

Ruído Browniano

27 de maio de 2018

```
In [1]: from scipy.stats import moment
        from scipy.stats import kurtosis, skew, scoreatpercentile
        from scipy.stats import norm, lognorm, beta
        from scipy.optimize import minimize

        from numpy import zeros, fromiter, savetxt, loadtxt
        from IPython.display import Image

        import subprocess

        import numpy as np
        import pandas as pd
        import matplotlib.pyplot as plt
        import seaborn as sns

        import auxiliar_matcomp as aux

        ##matplotlib inline

        size = 2**12
        t = fromiter((i for i in range(0,size)), int, size)
```

1 Série Completa

1.1 Gerando série temporal e plotando resultado

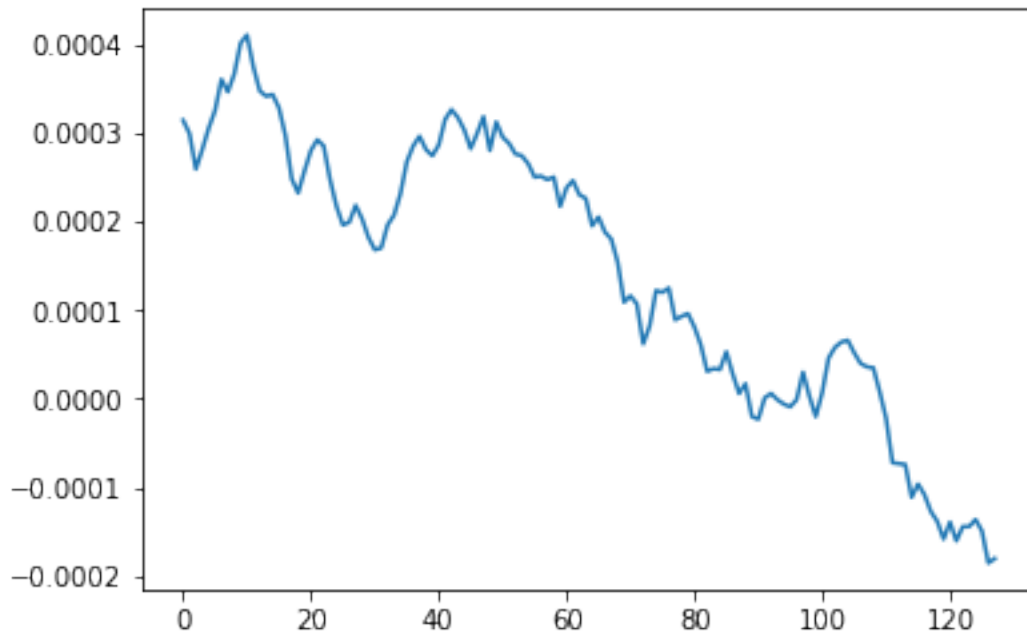
```
In [2]: name = "A.ex:1.3.d"

        A = loadtxt("noise_equals_2.txt")

        savetxt(name + ".txt", A)

        save_A = A

In [3]: num_points = 128
        plt.plot(t[0:num_points], A[0:num_points])
        plt.show()
```



1.2 Calculando os momentos do ensemble

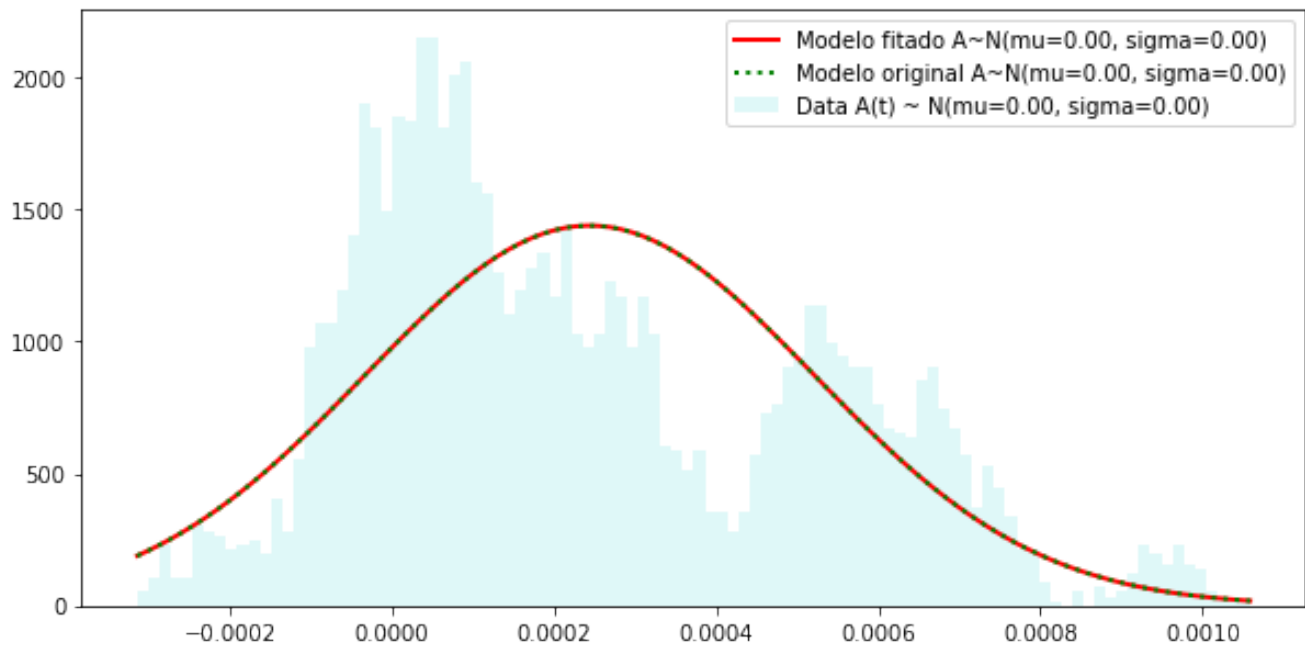
```
In [4]: A_mean, A_var, A_skew, A_kurtosis = aux.calcMoments(A)
```

```
print("mean : ", A_mean)
print("var  : ", A_var)
print("skew : ", A_skew)
print("kurt : ", A_kurtosis)
```

```
mean : 0.000244137451172
var  : 7.68228788123e-08
skew : 0.552554516864
kurt : -0.526957500598
```

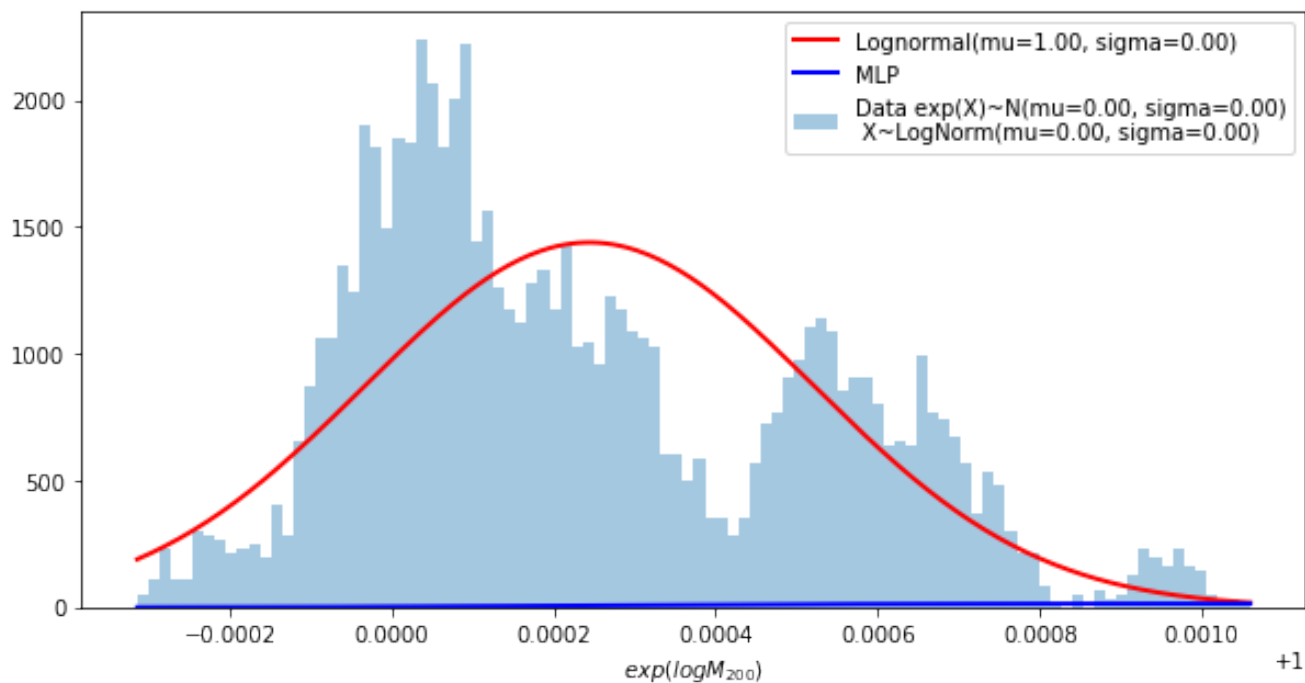
1.3 Fitando uma distribuição normal

```
In [5]: aux.fitting_normal_distribution(A)
```



1.4 Fitando uma distribuição lognormal

In [6]: `aux.fitting_lognormal_and_mlp_distribution(A)`

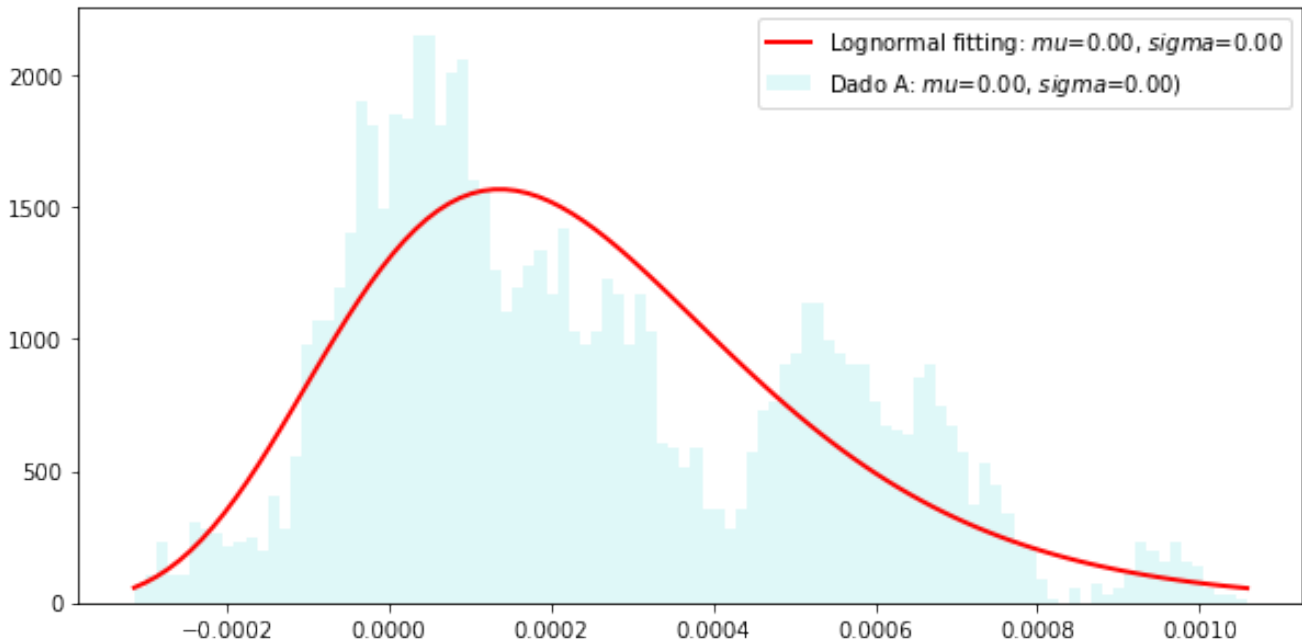


1.5 Fitando uma distribuição lognormal (utilizando minha implementação)

In [7]: `aux.fitting_lognormal_distribution(A)`

parametros de fitting: (0.27572050283128752, -0.00075154414848649723, 0.00095853280766207839)

| | Fitado | Original |
|--------|------------------------|---------------------|
| mean : | 0.00024412466715190866 | 0.000244137451172 |
| var : | 7.830336620534376e-08 | 7.68228788123e-08 |
| skew : | 0.8653325455765708 | 0.5525545168644652 |
| kurt : | 1.3603550915502023 | -0.5269575005976916 |



1.6 Plotando dados no espaço de Cullen-Frey

```
In [8]: command = 'Rscript'
path_script = 'cullen_frey_script.R'

# define arguments
args = [name,]

# build subprocess command
cmd = [command, path_script] + args

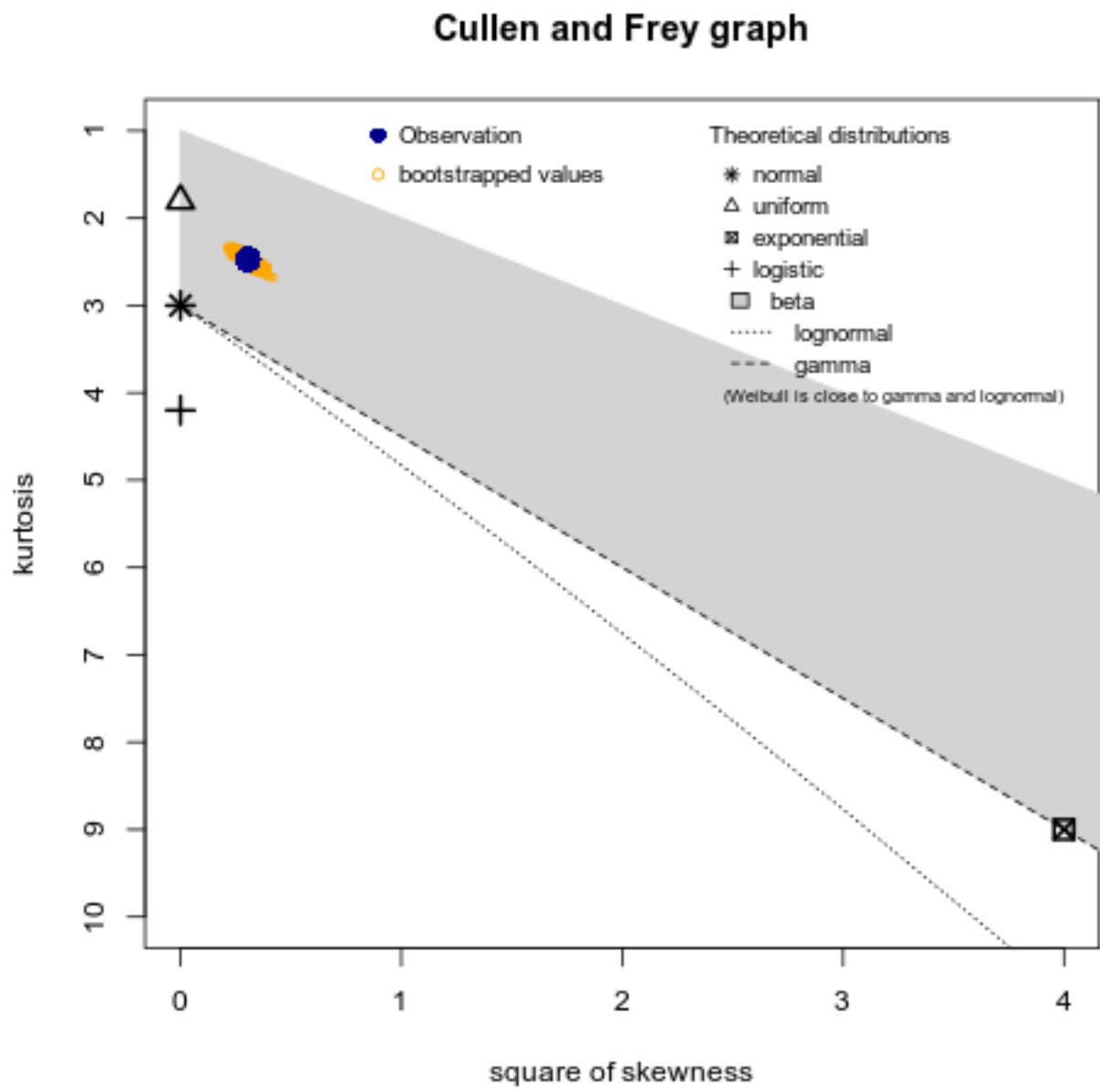
x = subprocess.check_output(cmd, universal_newlines=True)
print(x)

Image(name+'.png')
```

summary statistics

```
-----
min: -0.000314    max:  0.001059
median:  0.0001815
mean:  0.0002441375
estimated sd:  0.0002772032
estimated skewness:  0.552757
estimated kurtosis:  2.473865
```

Out [8] :

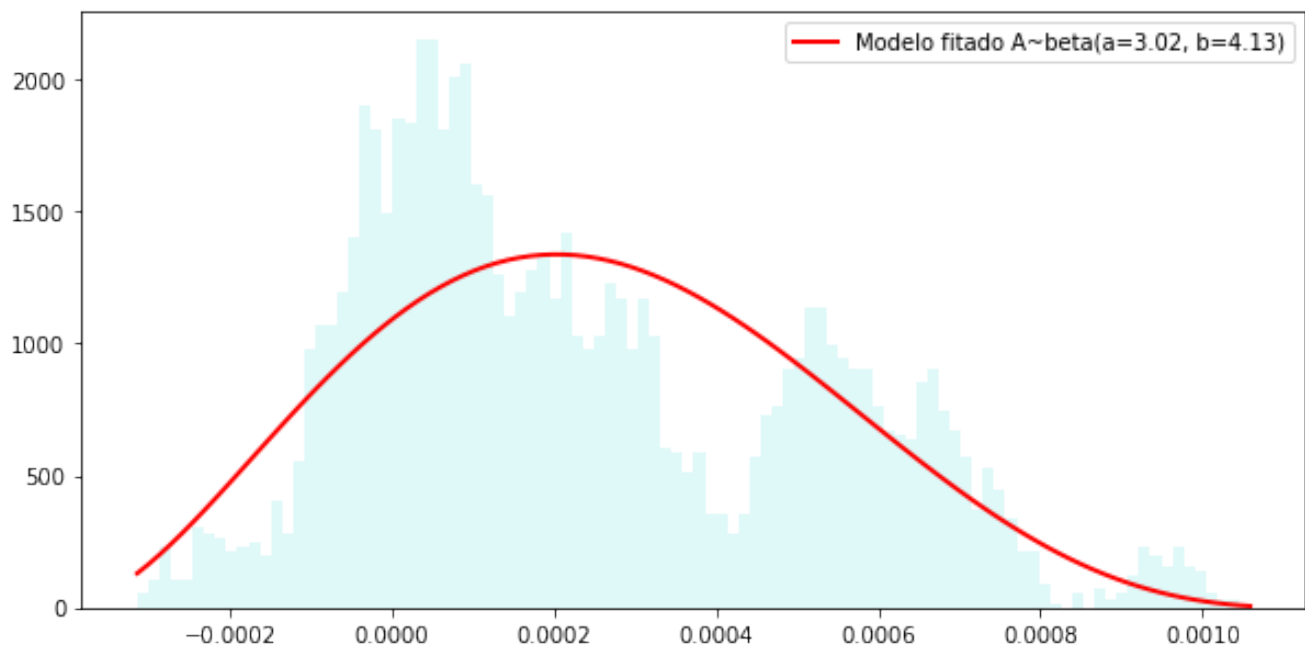


1.7 Fitando melhor distribuição segundo método de Cullen-Frey

```
In [9]: aux.fitting_beta_distribution(A)

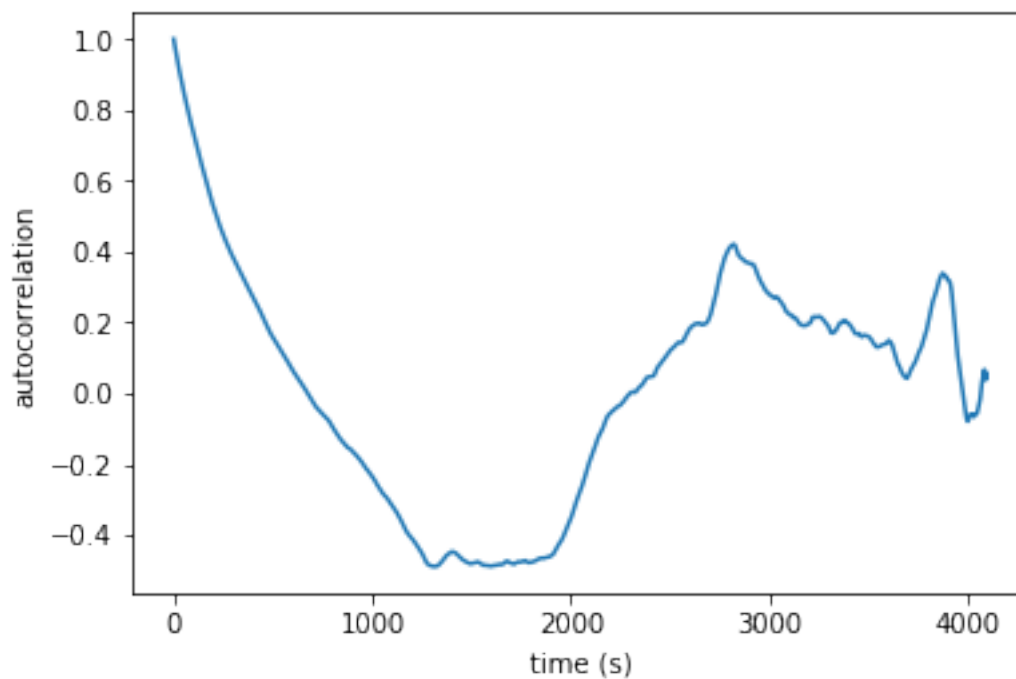
parametros de fitting: (3.0229491910543635, 4.1328353893033425, -0.00041399999999999998, 0.0015730000000000001)

    Fitado      Original
mean : 0.00025051121105308834    0.000244137451172
var  : 7.402120291715554e-08      7.68228788123e-08
skew : 0.19588729808864974        0.5525545168644652
kurt : -0.5389060385985043        -0.5269575005976916
```



1.8 Calculando autocorrelação

In [10]: `aux.plot_estimated_autocorrelation(t, A, 0, len(A))`



1.9 Plotando DFA e PSD

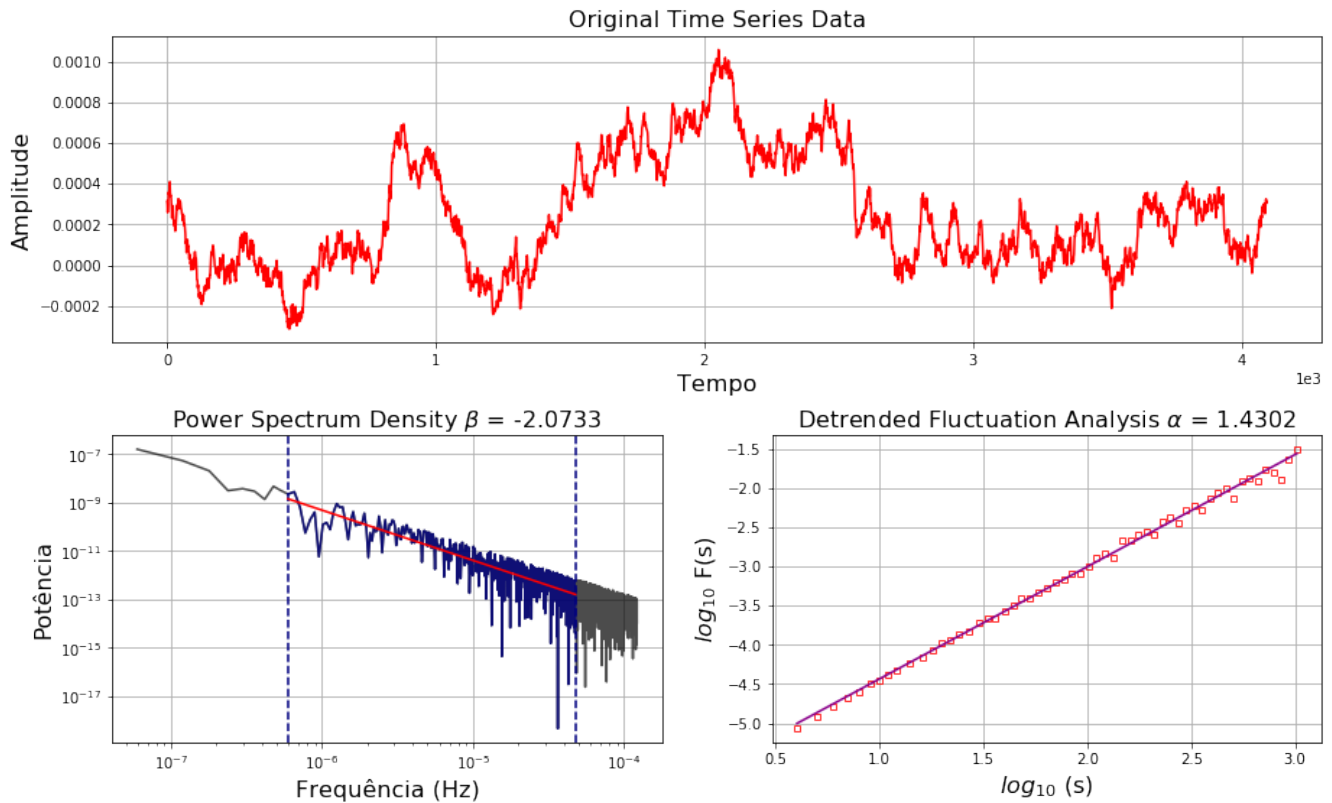
In [11]: `aux.plot_psd_dfa(A, 'Ruído Browniano')`

Original time series data (4096 points):

First 10 points: [0.000314 0.000299 0.000259 0.000281 0.000305 0.000325 0.00036
0.000346 0.000366 0.000401]

1. Plotting time series data...
2. Plotting Power Spectrum Density...
3. Plotting Detrended Fluctuation Analysis...

Ruído Browniano



2 Análise dos primeiros 1024 pontos

```
In [12]: A = save_A[1024:]  
         name = "A.ex:1.3.d"  
         savetxt(name + ".txt", A)
```

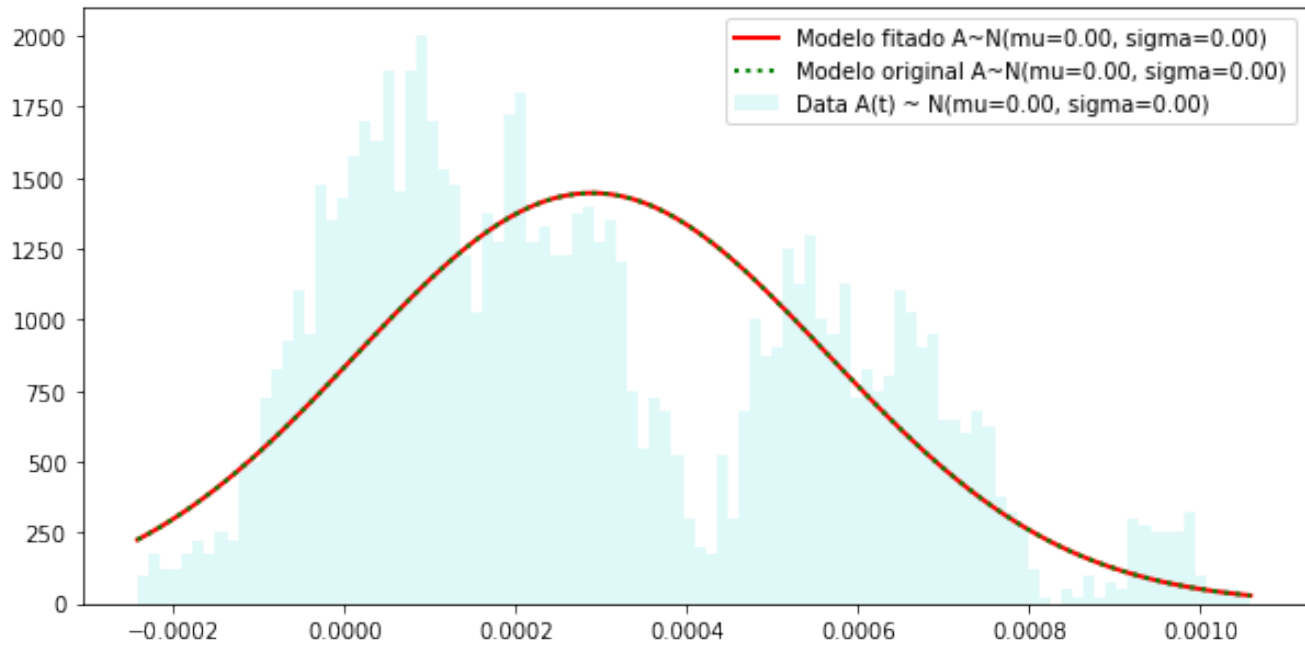
2.1 Calculando os momentos do ensemble

```
In [13]: A_mean, A_var, A_skew, A_kurtosis = aux.calcMoments(A)  
  
print("mean : ", A_mean)  
print("var : ", A_var)  
print("skew : ", A_skew)  
print("kurt : ", A_kurtosis)
```

```
mean : 0.000289416015625
var : 7.60334102643e-08
skew : 0.492223906348
kurt : -0.656631729673
```

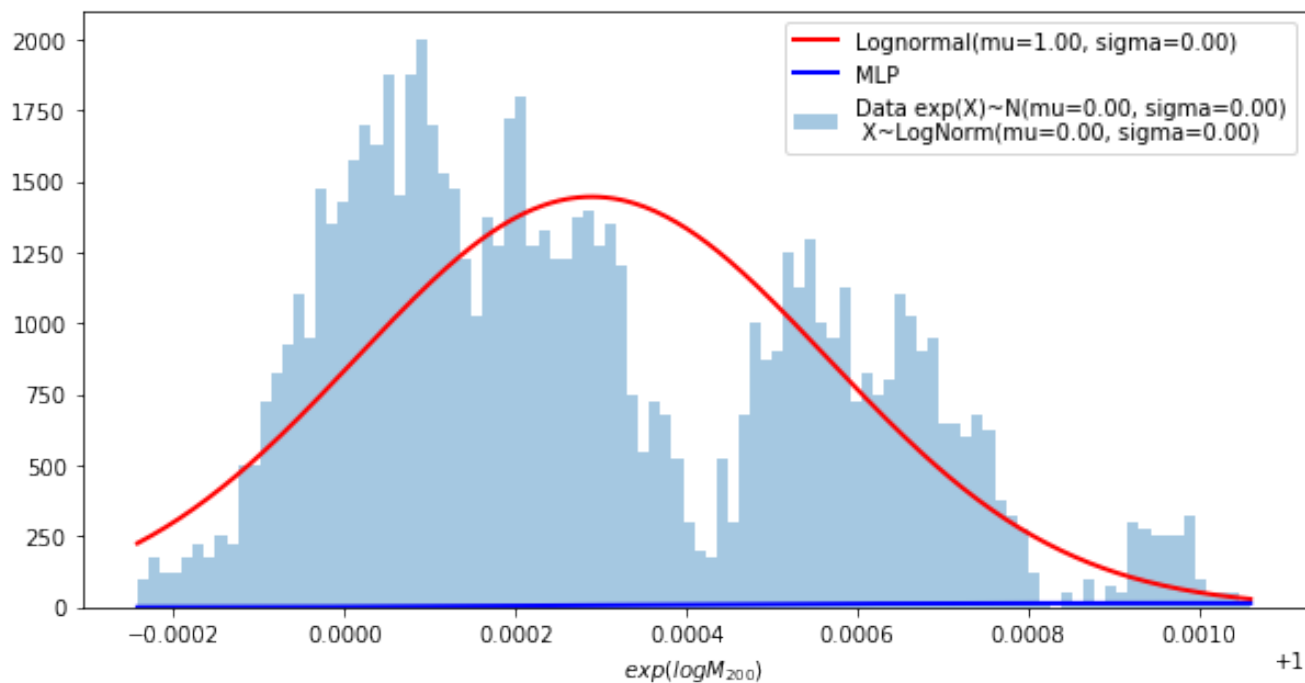
2.2 Fitando uma distribuição normal

```
In [14]: aux.fitting_normal_distribution(A)
```



2.3 Fitando uma distribuição lognormal

```
In [15]: aux.fitting_lognormal_and_mlp_distribution(A)
```

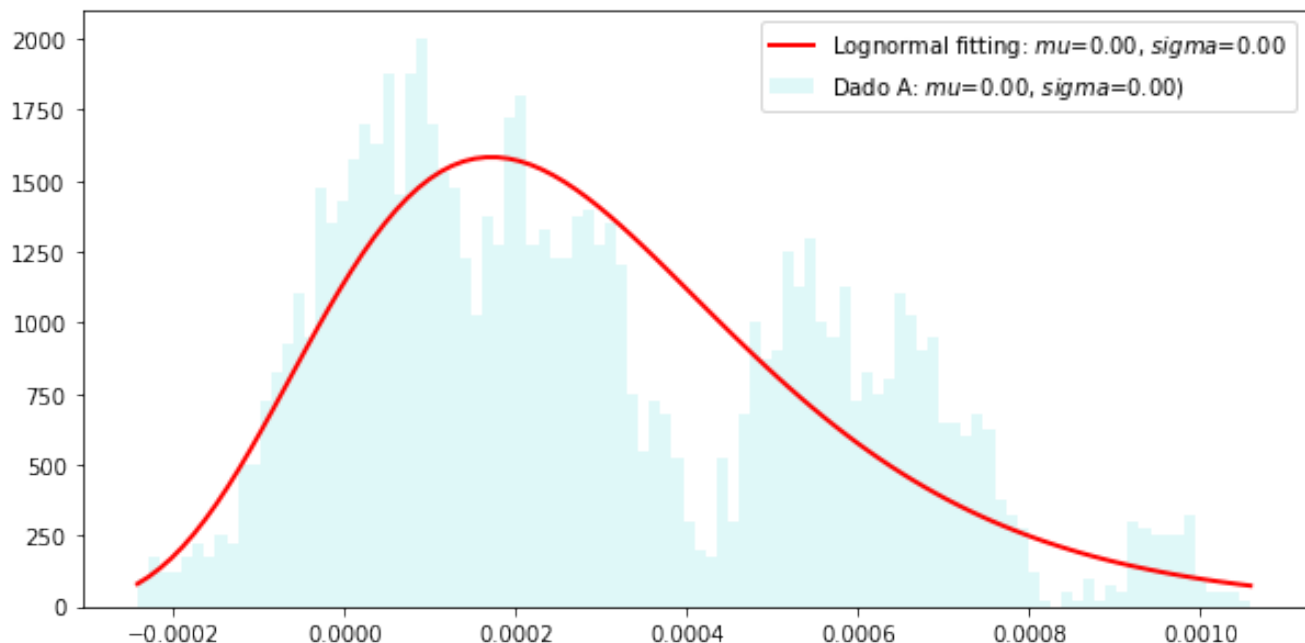



2.4 Fitando uma distribuição lognormal (utilizando minha implementação)

In [16]: `aux.fitting_lognormal_distribution(A)`

parametros de fitting: (0.30462333992505852, -0.00061761515411332894, 0.00086619852120198293)

| | Fitado | Original |
|--------|------------------------|---------------------|
| mean : | 0.00028971991823909156 | 0.000289416015625 |
| var : | 8.005119479313776e-08 | 7.60334102643e-08 |
| skew : | 0.9658077292738554 | 0.49222390634796254 |
| kurt : | 1.703226903562415 | -0.6566317296729003 |



2.5 Plotando dados no espaço de Cullen-Frey

```
In [17]: command = 'Rscript'
        path_script = 'cullen_frey_script.R'

        # define arguments
        args = [name,]

        # build subprocess command
        cmd = [command, path_script] + args

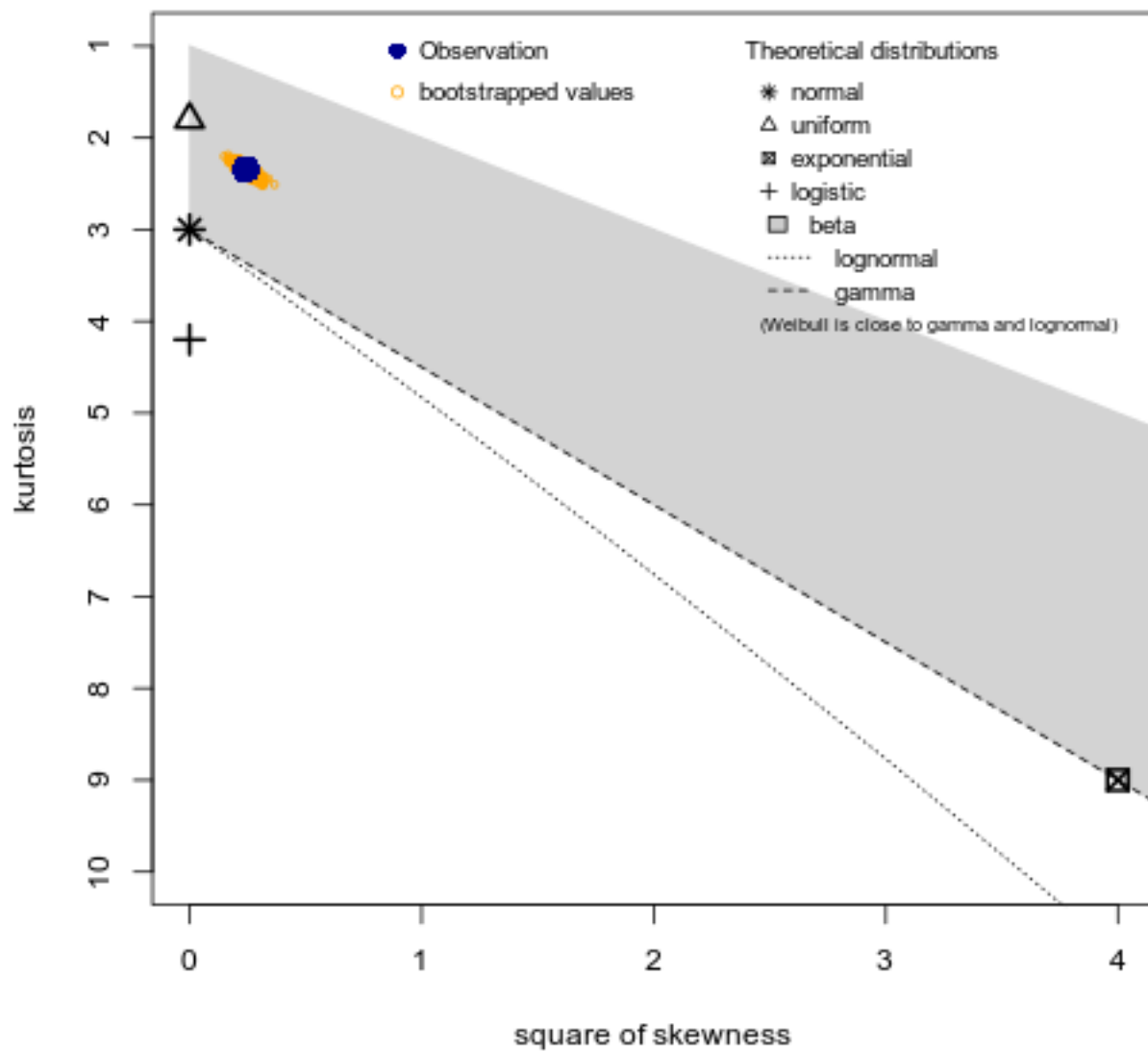
        x = subprocess.check_output(cmd, universal_newlines=True)
        print(x)

        Image(name+".png")

summary statistics
-----
min:  -0.000242   max:  0.001059
median:  0.000231
mean:  0.000289416
estimated sd:  0.0002757865
estimated skewness:  0.4924644
estimated kurtosis:  2.344254
```

Out[17]:

Cullen and Frey graph

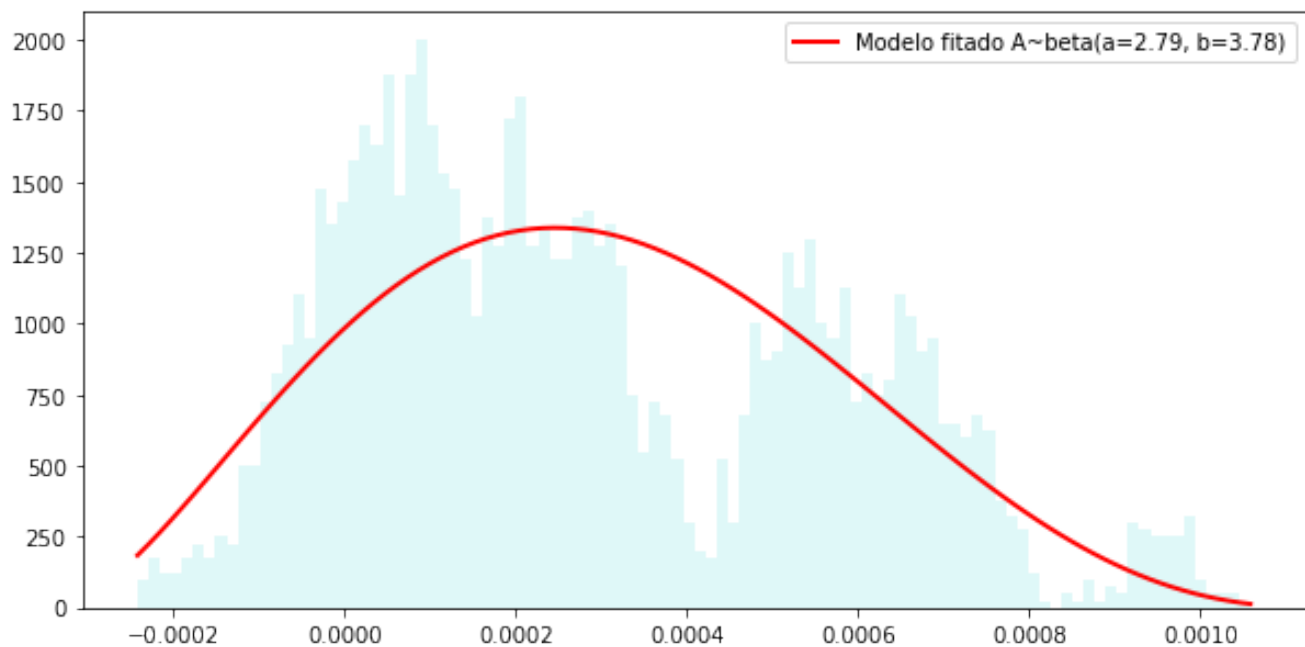


2.6 Fitando melhor distribuição segundo método de Cullen-Frey

In [18]: `aux.fitting_beta_distribution(A)`

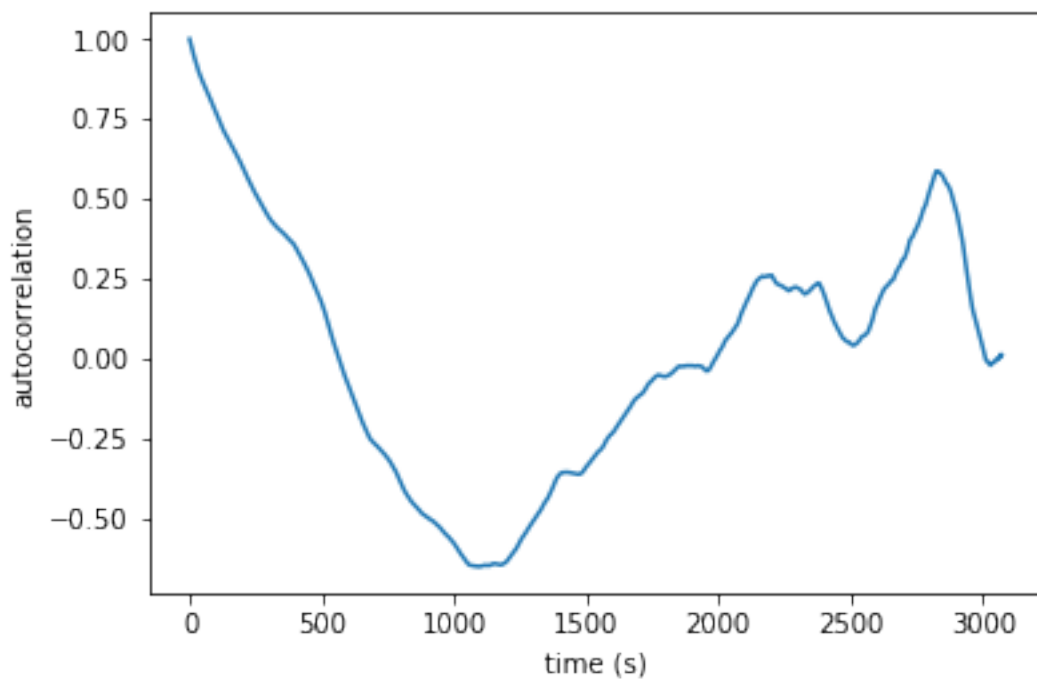
parametros de fitting: (2.7881563991506124, 3.7760423395852598, -0.00034200000000000002, 0.0015010000000000000)

| | Fitado | Original |
|--------|------------------------|---------------------|
| mean : | 0.00029555271918092746 | 0.000289416015625 |
| var : | 7.277613674222103e-08 | 7.60334102643e-08 |
| skew : | 0.19554852093283057 | 0.49222390634796254 |
| kurt : | -0.5759779443165691 | -0.6566317296729003 |



2.7 Calculando autocorrelação

In [19]: `aux.plot_estimated_autocorrelation(t, A, 0, len(A))`



2.8 Plotando DFA e PSD

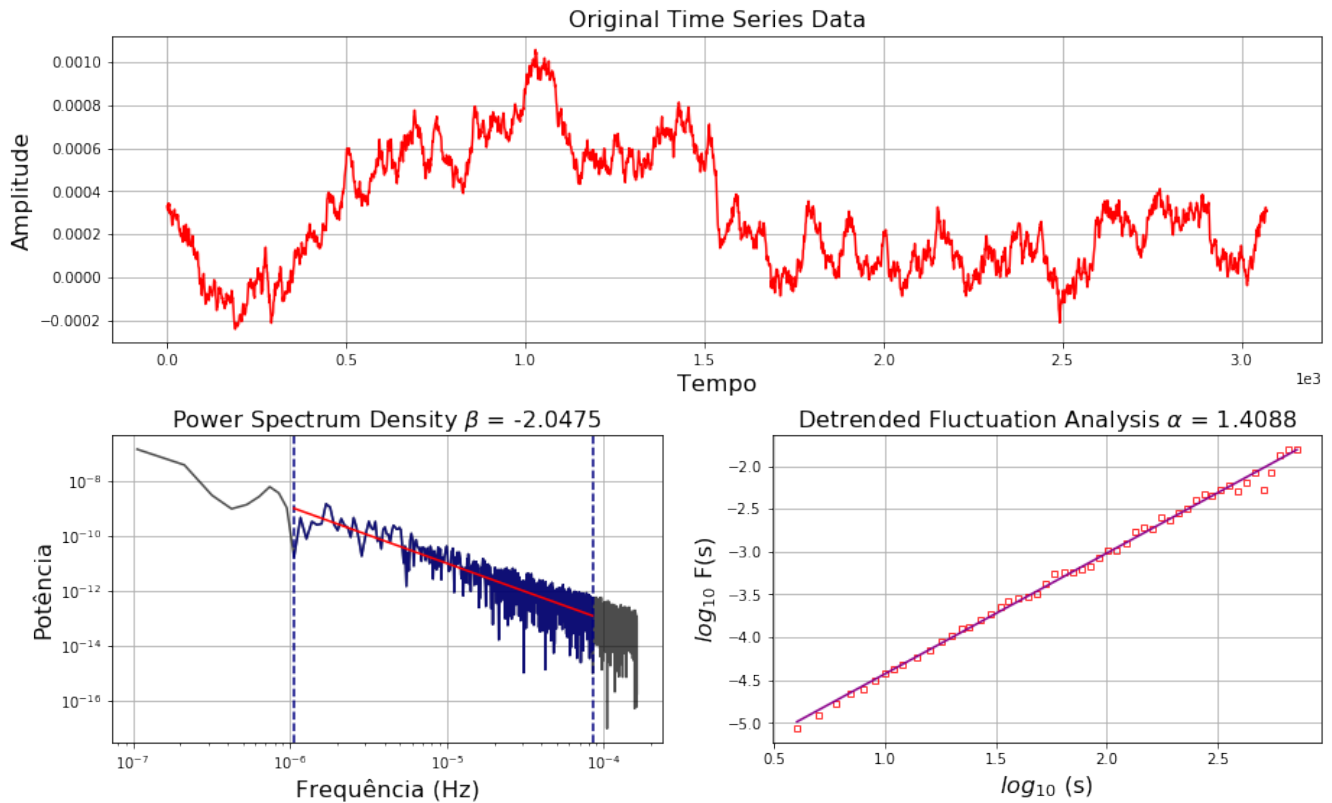
In [20]: `aux.plot_psd_dfa(A, 'Ruído Browniano, primeiros 1024 pontos')`

Original time series data (3072 points):

First 10 points: [0.000329 0.000318 0.00031 0.000343 0.000343 0.000331 0.000341
0.000313 0.000295 0.000311]

1. Plotting time series data...
2. Plotting Power Spectrum Density...
3. Plotting Detrended Fluctuation Analysis...

Ruído Browniano, primeiros 1024 pontos



3 Analise dos últimos 1024 pontos

```
In [21]: A = save_A[3*1024:4096]
        name = "A.ex:1.3.d"
        savetxt(name + ".txt", A)
```

```
In [22]: A.shape
```

```
Out[22]: (1024,)
```

3.1 Calculando os momentos do ensemble

```
In [23]: A_mean, A_var, A_skew, A_kurtosis = aux.calcMoments(A)

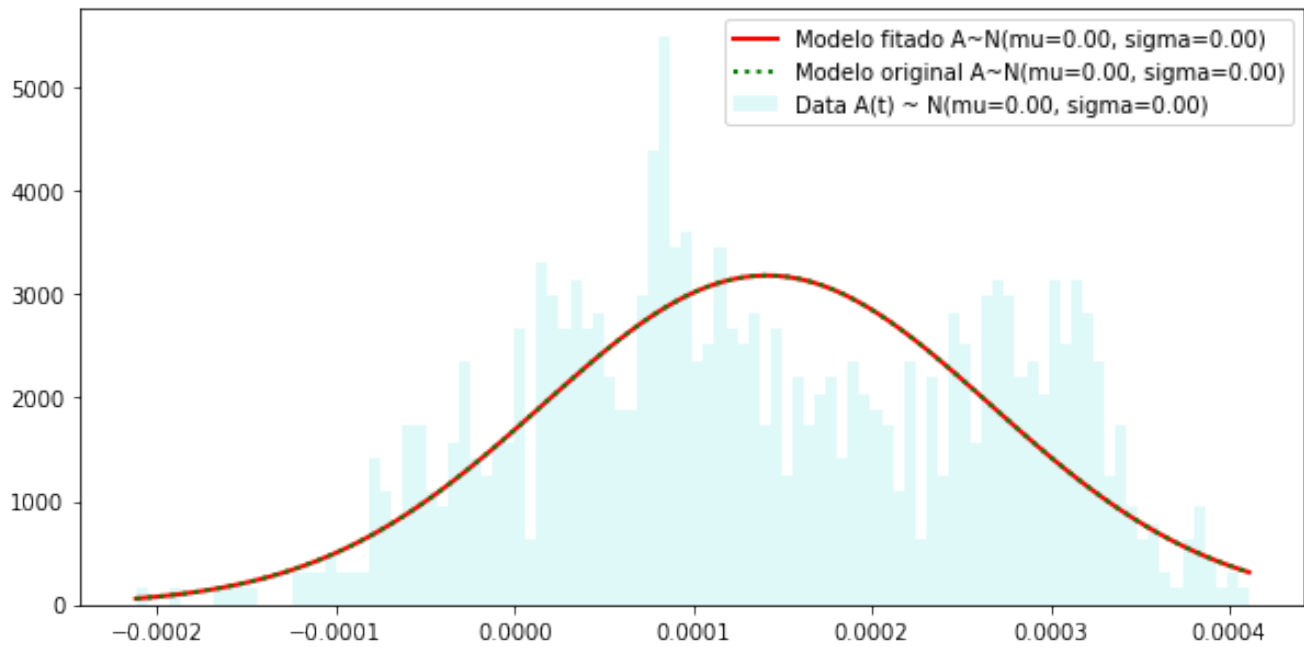
        print("mean : ", A_mean)
```

```
print("var : ", A_var)
print("skew : ", A_skew)
print("kurt : ", A_kurtosis)
```

```
mean : 0.000141081054688
var : 1.57486057348e-08
skew : 0.00889858728318
kurt : -0.905696021218
```

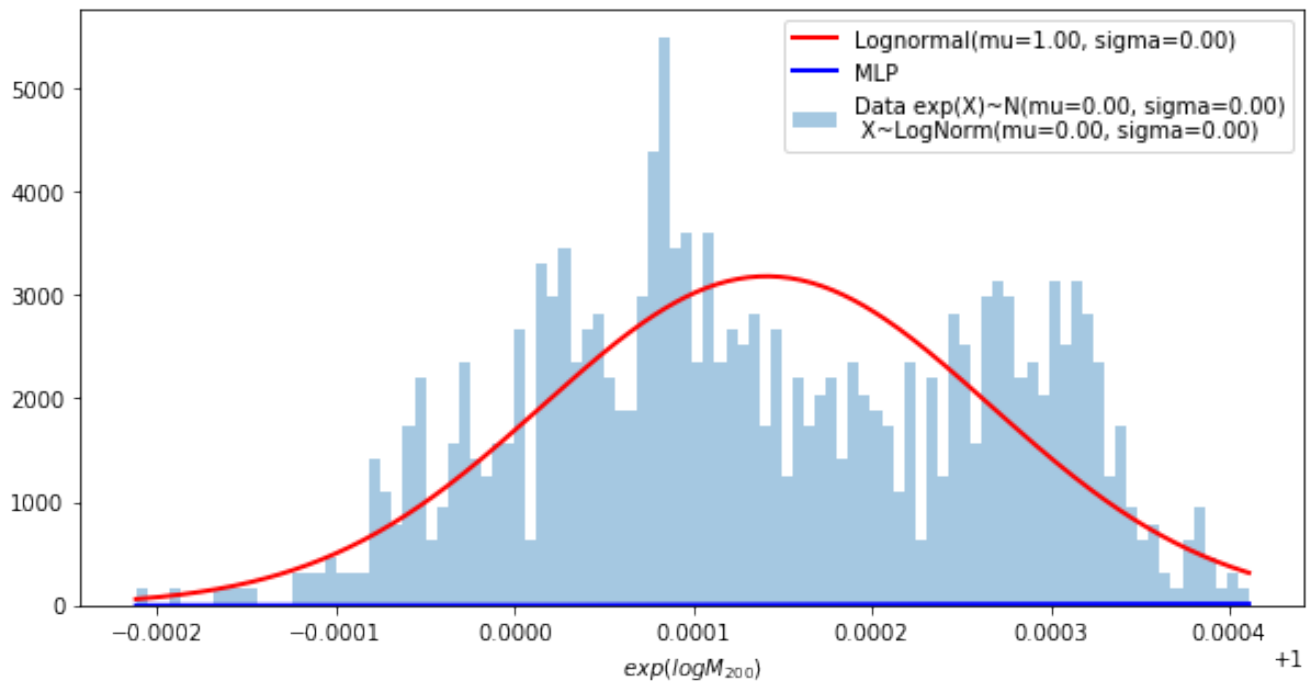
3.2 Fitando uma distribuição normal

```
In [24]: aux.fitting_normal_distribution(A)
```



3.3 Fitando uma distribuição lognormal

```
In [25]: aux.fitting_lognormal_and_mlp_distribution(A)
```

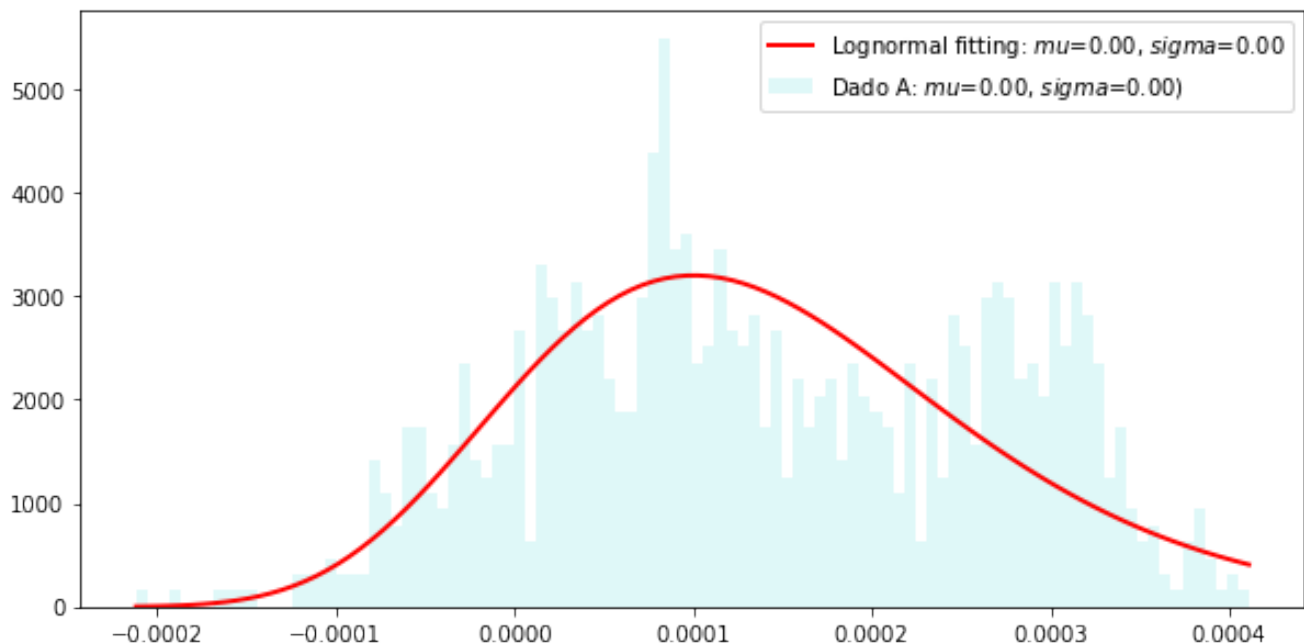


3.4 Fitando uma distribuição lognormal (utilizando minha implementação)

In [26]: `aux.fitting_lognormal_distribution(A)`

parametros de fitting: (0.21743451661782692, -0.00045984127487144457, 0.00058727444037858358)

| | Fitado | Original |
|--------|------------------------|----------------------|
| mean : | 0.00014148106232931304 | 0.000141081054688 |
| var : | 1.7505653642840885e-08 | 1.57486057348e-08 |
| skew : | 0.6707422453651557 | 0.008898587283178017 |
| kurt : | 0.8104548422392481 | -0.9056960212181342 |



3.5 Plotando dados no espaço de Cullen-Frey

```
In [27]: command = 'Rscript'
        path_script = 'cullen_frey_script.R'

        # define arguments
        args = [name,]

        # build subprocess command
        cmd = [command, path_script] + args

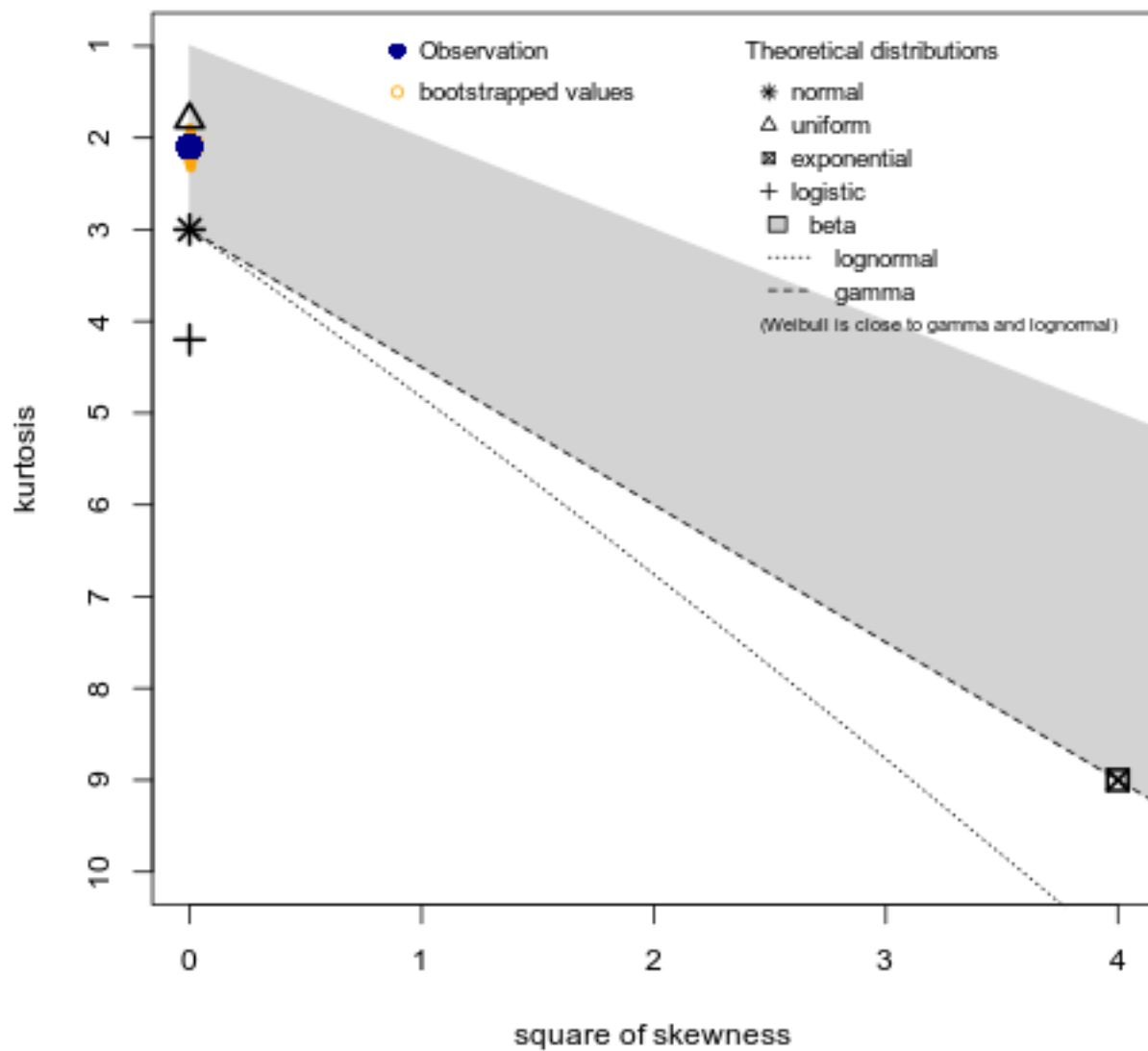
        x = subprocess.check_output(cmd, universal_newlines=True)
        print(x)

        Image(name+".png")

summary statistics
-----
min:  -0.000212    max:  0.000411
median:  0.000127
mean:  0.0001410811
estimated sd:  0.0001255548
estimated skewness:  0.008911647
estimated kurtosis:  2.095748
```

Out[27]:

Cullen and Frey graph

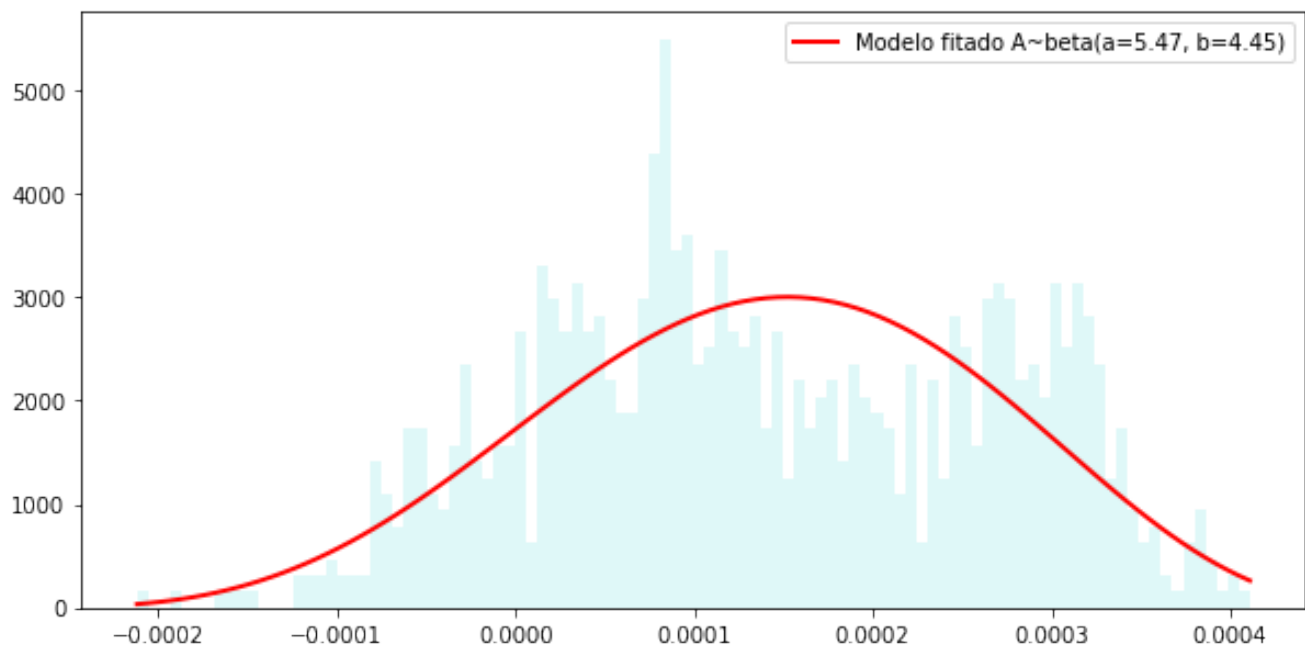


3.6 Fitando melhor distribuição segundo método de Cullen-Frey

In [28]: `aux.fitting_beta_distribution(A)`

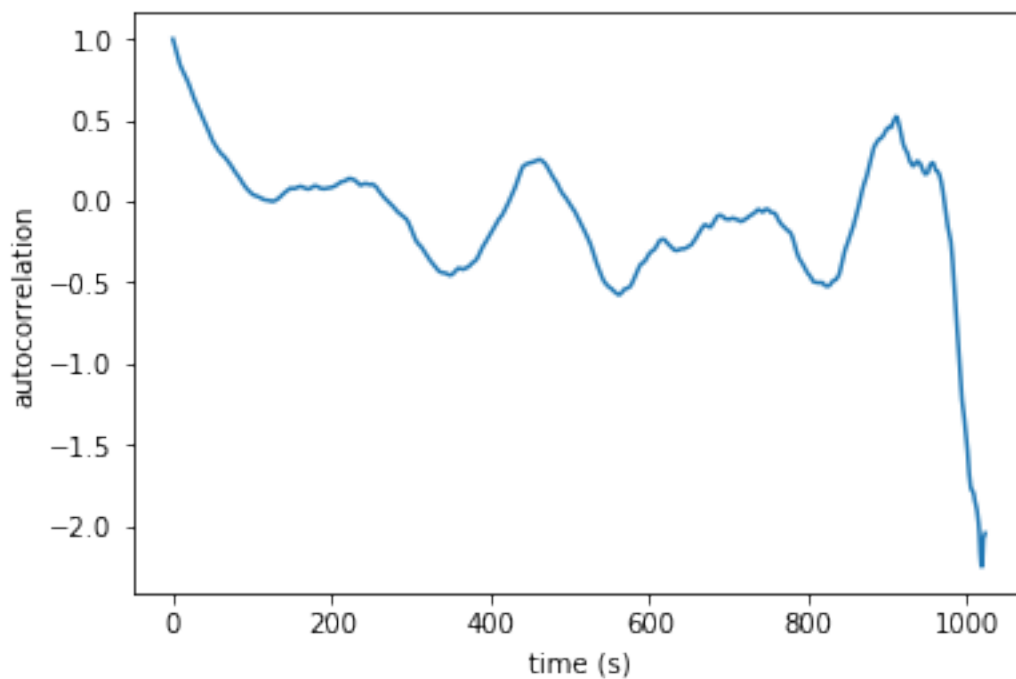
parametros de fitting: (5.4657271200783075, 4.4547102501875706, -0.0003119999999999999, 0.0008230000000000000)

| | Fitado | Original |
|--------|-----------------------|----------------------|
| mean : | 0.0001414370060444108 | 0.000141081054688 |
| var : | 1.534494744508124e-08 | 1.57486057348e-08 |
| skew : | -0.11360109578211047 | 0.008898587283178017 |
| kurt : | -0.446520983143211 | -0.9056960212181342 |



3.7 Calculando autocorrelação

In [29]: `aux.plot_estimated_autocorrelation(t, A, 0, len(A))`



3.8 Plotando DFA e PSD

In [30]: `aux.plot_psd_dfa(A, 'Ruído Browniano, últimos 1024 pontos')`

Original time series data (1024 points):

First 10 points: [-5.30000000e-05 -5.10000000e-05 -5.90000000e-05 -8.10000000e-05
-8.70000000e-05 -8.80000000e-05 -6.90000000e-05 -4.40000000e-05
-2.50000000e-05 -2.60000000e-05]

1. Plotting time series data...
2. Plotting Power Spectrum Density...
3. Plotting Detrended Fluctuation Analysis...

Ruído Browniano, últimos 1024 pontos

