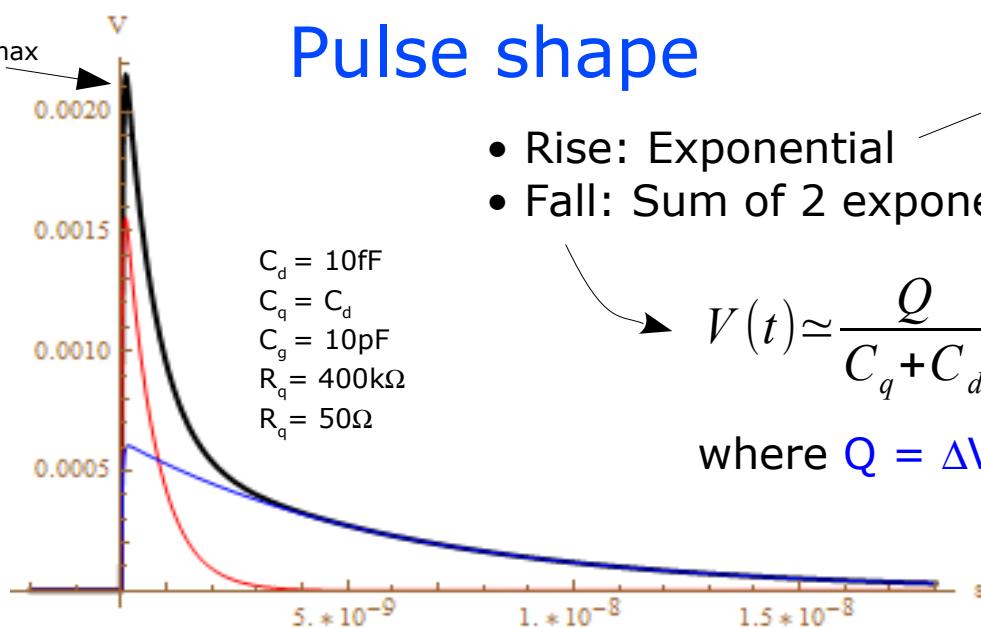
- Rise: Exponential
- Fall: Sum of 2 exponentials

Sp. Charge $R_d \times C_{d,q}$ filtered by parasitic inductance, stray C, ... (Low Pass)

$$V(t) \approx \frac{Q}{C_q + C_d} \left(\frac{C_q}{C_{tot}} e^{\frac{-t}{\tau_{FAST}}} + \frac{R_{load}}{R_q} \frac{C_d}{C_q + C_d} e^{\frac{-t}{\tau_{SLOW}}} \right) \quad \text{for } R_{load} \ll R_q$$

where $Q = \Delta V (C_q + C_d)$ is the total charge released by the cell

→ 'prompt' charge on C_{tot} is $Q_{fast} = Q C_q / (C_q + C_d)$



Pulse shape

$$V(t) \simeq \frac{Q}{C_q + C_d} \left(\frac{C_q}{C_{tot}} e^{\frac{-t}{\tau_{fast}}} + \frac{R_{load}}{R_q} \frac{C_d}{C_q + C_d} e^{\frac{-t}{\tau_{slow}}} \right) = \frac{Q R_{load}}{C_q + C_d} \left(\frac{C_q}{\tau_{fast}} e^{\frac{-t}{\tau_{fast}}} + \frac{C_d}{\tau_{slow}} e^{\frac{-t}{\tau_{slow}}} \right)$$

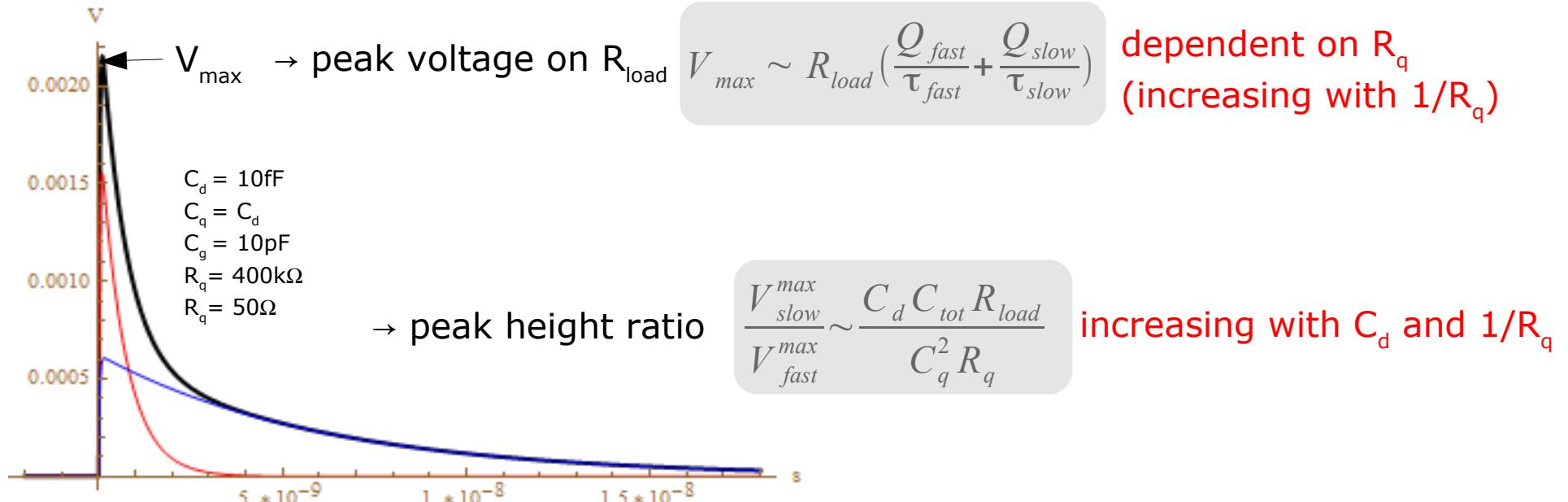
→ gain $G = \int dt \frac{V(t)}{q_e R_{load}} = Q/q_e = \frac{\Delta V(C_d + C_q)}{q_e}$ independent of R_q

→ charge ratio $\frac{Q_{slow}}{Q_{fast}} \sim \frac{C_d}{C_q}$

Note: valid for low impedance load

$$R_{load} \ll R_q$$

- $\tau_{fast} = R_{load} C_{tot}$
- $\tau_{slow} = R_q (C_q + C_d)$



Pulse shape: dependence on Temperature

The two current components behave differently with Temperature
→ fast component is independent of T because C_{tot} couples to external R_{load}
→ slow component is dependent on T because $C_{d,q}$ couple to $R_q(T)$

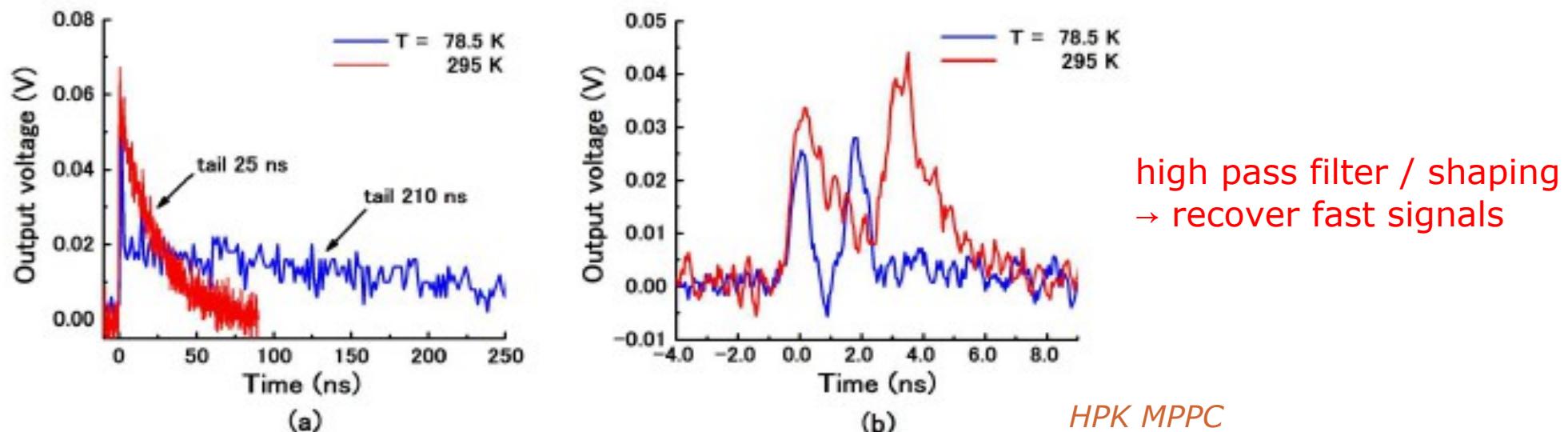
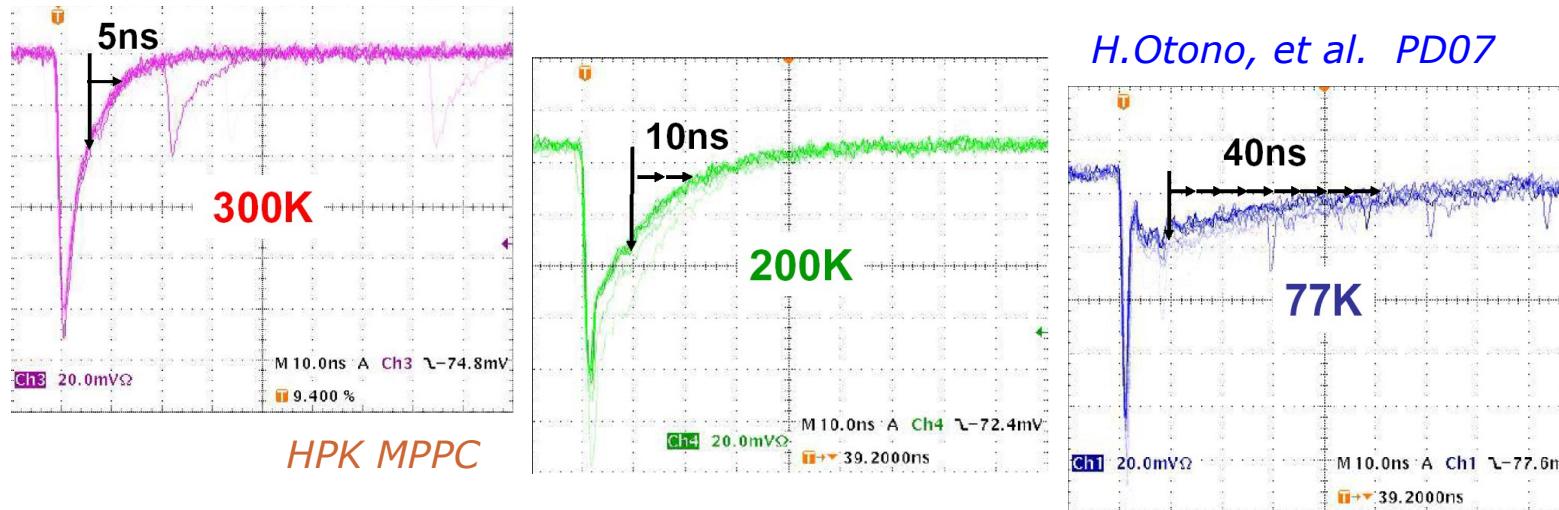
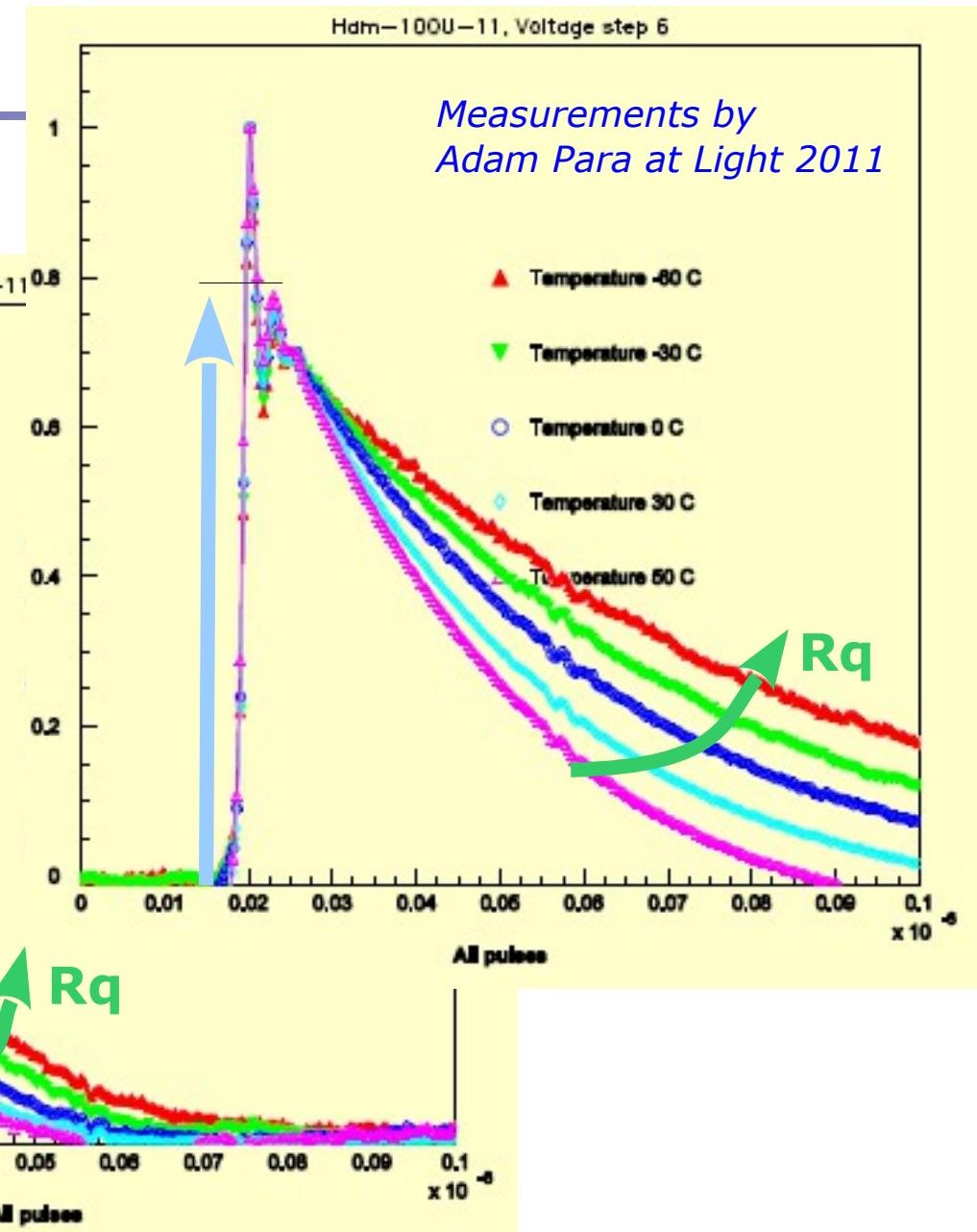
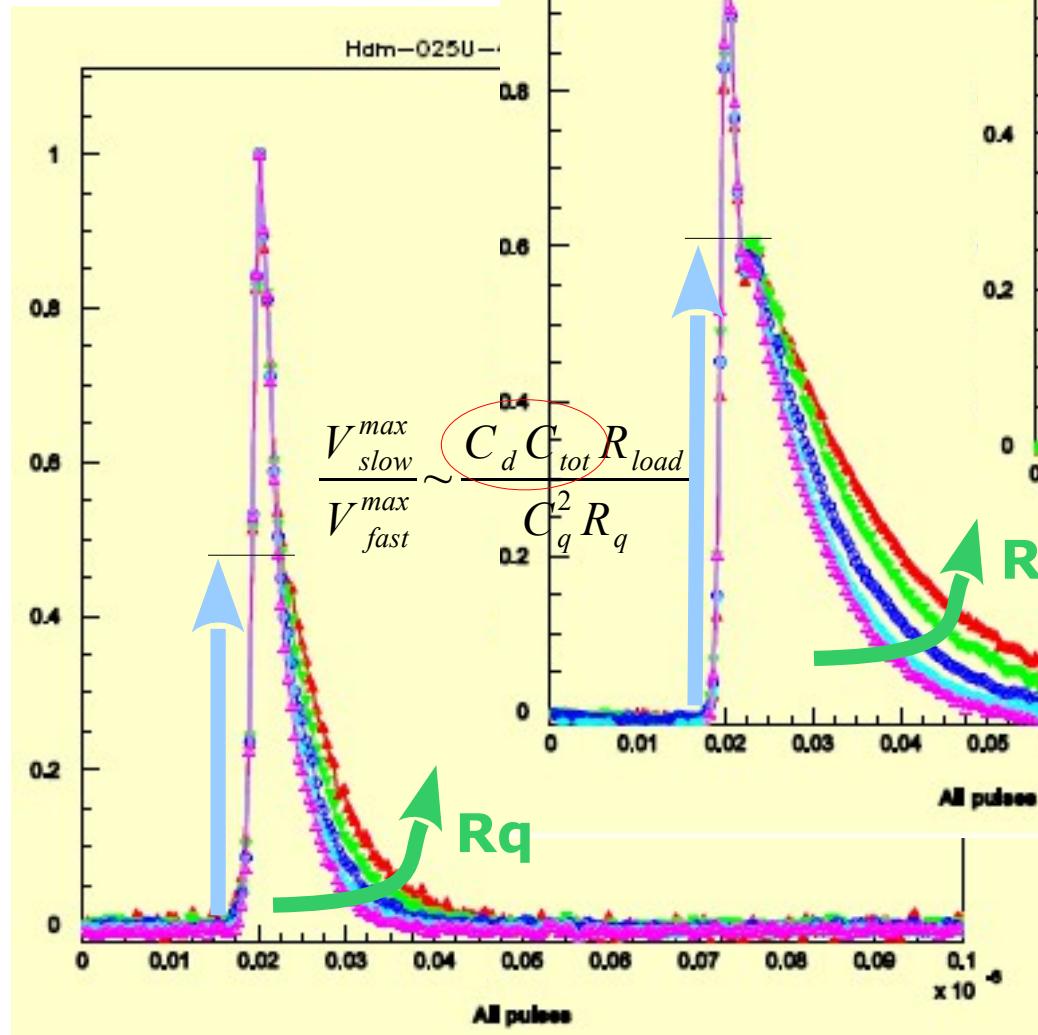


Fig. 2. (a) Output signals from the MPPC when no high-pass filter is used, and (b) output signals from the high-pass filter when two pulses were generated successively.

Akiba et al Optics Express 17 (2009) 16885

Pulse shape vs T

HPK MPPC: 25μm, 50μm, 100μm



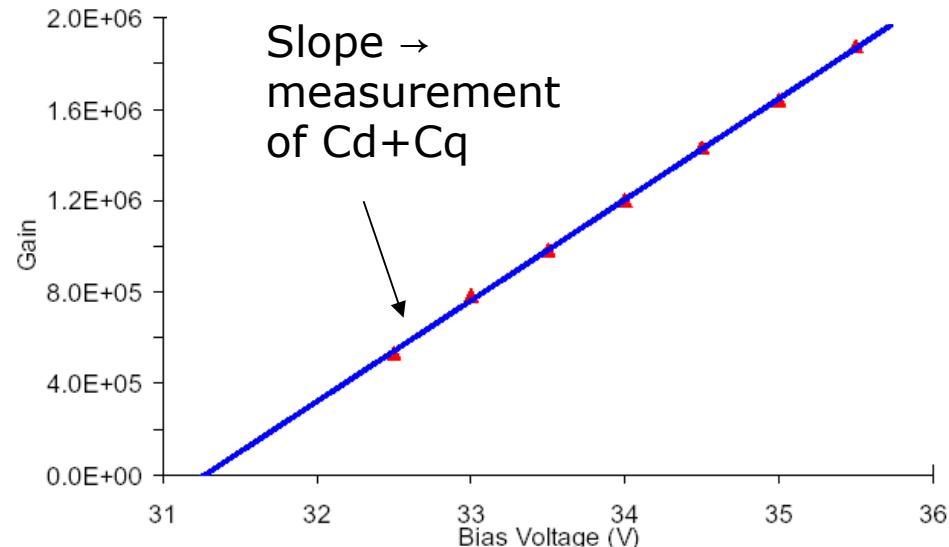
Measurements by
Adam Para at Light 2011

Gain and its Fluctuations

$$G = \Delta V (C_q + C_d) / q_e$$

→ Gain is linear if ΔV in quenching regime
but

there are many sources for non-linearity of response (non proportionality)



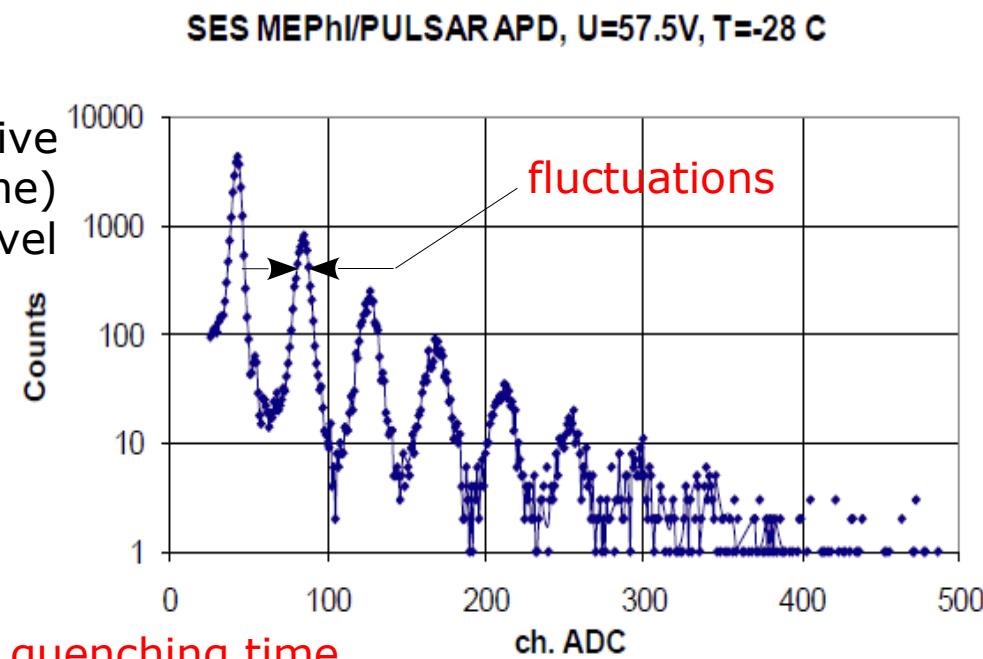
SiPM gain fluctuations (intrinsic) differ in nature compared to APD where the statistical process of internal amplification shows a characteristic fluctuations

$$\frac{\delta G}{G} = \frac{\delta V_{bd}}{V_{bd}} \oplus \frac{\delta C_{dq}}{C_{dq}}$$

cell to cell uniformity (active area and volume) control at % level

- doping densities (Poisson):
 $\delta V_{bd} \geq 0.3V$
Shockley, Sol. State Ele. 2 (1961) 35
- doping, epitaxial, oxide (processing):
 $\delta V_{bd} \sim O(0.1V)$

In addition δG might be due to fluctuations in quenching time
... and of course after-pulses contribute too (not intrinsic → might be corrected)



Response Non-Linearity

Non-proportionality of charge output w.r.t. number of photons (i.e. response) at level of several % might show up even in quenching regime (negligible quenching time), depending on ΔV and on the intensity and duration of the light pulse.

Main sources are:

- finite number of pixels
- finite recovery time w.r.t. pulse duration
- after-pulses, cross-talk
- drop of ΔV during the light pulse due to relevant signal current on (large) series resistances (eg ballast)

T.van Dam IEEE TNS 57 (2010) 2254

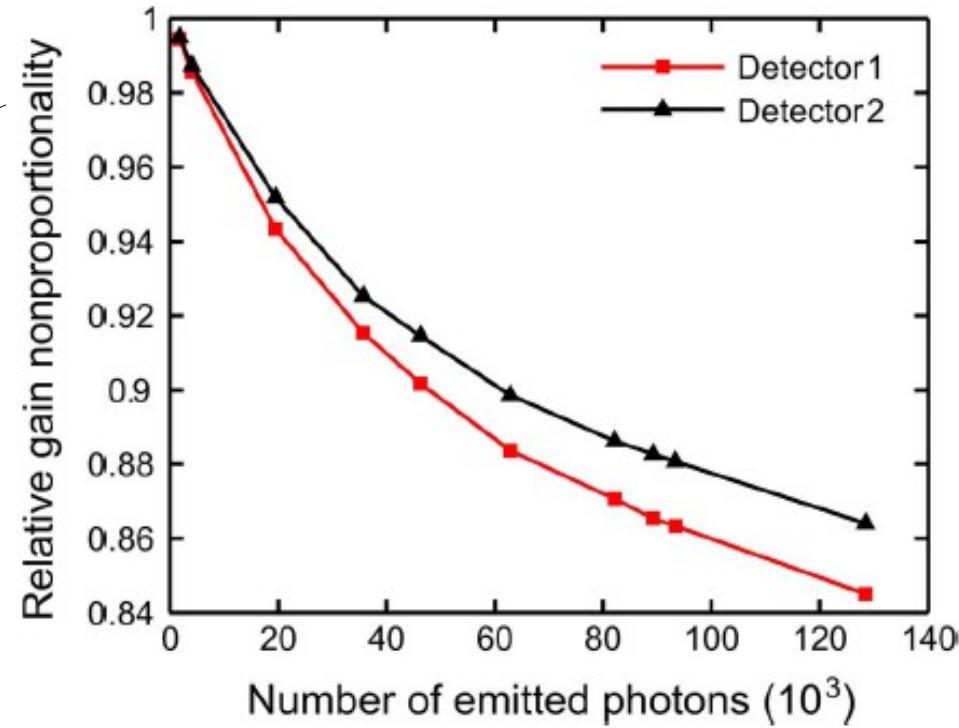
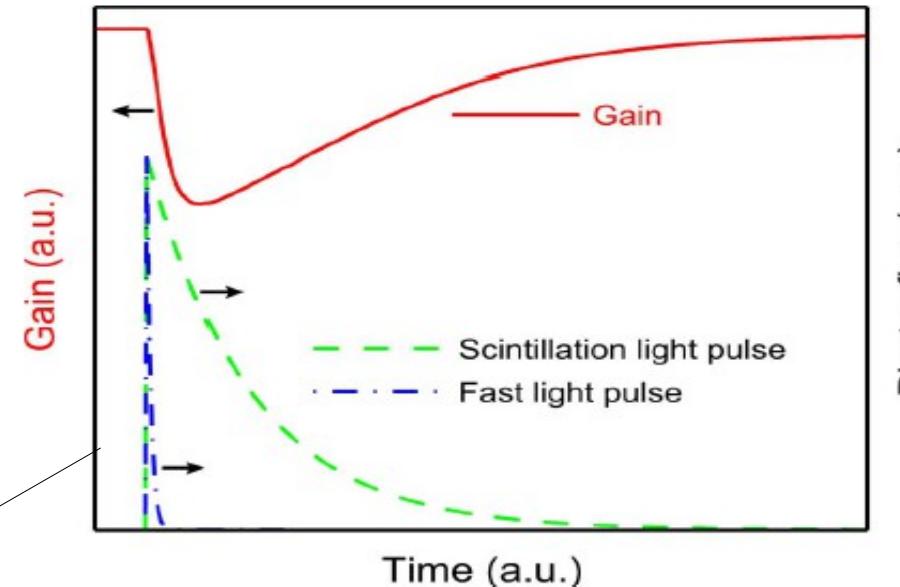
Detailed model to estimate non-lin. corrections

Finite number of cells is main contribution in case number of photons $\sim O(\text{number of cells})$ (dynamic range not adequate to application)

$$\rightarrow \text{saturation} \quad n_{\text{fired}} = n_{\text{all}} \left(1 - e^{-\frac{n_{\text{phot. PDE}}}{n_{\text{all}}}} \right)$$

\rightarrow loss of energy resolution

see Stoykov et al JINST 2 P06500 and Vinogradov et al IEEE NSS 2009 N28-3

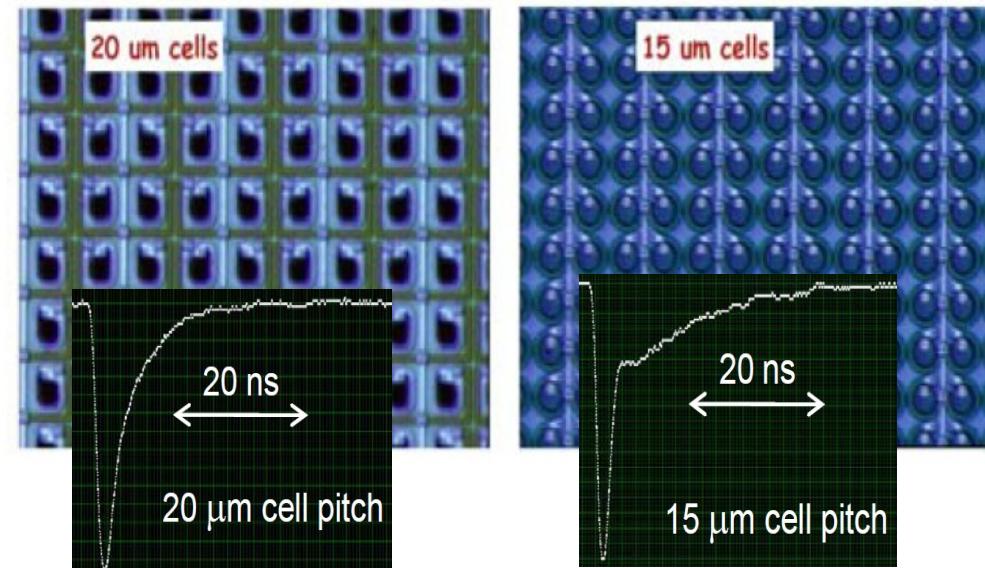


New high dynamic range SiPMs

Different types available or in preparation:

- **tiny cells**
→ HPK, FBK, NDL, MPI-LL
- **micro cells**
→ Zecotek, AmpliticationTech

Latest MPPC tiny cell by Hamamatsu



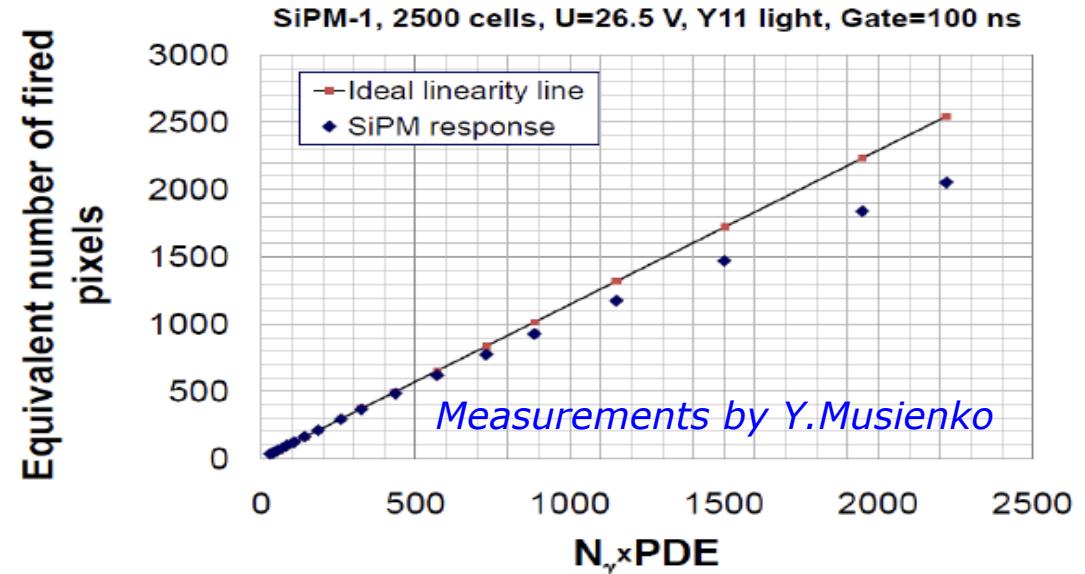
SiPMs NDL (Beijing)

Zhang et al NIM A621 (2010) 116

Han at NDIP 2011

- type: n-on-p, Bulk Rq
- high cell density ($10000/\text{mm}^2$)
- fast recovery (5ns)
- low gain

→ dynamic range
→ radiation hardness



Noise sources:

Dark counts

After-pulsing

Cross-Talk

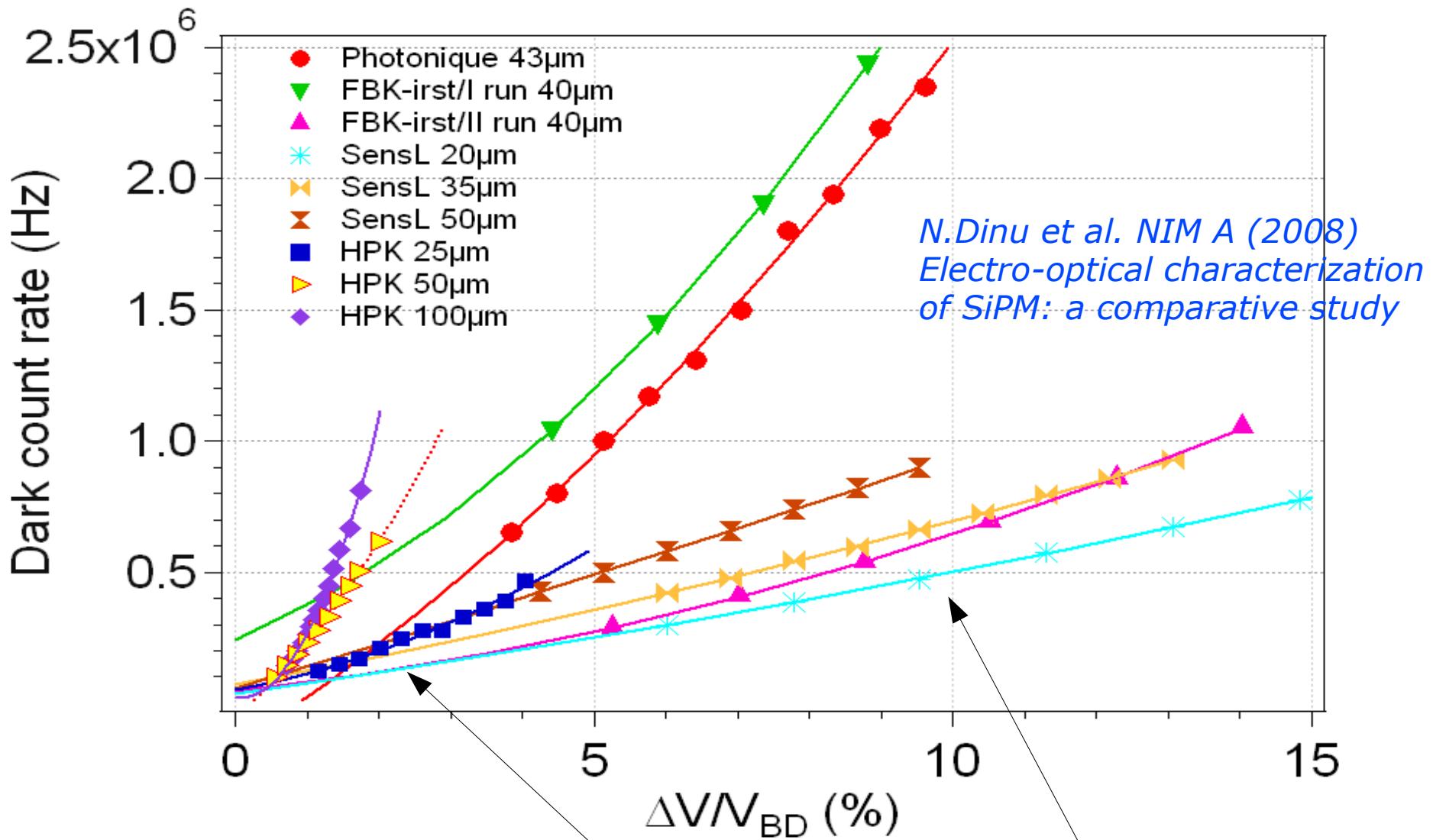
"optical"

pulses triggered by non-photo-generated carriers (thermal / tunneling generation in the bulk or in the surface depleted region around the junction)

carriers can be trapped during an avalanche and then released triggering another avalanche

photo-generation during the avalanche discharge. Some of the photons can be absorbed in the adjacent cell possibly triggering new discharges

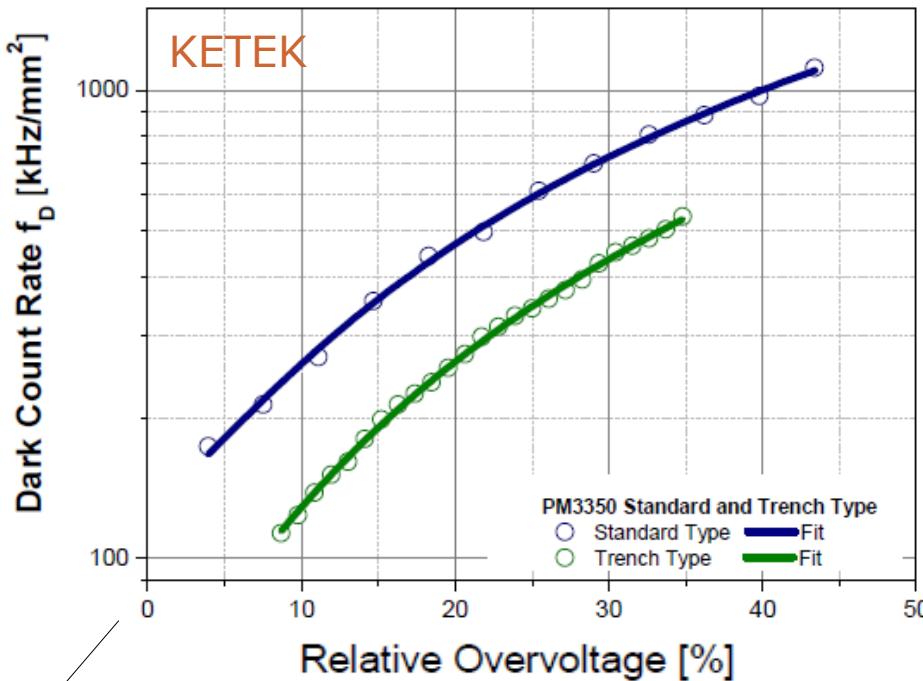
Dark Count Rate



- DCR \rightarrow linear dependence due to $P_{01} \propto \Delta V$ (\rightarrow same as PDE vs ΔV)
 \rightarrow non-linear at high ΔV due to cross-talk and after-pulsing $\rightarrow \propto \Delta V^2$
- DCR scales with active surface (not with volume: high field region dominating)

Dark Count Rate

KETEK PM 3350 (p⁺-on-n, shallow junction)
3x3mm² active area pixel size 50x50 μm²



$V_{bd} \sim 25V$

F.Wiest - AIDA 2012 at DESY

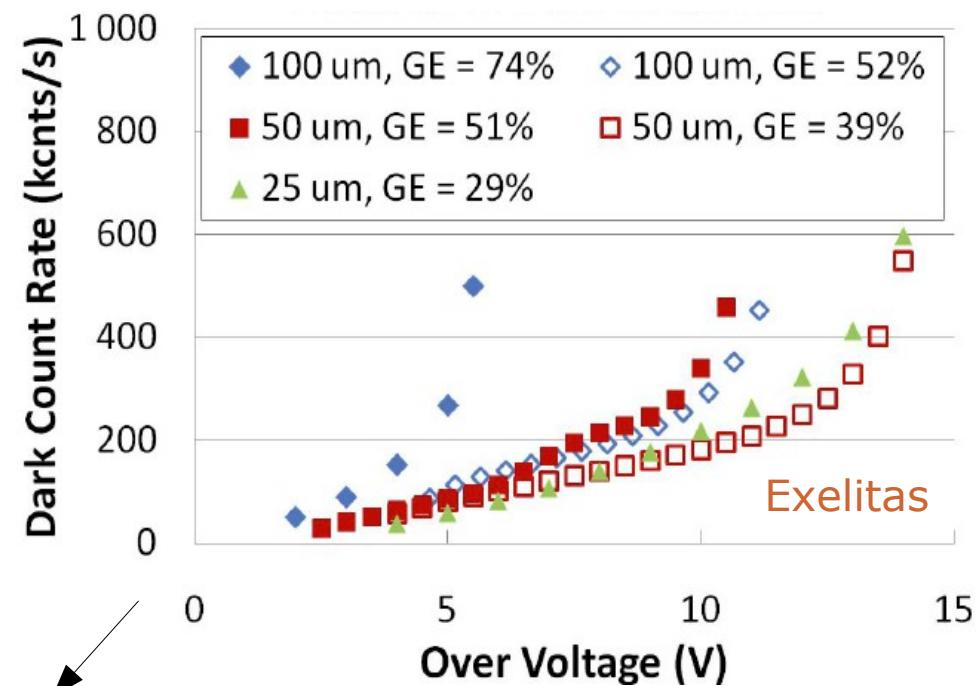
Latest Hamamatsu devices
reached ~80kHz/mm²

HPK claiming for additional
improvements coming
(HPK at LIGHT 2011)

Critical issues:

- quality of epitaxial layer
- gettering techniques
- Efield engineering (low T)

Exelitas 1st generation SiPM 2011
(p⁺-on-n) 1x1mm²

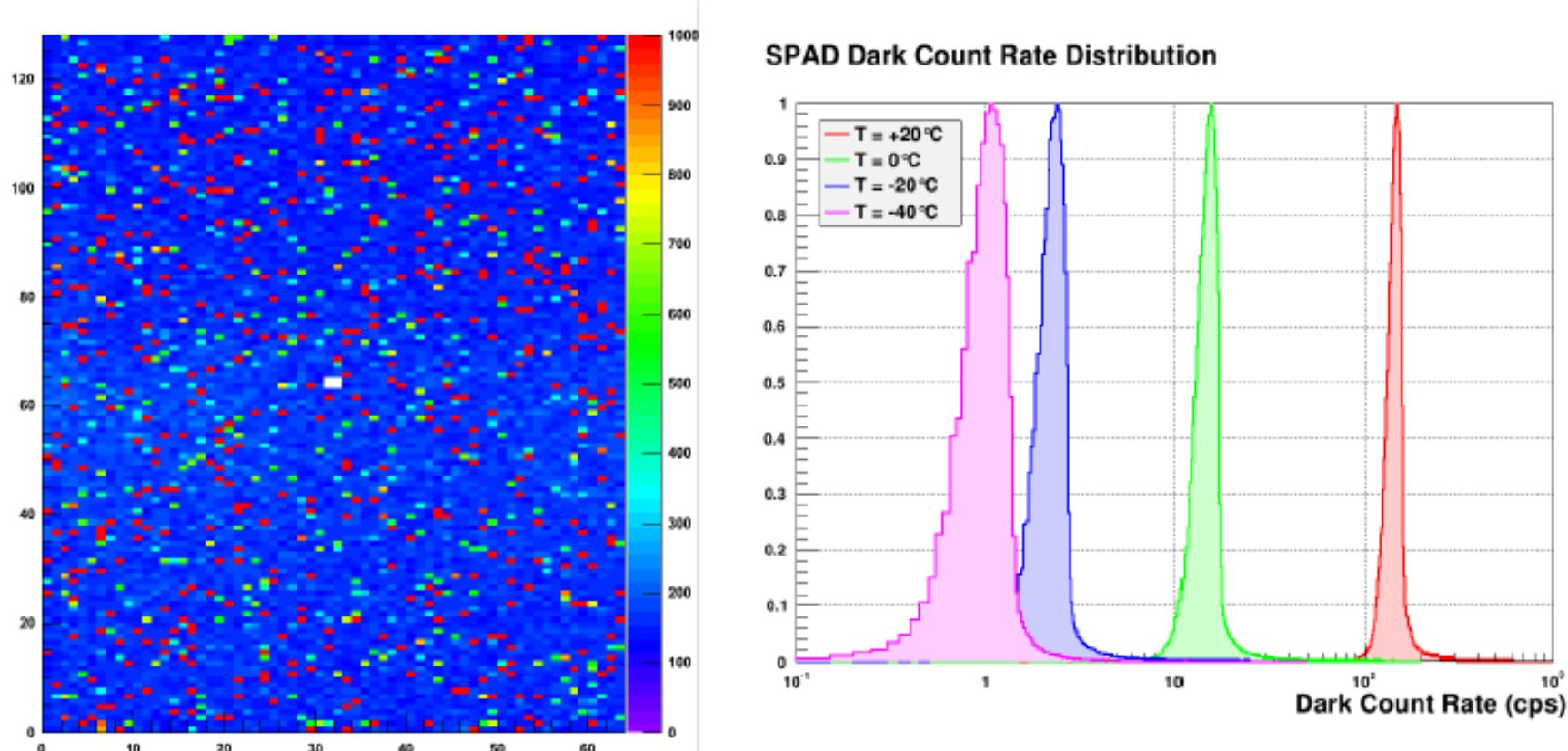


P.Berard - NDIP 2011

Dark Count Rate

dSiPM

Control over individual SPADs enables detailed device characterization



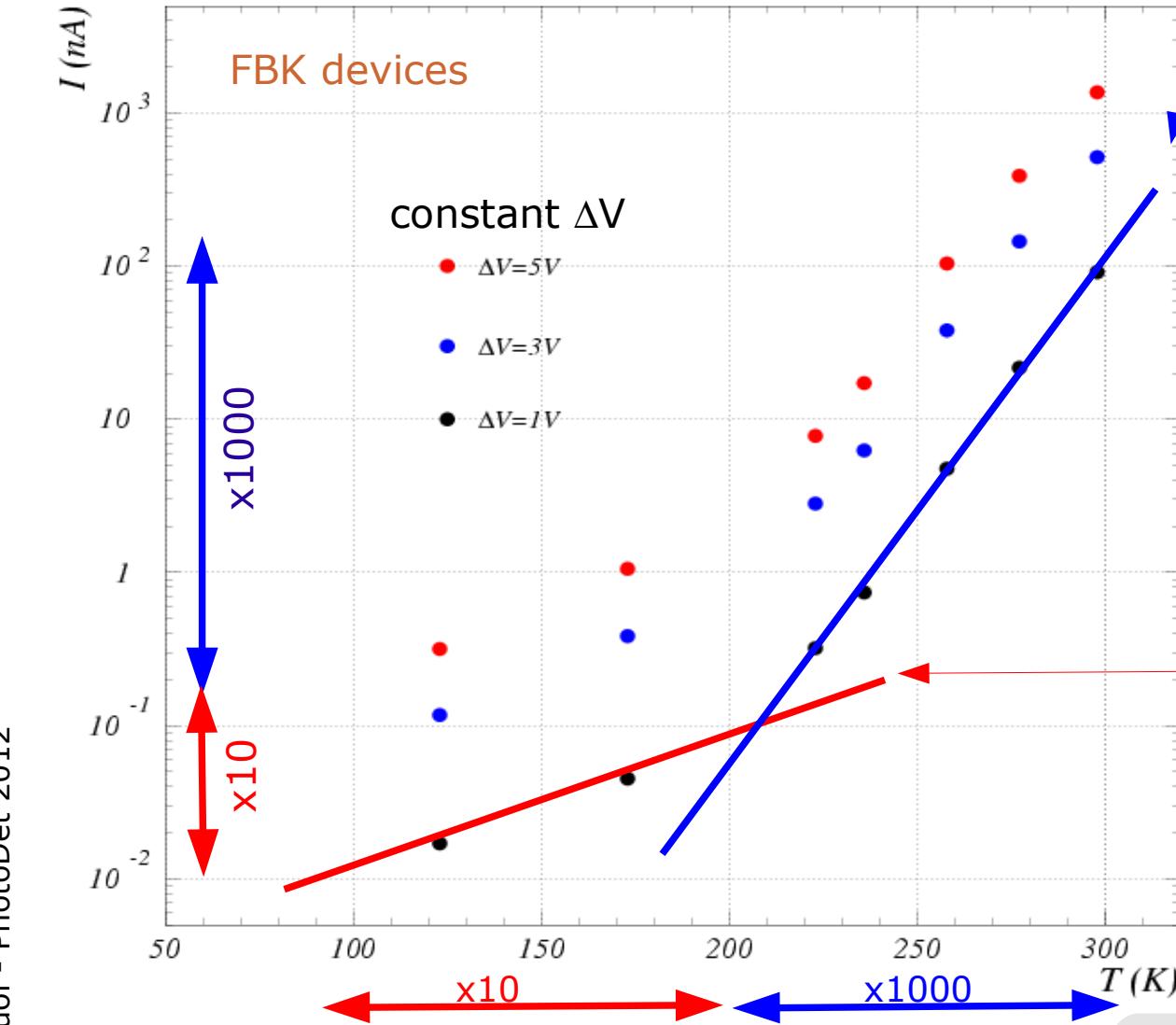
- Over 90% good diodes (dark count rate close to average)
- Typical dark count rate at 20°C and 3.3V excess voltage: ~150cps / diode
- Low dark counts (~1-2cps) per diode at -40°C

T.Frach at NDIP 2011

Dark current vs T sources of DCR

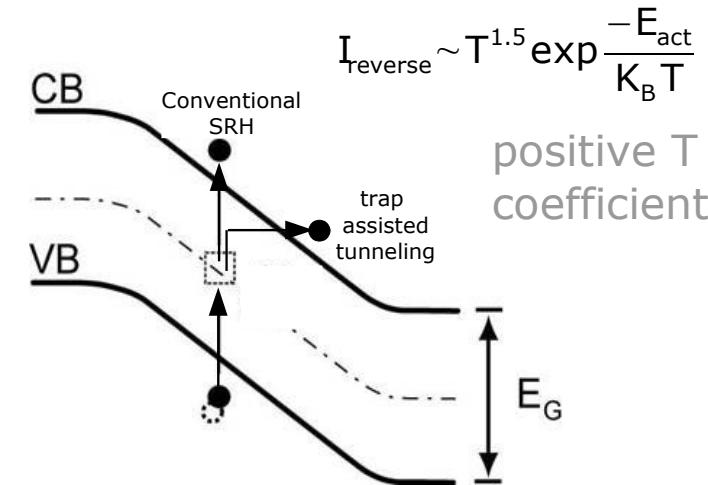
contribution to DCR
from diffusion of minority
carriers negligible below 350K

Noise mainly comes from the **high E Field**
region (no whole depletion region)



Tunneling noise dominating for $T < 200K$
(FBK devices have E field quite peaked)

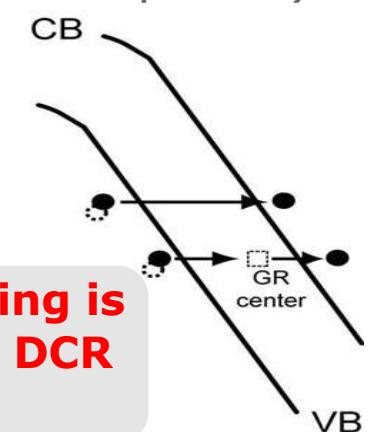
1) Generation/Recombination
SRH noise (enhanced by
trap assisted tunneling)



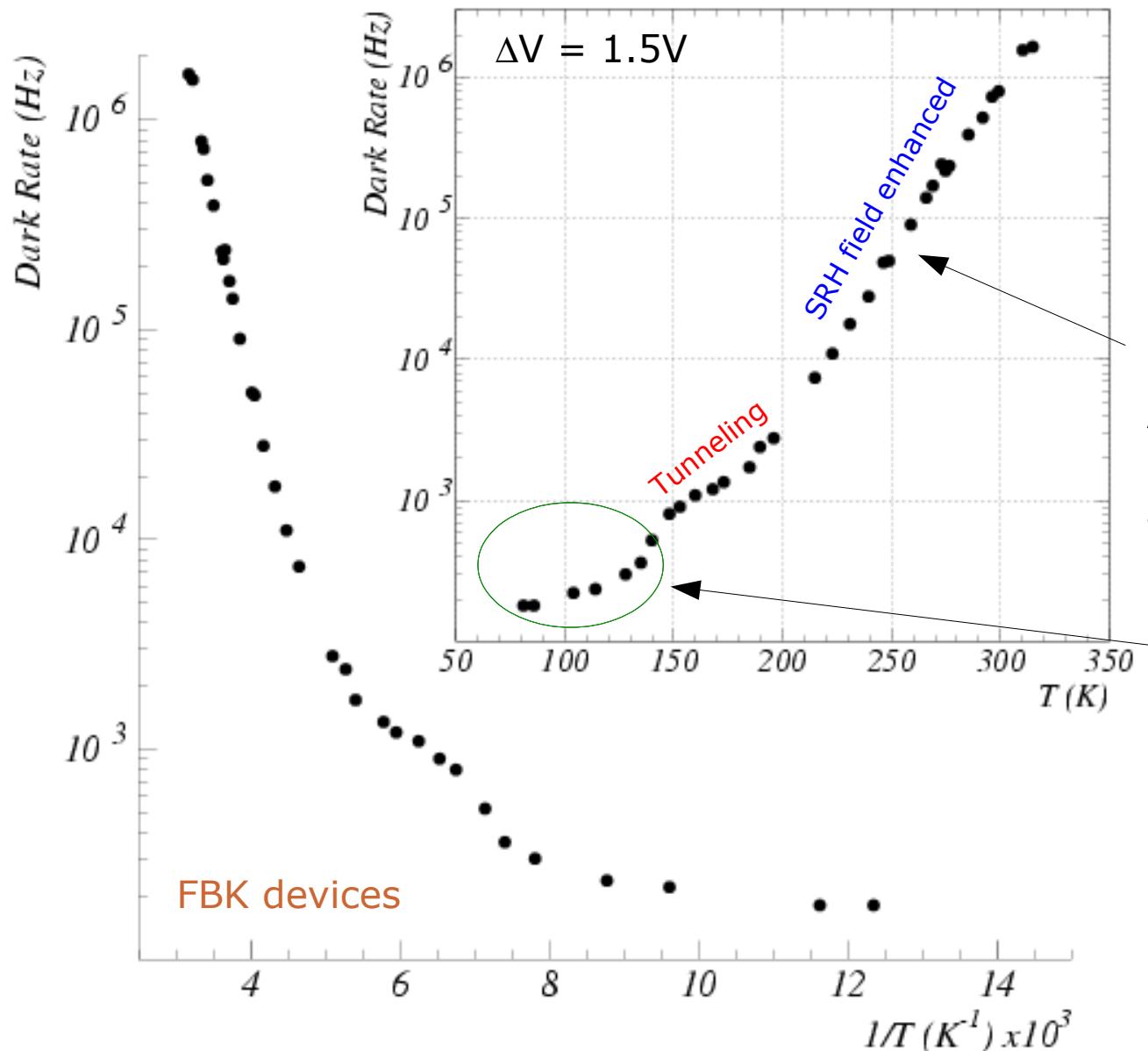
2) Band-to-band Tunneling
noise (strong dependence on
the Electric field profile)

negative T
coefficient

Efield engineering is
crucial for min. DCR
(esp. at low T)



Dark Count Rate vs T (constant ΔV)



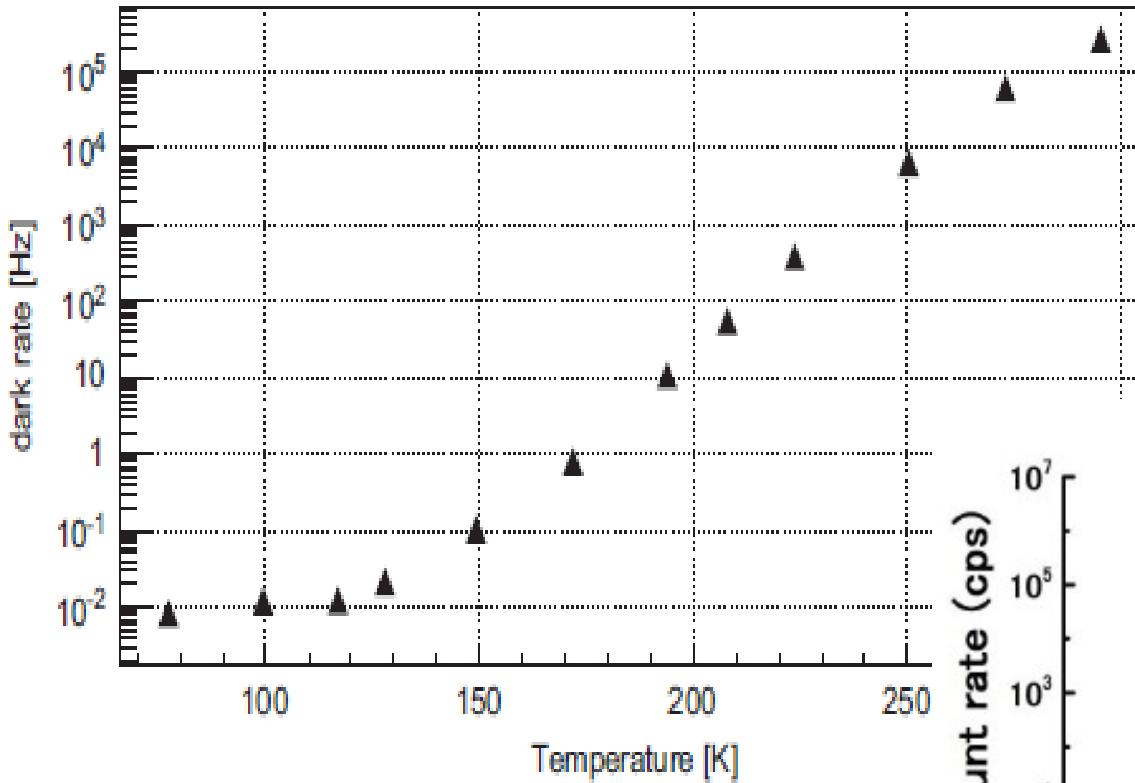
Measurement of
counting rate of ≥ 1 p.e.
at fixed $\Delta V=1.5V$
(\rightarrow constant gain)

$$DCR \sim T^{1.5} \exp \frac{-E_{act}}{2K_B T}$$

Activation energy $E_{act} \sim 0.72\text{eV}$
Note: E_{act} should be $\sim E_g$ but
tunneling makes effective gap
smaller

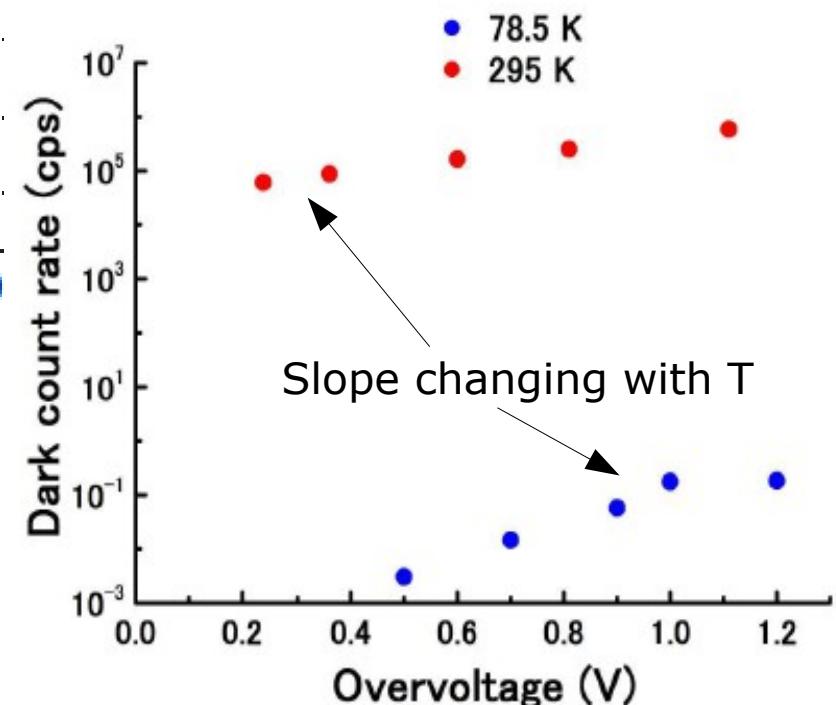
Additional structure
carriers **freeze-out** (?)
(carrier **collection losses** at
very low T due to ionized
impurities acting as shallow
traps \rightarrow drop in PDE)

Dark Count Rate vs T



J.Csathy et al NIM A 654 (2011) 225

Hamamatsu
(100 μ m pixels)



Slope changing with T

Comprehensive MPPC
characterization at low T

→ Akiba et al Optics Express 17 (2009) 16885

After-Pulsing Carrier trapping and delayed release

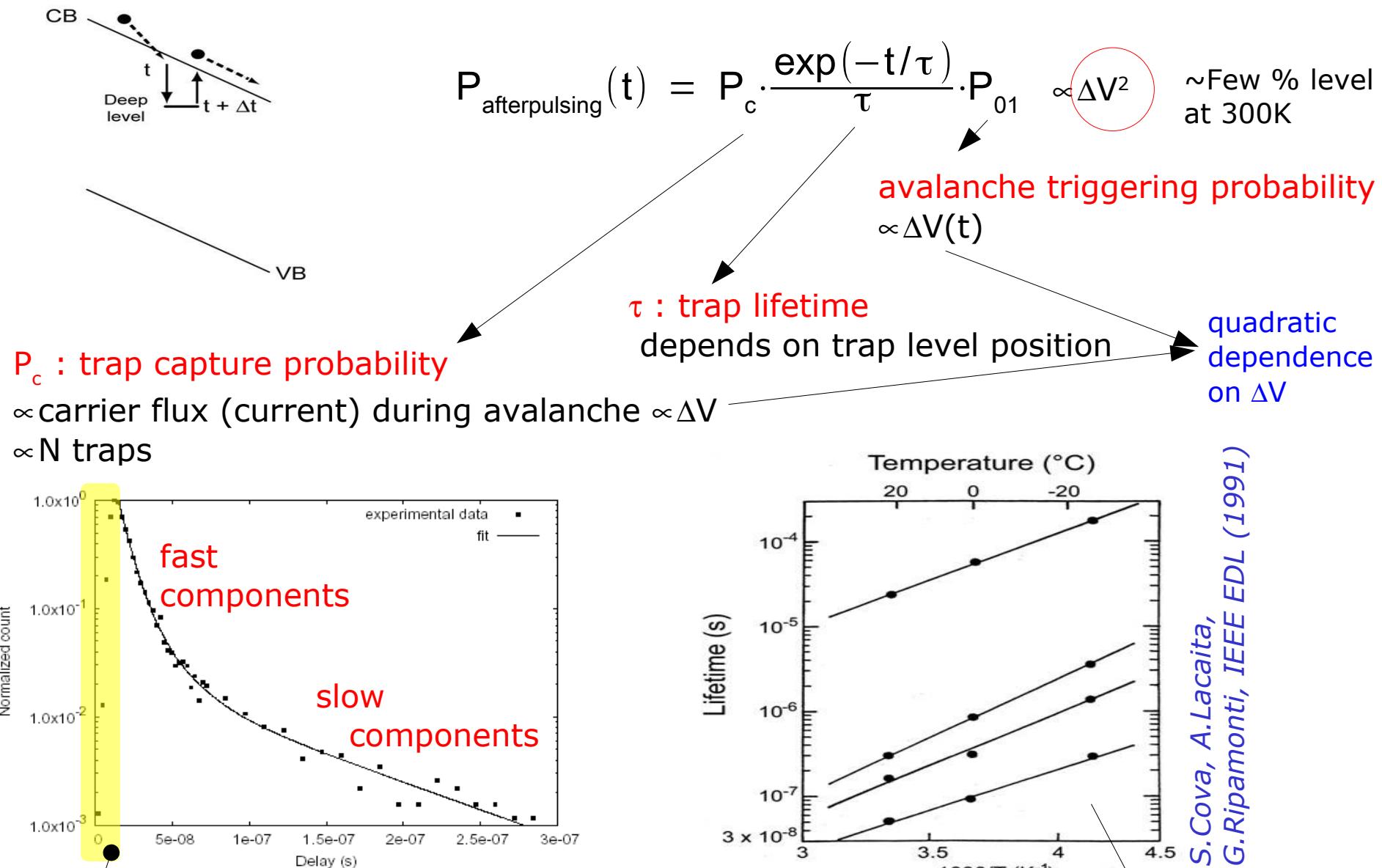


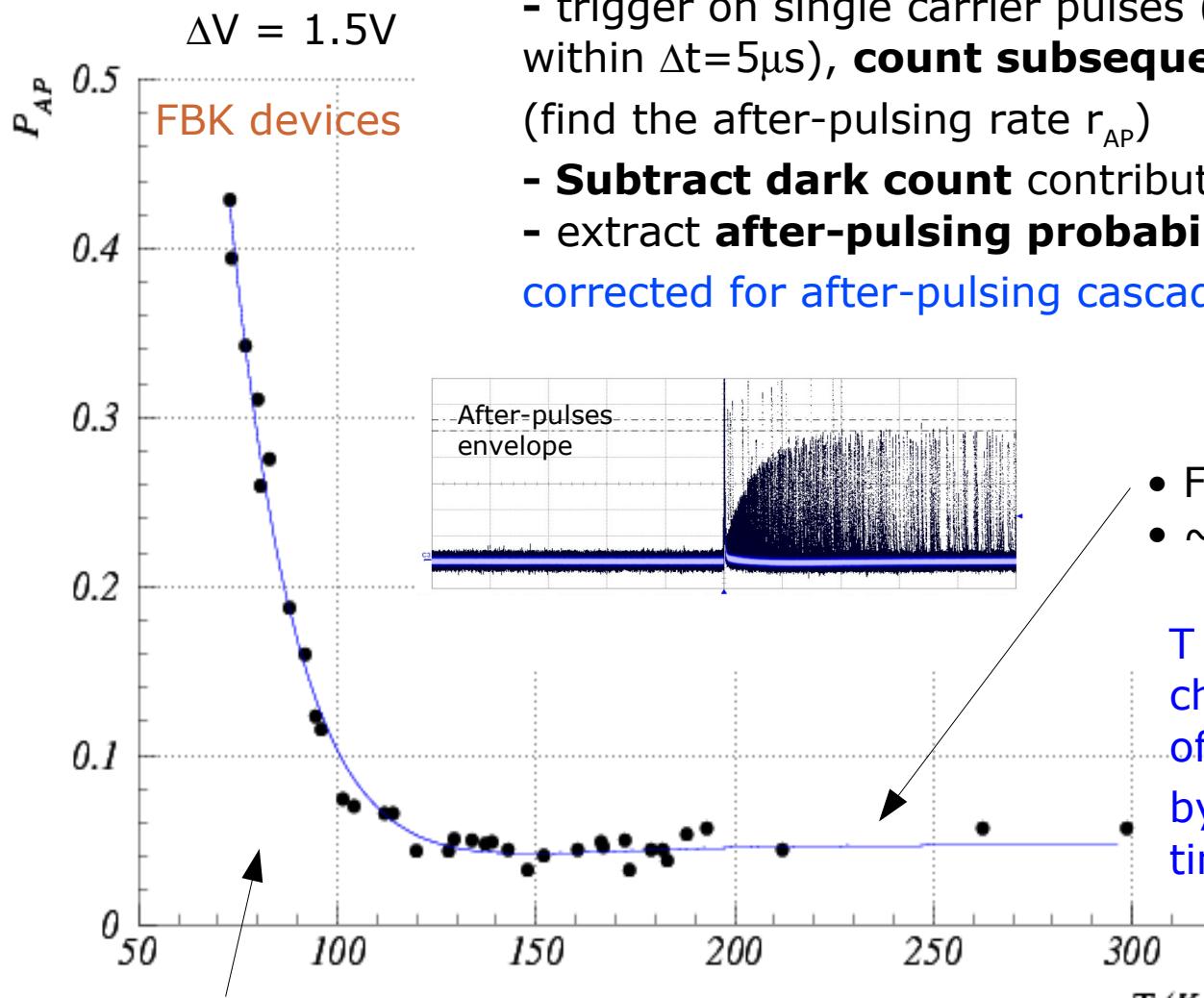
Fig. 10. Spectrum of the delay time from the primary pulse to the after-pulse.

Only partially sensitive to after-pulsing during recovery
ie recovery hides After-pulses (does not cancel them)

not trivial
dependence on T

S.Cova, A.Lacaita,
G.Ripamonti, IEEE EDL (1991)

After-Pulses vs T (constant ΔV)



Measurement by waveform analysis:

- trigger on single carrier pulses (with no preceding pulses within $\Delta t=5\mu s$), **count subsequent pulses** within $\Delta t=5\mu s$ (find the after-pulsing rate r_{AP})
- **Subtract dark count** contribution
- extract **after-pulsing probability P_{AP}** corrected for after-pulsing cascade

$$P_{AP} = \frac{r_{AP}}{1 + r_{AP}}$$

- Few % at room T
- ~constant down to $\sim 120K$

T decreasing: increase of characteristic time constants of traps (τ_{traps}) compensated by increasing cell recovery time (R_q)

- several % below 100K

$T < 100K$: additional trapping centers activated possibly (?) related to onset of carriers freeze-out

→ Analysis of life-time evolution vs T of the various traps (at least 3 types at T_{room})

Optical cross-talk Avalanche luminescence (NIR)

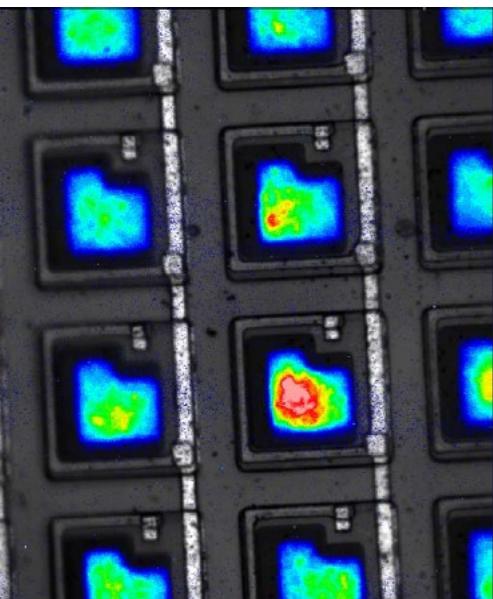
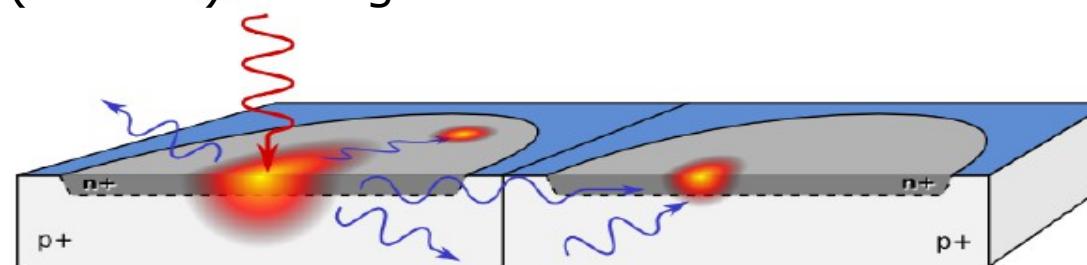
Carriers' luminescence (spontaneous direct relaxation in the conduction band) during the avalanche: probability $3 \cdot 10^{-5}$ per carrier to emit photons with $E > 1.14$ eV

A.Lacaita et al. IEEE TED (1993)

Photons can induce avalanches in neighboring cells.
Depends on distance between high-field regions

ΔV^2 dependence on over-voltage:

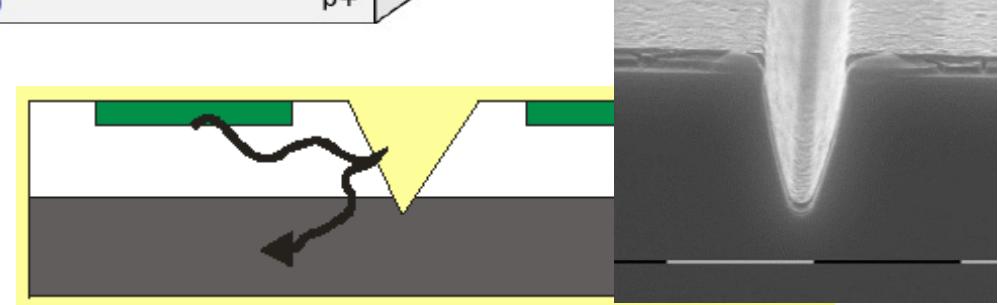
- carrier flux (current) during avalanche $\propto \Delta V$
- gain $\propto \Delta V$



N.Otte, SNIC 2006

Counteract:

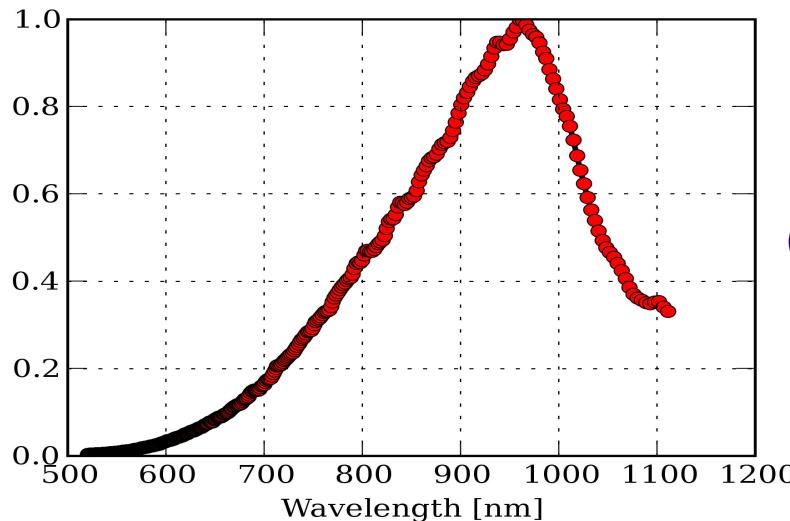
- **optical isolation** between cells by trenches filled with opaque material
- low over-voltage operation helps



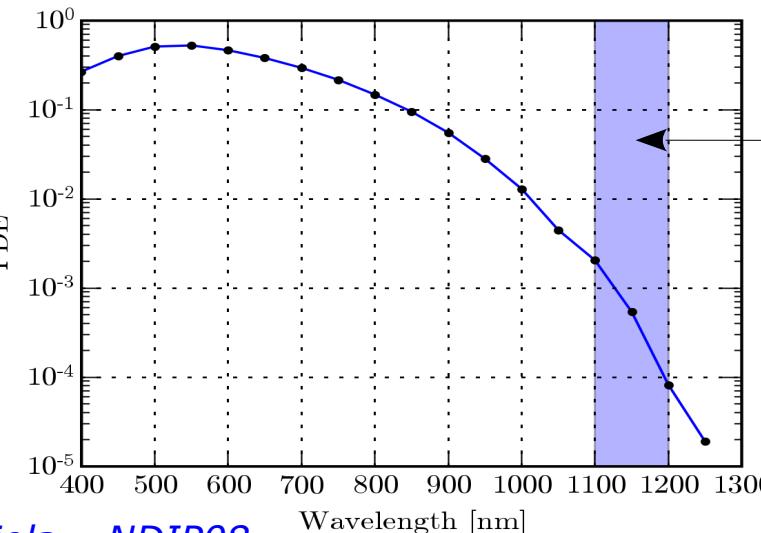
It can be reduced to a level below % in a wide ΔV range

Optical cross-talk: reflections from the bottom

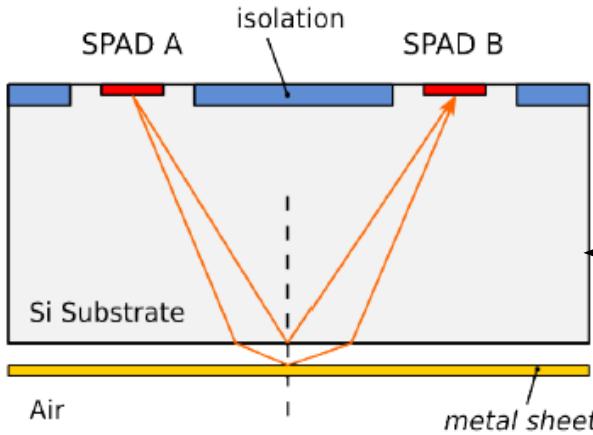
Measured Emission spectrum



PDE



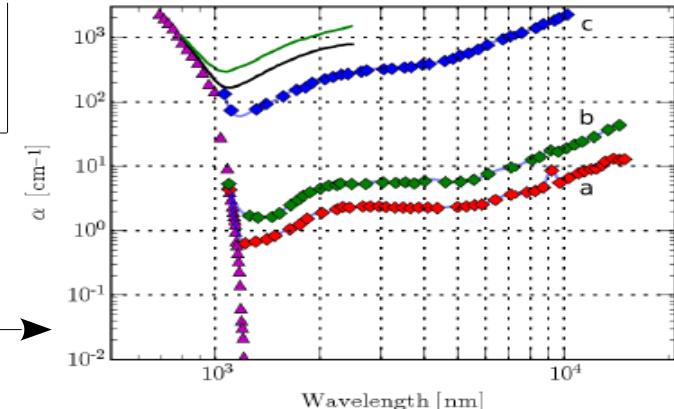
A. Ingargiola - NDIP08
Rech et al Proc. of SPIE Vol. 6771 677111-1



(2) Main component due to total reflection internal from the bottom (substrate)

(3) Isolation implants are sufficient to stop direct component

Silicon absorption coefficients:



- Crosstalk can't be eliminated simply by means of trenches
- Main contribution to crosstalk comes from bottom reflections (using trenches)

DCR, AP, Gain, X-talk vs ΔV (various T)

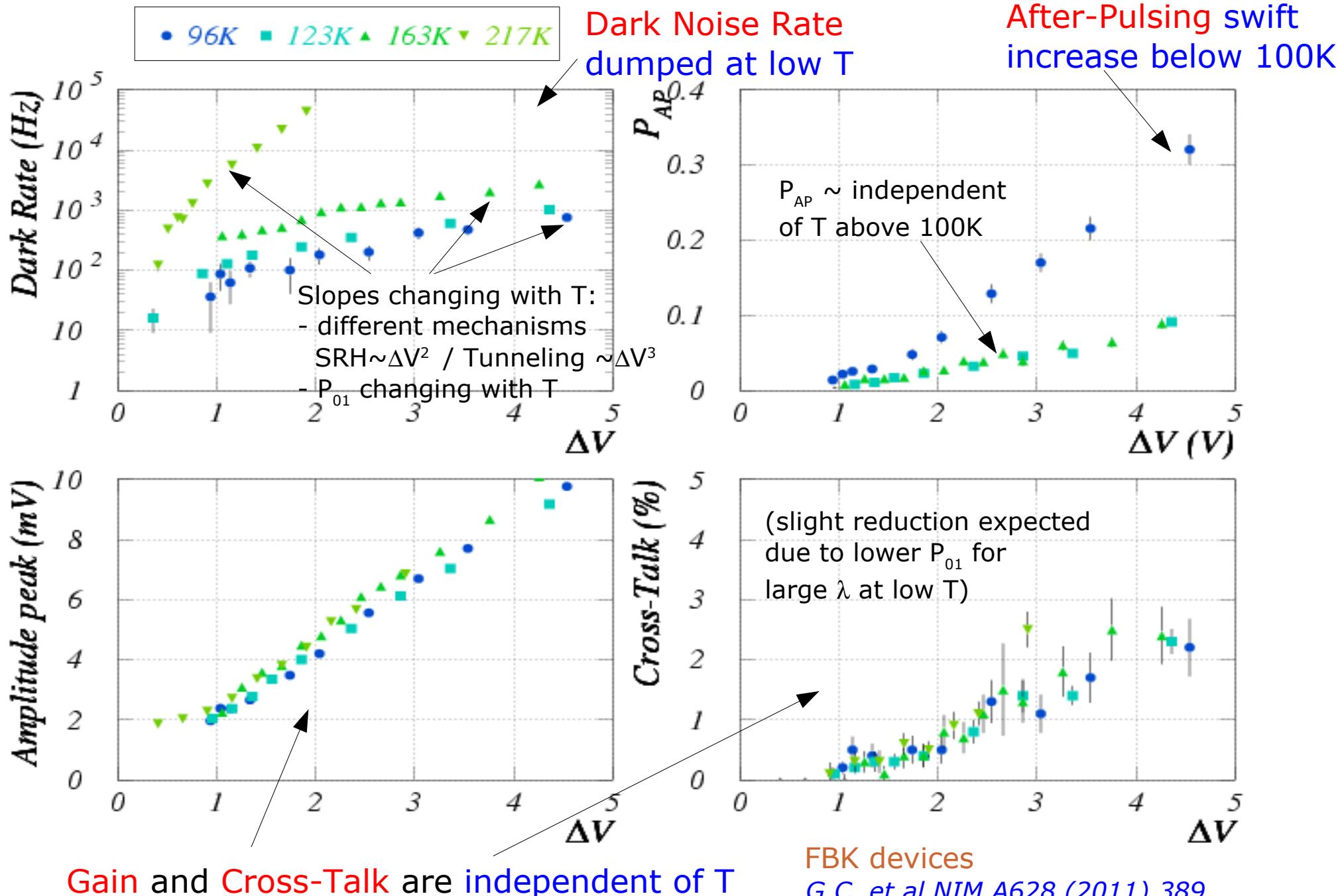




Photo-Detection Efficiency (PDE)

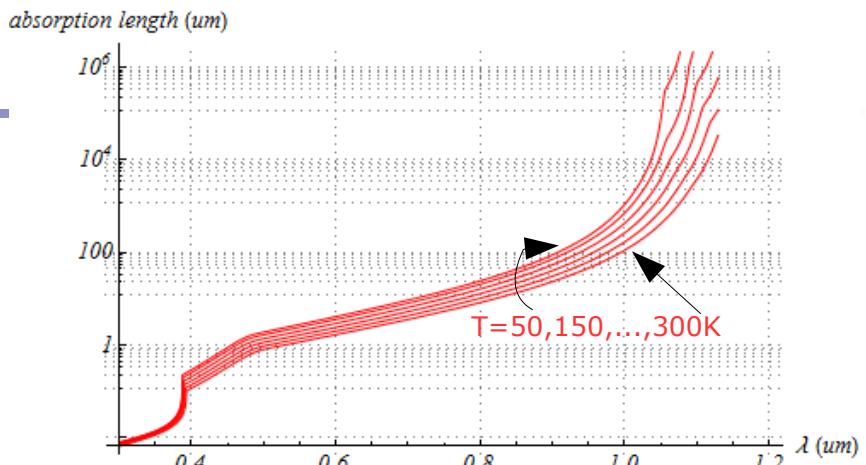
PDE = QE · P₀₁ · FF

QE: carrier Photo-generation

probability for a photon to generate a carrier that reaches the high field region

→ λ and T dependent

→ ΔV independent if full depletion at V_{bd}

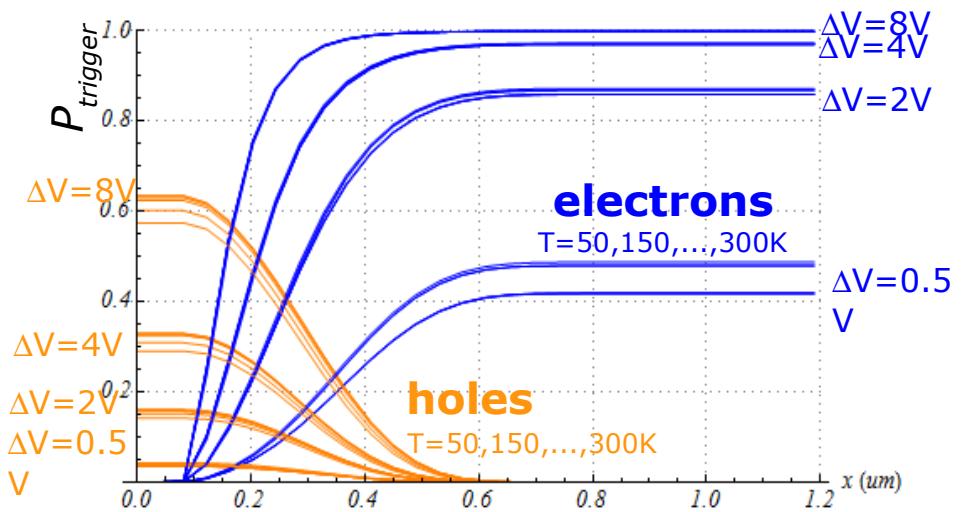


Rajkanan et al, Solid State Ele 22 (1979) 793

P₀₁ : avalanche triggering probability

probability for a carrier traversing the high-field to generate the avalanche

→ λ, T and ΔV dependent

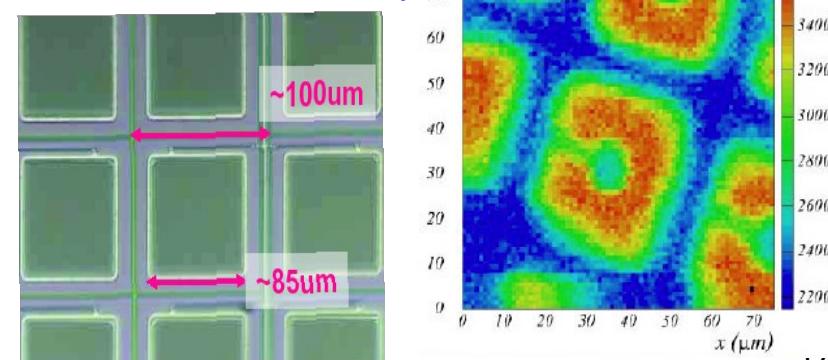


FF: geometrical Fill Factor

fraction of dead area due to structures between the cells, eg. guard rings, trenches

→ mild ΔV dependence (cell edges)

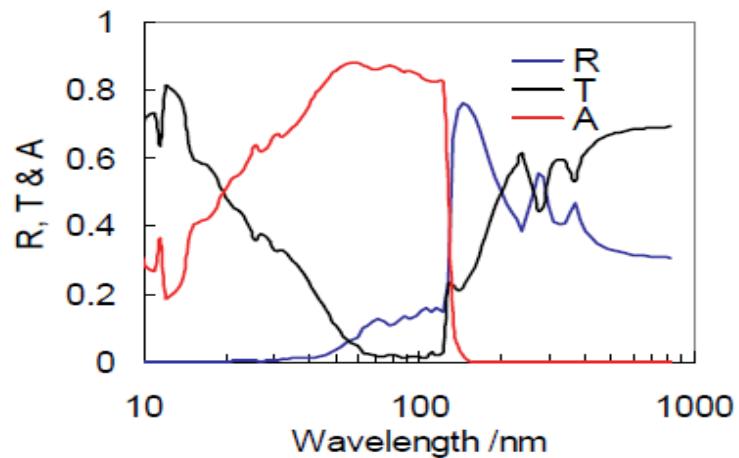
Hamamatsu MPPCs close up



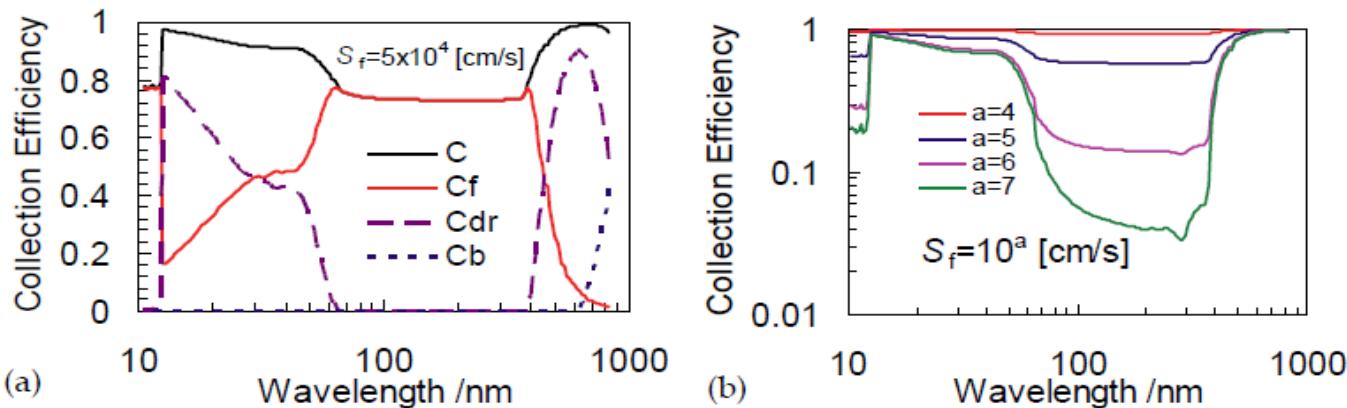
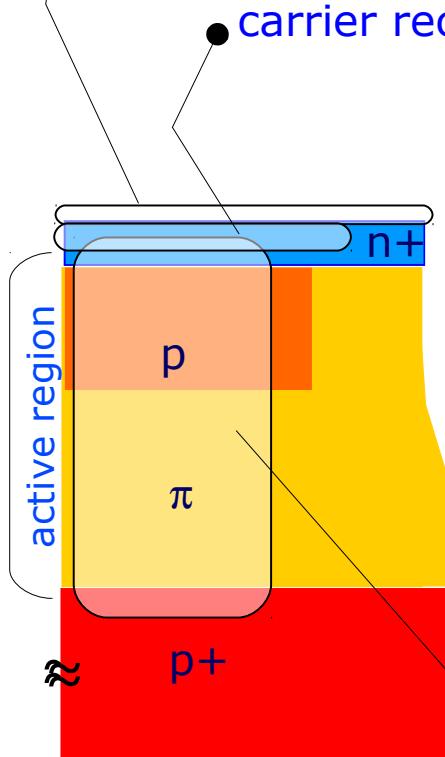
QE

calculation
for 30nm SiO_2
on Si layer

- optical T,A,(R) of the entrance window
(dielectric on top of silicon surface)
→ angular and polarization dependence



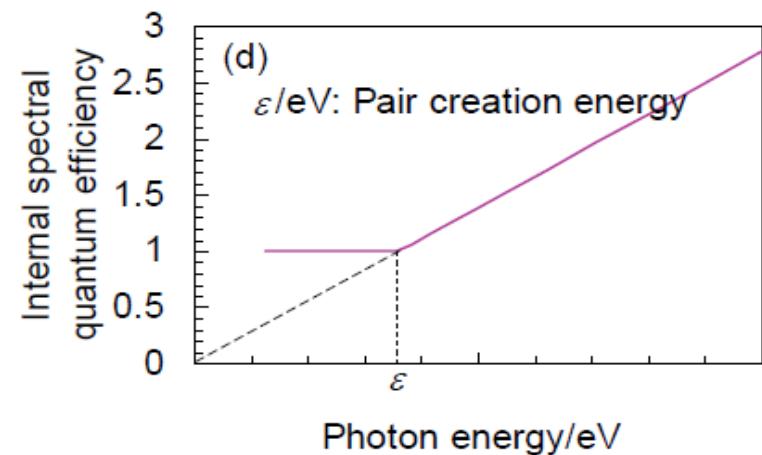
carrier recombination loss: collection efficiency front, depl. region, back



- front region critical for $60\text{nm} < \lambda < 400\text{nm}$
- C eff. depends on surface recombination velocity S_f
- freeze-out at low T

eg of QE optimization (blue)

- Anti-reflective coating (ARC)
- Shallow junctions for short λ
- Thick epi layers for long λ

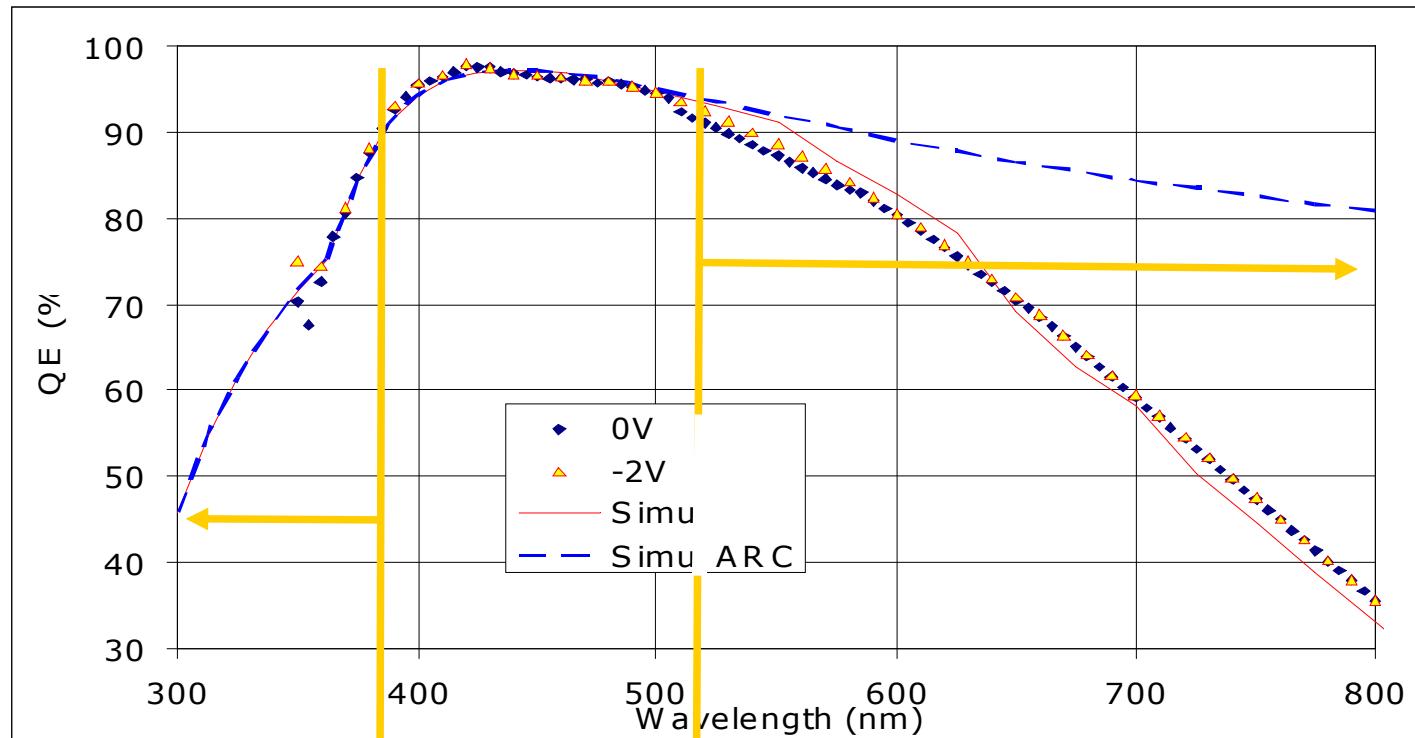


Photon energy/eV

QE single cell

FBK single cell

photo-voltaic regime ($V_{bias} \sim 0$ V)

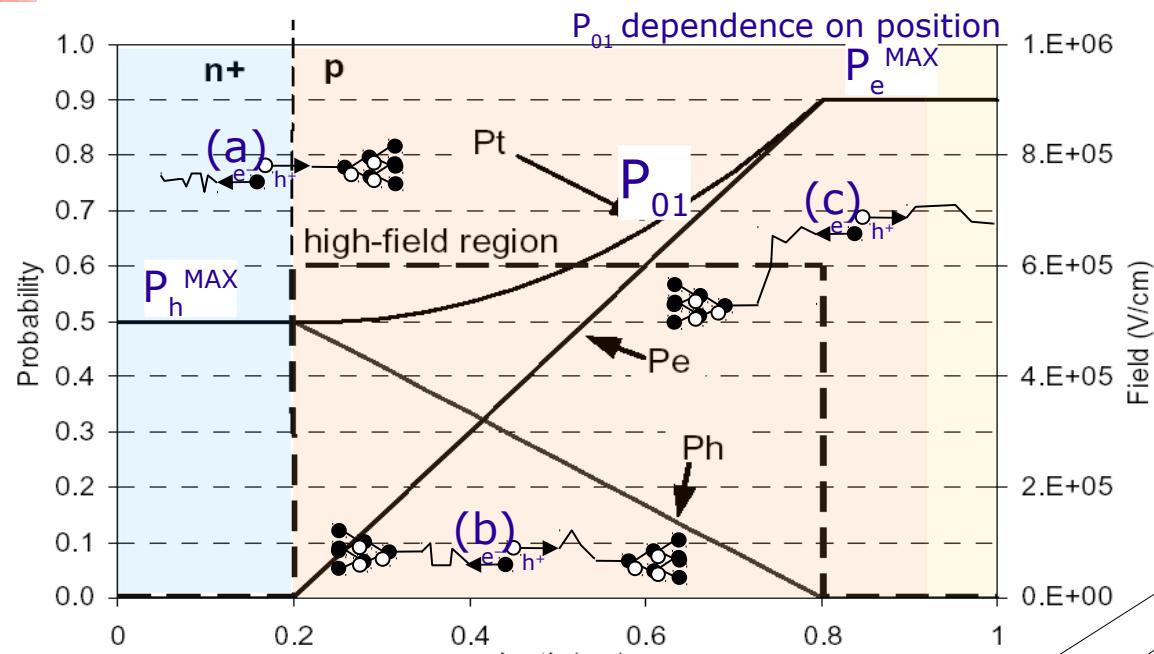


limited by
ARC Transmittance
&
Superficial
Recombination

limited by the
small π layer thickness

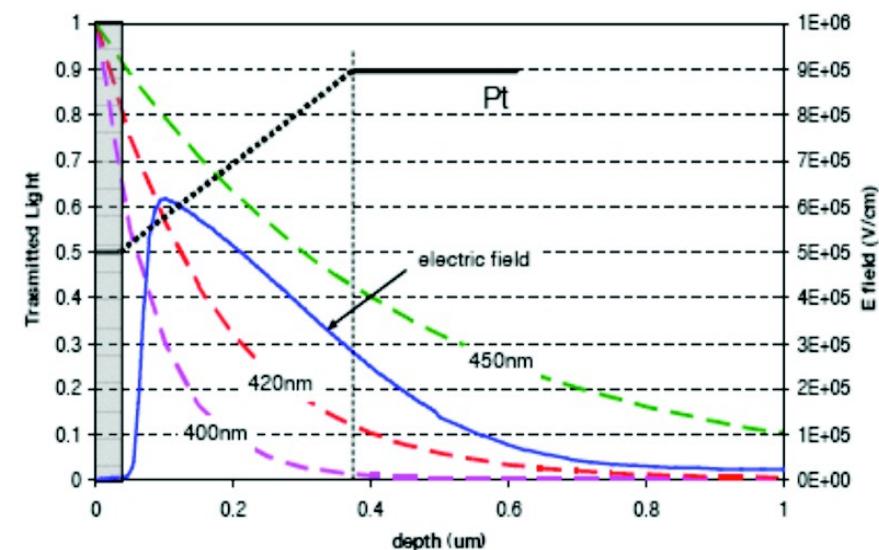
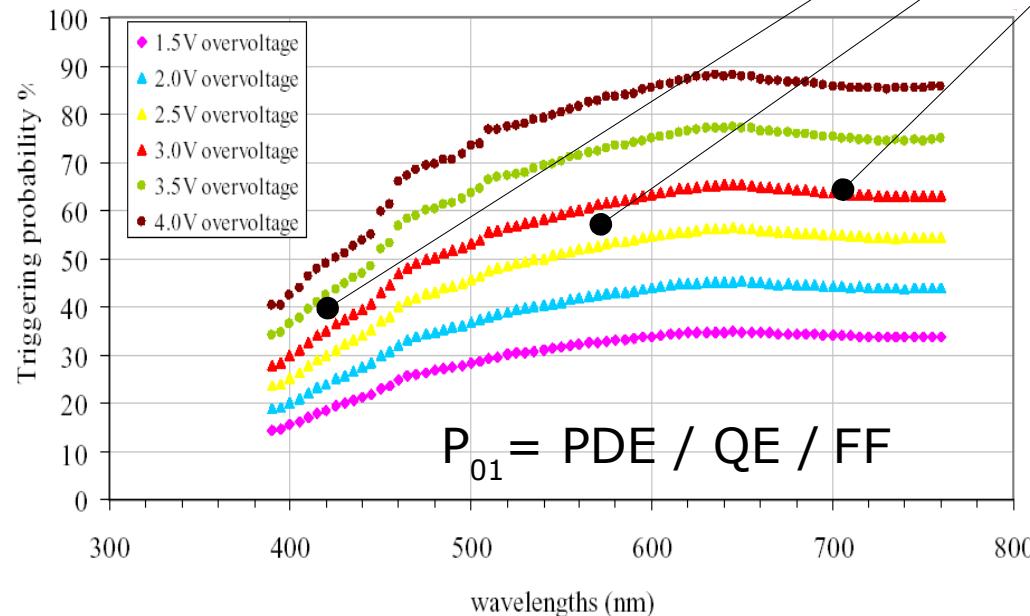
Most critical issue for **Deep UV SiPM**
note: reduced superficial recombination
in n-on-p wrt p-on-n

Avalanche trigger probability (P_{01})



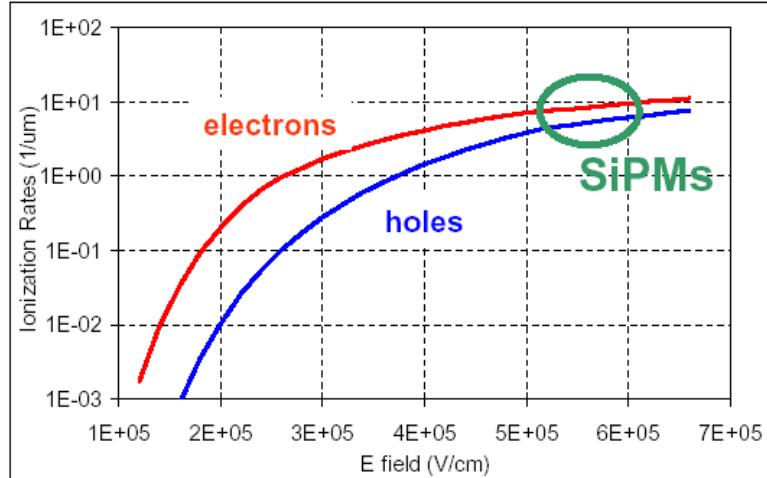
Probability calculations
after [W. Oldham et al.
IEEE TED \(1972\)](#)

Example with constant high-field:
(a) only holes trigger the avalanche
(b) both electrons and holes trigger
(c) only electrons trigger



PDE vs ΔV

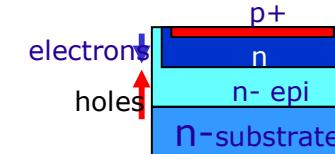
Ionization rate in Silicon



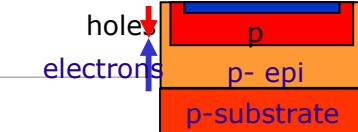
P_{01} optimization
(n-on-p)

- high over-voltage
- photo-generation in the p-side of the junction

p-on-n structure

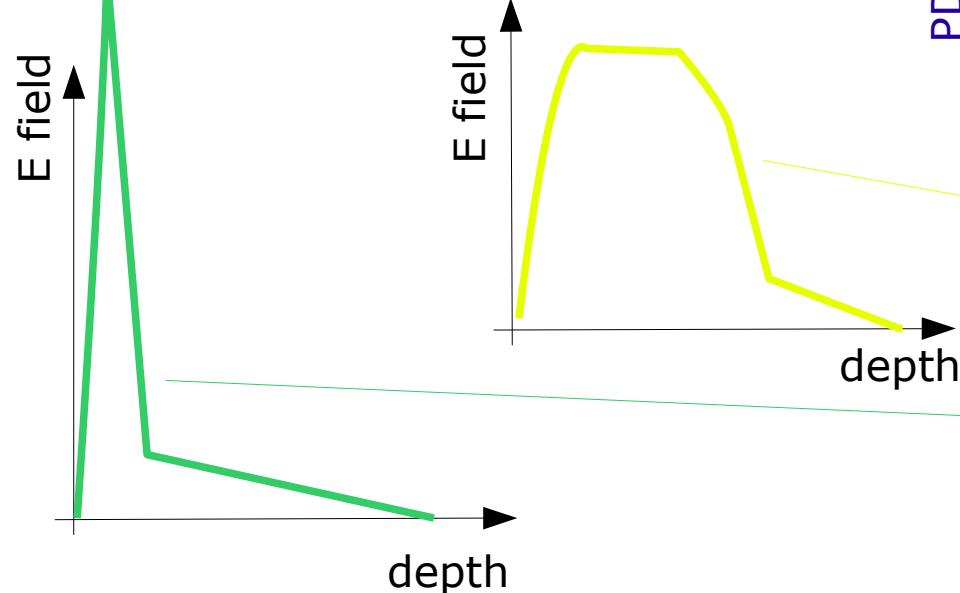
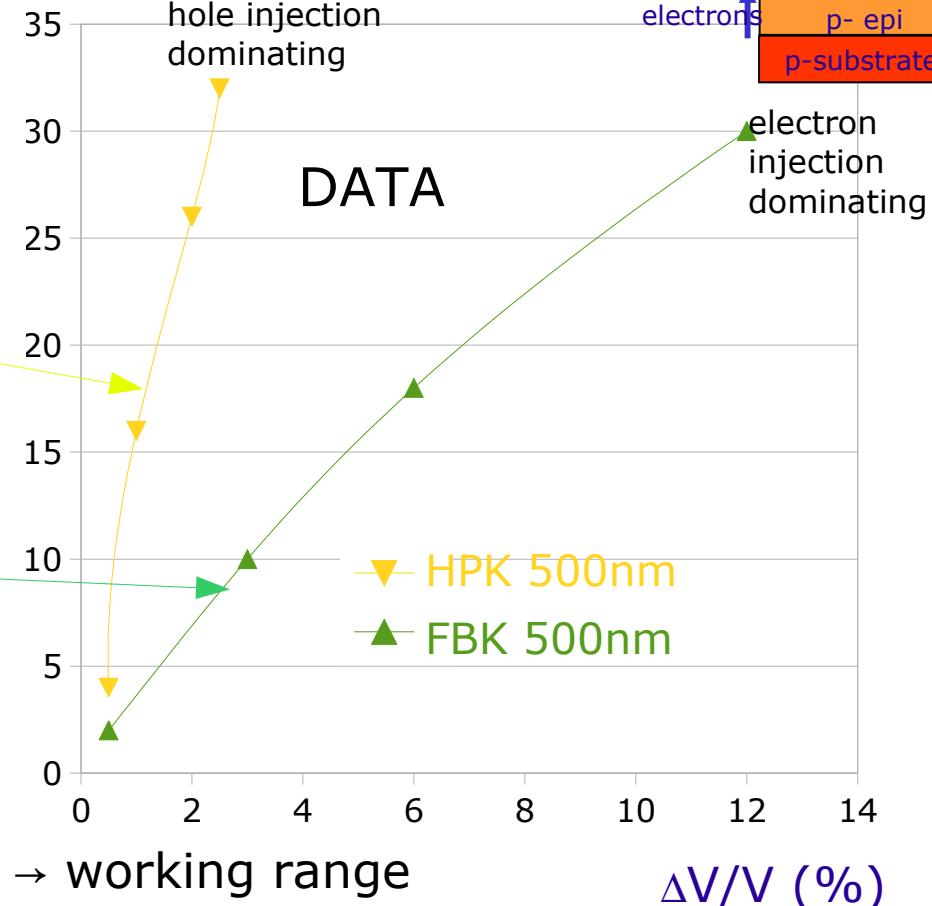


n-on-p structure



hole injection dominating

DATA



E field profile → the slope of PDE vs ΔV

note: P_{01} fixes also the slope of DCR vs ΔV → working range

PDE VS λ (shape)

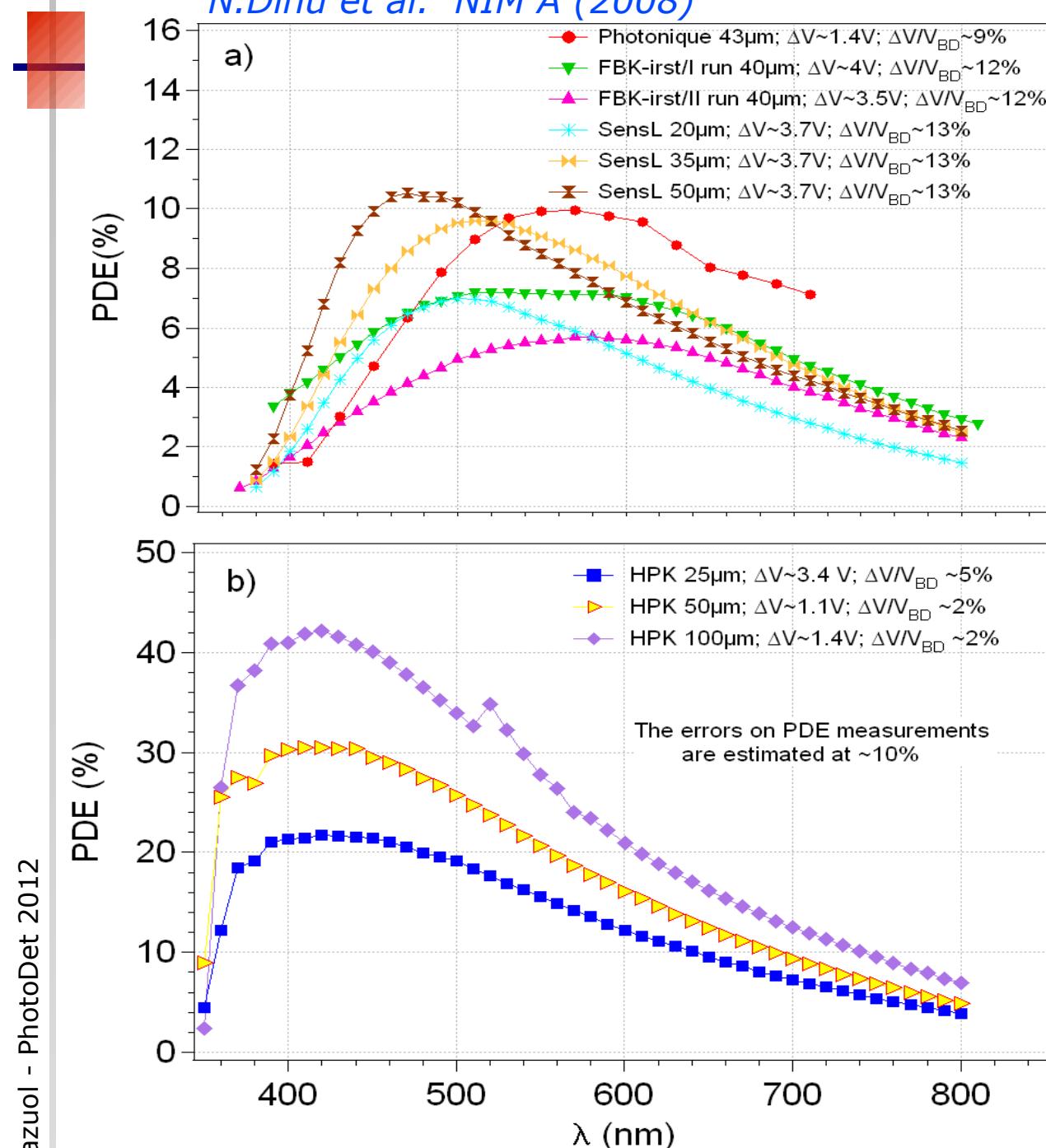
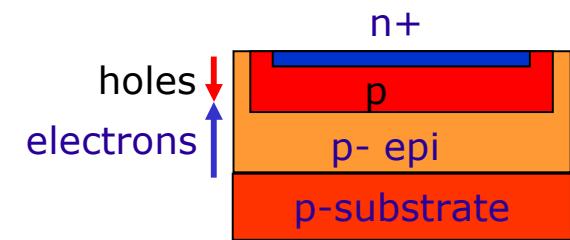
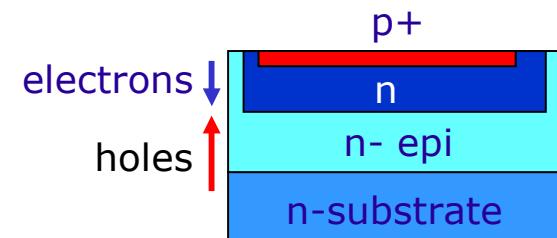


Fig. 5a) The PDE vs. λ of the Photonique, FBK-irst and Sensl devices and b) HPK

n-on-p structures



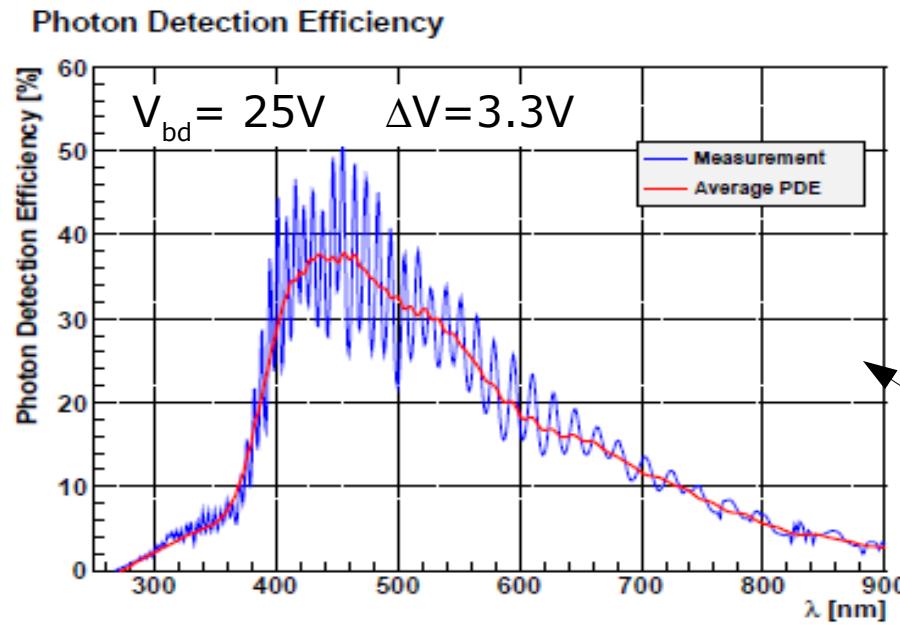
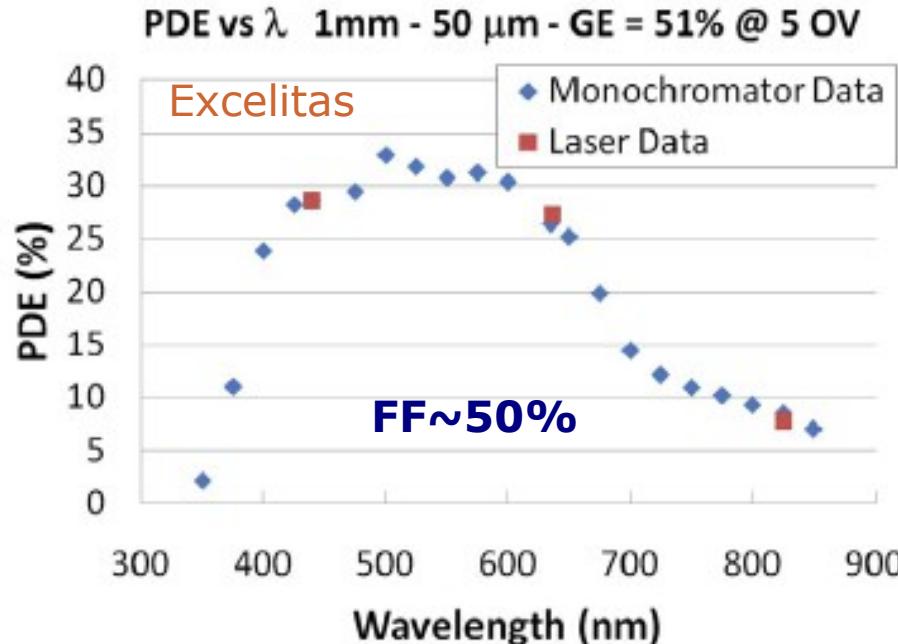
p-on-n structure



Note: geometrical fill factor included

Improving PDE

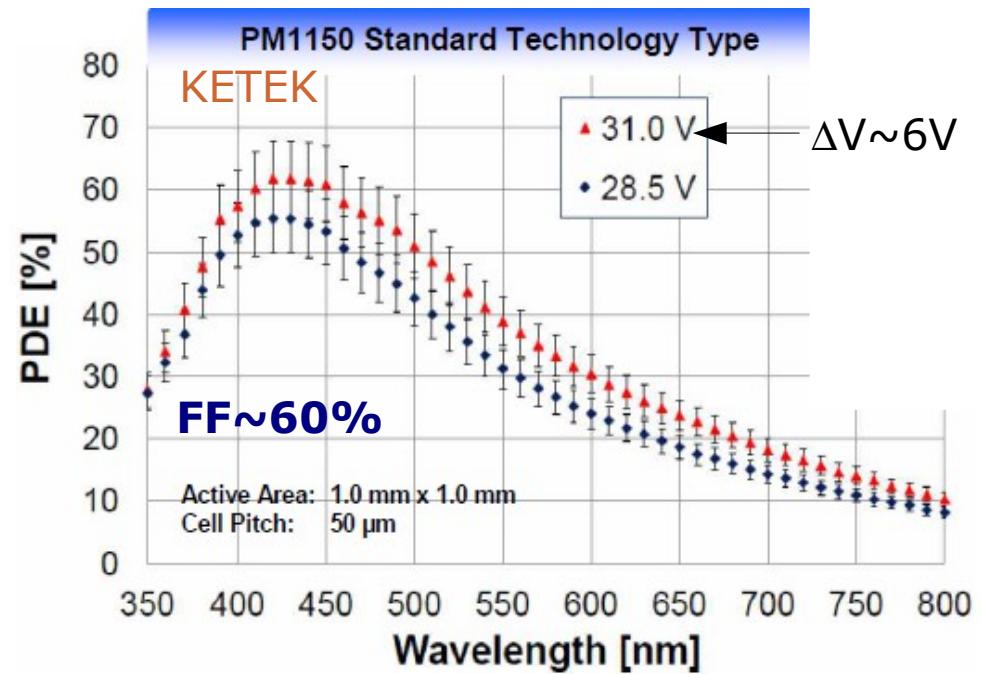
Barlow - LIGHT 2011



T.Frach 2012 JINST 7 C01112

- PDE peak constantly improving for many devices
- every manufacturer shape PDE for matching target applications
- UV SiPM eg from MePhi/Excelitas (see *E.Popova at NDIP 2011*)
- DUV SiPMs in development too

F.Wiest - AIDA 2012 at DESY

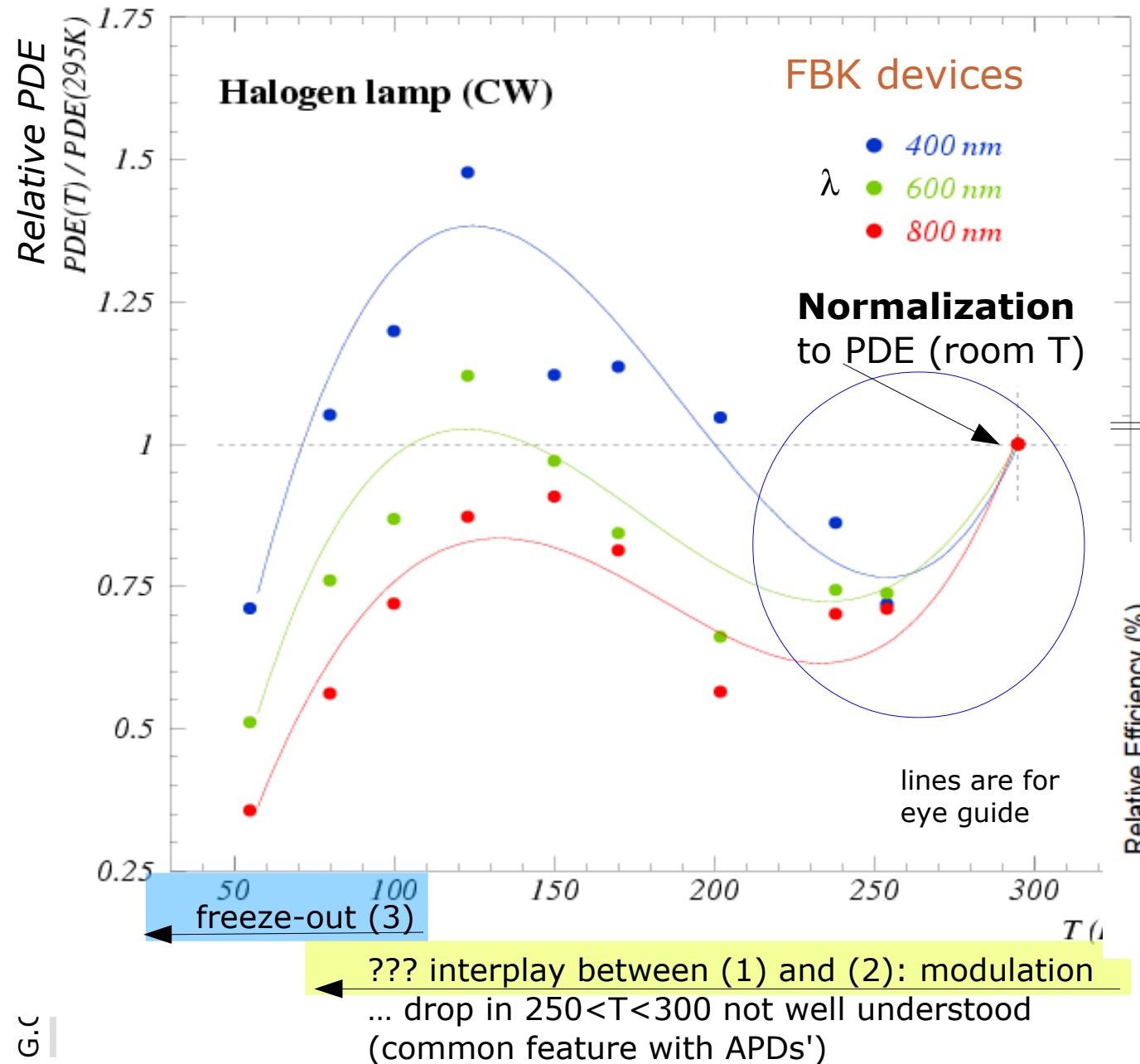


dSiPM (latest sensor 2011)

- up to now no optical stack optimization
- no anti-reflecting coating
- potential improvement up to 60% peak PDE (*Y.Haemish at AIDA 2012*)

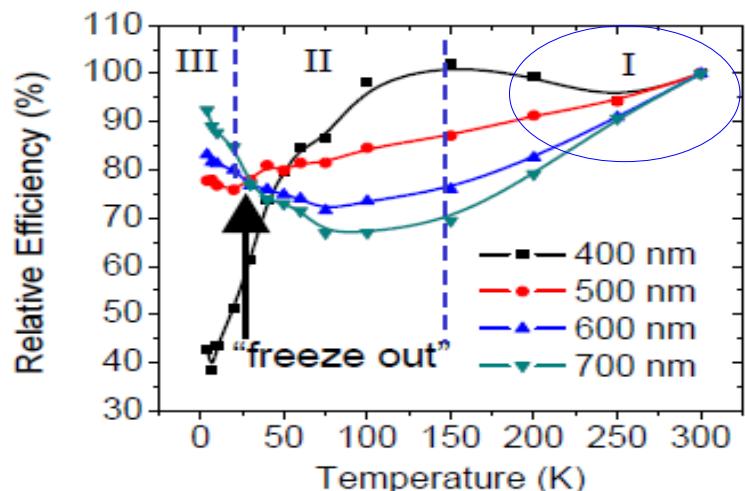
PDE vs T (ΔV constant)

G.C. et al NIM A628 (2011) 389



- When T decreases:
- 1) silicon E_{gap} increasing
→ larger attenuation length
→ lower QE (for larger λ)
 - 2) mobility increasing
→ larger impact ionization
→ larger trigg. avalanche P_{01}
 - 3) carriers freeze-out
onset below 120K
→ loss of carriers

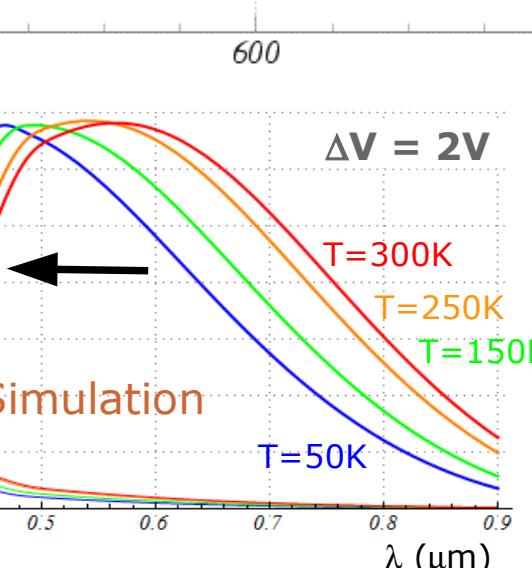
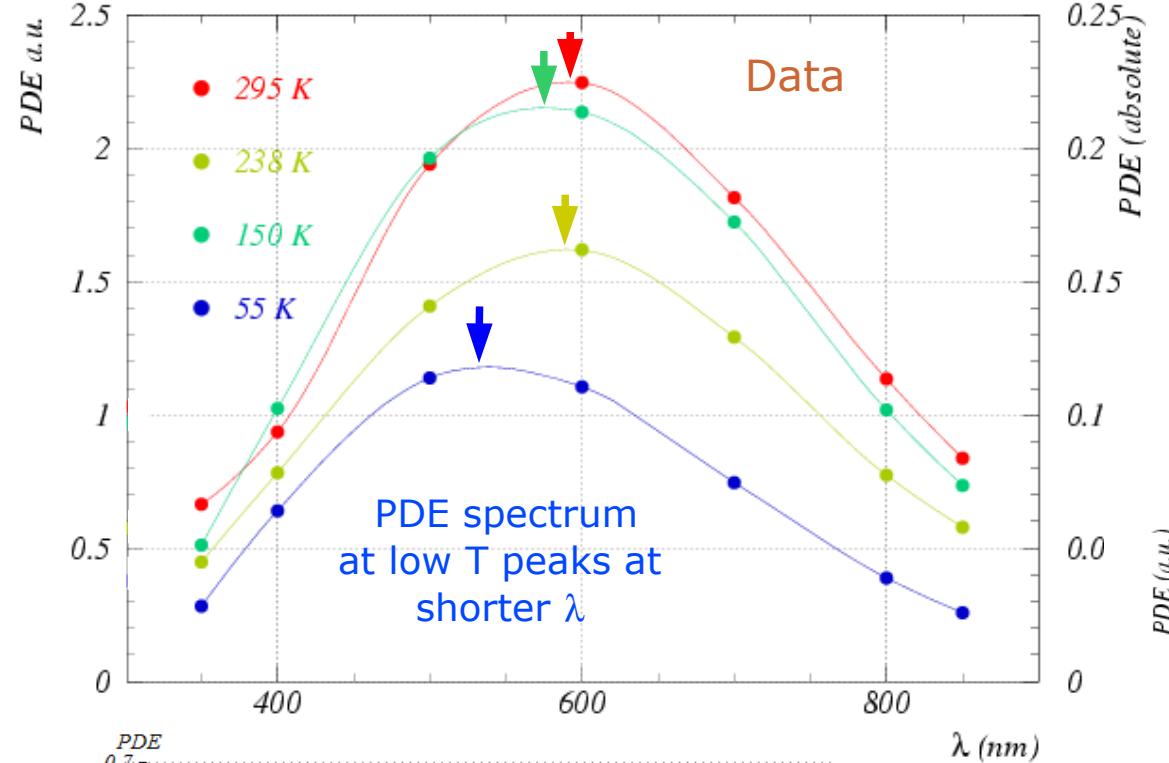
RMD APD at $400\text{nm} < \lambda < 700\text{nm}$
Johnson et al, IEEE NSS 2009



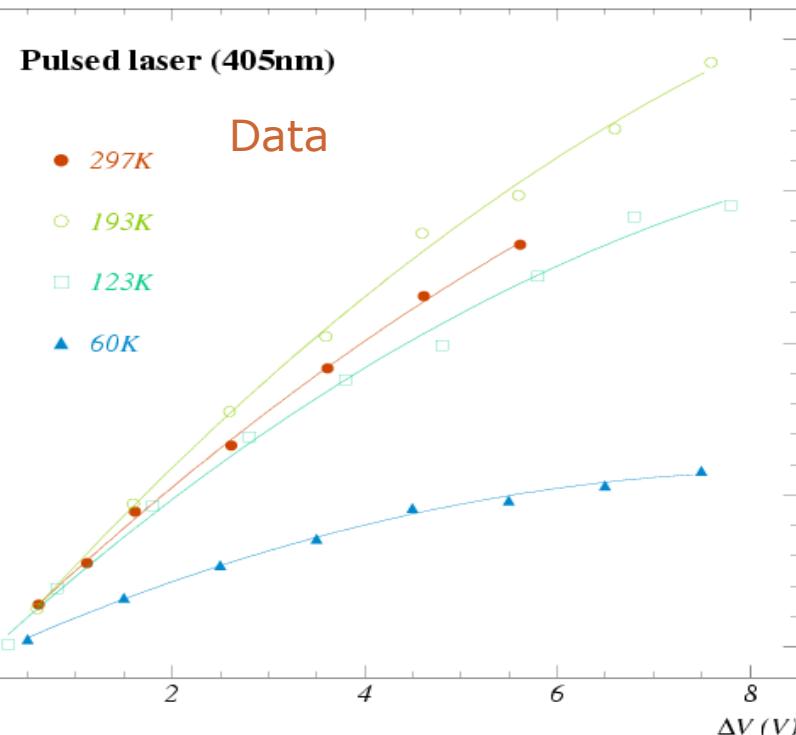
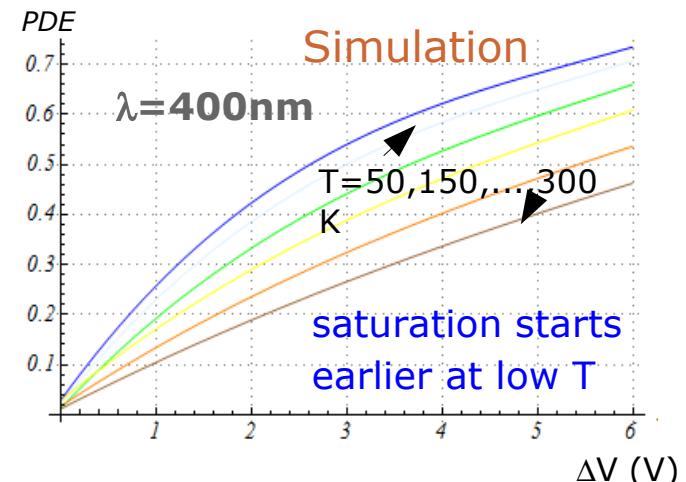
Additional effects in APD
(depletion region depends on T, ...)

PDE dependences, changing with T

PDE vs λ (ΔV constant)



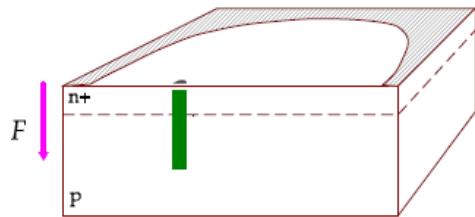
PDE ΔV vs (λ constant)



Timing

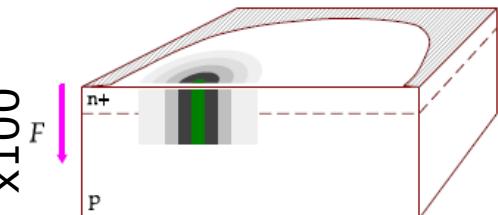
- SiPM are **intrinsically very fast**
 - jitter (gaussian) below **100ps**, depending on ΔV
 - but also → non-gaussian tails up to **O(ns)**, depending on wavelength
- **Timing measurement:**
 - use of fast signal shape component
 - use waveform, better than CFD (much than ToT)

GM-APD avalanche development



Longitudinal multiplication

Duration ~ few **ps**
Internal current up to ~ few **μ A**



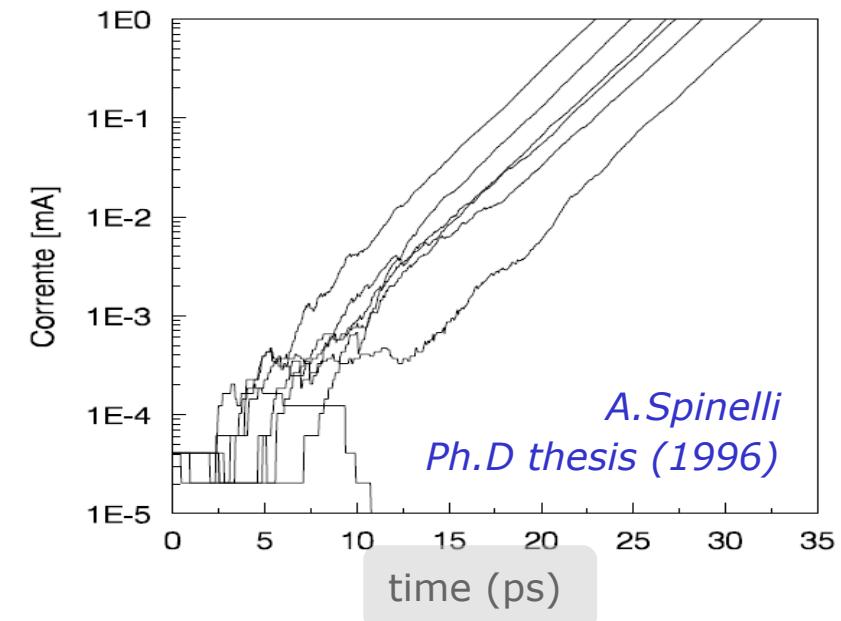
Transverse multiplication

Duration ~ few **100ps**
Internal current up to ~ several **10μ A**

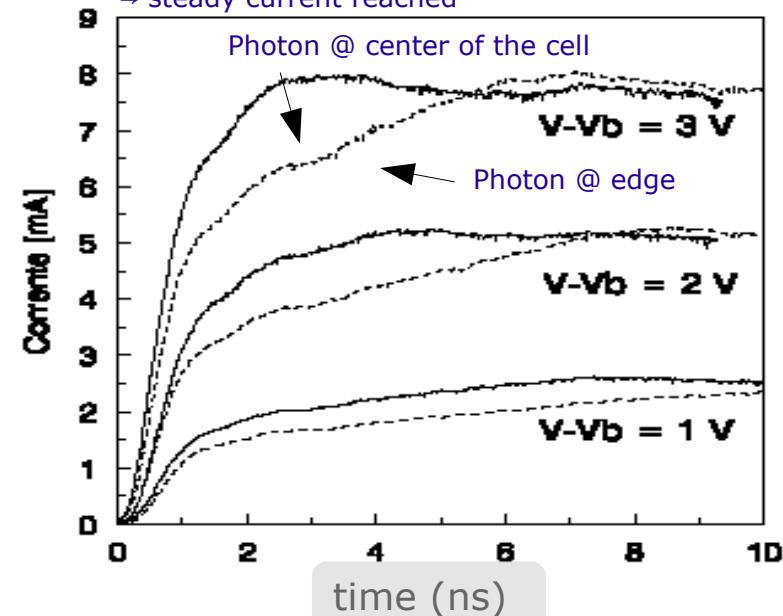
(1) Avalanche "seed": free-carrier concentration rises exponentially by "**longitudinal**" **multiplication**

(1') Electric field locally lowered (by **space charge R effect**) towards breakdown level

Multiplication is self-sustaining
Avalanche current steady until new multiplication triggered in near regions



Simulation w/o quenching:
→ steady current reached



(2) **Avalanche spreads**
"**transversally**" across the junction

(diffusion speed ~up to 50μ m/ns
enhanced by multiplication)

(2') **Passive quenching mechanism**
effective after transverse
avalanche size ~ 10μ m

(if no quench, avalanche spreads over the whole active depletion volume
→ avalanche current reaches a final saturation steady state value)

GM-APD avalanche transverse propagation

Avalanche transverse propagation by a kind of **shock wave**: the **wavefront** carries a **high density of carriers** and high E field gradients (inside: carriers' density lower and E field decreasing toward breakdown level)

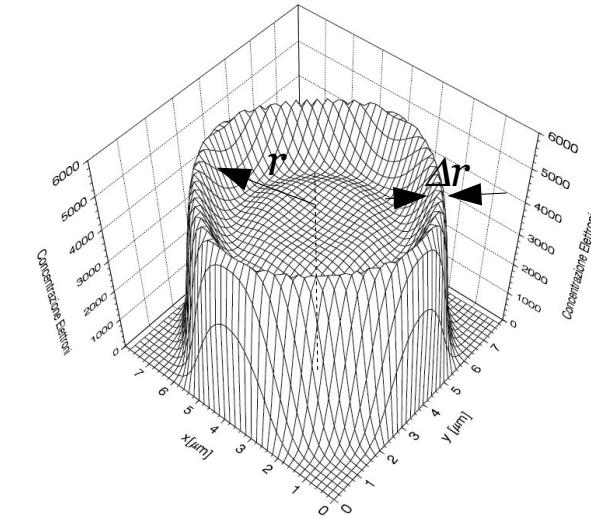
$$\frac{dS}{dt} = \frac{d}{dt} 2\pi r(t) \Delta r = 2\pi v_{diff} \Delta r = 4\pi \Delta r \sqrt{\frac{D}{\tau}}$$

Rate of current production: $\frac{dI}{dt} = \frac{dI}{dS} \frac{dS}{dt} \sim \frac{\sqrt{D}}{R_{sp} \sqrt{\tau}}$

$$\frac{dI}{dS} = J = \frac{V_{bias}}{R_{sp}(S)}$$

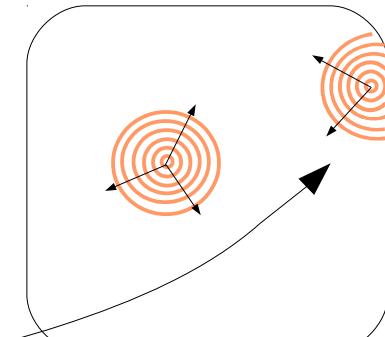
Internal **current rising front**:
the **faster it grows, the lower the jitter**
 $dI/dt \rightarrow$ understand/engineer timing features of SiPM cells

- timing resolution improves at **high V_{bias}**
- **E field profile affects τ and R_{sp}** (wider E field profile → smaller R)
(should be engineered when aiming at ultra-fast timing)
- **T dependence of timing** through τ and D
- slower growth at GAPD cell edges → **higher jitter at edges**
reduced length of the propagation front



S = surface of wavefront (ring of area $2\pi r \Delta r$)
 $R_{sp}(S)$ = space charge resistance $\sim w^2/2\varepsilon v \sim O(50 k\Omega \mu m^2)$
 $v_{diff} \sim O(\text{some } 10 \mu m/\text{ns})$
 D = transverse diffusion coefficient $\sim O(\mu m^2/\text{ns})$
 τ = longitudinal (exponential) buildup time $\sim O(\text{few ps})$

$$\tau \sim \frac{1}{1 - (E_{max}/E_{breakdown})^n}$$

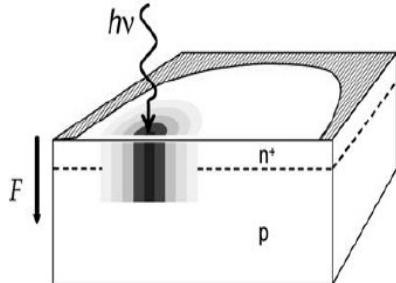


GM-APD timing jitter: fast and slow components

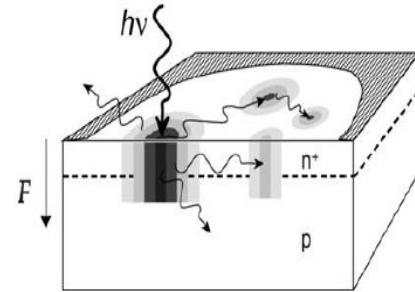
1) Fast component: gaussian with time scale $O(100\text{ps})$

Statistical fluctuations in the avalanche:

- **Longitudinal** build-up (minor contribution)
- **Transversal** propagation (main contribution):
 - via multiplication assisted diffusion (dominating in few μm thin devices)
A.Lacaita et al. APL and El.Lett. 1990
 - via photon assisted propagation (dominating in thick devices – $O(100\mu\text{m})$)
PP.Webb, R.J. McIntyre RCA Eng. 1982
A.Lacaita et al. APL 1992



Multiplication assisted diffusion



Photon assisted propagation

Fluctuations due to

- a) impact ionization statistics
- b) variance of longitudinal position of photo-generation: finite drift time even at saturated velocity
note: saturated $v_e \sim 3 v_h$
(n-on-p are faster in general)

→ Jitter at minimum → **$O(10\text{ps})$**
(very low threshold → not easy)

Fluctuations due to

- c) variance of the transverse diffusion speed v_{diff}

d) variance of transverse position of photo-generation: slope of current rising front depends on transverse position

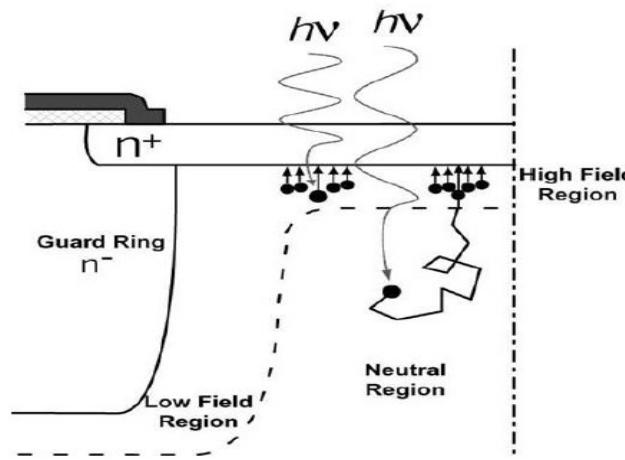
→ Jitter → **$O(100\text{ps})$**
(usually threshold set high)

GM-APD timing jitter: fast and slow components

2) Slow component: non-gaussian tails with time scale O(ns)

Carriers photo-generated in the neutral regions above/beneath the junction and reaching the electric field region by diffusion

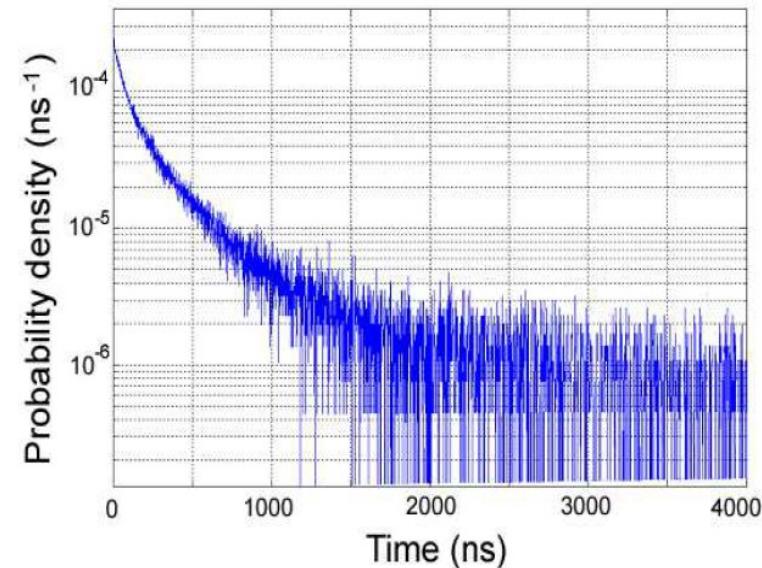
G.Ripamonti, S.Cova Sol.State Electronics (1985)



tail lifetime: $\tau \sim L^2 / \pi^2 D \sim$ up to some ns

L = effective neutral layer thickness

D = diffusion coefficient

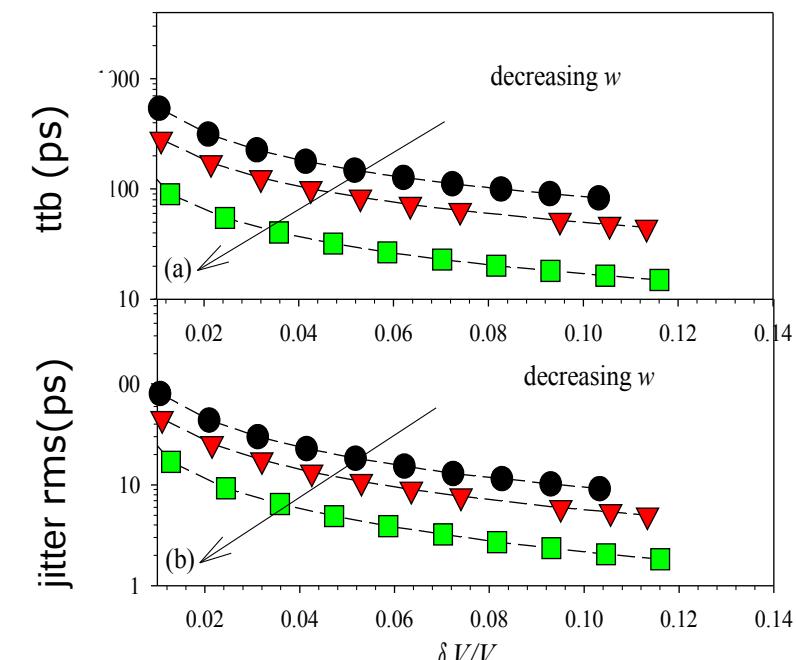
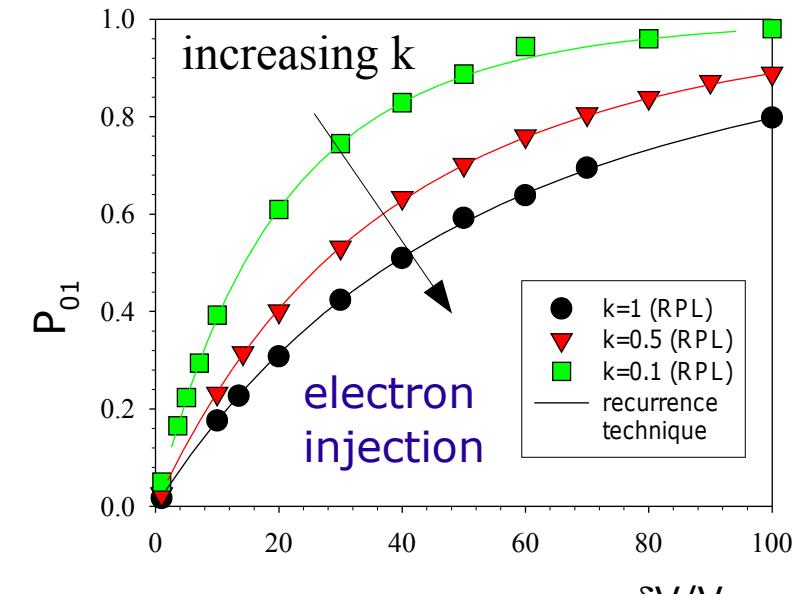
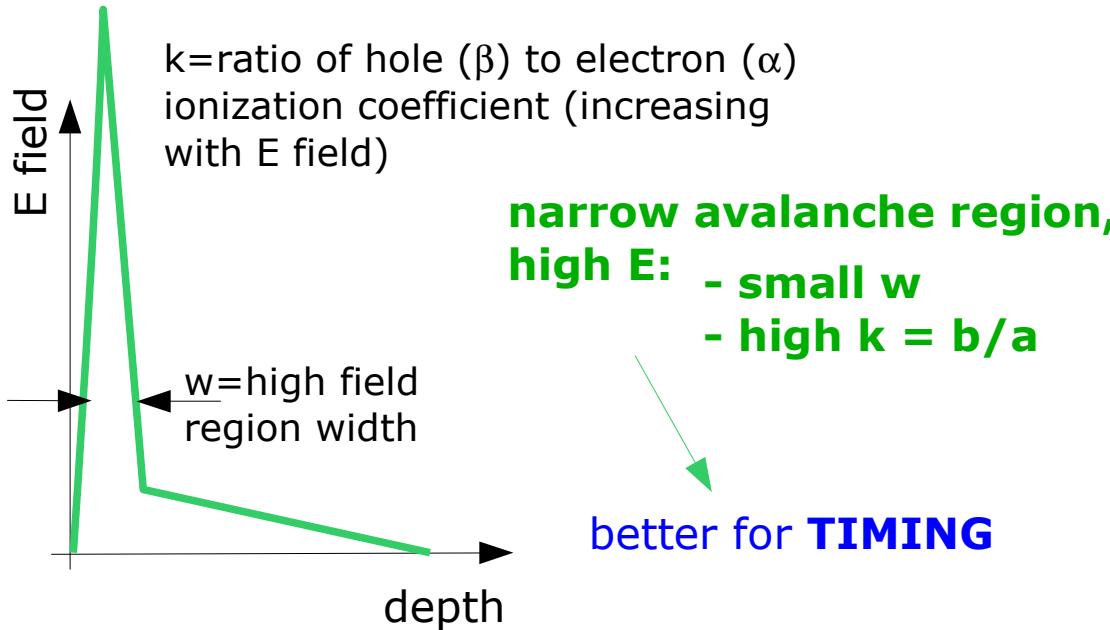


S.Cova et al. NIST Workshop on SPD (2003)

- **Neutral regions** underneath the junction : timing tails for long wavelengths
- **Neutral regions** in APD entrance: timing tails for short wavelengths

PDE vs timing optimization

C.H.Tan et al IEEE J.Quantum Electronics 13 (4) (2007) 906



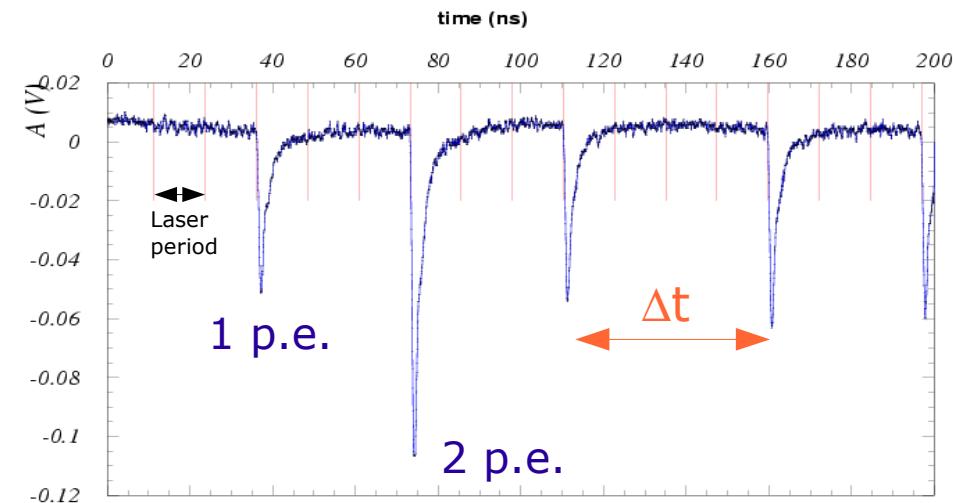
Plots are courtesy of C.H.Tan

Waveform analysis: optimum timing filter

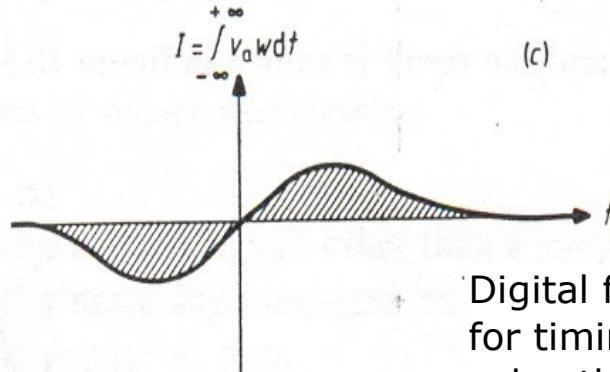
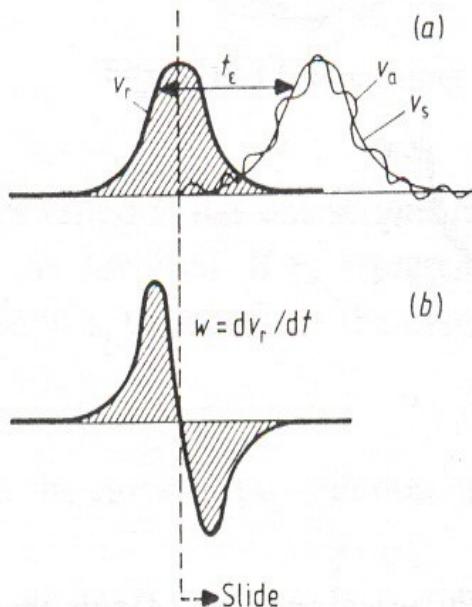
Example of intrinsic SPTR measurement from Δt of consecutive pulses by laser shots

Different algorithms to reconstruct the time of the pulses:

- x parabolic fit to find the peak maximum
- x CFD (digital)
- x average of time samples weighted by the waveform derivative
- ✓ digital filter: weighting by the derivative of a reference signal
→ optimum against (white) noise (if signal shape fixed)



G.C. et al NIMA 581 (2007) 461



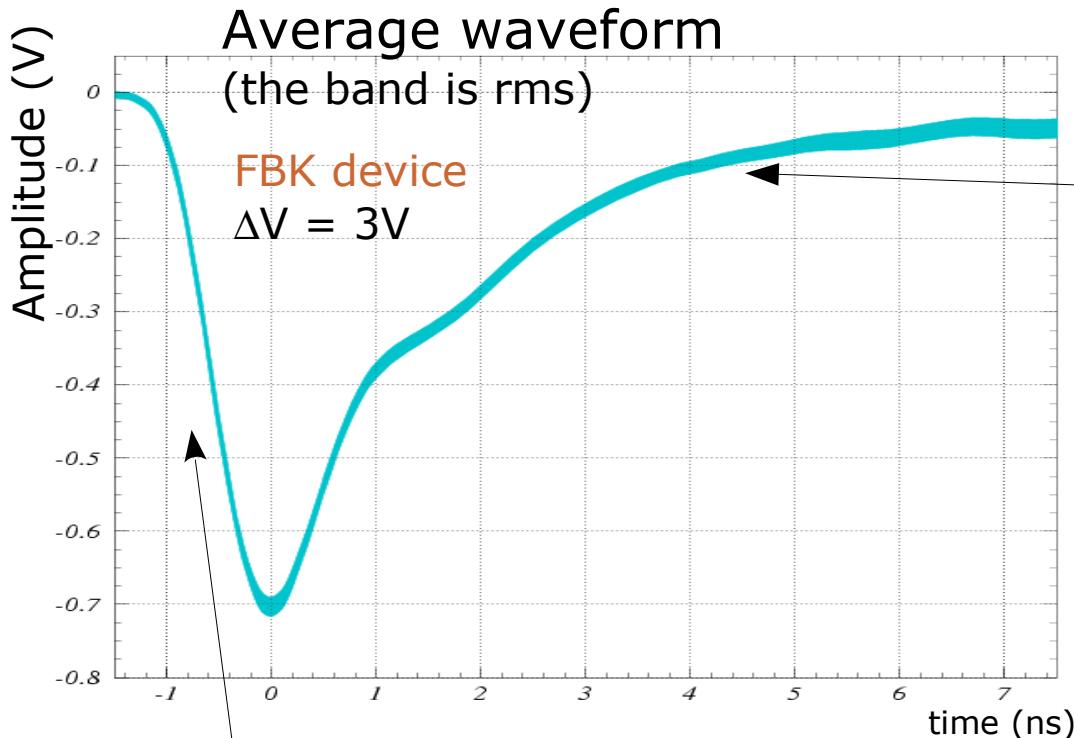
Digital filter to minimize N/S for timing measurements:
solve the following equation on t_0 :

$$\int V_a(t) \frac{\partial V_r(t-t_0)}{\partial t} dt = 0$$

V_a = measured signal (includes noise)
V_r = reference signal
 t_0 = reference time

see e.g. Wilmshurst "Signal recovery from noise in electronic instrumentation"

Waveform (single p.e.)



Falling signal shape fluctuates considerably (due eg to after-pulses)
→ signal tail is non useful for timing, if not detrimental

note: using Time-over-Threshold method for slew correction might lead to worse resolution

Reminder:

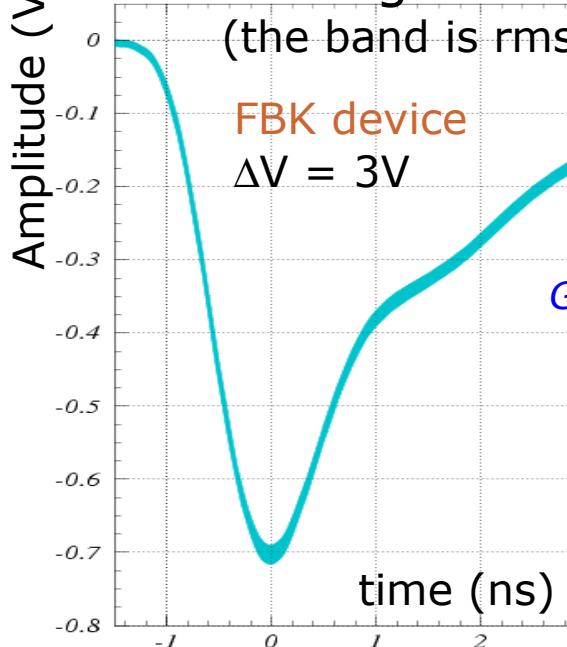
$$\frac{dI}{dt} \sim \frac{\sqrt{D}}{R_{sp} \sqrt{\tau}}$$
$$\tau \sim \frac{1}{1 - (E_{max}/E_{breakdown})^n}$$

Rise-time depends on ΔV , T and impact position
ie **signal shape is not constant**, then:
1) CFD method only partially effective in canceling time walk effects
2) any digital timing filter should account for shape variations (ΔV , T)

For comparison about **waveform method** and various digital algorithms
see [Ronzhin et al NIM A 668 \(2012\) 94](#)

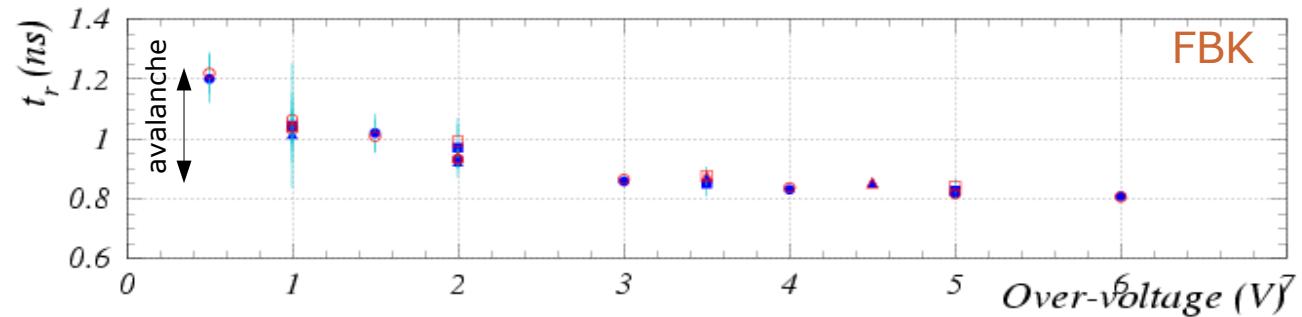
Waveform analysis: 1 p.e. reference signal

Average waveform
(the band is rms)



Additional contribution to rms
(after-pulses)

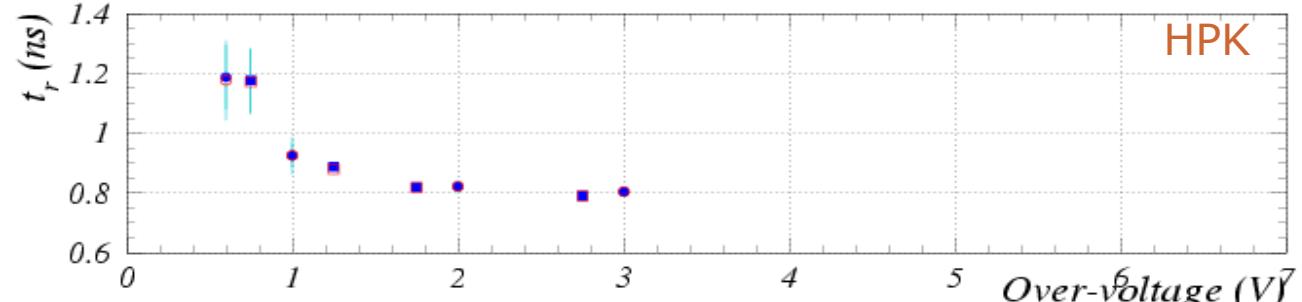
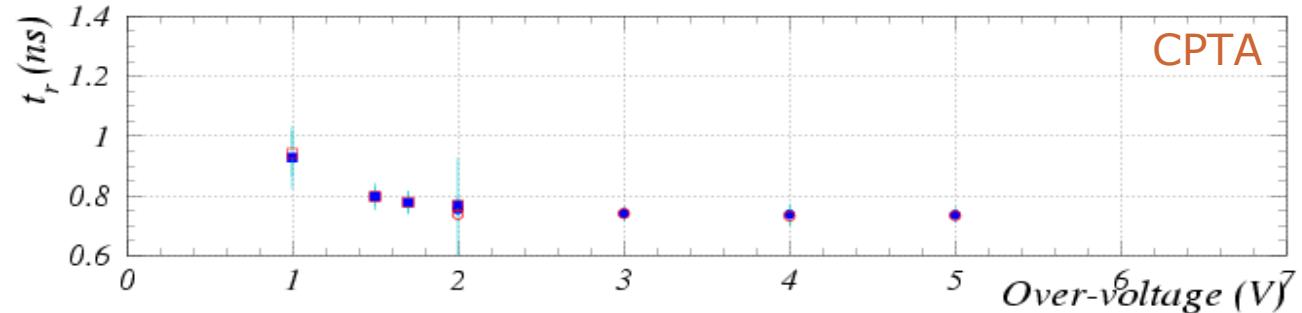
Rise time (10%-90%)
(dominated by electronics contribution)



Reminder:

$$\frac{dI}{dt} \sim \frac{\sqrt{D}}{R_{sp} \sqrt{\tau}}$$

$$\tau \sim \frac{1}{1 - (E_{max}/E_{breakdown})^n}$$



For comparison about rise-time
of HKP devices see
[P.Avella et al doi:10.1016/
j.nima.2011.11.049](https://doi.org/10.1016/j.nima.2011.11.049)

Single Photon Time Resolution = gaussian + tails

Time resolution of SiPM is not just a gaussian, but gaussian + tails
(in particular at long wavelengths)

G.C. et al NIMA 581 (2007) 461

Data at $\lambda=400\text{nm}$

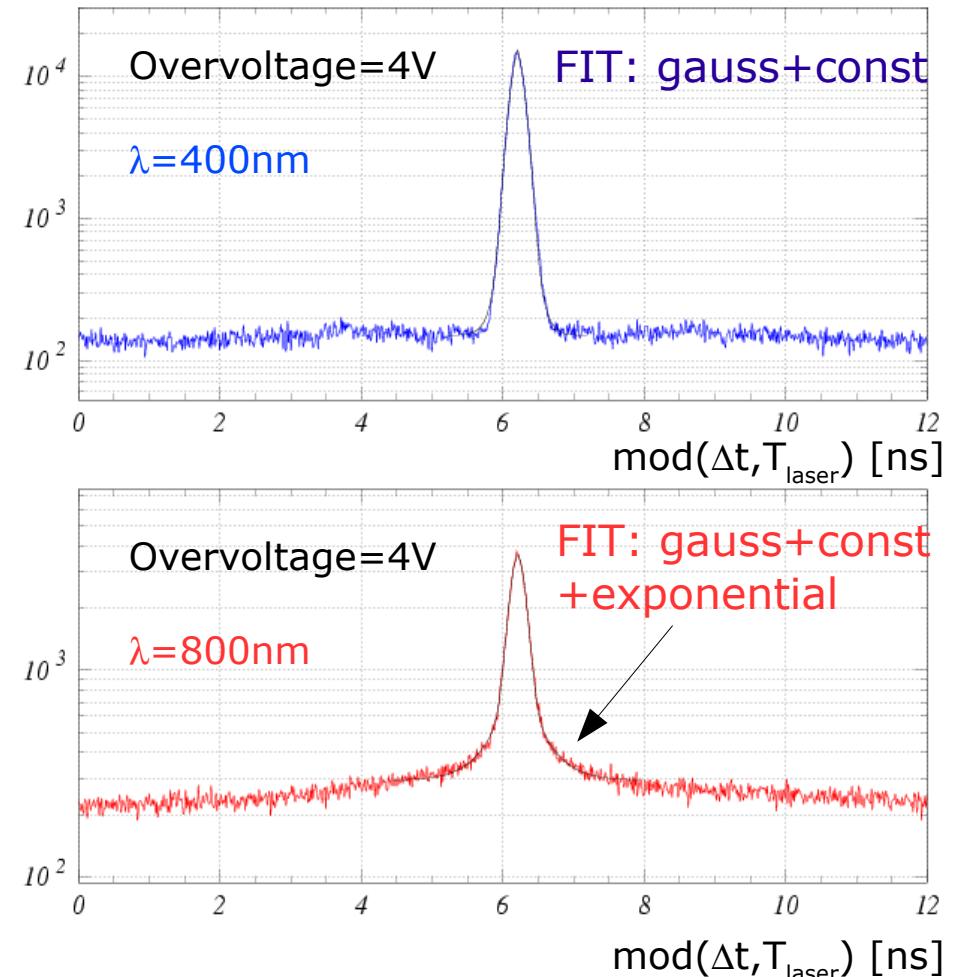
A simple **gaussian component**
fits fairly

Data at $\lambda=800\text{nm}$

fit gives reasonable χ^2 in case of an
additional exponential term
 $\exp(-|\Delta t|/\tau)$ summed with a weight

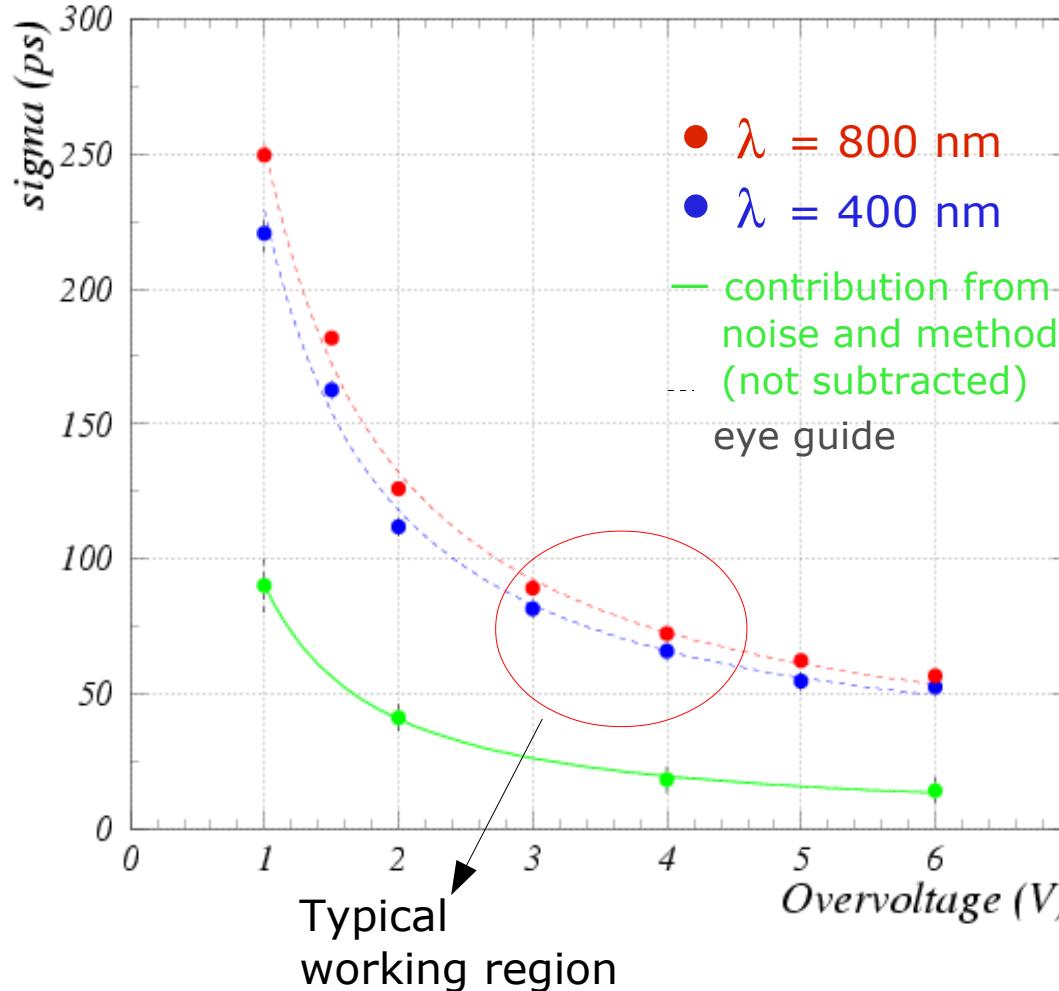
- $\tau \sim 0.2 \div 0.8\text{ns}$ (depending on device)
in rough agreement with diffusion tail lifetime: $\tau \sim L^2 / \pi^2 D$ where L is the diffusion length
- Weight of the **exp. tail $\sim 10\% \div 30\%$**
(depending on device)

Gaussian + Tails (long λ)
 $\text{rms} \sim 50\text{-}100\text{ ps}$
 $\sim \exp(-t / \tau)$
contrib. several %
for long wavelengths



Distributions of the difference in time between successive peaks

SPTR: FBK devices – shallow junction



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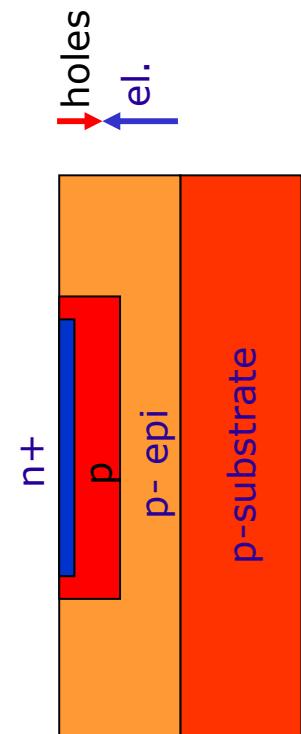
NOTE: good timing performances kept up to 10MHz/mm² photon rates

electron
injection
hole
injection

contribution from
noise and method
(not subtracted)

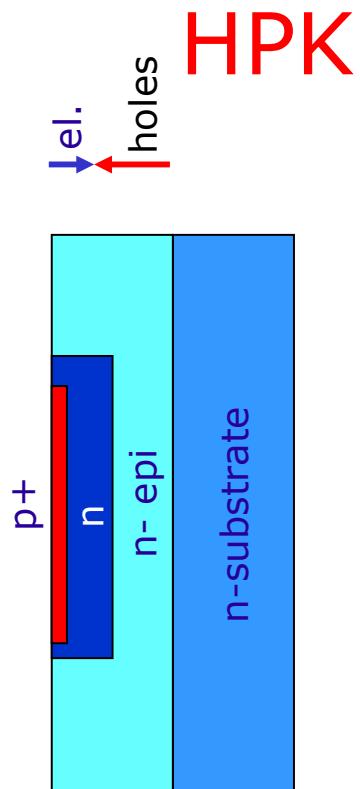
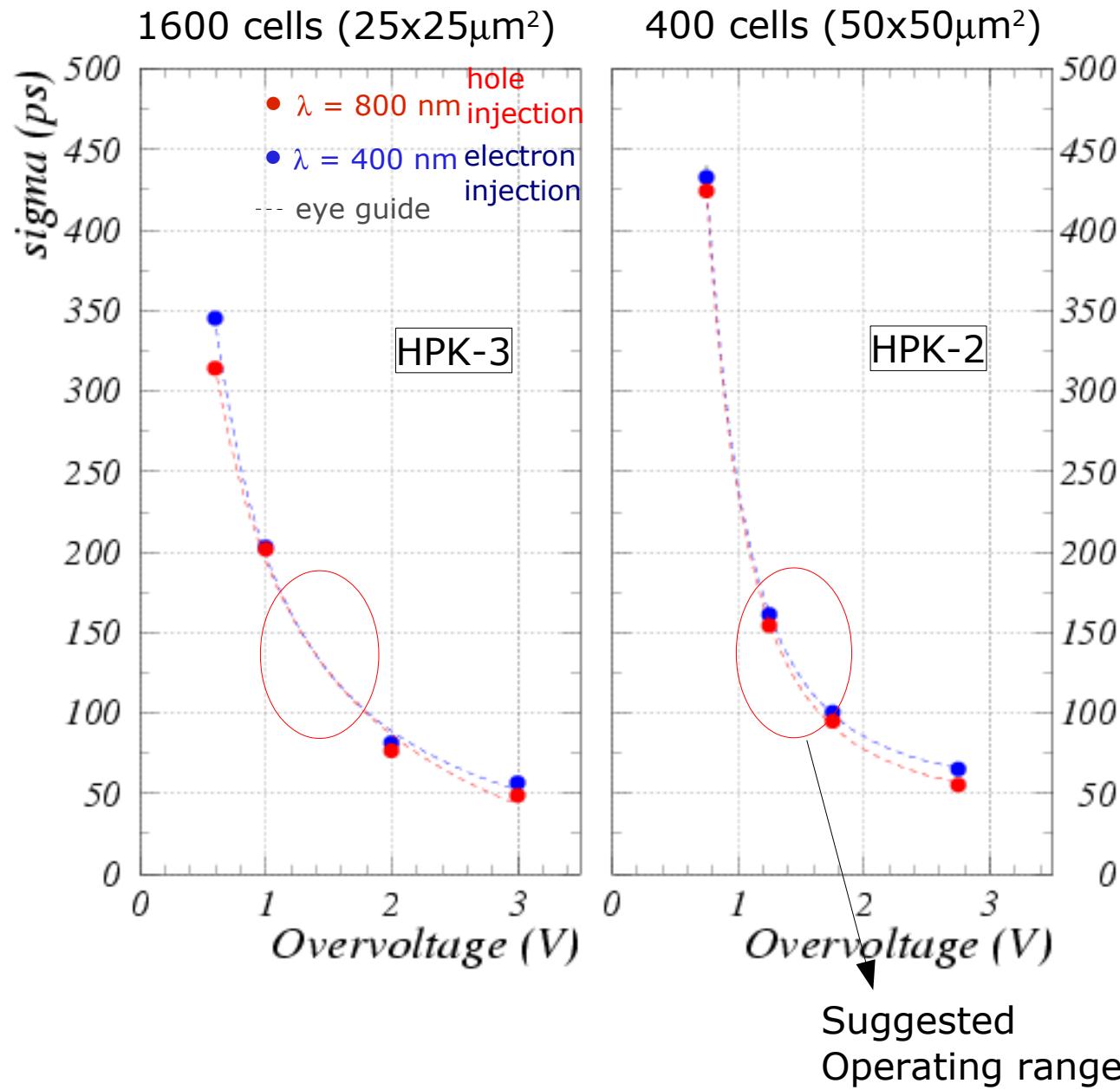
eye guide

In general due to
drift, resolution
differences

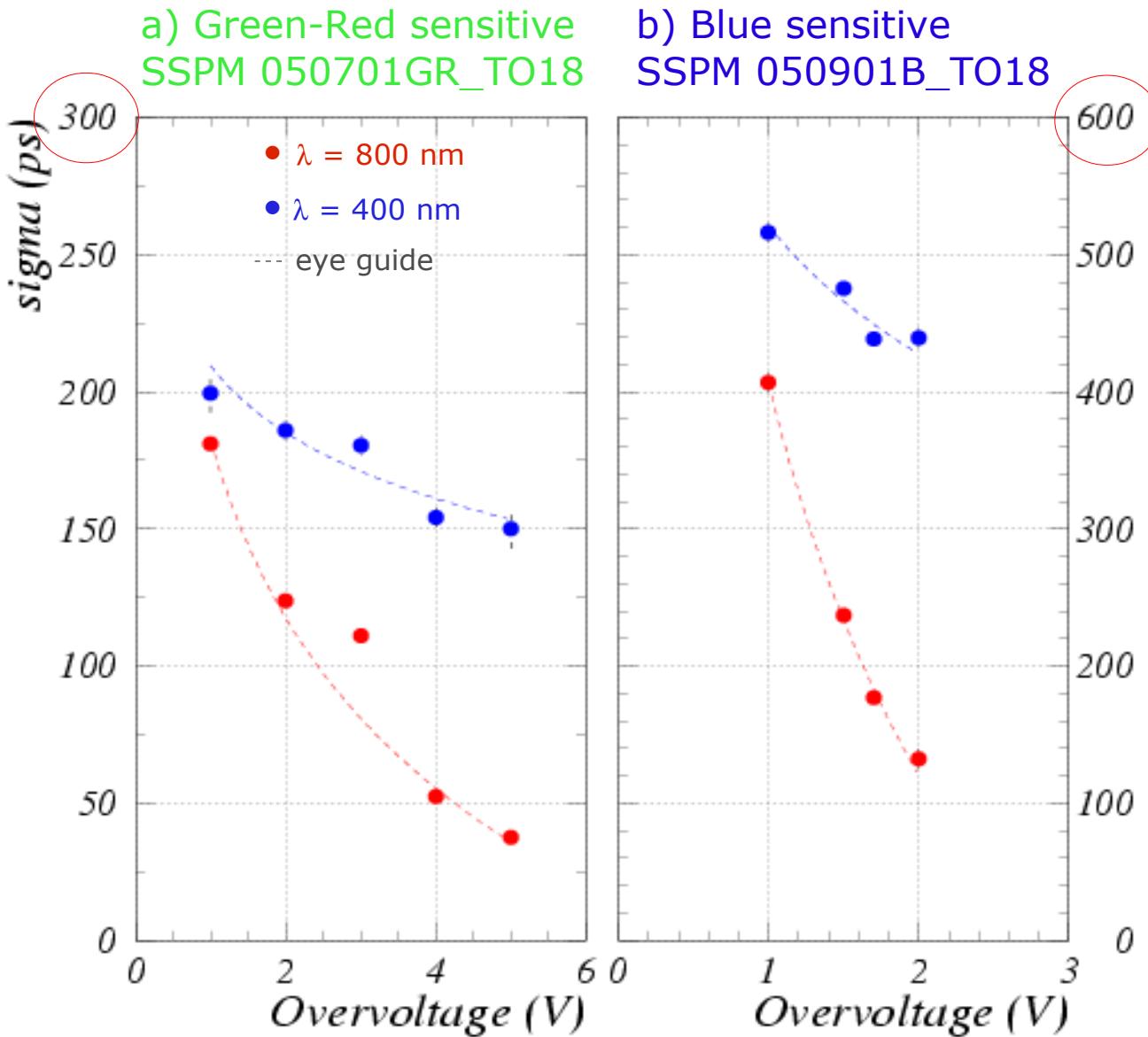


- 1) **high field junction position**
 - shallow junction: $\sigma_t^{\text{red}} > \sigma_t^{\text{blue}}$
 - buried junction: $\sigma_t^{\text{red}} < \sigma_t^{\text{blue}}$
- 2) **n⁺-on-p smaller jitter than p⁺-on-n** due to electrons drifting faster in depletion region (but λ dependence)
- 3) above differences more relevant in **thick devices than thin**

SPTR: Hamamatsu



SPTR: CPTA/Photonique – thick structures



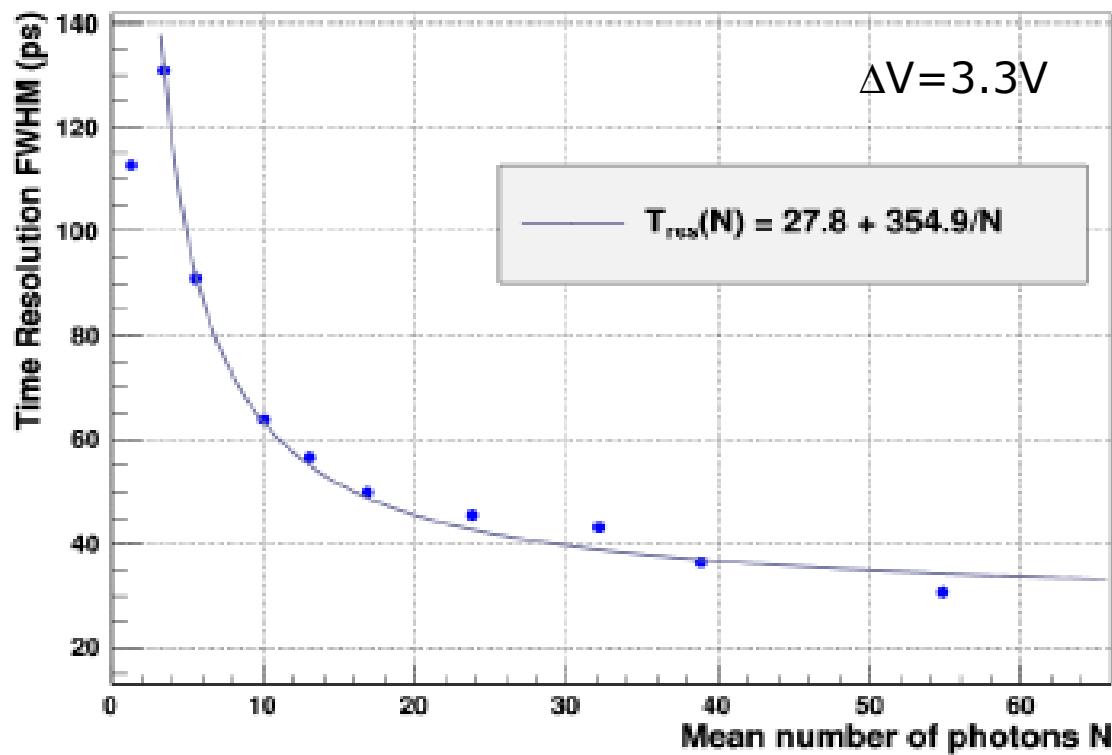
- **thick structures**
- **deep junctions**

a) n^+ -on-p
→ electrons drift

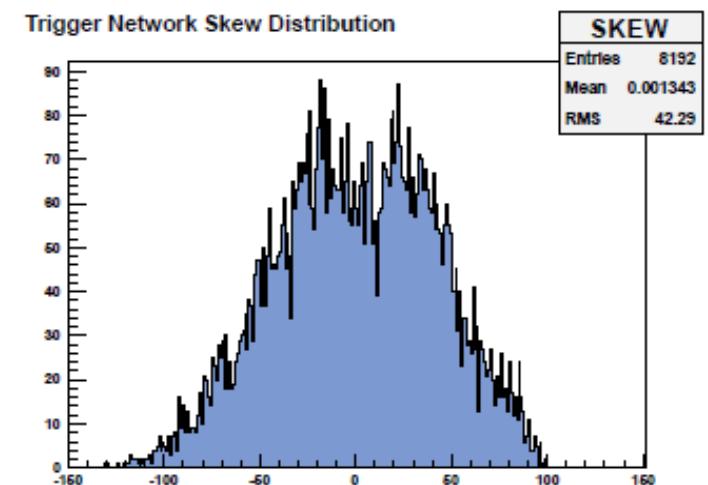
b) p^+ -on-n
→ holes drift ($v_e/3$)

dSiPM timing resolution

Time Resolution

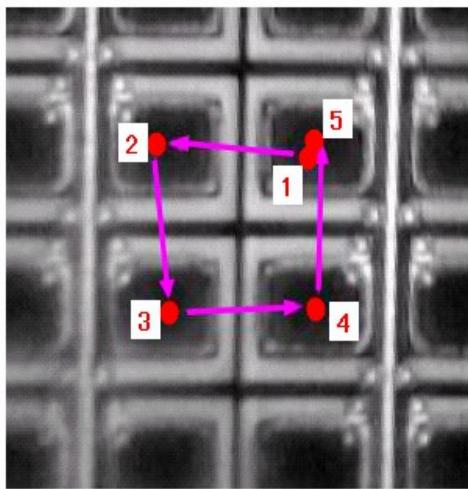


T.Frach at LIGHT 2011

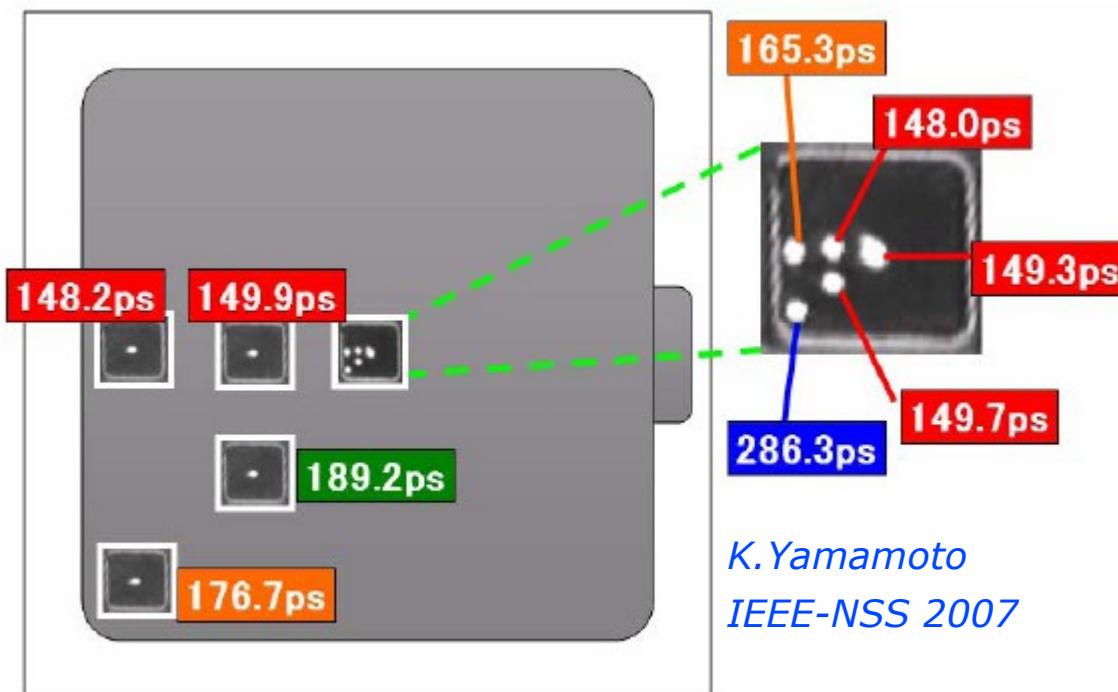


- Sensor triggered by attenuated laser pulses at first photon level
- Laser pulse width: 36ps FWHM, $\lambda = 410\text{nm}$
- Contribution to time resolution (FWHM):
 - SPAD: 54ps, trigger network: 110ps, TDC: 20ps
- Trigger network skew currently limits the timing resolution

SPTR: position dependence → cell size

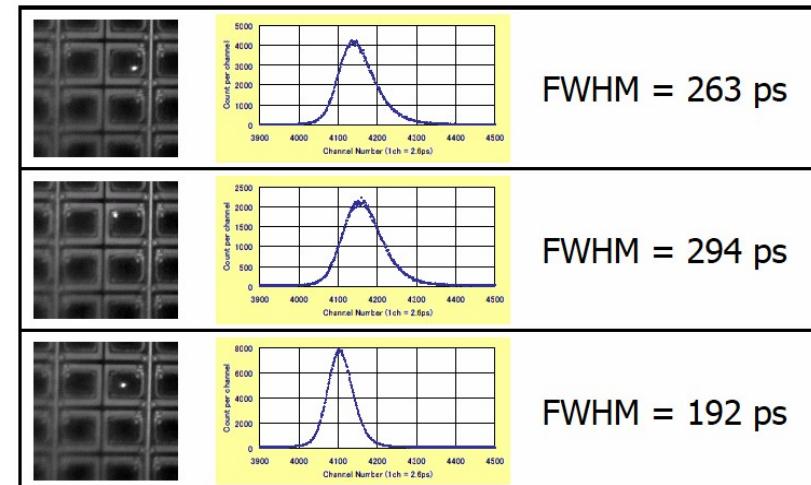


	FWHM (ps)	FWTM (ps)
1	199	393
2	197	389
3	209	409
4	201	393
5	195	383



Data include the system jitter
(common offset, not subtracted)

K.Yamamoto PD07



FWHM = 263 ps

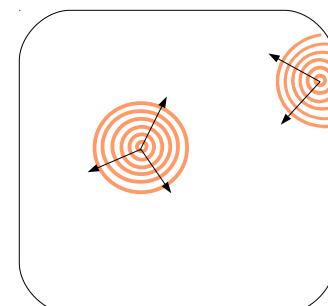
FWHM = 294 ps

FWHM = 192 ps

Larger jitter if photo-conversion at the border of the cell

Due to:

- 1) slower avalanche front propagation
- 2) lower E field at edges
→ cfr PDE vs position



SPTR: timing at low T

Timing: improves at low T

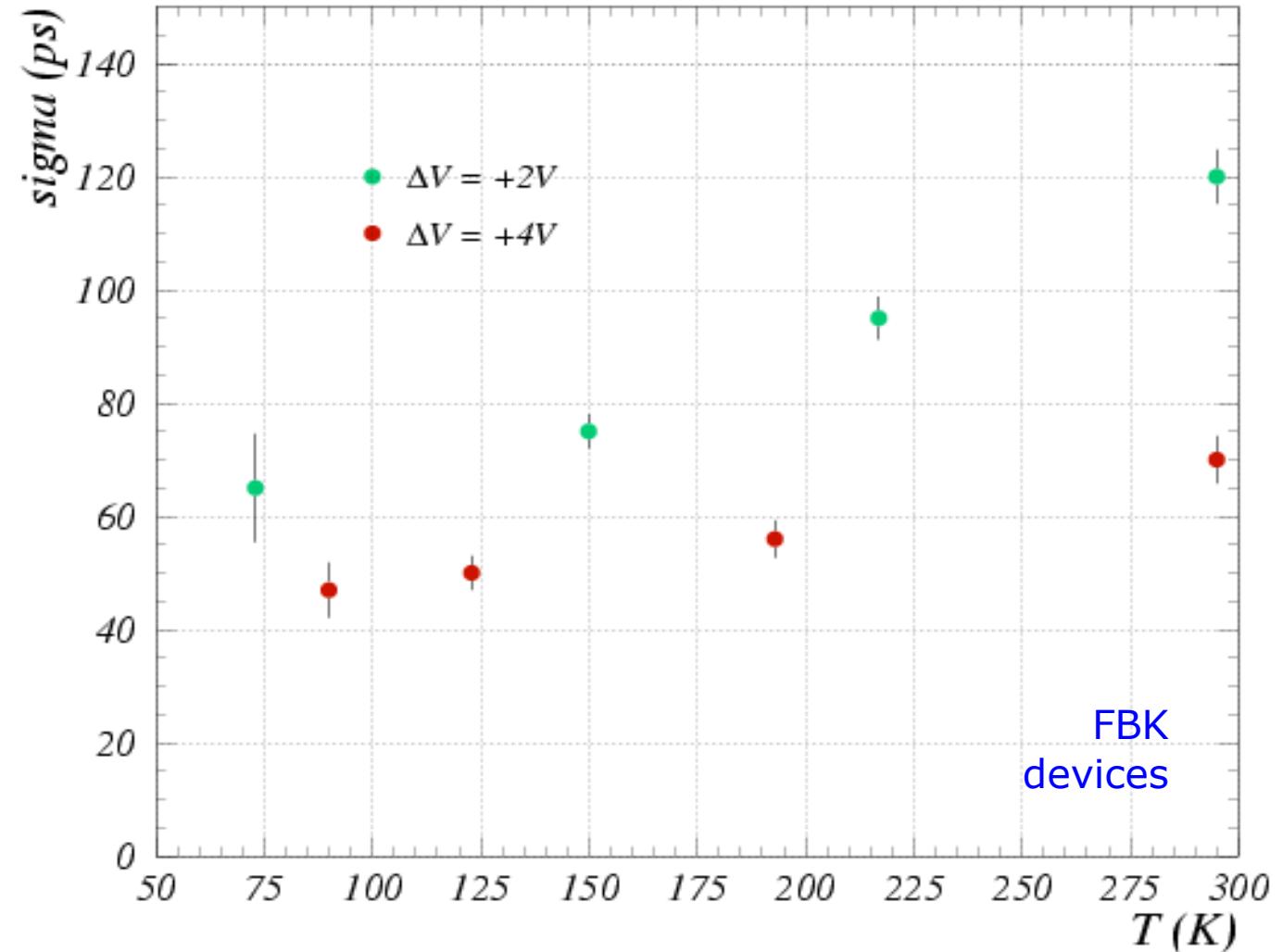
Lower jitter at low T due to
higher mobility:

- a) avalanche process is faster
- b) reduced fluctuations

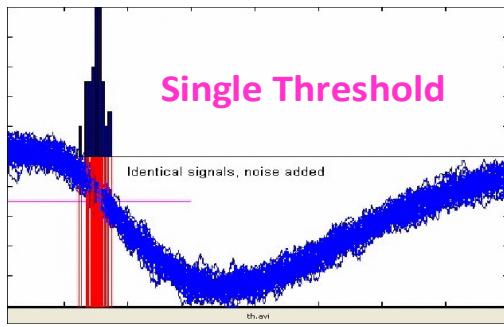
(Over-voltage fixed)

Note:

$$\frac{dI}{dt} \sim \frac{\sqrt{D}}{R_{sp} \sqrt{\tau}}$$



Optimizing signal shape for timing



Timing by (single) threshold:

→ time spread proportional to
1/rise-time and noise

$$\sigma_{time} = \frac{\sigma_{amplitude}}{\frac{df(t)}{dt}}$$

Timing with optimum filtering:

→ best resolution with

$f'(t)$ weighting function

$$\sigma_{time}^2 = \frac{\sigma_{amplitude}^2}{\int dt \left[\frac{df(t)}{dt} \right]^2}$$

Pulse sampling and Waveform analysis:

Sample, digitize, fit the (known) waveform
→ get time and amplitude

$$\sigma_{time}^2 = \frac{\sigma_{amplitude}^2}{N_{samples} \int dt \left[\frac{df(t)}{dt} \right]^2}$$

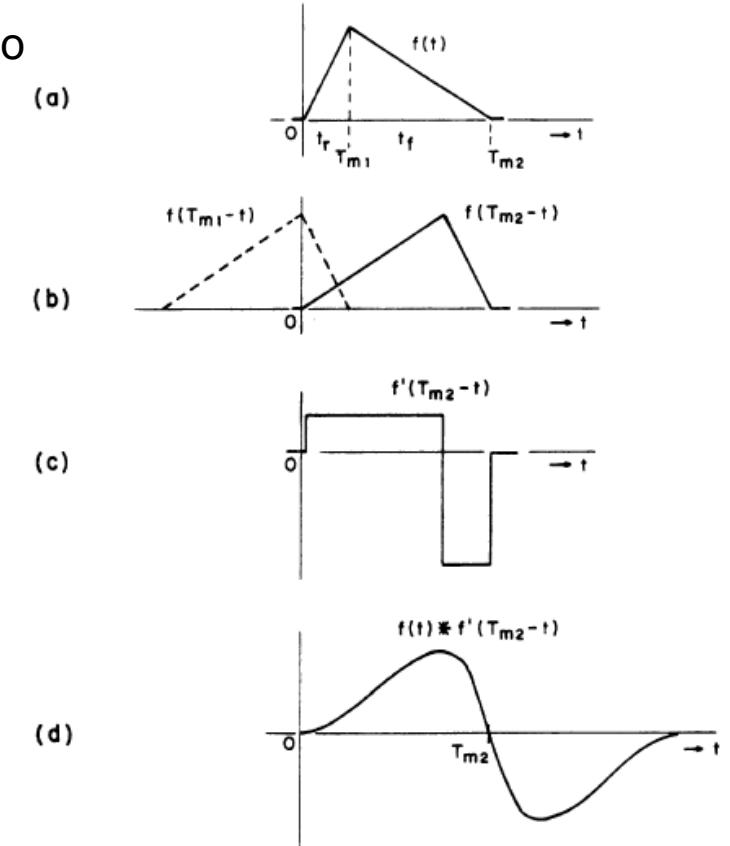


Fig. 7. Optimum filter for timing in presence of white noise (method of derivation).

(a) signal waveform

(b) optimum filter for amplitude measurements.

(c) optimum filter for timing - derivative of (b).

(d) output waveform.

V.Radeka IEEE TNS 21 (1974)...

Optimizing signal shape for timing

Single cell model $\rightarrow (R_d || C_d) + (R_q || C_q)$

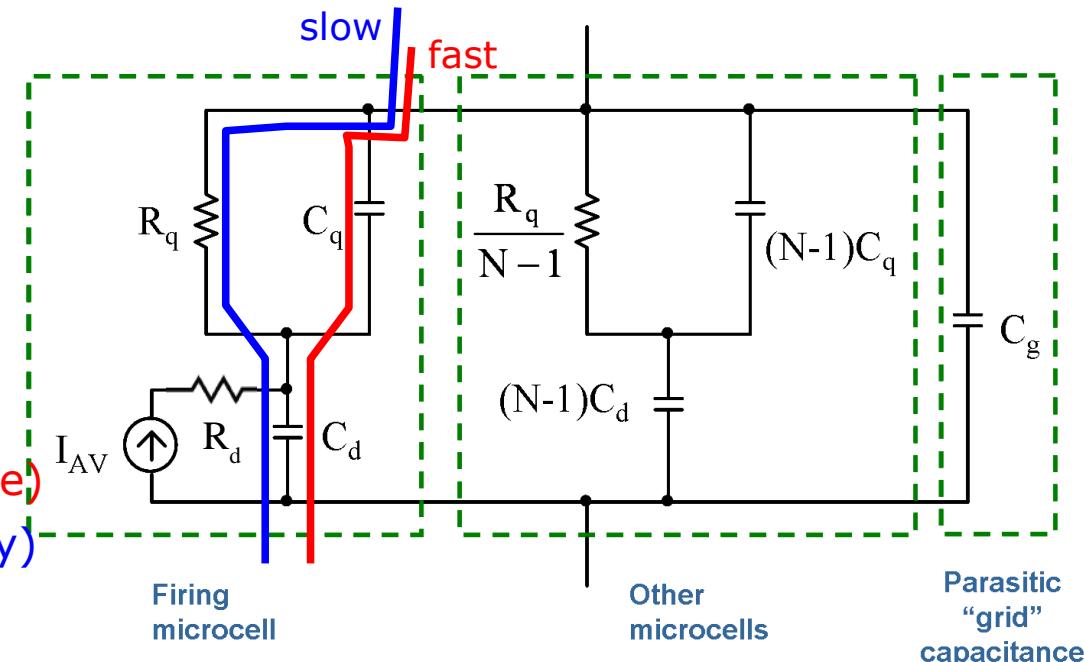
SiPM + load $\rightarrow (||Z_{cell}) || C_{grid} + Z_{load}$

Signal = **slow** pulse ($\tau_{d(rise)}, \tau_{q-slow(fall)}$) +
+ **fast** pulse ($\tau_{d(rise)}, \tau_{q-fast(fall)}$)

- $\bullet \tau_{d(rise)} \sim R_d(C_q + C_d)$

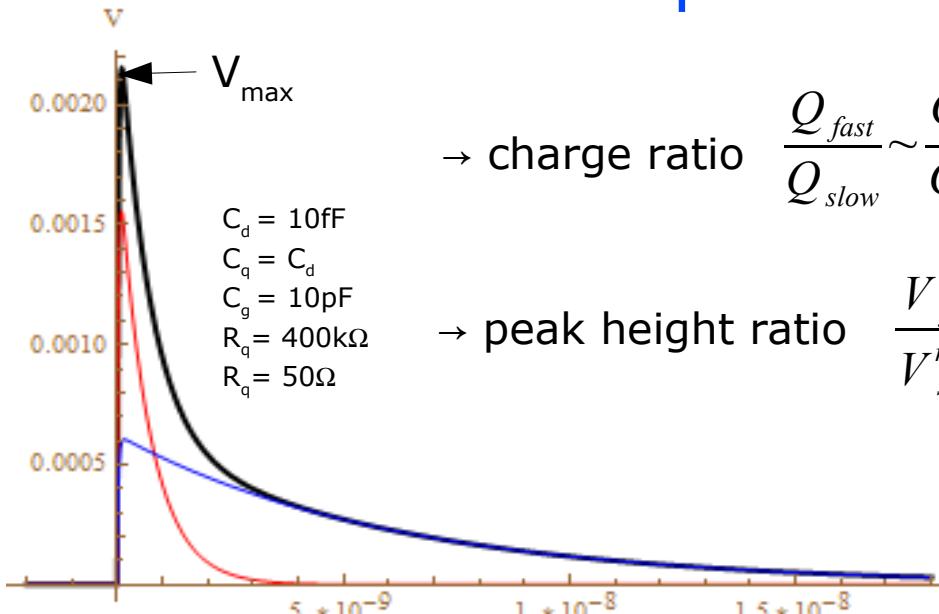
- $\bullet \tau_{q-fast(fall)} = R_{load} C_{tot}$ (fast; parasitic spike)

- $\bullet \tau_{q-slow(fall)} = R_q(C_q + C_d)$ (slow; cell recovery)



Pulse shape

$$V(t) \approx \frac{Q}{C_q + C_d} \left(\frac{C_q}{C_{tot}} e^{\frac{-t}{\tau_{FAST}}} + \frac{R_{load}}{R_q} \frac{C_d}{C_q + C_d} e^{\frac{-t}{\tau_{SLOW}}} \right)$$



$$\rightarrow \text{charge ratio } \frac{Q_{fast}}{Q_{slow}} \sim \frac{C_q}{C_d}$$

$$\rightarrow \text{peak height ratio } \frac{V_{fast}^{max}}{V_{slow}^{max}} \sim \frac{C_q^2 R_q}{C_d C_{tot} R_{load}}$$

increasing with R_q and $1/R_{load}$
(and C_q of course)

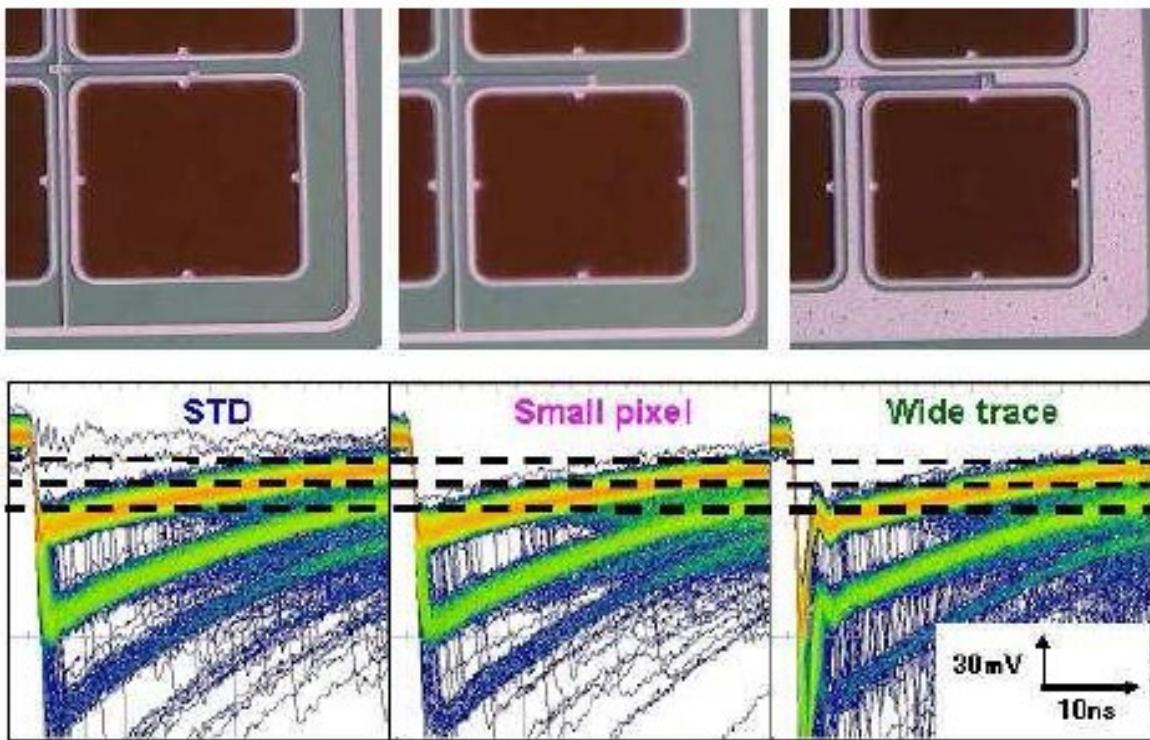
Increasing C_q/C_d or/and R_q/R_{load}
 \rightarrow spike enhancement
 \rightarrow better timing

Optimizing signal shape for timing (S PTR)

→ peak height ratio

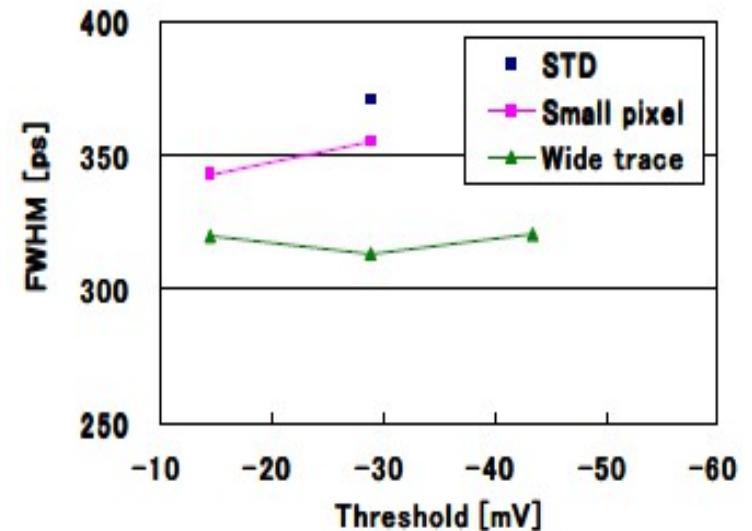
$$\frac{V_{fast}^{max}}{V_{slow}^{max}} \sim \frac{C_q^2 R_q}{C_d C_{tot} R_{load}}$$

Enhancing C_q does improve timing performances



Yamamura et.al. at PD09

1mm□100um (GAIN=2.4E+06, 25°C)
Timing resolution of 1p.e. vs threshold



Analogous method for timing optimization proposed in C.Lee et al NIM A 650 (2010) 125
"Effect on MIM structured parallel quenching capacitor of SiPMs"

Note:

The **steep falling front** of the fast peak could be exploited too for optimum timing

$$\sigma_{time}^2 = \frac{\sigma_{amplitude}^2}{N_{samples} \int dt [f'(t)]^2}$$

Summary

Significant development of SiPMs
over the last few years
and **new players**

- **Operative ΔV over-bias range:**
from 2V (eg HPK) to 10V (eg FKB) depending on E field profile and Rq
- **T coefficient:** low, below 0.3%/°C for many devices
→ might be lower, but **tradeoff** against PDE and noise
- **Pulse Shape** and **Gain:** tuned for matching application requirements (**tradeoffs**)
→ photon counting and timing vs energy measurement (signal spike, E_{field} profile)
- **Dynamic range:** Large, up a few x10000 pixels (eg NDL, Zecotek)
→ improved **radiation hardness** (not covered in this review) is relevant bonus
→ trade-off with Fill Factor
- **PDE:** up to 60% for blue-green light (eg. KETEK)
→ easily tuned to match applications (but only in visible optical range)
- **DCR** at T room can be $< 100\text{kHz/mm}^2$ (eg. Hamamatsu)
- **Cross-Talk:** can be as low as 1% in operative range (eg. FBK, MePhi/Pulsar)
- **After-Pulsing:** still at some % level for many devices
→ exploiting higher Rq "just" to hide A-P is not a good practice...
→ Digital SiPM is prone too, though less affected (active quenching)
- **Timing:** intrinsically fast, SPTR $< 50\text{ps}$ in operative range
→ but mind the **diffusion non-gaussian tails** in temporal response (long λ)
- **Calibration:** precise, thanks to existing detailed operative models

Still missing and Future threads

- Avalanche **detailed physical models are still missing**. In particular for
 - **ultra-fast timing** applications there is room for device improvement
 - techniques for reducing **long timing tails** might be exploited
- Physical models might be of help also in further reducing **DCR** and **A-P**
 - eg: E field engineering for reducing tunneling
- **PDE**: expected soon are
 - improvements the **UV, VUV, EUV region**
 - devices with **through vias** → coupling with scintillators, fast imaging !
- GM-APD arrays for **NIR, IR sensitivity**: **different semiconductors**
 - InGaAs GM-APD arrays from AmplificationTechnologies do exist but... small area, noise and cost (!)
- **DCR**:
 - expected in 2012 a factor **x3 improvement** → larger area devices will follow
 - in the mean time devices tuned for working at **cryogenic T** easy to devise
- **Low T**: SiPM perform ~ideally in the range $100K < T < 200K$
 - Rq should be tuned shorter recovery (ad hoc devices)
 - lower gain (small cells) might be desired to mitigate after-pulses



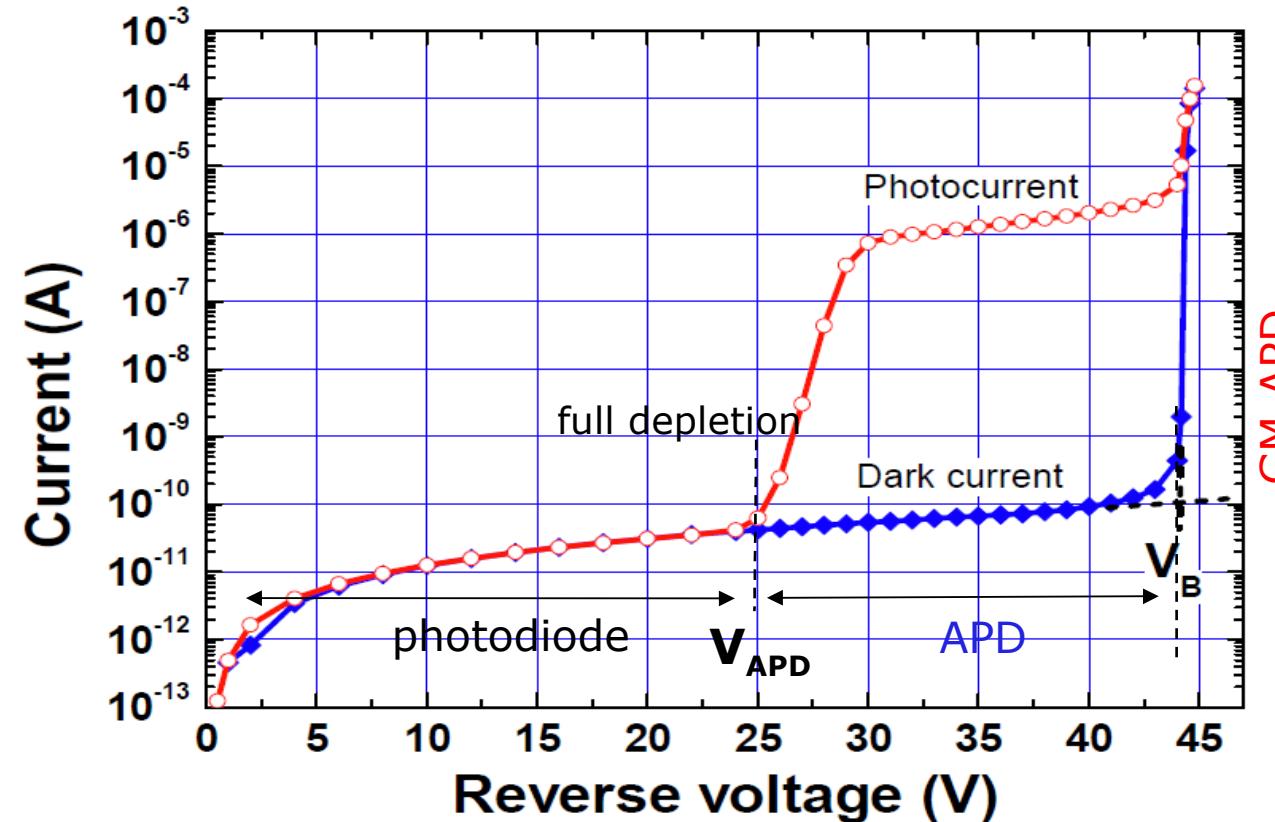
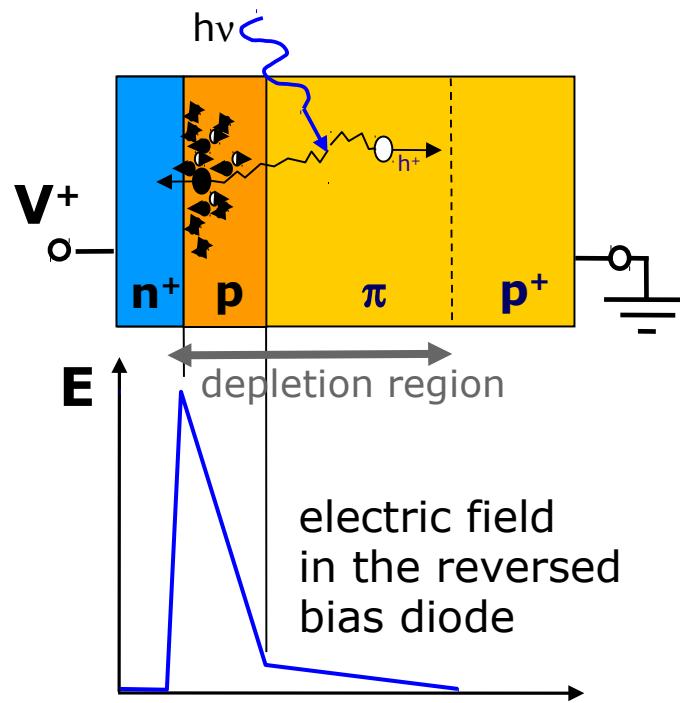
Thanks for your attention



Additional material

The building block of a SiPM: GM-APD

Reverse biased junction



APD: Linear-Proportional Mode

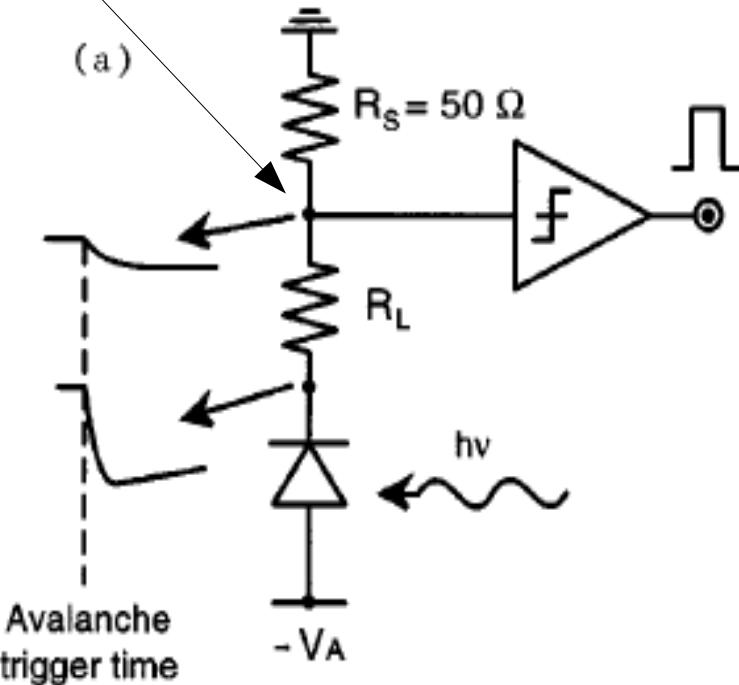
- Bias **BELOW** V_{BD} ($V_{APD} < V < V_{BD}$)
- It's an **AMPLIFIER**
- Multiplication: in practice limited to 10^4 by fluctuations
- No single photo-electron resolution
...except at low T with slow electronics,
Dorokhov et.al. J.Mod.Opt. 51 (2004)

GM-APD: Geiger Mode

- Bias **ABOVE** V_{BD} ($V - V_{BD} \sim$ a few volts)
- It's a **TRIGGER (BINARY)** device
- Multiplication: ∞ ... in practice limited by macroscopic parameters (R,C)
- Limited by dark count rate
- Single photo-electron resolution
- Need Reset (Feedback - Quenching)

Readout Mode

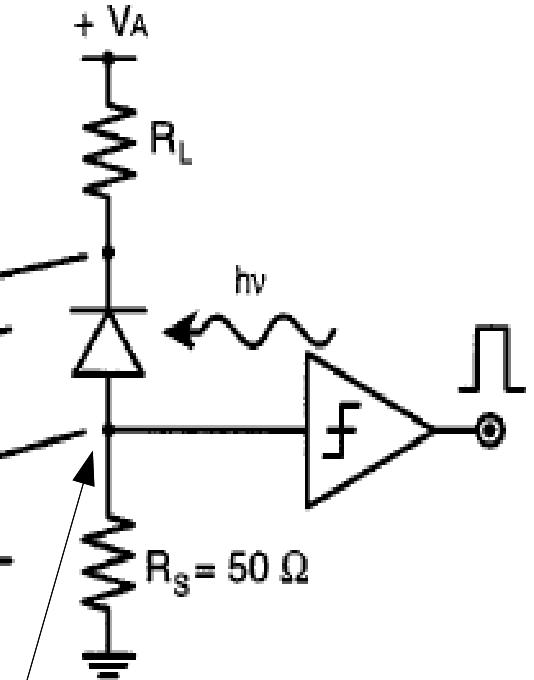
High Z node



Voltage Mode

Current Mode

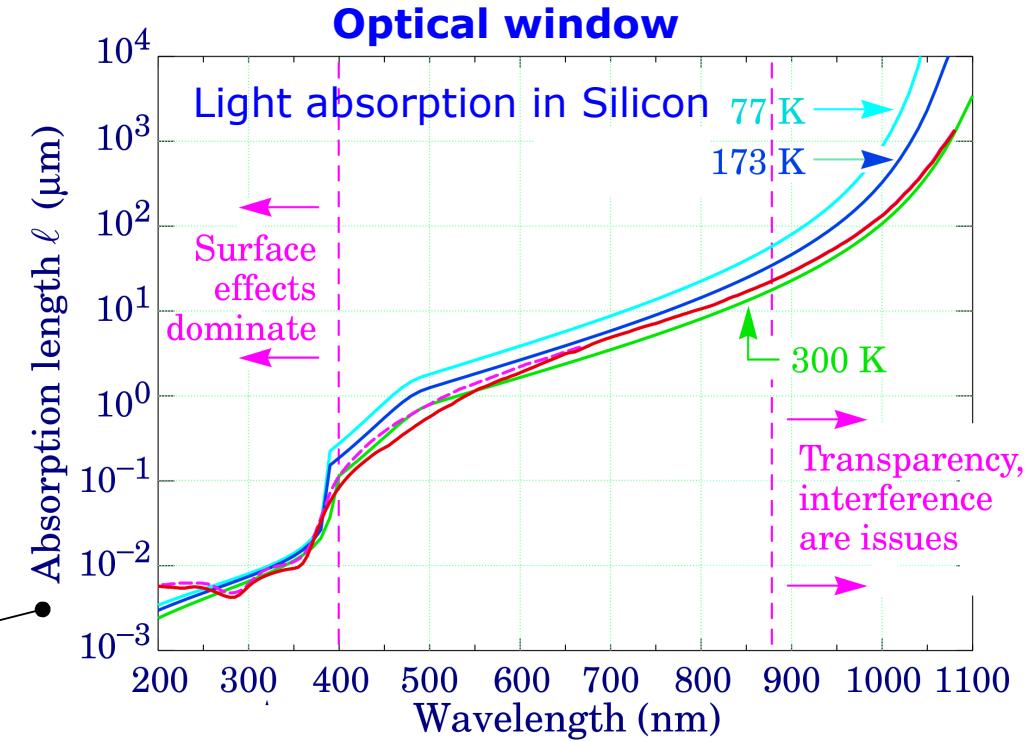
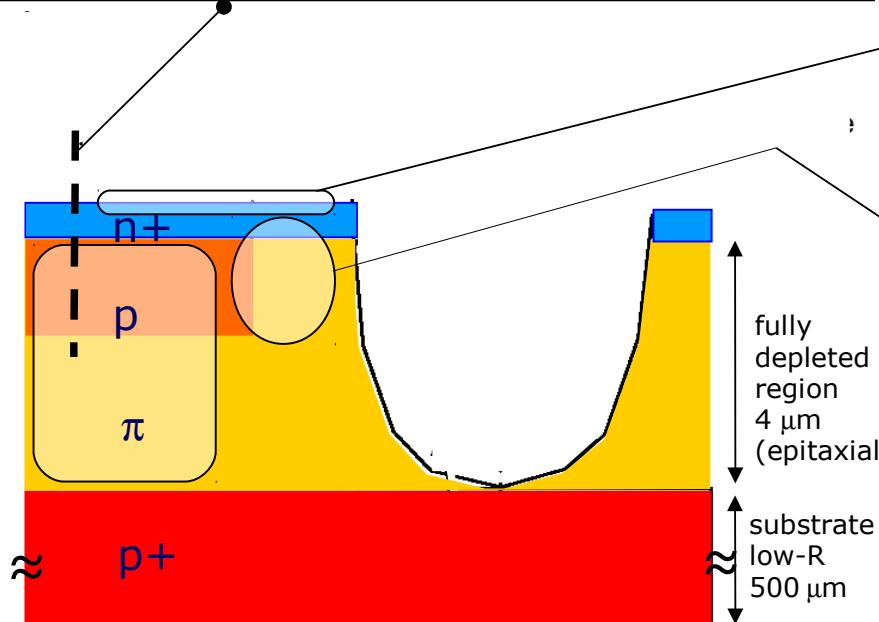
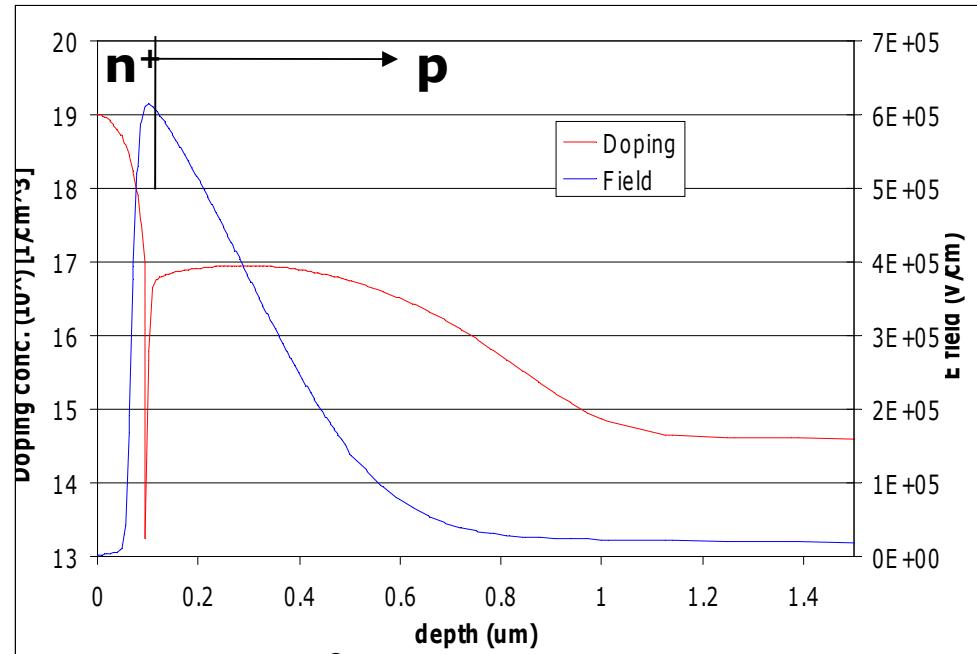
(b)



Low Z node

Key elements in SiPM cell

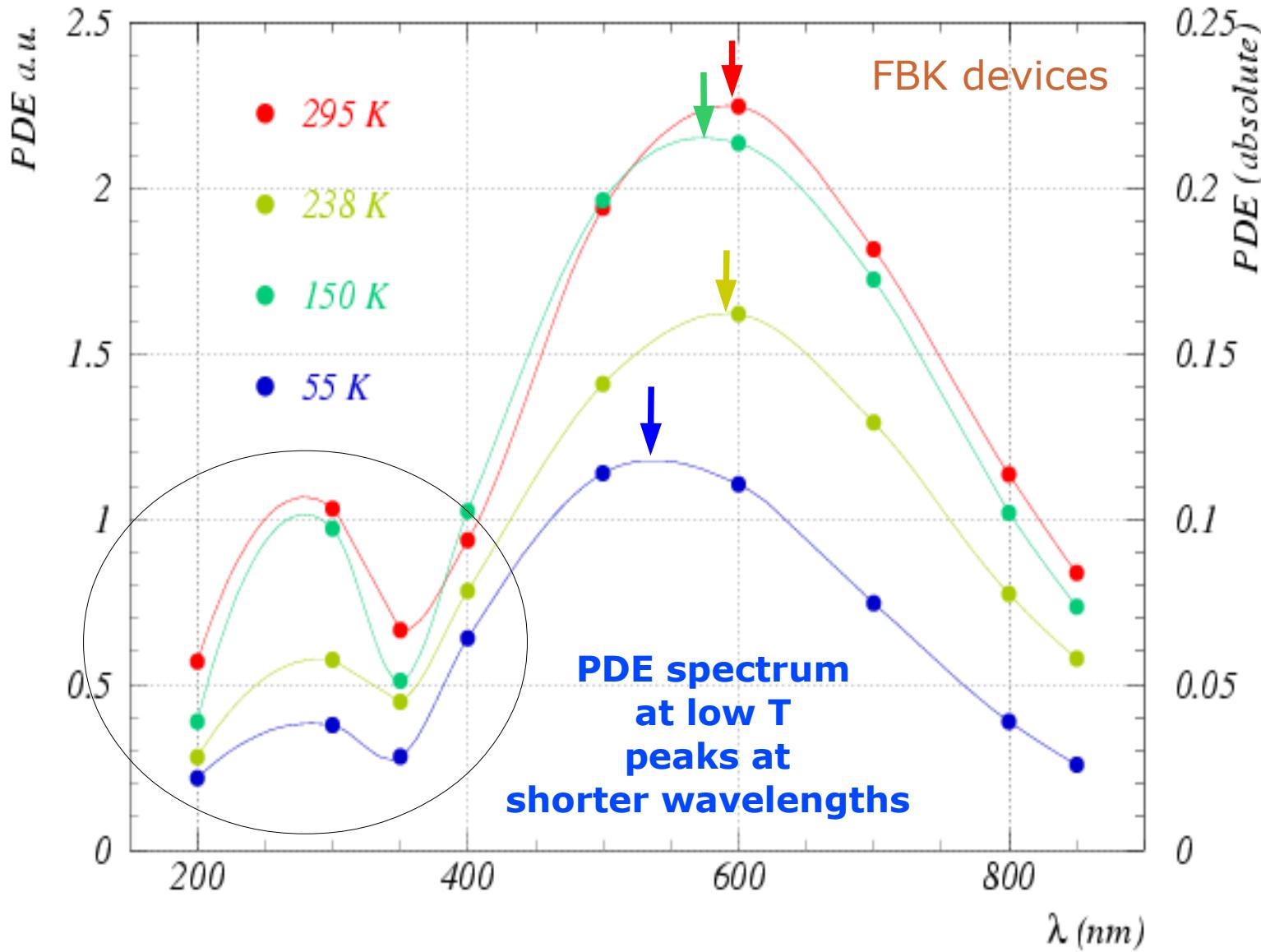
Doping and Field profiles



Guard Ring:

- for avoiding early edge breakdown
- for isolating cells
- for tuning E field shape
- has important impact on fill factor
(more than Rq and metal grid)

PDE vs λ (ΔV fixed, various T)



RPL model: fast simulation

"Statistics of Avalanche Current Buildup Time in Single-Photon Avalanche diodes"
C.H.Tan, J.S.Ng, G.J.Rees, J.P.R.David (Sheffield U.)
IEEE J.Quantum Electronics 13 (4) (2007) 906

Numerical model (MC): Random distribution of impact ionization Path Length (RPL)

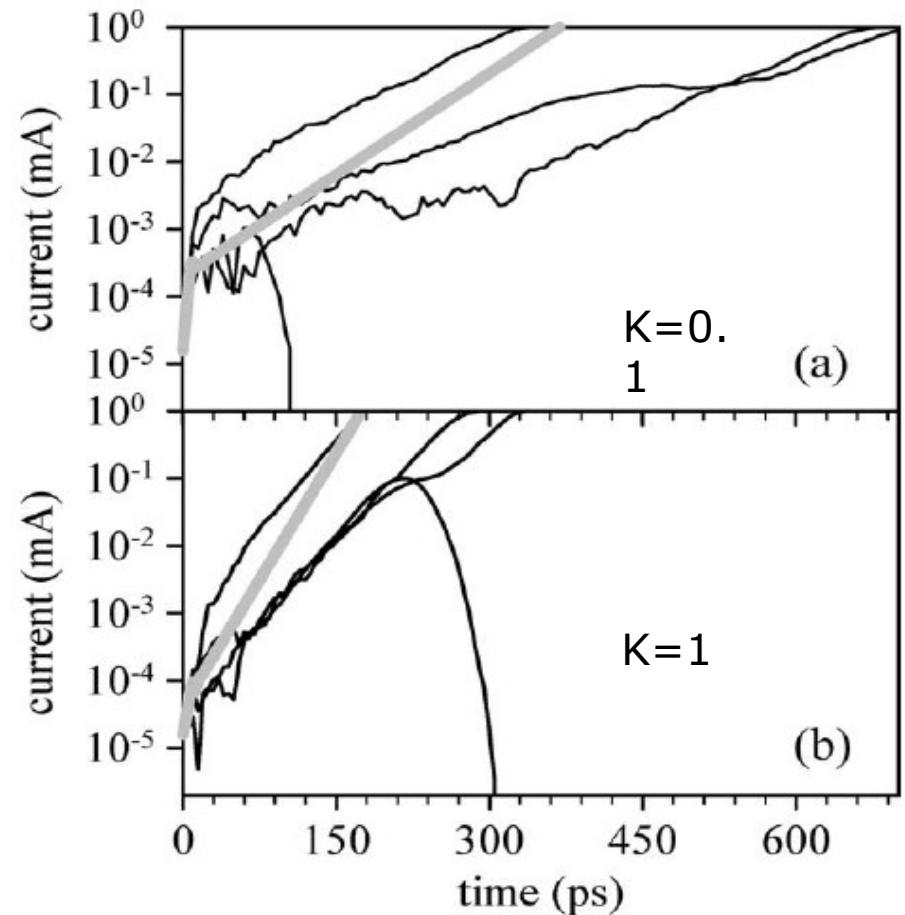
Analysis of **breakdown probability**,
breakdown time and **timing jitter** as
functions of avalanche region width (w),
ionization coefficient ratio ($k = \beta_{\text{hole}}/\alpha_{\text{electron}}$)
and dead space parameter (d)
(uniform E field, constant carrier velocity)

1) increasing k :

- improves timing performances
- but breakdown probability P_{br} increases slowly with overvoltage

1a) hole injection results in better timing than electron injection (in Si devices)

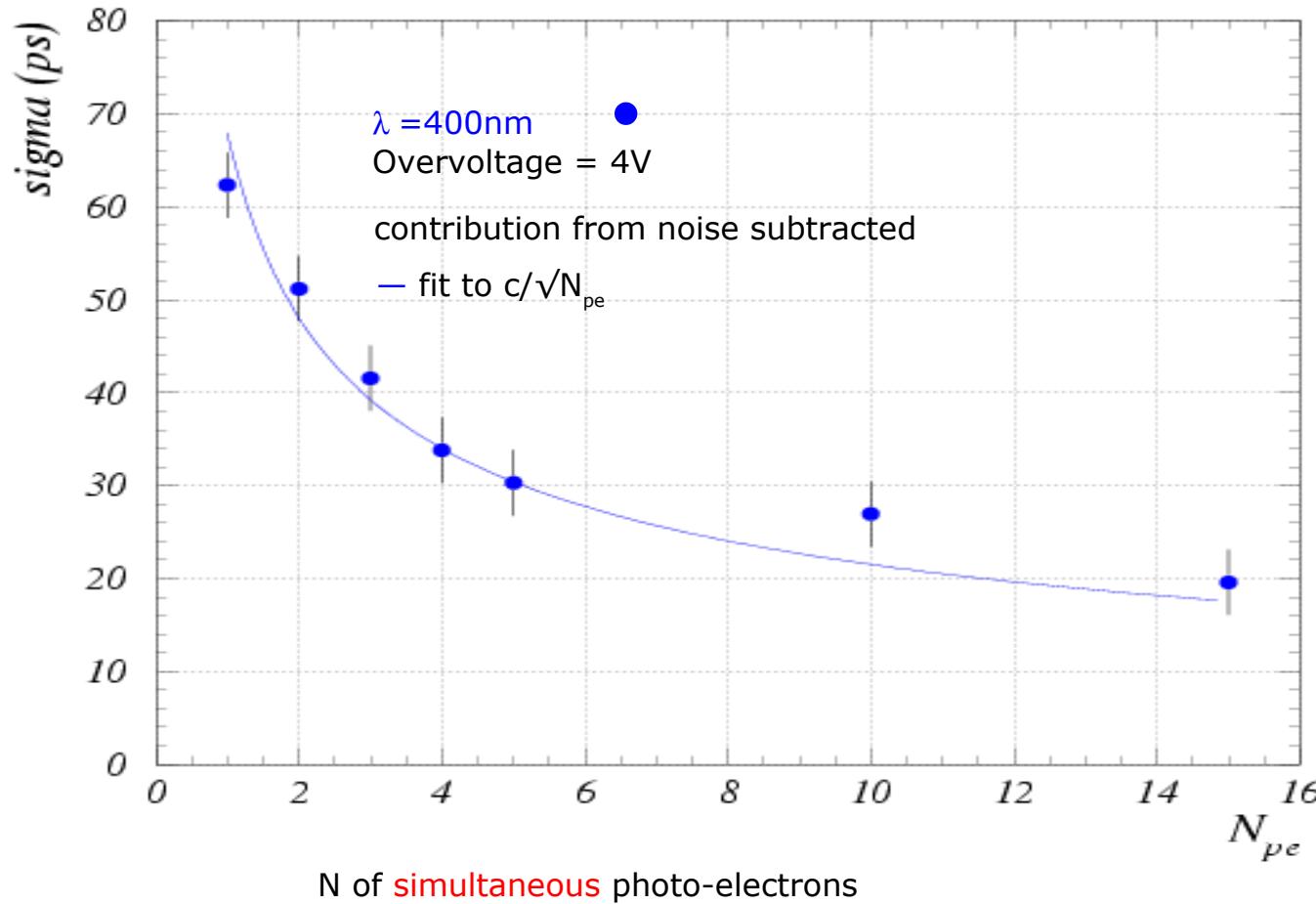
2) dead space effects worsen timing performances (the more at small k)
Important for devices with **small w**



Many photons (simultaneous)

Dependence of SiPM timing on the number of simultaneous photons

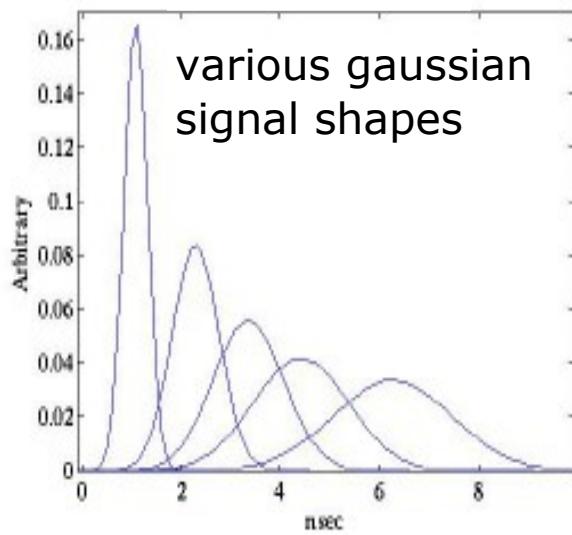
Poisson statistics: $\sigma_t \propto 1/\sqrt{N_{pe}}$



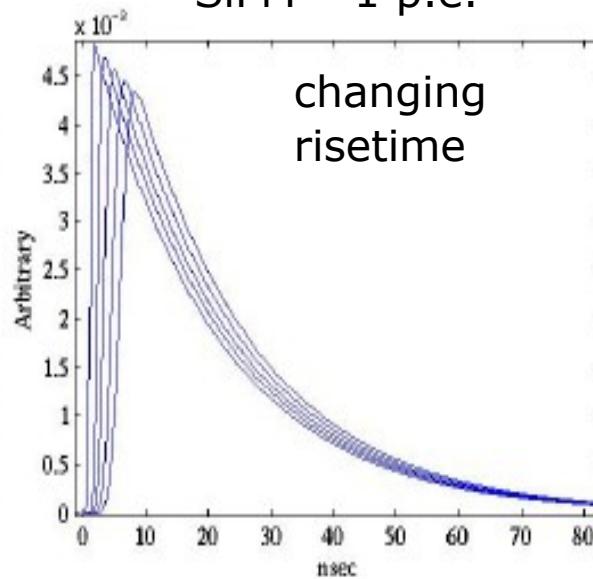
Signal shape for timing - many photons

Single p.e. signal slow falling-time component $\tau_{\text{fall}} = R_q (C_d + C_s)$
strongly affects multi-photon signal risetime

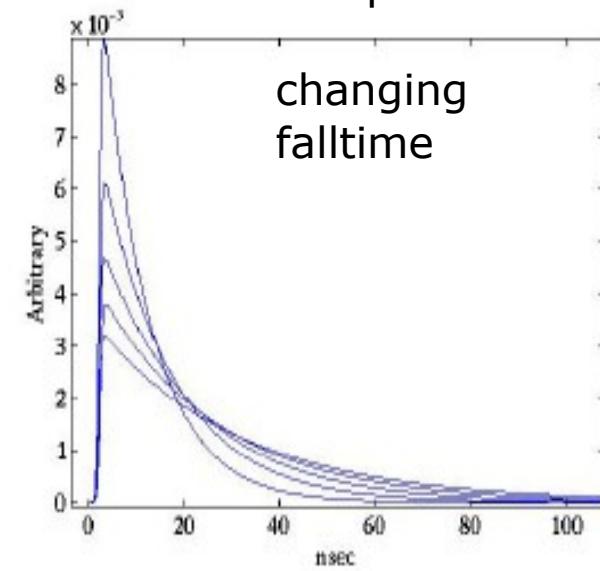
PMT - 1 p.e.



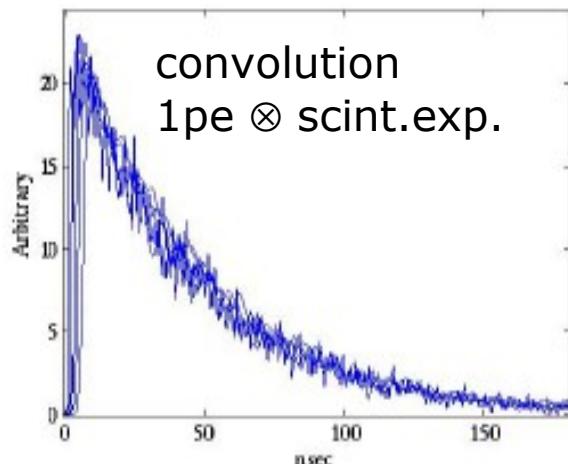
SiPM - 1 p.e.



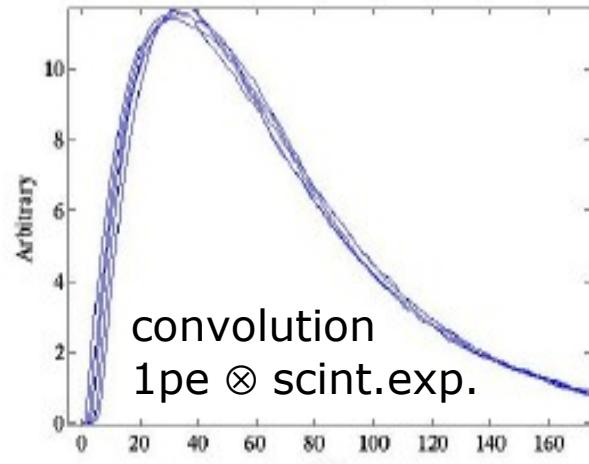
SiPM - 1 p.e.



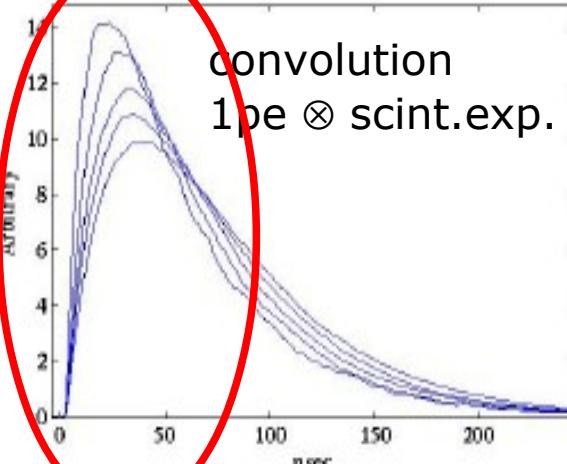
PMT - 511keV in LYSO



SiPM - 511keV in LYSO



SiPM - 511keV in LYSO



convolution

Optimizing shape for timing - many photons

→ peak height ratio

$$\frac{V_{fast}^{max}}{V_{slow}^{max}} \sim \frac{C_q^2 R_q}{C_d C_{tot} R_{load}}$$

Enhancing C_q and R_q does improve timing performances

FBK devices type:

- Active area: $4 \times 4 \text{ mm}^2$;
- Cell size: $67 \times 67 \mu\text{m}^2$;
- Fill factor: 60%;
- $C_Q + C_D$: about 180 fF ;
- R_Q : $1.1 \text{ M}\Omega$;
- Dark noise rate:
 $\sim 100 \text{ MHz}$ at $DV > 4 \text{ V}$

C.Piemonte et al IEEE TNS (2011)

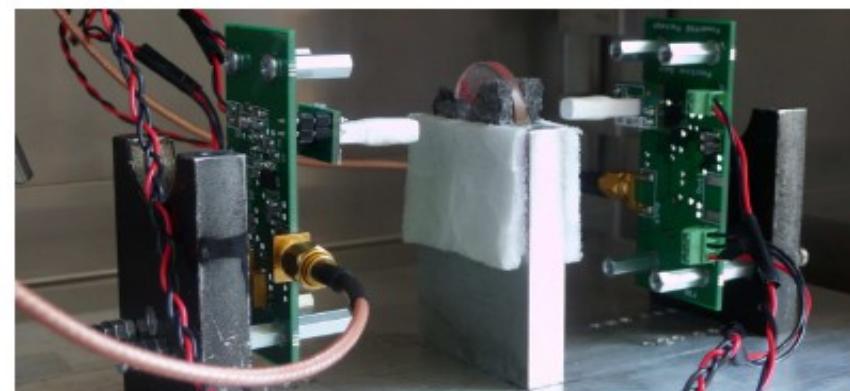
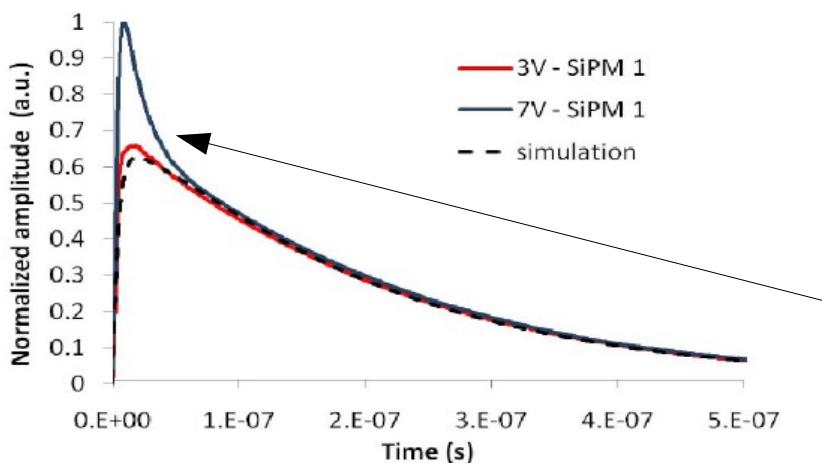


Fig. 2. Test set-up consists of two similar gamma ray detectors (LYSO crystal + SiPM) in coincidence. A ^{22}Na source (disc in the middle) was used to generate two opposite 511keV photons in coincidence.



- Signal rise-time $< 5 \text{ ns}$
 - CRT $\sim 320 \text{ ps}$ (*) FWHM triggering at 5% height
- Both are much better than for different structures with high C_{tot} and/or lower C_q , R_q (risetime up to several $\times 10 \text{ ns}$, CRT $> 400 \text{ ps}$)

??? peak shape is not scaling with ΔV
(**non linearity** in the F.Corsi et al electrical model)
Can be corrected → energy resol. $\sim 11\%$

(*) $\sim 40\%$ from light propagation in crystals



Radiation damage

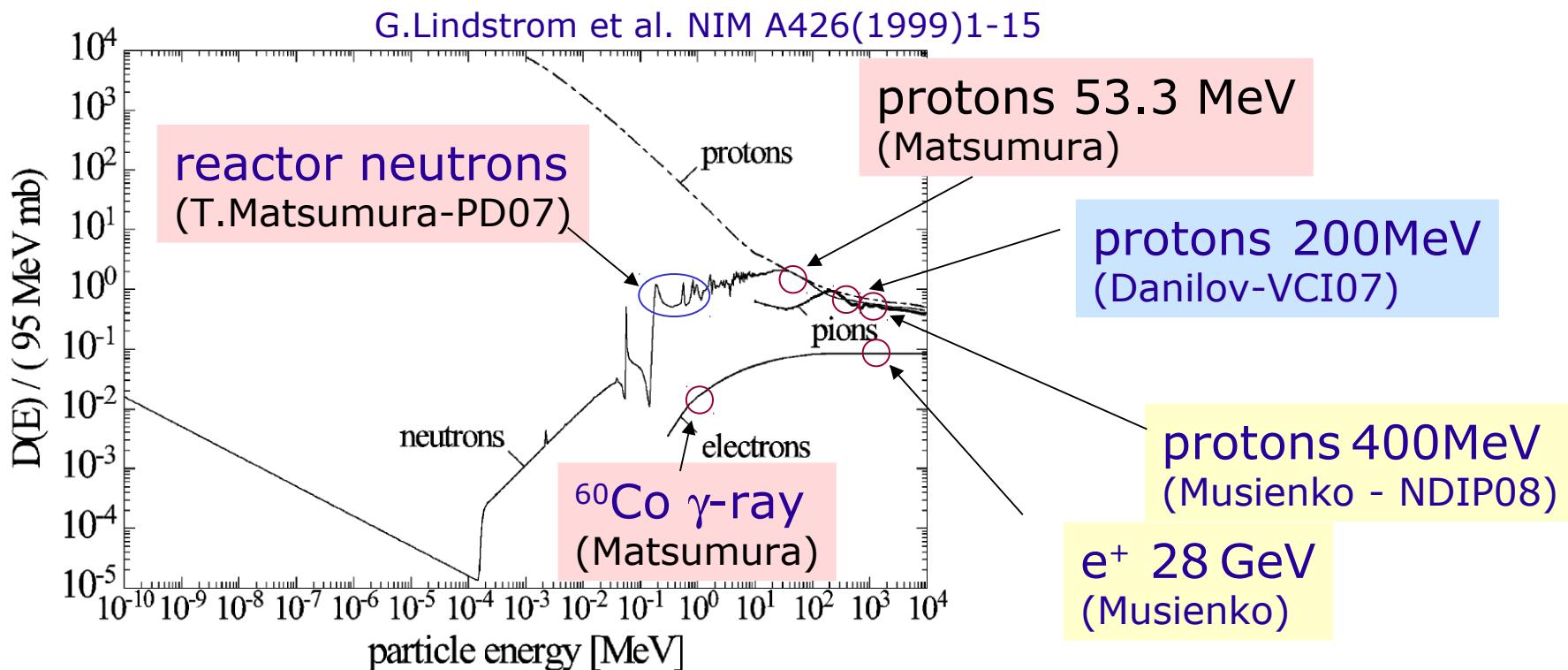
Note:

- small cells smaller charge flow (small gain, high dynamic range)
- small epi-layered width

Radiation damage: two types

- Bulk damage due to Non Ionizing Energy Loss (NIEL) ← neutrons, protons
- Surface damage due to Ionizing Energy Loss (IEL) ← γ rays
(accumulation of charge in the oxide (SiO_2) and the Si/SiO_2 interface)

Assumption: damage scales linearly with the amount of Non Ionizing Energy Loss (NIEL hypothesis)



Examples of radiation tolerances for HEP and space physics
ATLAS inner detector ... 3×10^{14} hadrons/cm 2 /10 year
 $\sim 10^4$ hadrons/mm 2 /s

General satellites ... ~ 10 Gy/year

Expectations:
protons / γ -ray ~ 100
protons / neutrons $\sim 2 \sim 10$

Radiation damage: effects on SiPM

1) Increase of dark count rate due to introduction of generation centers

Increase (ΔR_{DC}) of the dark rate:

$$\Delta R_{DC} \sim P_{01} \alpha \Phi_{eq} Vol_{eff} / q_e$$

where $\alpha \sim 3 \times 10^{-17} \text{ A/cm}$ is a typical value of the radiation damage parameter for low E hadrons

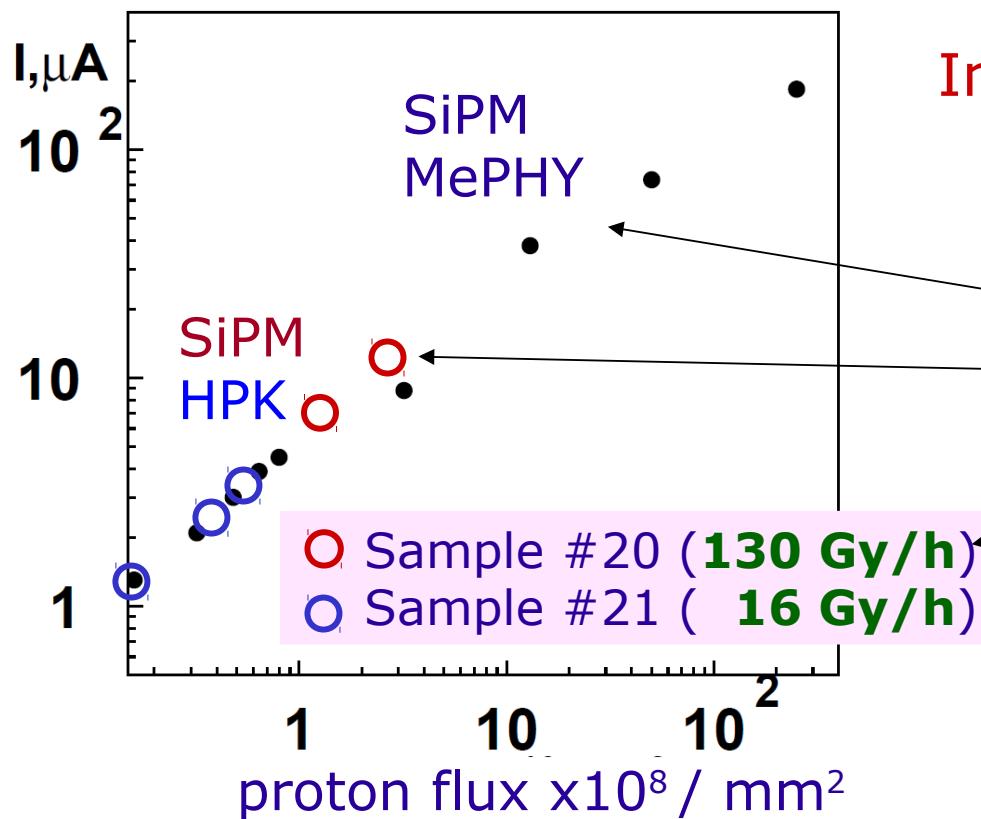
and $Vol_{eff} \sim \text{Area}_{SiPM} \times \epsilon_{geom} \times W_{epi}$

NOTE:

The effect is the same as in normal junctions:

- independent of the substrate type
- dependent on particle type and energy (NIEL)
- proportional to fluence

2) Increase of after-pulse rate due to introduction of trapping centers → loss of single cell resolution → no photon counting capability



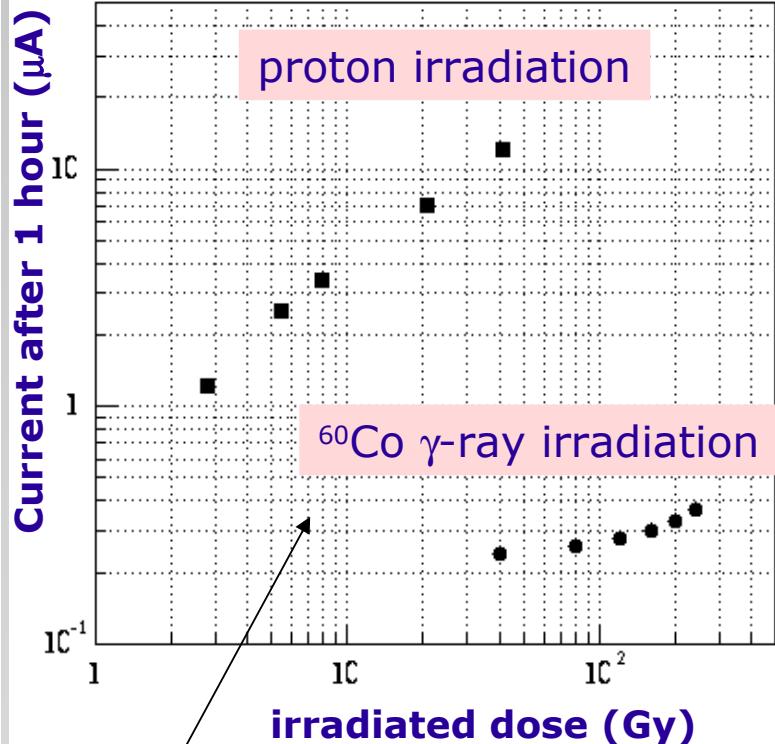
- 1) no dependence on the device
similar effects found for SiPM from MePHY (Danilov) and HPK (Matsumura)
(normaliz. to active volume)
- 2) no dependence on dose-rate
HPK (Matsumura)
- 3) n similar damage than p
- 4) p $\times 10^{1-10^2}$ more damage than γ

Damage comparison

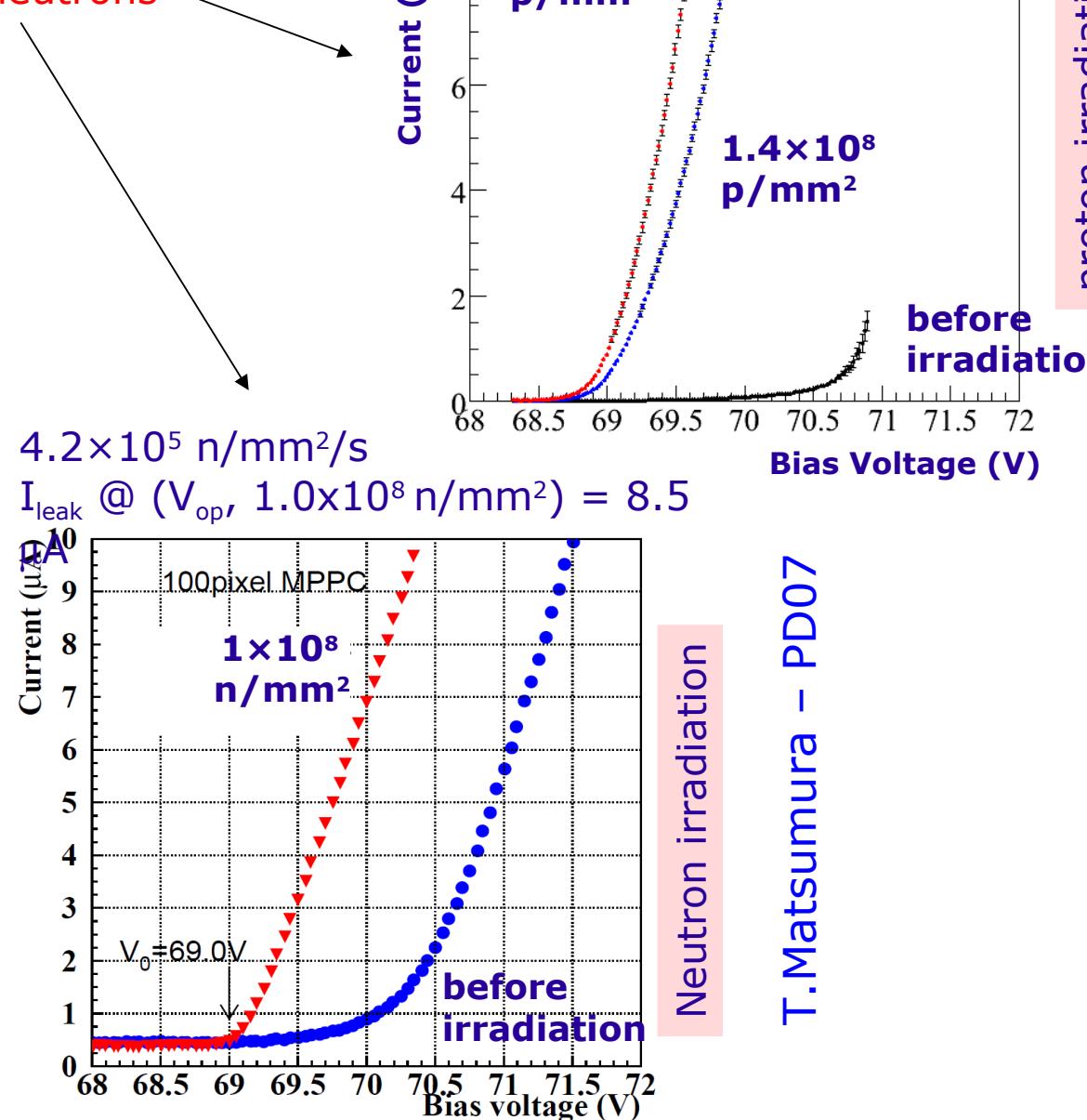
$2.3 \times 10^5 \text{ p/mm}^2/\text{s}$ (130 Gy/h)
 $I_{\text{leak}} @ (V_{\text{op}}, 1.4 \times 10^8 \text{ p/mm}^2) = 6.7 \mu\text{A}$

Damage effect ...
almost the same for
protons and neutrons

HPK devices
T. Matsumura - PD07



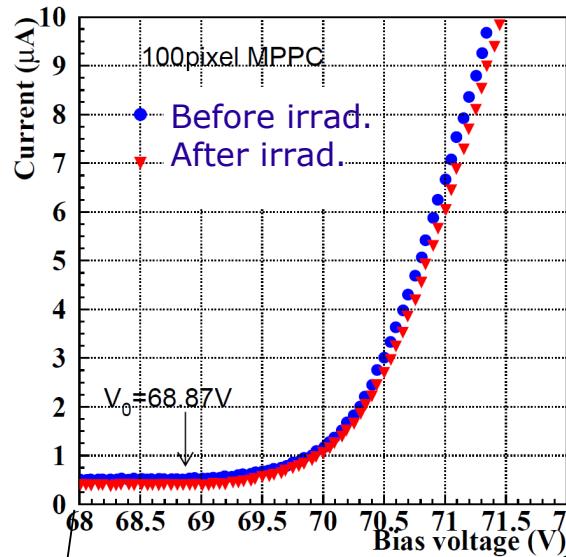
Damage effect ...
1~2 orders larger with protons
than γ-ray irradiation



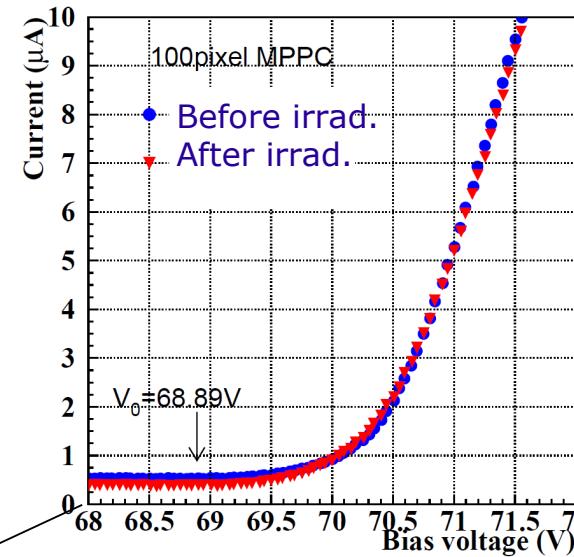
proton irradiation

Radiation damage: neutrons (0.1 -1 MeV)

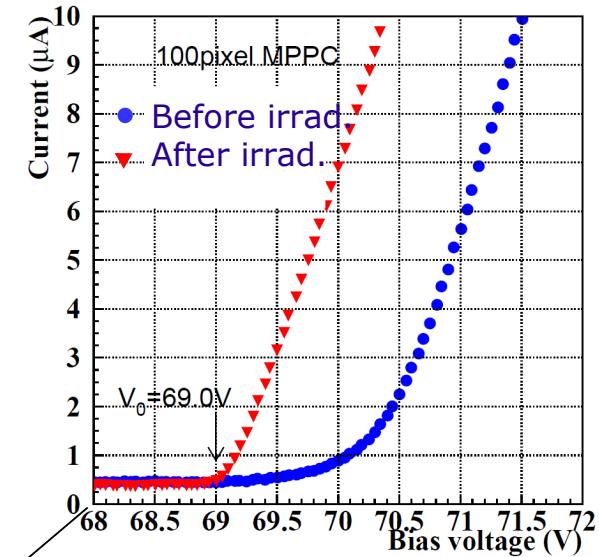
$8.3 \times 10^4 \text{ n/mm}^2$



$3.3 \times 10^5 \text{ n/mm}^2$



$1.0 \times 10^8 \text{ n/mm}^2$



10^5 n/mm^2 10^6 n/mm^2

10^7 n/mm^2

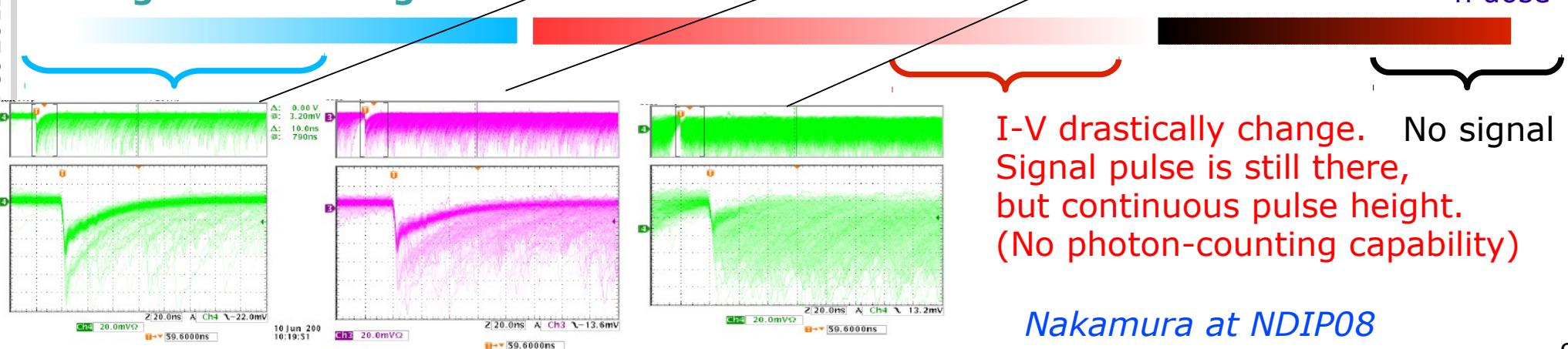
10^8 n/mm^2

10^9 n/mm^2

10^{10} n/mm^2

No significant change

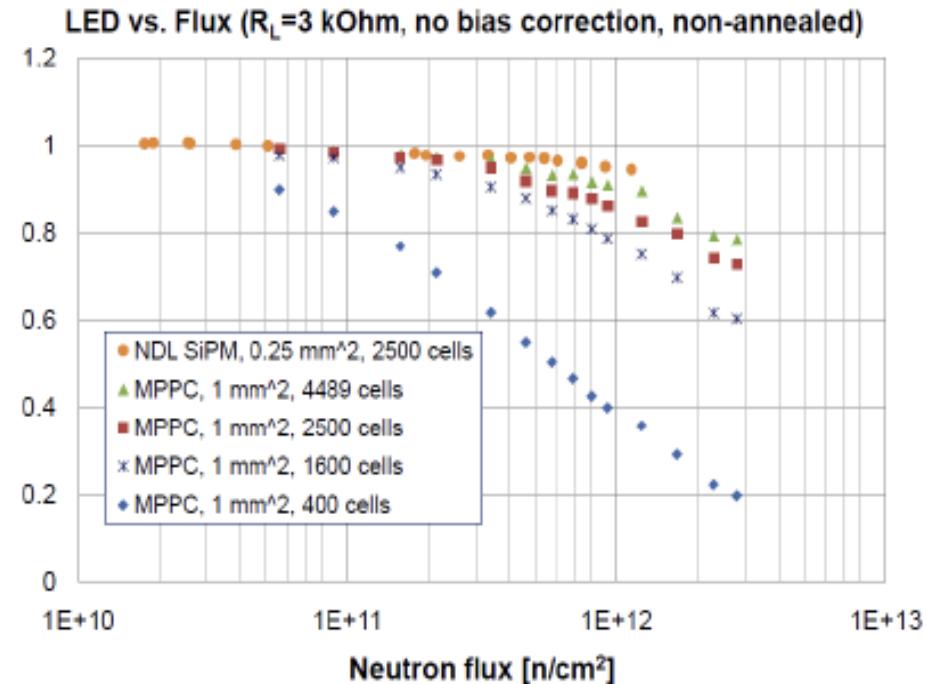
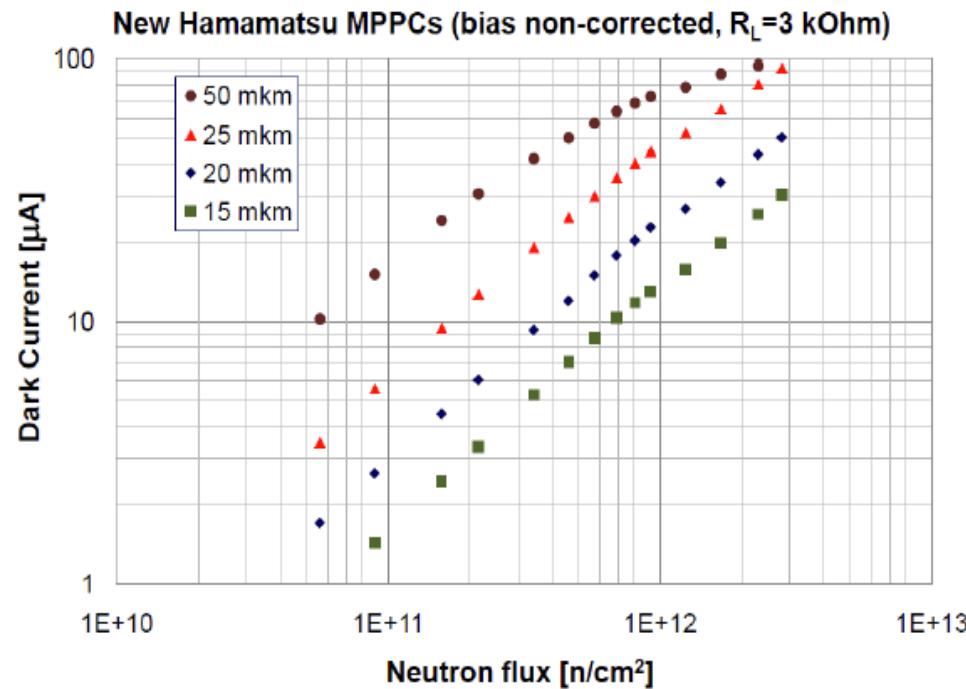
n dose



Nakamura at NDIP08

T. Matsumura - PD07

Radiation damage: neutrons 1 MeV E_{eq}



- No change of V_{bd} (within 50mV accuracy)
- No change of R_q (within 5% accuracy)
- I_{dark} and DCR significantly increase

SiPMs with high cell density and fast recovery time can operate up to $3 \times 10^{12} \text{ n/cm}^2$ ($\delta G < 25\%$)

Y.Musienko at SiPM workshop CERN 2011